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Calibration of frictional forces in atomic force microscopy

D. F. Ogletree University of California

Robert W. Carpick *University of Pennsylvania*, carpick@seas.upenn.edu

Miguel Salmeron University of California

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NOTE: At the time of publication, author Robert W. Carpick was affiliated with the University of Wisconsin. Currently (June 2007), he is a faculty member in the Department of Mechanical Engineering and Applied Mechanics at the University of Pennsylvania.

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Abstract

The atomic force microscope can provide information on the atomic-level frictional properties of surfaces, but reproducible quantitative measurements are difficult to obtain. Parameters that are either unknown or difficult to precisely measure include the normal and lateral cantilever force constants (particularly with microfabricated cantilevers), the tip height, the deflection sensor response, and the tip structure and composition at the tip-surface contact. We present an *in situ* experimental procedure to determine the response of a cantilever to lateral forces in terms of its normal force response. This procedure is quite general. It will work with any type of deflection sensor and does not require the knowledge or direct measurement of the lever dimensions or the tip height. In addition, the shape of the tip apex can be determined. We also discuss a number of specific issues related to force and friction measurements using optical lever deflection sensing. We present experimental results on the lateral force response of commercially available V-shaped cantilevers. Our results are consistent with estimates of lever mechanical properties using continuum elasticity theory.

Keywords

microscopes, calibration, sliding friction, static loads, probes, measuring methods, interfaces

Comments

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Calibration of frictional forces in atomic force microscopy

D. F. Ogletree, R. W. Carpick, a) and M. Salmeron Materials Sciences Division, Lawrence Berkeley National Laboratory, Berkeley, California 94720

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The atomic force microscope can provide information on the atomic-level frictional properties of surfaces, but reproducible quantitative measurements are difficult to obtain. Parameters that are either unknown or difficult to precisely measure include the normal and lateral cantilever force constants (particularly with microfabricated cantilevers), the tip height, the deflection sensor response, and the tip structure and composition at the tip-surface contact. We present an in situ experimental procedure to determine the response of a cantilever to lateral forces in terms of its normal force response. This procedure is quite general. It will work with any type of deflection sensor and does not require the knowledge or direct measurement of the lever dimensions or the tip height. In addition, the shape of the tip apex can be determined. We also discuss a number of specific issues related to force and friction measurements using optical lever deflection sensing. We present experimental results on the lateral force response of commercially available V-shaped cantilevers. Our results are consistent with estimates of lever mechanical properties using continuum elasticity theory. © 1996 American Institute of Physics. [\$0034-6748(96)04709-0]

I. INTRODUCTION

Since the invention of the atomic force microscope (AFM)¹ a great deal of attention has been focused on using AFM techniques to measure nanometer-scale frictional properties, starting from the first observations of friction and atomic-scale stick-slip behavior with an AFM by Mate et al.² Significant efforts have been made using friction force microscopy (FFM) to understand the fundamental mechanisms of friction and adhesion.³ These efforts have been hindered by the lack of quantitative data on frictional properties, as the accurate calibration of both normal and frictional forces in most types of FFM apparatus is not an elementary task.

The most common experimental apparatus for FFM combines commercially available microfabricated silicon or silicon nitride cantilever-tip assemblies⁴ with an AFM using optical beam deflection sensing.⁵ All commercially available scanning probe microscopes capable of FFM and many custom designed instruments use this combination.⁶

Microfabricated cantilevers offer many advantages they are available in a range of force constants, their small size leads to high resonant frequencies, they are relatively easy to use, and the tips are relatively sharp and durable. On the other hand, their small size makes it difficult to make direct measurements of mechanical properties. Several methods have been proposed for experimentally calibrating lever normal force constants—observing shifts in lever resonant frequencies for loaded levers, observing thermal vibrations of free levers,8 or deflecting the AFM lever with a larger lever of known spring constant, but these methods cannot be used for lateral force calibration. 10

Calculation of cantilever force constants are also difficult as they depend on knowledge of critical dimensions such as lever thickness and tip height that are difficult to control in fabrication and difficult to measure accurately even with a good scanning electron microscope (SEM). Calculations for the commonly used V-shaped levers require numerical methods. 11 The mechanical properties of silicon nitride cantilevers produced by chemical vapor deposition (CVD) can vary widely. 12 Levers are often metalized to increase optical reflectivity, but the thickness and mechanical properties of the coating (grain size, etc.) may not be known and the effect of metalization on the cantilever force constants must be considered.¹³

The optical beam deflection sensor also has experimental advantages for FFM along with difficulties for quantitative friction measurements. One sensor can measure deflections due to both normal and lateral forces. The sensitivity and signal/noise ratio of this method are good and changing cantilevers is relatively easy. However, both the absolute values and the ratio of normal and lateral force sensitivity depends on the precise alignment of the laser beam with respect to the cantilever. Furthermore, the angular deflection of commercial cantilevers due to lateral forces is one to two orders of magnitude smaller than for normal forces, so small misalignments can cause significant errors in lateral force measurement due to cross-talk between normal and lateral deflec-

In this article we describe an in situ method of experimentally measuring the combined response of the lateral force transducer (the cantilever/tip combination) and the deflection sensor. Our method is based on comparing lateral force signals on surfaces with different slopes. The known geometrical contribution to the total lateral force gives a direct calibration of lateral force response in terms of the normal force response. If the normal force constant is known, then completely quantitative friction measurements can be made. Even if the normal force constant is uncertain, the ratio of normal to lateral forces (the friction coefficient) can be determined quantitatively.

We will now discuss some experimental aspects of the optical deflection FFM, present methods for estimating the normal and lateral response of microfabricated cantilevers, describe the "wedge" method of force calibration, and

a) Also at: Department of Physics, University of California, Berkeley.

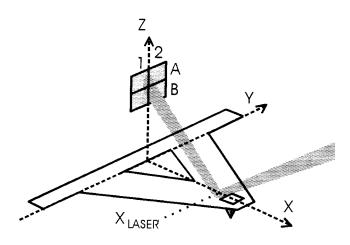


FIG. 1. Schematic cantilever and deflection sensor for the optical beam deflection FFM. The incident laser beam in the X-Z plane is deflected proportional to the slope (not the displacement) of the lever X-Z plane, and to the twist of the lever normal out of this plane, at the point where the laser beam hits the lever.

present experimental results for commercial V-shape cantilevers.

II. OPTICAL BEAM FFM

In the optical beam deflection method, a laser beam is reflected off the back of the AFM cantilever into a quadrant photodiode position sensitive detector. We define a coordinate system with X along the lever long axis, Z along the tip axis, and the origin at the base of the lever. The incident laser beam is in the X-Z plane, and the reflected beam is incident on a four-quadrant photodiode which is (ideally) oriented with one axis along the Y direction in the X-Z plane (Fig. 1). For small deflections the difference in photocurrent between the upper and lower pairs of diodes (A-B) will be proportional to the slope of the lever in the X-Z plane at the point of reflection $X_{\rm LASER}$. Similarly, the difference in photocurrent between the left and right pairs of diodes (1-2) is proportional to the lever twist out of the X-Z plane at $X_{\rm LASER}$.

The photodiode output signal S as a function of angular deflection φ can be calculated for a Gaussian beam if the total size of the photodiode is large compared to the laser spot and the "dead" area between the quadrants is neglected. In this case

$$S(\varphi) = \frac{A - B}{A + B} = 1 - \frac{1}{\Delta \omega} \sqrt{\frac{8}{\pi}} \int_{\varphi}^{\infty} e^{-2u^2/\Delta \omega^2} du,$$

where $\Delta \omega$ is the Gaussian half-width (angular divergence) of the beam, A is the photocurrent on the upper two quadrants, and B is the photocurrent on the lower two quadrants. This expression cannot be integrated analytically, but it may be expanded around $\varphi=0$ (see the Appendix), with $x=\varphi/\Delta\omega$:

$$S(x) = \sqrt{\frac{8}{\pi}} x \left[1 - \frac{2}{3} x^2 + \frac{2}{5} x^4 - \frac{4}{21} x^6 + \dots \right].$$

The term in square brackets describes the nonlinearity of the detector response. For S=0.2, the deviation from linearity is -1% and for S=0.5 it is -6.1%. Under our typical experi-

mental conditions, a normal force of ~ 1 nN produces a deflection $S \sim 0.002$. The photodiode detector signal is quite linear in response to FFM lever deflection over a relatively wide range, which we have verified experimentally using a laser interferometer.

If the reflected laser beam is round, the angular sensitivity is equal for deflections due to normal and lateral forces. This is often not the case under experimental conditions. Most optical beam FFMs use diode lasers, which produce asymmetric beams. In addition, if the laser spot is not carefully focused and aligned on the cantilever, there may be significant diffraction effects where the reflected spot is cut off by the cantilever edge. Let

$$R_{\text{DETECTOR}} = \frac{dS_{\text{NORMAL}}}{d\vartheta} / \frac{dS_{\text{LATERAL}}}{d\phi}$$

describe the angular sensitivity ratio for normal and lateral angular deflections. If the beam is focused on the cantilever through a single-mode optical fiber, it is possible to have a radially symmetric and well focused Gaussian beam incident on the cantilever. In this case $R_{\rm DETECTOR}$ can be very near 1.

Forces acting on the apex of the tip in the Z direction cause the lever to bend with a displacement and tip spring constant of the form

$$z(F_Z,x) = F_Z f(x), \quad k_Z = 1/f(X_{TIP}),$$

with the tip located at $X_{\rm TIP}$. Microfabricated levers are generally planar, and quite stiff with respect to bending in the X-Y plane, and in any case such deformations cannot be detected by the optical beam method. The main effect of forces acting on the tip apex in the Y directions is to twist the lever, with an angular displacement and resulting tip spring constant of the form

$$\Theta(F_Y,x) = F_Y g(x), \quad k_Y = 1/H_{\text{TIP}} g(X_{\text{TIP}}),$$

where H_{TIP} is the cantilever tip height. Forces acting on the tip apex in the X direction are more complicated for the optical beam FFM. The in-plane compression of the lever is insignificant, so the main effect is to cause a bending or buckling of the lever in the X-Z plane,

$$z(F_x) = F_x h(x)$$
.

The tip displacement and associated spring constant for the tip apex in the X direction due to cantilever buckling are

$$\Delta x = F_X H_{\text{TIP}} \frac{\partial h(X_{\text{TIP}})}{\partial x}, \quad k_X = 1/H_{\text{TIP}} \frac{\partial h(X_{\text{TIP}})}{\partial x}.$$

Bending of the tip itself due to forces in the *X* or *Y* direction will not be detected by the optical beam method. Compression of the tip along its axis (*Z* direction) is insignificant.

We can define lever deflection sensitivity ratio

$$R_{\text{LEVER}}(x) = \frac{\partial f(x)}{\partial x} / g(x),$$

as the ratio of angular deflections produced by normal and lateral forces.

For the "V-shape" cantilevers commonly used in FFM the functions f(x), g(x), and h(x) that describe the lever response must be calculated numerically. Some insight into

the general properties of the optical beam method can be gained by considering the form of these functions for a simple beam cantilever of width W and thickness T which is small compared to its length L, with a top of height H at the extreme end $(X_{\rm TIP}=L)$. Using familiar engineering formulas¹⁴

$$f(x) = \frac{6Lx^2 - 2x^3}{EWT^3}, \quad g(x) = \frac{3Hx}{GWT^3}, \quad h(x) = \frac{6Hx^2}{EWT^3},$$

where E and G are the elastic and shear moduli of the cantilever. Notice that these functions do not have the same x dependence. The ratio as well as the absolute values of the angular sensitivities to normal and lateral forces depend on the laser spot position $X_{\rm LASER}$. For the simple beam

$$R_{\text{LEVER}}(x) = \frac{2L - x}{H(1 + \nu)}, \text{ where } G = \frac{E}{2(1 + \nu)}$$

defines the Poisson ratio ν .

Typical microfabricated cantilevers have top heights \sim 3–4 μ m and lengths \sim 80–300 μ m, so the lateral force signals are \sim 20–80 times smaller than the normal force signals. Uncertainty in tip height will cause an error $\Delta R/R$ of $\sim \Delta H/H$, and uncertainty in laser spot position will cause an error of $\sim \Delta X_{\rm LASER}/L$ if the laser spot is near the end of the lever.

III. SPRING CONSTANT ESTIMATES

An estimate of the response of a "V" lever can be made by treating this as a variable width beam. The curvature of a small solid element is proportional to the moment of torque acting on it and inversely proportional to the product of the elastic modulus and the moment of inertia around the bending axis. ¹⁵ Using this approach for the lever, the curvature at a distance *x* from the base of the lever is

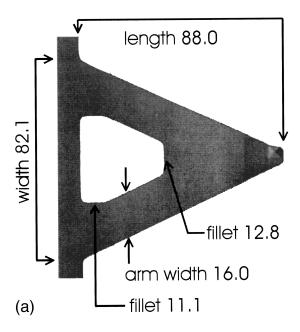
$$\frac{\partial^2 z(x)}{\partial x^2} = \frac{F_Z(L_{\text{TIP}} - x)}{EI(x)},$$

where the moment of inertia $I(x) = \frac{1}{12}W(x)T^3$ depends on the projected width of the lever along the y axis. Likewise the curvature due to lateral forces is

$$\frac{\partial \Theta(x)}{\partial x} = \frac{F_Y H_{\text{TIP}}}{GI(x)}.$$

These expressions can be integrated analytically for each section and combined, matching boundary conditions for continuity, to give g(x) and $\partial f(x)/\partial x$ along the lever.

This approach is similar to the "parallel beam approximation" (PBA) recently analyzed in detail by Sader. Warmack *et al.* 17 have also used this type of approach to analyze normal deflections and the effects of cantilever buckling on AFM response. Unlike Sader and references therein, we also calculate torsional and buckling force constants, and explicitly include the effect of the triangular "fillets" (a 10% effect for short levers) in the corners of the central area cutout of the V lever [Fig. 2(b)]. Our approach gives the same result as Sader's first solution for the solid triangle region at the end of the lever. His analysis shows that using the actual arm width, instead of the arm width projected in the y direction,



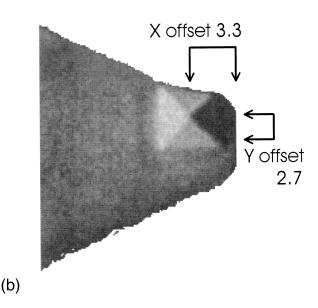
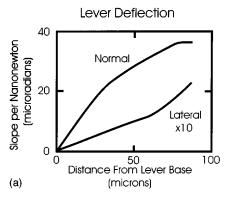


FIG. 2. (a) A scanning electron micrograph of a gold coated Park Scientific Instruments "F" cantilever. The indicated dimensions are in micrometers. (b) A higher magnification view of the end of the lever, showing the position of the tip (at the apex of the pyramid) relative to the lever. The tip is off-axis by an amount close to its nominal height of 3 μ m, which is an additional source of coupling between normal and lateral forces.

is a better approximation for the normal force constant. Sader's analysis also shows that values for the normal force constant estimated by good PBA-type approximations are within 10%–20% of the results of a detailed finite element calculation. The errors resulting from the approximations used in the force estimates are probably less than the errors due to uncertainty in the physical properties of the lever (thickness, modulus, tip height, metalization thickness, etc.).

The results of this calculation for a Park Scientific Instruments F lever (dimensions indicated on the SEM photo of Fig. 2) are shown in Fig. 3(a), assuming an elastic modulus of 155 GPa and a Poisson ratio of 0.27 for CVD silicon



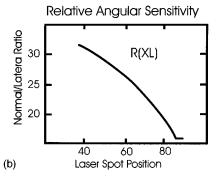


FIG. 3. (a) Calculated curves showing the variation in slope (in microradians) along the length of the triangular region at the end of the cantilever shown in Fig. 2 for a 1 nN normal or lateral force (lateral slope $\times 10$). (b) The ratio of angular deflections for this lever in response to normal and lateral forces, as a function of the laser spot position. A 10 micron uncertainty in laser spot position will give a 20% variation in measured friction coefficient.

nitride.¹⁸ If the laser beam is positioned in the center of the triangular region at the end of the lever, the estimated angular deflections produced by normal, lateral, and buckling forces are 32.2, 1.26, and 1.99 μ rad/nN, respectively. For this relatively short and stiff lever, the triangular fillets increase the normal stiffness by ~10%. Integrating the expressions for angular deflection a second time, we obtain estimates for the force constants of 0.508, 132, and 209 N/m. The nominal normal force constant for the F lever is 0.5 N/m.

The sensitivity ratio $R_{\rm LEVER}(x)$ is plotted in Fig. 3(b). This graph shows that $R_{\rm LEVER}$ is about 20% more sensitive to laser spot position for the V lever than for the simple beam of the same length and tip height. This is because the triangle at the end of the V lever twists more than any other part, while most of the bending takes place near the base of the cantilever, where the normal force lever moment is the greatest.

IV. LATERAL FORCE WEDGE CALIBRATION

Quantitative FFM measurements will be far more reliable if an *in situ* method of *experimental* lateral force calibration can be developed, as indicated in the above discussion. We have solved this problem with the wedge calibration technique.

Our approach is to measure the normal and lateral force signals on a sloped surface. There is then a geometrical contribution to the lateral force, i.e., the product of the applied load and the tangent of the slope. An experimental force calibration is made by sliding the tip across a surface of known slope and measuring the lateral force signal as a function of applied load.

In principle, this could be carried out on any surface that is tilted with respect to the lateral scanning direction. In practice, this is difficult to realize because (a) if the surface is tilted by the experimenter, there will be some uncertainty in the tilt angle, (b) we will show that to accurately calibrate the lateral force response, *two* surfaces of different tilt angles must be used and (c) it may not be possible to contact the tip to a tilted surface without the surface touching the side of the cantilever chip or its holder, since microfabricated cantilever tips are usually very short.

These problems are resolved by using the faceted SrTiO₃ (305) surface proposed by Sheiko *et al.*¹⁹ as a measure of tip sharpness. When annealed in oxygen, SrTiO₃ (305) facets into (101) and (103) planes which form extended ridges along the [010] direction. The (101) and (103) planes are respectively tilted +14.0° and -12.5° with respect to the original (305) surface.²⁰ The ridges are typically 5–20 nm high and are spaced 10–100 nm apart (Fig. 4). We thus have a test sample that provides two sloped surfaces with exactly known relative angles. Furthermore, as demonstrated by Sheiko *et al.*, the top of the SrTiO₃ ridges are extremely sharp, and a topographic AFM scan over the ridge produces an image of the tip. This is also quite important, as accurate knowledge of the tip shape is also required for quantitative FFM experiments.²¹

The wedge method has some additional advantages. It can be used to determine the absolute orientation of the sample while confirming the microscope Z calibration. Even though the angle between the two SrTiO₃ (305) facets is known, the average surface normal may be tilted by a small angle relative to the microscope Z axis. Calibrating the AFM XY displacement is usually not too difficult. Crystal lattices can be used for nanometer scale standards, and lithographically patterned standards work on the micron scale. We calibrate Z displacement in terms of XY displacement by making a topographic image of the SrTiO₃ sample, and adjusting Z until the angle between the facets is 153.5°. Now that XY and Z are calibrated, the overall slope of the surface can be directly determined from the image (in practice we solve for the slope and Z calibration simultaneously, see the Appendix for details).

To get an accurate force calibration with the wedge method, the tip must slide across one facet for a reasonable distance before reaching the next facet or ridge crest. This is not possible unless $2R_{\rm tip} \sin \theta$ is significantly smaller than the spacing between ridge crests. It is difficult to calibrate tips with radii greater than ~ 100 nm even using the widest facets on our SrTiO₃ sample. The procedure is straightforward for tip radii ~ 50 nm or less. It may be possible to prepare a similar sample with larger facets for calibrating blunt tips.

V. WEDGE CALCULATIONS

The vector diagrams in Fig. 5 show the forces acting on the end of the tip while scanning up or down a sloped sur-

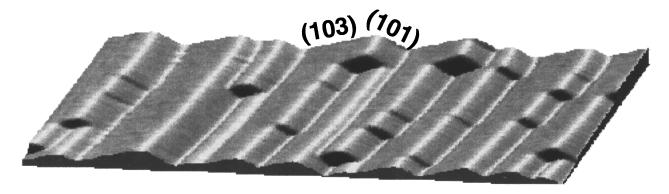


FIG. 4. A 410 nm \times 410 nm topographic AFM image (light shaded) of the SrTiO₃ surface showing (103) and (101) facets. The apparent rounding of the ridge crests is due to the \sim 40 nm radius of the AFM tip used for this image. The widest facets are used to measure lateral signals as a function of load for the cantilever lateral force calibration.

face. The two forces applied by the tip on the surface, the vertical load L (down is positive) and the horizontal tractive force T (right is positive) must be balanced by a reaction force from the surface acting on the tip. This can be divided into two components, a friction component f parallel to the surface and a second component N normal to the surface. When the tip slides across the surface, these forces are in equilibrium. At a given load, the tractive force, friction and normal forces depend on the direction of motion, so

$$N_{\pm} = L \cos \theta \pm T_{\pm} \sin \theta$$
,

$$f(N_+) = T_+ \cos \theta \mp L \sin \theta$$
.

In these equations + denotes up hill and motion and - downhill motion. N, L, and T are signed quantities, while f is the positive magnitude of the frictional force acting against the direction of motion.

We experimentally measure the voltage output from the lateral force transducer T_o where $\alpha T_o = T$ (the "o" subscript will be used to indicate a force measured in transducer output volts rather than Newtons). If we can find α (Newtons per volt) we have a direct calibration of the lateral force response of the FFM. The calibration constant α is a product of all the factors of the experiment—the lever lateral force constant, the deflection of the reflected laser beam as a function of lateral tip displacement, and the photodiode angular

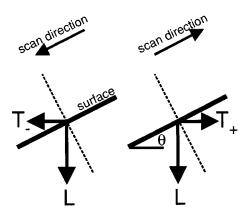


FIG. 5. Forces exerted on the surface by the AFM tip while scanning up or down a sloped surface.

sensitivity. This method will work equally well for other types of lateral force transducers, including optical interferometry and piezoresistive detection.

To solve the calibration problem we need a functional form for the frictional force $f(L) = \alpha f_o(L)$. This can be an empirical fit from measuring f_o on a flat surface, or a theoretical form from the Hertz or Johnson–Kendall–Roberts (JKR) theories (see Ref. 21). Tip-surface adhesion usually has a significant effect of f(L) in FFM experiments. In the JKR theory, the load dependent adhesion is part of the model. When friction is linearly dependent on the load, adhesion is often treated as a force offset. We find experimentally that the friction-load relation for silicon or silicon nitride tips on the SrTiO₃(305) sample in air is well represented by a linear form $f(L) = \mu(L+A)$, where A is the adhesion or pull-off force. In this case

$$N_{+} = \frac{L + \mu A \sin \theta}{\cos \theta - \mu \sin \theta}$$
 and $N_{-} = \frac{L - \mu A \sin \theta}{\cos \theta + \mu \sin \theta}$.

Note that the normal force depends on the friction and on the direction of motion.

On a flat surface, the "frictional force" is determined by taking half the difference between the left-to-right and right-to-left lateral deflection forces, i.e., the half-width of the friction loop W(L). In this case, since the surface is tilted, the effective load is direction-dependent, and the expression for W(L) is more complicated. Furthermore, the offset of the friction loop $\Delta(L)$ is not zero and depends on load. This is illustrated in Fig. 6, where bi-directional lateral force loops are drawn for flat, positively tilted, and negatively tilted surfaces respectively and the measured quantities W_o and Δ_o are indicated.

Experimentally, we measure lateral forces for a range of applied loads, and use the slopes $\Delta' \equiv d\Delta/dL$ and $W' \equiv dW/dL$ in calculations, which are independent of L due the assumption of linearity. This eliminates the pull-off force from the equations, as well as any dc offset in the lateral force sensor. These slopes are given by

$$\alpha \Delta_o' = \Delta' = \frac{(1 + \mu^2)\sin \theta \cos \theta}{\cos^2 \theta - \mu^2 \sin^2 \theta}$$

and

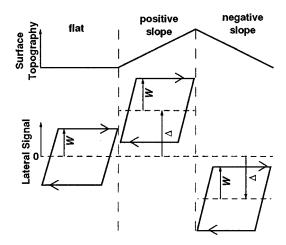


FIG. 6. Schematic friction loops (lateral signals for back and forth scans) for flat, positively sloped and negatively sloped surfaces at the same applied load. The friction loop half-width W is slightly different for the three cases, while the loop offset Δ is substantially different and is indicative of the overall tilt of each surface. The values of W and Δ are measured over a range of applied loads for known slopes and used to calibrate the lateral force response of the cantilever.

$$\alpha W_o' = W' = \frac{\mu}{\cos^2 \theta - \mu^2 \sin^2 \theta}.$$

In the limiting cases of no friction, $\Delta' \rightarrow \tan \theta$ and $W' \rightarrow 0$, and for no slope $\Delta' \rightarrow 0$ and $W' \rightarrow \mu$ as expected. Using these two equations, we can calculate the tip-surface friction coefficient and lateral force calibration constant. The ratio of these expressions gives μ :

$$\mu + \frac{1}{\mu} = \frac{2\Delta_o'}{W_o' \sin 2\theta}.$$

From the form of this expression, there is an ambiguity in the problem, since μ and $1/\mu$ are equally good mathematical solutions which give different results for α . This ambiguity may be resolved by choosing the appropriate root using an estimate for α from the type of calculation described in Sec. III, or if μ is known to be less than one. Once μ is determined, α can be found from the equations defining W' or Δ' . Experimentally, it is best to solve for α using data from two different slopes, as discussed below.

VI. EXPERIMENTAL DIFFICULTIES

In the ideal case the lateral force response of the cantilever and deflection sensor has been calculated. However, there can be significant cross talk between normal and lateral cantilever deflections. As discussed above, the response of the optical beam FFM deflection sensor is 20–80 times greater for normal forces than for lateral forces. In addition, the normal forces are often larger than the lateral forces. A small misalignment of the laser or cantilever with respect to the quadrant photodiode, for example a rotation of the photodiode by \sim 2°, can mean that the normal force contribution to the lateral deflection output is as large as the lateral force contribution. In normal FFM experiments this problem is avoided by measuring friction loop width, or W(L), since the cross talk primarily effects the friction loop offset $\Delta(L)$.

Cross talk is a concern in the wedge calibration experiment since the lateral force offset $\Delta(L)$ is important in the calibration calculation.

In our experiment, we compensate for the cross talk electronically, by adding or subtracting a fraction of the normal force output from the lateral force output. The compensation is adjusted by taking a force–distance curve, or by oscillating the cantilever out of contact with the surface, where there should be no real lateral forces, and adjusting the compensation to null the lateral force output. Such compensation is also available on some commercial FFM electronics. Even with careful compensation, the residual cross talk may be too large to neglect in the calibration calculations.

The effect of cross talk can be minimized by measuring Δ'_o and W'_o on the 103 and 101 facets of the SrTiO₃ surface and then using $\Delta'_{o103} - \Delta'_{o101}$, W'_{o101} , and W'_{o103} for the calibration calculation. These quantities all involve differences between lateral signals for the same applied load, so cross talk has a negligible effect. The details of the two-slope calibration are given in the Appendix.

The above discussion has assumed that the applied load L is known. Since the direct experimental calibration of normal spring constants is also difficult, in some cases only an experimental signal L_o proportional to the normal load, $L=\beta L_o$, is known. In this case it is not possible to get the absolute lateral force calibration but only $R_{\rm DETECTOR}$ $R_{\rm LEVER}(X_{\rm LASER})=\alpha/\beta$. It is still possible to get the friction coefficient μ if friction is proportional to load, since on a flat surface $\mu=R_{\rm DETECTOR}R_{\rm LEVER}(X_{\rm LASER})$ T_o/L_o . It is important to have an accurate measure of applied load. It is not sufficient to assume that the voltage applied to the Z piezo is proportional to load. There are significant nonlinearities in piezo response, which depend on the speed and direction of displacement. 23

VII. EXPERIMENTAL LEVER CALIBRATION

We have used the wedge calibration procedure described with our AFM to measure α/β for cantilevers of three different nominal spring constants. In this system the laser beam is carried by a single-mode fiber and well-focused on the cantilever, so $R_{\rm DETECTOR}{\approx}1.^{24}$ The cantilevers are V-shaped silicon nitride sharpened microlevers from Park Scientific Instruments. The levers are gold coated, and the pyramidal tips are etched back to get a sharp tip with a nominal radius of ${\approx}30$ nm. We made measurements on the "D," "E," and "E" levers which have nominal normal force constants 0.03, 0.10, and 0.50 N/m. Two different E levers from the same wafer were analyzed.

The SrTiO₃ sample was aligned so that the ridges were perpendicular to the lateral scanning direction. The lateral and normal bending signals were recorded as the tip scanned back and forth over both facets of a single ridge. The feedback was active so that each line scan across the sloped surface was recorded at the same externally applied load. After each line was recorded, the feedback set point (applied load) was increased under computer control, and another line scan acquired. 256 line scans of 256 points were recorded in

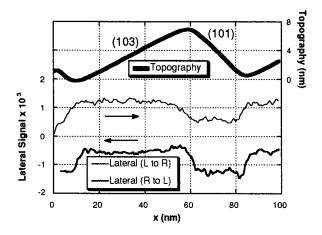


FIG. 7. Experimental lateral deflection signals $T_0(1-2/A+B)$ measured on the (101) and (103) facets of the SrTiO₃(305) sample for each direction at a given load. The simultaneously acquired topography (thick line) is also shown. W(L) and $\Delta(L)$ are calculated from this data. The complete series of measurements over a range of loads is shown in Fig. 8.

each data set. The average value of the subset of points for each facet was calculated for each load. Figure 7 shows an example of unprocessed data from a single line scan (friction loop), showing the simultaneous topography and lateral deflection signals for both scanning directions.

A plot of lateral force versus load, obtained in this case with an E lever, is shown in Fig. 8. Figure 8(a) shows the lateral bending signals (left-to-right and right-to-left) plotted versus the normal bending signal for both facets. Figure 8(b) shows the resulting friction loop width and offset plotted versus the normal bending signal (load) for both facets, with linear fits to the data. As predicted in Sec. VI, the slopes W'_{o101} and W'_{o103} are similar, while Δ'_{o101} and Δ'_{o103} reflect the change in sign of the tilt angle.

The two-slope wedge equations in the Appendix were used to calculate α/β . We did not have a good experimental value for the lever normal force constant, so we report α/β instead of the absolute lateral force response α . The results are summarized in Table I. The α/β values are averages of several data sets, each acquired on a different ridge. For comparison, the table includes the spring constants estimated by the method of Sec. III, and the value for $R_{\rm LEVER}$ assuming that $X_{\rm LASER}$ was located in the center of the solid triangular region at the end of the lever (Fig. 2). Some data sets were recorded on different days. The error quoted is the statistical variation. Measurements with the same tip on different parts of the wedge sample were reproducible within $\sim 10\%$.

The experimental α/β values are generally consistent with the $R_{\rm LEVER}$ values estimated from material properties. The experimental friction coefficients tend to be slightly higher for the 103 facet of strontium titanate relative to the 101 facets. We noted more substantial variations in friction coefficients from day to day. As mentioned, these experiments were carried out in air with no humidity control. Friction coefficients on other materials measured with AFM have been observed to vary with relative humidity. This may partially account for the variation of friction coefficients observed. Friction coefficients may also vary from lever to lever due to changes in tip radius.

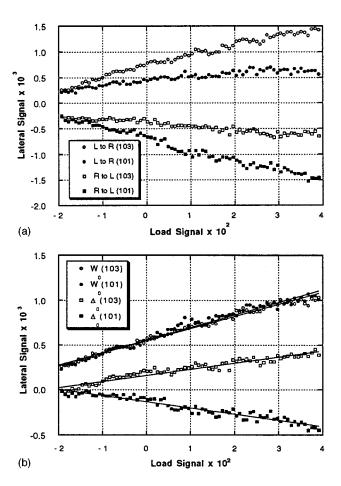


FIG. 8. (a) Lateral deflection signals for left-to-right and right-to-left scanning directions (1-2/A+B) as a function of load deflection signal (A-B/A+B) for the (101) and (103) facets. The total A+B signal (photodiode current) was 185 μ A. (b) The friction loop width W(L) and offset $\Delta(L)$ as a function of load for the (101) and (103) facets. Straight lines fit the data very well, justifying our assumption of linear friction behavior. The slopes of each line are measured and used in formulae given in the Appendix to solve for α/β , the normal force to lateral force deflection ratio.

We have demonstrated a quantitative method of lateral force calibration for the microfabricated tip-cantilever assemblies used in friction force microscopy. We find that there are significant variations among cantilevers fabricated from the same wafer. Tip variations also play a role. Furthermore, the overall system calibration depends on the precise alignment of the deflection sensor where optical detection is used.

In order to perform quantitative frictional force microscopy with the atomic force microscope, it is important to perform an experimental force calibration for *each* cantilever sensor. Quantitative measurements of nanoscale friction and adhesion based on calculated force constants, or average measured values for a given cantilever design, are unlikely to yield reproducible results.

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TABLE I. Experimental lever calibration results compared with numerical estimates. The experimental α/β ratio is approximated by $R_{\rm LEVER}$.

Lever	Experimental			Estimated		
	α/β	$\mu(103)$	μ(101)	$R_{ m LEVER}$	$k_{ m NORMAL}$	k_{LATERAL}
D(0.03)	51±6	0.51±0.09	0.42±0.10	61.6	0.037	66.6
E#1(0.1)	43 ± 3	0.52 ± 0.05	0.50 ± 0.05	39.4	0.111	92.7
E#2(0.1)	36 ± 4	0.74 ± 0.12	0.66 ± 0.14	39.4	0.111	92.7
F(0.5)	19±1	0.41 ± 0.03	0.33 ± 0.02	25.5	0.508	132

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APPENDIX

1. Photodiode response

An elliptical Gaussian beam has a normalized intensity

$$\psi(y,z) = \frac{2}{\pi \Delta \omega_{y} \Delta \omega_{z}} e^{(-2y^{2}/\Delta \omega_{y}^{2}) + (-2z^{2}/\Delta \omega_{z}^{2})}.$$

Here $\Delta \omega$ is the angular half-width of the *field* distribution, following the conventions of Gaussian optics. The half-width of the intensity distribution is then $\Delta \omega / \sqrt{2}$. If the beam is deflected by d in the y direction, the signal is given by

$$S(d) = \frac{A - B}{A + B} = 1 - \frac{1}{\Delta \omega_y} \sqrt{\frac{8}{\pi}} \int_d^{\infty} e^{-2y^2/\Delta \omega_y^2} dy.$$

The integral

$$I(d) = \int_{d}^{\infty} e^{-2y^{2}/\Delta\omega_{y}^{2}} dy = \int_{0}^{\infty} e^{-2(t+d)^{2}/\Delta\omega_{y}^{2}} dt$$

can be expanded around d=0 by taking a derivative

$$\begin{aligned} \frac{dI}{dd} &= \int_0^\infty \frac{\partial}{\partial d} \left[e^{-2(t+d)^2/\Delta \omega_y^2} \right] dt \\ &= \int_0^\infty -\frac{4(t+d)}{\Delta \omega_y^2} e^{-2(t+d)^2/\Delta \omega_y^2} dt = -e^{-2d^2/\Delta \omega_y^2}, \end{aligned}$$

likewise higher derivatives can be calculated:

$$\frac{d^2I}{dd^2} = \frac{4d}{\Delta\omega_y^2} e^{-2d^2/\Delta\omega_y^2}$$

and

$$\frac{d^3I}{dd^3} = \left[\frac{4}{\Delta\omega_y^2} - \frac{16d^2}{\Delta\omega_y^4}\right] e^{-2d^2/\Delta\omega_y^2}.$$

When these derivatives are evaluated at d=0, the even terms vanish, as expected, since S(d) is an odd function. Finally we put these terms into a Taylor expansion and get

$$S(d) = \sqrt{\frac{8}{\pi}} \frac{d}{\Delta \omega_y} \left[1 - \frac{4}{3!} \left(\frac{d}{\Delta \omega_y} \right)^2 + \frac{48}{5!} \left(\frac{d}{\Delta \omega_y} \right)^4 - \frac{960}{7!} \left(\frac{d}{\Delta \omega_y} \right)^6 + \dots \right].$$

2. Z and tilt calibration

We assume that the X calibration of the piezo scanner is correct and that the initial Z calibration is approximate. We make a topographic image of the faceted strontium titanate surface, with known facet angles of θ_1 =14.0° and θ_2 =-12.5° relative to the (305) surface normal. We wish to determine the correction factor γ for the Z calibration such that Z_{TRUE} = $\gamma Z_{INITIAL}$ and the tilt angle β of the (305) surface normal relative to the piezo scanner Z axis.

From the image we measure the apparent slopes $(\Delta Z/\Delta X)$ of the facets S_1 and S_2 . Then $\tan(\theta_1+\beta)=\gamma S_1$ and $\tan(\theta_2+\beta)=\gamma S_2$. From this we make a quadratic equation $\tan(\theta_1-\theta_2)=(\gamma S_1-\gamma S_2)/(1+\gamma^2 S_1 S_2)$. Solving for γ gives positive and negative solutions. The positive solution is physically reasonable:

$$\gamma = \frac{(S_1 - S_2) - \sqrt{(S_1 - S_2)^2 - 4S_1S_2 \tan^2(\theta_1 - \theta_2)}}{2S_1S_2 \tan(\theta_1 - \theta_2)}.$$

Then the tilt angle is easily calculated $\beta = \tan^{-1}(\gamma S_1) - \theta_1$.

3. Two slope calibration

We wish to find the lateral force calibration α in terms of the experimentally measured quantities $W_o'(101)$, $W_0'(103)$, $\Delta_o'(101)$, and $\Delta_o'(103)$. Since the magnitude and offset of lateral force coupling is unknown, we use the difference $\Delta_o'(101) - \Delta_o'(103)$ in the calculation. The ratios of uncalibrated experimental values should be equal to the ratios of the forces as calculated from geometry in Sec. V. Therefore

$$p = \frac{W'_o(101)}{W'_o(103)} = \frac{W'_{101}}{W'_{103}},\tag{A1}$$

$$q = \frac{\Delta'_o(101) - \Delta'_o(103)}{W'_o(101)} = \frac{\Delta'_{101} - \Delta'_{103}}{W'_{101}},$$
 (A2)

$$\alpha = \frac{W'_{103}}{W'_{o}(103)}. (A3)$$

Here p and q are pure number ratios derived from experimental data such as that in Fig. 8. From Eq. (A1) and the equations in Sec. V:

$$\mu_{101} = \frac{-1 + \sqrt{1 + \kappa^2 \sin^2 2\theta_{101}}}{2\kappa \sin^2 \theta_{101}},$$
 (A4a)

$$\kappa \equiv p \frac{\mu_{103}}{\cos^2 \theta_{103} - \mu_{103}^2 \sin^2 \theta_{103}}.$$
 (A4b)

There is also an ambiguity here between a friction coefficient and its reciprocal, similar to the one slope solution of Sec. V.

We choose the quadratic roots giving μ <1, which gives calibration results consistent with the calculated lever properties. Equation [A4(b)] expressed μ_{101} in terms of μ_{103} . From Eq. (A2),

$$2q = \left(\frac{1}{\mu_{101}} + \mu_{101}\right) \sin 2\theta_{101} - \left(\frac{1}{\mu_{103}} + \mu_{103}\right) \sin 2\theta_{103} \frac{1}{p}.$$
(A5)

Now we can substitute Eq. (A4) into Eq. (A5) to eliminate μ_{101} . As the resulting expression is difficult to invert, we solve it numerically for the root such that $0 < \mu_{103} < 1$. With this solution, we find the calibration

$$\alpha = \frac{1}{W_o'(103)} \frac{\mu_{103}}{\cos^2 \theta_{103} - \mu_{103}^2 \sin^2 \theta_{103}}.$$
 (A6)

- ¹G. Binnig, C. F. Quate, and C. Gerber, Phys. Rev. Lett. **56**, 930 (1986).
- ²C. M. Mate, G. M. McClelland, R. Erlandsson, and S. Chiang, Phys. Rev. Lett. **59**, 1942 (1987).
- ³ Fundamentals of Friction: Macroscopic and Microscopic Processes, edited by I. L. Singer and H. M. Pollock, NATO ASI Series E, Vol. 220 (Kluwer Academic, Dordrecht, 1992); Forces in Scanning Probe Methods, edited by H.-J. Guntherödt, D. Anselmetti, and E. Meyer, NATO ASI Series E, Vol. 286 (Kluwer Academic, Dordrecht, 1994).
- ⁴Park Scientific Instruments Inc., Sunnyvale, CA; Digital Instruments Inc., Santa Barbara, CA; Nanosensors GmbH, Aidlingen Germany; Olympus Optical Company, Japan.
- ⁵G. Meyer and N. M. Amer, Appl. Phys. Lett. **57**, 2089 (90); O. Marti, J. Colchero, and J. Mlynek, Nanotechnology **1**, 141 (1991).
- ⁶W. F. Kolbe, D. F. Ogletree, and M. B. Salmeron, Ultramicroscopy **42–44**, 1113 (1992); Q. Dai, R. Vollmer, R. W. Carpick, D. F. Ogletree, and M. Salmeron, Rev. Sci. Instrum. **66**, 5266 (1995).
- ⁷J. P. Cleveland, S. Manne, D. Bocek, and P. K. Hansma, Rev. Sci. Instrum. **64**, 403 (1993); T. J. Senden and W. A. Druker, Langmuir **10**, 1003 (1994).
- ⁸ M. Jaschke and H. J. Butt, Rev. Sci. Instrum. 66, 1258 (1995); H. J. Butt and M. Jaschke, Nanotechnology 6, 1 (1995). An incorrect implementa-

- tion of this approach is also discussed in J. L. Hutter and J. Bechhoefer, Rev. Sci. Instrum. **64**, 1868 (1993).
- ⁹ Y. Q. Li, N. J. Tao, J. Pan, A. A. Garcia, and S. M. Lindsay, Langmuir 9, 637 (1993); J. A. Ruan and B. Bushan, Trans. ASME J. Tribology 116, 378 (1994).
- ¹⁰ S. Fujisawa, E. Kishi, Y. Sugawara, and S. Morita, Appl. Phys. Lett. 66, 23 (1995), discusses lateral force calibration, but in fact the article presents a method for calibration the lateral force deflection sensor given the (calculated) lateral force constant.
- ¹¹ J. E. Sader and L. R. White, J. Appl. Phys. **74**, 1 (1993); J. M. Newmeister and W. Ducker, Rev. Sci. Instrum. **65**, 2527 (1994); M. Labardi, M. Allegrini, C. Ascoli, C. Frediani, and M. Salerno (to be published).
- ¹²Rod Alley, Berkeley Sensor, Actuator Center, University of California at Berkeley, and Marco Tortonese, Park Scientific Instruments, Sunnyvale California (private communication).
- ¹³ J. E. Sader, I. Larson, P. Mulvaney, and L. R. White, Rev. Sci. Instrum. 66, 3789 (1995).
- ¹⁴S. P. Timoshenko and J. N. Goodier, *Theory of Elasticity*, 3rd ed. (McGraw-Hill, New York, 1987).
- ¹⁵Reference 14.
- ¹⁶J. E. Sader, Rev. Sci. Instrum. 66, 4583 (1995).
- ¹⁷R. J. Warmack, X.-Y. Zheng, T. Thundat, and D. P. Allison, Rev. Sci. Instrum. **65**, 394 (1994).
- ¹⁸Dr. Marco Tortonese, Park Scientific Instruments Inc., Sunnyvale, California (private communication).
- ¹⁹ S. S. Sheiko, M. Möller, E. M. C. M. Reuvekamp, and H. W. Zandbergen, Phys. Rev. B 48, 5675 (1993).
- 20 In Sheiko *et al.*, the facet angles were given as $+14.0^{\circ}$ and -11.6° . The correct values are $+14.0^{\circ}$ and -12.5° .
- ²¹R. Carpick, N. Agraït, D. F. Ogletree, and M. Salmeron, J. Vac. Sci. Technol. B **14**, 1289 (1996).
- ²²AFM-100 control unit, RHK Technology Inc., Rochester Hills, MI.
- ²³ S. M. Hues, C. F. Draper, K. P. Lee, and R. J. Colton, Rev. Sci. Instrum. 65, 1561 (1994); A. E. Holman, P. M. L. O. Scholte, W. Chr. Heerens, and F. Tuinstra, *ibid.* 66, 3208 (1995); J. Fu, *ibid.* 66, 3785 (1995).
- ²⁴ Q. Dai, R. Vollmer, R. W. Carpick, D. F. Ogletree, and M. Salmeron, Rev. Sci. Instrum. 66, 5266 (1995).
- ²⁵Park Scientific Instruments, Sunnyvale, CA.
- ²⁶ M. Binggeli and C. M. Mate, Appl. Phys. Lett. **65**, 415 (1994); J. Hu, X.-D. Xiao, D. F. Ogletree, and M. Salmeron, Surf. Sci. **327**, 358 (1995).