



University of Pennsylvania  
ScholarlyCommons

---

Department of Physics Papers

Department of Physics

---

5-2-2008

# Non-Gaussianities in New Ekpyrotic Cosmology

Evgeny I. Buchbinder

*Perimeter Institute for Theoretical Physics*

Justin Khoury

*University of Pennsylvania, jkhoury@sas.upenn.edu*

Burt A. Ovrut

*University of Pennsylvania, ovrut@elcapitan.hep.upenn.edu*

Follow this and additional works at: [http://repository.upenn.edu/physics\\_papers](http://repository.upenn.edu/physics_papers)

 Part of the [Physics Commons](#)

---

## Recommended Citation

Buchbinder, E. I., Khoury, J., & Ovrut, B. A. (2008). Non-Gaussianities in New Ekpyrotic Cosmology. Retrieved from [http://repository.upenn.edu/physics\\_papers/113](http://repository.upenn.edu/physics_papers/113)

### Suggested Citation:

E.I. Buchbinder, J. Khoury and B.A. Ovrut. (2008). "Non-Gaussianities in New Ekpyrotic Cosmology." *Physical Review Letters*. **100**, 171302.

© 2008 The American Physical Society

<http://dx.doi.org/10.1103/PhysRevLett.100.171302>

This paper is posted at ScholarlyCommons. [http://repository.upenn.edu/physics\\_papers/113](http://repository.upenn.edu/physics_papers/113)

For more information, please contact [repository@pobox.upenn.edu](mailto:repository@pobox.upenn.edu).

---

# Non-Gaussianities in New Ekpyrotic Cosmology

## Abstract

The new ekpyrotic model is an alternative scenario of the early Universe which relies on a phase of slow contraction before the big bang. We calculate the 3-point and 4-point correlation functions of primordial density perturbations and find a generically large non-Gaussian signal, just below the current sensitivity level of cosmic microwave background experiments. This is in contrast with slow-roll inflation, which predicts negligible non-Gaussianity. The model is also distinguishable from alternative inflationary scenarios that can yield large non-Gaussianity, such as Dirac-Born-Infeld inflation and the simplest curvatonlike models, through the shape dependence of the correlation functions. Non-Gaussianity therefore provides a distinguishing and testable prediction of New Ekpyrotic Cosmology.

## Disciplines

Physical Sciences and Mathematics | Physics

## Comments

Suggested Citation:

E.I. Buchbinder, J. Khoury and B.A. Ovrut. (2008). "Non-Gaussianities in New Ekpyrotic Cosmology." *Physical Review Letters*. **100**, 171302.

© 2008 The American Physical Society

<http://dx.doi.org/10.1103/PhysRevLett.100.171302>

## Non-Gaussianities in New Ekpyrotic Cosmology

Evgeny I. Buchbinder,<sup>1</sup> Justin Khoury,<sup>1</sup> and Burt A. Ovrut<sup>2</sup>

<sup>1</sup>*Perimeter Institute for Theoretical Physics, 31 Caroline St. N., Waterloo, ON, N2L 2Y5, Canada*

<sup>2</sup>*Department of Physics, The University of Pennsylvania, Philadelphia, Pennsylvania 19104-6395, USA*  
(Received 8 November 2007; revised manuscript received 20 March 2008; published 2 May 2008)

The new ekpyrotic model is an alternative scenario of the early Universe which relies on a phase of slow contraction before the big bang. We calculate the 3-point and 4-point correlation functions of primordial density perturbations and find a generically large non-Gaussian signal, just below the current sensitivity level of cosmic microwave background experiments. This is in contrast with slow-roll inflation, which predicts negligible non-Gaussianity. The model is also distinguishable from alternative inflationary scenarios that can yield large non-Gaussianity, such as Dirac-Born-Infeld inflation and the simplest curvatonlike models, through the shape dependence of the correlation functions. Non-Gaussianity therefore provides a distinguishing and testable prediction of New Ekpyrotic Cosmology.

DOI: [10.1103/PhysRevLett.100.171302](https://doi.org/10.1103/PhysRevLett.100.171302)

PACS numbers: 98.80.Cq, 98.80.Es

The ekpyrotic scenario is a candidate theory of early-Universe cosmology. Instead of invoking a short burst of accelerated expansion from a hot initial state, as in inflation, the ekpyrotic scenario relies on a cold beginning followed by a phase of very slow contraction. Despite such diametrically opposite dynamics, both models predict a flat, homogeneous, and isotropic Universe, endowed with a nearly scale-invariant spectrum of density perturbations, and are, therefore, equally successful at accounting for all current cosmological observations.

An important drawback of the original ekpyrotic theory [1] is how to avoid the big crunch singularity without introducing ghost instabilities. Moreover, the matching of perturbations through the bounce is ambiguous [2].

Both of these issues have been resolved in the recently proposed New Ekpyrotic scenario [3]. In [3], we derived a fully *nonsingular* bounce within a controlled and ghost-free four-dimensional effective theory using the ghost condensation mechanism [4]. Moreover, the curvature perturbation on uniform-density hypersurfaces,  $\zeta$ , acquires a scale-invariant spectrum well before the bounce, thanks to an entropy perturbation generated by a second scalar field [3,5,6]. Thus, New Ekpyrotic Cosmology appears to be a consistent alternative to the inflationary scenario.

A distinguishing prediction lies in the tensor spectrum [1]: inflation predicts scale-invariant primordial gravity waves, whereas ekpyrosis does not. Detecting tensor modes from cosmic microwave background (CMB) *B*-mode polarization could rule out the ekpyrotic scenario, whereas an absence of detection would not discriminate between the two models.

In this Letter, we focus on another key observable: the non-Gaussianity of primordial density perturbations. We show that New Ekpyrotic Cosmology generically predicts large non-Gaussianity, potentially just below current sensitivity levels and detectable by near-future experiments.

We calculate the 3-point and 4-point functions. For typical parameter values, the amplitude of the 3-point

function is generically large, with  $f_{\text{NL}}$  around the current Wilkinson microwave anisotropy probe (WMAP) bound [7]:  $-36 < f_{\text{NL}} < 100$ . That is, assuming all parameters are  $\mathcal{O}(1)$ ,  $f_{\text{NL}}$  approaches the limits of this bound, depending on the sign of a parameter. These values are well above the expected sensitivity of the Planck experiment:  $|f_{\text{NL}}| \lesssim 20$ . The amplitude of the 4-point function is also generically large:  $\tau_{\text{NL}} \sim 10^4$ , which is again near the estimated WMAP bound and within the reach of Planck:  $\tau_{\text{NL}} \lesssim 600$  [8].

This is in stark contrast with the highly Gaussian spectrum predicted by slow-roll inflation. Comparably large non-Gaussianity does arise in non-slow-roll models, such as Dirac-Born-Infeld (DBI) inflation [9], and whenever the precursor of density fluctuations is a light spectator field, such as in the curvaton [10,11] or modulon scenarios [12,13]. However, as we will see, New Ekpyrosis predicts a different shape dependence in momentum space for the 3- and/or 4-point spectrum than the simplest such models.

Non-Gaussianity therefore offers a distinguishing prediction of New Ekpyrotic Cosmology, potentially testable in CMB experiments within the next few years.

*New ekpyrotic cosmology.*—As with inflation, ekpyrosis relies on a scalar field  $\phi$  rolling down a potential  $\mathcal{V}(\phi)$ . Instead of being flat and positive, however, here  $\mathcal{V}(\phi)$  must be steep, negative, and nearly exponential in form. For concreteness, we take

$$\mathcal{V}(\phi) = -V_0 e^{-\phi/\Lambda}, \quad (1)$$

where  $\Lambda \equiv \sqrt{\epsilon} M_{\text{Pl}}$  and  $\epsilon \ll 1$ . The Friedmann and scalar field equations then yield a background scaling solution,

$$a(t) \sim (-t)^{2\epsilon}; \quad \bar{\phi}(t) = \Lambda \log\left(\frac{V_0}{2\Lambda^2(1-6\epsilon)} t^2\right), \quad (2)$$

with Hubble parameter  $H = 2\epsilon/t$ . Since  $\epsilon \ll 1$ , this describes a slowly-contracting Universe with rapidly increas-

ing  $H$ , again in contrast with the rapid expansion and nearly constant  $H$  in inflation.

In single-field ekpyrosis, fluctuations in  $\phi$  acquire a scale-invariant spectrum. As we review shortly, this traces back to the fact that the above solution satisfies  $\bar{V}_{,\phi\phi} = -2/t^2$ . However, this contribution exactly projects out of  $\zeta$ , leaving the latter with an unacceptably blue spectrum. Since  $\zeta$  is conserved on super-horizon scales barring entropy perturbations, it is generally expected to match continuously through the bounce, although stringy effects could alter this picture [2].

New Ekpyrotic Cosmology introduces a second field,  $\chi$ , as the progenitor of the scale-invariant perturbation spectrum [3,5]. This field has no dynamics during the ekpyrotic phase and remains approximately fixed at  $\bar{\chi} = 0$ . However, as we describe below, its fluctuations generate a scale-invariant spectrum of entropy perturbations, which gets imprinted onto  $\zeta$  at the end of the ekpyrotic phase.

An essential condition in obtaining a scale-invariant spectrum is that at  $\bar{\chi} = 0$ , the curvature of the potential be nearly the same along the  $\chi$  and  $\phi$  directions:  $\bar{V}_{,\chi\chi} \approx \bar{V}_{,\phi\phi}$ . An example of such a potential is

$$V(\phi, \chi) = \mathcal{V}(\phi) \left( 1 + \frac{\chi^2}{2\Lambda^2} + \frac{\alpha_3}{3!} \frac{\chi^3}{\Lambda^3} + \frac{\alpha_4}{4!} \frac{\chi^4}{\Lambda^4} + \dots \right). \quad (3)$$

The higher-order  $\chi$  terms are naturally expected to be suppressed by the same scale  $\Lambda$  as the quadratic term, hence the form (3). For simplicity, we take  $\alpha_3, \alpha_4, \dots$  to be constants. While potential (3) yields a slightly blue spectral tilt, a more general potential is presented in [3] which allows for the observed red tilt without altering the conclusions for non-Gaussianity arrived at in this Letter. Note that the required field trajectory lies along an unstable point. However, a pre-ekpyrotic, stabilizing phase can easily create initial conditions so that this trajectory is arbitrarily close to the tachyonic ridge [3].

*Power spectrum for  $\chi$* —Since our space-time background is nearly static, we ignore gravity in studying  $\chi$  perturbations. To linear order, the Fourier modes  $\delta\chi_k^{(0)}$  around  $\bar{\chi} = 0$  satisfy a free field equation with time-dependent mass  $\bar{V}_{,\chi\chi} = \bar{V}_{,\phi\phi} = -2/t^2$ :

$$\ddot{\delta\chi}_k^{(0)} + \left( k^2 - \frac{2}{t^2} \right) \delta\chi_k^{(0)} = 0. \quad (4)$$

Assuming the usual adiabatic vacuum, we find

$$\delta\chi_k^{(0)} = \frac{e^{-ikt}}{\sqrt{2k}} \left( 1 - \frac{i}{kt} \right). \quad (5)$$

On super-Hubble scales,  $k(-t) \ll 1$ , the power spectrum, defined by  $\langle \delta\chi_k^{(0)} \delta\chi_{k'}^{(0)} \rangle = (2\pi)^3 \delta^3(\vec{k} + \vec{k}') P_\chi(k)$ , is

$$k^3 P_\chi(k) = \frac{1}{2t^2}, \quad (6)$$

which is scale invariant. Including gravity and departing from the pure exponential form (1) results in small deviations from scale invariance. This can yield a small red tilt, consistent with current CMB observations [3].

*Evolution of  $\zeta$* .—We focus for simplicity on the regime where all relevant modes are well outside the horizon,  $k \ll aH$ . In the small-gradient approximation, the metric can be written as  $ds^2 = -\mathcal{N}^2 dt^2 + e^{2\zeta(\bar{x},t)} a^2(t) d\bar{x}^2$  [14], where  $\mathcal{N}$  is the lapse function, and  $\zeta$  is the curvature perturbation. The evolution of  $\zeta$  on uniform-density hypersurfaces is governed by

$$\dot{\zeta} = 2H \frac{\delta V}{\bar{\phi}^2 - 2\delta V}, \quad (7)$$

where  $\delta V \equiv V(\phi, \chi) - V(\bar{\phi}, \bar{\chi})$ . A key simplification is that  $\delta\phi$  has a steep blue spectrum at long wavelengths and, hence, can be neglected. Thus, for the potential (3), we have  $\delta V \approx \mathcal{V}(\bar{\phi}) \delta\chi^2 / 2\Lambda^2 + \dots$

To proceed further, one needs an expression for  $\delta\chi$  to higher-order than the “free” part  $\delta\chi^{(0)}$ . To do this, we solve  $\ddot{\delta\chi} + \bar{V}_{,\chi\chi} \delta\chi = 0$ , valid at long wavelengths, perturbatively:  $\delta\chi = \delta\chi^{(0)} + \delta\chi^{(1)} + \dots$ . To lowest order, this equation reduces to (4) in the limit  $k \rightarrow 0$ . The next order,  $\delta\chi^{(1)}$ , satisfies  $\ddot{\delta\chi}^{(1)} + \bar{V}_{,\chi\chi} \delta\chi^{(1)} + \bar{V}_{,\chi\chi\chi} (\delta\chi^{(0)})^2 / 2 = 0$ . Using (2) and (3), and  $\delta\chi^{(0)} \sim 1/t$ , we find

$$\delta\chi = \delta\chi^{(0)} + \frac{\alpha_3}{4\Lambda} (\delta\chi^{(0)})^2 + \dots \quad (8)$$

Substituting into (7), one can integrate to obtain

$$\zeta_{\text{ek}} = \frac{1}{2} \left( \frac{\delta\chi^{(0)}}{M_{\text{Pl}}} \right)^2 + \frac{5\alpha_3}{18\sqrt{\epsilon}} \left( \frac{\delta\chi^{(0)}}{M_{\text{Pl}}} \right)^3 + \dots \quad (9)$$

The ekpyrotic phase must eventually end if the Universe is to undergo a smooth bounce and reheat into a hot big bang phase. This is achieved by adding a feature to the potential (3) which eventually pushes  $\chi$  away from the tachyonic ridge [3]. Denote the time at which ekpyrosis stops as  $t_{\text{end}}$ . For simplicity, we model this with  $V_{,\chi}$  suddenly becoming nonzero and nearly constant at  $\chi = 0$ . Denote this constant by  $V_{,\chi}|$ . The exit phase is assumed to last for a time interval  $\Delta t$  which is short compared to a Hubble time:  $|H_{\text{end}}| \Delta t \ll 1$ . This will be the case provided the potential satisfies

$$\epsilon_\chi \equiv \frac{H_{\text{end}}^4 M_{\text{Pl}}^2}{V_{,\chi}|^2} \lesssim 1. \quad (10)$$

The exit phase generates an additional contribution to  $\zeta$ . To compute this in the rapid-exit approximation, we can treat the right-hand side of (7) as approximately constant. In evaluating this constant, note that, to leading order in  $\delta\chi$ , we have  $\delta V \approx V_{,\chi}| \delta\chi = \pm H_{\text{end}}^2 M_{\text{Pl}} \delta\chi / \sqrt{\epsilon_\chi}$ . (Higher-order terms in  $\delta\chi$  yield small corrections to (9) and are therefore negligible.) Thus,  $\zeta$  changes from  $\zeta_{\text{ek}}$  by

an amount  $\zeta_c$  during the exit, given by

$$\zeta_c = \mp 2\sqrt{\epsilon}\beta \frac{\delta\chi(t_{\text{end}})}{M_{\text{Pl}}}, \quad (11)$$

where  $\beta \equiv |H_{\text{end}}|\Delta t\sqrt{\epsilon/\epsilon_\chi}$ . Noting that to lowest order  $\delta\chi \approx \delta\chi^{(0)}$  and substituting (6) evaluated at  $t_{\text{end}}$ , it follows from (11) that the  $\zeta$  power spectrum is

$$k^3 P_\zeta(k) = \frac{4\epsilon\beta^2}{M_{\text{Pl}}^2} k^3 P_\chi(k) = \beta^2 \frac{H_{\text{end}}^2}{2\epsilon M_{\text{Pl}}^2}. \quad (12)$$

Up to the prefactor  $\beta^2$ , this is identical to the inflationary result, with  $\epsilon$  playing the role of the usual slow-roll parameter. In the exit mechanism of [3],  $\beta$  denotes the overall change in angle in the field trajectory:  $\beta = \Delta\theta$ .

Let us pause to discuss the parameter values that satisfy the CMB constraint  $k^3 P_\zeta(k) \approx 10^{-10}$ . Although  $H$  passes through zero at the bounce, as argued in [3] its magnitude is essentially the same at the beginning of the hot big bang phase as it was at  $t_{\text{end}}$ , the end of the ekpyrotic phase. In other words,  $H_{\text{end}}$  sets the reheat temperature in the expanding phase. For GUT-scale reheat temperature, we have  $H_{\text{end}}/M_{\text{Pl}} \approx 10^{-6}$ . Meanwhile,  $\beta$  is a free parameter whose value depends on the exit dynamics. For the explicit exit mechanism of [3], however, the natural value is  $\beta \sim \mathcal{O}(1)$ . In this case, setting  $k^3 P_\zeta(k) = 10^{-10}$  implies  $\epsilon \approx 10^{-2}$ . We will henceforth take  $\beta = 1$  and  $\epsilon = 10^{-2}$  as fiducial parameter values.

Combining (11) with (8) and (9) yields

$$\zeta(x) = \zeta_c(x) + \frac{1}{8\epsilon\beta^2} \zeta_c^2(x) \mp \frac{5\alpha_3}{144\epsilon^2\beta^3} \zeta_c^3(x) + \dots \quad (13)$$

The exit from the ekpyrotic phase is followed by a ghost condensate phase which leads to a *nonsingular* bounce and reheating. Meanwhile,  $\chi$  gets stabilized and further evolution is governed by the single scalar  $\phi$ . It follows that  $\zeta$  is conserved through the bounce and emerges unscathed in the hot big bang phase.

*3-point function.*—The 3-point  $\zeta$  correlation function in New Ekpyrotic Cosmology is given by [3]

$$\langle \zeta_{k_1} \zeta_{k_2} \zeta_{k_3} \rangle = (2\pi)^3 \delta^3(\vec{k}_1 + \vec{k}_2 + \vec{k}_3) \cdot \frac{6}{5} f_{\text{NL}} \{P_\zeta(k_1)P_\zeta(k_2) + \text{perm.}\}. \quad (14)$$

This *local* shape [15] is consistent with  $\zeta(x)$  of the form  $\zeta(x) = \zeta_g(x) + \frac{2}{5} f_{\text{NL}} \zeta_g^2(x)$ , where  $\zeta_g$  is Gaussian. The correlation function is evaluated at  $t_{\text{end}}$  ignoring gravity.

Thus, the 3-point function is fully specified by  $f_{\text{NL}}$  [16]. This parameter receives two contributions. To begin with, the non-Gaussianity of  $\delta\chi$ , due to its cubic interaction in (3), is inherited by  $\zeta$  through (11). Following Maldacena [17], the  $\delta\chi$  3-point function is given by

$$\langle \delta\chi_1 \delta\chi_2 \delta\chi_3 \rangle = -i \int_{-\infty}^{t_{\text{end}}} ds \langle 0 | [\delta\chi_1 \delta\chi_2 \delta\chi_3, \mathcal{H}_{\text{int}}(s)] | 0 \rangle + \text{c.c.}, \quad (15)$$

where  $\delta\chi_i \equiv \delta\chi(x_i)$ , and  $\mathcal{H}_{\text{int}}$  is the cubic interaction Hamiltonian from (3):  $\mathcal{H}_{\text{int}} = \mathcal{V}(\vec{\phi})\alpha_3\chi^3/3!\Lambda^3$ . An explicit calculation yields the *intrinsic* contribution

$$f_{\text{NL}}^{\text{int}} = \mp \frac{5}{24} \frac{\alpha_3}{\beta\epsilon}. \quad (16)$$

The  $\mp$  sign corresponds to choosing  $V_{,\chi}$  to be  $\pm$ .

The second contribution comes from the nonlinear relation between  $\delta\chi$  and  $\zeta$  embodied in (11) and (13). Even if  $\delta\chi$  were Gaussian, this nonlinearity would make  $\zeta$  non-Gaussian. This *conversion* contribution to  $f_{\text{NL}}$  is

$$f_{\text{NL}}^{\text{conv}} = \frac{5}{24} \frac{1}{\beta^2\epsilon}. \quad (17)$$

Summing (16) and (17) yields a combined  $f_{\text{NL}}$ :

$$f_{\text{NL}} \equiv f_{\text{NL}}^{\text{int}} + f_{\text{NL}}^{\text{conv}} = \frac{5}{24\beta^2\epsilon} \left( 1 \mp \alpha_3\beta \right). \quad (18)$$

Since this is inversely proportional to  $\epsilon \ll 1$ , non-Gaussianity tends to be large in New Ekpyrotic Cosmology. Related ekpyrotic models [6,18] also give  $f_{\text{NL}} \sim \epsilon^{-1}$ . (A ghost condensate bounce and second scalar field are also invoked in [6], albeit without an explicit conversion mechanism, and while the two-field ekpyrotic phase of [18] is similar to ours, the bounce physics remains unspecified.) This is in sharp contrast with slow-roll inflation, where  $f_{\text{NL}}$  is *proportional* to the slow-roll parameters and therefore unobservably small. For concreteness, consider our fiducial model with GUT-scale reheating,  $\beta = 1$  and  $\epsilon = 10^{-2}$ . Taking, for example, the  $-$  sign in (16) and choosing  $2.728 > \alpha_3 > -3.8$  yields  $f_{\text{NL}}$  within the present WMAP  $2\sigma$  range:  $-36 < f_{\text{NL}} < 100$ . Thus,  $\alpha_3 \sim \mathcal{O}(1)$  yields a non-Gaussian signal near the WMAP bound. Lower reheating temperatures correspond to smaller  $\epsilon$  and, therefore, larger non-Gaussian signal. Of course,  $|f_{\text{NL}}|$  can always be made smaller by taking  $\beta$ ,  $\epsilon$  to be larger and/or by suitably choosing  $\alpha_3$ .

*4-point function.*—The connected 4-point function,

$$\langle \zeta_{k_1} \zeta_{k_2} \zeta_{k_3} \zeta_{k_4} \rangle = (2\pi)^3 \delta^3(\vec{k}_1 + \vec{k}_2 + \vec{k}_3 + \vec{k}_4) \cdot [T(k_1, k_2, k_3, k_4) + T'(k_1, k_2, k_3, k_4)], \quad (19)$$

involves two different shape functions, evaluated at  $t_{\text{end}}$ :

$$T = \frac{1}{2} \tau_{\text{NL}} \{P_\zeta(k_1)P_\zeta(k_2)P_\zeta(k_4) + 23\text{perm.}\}; \quad (20)$$

$$T' = \kappa_{\text{NL}} \{P_\zeta(k_1)P_\zeta(k_2)P_\zeta(k_3) + 3\text{perm.}\},$$

where  $\vec{k}_{ij} \equiv \vec{k}_i + \vec{k}_j$ . Thus,  $T$  and  $T'$  are specified, respectively, by the  $\tau_{\text{NL}}$  and  $\kappa_{\text{NL}}$  parameters. (Note that  $\kappa_{\text{NL}}$  is



proportional to the  $f_2$  parameter of [8]. Equations (19) and (20) are consistent with  $\zeta(x)$  of the form  $\zeta(x) = \zeta_g(x) + \frac{\sqrt{\tau_{\text{NL}}}}{2} \zeta_g^2(x) + \frac{\kappa_{\text{NL}}}{6} \zeta_g^3(x)$ , where  $\zeta_g$  is Gaussian. Note that we can obtain  $\tau_{\text{NL}}$  immediately by simply comparing its definition with that of  $f_{\text{NL}}$ :

$$\tau_{\text{NL}} = \frac{36}{25} f_{\text{NL}}^2 = \frac{1}{16\beta^4 \epsilon^2} \left(1 \mp \alpha_3 \beta\right)^2. \quad (21)$$

This was also checked by explicit computation.

Meanwhile,  $\kappa_{\text{NL}}$  receives two contributions. The first contribution arises from cubic and quartic terms in  $\chi$  in the potential (3). An explicit calculation gives

$$\kappa_{\text{NL}}^{\text{int}} = \frac{2\alpha_4 + 3\alpha_3^2}{40\beta^2 \epsilon^2}. \quad (22)$$

The second contribution is encoded in the  $\zeta_c^2$  and  $\zeta_c^3$  terms in (13). Comparing with (19), we obtain

$$\kappa_{\text{NL}}^{\text{conv}} = \mp \frac{5\alpha_3}{24\beta^3 \epsilon^2}. \quad (23)$$

Combining the above results, we find

$$\kappa_{\text{NL}} \equiv \kappa_{\text{NL}}^{\text{int}} + \kappa_{\text{NL}}^{\text{conv}} = \frac{\alpha_3(9\alpha_3\beta \mp 25) + 6\alpha_4\beta}{120\beta^3 \epsilon^2}. \quad (24)$$

Both  $\tau_{\text{NL}}$  and  $\kappa_{\text{NL}}$  are proportional to  $\epsilon^{-2}$  and therefore also tend to be relatively large. Note that  $\tau_{\text{NL}}$  is always positive, whereas  $\kappa_{\text{NL}}$  can have either sign. For instance, our fiducial parameter values for GUT-scale reheating with  $\alpha_3, \alpha_4 \sim \mathcal{O}(1)$  yield  $\tau_{\text{NL}} \sim 10^4$ , which is around the estimated WMAP bound [8]. Lower non-Gaussianity can again be achieved by taking larger  $\beta$ ,  $\epsilon$  and/or by a suitable choice of  $\alpha_3$  and  $\alpha_4$ .

*Discussion.*—The simplest inflationary models, consisting of one or more slowly-rolling scalar fields, all predict negligible 3-point and higher-order correlation functions. Non-Gaussianity therefore offers a robust test to distinguish New Ekpyrotic Cosmology from slow-roll inflation.

Significant inflationary non-Gaussianity can be obtained in non-slow-roll models, such as DBI, albeit with a distinguishable 3-point shape dependence [15].

Large non-Gaussianity may also be achieved in the curvaton scenario. While the 3-point function is also local, there is an essential difference at the 4-point level. In the simplest curvaton model, the progenitor of density perturbations is a free field. Thus,  $\kappa_{\text{NL}} \sim f_{\text{NL}}$  [11]. In New Ekpyrosis, however, both  $\tau_{\text{NL}}$  and  $\kappa_{\text{NL}}$  are  $\sim f_{\text{NL}}^2$ , leading to a distinguishable 4-point shape dependence. More intricate curvaton models can also yield large  $\kappa_{\text{NL}}$ . Similarly, for general modulon scenarios [13].

Near-future non-Gaussianity observations will, therefore, test the new ekpyrotic paradigm and can potentially distinguish it from its inflationary alternatives.

We thank E. Komatsu, P.J. Steinhardt, A. Tolley, and especially F. Vernizzi for helpful discussions. This work is supported in part by NSERC and MRI (E. B. and J. K.), and by the DOE under Contract No. DE-AC02-76-ER-03071 and the NSF Focused Research Grant No. DMS0139799 (B. A. O.).

- 
- [1] J. Khoury, B. A. Ovrut, P.J. Steinhardt, and N. Turok, Phys. Rev. D **64**, 123522 (2001); Phys. Rev. D **66**, 046005 (2002); J. Khoury, B. A. Ovrut, N. Seiberg, P.J. Steinhardt, and N. Turok, Phys. Rev. D **65**, 086007 (2002).
  - [2] A. J. Tolley, N. Turok, and P. J. Steinhardt, Phys. Rev. D **69**, 106005 (2004); P. L. McFadden, N. Turok, and P. J. Steinhardt, Phys. Rev. D **76**, 104038 (2007); T. J. Battefeld, S. P. Patil, and R. H. Brandenberger, Phys. Rev. D **73**, 086002 (2006).
  - [3] E. I. Buchbinder, J. Khoury, and B. A. Ovrut, Phys. Rev. D **76**, 123503 (2007); J. High Energy Phys. 11 (2007) 076.
  - [4] N. Arkani-Hamed, H. C. Cheng, M. A. Luty, and S. Mukohyama, J. High Energy Phys. 05 (2004) 074; P. Creminelli *et al.*, J. High Energy Phys. 12 (2006) 080.
  - [5] F. Finelli, Phys. Lett. B **545**, 1 (2002); J. L. Lehners *et al.*, Phys. Rev. D **76**, 103501 (2007).
  - [6] P. Creminelli and L. Senatore, J. Cosmol. Astropart. Phys. 11 (2007) 010.
  - [7] D. N. Spergel *et al.*, Astrophys. J. Suppl. Ser. **170**, 377 (2007); P. Creminelli *et al.*, J. Cosmol. Astropart. Phys. 03 (2007) 005.
  - [8] N. Kogo and E. Komatsu, Phys. Rev. D **73**, 083007 (2006).
  - [9] M. Alishahiha, E. Silverstein, and D. Tong, Phys. Rev. D **70**, 123505 (2004).
  - [10] D. H. Lyth and D. Wands, Phys. Lett. B **524**, 5 (2002); K. Enqvist and M. S. Sloth, Nucl. Phys. B **626**, 395 (2002); T. Moroi and T. Takahashi, Phys. Lett. B **522**, 215 (2001); **539**, 303(E) (2002).
  - [11] D. H. Lyth, J. Cosmol. Astropart. Phys. 06 (2006) 015; M. Sasaki, J. Valiviita, and D. Wands, Phys. Rev. D **74**, 103003 (2006).
  - [12] G. Dvali, A. Gruzinov, and M. Zaldarriaga, Phys. Rev. D **69**, 023505 (2004); L. Kofman, arXiv:astro-ph/0303614.
  - [13] M. Zaldarriaga, Phys. Rev. D **69**, 043508 (2004); F. Vernizzi, Phys. Rev. D **69**, 083526 (2004).
  - [14] D. S. Salopek and J. R. Bond, Phys. Rev. D **42**, 3936 (1990); D. H. Lyth, K. A. Malik, and M. Sasaki, J. Cosmol. Astropart. Phys. 05 (2005) 004.
  - [15] D. Babich, P. Creminelli, and M. Zaldarriaga, J. Cosmol. Astropart. Phys. 08 (2004) 009.
  - [16] E. Komatsu and D. N. Spergel, Phys. Rev. D **63**, 063002 (2001).
  - [17] J. M. Maldacena, J. High Energy Phys. 05 (2003) 013.
  - [18] K. Koyama and D. Wands, J. Cosmol. Astropart. Phys. 04 (2007) 008; K. Koyama *et al.*, J. Cosmol. Astropart. Phys. 11 (2007) 024.