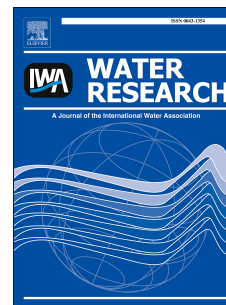


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Philani Ncube, Marc Pidou, Tom Stephenson, Bruce Jefferson, Peter Jarvis



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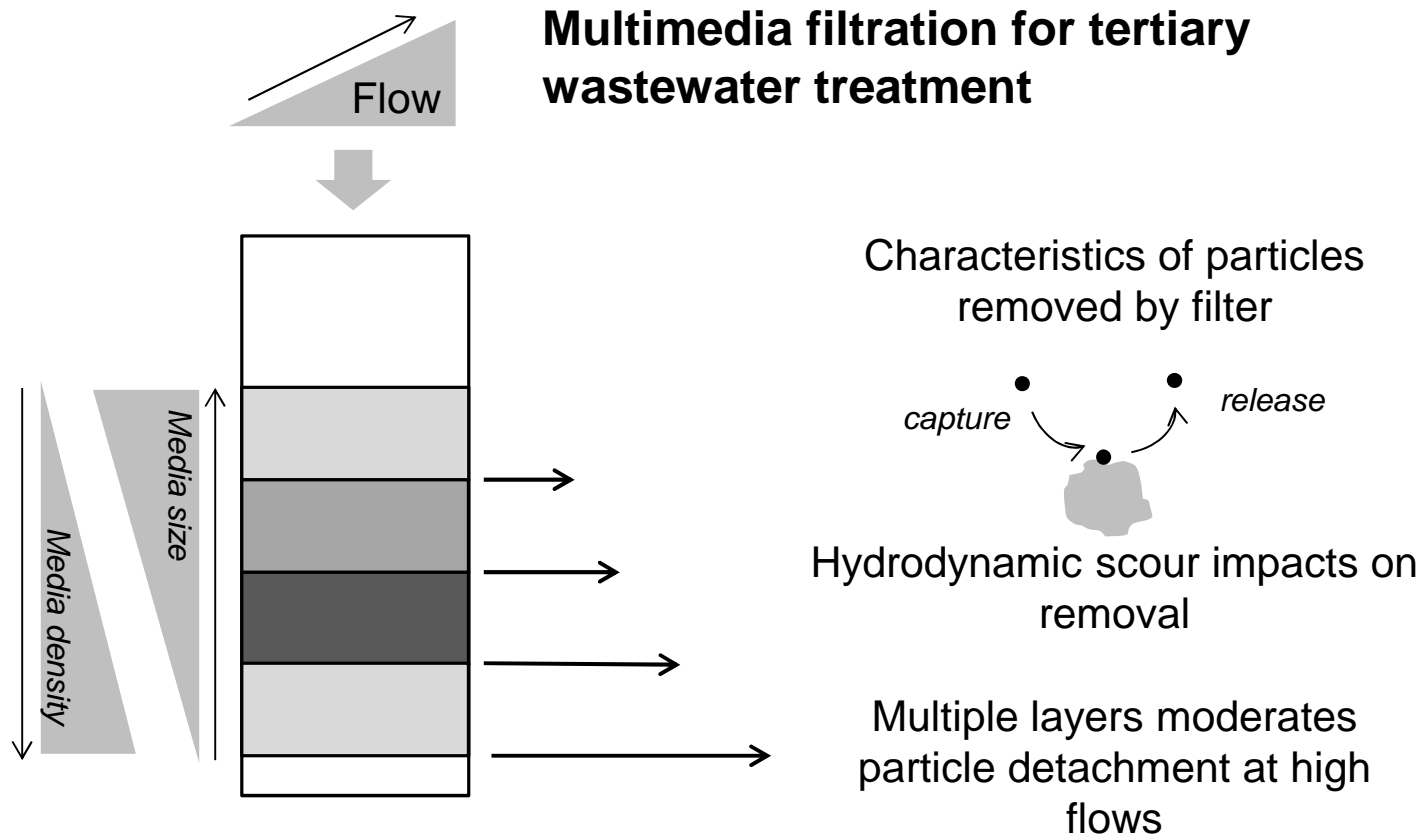
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1 The effect of high hydraulic loading rate on the removal efficiency of a
2 quadruple media filter for tertiary wastewater treatment

3

4 *Philani Ncube, Marc Pidou, Tom Stephenson, Bruce Jefferson, Peter Jarvis**

5 ^aCranfield Water Science Institute, Cranfield University, College Road, Cranfield,
6 Bedfordshire, MK43 0TE UK.

7 *Corresponding author: p.jarvis@cranfield.ac.uk, 00 44 1234 750111 ext 3374

8 **Abstract**

9 It is well known that filtration removal efficiency falls with an increase in flow rate; however,
10 there is limited supporting experimental data on how removal efficiency changes for filters
11 with multiple layers of media and for wastewater filtration, a practice that is becoming more
12 common. Furthermore, information is not available on the characteristics of particles that are
13 removed at different flow rates. Here, a quadruple media filter was operated at hydraulic
14 loading rates (HLRs) between 5 and 60 m h^{-1} with subsequent measurement of total
15 suspended solids, turbidity and particle size distribution (PSD). Samples were collected from
16 the filter influent, effluent and also from between media layers. Pressure changes across the
17 filter layers were also measured. The solids removal efficiency of the filter varied inversely
18 with the increase in filtration rate. However, the multiple media layers reduced the negative
19 impact of increased HLR in comparison to a single media filter. High filtration rates were
20 shown to transport solids, such that particle retention and headloss development was
21 distributed across the entire depth of the multi-media filter. There was also a progressive
22 decrease in the suspension particle size leaving each of the filter layers. The particle

- 23 hydrodynamic force simulation was consistent with the changes in measured PSD through the
24 filter layers.

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25 Introduction

26 Granular media filtration is one of the oldest forms of treatment technology used in the
27 production of potable water and is still widely used due to its reliability and low cost (Burton
28 et al., 2003; Han et al., 2009; Kim et al., 2012). However, the filtration of wastewater
29 secondary effluent is a relatively recent practice in situations that demand high water quality.
30 This includes tertiary treatment of wastewater for water reuse in water stressed areas
31 (Bloetscher et al., 2014; Christou et al., 2014; Ho et al., 2011), or to meet the standards
32 required for discharge to sensitive water courses and drinking water protected areas (Defra,
33 2012).

34 Granular media filtration removes suspended solids and colloidal particles, which includes
35 particulate biochemical oxygen demand (BOD), chemical oxygen demand (COD), microbes
36 and other suspended chemical contaminants from wastewater secondary effluent (Illueca-
37 Munoz et al., 2008). Removal of solids is also necessary prior to chemical and UV
38 disinfection that may be used for wastewater reclamation (Lazarova et al., 1999; Williams et
39 al., 2007) by reducing shielding of viruses by solid particles (Kirkpatrick et al., 1986). In the
40 UK, tertiary filtration of wastewater secondary effluent is usually necessary in
41 environmentally sensitive areas where tight regulatory discharge requirements are needed.
42 Tertiary treatment is therefore becoming more common to safeguard public health as well as
43 to minimise pollution (Ho et al., 2011; Langenbach et al., 2010; Li et al., 2012).

44 Filtration of wastewater is significantly more challenging than for potable water due to the
45 higher solid loads, much of which is organic in nature. To illustrate, the average influent
46 turbidity to a drinking water works filtration system is typically around 1 NTU with
47 occasional spikes up to 8 NTU (Zouboulis et al., 2007). However, secondary effluents
48 typically have turbidity between 5 to 20 NTU (TSS 10-40 mgL⁻¹) which causes rapid

49 headloss development in most conventional mono-media filters (Aronino et al., 2009; Lander,
50 1994). Aronino et al. (2009) observed cake formation on a single media depth filter treating
51 wastewater secondary effluent and while the filter was effective for virus removal, the
52 headloss build up was rapid. The increase in normalised headloss (NHL) per filtered volume
53 was $1.65 \text{ (m}^3\text{/m}^2\text{)}^{-1}$ at a filtration rate of 5 mh^{-1} . Rapid headloss development shortens the
54 filter runs and hence results in a low product water throughput before backwash is necessary.

55 One of the reasons for rapid headloss development in conventional mono-media filters is
56 because the backwash cycle leads to media stratification, with small media grains at the top
57 and large grains at the bottom (Baruth, 2005). The stratified arrangement leads to
58 accumulation of the solids in the top layer in the subsequent filter cycle and hence results in
59 underuse of the rest of the filter depth for solid retention. One proprietary mono-media filter
60 (the Tetra filtration system) overcomes this through the use of coarse media of uniform size
61 to discourage size stratification and also to promote deep penetration of solids (Crittenden et
62 al., 2012). Use of coarse media, however, has a disadvantage in that it reduces surface area
63 for particle capture. This may be overcome by operating the filter in an up-flow
64 configuration, which has been shown to provide greater particle deposition (Chrysikopoulos
65 and Syngouna, 2014). However, down-flow multimedia filters benefit from the use of both
66 large and small media grains, using large grains of low density media and small grains of
67 dense media. Such a design enables the backwash to stratify the filter bed keeping large
68 grains at the top and small grains at the bottom; hence encouraging deep penetration of solids
69 and improved removal performance with depth. This counters some of the operational
70 problems associated with single media filters offering the opportunity for such filters to
71 operate longer and at increased hydraulic loading therefore retaining more solids. In this
72 research a quadruple media filter was studied consisting of layers of anthracite, flint, alumina
73 and magnetite, moving from large to small grain size from top to bottom.

74 Previous studies involving granular media filters have investigated hydraulic loading rates
75 (HLRs) up to 25 mh^{-1} (Williams et al., 2007; Li et al., 2012; Cleasby et al., 1962; Suthaker et
76 al., 1995), rates typical of rapid gravity filters. Pressure filters have the capacity to operate at
77 a higher rate (Tobiason et al., 2011). However, there is a paucity of information on particle
78 capture when pressure filters operate at high HLRs. Operating the filter at higher rates is a
79 cost effective means to increase throughput for the same area of filter bed. The aim of this
80 research was to therefore investigate the effect of high hydraulic loading rate on the solids
81 removal efficiency of a quadruple media filter treating wastewater secondary effluent. The
82 contribution of each media layer was evaluated and the change in treated water particle size
83 distribution (PSD) was assessed through each media layer.

84 **Materials and Methods**

85 *Filtration tests*

86 The investigation was carried out using a pilot plant located at a small sewage treatment
87 works (STW) in the United Kingdom, filtering real secondary treated wastewater effluent.
88 The STW treats $2,500 \text{ m}^3\text{d}^{-1}$ of municipal wastewater using preliminary screening and grit
89 removal, primary sedimentation, alum dosing, trickling filters and secondary sedimentation.
90 Secondary effluent from the STWs discharge well was pumped to a mixed holding tank from
91 where the feed was transferred to the filter rig (Figure 1). The quadruple media filter pilot
92 plant was adapted using the same media layers as used in a commercial filter system
93 (FilterClear, Bluewater Bio, UK). For the purpose of this study, the media were separated
94 into different columns and connected in series so that the effect of each layer could be
95 isolated. In the pilot plant, transfer between the layers had a retention time of less than 2
96 minutes, and particle size analysis confirmed that particle characteristics were not changed
97 during transfer from one filter layer to the next. Wastewater was pumped from a holding tank

98 to the filter columns by a variable rate peristaltic pump (620 Industrial LoadSure, Watson
99 Marlow, UK) through a flowmeter (SM6000, IMF Electronic Ltd, Germany). The filter rig
100 consisted of four clear acrylic perspex columns of 700 mm height and 74 mm internal
101 diameter. The columns were connected using PVC fittings and a clear PVC hose. Filter
102 nozzles (Type KRI, KSHFisher, Germany) were fitted at the base of the columns to hold the
103 filter media in place and evenly distribute the flow during the backwash cycle. The columns
104 were connected so that the outlet of one column was fed into the inlet of the next.

105 Each column contained a different media at a depth of 100 mm. The media were anthracite
106 (effective size, ES =1.12 mm, uniformity coefficient, UC =1.49, loose bed porosity, $\epsilon_0 = 0.51$,
107 sphericity, $\psi = 0.54$), flint (ES=0.55 mm, UC =1.42, $\epsilon_0 = 0.52$, $\psi = 0.64$), alumina (ES=0.58
108 mm, UC =1.13, $\epsilon_0 = 0.55$, $\psi = 0.63$) and magnetite (ES =0.26 mm, UC =1.54, $\epsilon_0 = 0.47$, $\psi =$
109 0.84) respectively. A standard method was used to obtain the media effective size and
110 uniformity coefficient (American Society for Testing and Materials (ASTM) C136-2006).
111 The loose bed porosity ϵ_0 was determined by method ASTM C1252-2006 and the sphericity
112 ψ was determined by calculations based on clean bed headloss measurement and the Kozeny-
113 Carmen equation.

114 Online instruments for flow, pressure and turbidity were connected to the filter rig and the
115 output analogue signals were logged into a laptop by an analogue-digital data logger (D-149,
116 Dataq Instruments, UK). The columns were fitted with pressure transducers (PN2026, IMF
117 Electronic Ltd, Germany) at the bottom and top of each media bed (100 mm apart) to
118 measure the pressure drop across the filter bed. Sampling points were positioned at the
119 influent and effluent to each column. The influent and effluent turbidity was monitored by
120 probes placed in the influent holding tank and the effluent pipe (Turbi-Tech 2000LS and
121 WaterWatch 2310, Partech, UK, respectively). The filter was run at a determined constant

122 flow rate (from 5 to 60 m h^{-1}) for each filter run and grab samples were collected on an hourly
123 basis for analysis. Each flow rate condition was run in triplicate. At the end of the filter run,
124 the columns were backwashed individually by an air scour (2 minutes) followed by high rate
125 (60 m h^{-1}) water wash (10 minutes) using the filtrate. As each filter column could be isolated,
126 it was not possible for the different media layers to mix with one another during filter
127 backwash.

128 [FIG 1 HERE]

129 *Performance Measurements*

130 The total suspended solids (TSS) were determined from grab samples by gravimetric analysis
131 Method 290D (APHA, 2005). Turbidity was measured in the laboratory using a turbidity
132 meter (2100 Lab Turb, Hach, US). Zeta potential was measured by a zetasizer (Zetasizer
133 Nano ZS, Malvern, UK). During sampling, the opening and closing of the sampling taps was
134 carried out slowly to avoid hydraulic shocks in the system. The PSD of suspension particles
135 was measured using a laser diffraction particle sizer (Spectrex PC-2200, Spectrex
136 Corporation, California) within 30 minutes of sampling to minimize aggregation. The grab
137 samples were diluted by a factor of 12 to reduce the effect of particle shielding at high
138 concentrations.

139 *Filtration models*

140 Filtration was modelled using colloid filtration theory to show the effect of HLR on the
141 retention of suspension particles by collectors, an approach used in drinking water filtration,
142 but not to our knowledge in wastewater filtration. Filtration models have been defined
143 assuming laminar flow conditions (Tobiason et al., 2011). To show that the filtration systems

144 used in this work was operating under laminar conditions, the Reynolds number was
145 calculated from

$$\text{Re} = \frac{\rho_w u d_{eq}}{\mu} \quad (1)$$

146 Where ρ_w is the water density, u is the superficial velocity, d_{eq} is the media equivalent
147 diameter and μ is the dynamic viscosity. $\text{Re} < 1$ relates to Darcy flow, $1 < \text{Re} < 100$ is
148 Forchheimer flow, $600 < \text{Re} < 800$ is transitional flow and $800 < \text{Re}$ is considered fully
149 turbulent flow (Crittenden et al., 2012). In this study HLR of 5-60 mh^{-1} were investigated for
150 which the Reynolds numbers for each media in the respective flow range were anthracite (2.2
151 $< \text{Re} < 26.4$), flint ($0.9 < \text{Re} < 11.2$), alumina ($0.9 < \text{Re} < 11.4$) and magnetite ($0.6 < \text{Re} <$
152 6.7). These Reynolds numbers were within the Darcy and Forchheimer flow regimes which
153 are considered steady laminar flow and hence in the range where fundamental filtration
154 models can be applied. These models, however, do not address the hydrodynamic variability
155 in flow and the effect on streamlines introduced by the use of angular media (Crittenden et
156 al., 2012). This was therefore an important element of investigation for this study.

157 HLR is a major factor affecting both particle deposition and detachment in filtration (Bai et
158 al., 1997). The particle deposition rate was calculated from the single collector transport
159 efficiency η and attachment efficiency α (Yao et al., 1971). The contact/transport efficiency is
160 the rate at which approaching suspension particles contact the collector. This has been
161 described analytically (Yao et al., 1971) and through regression analysis of numerical
162 simulation data (Tufenkji et al., 2004; Rajagopalan and Tien, 1976) and takes into account
163 the suspension hydrodynamics (Lander, 1994). The retention of particles (attachment
164 efficiency) on collectors has mainly been explained in terms of the chemical interactions and
165 adhesive forces such as the double layer forces and the London-van der Waals forces (Stumm

166 and Morgan, 1996; Tien, 2000), however the hydrodynamic conditions also have a strong
 167 influence on whether the particles are retained on collectors (Torkzaban et al., 2007).
 168 Adhesive forces depend on the physicochemical characteristics of the particles and media and
 169 are therefore independent of HLR. High HLR increases the hydrodynamic scouring force and
 170 can impair the retention of particles in the filter. The quadruple media filter has a tapered
 171 void; as such the channels between the collectors narrow down the bed, bringing particles
 172 nearer to the collectors hence increasing the chance of being captured. However
 173 hydrodynamic forces may also change in each media layer due to different bed porosities
 174 between layers. This investigation therefore explored the change in HLR and its direct
 175 influence on the hydrodynamic forces in each layer. The model demonstrated how
 176 hydrodynamic forces impact on the retention of particles on collectors and to demonstrate the
 177 change in suspension particle size changes through the media layers.

178 *Hydrodynamic Forces*

179 Particles near collectors are subject to hydrodynamic forces. Since the suspension particles
 180 are much smaller than the media grain, they can be modelled as small spheres on a collector
 181 plane (Bai et al., 1997). The hydrodynamic force acting on the particles can be resolved to
 182 two components, the hydrodynamic lifting force (F_l) (normal to the plane of the collector)
 183 and the hydrodynamic drag force (F_{Hydro}) (tangential to the collector) from Tien and Ramarao
 184 (2007). The hydrodynamic lifting force is given by:

$$F_l = k_l d_p^3 (\mu \gamma)^{-0.5} \left(3\mu \frac{A_s}{d_m} \frac{u}{\varepsilon_0 - \sigma} \right)^{1.5} \quad (2)$$

185 Where k_l is the coefficient for lifting force, d_p is the suspended particle diameter, d_m is the
 186 filter media diameter, μ is the dynamic viscosity, ν is the kinematic viscosity, σ is the bulk
 187 specific deposit, ε_0 is the clean bed porosity, u is the filtration velocity and the porosity-

188 dependent parameter based on the Happel's flow model, A_s is defined as $2(1-p^5)/w$, and $w=2-$
 189 $3p+3p^5-2p^6$, $p= (1-\varepsilon)^{1/3}$. The lifting force acts in the same plane as the adhesion forces
 190 between the particle and the media; it is assumed to be the force causing the particle to drift
 191 away from the collector if it detaches (Tien and Ramarao, 2007). The hydrodynamic drag
 192 force on a particle is the component of the hydrodynamic force along the collector plane
 193 given by:

$$F_{Hydro} = 2.551 \times 3\pi\mu \frac{A_s}{d_m} d_p^2 \frac{u}{\varepsilon_0 - \sigma} \quad (3)$$

194 The hydrodynamic drag force has an effect of either sliding or rolling the particle along the
 195 collector depending on its point of action on the particle. This displacement is resisted by a
 196 sliding frictional force (F_f) calculated as:

$$F_f = k_f \frac{6(1-\varepsilon_0)}{d_m} \frac{Hd_p}{12\delta^2} \quad (4)$$

197 Where k_f is the sliding friction coefficient, H is the Hamaker constant and δ is the particle-
 198 media separation distance. The coefficient k_f may also be the rolling friction coefficient if the
 199 mechanism of particle motion is rolling instead of sliding (Bergendahl and Grasso, 2003).
 200 Both the hydrodynamic drag force and the sliding frictional force act tangentially to the
 201 collector, such that the net tangential force (F_T) is given by $F_T = F_f - F_{Hydro}$. The
 202 hydrodynamic drag force increases with filtration rate while the frictional force is
 203 independent of the filtration rate.

204

205

206

207 **Results and Discussion**

208 *Turbidity and TSS measurement*

209 The wastewater influent to the filter had the following characteristics: TSS = 21 ± 2 mgL⁻¹,
210 turbidity = 10.2 ± 0.9 NTU, temperature = 20 ± 2 °C and pH = 7.6 ± 0.3 . The influent particles
211 had a d(0.5) size of 20 µm. Wastewater TSS was linearly correlated to turbidity with a
212 gradient of 2.3 mgL⁻¹NTU⁻¹ (root mean square fit of 0.7), this fits well with previously
213 published data for secondary effluent having gradients of 2-2.4 mgL⁻¹NTU⁻¹ (Burton et al.,
214 2003). The TSS removal versus turbidity removal efficiency correlates with a gradient of
215 0.78 (root mean square fit of 0.8). This comparison of removal efficiency shows that TSS
216 removal efficiency was slightly less than turbidity removal efficiency since unlike turbidity,
217 the TSS is insensitive to the contribution of very small particles that might pass through the
218 filter paper. In this study turbidity was chosen over TSS measurement to evaluate the removal
219 of suspended solids since turbidity can better detect small changes in solids concentration,
220 particularly for the small particles in the system and because it was easier to obtain more data
221 from online turbidity monitors. Williams et al. (2007) also found the removal of turbidity to
222 be a representative measure of particle and bacteria removal and hence a good indicator of
223 the overall filter performance.

224 *Overall filter performance*

225 Throughout the study, the influent wastewater turbidity was kept at 10.2 ± 0.9 NTU. The
226 average effluent turbidity increased from 1.9 ± 0.1 NTU at 5.0 mh⁻¹ to 6.8 ± 0.5 NTU at 62.7
227 mh⁻¹; resulting in removals of 80 and 40% respectively for the quadruple filter (Figure a). The
228 filter operated effectively throughout the duration of the experimental programme, with a
229 stable effluent quality observed during each filter run of 8 hours. No inter-mixing of media
230 was observed following backwashing, the media remained structurally stable and no

231 accumulation of solids or mud-balling was observed in the filters. The turbidity removal
232 efficiency decreased almost linearly with increasing HLR. The turbidity removal results were
233 compared with literature wastewater filtration removal for increasing HLR (2a). To facilitate
234 comparison, the gradients of linear regression fits were used to demonstrate the change in
235 turbidity removal per unit change in HLR (measured as $\%m^{-1}h$). For single media sand filters
236 the suspended solid removal efficiency reduced by $4.4 \%m^{-1}h$ for an initial influent turbidity
237 of 35 NTU when the HLR changed from 5 to $10 mh^{-1}$ (Li et al., 2012). A separate study saw
238 reductions of $3.9 \%m^{-1}h$ for an initial turbidity of 10 NTU when the HLR increased from 5 to
239 $15 mh^{-1}$ (Yu et al., 2015). In an anthracite-sand dual-media filter removal reduced by 1.25
240 $\%m^{-1}h$ for an initial turbidity of 6.5 NTU and the HLR increased from 12.2 to $24.4 mh^{-1}$
241 (Williams et al., 2007). In the present study, the quadruple-media filter had turbidity removal
242 reducing by $0.67 \%m^{-1}h$ for an initial influent turbidity of 10.2 NTU with HLR increasing
243 from 5 to $60 mh^{-1}$. Hence the increase in HLR has a greater impact on the filter removal
244 efficiency for single media filters than for dual media filters. The impact was even less for the
245 quadruple filter used here, demonstrating the smallest deterioration in effluent quality with
246 increasing HLR was seen for the quadruple filter, even though the HLR was also over a much
247 wider range. This comparison shows that increasing the number of filter layers buffers the
248 effect of the increased HLR hence giving more robust filter performance.

249 In this study the removal efficiency of the top (anthracite) layer decreased quickly from 58 to
250 40% between $5 mh^{-1}$ and $10 mh^{-1}$, a reduction of $3.5 \%m^{-1}h$ (Figure 2c), a value similar to the
251 literature values seen for a single media filter ($4.4 \%m^{-1}h$ in Li et al. (2012) and $3.9 \%m^{-1}h$ in
252 Yu et al. (2015)). The quicker change in removal efficiency across a single layer such as may
253 be seen in conventional sand filters may be one of the key reasons why there has been
254 reluctance to increase HLRs in conventional mono-media filters. There have been attempts to
255 buffer the effect of increasing HLR on removal efficiency by increasing the coagulant dose or

256 changing the filter bed depth which works to some extent, but has the downside of quickly
257 raising the filter headloss (Lawler and Nason, 2006). In this study, the impact became less
258 abrupt for the combined anthracite and flint layers ($2.1 \%m^{-1}h$), for the combined anthracite,
259 flint and alumina ($1.7 \%m^{-1}h$) and for the quadruple filter ($1.2 \%m^{-1}h$) in the HLR range 5 to
260 $10 mh^{-1}$, showing the moderation that the additional layers have when the HLR was increased
261 (Figure 2c).

262 Increasing HLR was observed to significantly affect the particle sizes exiting the filter.
263 Analysis of the 10th, 50th and 90th percentile particle size showed that while influent particle
264 size was consistent, the effluent particle sizes increased with the HLR (Figure b). This shows
265 that retention of large particles became harder at high HLRs. Increasing the HLR also had the
266 consequence of raising both the clean bed and filtration headloss due to increased frictional
267 forces (Figure 2d). The NHL increase during a filter run was proportional to the mass
268 deposition (specific deposit) and hence was a measure of mass retention (Mays et al., 2005).
269 The NHL increase was calculated as $(\Delta H - \Delta H_0) / \Delta H_0$ where ΔH is the filtration headloss and
270 ΔH_0 is the clean bed headloss. The increase in NHL rose with filtered volume at all HLRs
271 (Figure 2d); however the rates of change (slopes of fitting lines) did not change significantly
272 ($0.0042-0.0164 m^{-3}m^2$) compared to the large change in HLRs. This was because while high
273 HLR leads to a high solids loading to the filter, the solids removal efficiency reduced at high
274 flow rates (Figure 2a) such that fewer solids were retained per filtered volume. Therefore, the
275 rate of increase in NHL remains low at high HLRs making filter operation possible under
276 such conditions.

277 [FIG 2 HERE]

278

279

280 ***Individual filter layer performance***

281 Each media layer contributed differently to the removal of solids. As wastewater particles
282 penetrate down through the filter, the larger particles are removed and the overall solids
283 concentration decreases. Therefore, the bottom filter layers receive particles that were not
284 removed upstream or that have been detached from layers above. Solids removed by each
285 layer also depended on the HLR. For example there was high removal efficiency for
286 anthracite and flint (60% and 40% respectively) at flow rates of 5 mh^{-1} but much lower
287 removal efficiencies of 10% at high HLRs of 60 mh^{-1} (Figure 3). Anthracite received a
288 consistent turbidity influent at all different loading rates. The removal efficiency of the
289 anthracite layer demonstrated the profile of a typical single media filter with increasing
290 hydraulic loading (Figure 3a). Consequently the turbidity of the influent to the flint layer
291 increased with HLR (Figure 3b). With the increasing turbidity load and HLR, the removal
292 efficiency also decreased for the flint layer.

293 In contrast, the bottom two layers (alumina and magnetite) had removal efficiency which
294 started at 15% at low flow rates increasing to a maximum of 20% at 25 mh^{-1} for alumina and
295 40 mh^{-1} for magnetite before dropping with a further increase in flow rate (Figure 3c and d).
296 Although these media had comparatively lower solid removal efficiency, these layers receive
297 much lower suspended solids loads that contained a large number of hard to remove small
298 particles (Williams et al., 2007). The alumina and magnetite turbidity removal efficiency
299 initially improved because of the increased quantity of solids reaching these layers as the
300 HLR increased because of lower removal in upstream media layers. Raising the HLR
301 transported solids deeper into the filter bed, however high HLR also increased hydrodynamic
302 scouring which prevented further improvement in removal efficiency (discussed below).

303

304

[FIG 3 HERE]

305 The mass accumulation of solids in the filter per unit filter volume, termed specific deposit
306 (Crittenden et al., 2012) was examined for each media at different HLRs. The suspended
307 solids for specific deposit calculation was approximated by multiplying the turbidity
308 measurements by the conversion factor of $2.3 \text{ mgL}^{-1}\text{NTU}^{-1}$ (from the regression line as
309 discussed earlier). At low HLRs, most solids were retained on the anthracite layer (Figure 4).
310 As the HLR increased, the specific deposit also increased due to the increased solid loading
311 rate, but the continued rise was halted by the increased hydrodynamic scouring that limited
312 the retention of solids. In anthracite and flint, the specific deposit rose up to a HLR of 25 mh^{-1}
313 and then became constant with further increases in HLR (Figure 4a and b). In the alumina
314 layer, the specific deposit increased to a maximum at 30 mh^{-1} , then dropped with increasing
315 HLR (Figure 4c). The specific deposit in the magnetite layer continued to increase through
316 the HLRs investigated, a feature that gives the filter added resilience (Figure 4d). As the HLR
317 increased, the solids reaching downstream layers increased hence the improved solid
318 retention of downstream layers.

319 For each filter run, increasing solid retention resulted in an increase in headloss through the
320 filter bed (Veerapaneni and Weisner, 1997). The NHL change for the media layers of the
321 quadruple media filter at different HLRs was quite different for each layer (Figure 4). The
322 variation of HLR in this study was thought to affect the NHL change with solids retention in
323 three main ways: (1) increased flow resistance due to increased friction at higher filtration
324 velocity; (2) the differences in the compactness of solid deposits at different HLR
325 (Veerapaneni and Weisner, 1997), and (3) the size of solids reaching each layer. For HLR up
326 to 30 mh^{-1} , an increase in HLR was coupled by an increase in the flow resistance through the
327 porous media hence an increase in the NHL was observed (Tien and Ramarao, 2007).

328 Previous work has also shown that large particle deposits are more compact than deposits
329 from small particles (Veerapaneni and Weisner, 1997). Here, the anthracite layer received
330 large particles with a concurrent low increase in NHL, perhaps as a result of more compact
331 deposits filling the large pores to a much lower degree than expected and hence providing
332 less resistance to flow (Figure 4a). In comparison, the downstream layers had higher NHL
333 increase since the the smaller pores received less compact particles that filled the pore space
334 compariatively more than for the upper layers. This effect was particularly noticeable at the
335 low range of HLR ($<15 \text{ mh}^{-1}$) investigated in this work (Figure 4b, c, d). For HLR of 40 mh^{-1}
336 and above, a mich higher rate in NHL was expected than was observed (Figure 4). However,
337 this was not seen in this work and may be explained by the differences in compactness of
338 solid deposits with increasing HLR (Veerapaneni and Weisner, 1997). While there are
339 differences in compactness of solids for different particle sizes, there are also differences in
340 partcile compactness with increasng filtration veolcity. Solids deposited at low HLR have a
341 tendency to form more open deposits that occupy more pore space when compared to solids
342 at high HLR (Veerapaneni and Weisner, 1997), hence there is a significant NHL increase for
343 a relatively low specific deposit (Figure). At high HLR ($>40 \text{ mh}^{-1}$), the NHL would be
344 expected to increase. At high HLR, small solids formed compact deposits which occupied
345 less pore space within the porous media hence moderating the headloss increase. For
346 example, in the alumina layer, the NHL remained fairly stable while the specific deposit was
347 rising with HLR in the alumina layer due to the solids being deposited compactly at high
348 HLR (Figure 4c). Similar observations were seen in the anthracite, flint and magnetite layers
349 at high HLR where the NHL did not increase appreciably.

350 The specific deposit and headloss development of the quadruple media filter occurred in all
351 the media layers (Figure), therefore the entire depth of the filter was utilised for solids
352 storage. High HLR was also seen to increase the deposition of solids in the downstream

353 layers as it caused solids to penetrate deeper into the bed (Kau and Lawler, 1995). The
354 utilization of the entire filter depth for solid storage ensured a slow overall headloss
355 development enabling the quadruple filter to be operated at high HLRs, a feature that would
356 not be operationally possible in single media filters.

357 [FIG 4 HERE]

358 *Particle size analysis*

359 Further support for the changes in the removal efficiencies and headloss development
360 observed in this study were made by examining the changes in the PSDs with filter depth and
361 at different HLRs. The wastewater particle sizes decreased at each stage of the filter for all
362 HLRs; an example of the PSD through each filter layer has been shown for an HLR of 5 mh^{-1}
363 (Figure 5a). The influent PSD remained unchanged throughout all the filter runs while the
364 effluent sizes were observed to increase when the HLR rose (Figure b). Therefore when the
365 filter was run at higher HLRs, the particle sizes passing through the filter gradually increased,
366 for example, the median particle size $d(50)$ in the filter effluent was $6.5 \mu\text{m}$ at 5 mh^{-1} ,
367 increasing to $15 \mu\text{m}$ at 60 mh^{-1} (Figure b).

368 One of the surprising observations seen in this work was the appearance of some large
369 particles in the filtered water. To demonstrate, the presence of 3 classes of particles in the
370 final filtered water that were $>15 \mu\text{m}$ were seen (Figure 5c). As can be seen, there was a
371 significant increase in the presence of larger particles with increasing HLR. For example, at 5
372 mh^{-1} , more than 95% of solids $>15 \mu\text{m}$ were removed, while at 60 mh^{-1} , this had reduced to
373 30% removal of solids that were between 15-30 μm and only 75% removal of solids between
374 50-100 μm .

375 To analyse the trend in turbidity and particle removal efficiency further, comparison was
376 made to removal predicted from filtration models from Tufenkji and Elimelech (2004)
377 (commonly called the TE model) (Figure d). The TE model parameters were assumed as:
378 attachment efficiency $\alpha = 1$; suspension particle density $\rho_p = 1.05 \text{ kgm}^{-3}$; $\rho_w = 998 \text{ kgm}^{-3}$ at
379 temperature $T = 20 \text{ }^\circ\text{C}$; the Hamaker constant $H = 10^{-20} \text{ J}$; and the transport efficiency η was
380 calculated from media characteristics defined in the materials and methods section.
381 Favourable attachment ($\alpha = 1$) was assumed for all particle sizes in the wastewater, following
382 Tufenkji and Elimelech (2004). In the present research this was justified given the low
383 magnitude of the charge on the wastewater particles (zeta potential between -10 and -12mV),
384 indicative of particle destabilization. The TE model predicted near complete removal of
385 particles $>15 \text{ }\mu\text{m}$, while $10 \text{ }\mu\text{m}$ particles were also very well removed across all HLRs
386 (Figure d). Smaller particles were modelled to be progressively more poorly removed. For
387 example at 20 mh^{-1} , $5 \text{ }\mu\text{m}$ particles were removed by 50% while $1 \text{ }\mu\text{m}$ particles were removed
388 by only 28%. There was therefore a discrepancy in the predictions of the filtration model with
389 the observed presence of larger particles in the filtrate, particularly with an increase in HLR
390 above 20 mh^{-1} . It is proposed that the TE model overestimates the removal of large particles
391 by not accounting for particle detachment that might occur as a result of hydrodynamic forces
392 that become more and more relevant at high HLR (Crittenden et al., 2012). The effect of
393 hydrodynamic forces on the retention of particles is explored further in the next section.

394 [FIG 5 HERE]

395 *Impact of scouring on filter performance*

396 Further understanding of the filter performance was achieved by analysing the hydrodynamic
397 forces acting on particles in the filter bed as the HLR was changed. An increase in HLR
398 intensified the hydrodynamic scouring on deposited solids with a consequence of reducing

399 particle retention (Tobiason et al., 2011). The modelled net tangential force for a clean bed (σ
400 = 0) for increasing particle size and HLR shows that large particles are subject to greater
401 hydrodynamic forces and the forces differ in each filter media layer (Figure a), a similar
402 observation to that made by Bai and Tien (1997). The effect of hydrodynamic force is
403 therefore likely to be much greater in wastewater filtration where there is usually a greater
404 proportion of large particles to be filtered than is the case in drinking water filtration.

405 The frictional force component (F_f) of the net tangential forces acting on a particle attached to
406 a collector does not vary with HLR, however the hydrodynamic drag force (F_{Hydro}) increases
407 with HLR. The net tangential force becomes negative when the hydrodynamic drag force
408 exceeds the frictional force with the implication that the particle is liable to slide along the
409 collector or get fragmented, hence increasing the chance of detachment. A particle detaches
410 from the collector when the net tangential force exceeds the attachment forces between the
411 particle and collector. The differences in the force balance for particles being removed by
412 different media demonstrates the spatial variation that may be experienced by particles
413 attached to media of different physical structure.

414 At low HLR, the net tangential force is positive for all particle sizes (Figure) such that scour
415 plays little to no role in removing particles from collectors hence the high removal efficiency.
416 As the HLR increases, the net tangential force on particles becomes more negative with the
417 effect being much greater on large particles compared to small ones (Bai and Tien, 1997).
418 This is therefore consistent with the observed increase in average particle sizes exiting each
419 media layer (Figure b) and also the rising influent turbidities to flint, alumina and magnetite
420 layers (Figure 3b, c, d) as it became difficult to retain particles at high HLRs. The changes in
421 net tangential force with HLR were also different for each media layer because of the
422 different bed properties (media size and shape and the bed porosity) and the range of particles

423 received by each media layer (Figure a). Although the surface plots illustrate the forces that
424 would be experienced by a range of particles (0-90 μm), the very negative net tangential
425 forces that might be experienced by larger particles ($>50 \mu\text{m}$) in the lower filter layers, would
426 not be seen in practice because the upper layers would have removed and retained these
427 particles (Figure a).

428 To investigate the effect of the net tangential force acting on particles in relation to the
429 particles observed to leave each filter layer in this study, the critical particle sizes reaching
430 each layer were examined. For the average influent particle size of 20 μm going on to the
431 anthracite layer, the scouring model predicts that these particles would be dislodged at an
432 HLR of 27 mh^{-1} (point A1 in Figure 6b). Observations were very close to this predicted
433 value, where the median particle size seen in the anthracite effluent was 15 μm (Figure b).
434 For 15 μm particles reaching the flint layer, the model predicted these particles would be
435 dislodged at 38 mh^{-1} (point A2 in Figure b), identical to what was observed at this HLR
436 (Figure b). Similarly, 12 μm particles reaching both alumina and magnetite would potentially
437 be dislodged at 57 mh^{-1} (point A3) and 38 mh^{-1} HLR respectively (Figure b). The observed
438 results agree very closely as the median particle size leaving the filter layers at both HLR
439 were approximately 12 μm in diameter (Figure b). The anthracite layer reached the critical
440 force first as it was the largest media and received the largest particles (Bai and Tien, 1997).
441 The removal efficiencies of alumina and magnetite were observed to drop for HLR beyond
442 40 mh^{-1} thus indicating a point where the buffering effect produced by the additional layers
443 began to fall (Figure c and d), a HLR similar to what the model predicted for flint and
444 magnetite. The specific deposit was also observed to drop after the critical HLR was reached
445 for each layer (Figure).

446 The hydrodynamic model was therefore successful in demonstrating the deviation between
447 the TE model and the observed results, the differences arising due to the scouring effect of
448 hydrodynamic forces at high HLRs. Wastewater has a significant amount of large particles
449 which are subject to larger detachment forces. The TE model does not account for
450 detachment of retained particles hence may therefore be more appropriate for modelling
451 drinking water filtration where the suspension particles are smaller and lower HLRs are
452 usually used.

453 [FIG 6 HERE]

454 **Conclusions**

455 The results from this work have shown that the impact of the increase in HLR for the
456 quadruple media filter was much less than for a single media filter as the system was buffered
457 by the additional layers moderating the loss of performance. High HLR transported solids
458 deeper into the filter bed hence the entire depth of the filter was used for solid storage,
459 ensuring the headloss was distributed to all media layers. The hydrodynamic model
460 successfully explained the observed solids removal and the PSD at changing HLR for the
461 quadruple filter treating wastewater secondary effluent. The hydrodynamic model also
462 explained the deviation of the TE Model from the observed results particularly at high HLR
463 by showing the effects of hydrodynamic scouring on particle retention. The implications of
464 this research are the possibilities of operating the quadruple media filter at high HLR (up to
465 40 mh^{-1}) to increase the throughput with a moderate impact on the effluent quality.

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471 Bluewater Bio Ltd for funding and permitting the use of their patent technology to carry out
472 this investigation.

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Nomenclature		$d(0.1)$	10 percentile particle size
F_{Hydro}	hydrodynamic drag force	$d(0.5)$	50 percentile particle size
F_l	hydrodynamic lifting force	$d(0.9)$	90 percentile particle size
F_f	Frictional force	ε_0	clean bed porosity
k_l	Coefficient of lifting force	ε	filter bed porosity
k_f	Coefficient of sliding friction	p	$(1-\varepsilon)^{1/3}$
d_p	suspension particle diameter	w	$2-3p+3p^5-2p^6$
d_m	filter media diameter	A_s	$2(1-p^5)/w$
d_{eq}	Media equivalent diameter	ρ_w	Density of water
H	Hamaker constant	ψ	Filter media sphericity
ΔH	Headloss	μ	dynamic viscosity
ΔH_0	Clean bed headloss	δ	particle-media separation distance
u	filtration flow velocity	σ	bulk specific deposit
ES	Effective size	η	transport efficiency
UC	Uniformity Coefficient	α	attachment efficiency
HLR	Hydraulic loading rate	NHL	Normalized headloss

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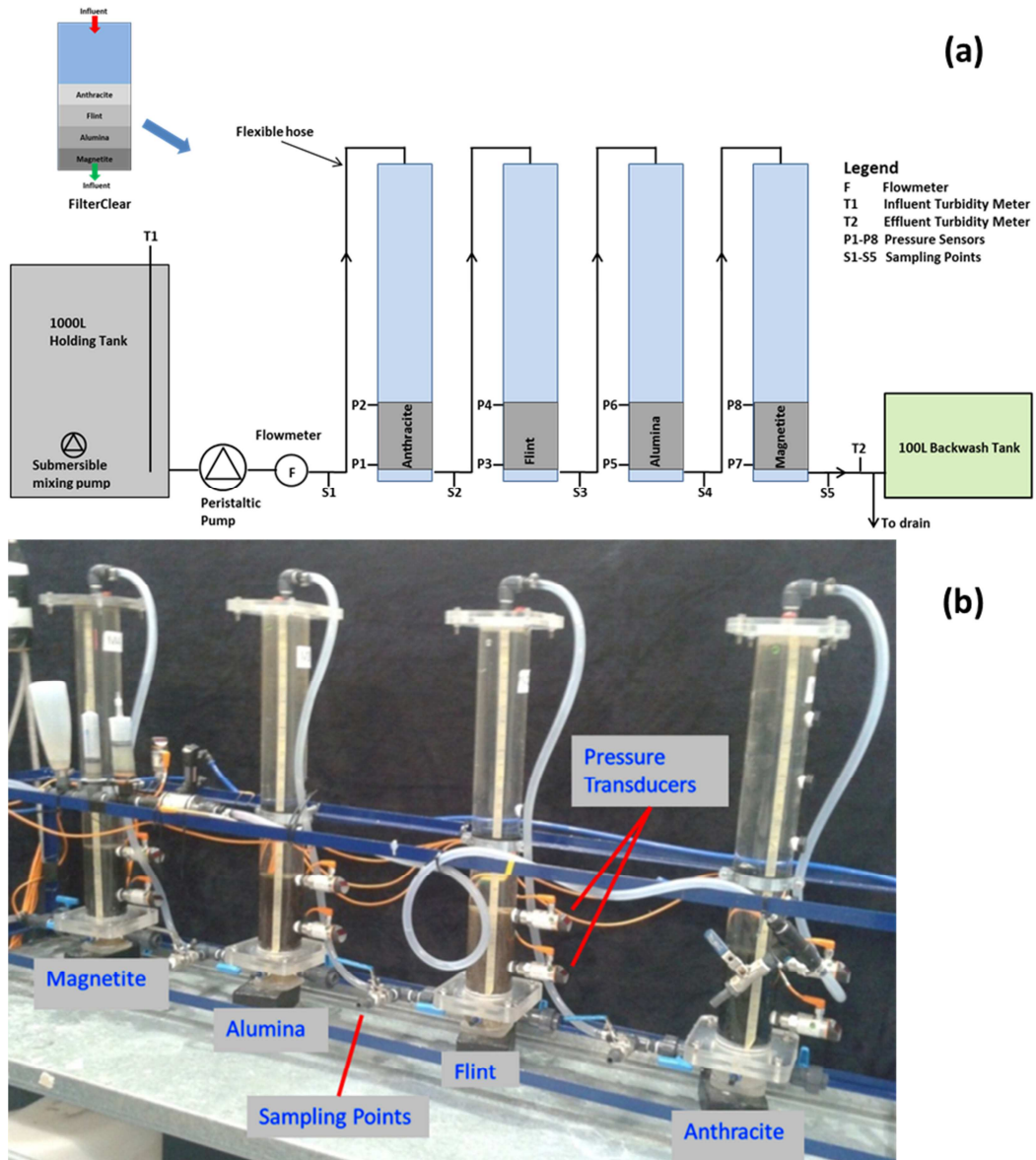
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581 Figure 1: (a) Schematic and (b) photograph of the pilot filter rig.

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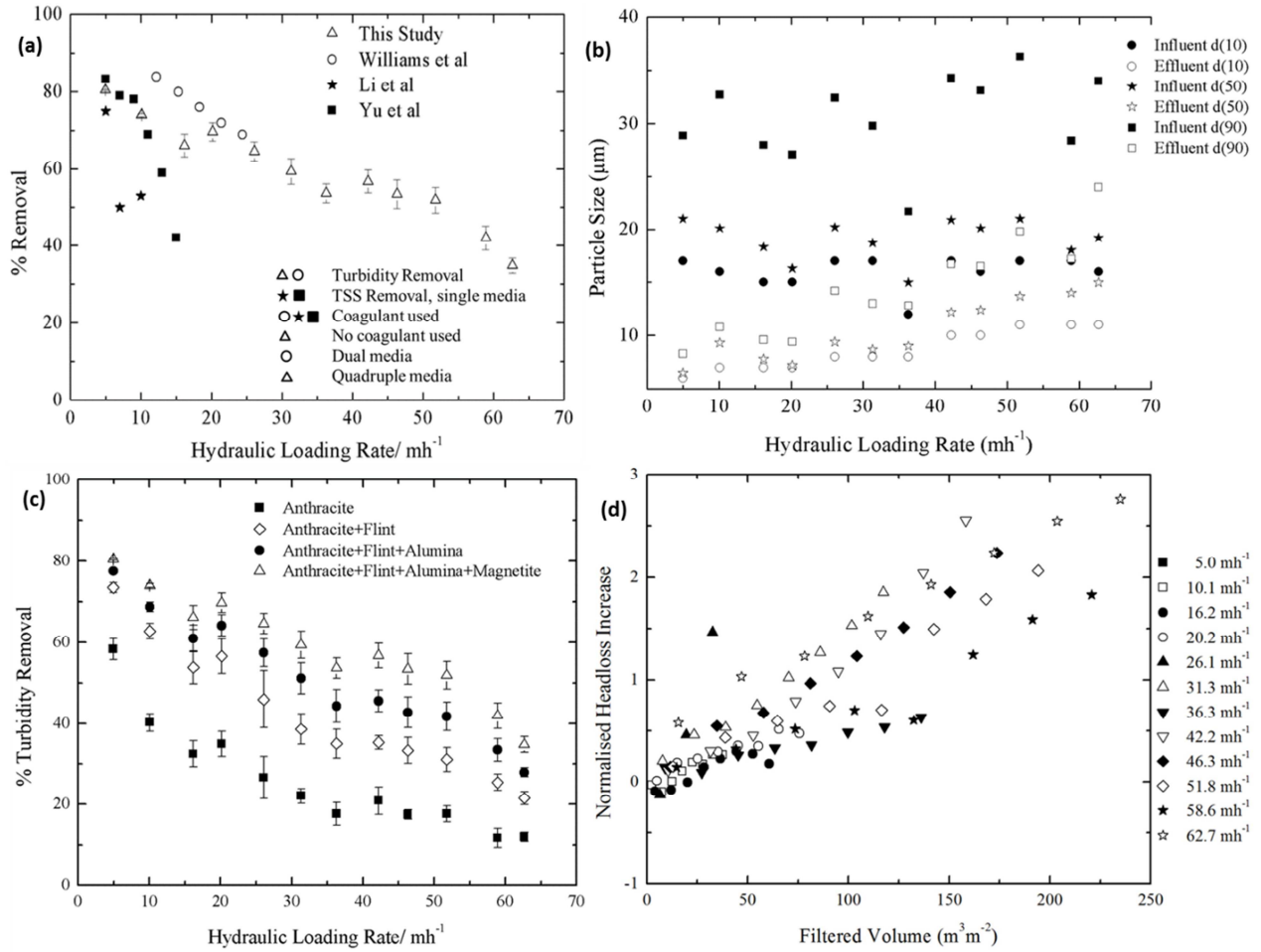
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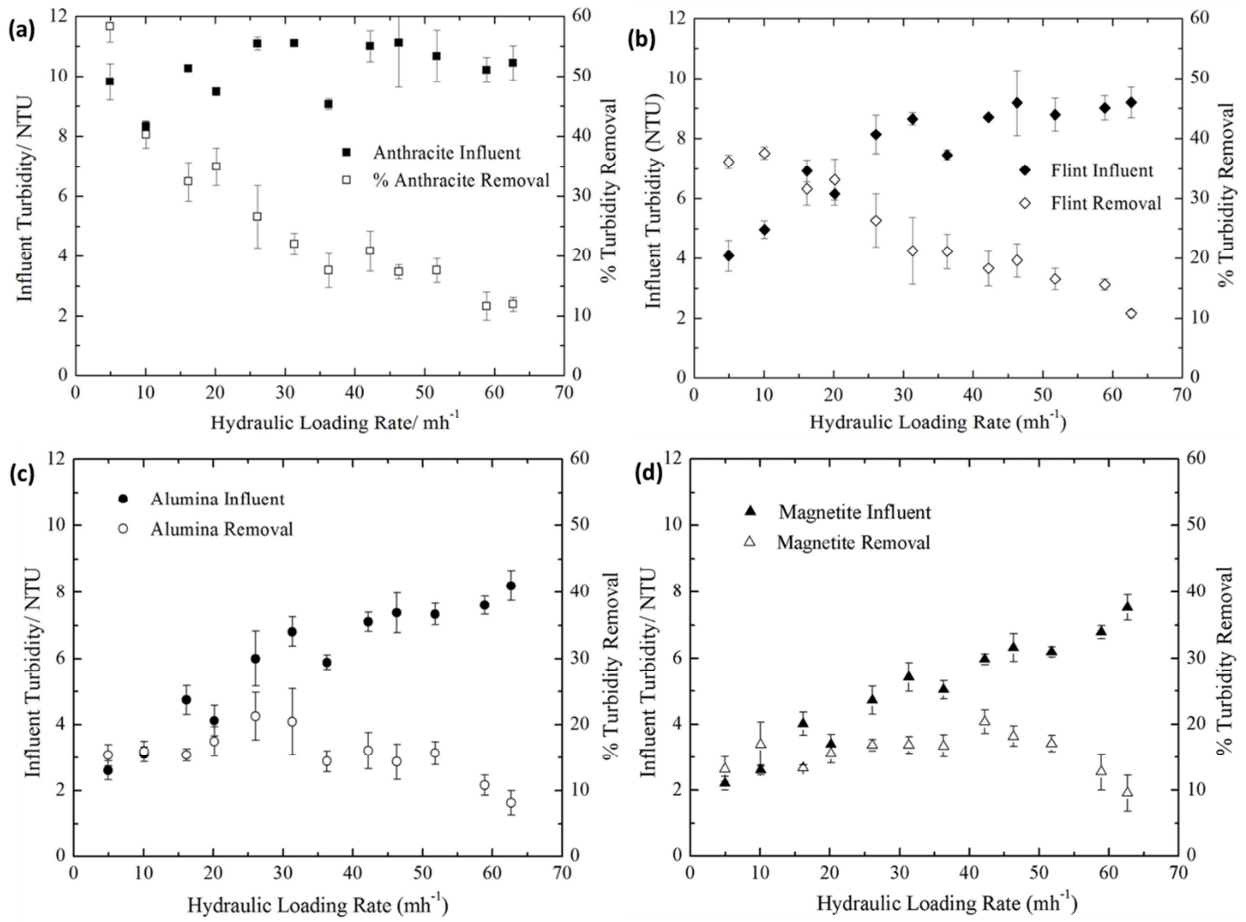
589 Figure 2: (a) Overall turbidity removal efficiency in this study and comparable data from
 590 previous studies, (b) $d(10)$, $d(50)$, $d(90)$ particle sizes for both the influent and effluent at
 591 different HLRs. (c) The impact of HLR on the average filter turbidity removal efficiency for
 592 the quadruple (anthracite, flint, alumina and magnetite) filter, tri-media (anthracite, flint and
 593 alumina) filter, dual-media (anthracite and flint) filter and the mono-media (anthracite) filter,
 594 (d) Change in NHL increase with filtered volume at different HLRs.

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600 Figure 3: Turbidity removal for each media at different HLRs and the turbidity influent to
 601 each layer.

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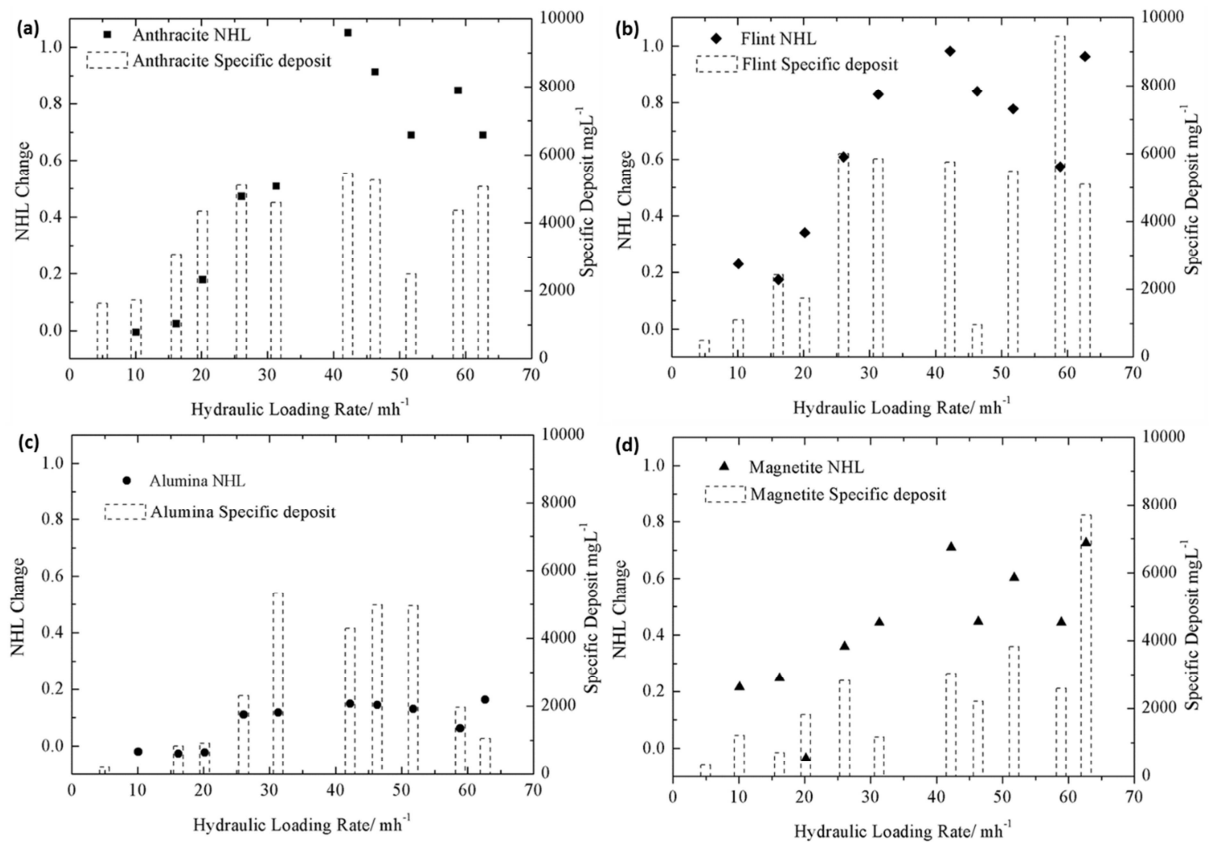
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611 Figure 4: NHL change and specific deposit at different filtration rates for the four media.

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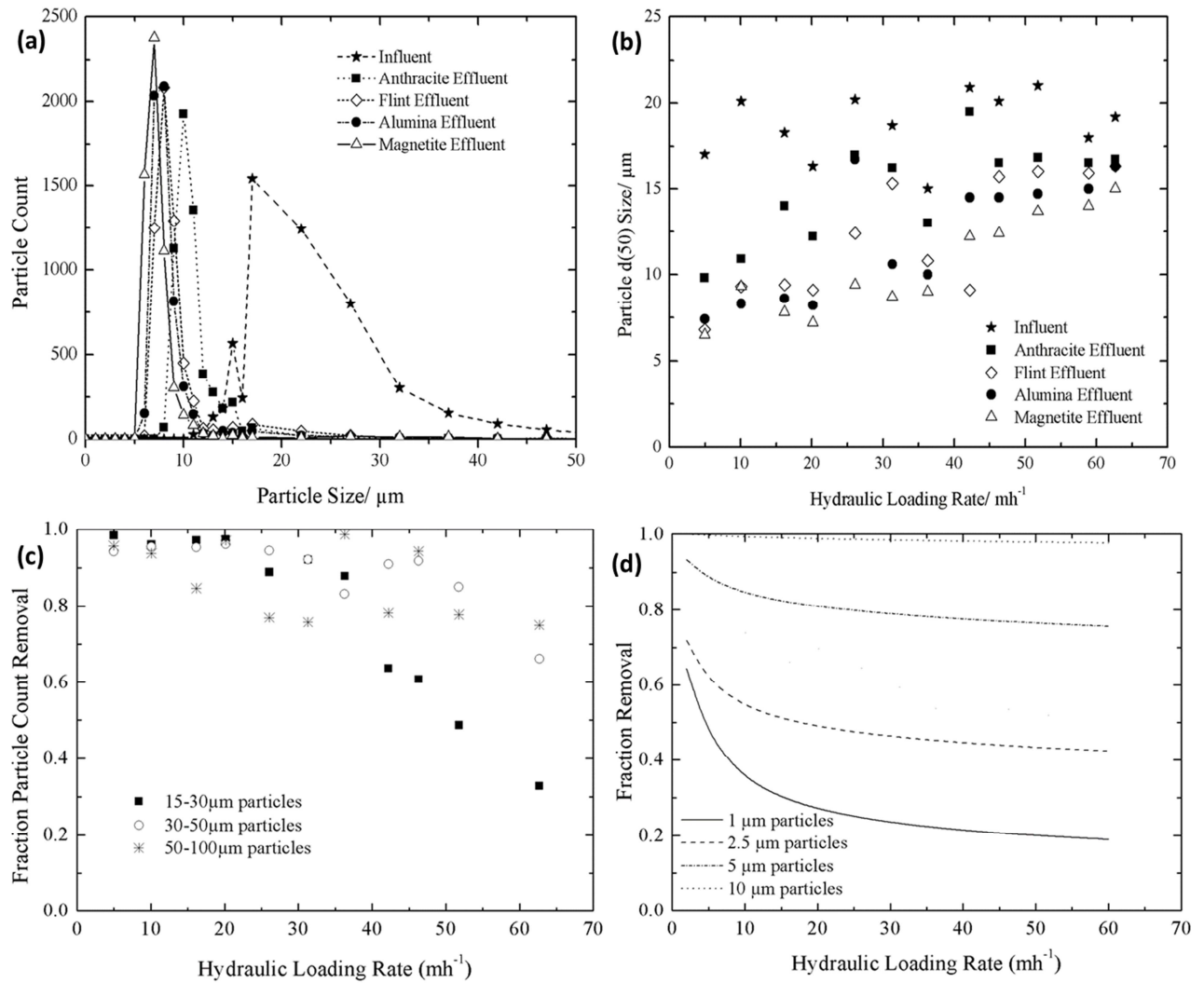
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622 Figure 5: (a) Typical PSDs of the wastewater at different stages through the filter (for the 5
 623 $\text{m}^3/\text{m}^2/\text{h}$ filter run), (b) The average size of particles passing through each filter stage at different
 624 HLRs, (c) Overall removal of 15-30 μm , 30-50 μm and 50-100 μm particles, (d) The TE
 625 model plots for the particle sizes 1, 2.5, 5 and 10 μm .

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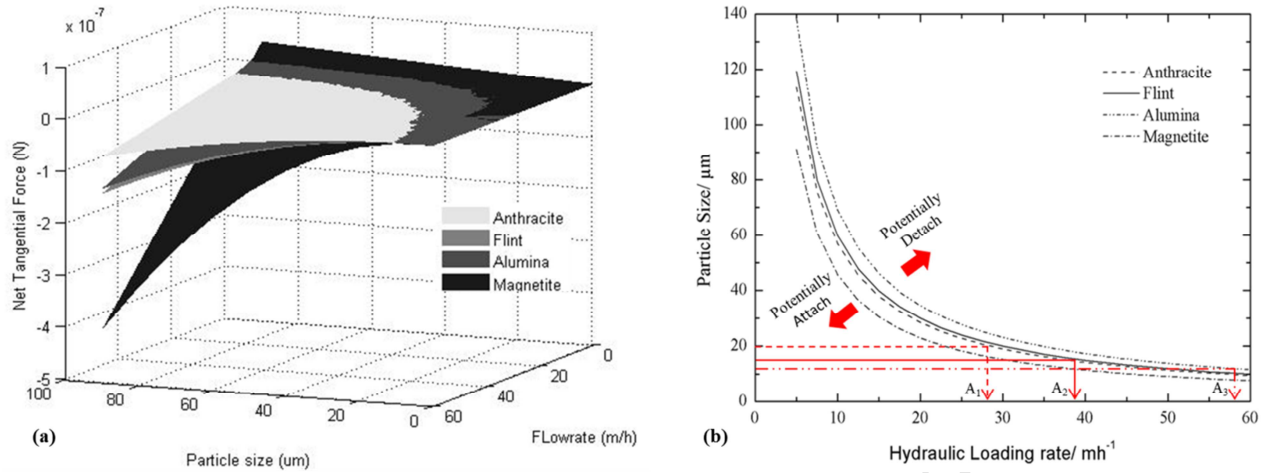
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633 Figure 6: Modelled net tangential force (equation (3) and (4)) in a clean bed ($\sigma = 0$) (a) 3D
 634 plot for the different particle sizes and HLRs in the four media layers, (b) Plot of the particle
 635 sizes and HLR when the net tangential force is zero for the four layers ($k_f = 3.79 \times 10^{-6} \text{ m}$ from
 636 Bai and Tien (1997), $H = 1.4 \times 10^{-20} \text{ kgm}^2\text{s}^{-2}$ and $\delta = 3 \times 10^{-10} \text{ m}^{24}$, $\mu = 0.000955 \text{ kgm}^{-1}\text{s}^{-1}$ and
 637 the parameters defined in Materials and Methods were used in the simulation).

638

Highlights

A multimedia filter successfully treated tertiary wastewater at rates up to 40 m h^{-1}

The impact of loading onto the multimedia filter was much less than for a single media filter

Hydrodynamic scouring models successfully explained the observed solids removal

The multimedia filter provides an effective way to provide enhanced wastewater treatment