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# Active Power Quality Improvement Strategy for Grid-connected Microgrid Based on Hierarchical Control

Wei Feng, *Student Member, IEEE*, Kai Sun, *Senior Member, IEEE*, Yajuan Guan, *Student Member, IEEE*, Josep M. Guerrero, *Fellow, IEEE*, Xi Xiao, *Member, IEEE*

**Abstract**—When connected to a distorted grid utility, droop-controlled grid-connected microgrids (DCGC-MG) exhibit low equivalent impedance. The harmonic and unbalanced voltage at the point of common coupling (PCC) deteriorates the power quality of the grid-connected current (GCC) of DCGC-MG. This work proposes an active, unbalanced, and harmonic GCC suppression strategy based on hierarchical theory. The voltage error between the bus of the DCGC-MG and the grid's PCC was transformed to the  $dq$  frame. On the basis of the grid, an additional compensator, which consists of multiple resonant voltage regulators, was then added to the original secondary control to generate the negative fundamental and unbalanced harmonic voltage reference. Proportional integral and multiple resonant controllers were adopted as voltage controller at the original primary level to improve the voltage tracking performance of the inverter. Consequently, the voltage difference between the PCC and the system bus decreased. In addition, we established a system model for parameter margin and stability analyses. Finally, the simulation and experiment results from a scaled-down laboratory prototype were presented to verify the validity of the proposed control strategy.

**Index Terms**—grid-connected current; power quality; droop; distorted; unbalance; hierarchical control.

## I. INTRODUCTION

Renewable energy has drawn considerable attention in recent years because of growing concerns regarding traditional fossil energy shortages and other environmental problems. Therefore, power systems have undergone major changes not only for ensuring sustainable development but also for solving power supply problems in remote areas [1]–[2]. One such innovation is the microgrid (MG), which can integrate different kinds of energy sources and power electronics interfaced with units of distributed generations (DGs).

Over time, MGs became expected to perform even more functions and complex. Thus, an advanced MG hierarchical theory was proposed to define the system on three levels, thereby facilitating controller design depending on the different

functions [3]–[4]. Although the MG's traditional hierarchical structure has been well developed over the past years, several issues have been raised as regards its practical operation, and a number of improvements have been made for the system's ancillary services [5]–[8].

The virtual impedance control loop was developed to optimize inductance-to-resistance ( $X/R$ ) ratio of the inverter's equivalent output impedance. This control loop is usually added to the MG's primary control to guarantee the good performance of a regular droop controller. However, reactive load sharing precision is closely associated with voltage, rather than frequency, and the voltage along distributed lines in the MG is not constant. Therefore, a secondary controller that includes a reactive power sharing loop was proposed in [5], thus allowing the central controller to be used for improving robustness instead for distributed control strategies. Nonetheless, communication conflicts and delays would occur more frequently as the number of DGs in the MG increases, and system stability will be impeded by the communication network's bandwidth in a hierarchical-controlled MG. The margin of communication delay was investigated in [6] with a small signal model of the system, and a gain scheduling approach was proposed in that paper to compensate for the effects of communication delay in a hierarchical-controlled MG.

As the nonlinear and unbalanced loads increasing along the low voltage distribution line, the power quality issue of islanded MG has drawn considerable attention by researchers recently. Many improving control approaches for droop controlled VCIs without communication network are proposed in [9]–[11]. A cooperative harmonic filtering strategy through G-H droop was proposed in [9]. With this strategy, harmonic current can be shared precisely and the power quality of MG bus voltage can be guarantee. Harmonic current is associated with the equivalent impedance of VCIs in MG. As harmonic current increases, the occurrence risk of high-frequency resonance in MG also increases. Therefore, a resonance suppression and harmonic current sharing strategy was investigated in [10] by extending the harmonic virtual impedance control loop. Moreover, an enhanced droop control method involving online virtual impedance adjustment was proposed in [11] for autonomous islanded MG; the virtual impedance at different components and sequences were tuned on line to realize accurate power sharing.

Researchers have reported on a communication-based hierarchical control for the unbalanced and harmonic bus voltage suppression of an islanded MG. The system's harmonic

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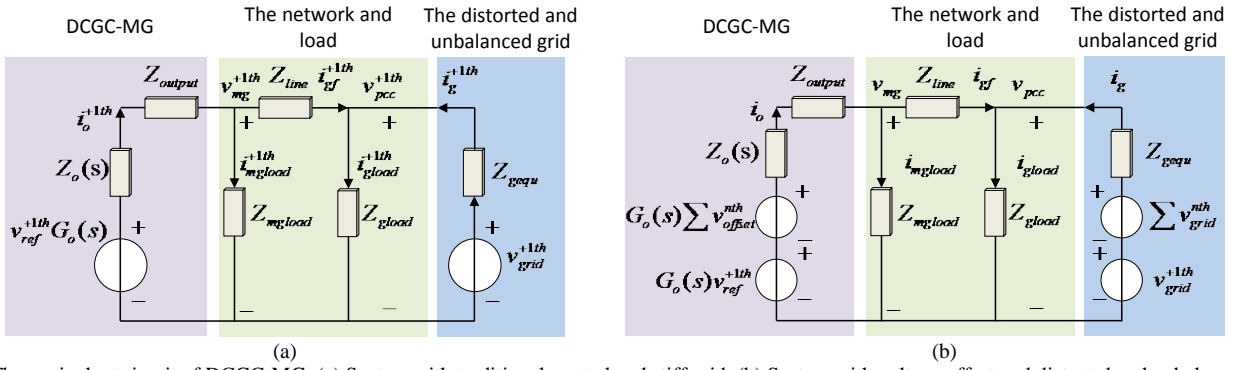


Fig. 1. The equivalent circuit of DCGC-MG. (a) System with traditional control and stiff grid, (b) System with voltage offset and distorted and unbalanced grid.

current sharing improvement was provided at the expense of increased voltage harmonic distortion. Thus, in [12], harmonic compensation was calculated using a secondary controller and then sent to inverters at the primary level. Following the same principle, the point of common coupling (PCC) unbalanced depression strategy was considered in [13]. Another voltage waveform control approach for suppressing harmonics in an islanded MG was proposed in [14], and a selective harmonic compensator was implemented in the secondary voltage control system to redistribute bus harmonic voltage distortions.

Given that the output impedance of DCGC-MG is small, the system, when connected to the grid, is equivalent to a controlled voltage source [15]–[16]. Few studies have been conducted on connecting DCGC-MG with the grid, and only a stiff grid scenario is considered in these works [17]. However, grid-connected voltage controlled inverters (GF-VCI), whose output feature is similar to that of the DCGC-MG, has been extensively investigated [18]–[20]. The control principle of GF-VCI was presented in [18], wherein multiple resonant ( $R$ ) controllers were adopted in the voltage control loop and different voltage components of the grid were extracted by sliding discrete Fourier transform. The harmonic voltage components were then feedforward to the inner loop of the system, consequently reducing the harmonic GCC of the GF-VCI [19]. Moreover, a closed-loop triple-loop control algorithm was proposed in [20]. The error of the grid-connecting current reference generated by fundamental power reference was calculated with an outer current controller to generate the voltage reference for GF-VCI. Then, accurate grid current harmonic compensation was realized.

Analogously, the distorted grid voltage will seriously deteriorate the power quality of the GCC of the DCGC-MG. However, no study has examined the power quality of the GCC of a system connected to an unbalanced and distorted grid at PCC. Therefore, the contribution of paper is to propose a control strategy for improving the power quality of the GCC and for suppressing the harmonic GCC components when DCGC-MGs are connected to a distorted grid. In this study, a detailed steady and dynamic performance analysis is performed, as well as a parameter margin analysis based on the equivalent transfer function model. A detailed design guideline for specific and practical parameters is also provided.

This work is organized as follows. Section II presents the model of the DCGC-MG connected to the distorted grid.

Section III describes the proposed control strategy based on a hierarchical structure. Section IV analyzes the steady performance and the control parameter margin. Section V discusses the experimental results. Section VI concludes the paper.

## II. MODELING OF THE SYSTEM

Fig. 1 (a) shows the simplified equivalent circuit of the DCGC-MG with a conventional control strategy when connected to the stiff grid utility. To facilitate this analysis, only one-droop controlled VCI is assumed to be present in the system, in which the droop controller generates the fundamental reference ( $v_{ref}^{+1th}$ ). The VCI's voltage transfer function and the equivalent impedance is represented by  $G_o(s)$  and  $Z_o(s)$ , respectively. A high  $X/R$  ratio between VCIs is guaranteed either by physical or virtual impedance ( $Z_{output}$ ) when the droop law is adopted. Local loads ( $Z_{mgload}$ ) are connected to the bus of the DCGC-MG. The system is connected to the stiff grid at the PCC through the line impedance ( $Z_{line}$ ), where the voltage is  $v_{pcc}^{+1th}$ , and the bus voltage of the DCGC-MG is  $v_{mg}^{+1th}$ . The grid utility is modeled as an ideal voltage source with the only fundamental positive voltage ( $v_{grid}^{+1th}$ ). The equivalent line impedance of the grid is  $Z_{g^{equ}}$ . The fundamental GCC ( $i_{gf}^{+1th}$ ) can be calculated as follows:

$$i_{gf}^{+1th} = \frac{v_{mg}^{+1th} - v_{pcc}^{+1th}}{Z_{line}} \quad (1)$$

However, when unexpected harmonic and unbalanced voltage disturbances occur at the grid, the grid can be denoted as the sum of  $v_{grid}^{+1th}$  and other components ( $\sum v_{grid}^{nth}$ ), at which point the voltage and current in the model can be decomposed as corresponding positive and negative sequences based on the method of symmetrical components. The magnitude of the negative fundamental or harmonic GCCs can be calculated based on the superposition theorem as follows:

$$|i_{gf}^{nth}(j\omega_b^{nth})| = \left| \frac{v_{mg}^{nth}(j\omega_b^{nth}) - v_{pcc}^{nth}(j\omega_b^{nth})}{Z_{line}(j\omega_b^{nth})} \right|_{n=-1, \pm 5, \pm 7, \dots} \quad (2)$$

being:

$$v_{mg}^{nth}(j\omega_b^{nth}) = v_{ref}^{nth} G_o(j\omega_b^{nth}) - i_o^{nth} [Z_o(j\omega_b^{nth}) + Z_{output}(j\omega_b^{nth})]$$

$$v_{pcc}^{nth}(j\omega_b^{nth}) = v_{grid}^{nth}(j\omega_b^{nth}) - i_g^{nth} Z_{gequ}(j\omega_b^{nth})$$

where,  $i_{gf}^{nth}$ ,  $i_o^{nth}$ ,  $i_g^{nth}$  are the negative fundamental or harmonic components of the GCC, inverter output current, and main grid current, respectively;  $v_{mg}^{nth}$ ,  $v_{grid}^{nth}$ ,  $v_{pcc}^{nth}$ , and  $v_{ref}^{nth}$  are the negative fundamental or harmonic components of the MG bus's voltage, the grid voltage, the PCC voltage at the grid side, and the offset voltage, respectively. Here,  $\omega_b^{nth}$  is the angular frequency.

The original control loops of droop-based VCIs are designed to maintain the positive fundamental component of the voltage. As such, the closed loop gain at the harmonic angular frequency of VCIs is very small, specifically  $G_o(j\omega_b^{nth}) \ll 0dB$ . Moreover, no negative fundamental or unbalanced harmonic components of grid voltage are directly sent back to the primary control. The DCGC-MG is almost a shortcut to the corresponding frequency when connected to the distorted grid. The amplitude of the negative fundamental and harmonic GCC can be approximated as follows:

$$|i_{gf}^{nth}(j\omega_b^{nth})| = \left| \frac{-v_{imped}^{nth}(j\omega_b^{nth}) - v_{pcc}^{nth}(j\omega_b^{nth})}{Z_{line}(j\omega_b^{nth})} \right|_{n=-1, \pm 5, \pm 7, \dots} \quad (3)$$

As shown in (3), the distortion of the GCC of the DCGC-MG is inevitable unless an additional control is adopted. However, the proposed compensator in the secondary control is responsible for generating an additional harmonic and unbalanced voltage offset (Fig.1 (b)) to reduce the voltage difference in the corresponding components across the line impedance, as shown in (4). In other words, the distorted and unbalanced GCC can be suppressed by decreasing the numerator in (4). Therefore, the system can be improved by generating and tracking the appropriate voltage offsets.

$$|i_{gf}^{nth}(j\omega_b^{nth})| = \left| \frac{v_{offset}^{nth} G_o(j\omega_b^{nth}) - v_{imped}^{nth}(j\omega_b^{nth}) - v_{pcc}^{nth}(j\omega_b^{nth})}{Z_{line}(j\omega_b^{nth})} \right|_{n=-1, \pm 5, \pm 7, \dots} \quad (4)$$

### III. PROPOSED POWER QUALITY IMPROVING STRATEGY

#### A. Improved primary control level

Because the voltage compensating offsets are transmitting to the VCIs at the primary level, two improvements are made to the original control loop. The DC offset signals in the  $dq$  frame are adopted to decrease the bandwidth requirements of the communication network. Therefore, the DC offset signals are transformed back to the  $abc$  frame by the different inverters in the primary control. The other improvement is that the tracking performances of all components are improved to generate accurate voltage offset at the output of each VCIs, as shown in Fig. 2.

Located at the primary control level are the VCI's inner voltage/current control loop, the virtual impedance control loop, and the well-known droop controller. The angle ( $\theta_{inv}^{+1th}$ ) and amplitude ( $E_{inv}^{+1th}$ ) of VCIs' fundamental voltage reference is generated by the droop controller, as shown below:

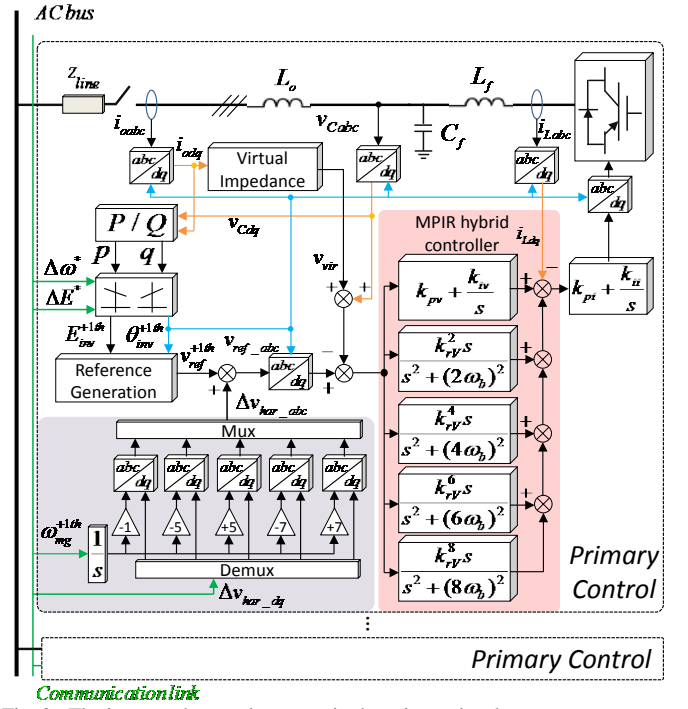


Fig. 2. The improved control strategy in the primary level

$$\begin{cases} \theta_{inv}^{+1th} = \int [\omega_b^* + \Delta\omega^* - m_p (P^* - G_{LPF}(s)P)] dt \\ E_{inv}^{+1th} = E_b^* + \Delta E^* - m_q [Q^* - G_{LPF}(s)Q] \end{cases} \quad (5)$$

where  $m_p$  and  $m_q$  are droop parameters for active power and reactive power, respectively;  $P^*$  and  $Q^*$  are the rated active and reactive power of the inverters, and  $\omega_b^*$  and  $E_b^*$  represent the rated angular frequency and amplitude of the fundamental component.  $\Delta\omega^*$  and  $\Delta E^*$  are the angular frequency and the amplitude of fundamental increments transferred through the communication link.  $G_{LPF}(s)$  is a regular low pass filter (LPF), which smoothes the calculated instantaneous power ( $P$  and  $Q$ ) and provides more damping to the system.

The restoring and synchronization controllers at the secondary control level and the power flow controller at the tertiary control level will be switched in the islanded mode or the grid-connected mode of the system, respectively. Therefore,  $\Delta\omega^*$  and  $\Delta E^*$  are calculated differently depending on the system's operation mode, as follows:

$$\Delta\omega^* = \begin{cases} \Delta\omega_{syn}^{+1th} + \Delta\omega_p^{+1th} (Grid - connecting) \\ \Delta\omega_{rest}^{+1th} & (Islanded) \end{cases} \quad (6a)$$

$$\Delta E^* = \begin{cases} \Delta E_{syn}^{+1th} + \Delta E_Q^{+1th} (Grid - connecting) \\ \Delta E_{rest}^{+1th} & (Islanded) \end{cases} \quad (6b)$$

where  $\Delta\omega_{syn}^{+1th}$  and  $\Delta E_{syn}^{+1th}$  are the outputs of the synchronization controller,  $\Delta\omega_{rest}^{+1th}$  and  $\Delta E_{rest}^{+1th}$  are the outputs of the restoring controller in the secondary control.

The DC offset signals in the  $dq$  frame based on  $\omega_b^{nth}$  must be transformed back to the  $abc$  frame to combine the final three-phase voltage reference ( $v_{ref\_abc}$ ) of the VSIs as follows:



$$\begin{cases} v_{ref\_a} = E_{inv}^{+1th} \sin(\theta_{inv}^{+1th}) + \Delta v_{har\_a} \\ v_{ref\_b} = E_{inv}^{+1th} \sin(\theta_{inv}^{+1th} - 2\pi/3) + \Delta v_{har\_b} \\ v_{ref\_c} = E_{inv}^{+1th} \sin(\theta_{inv}^{+1th} + 2\pi/3) + \Delta v_{har\_c} \end{cases} \quad (7)$$

where  $\Delta v_{har\_abc}$  is the voltage offset in the  $abc$  frame that is generated by the proposed compensator.

Then,  $v_{ref\_abc}$  is transformed to the  $dq$  frame with  $\theta_{inv}^{+1th}$  for the inner voltage/current controllers of the VCI. Given that DC components and  $2n^{th}$  harmonic components are present in the voltage offset in the  $dq$  frame, a hybrid controller consisting of a regular proportional integral (PI) controller and multiple  $R$  controllers (PIMR) is adopted as the voltage control loop, shown in (8). The use of the PIMR voltage controller is advantageous as it will improve the power quality when the DCGC-MG is operated under islanded mode with nonlinear loads [21]–[22].

$$G_v = k_{pv} + \frac{k_{iv}}{s} + \sum_{n=2,4,6,\dots} \frac{k_{rv}^{nth}}{s^2 + (n\omega_b)^2} \quad (8)$$

where  $k_{pv}$  and  $k_{iv}$  are the control parameters of the regular PI controller, and  $k_{rv}^n$  is the integral parameter for  $R$  controller.

### B. Improved secondary control level

The system's improved secondary control level is depicted in Fig. 3. The conventional frequency/amplitude restoring controller in the islanded mode and the synchronization controller in the grid-connected mode have been discussed thoroughly in previous works [5], [8].

However, even when the PIMR voltage controller is adopted at the primary level, the system's GCC will still be distorted by the inevitable harmonic and unbalanced voltage differences between the PCC and the system bus. Therefore, to overcome this problem, a harmonic and unbalanced compensator is introduced at the secondary level to eliminate the corresponding voltage differences and improve the power quality of the GCC, as shown in Fig. 4. When Park transformation is applied, the three-phase error voltage with an angular frequency of  $n\omega_b$  in the  $abc$  frame can be transformed to sine and cosine signals in the  $dq$  frame. Therefore, multiple parallel  $R$  controllers are adopted, as shown in (9).

$$G_{r\_sec}(s) = \sum_{n=2k} G_{r\_sec}^{nth}(s) = \sum_{n=2k} \frac{k_{r\_Sec}^{nth} s}{s^2 + (n\omega_b)^2} \quad (9)$$

where  $k_{r\_Sec}^{nth}$  is the control parameter of  $R$  controllers for different harmonic components.

The  $R$  controllers with resonant angular frequencies of  $2\omega_b$ ,  $4\omega_b$  and  $8\omega_b$  are used to compensate for the negative 1<sup>st</sup>, positive 5<sup>th</sup>, negative 7<sup>th</sup> components in the  $abc$  frame, respectively, while the  $R$  controller with resonant angular frequency of  $6\omega_b$  is used to compensate for the negative 5<sup>th</sup> and positive 7<sup>th</sup> components. The specific harmonic component selection and calculation are realized through the infinite gain of the corresponding  $R$  controller at the resonant angular frequency, which is attenuated sharply at the other angular

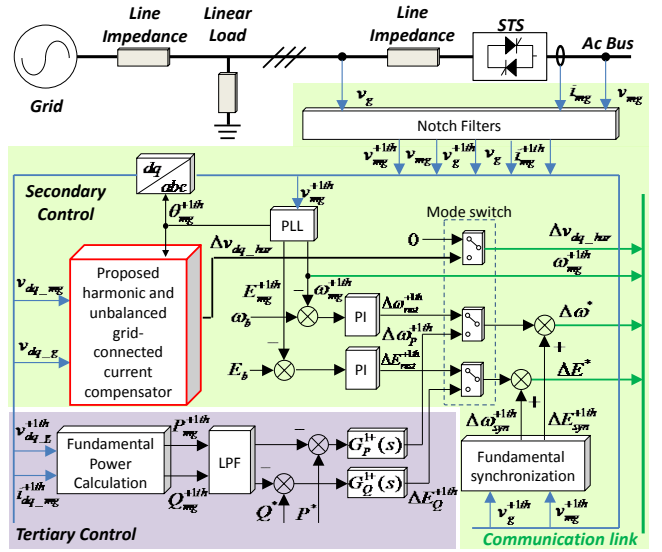


Fig. 3. The tertiary and improved secondary control for DCGC-MG with the proposed compensator

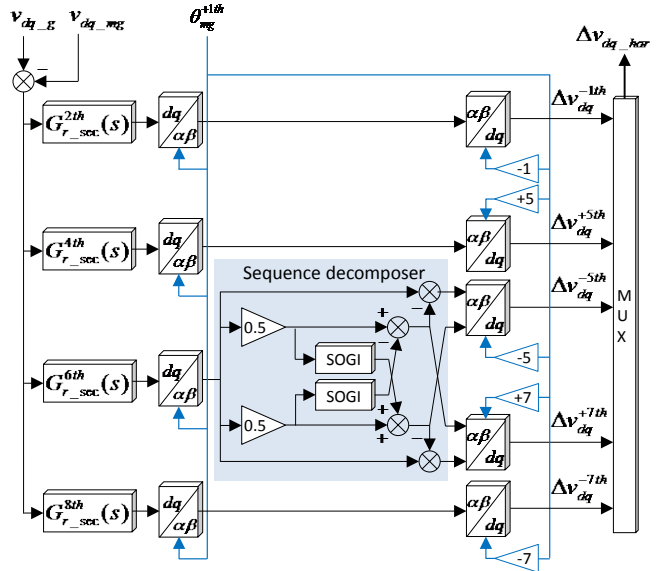


Fig. 4 The proposed compensator in the secondary level

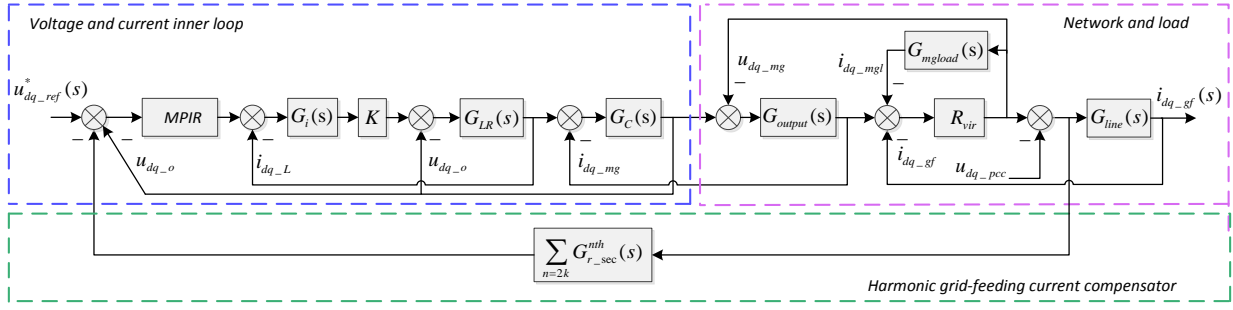
frequency. Therefore, no additional harmonic component estimators are needed, and the proposed control strategy can be implemented with minor calculation requirements.

To transform the offset signal to the DC signal, the output of  $R$  controllers are first transformed to the  $\alpha\beta$  frame with an angular frequency of  $\omega_b$  and then transformed to the DC signal by using Park transformation with the corresponding angular frequency and sequence, as shown in Fig. 4. Therefore, a regular sequence decomposer based on the 1/4 delay method is adopted for extracting the positive and negative 6<sup>th</sup> signals from the output of  $G_{r\_sec}^{6th}(s)$ , in which a second-order generalized integrator (SOGI) is used for the phase delay, as shown below:

$$G_{SOGI}(s) = \frac{k(6\omega_b)^2}{s^2 + 6k s \omega_b + (6\omega_b)^2} \quad (10)$$

where  $k$  is the coefficient affecting the SOGI's bandwidth.

The negative fundamental and unbalanced harmonic voltage offsets are then sent back to the primary control level. The

Fig. 5. The equivalent control model in the  $dq$  frame

proposed compensator is switched on when the DCGC-MG synchronizes with the distorted grid, and is switched off when the MG is converted to islanded mode.

#### IV. PERFORMANCE AND PARAMETER MARGIN ANALYSIS

To analyze the performance and parameter margin of the proposed compensator, the proposed compensation loop is made equivalent to another outer voltage loop of the VCI. Considering that the control parameters of the PIMR controller and the proposed compensator will affect system stability as well as grid-connected harmonic and unbalanced current suppression performance in coupling, an equivalent control model is established in the  $dq$  frame, as shown in Fig.5.

The fundamental positive reference of the VCI is generated by the droop controller, and this analysis focuses on the system's negative and harmonic components. Therefore, the droop control loop is omitted, and all the coupling items resulting from the Park transformation are ignored to simplify the analysis. The control model is divided into three parts. The first part consists of the inner voltage/current controller and the inverter's  $L_f C_f$  filter ( $G_{LR}(s)$  and  $G_C(s)$ ). The three-phase inverter is modeled again as ( $K$ ). The second part consists of the local loads ( $G_{mgload}(s)$ ), the line impedance between the VCI and the system bus ( $G_{output}(s)$ ), and the line impedance between the system bus and PCC ( $G_{line}(s)$ ). A virtual infinite resistor ( $R_{vir}$ ) is added to ensure that a numerical solution can be derived. The third part is the proposed offset compensator. We ignore the harmonic and sequence decomposer at the secondary control level, the re-composer in the primary control, and the communication link delay. We assume that the output of the compensator can be accurately sent to the primary level. Therefore, the controller parameters affect the steady-state performance only. The model's input is the voltage reference in the  $dq$  frame ( $u_{dq\_ref}^*(s)$ ), the output is the GCC of the DCGC-MG ( $i_{dq\_gf}(s)$ ), and the disturbance is the distorted grid voltage ( $u_{dq\_pcc}(s)$ ), as shown below:

$$i_{dq\_gf}(s) = G(s)u_{dq\_ref}^*(s) + \Phi(s)u_{dq\_pcc}(s) \quad (11)$$

where  $G(s)$  is the voltage transfer function of inverter, which mainly represents the influence of the fundamental positive reference generated by the local droop controller to the DCGC-MG's GCC, and  $\Phi(s)$  is the disturbance transfer function, which mainly denotes the influence of the harmonic voltage of the grid on the corresponding components of GCC.

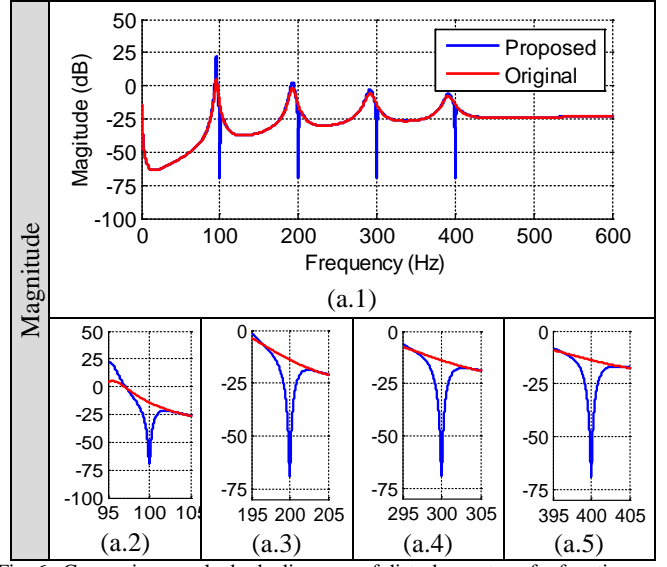


Fig. 6. Comparison on the bode diagrams of disturbance transfer function

The details of  $\Phi(s)$  is provided in the Appendix.

Fig. 6 shows the comparisons of the disturbance transfer functions. As shown, with the proposed compensator, the DCGC-MG's amplitude-frequency characteristic is attenuated at the angular frequency of  $2n\omega_b$  in the  $dq$  frame when compared to the conventional system with only the PIMR voltage controller. Therefore, the grid-connected harmonic and unbalanced currents in the  $abc$  frame can be impeded accordingly. Considering that the suppression performance of the  $2n^{\text{th}}$  harmonic GCC in the  $dq$  frame is affected by both the parameters of the PIMR controller and the proposed compensator, we can estimate the steady performance by the magnitude of  $\Phi(s)$  in frequency domain, as follows:

$$\begin{aligned} |i_{dq\_gf}(s)| &= |\Phi(s)u_{dq\_pcc}(s)| \\ &= f(k_{r\_Sec}^{nth}, k_{rV}^{nth}) \end{aligned} \quad (12)$$

being:

$$s = jn\omega_b, \quad u_{dq\_pcc}(s) = \sum_{n=2,4,6,8} \frac{v_{dq}^n n\omega_b}{s^2 + (n\omega_b)^2}$$

where  $k_{r\_Sec}^{nth}$  and  $k_{rV}^{nth}$  are the resonant control parameter in the proposed compensator and in the PIMR voltage controller, respectively; and  $v_{dq}^n$  is the disturbance voltage's amplitude in the grid utility.

Fig. 7 shows the simulation results of (12), which are

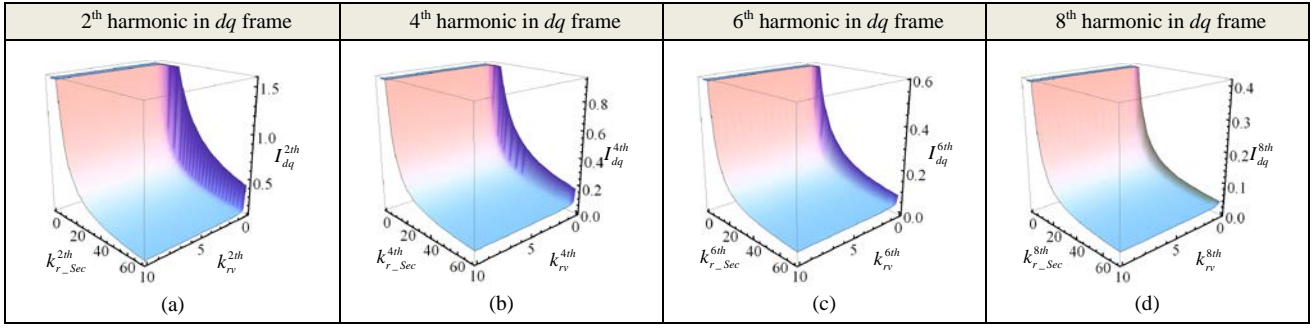


Fig. 7. The comparison on steady-state suppression performance.

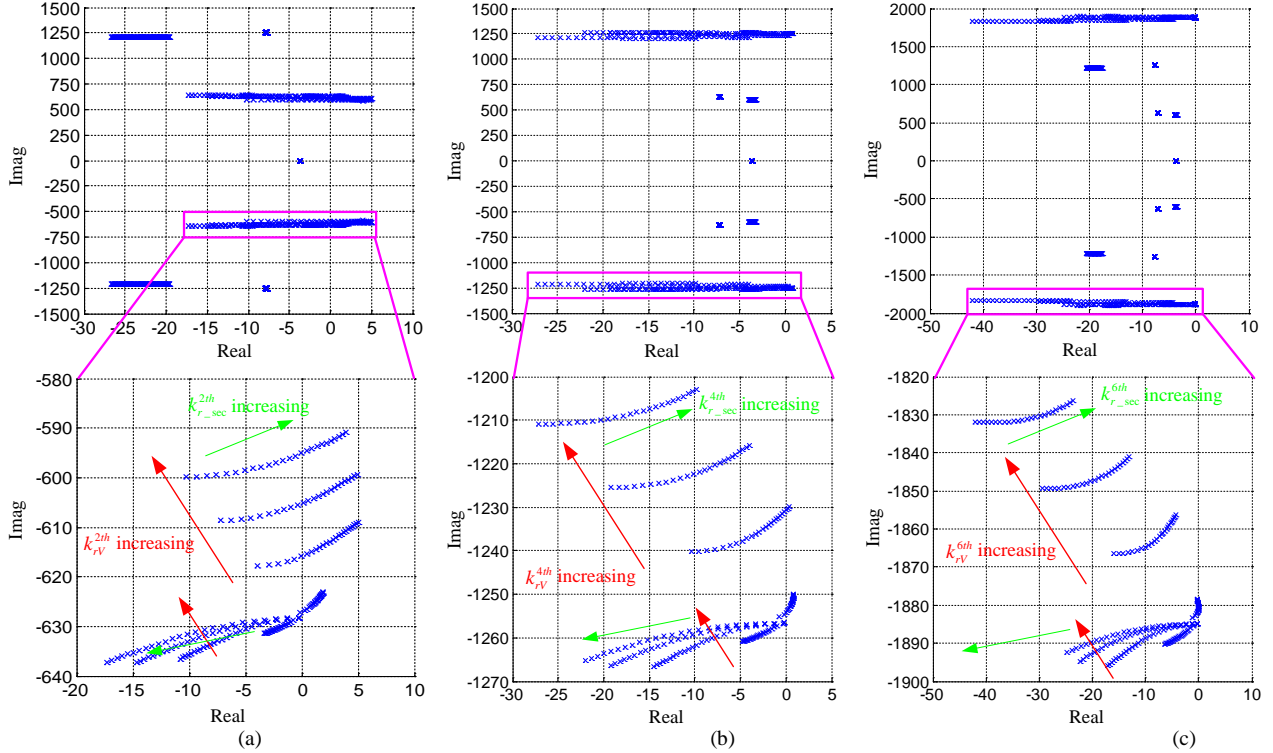


Fig. 8. Trace of modes as a function of resonant term for the PIMR voltage controller and the proposed compensator: (a) The latent root of  $\lambda_{20}$  and  $\lambda_{22}$  when  $1 < k_{r\_Sec}^{2th} < 100$  and  $1 < k_{rV}^{2th} < 40$ , (b) The latent root of  $\lambda_{15}$  and  $\lambda_{17}$  when  $1 < k_{r\_Sec}^{4th} < 100$  and  $1 < k_{rV}^{4th} < 40$ , (c) The latent root of  $\lambda_{11}$  and  $\lambda_{13}$  when  $1 < k_{r\_Sec}^{6th} < 100$  and  $1 < k_{rV}^{6th} < 40$ .

conducted under the same harmonic voltage amplitude with different angular frequencies of  $2n\omega_b$  in the  $dq$  frame. Based on the results, the following conclusions can be drawn:

- The  $2n^{th}$  of GCC in the  $dq$  frame decreases as  $n$  increases even without the suppression control, mainly because the equivalent harmonic impedance is increasing while the angular frequency is increasing.
- The  $2n^{th}$  of GCC in the  $dq$  frame cannot be suppressed by the PIMR voltage controller at primary control level alone, even with greater control parameters, because no corresponding voltage reference which presents the difference between the PCC and the bus of DCGC-MG is sent back to the primary controller.
- With the proper voltage tracking ability available in the primary control, the  $2n^{th}$  harmonic GCC are suppressed effectively when the compensator's control parameters are

increasing. Otherwise, the suppression performance will be compromised. The reason is that the harmonic voltage reference generated by the compensator should be properly tracked by VCIs to decrease the correspondent voltage error between the bus of DCGC-MG and grid's PCC.

Aside from the steady-state performance of the compensator, system stability is another important issue. The root locus based on different  $k_{r\_Sec}^{nth}$  and  $k_{rV}^{nth}$  at  $2n^{th}$  harmonic components in the  $dq$  frame are plotted to analyze the control parameter margins for DCGC-MG. As shown in Fig.8 (a), two pairs of conjugate poles are mainly involved when the resonant terms of the PIMR voltage controller and the proposed compensator are changing.  $\lambda_{20}$  and  $\lambda_{22}$  are moving away from each other as  $k_{r\_Sec}^{2th}$  increases, causing the pole to move across the imaginary

TABLE I  
THE PARAMETERS OF POWER STAGE AND CONTROL SYSTEM

	Item	Description		Item	Description		Item	Description	
Electrical Circuit	$V_{dc}$	DC Voltage	650V	$f$	MG Frequency	50 Hz	$C_f$	Filter Capacitance	9.9 $\mu$ F
	$V_{MG}$	MG Voltage	311 V	$L_f$	Filter Inductance	1.8 mH	$L_{line}$	Line Inductance	1.8 mH
Loads	$P_{reg}$	P of regular load	2.2 kW	$P_{sen}$	P of sensitive load	0.3 kW			
	$Q_{reg}$	Q of regular load	0 Var	$Q_{sen}$	Q of sensitive load	0 Var			
Primary	$k_{pi}$	Current P term	0.8	$K_{iv}$	Voltage I term	50	$k_{rv}^{4th}$	4 <sup>th</sup> PR integral term	40
	$K_{pv}$	Voltage P term	0.7	$k_{rv}^{2th}$	2 <sup>th</sup> PR integral term	35	$k_{rv}^{6th}$	6 <sup>th</sup> PR integral term	40
	$k_{rv}^{8th}$	8 <sup>th</sup> PR integral term	40	$m_q$	Droop Q term	0.02			
	$m_p$	Droop P term	1e-4	$\omega_c$	LPF time coefficient	50			
Secondary	$k_{rSec}^{2th}$	2 <sup>th</sup> PR integral term	35	$k_{rSec}^{6th}$	6 <sup>th</sup> PR integral term	45			
	$k_{rSec}^{4th}$	4 <sup>th</sup> PR integral term	40	$k_{rSec}^{8th}$	8 <sup>th</sup> PR integral term	50			
Tertiary	$k_{pP}$	P for $Q_{mg}$	2e-4	$k_{dP}$	D for $P_{mg}$	2e-6	$k_{iQ}$	I for $Q_{mg}$	1e-2
	$k_{iP}$	I term for $P_{mg}$	2e-3	$k_{pQ}$	P for $Q_{mg}$	1e-3	$k_{dQ}$	D for $Q_{mg}$	2e-6

axis and making the system unstable. However, the poles of  $\lambda_{20}$  and  $\lambda_{22}$  move close to the real axis as  $k_{rv}^{2th}$  increases, also causing the poles to move across the imaginary axis when  $k_{rSec}^{2th}$  becomes sufficiently large. The situation for the 4<sup>th</sup> and 6<sup>th</sup> harmonic controllers in the  $dq$  frame are similar, except that the resonant parameter margins for both resonant controllers in the PIMR and the proposed compensator are enlarged as the order increases.

## V. EXPERIMENTAL VERIFICATION

A scaled-down experimental setup consisting of two Danfoss 2.2 kW inverters, a real-time dSPACE1006 platform,  $L_f C_f$  filters, line impedance, and two resistive loads is built, as shown in Fig. 9. One inverter is used for emulating the distorted and unbalanced grid, whereas the other two are controlled as the DCGC-MG for verifying the validity of proposed control strategy. The electrical setup and the control system parameters are listed in Table I.

Considering that the purpose is to test DCGC-MG (with or without the proposed control strategy) when it is connected to the distorted grid, the magnitude and angular frequency of harmonic components of the distorted grid voltage are set based on a general assumption that the low frequency harmonic components resulting from non-linear and single phase loads cover the main part of the distorted PCC voltage, and the magnitude of harmonic voltage components are attenuated as the order increases, as shown in Fig. 10 (a). The harmonic analysis reveals that there are negative 1<sup>st</sup>, positive and negative 5<sup>th</sup>, positive and negative 7<sup>th</sup> components, and so on in the grid voltage. The details are shown in Fig.10 (b).

The GCC of the DCGC-MG and the output current of the two VCIs when the system is connected to the distorted grid without the proposed compensator are shown in Figs. 11 (a.1), (a.2), and (a.3), and the results of the harmonic analysis are shown in Figs. 11 (b.1), (b.2), and (b.3). The GCC is highly distorted because of the existing harmonic voltage difference between the PCC and the DCGC-MG's bus. Moreover, the output harmonic current of the VCIs affects its output voltage and the system's bus voltage, further deteriorating the power quality of the output current of the VCIs. However, when the fundamental and harmonic voltage components between the PCC and the DCGC-MG's bus is decreased, and when

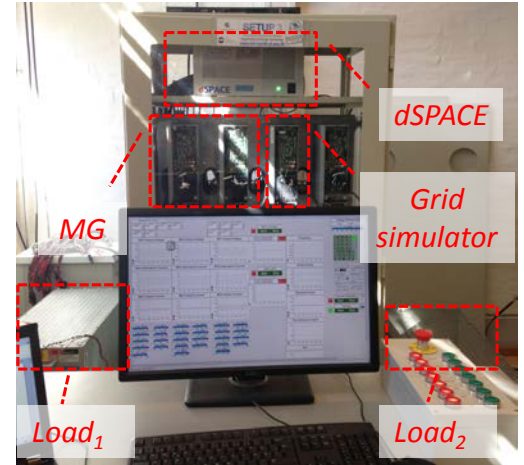


Fig. 9. The scaled-down experimental setup.

the proposed compensator is adopted, the difference of fundamental and harmonic voltage components between PCC and DCGC-MG's bus is decreased and the power quality of the GCC is improved, as shown in the Fig.11 (c.1). The negative fundamental, positive, and negative 5<sup>th</sup> and 7<sup>th</sup> components of the GCC are decreased to approximately 0.05, 0.025, and 0.02 A. The low output harmonic current will also improve the operation of the droop controller. Therefore, the output current of the VCIs is improved. The harmonic analyses are shown in detail in Figs. 11 (d.1), (d.2) and (d.3).

However, as the grid is distorted dynamically in reality, another scenario is used to test the dynamic response of the proposed control strategy, as shown in 12. The DCGC-MG is connected to the ideal grid at 0 s. The peak value of the GCC is 3.65 A. As shown in subfigure #1 in Fig. 12, the power quality of the GCC is high at 0 s. When the distorted voltage disturbance is added to the grid at 0.8 s, the GCC becomes distorted, as shown in subfigure #2 in Fig. 12. However, the proposed compensator only takes 2.7 s to generate the appropriate voltage offset to improve the power quality of the GCC, as shown in subfigure #3 in Fig. 12. Step down testing is also conducted on the distorted grid voltage disturbance at 7.5 s. The same phenomenon is observed in the system. Although the GCC is distorted during the dynamic response, the power quality of the GCC will be guaranteed when the system with proposed control strategy returns to a stable point.



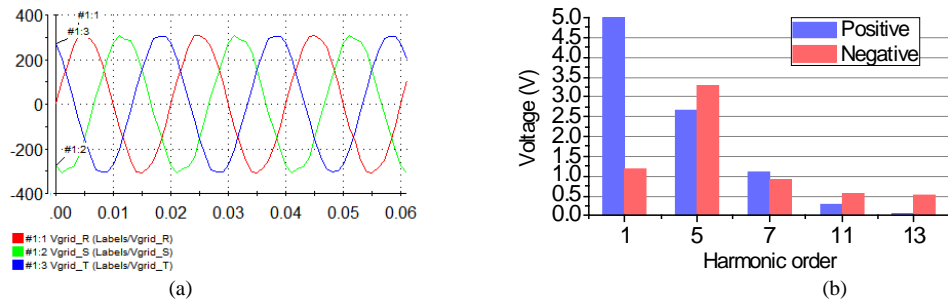


Fig. 10. The 3 phase distorted grid voltage in experiments. (a) The waveform of voltage, (b) The voltage harmonic analysis.

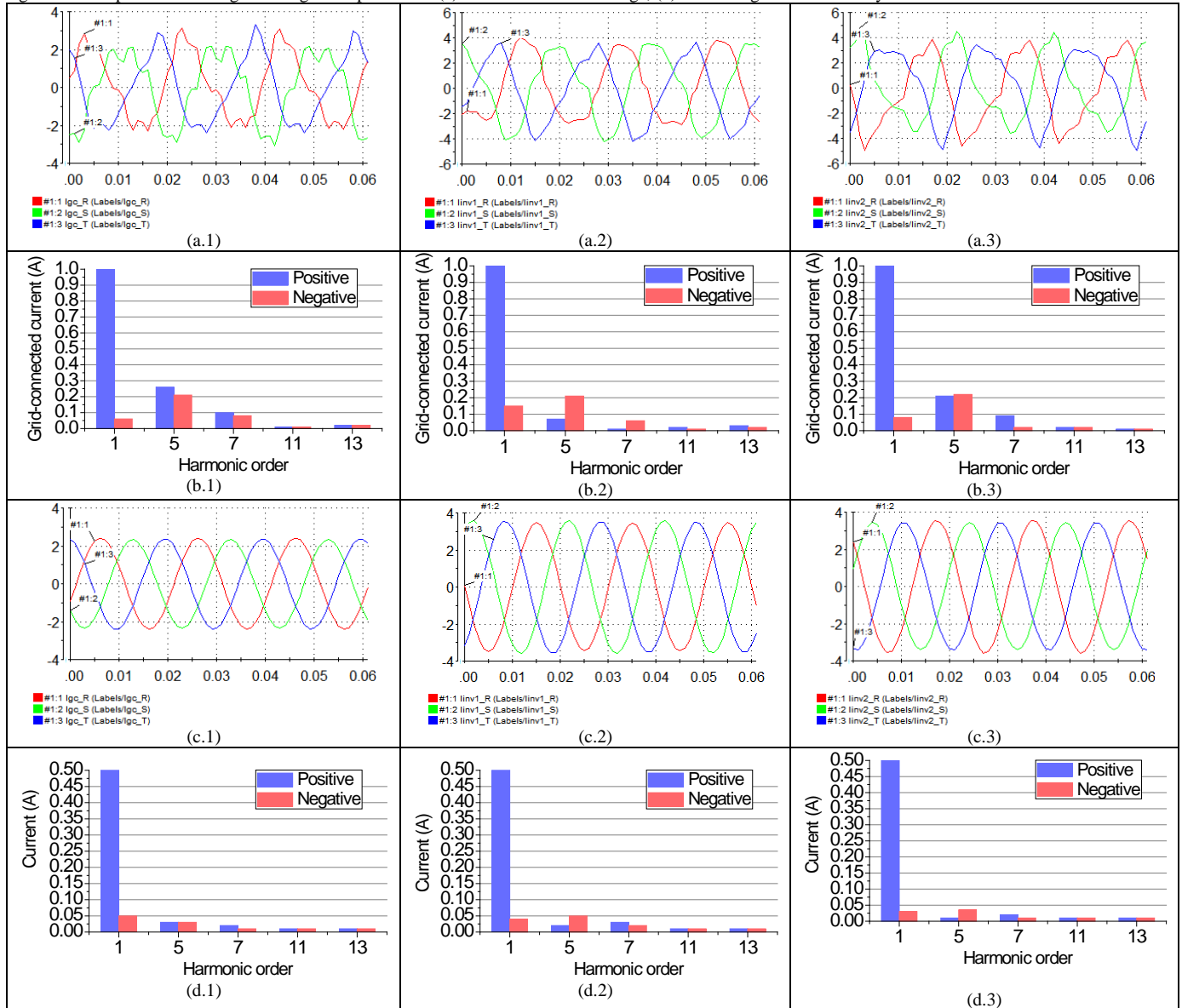


Fig. 11. The dynamic response of the proposed control strategy.

## VI. CONCLUSIONS

This work developed an active harmonic and unbalanced GCC compensation strategy based on hierarchical theory for the DCGC-MG. The voltage error between the bus of the system and the PCC was transformed to the  $dq$  frame, and an additional compensator consisting of multiple  $R$  voltage controllers were added to the original secondary control to

generate the negative fundamental and harmonic voltage offset of the VCIs in the primary control. PIMR controllers were adopted as voltage controllers at the original primary level to improve the VCI's voltage tracking performance. Consequently, the corresponding voltage component differences between the PCC and the bus of the DCGC-MG decreased significantly, thus improving the power quality of the GCC. Experimental results were included to validate the excellent behavior of the proposed compensation strategy.

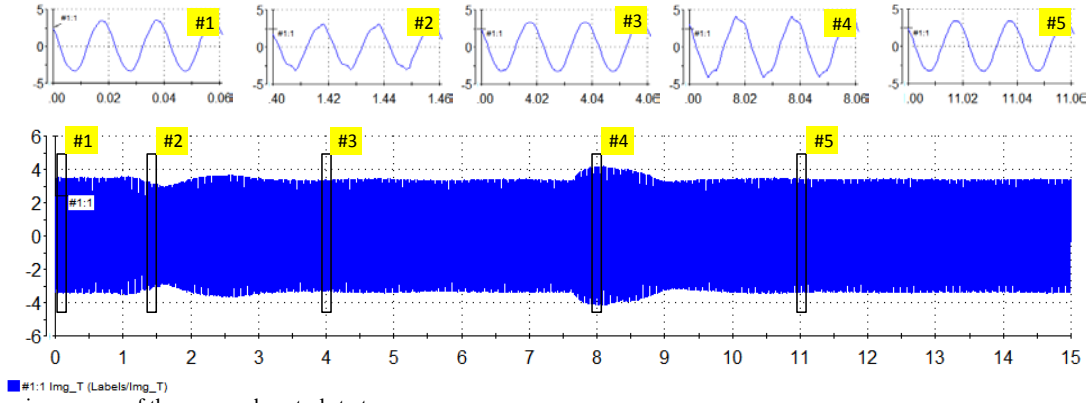


Fig. 12. The dynamic response of the proposed control strategy.

## APPENDIX

The detailed of disturbance transfer in Section IV is shown as follows:

$$\Phi(s) = \frac{\alpha}{\beta} \quad (\text{A.1})$$

Where:

$$\begin{aligned} \alpha = & -G_{line} - G_c G_{line} G_{LR} - G_c G_{line} G_{output} - G_i G_{line} G_{LR} K - G_c G_i G_{line} G_{LR} G_{output} K - G_c G_i G_{line} G_{LR} G_v K - G_{mgload} R_{vir} - G_c G_{LR} G_{mgload} R_{vir} \\ & - G_{line} G_{output} R_{vir} - G_c G_{line} G_{LR} G_{output} R_{vir} - G_c G_{mgload} G_{output} R_{vir} - G_i G_{LR} G_{mgload} K R_{vir} - G_i G_{line} G_{LR} G_{output} K R_{vir} - G_c G_i G_{LR} G_{mgload} G_{output} K R_{vir} \\ & - G_c G_i G_{LR} G_{mgload} G_v K R_{vir} - G_c G_i G_{line} G_{LR} G_{output} G_v K R_{vir} \end{aligned}$$

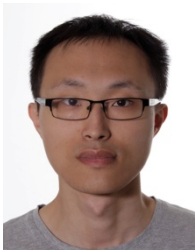
$$\begin{aligned} \beta = & 1 + G_c G_{LR} + G_c G_{output} + G_i G_{LR} K + G_c G_i G_{LR} G_{output} K + G_c G_i G_{LR} G_v K + G_{line} R_{vir} + G_c G_{line} G_{LR} R_{vir} + G_{mgload} R_{vir} + G_c G_{LR} G_{mgload} R_{vir} \\ & + G_{output} R_{vir} + G_c G_{line} G_{output} R_{vir} + G_c G_{LR} G_{output} R_{vir} + G_c G_{mgload} G_{output} R_{vir} + G_i G_{line} G_{LR} K R_{vir} + G_i G_{LR} G_{mgload} K R_{vir} + G_i G_{LR} G_{output} K R_{vir} \\ & + G_c G_i G_{line} G_{LR} G_{output} K R_{vir} + G_c G_i G_{LR} G_{mgload} G_{output} K R_{vir} + G_c G_i G_{line} G_{LR} G_v K R_{vir} + G_c G_i G_{LR} G_{mgload} G_v K R_{vir} + G_c G_i G_{LR} G_{output} G_v K R_{vir} \\ & + G_c G_i G_{LR} G_{output} G_{sec} G_v K R_{vir} \end{aligned}$$

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