

## ORIGINAL ARTICLE

# Microstructural evolution in infiltration-growth processed MgB<sub>2</sub> bulk superconductors

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## Abstract

The study reports phase and microstructural evolution in MgB<sub>2</sub> bulk superconductors fabricated by an infiltration and growth (IG) process. Three distinct stages, (1) intermediate boride formation, (2) bulk liquid Mg infiltration, and (3) MgB<sub>2</sub> layer formation, were identified in IG process after detailed examination of series of samples prepared with varied heating conditions. The intermediate phase Mg<sub>2</sub>B<sub>25</sub>, isomorphous to β-boron, was detected prior to MgB<sub>2</sub> phase formation in stage (1). Due to volume expansion involved in stage 1, cracks formed in the β-boron particles and propagated radially inwards during stage 3. The growing MgB<sub>2</sub> particles sintered simultaneously with formation of grain boundaries during the process, as evidenced by the measured hardness and critical current density in these samples. From our observations, we estimate the total time needed for complete transformation to MgB<sub>2</sub>.

## KEYWORDS

infiltration and growth, MgB<sub>2</sub>, superconductors

## 1 | INTRODUCTION

Superconducting MgB<sub>2</sub> is an exciting candidate for practical applications due to a relatively high T<sub>c</sub> (39 K), low raw material cost, low density (2.6 g/cm<sup>3</sup>), ease of fabrication, and the absence of any deleterious effect on critical current arising from grain boundaries.<sup>1,2</sup> Infiltration and growth (IG) is a promising route for the fabrication of MgB<sub>2</sub> bulk superconductors, typically involving impregnation of liquid magnesium, Mg(l), into a porous solid boron, B(s), preform. The resultant product is essentially a MgB<sub>2</sub>-Mg ceramic matrix composite, with Mg levels up to 15%. The relative density of IG processed MgB<sub>2</sub> is significantly higher (>90%) than samples

fabricated using conventional sintering techniques, with process requiring no high-pressure apparatus.<sup>3,4</sup> Moreover, near-net complex shapes can be fabricated with infiltration route that are not easily achievable by conventional sintering methods.<sup>5,6</sup>

Although significant advances have been made to the IG process to enable fabrication of high-quality bulk samples,<sup>5,7,8</sup> only a few reports have commented on underlying mechanism of the process. Notably, DeFouw et al.<sup>9</sup> proposed a diffusion based model for MgB<sub>2</sub> growth in boron fibers. They observed radial and circumferential growth of MgB<sub>2</sub>, via the formation of intermediate phases, including MgB<sub>7</sub> and MgB<sub>4</sub>. Radial growth of the MgB<sub>2</sub> phase occurred mainly due to the formation of radial cracks due

to an associated volume expansion. Similarly, Albisetti et al. suggested that  $Mg_2B_{25}$  could be a precursor to  $MgB_2$  formation in RLI process through analysis of various reactive liquid infiltration (RLI) processed samples.<sup>10</sup> More recently, Li et al.<sup>11</sup> have suggested that the thickness of the first layer of  $MgB_2$  formed at the  $Mg(l)$ - $B(s)$  interface is critical in determining the overall fraction of  $MgB_2$  in the final reacted IG processed  $MgB_2$  wires. They accounted for this as being due to the fact that Mg atoms needed to diffuse through the  $MgB_2$  layer in order to react with the B.

For this study, we devised experiments aimed at understanding the growth mechanism of the superconducting  $MgB_2$  phase during the IG process. The resultant microstructural evolution in the samples is discussed via the analysis of series of samples. Finally, we propose a possible mechanism for the growth of superconducting  $MgB_2$ .

## 2 | EXPERIMENTAL PROCEDURE

Crystalline  $\beta$ -boron (98% pure, HC Starck, <40  $\mu m$ ; Karlsruhe, Germany), weighing 1.5 g, was pressed uniaxially into cylindrical precursor pellets of diameter 16 mm and thickness 6 mm under a load of 20 MPa. SEM images (not shown here) of  $\beta$ -B powder suggested a bimodal particle size distribution with most particles with sizes of 5-10  $\mu m$  and  $\sim 30 \mu m$ . A total of 10 such boron precursors were prepared. The IG process was performed as follows- The pressed precursor pellets were placed in a perforated steel enclosure and the entire assembly was introduced in crucible containing liquid Mg at 750°C.  $N_2 + SF_6$  (volume ratio 95:5) cover gas was maintained above Mg melt surface to minimize oxidation of Mg.  $SF_6$  gas is known to react with  $Mg(l)$  to form  $MgF_2$ , which fills the pores in otherwise porous MgO film on the melt surface.<sup>12</sup> The temperature of the melt was then raised to a target temperature at 300°C/h. At the end of holding time, temperature of the melt was reduced to 750°C and steel enclosure containing IG processed  $MgB_2$  sample was recovered from the liquid Mg bath.<sup>13</sup> This procedure slightly varies from reactive liquid infiltration method adopted by Giunchi et al., where Mg bulk and B precursor were placed in a metallic container. It was later welded prior to heat treatment to obtain dense, bulk  $MgB_2$ .<sup>4</sup> Seven of the B precursors were subjected to IG process at fixed temperature of 750°C for durations of 5 minutes, 10 minutes, 20 minutes, 40 minutes, 1 hour, 2 hours, and 4 hours. To study the influence of reaction temperature, the remaining three precursors were reacted with a constant soaking time of 4 hours and varying reaction temperatures of 800°C, 850°C, and 900°C. The reacted product from IG process, when in the form of hard bulk, was slightly ground to remove Mg metal on bulk surface. Wherever powdery reacted product was obtained, especially for soaking time

<20 minutes, all the powder was carefully collected. Weight of all the samples were recorded to estimate Mg intake, since weight of starting B precursor was kept constant at 1.5 g. The samples were then characterized using various physical property and compositional measurement techniques such as scanning electron microscopy (SEM), X-ray diffraction (XRD), and Vickers hardness measurements. The critical current densities ( $J_c$ ) of these samples were calculated from measured magnetic moment hysteresis loops using the extended Bean model for a rectangular cross section in a perpendicular, applied magnetic field.<sup>14</sup>

## 3 | RESULTS

From our observations, we divide the overall growth of superconducting  $MgB_2$  in the IG process into three stages:

### 3.1 | Stage 1: Initiation of cracks in the boron particle: $Mg_2B_{25}$ phase formation process

The SEM images of samples reacted isothermally at 750°C at 5 minutes, 10 minutes, 20 minutes, and 40 minutes are shown in Figures 1A,B,C,D, respectively. The sample reacted for 5 minutes is observed to be free from Mg with no sign of phase transformation. The sample reacted for 10 minutes, however, shows initiation of cracks in some of the particles (indicated in Figure 1 by green dashed circles), whereas almost all the B particles in sample reacted for 20 minutes show radially inward multiple cracks, exposing fresh B region to Mg vapor. The XRD patterns of these samples, shown in Figure 2, reveal an increasing appearance of  $Mg_2B_{25}$ , a recently discovered phase, in sample reacted for 10 and 20 minutes, suggesting a strong correlation between cracking and transformation of  $\beta$ -rhombohedral into  $Mg_2B_{25}$ .<sup>15,16</sup> This is illustrated as stage 1 in schematic of IG process in Figure 3.

### 3.2 | Stage 2: Mg uptake in the porous precursor

The overall weight gain in the precursor as a function of reaction time at a fixed temperature (750°C), plotted in Figure 4, enables the study of rate of influx of Mg with time (Figure 3, Stage 2). Given that XRD did not detect any traces of MgO (Figure 2), all the gain in weight of the sample can be attributed to liquid Mg only. Mg uptake into the precursor pellet could only be observed after 40 minutes of reaction. Samples reacted for 5, 10, and 20 minutes showed no detectable weight gain. Conversely, the sample reacted for 40 minutes showed an 80% weight gain while the 1 hour sample exhibited a doubling in weight. It is

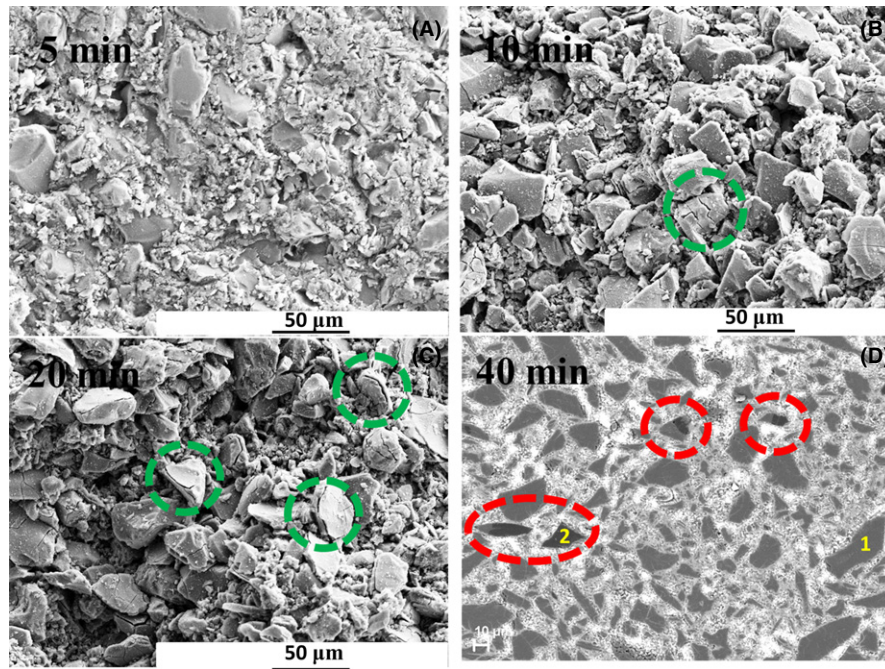


FIGURE 1 SEM images of samples reacted at 750°C for 5, 10, 20, and 40 minutes, respectively

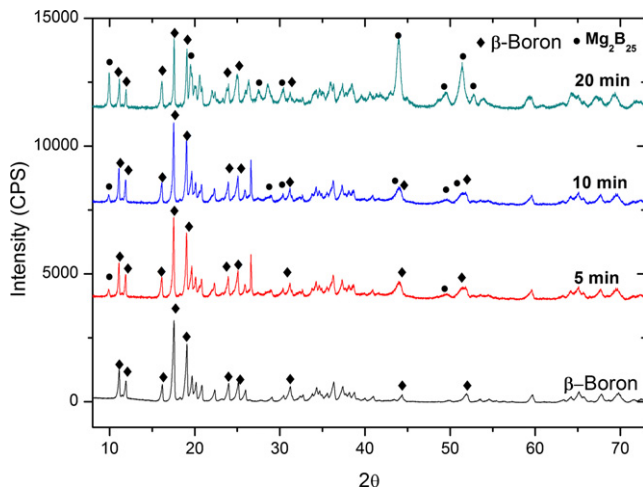


FIGURE 2 XRD patterns for the samples reacted for 5, 10, and 20 minutes, respectively, at 750°C. Plot for  $\beta$ -boron also shown for comparison

noted that doubling (100% weight gain-1.5 g Mg) also satisfies the stoichiometric requirement of the quantity of Mg needed to react with B in the precursor. The sample reacted for longer than 1 hour showed no further uptake of Mg.

### 3.3 | Stage 3: Transformation of $Mg_2B_{25}$ to $MgB_2$ : rate determining step

The following three phenomena are observed concurrently in the final stage IG process.

#### 3.3.1 | Propagation of primary cracks in $Mg_2B_{25}$ particles and fragmentation

Figures 5A,B show back scatter electron images of samples reacted at 750°C for 40 minutes and 2 hours, respectively. The sample reacted for 40 minutes shows the presence of Mg(l) (bright in contrast) within pores in the precursor and radial cracks that formed during Stage 1 (as shown by black arrows). It is quite apparent that cracks in the sample reacted for 2 hours are deeper in to the particle than that of particles in the sample reacted for 40 minutes. These cracks propagated through the  $Mg_2B_{25}$  particle, and even extend throughout the entire particle cross section, as can be seen from Figure 5B. Consequently, these cracks resulted in fracture and fragmentation in some of the particles indicated by red dashed circles). During Isothermal heat treatment at 750°C. XRD analysis (not shown here) indicates that samples reacted at 750°C for 40 minutes and 2 hours contained  $Mg_2B_{25}$  phase of up to 40% and 30% (volume), respectively.

#### 3.3.2 | Diffusion-controlled $MgB_2$ growth

Figures 6A,B compare the microstructures of samples reacted for 4 hours at 750°C and 900°C, respectively. High residual Mg content and a large amount of  $Mg_2B_{25}$  phase is present in the sample reacted at 750°C. The sample reacted for 900°C shows large depth of  $MgB_2$  layer thickness on individual particle or “diffusion zone”, indicating the Mg diffusion distance into  $Mg_2B_{25}$  particle. Moreover, smaller particles of size 5  $\mu m$  appear to have completely

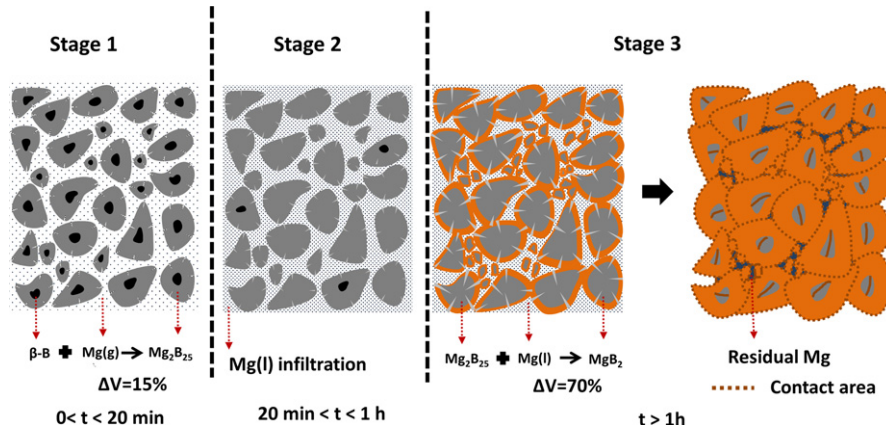


FIGURE 3 Schematic illustration of microstructure and phase evolution during the IG process

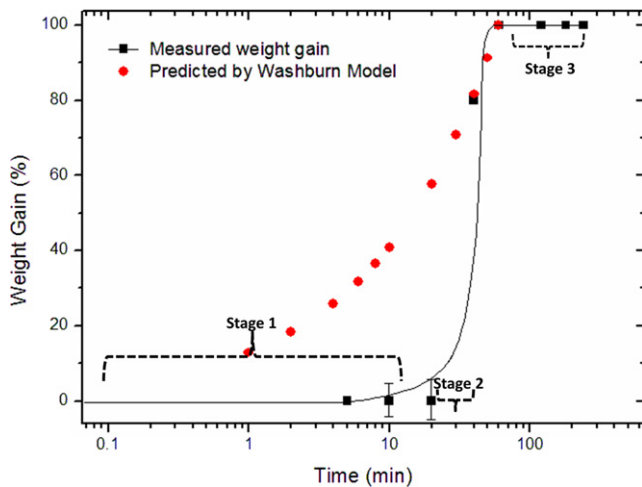


FIGURE 4 Measured weight gain in IG sample compared with that predicted by classical capillary infiltration, as a function of reaction time. The 5% error for samples reacted for 10 and 20 minutes accounts for losses associated with the handling of powdery, reacted product

transformed into a different phase. XRD patterns and the corresponding estimated phase contents at each temperature (750°C, 800°C, 850°C, and 900°C) are shown in Figures 7A,B, respectively. Phase content of Mg<sub>2</sub>B<sub>25</sub> and Mg at 750°C is estimated to be about ~26% and 33%, respectively. It is reduced progressively as the temperature increases and reaches ~12% and 14%, respectively, at 900°C, which clearly suggests that growth of superconducting MgB<sub>2</sub> phase occurs at the expense of Mg<sub>2</sub>B<sub>25</sub> and Mg phase consumption.

### 3.3.3 | Simultaneous sintering

Figure 8 shows the variation in bulk hardness and critical current density as a function of reaction temperature. It is

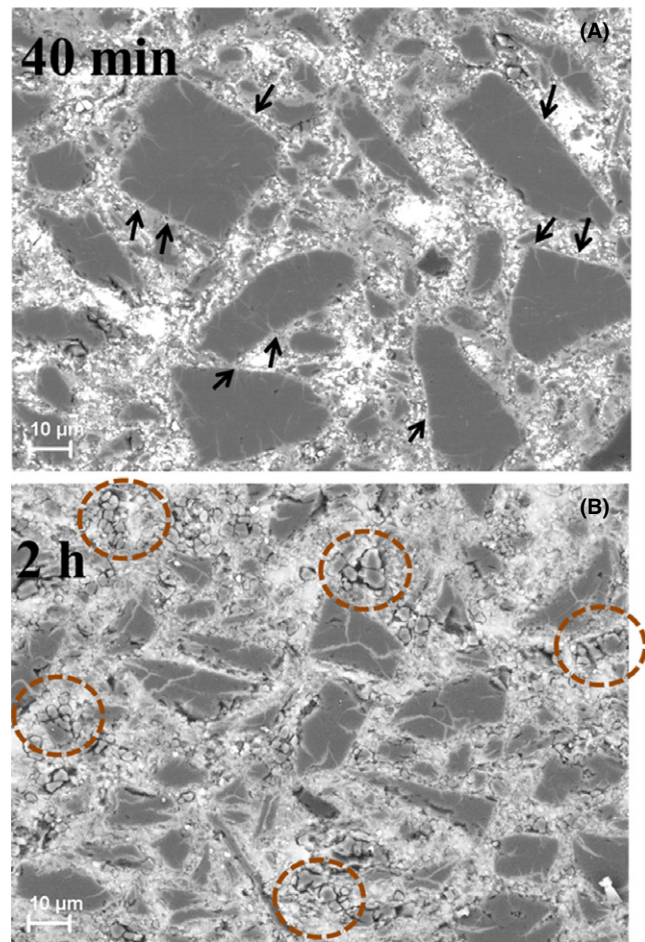
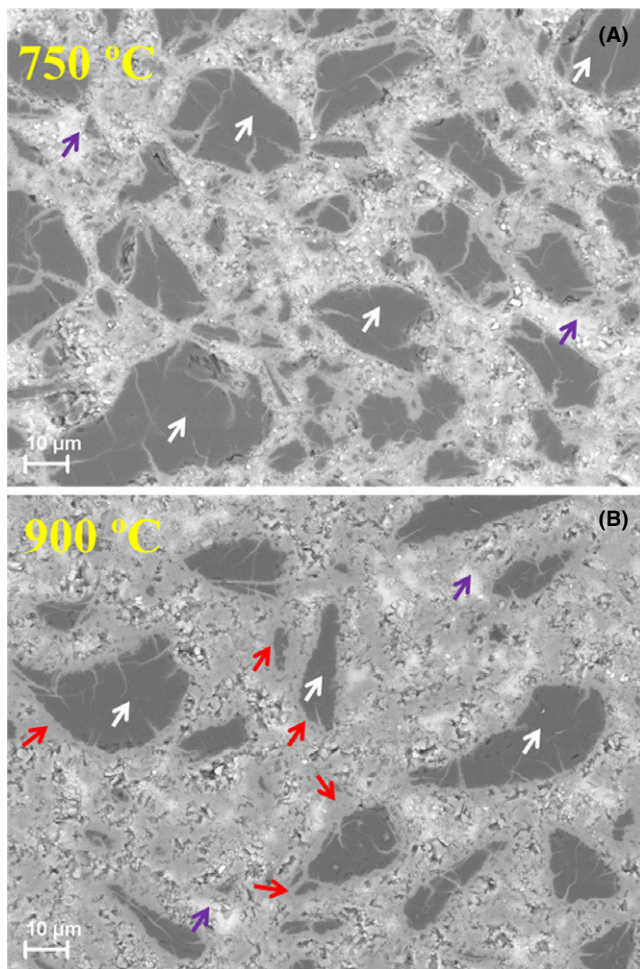


FIGURE 5 SEM images of IG processed samples. (A) The sample reacted for 40 minutes shows smaller crack length (shown by arrows). (B) The sample reacted for 2 h shows propagation of cracks and ultimate fracture in Mg<sub>2</sub>B<sub>25</sub> particles (indicated by dotted circles)

evident that critical current density increases with the reaction temperature. The growth of MgB<sub>2</sub> occurs radially inwards in the boron particles and this superconducting



**FIGURE 6** SEM images of samples reacted for 4 h at (A) 750°C and (B) 900°C. The red arrows indicate the “Diffusion zone”. The purple arrows indicate unreacted Mg and the white arrows indicate the  $Mg_2B_{25}$  phase

layer undergoes almost twofold volume expansion. These growing particles impinge on one another and sinter simultaneously (Figure 3, Stage 3), as evident in our previous studies<sup>6</sup>. The sintering process enhances the grain connectivity and is responsible for the observed increased  $J_c$  as a function of soaking temperature. Increased hardness as a function of temperature also suggests increased grain connectivity by the sintering process.

## 4 | DISCUSSION

It is clear from Stage 1 that  $Mg_2B_{25}$  is a nonequilibrium intermediate phase in the  $MgB_2$  phase formation and is also stable at room temperature. The crystal structure of the  $Mg_2B_{25}$  phase can be described as partial occupancy of Mg atoms (7.4 atomic %) at interstitial sites (namely A, D, E, and F) in a complex

rhombohedral unit cell of  $\beta$ -boron comprising of 105 atoms. Thus, major structural rearrangement of  $\beta$ -boron is not necessary, although lattice constants are slightly enhanced.<sup>15,16</sup> Given that the influx of Mg(l) is below detectable limits in the initial stages of the infiltration process, it is likely that the Mg atoms that are transported from liquid source to individual  $\beta$ -boron particles to form  $Mg_2B_{25}$  are in the vapor phase. A quick transformation of B ( $\sim 20$ -40 minutes) to form boron-rich boride according to following reaction suggests that the reaction kinetics are favorable.



When a B particle reacts with Mg vapor, the  $Mg_2B_{25}$  phase initially forms on the surface of boron particle (Figure 3, Stage 1), as shown in Figure 9. At this stage, an element of  $Mg_2B_{25}$  at the periphery of B particle experiences compressive tangential stresses. This is primarily because B (molar volume ( $V_B$ )=4.7  $cm^3$ ) particle (in equation I) undergoes volume expansion after transforming into  $Mg_2B_{25}$  (molar volume ( $V_{Mg_2B_{25}}$ )=129.7  $cm^3$ ) according to (I). The peripheral region is pushed away from the centre upon subsequent growth of the  $Mg_2B_{25}$  layer, unloads elastically and then experiences tensile tangential stress as illustrated schematically in Figure 9. This stress leads to the initiation of a radial crack due to the negligible plasticity of  $Mg_2B_{25}$ .<sup>17</sup> This phenomenon has been observed previously and reported as “Lithiation induced fracture” within the context of the diffusion of lithium in silicon particles.<sup>17-21</sup>

When elastic strain is small compared to reaction induced strain (volume strain: 11%), radial ( $\sigma_r$ ), and tangential ( $\sigma_\theta$ ) stresses at any distance  $R$  from centre of a spherical  $\beta$ -B particle upon formation of thin  $Mg_2B_{25}$  shell can be described as;<sup>17</sup>

$$\sigma_r = -2\sigma_y \log\left(\frac{b}{r}\right) \quad (1)$$

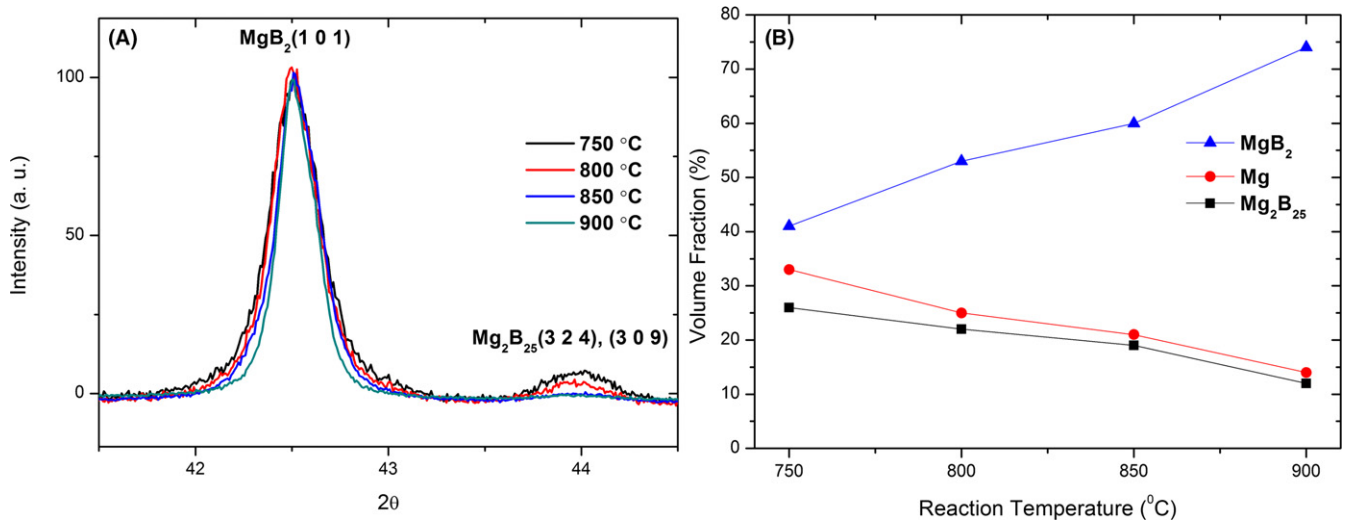
$$\sigma_\theta = \sigma_y - \sigma_y \log\left(\frac{b}{r}\right) \quad (a \leq R \leq b) \quad (2)$$

where  $b$  is the outer radius of sphere and  $a$  is the radius of an unreacted  $\beta$ -B sphere.

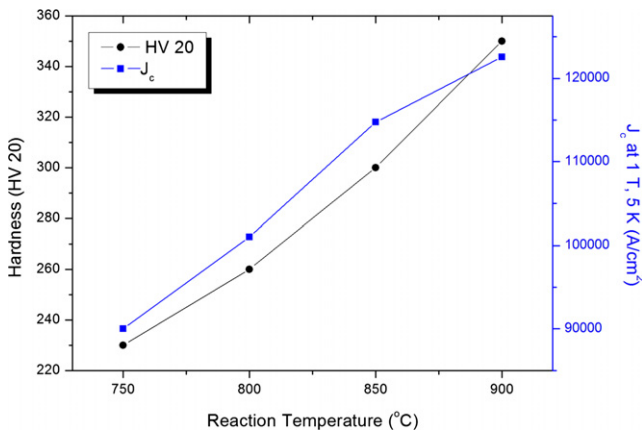
$b$  is also expressed as a function of initial radius of particle prior to reaction ( $b_i$ ) as

$$b = [a^3 + \beta(b_i^3 - a^3)]^{1/3} \quad (3)$$

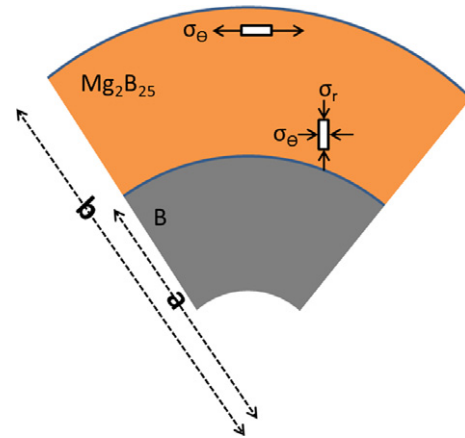
The above equation takes relative volume expansion  $\beta$  (ratio of molar volume of  $Mg_2B_{25}$  to  $\beta$ -B) into consideration. The hoop stress is tensile in nature at the periphery ( $b=R$ ) with a maximum value equal to the yield strength  $\sigma_y$ . Given the brittle nature of  $Mg_2B_{25}$ , hoop stress ( $\sigma_\theta = \sigma_y$ ) is likely to initiate fracture of particle by generation of a crack.<sup>12</sup> It is noted that residual stresses can



**FIGURE 7** A, XRD patterns of samples reacted for 4 h at 750°C, 800°C, 850°C, and 900°C. Note that changing the relative amount of MgB<sub>2</sub> and Mg<sub>2</sub>B<sub>25</sub> phases varies depending on the temperature. B, Estimated volume fraction phases (MgB<sub>2</sub>, Mg and Mg<sub>2</sub>B<sub>25</sub>) as a function of reaction temperature



**FIGURE 8** Variation of critical current density and hardness plotted as a function of reaction temperature



**FIGURE 9** Schematic illustration of a progressing Mg<sub>2</sub>B<sub>25</sub> front and the generation of stress

remain compressive in a particle with flat surface. Thus, curvature is critical for the initiation of cracks at the surface of a particle.

This stress  $\sigma_y$  ( $>\sigma_c$ ) would propagate the crack<sup>17</sup> if crack size is such that

$$G = Z \frac{\sigma_c^2}{E} b \quad (4)$$

where  $\sigma_c$  is the critical stress required to propagate a crack of length  $2b$ ,  $Z$  is a geometrical factor,  $E$  is elastic modulus of Mg<sub>2</sub>B<sub>25</sub>, and  $G$  is the energy release rate. Although  $\sigma_y$  is clearly sufficiently high to propagate a crack for a short distance (as apparent from Figure 5A), the cracks do not propagate freely inwards since the tensile hoop stress decreases steadily, eventually becoming compressive toward the center.<sup>17,21</sup>

Energy-dispersive X-ray analysis at locations 1 and 2 in Figure 1D confirms the Mg<sub>2</sub>B<sub>25</sub> phase formation and the corresponding EDAX patterns are shown in Figure 10. At this stage, a considerable amount of Mg has occupied the pores in the boron precursor. It is evident from Figure 2 that significant portion of B powder is transformed into Mg<sub>2</sub>B<sub>25</sub> within the first 20 minutes of soaking time and that no detectable amount of superconducting MgB<sub>2</sub> is observed. Several particles in the microstructure (Figure 1D), appearing dark in contrast indicated by red dashed circle, represent unreacted  $\beta$ -Boron particles with B/Mg ratio of 98 (eg location 2) that have not yet transformed into Mg<sub>2</sub>B<sub>25</sub>. The relatively lighter in contrast particles (location 1) are confirmed as Mg<sub>2</sub>B<sub>25</sub> particles. EDS analysis on several random points within such areas suggests a

B/Mg atomic ratio of 10 as opposed to an ideally expected ratio of 12.5. The slight underestimation of this ratio is attributed to the interaction volume of the penetrating electron beam, some of which probe Mg metal beneath the particle.

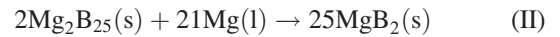
The Mg infiltration depth ( $\chi_0$ ) into the porous boron preform can be expressed by following Washburn's equation in the Stage 2 of the IG process,<sup>22</sup>

$$(\chi) = \left( \frac{r\gamma \cos\theta}{2\eta} \right)^{1/2} \cdot t(0)^{1/2} \quad (5)$$

$r$ ,  $\gamma$ ,  $\theta$ , and  $\eta$  represent the radius of cylindrical porous channels, surface tension, wetting angle between  $\beta$ -B(s)-Mg(l), and viscosity of Mg melt, respectively, whereas  $\chi$  and  $t$  represent infiltration depth and time taken. Since weight gain is directly proportional to  $\chi$ , equation 5 suggests a parabolic dependence of weight gain (dotted line in Figure 4) with time. A deviation from Washburn's model is expected in the present case as the pores are of irregular shapes and sizes. Moreover, other mechanisms, such as

gravity, hydrostatic fluid pressure and negative pressure (from volume shrinkage in  $\text{MgB}_2$  phase formation), are also expected to contribute to the uptake of Mg. The predicted and measured weight gain with reaction time is compared in Figure 4. Note that due to the unknown contact angle ( $\theta$ ), Washburn infiltration is assumed to reach completion after 1 hour, and weight gain from 0 to 1 hour is predicted. Li et al. observed that, at 675°C, Mg infiltrates to a depth of 40  $\mu\text{m}$  in 1 hour in  $\text{MgB}_2$  wires synthesized from nano-boron powder. Even after suitable correction for pore radius (assumed proportional to particle size), and a small change in viscosity, the rate of Mg uptake appears much more rapid in this study. It is therefore suggested that aside from liquid infiltration and other aforementioned mechanisms, vapor diffusion could also be another mode of transport of Mg from liquid reservoir since Mg is known for its high vapor pressure. The vapor diffusion process explains the observed phase transformation of B into  $\text{Mg}_2\text{B}_{25}$  everywhere within the sample and the absence of Mg phase in initial 20 minutes of the process. During this period, Mg atoms are adsorbed everywhere on  $\beta$ -B particle surface and react according to (I) to form  $\text{Mg}_2\text{B}_{25}$ , creating further driving force for Mg vapor influx. Mg pick up from classical Washburn liquid infiltration is likely to be limited to the edges of sample during initial 20 minutes of the soaking period.

In the third and final stage of the process, the propagation of cracks, formation of a  $\text{MgB}_2$  diffusion layer and sintering all occurred simultaneously. Mg(l) entered the cracks and reacted with  $\text{Mg}_2\text{B}_{25}$  at the crack tip/surface to form  $\text{MgB}_2$ . This chemical reaction can be expressed as;



Volumetric strain experienced at the crack tip by  $\text{Mg}_2\text{B}_{25}$  element can be described as

$$\varepsilon_V = \frac{2V_m^{\text{Mg}_2\text{B}_{25}} - 25V_m^{\text{MgB}_2}}{2V_m^{\text{Mg}_2\text{B}_{25}}} \sim 70\% \quad (6)$$

where  $V_m$  is molar volume, and  $\varepsilon_V$  and  $\varepsilon_L$  are volumetric and linear strains, respectively. Under the isotropic volume expansion, the linear strain  $\varepsilon_L$  is given by,

$$\varepsilon_L = \frac{\varepsilon_V}{3} \sim 23\% \quad (7)$$

Thus, the stress at the tip of the crack is given as<sup>23</sup>

$$\sigma_{\text{cracktip}} = E_{\text{MgB}_2} \varepsilon_L \sim 65\text{GPa} \quad (8)$$

Although such a volume expansion ahead of the crack tip is expected to blunt the tip and hinder crack propagation, as in the case of yttria-stabilized zirconia,<sup>24,25</sup> experimental evidence suggests that continuous formation of  $\text{MgB}_2$  can impart stress larger than the one that can be sustained

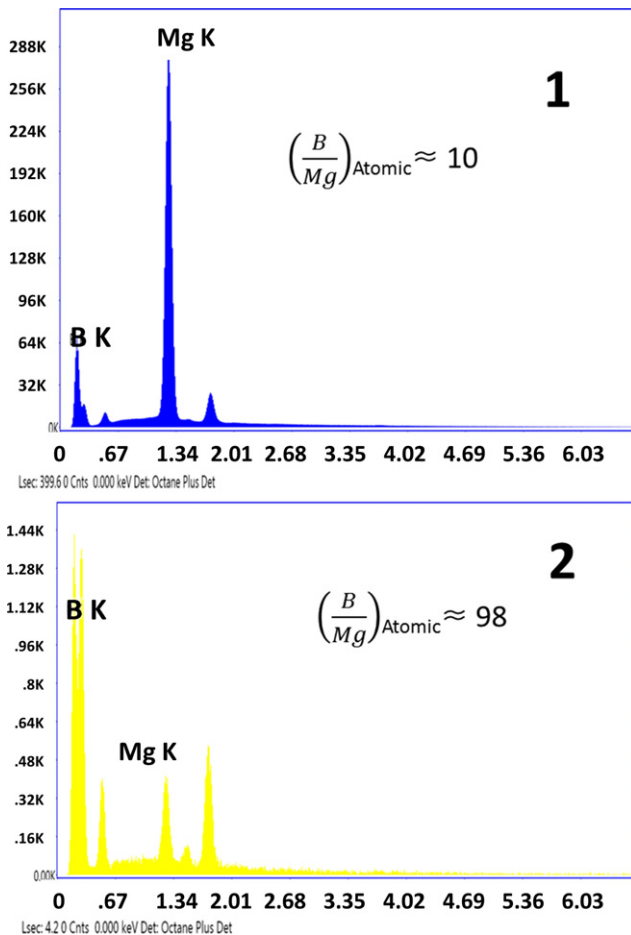


FIGURE 10 EDS point analysis on spots 1 and 2 (from Figure 1D) showing relative amounts of B and Mg

elastically by  $Mg_2B_{25}$ . Therefore, the crack propagates further exposing fresh  $Mg_2B_{25}$  to  $Mg(l)$ . DeFaw et al. also observed such time-dependent crack growth in  $MgB_2$  synthesis from boron fibers.<sup>9</sup> As a result, cracks propagate radially inward, often resulting in the fragmentation of particles. Formation and propagation of these cracks play a vital role in formation of  $MgB_2$  channels passing through the non-superconducting  $Mg_2B_{25}$  phase. This provides an added supercurrent path in the fully processed bulk material.

$MgB_2$  phase formation closely resembles a peritectic reaction where reaction occurs only on the surface and is governed by diffusion of various chemical species. Therefore, the reaction does not often reach completion, as is observed frequently in the fabrication of (RE)BCO superconductors, where the final microstructure invariably contains a considerable amount of unreacted phase (Y-211).<sup>26,27</sup> A decrease in  $Mg_2B_{25}$  phase content (12%) is observed as a result of  $Mg(l)$  reaction with  $Mg_2B_{25}$  phase and enhanced kinetics at higher temperature. Similarly, XRD patterns (Figure 7A) also show a diminishing phase content of  $Mg_2B_{25}$  with increasing reaction temperature. It is also worth noting that  $MgB_2$  formed at lower temperature is “dirtier”, as indicated by broader peaks in samples reacted at low temperature.

The so-called Deal and Grove model has been adopted to describe the Mg diffusion process in the growth of  $MgB_2$ .<sup>28,29</sup> In this model, it is assumed that all boron particles are spherical and of equal diameter, and that the diffusion process is a steady state. It is assumed that no reaction has taken place while  $Mg(l)$  occupies all the porous sites in the precursor.

According to Fick’s first law,

$$J_{Mg} = D \frac{C_{Mg-MgB_2} - C_{MgB_2-Mg_2B_{25}}}{x} \quad (9)$$

where  $D$  is the diffusivity of Mg in  $MgB_2$ ,  $C_{Mg-MgB_2}$  represents the concentration at Mg- $MgB_2$  interface,  $C_{MgB_2-Mg_2B_{25}}$  is the Mg concentration at  $MgB_2$ - $Mg_2B_{25}$  interface,  $J_{Mg}$  is influx of Mg atoms, and  $x$  is thickness of the  $MgB_2$  layer.

For mass balance, the influx of Mg ( $J_{Mg}$ ) should be equal to the rate of  $MgB_2$  formation given that the number of moles of Mg diffusing through the  $MgB_2$  layer is the same as that reacting with  $Mg_2B_{25}$  to form  $MgB_2$ . Assuming a first-order reaction,

$$J_{Mg} = KC_{MgB_2-Mg_2B_{25}} \quad (10)$$

where  $K$  is reaction constant in Equation 10.

Combining equations (9) and (10) yields

$$C_{MgB_2-Mg_2B_{25}} = \frac{DC_{Mg-MgB_2}}{D + xK} \quad (11)$$

$$J_{Mg} = \frac{K(DC_{Mg-MgB_2})}{D + xK} \quad (12)$$

Assuming that the  $MgB_2$  layer grows by an infinitesimally small length  $dx$  in time  $dt$ , the number of moles of Mg crossing a unit cross-sectional area in  $dt$  is therefore  $J_{Mg}dt$ . These are number of Mg atoms reacting to form  $MgB_2$  with volume of cuboid equaling unit area and length  $dx$  ( $V_{Mg}^{MgB_2}$ ). Note that 21 moles of Mg are required to form 25 moles of  $MgB_2$ . (equation II)

$$21J_{Mg}dt = 25V_{Mg}^{MgB_2} dx \quad (13)$$

$$dt = \frac{25(D + xK)}{21KDC_{Mg-MgB_2}} V_{Mg}^{MgB_2} dx \quad (14)$$

Invoking the assumption that the overall reaction is controlled by diffusion rather than reaction rates, equation (14) yields

$$\int_{t=0}^{t=t^*} dt = \frac{25V_{Mg}^{MgB_2}}{21} \int_{x=0}^{x=20 \times 10^{-6}} \left( \frac{x}{DC_{Mg-MgB_2}} \right) dx \quad (15)$$

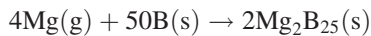
where  $t^*$  is the time necessary to complete reaction II (stage 3) at 900°C. The upper limit of  $x$  is chosen as the radius of the reacting particle. Values of  $D=10^{-14}$  m<sup>2</sup>/s (900°C),<sup>9</sup>  $C_{Mg-MgB_2}=6.6 \times 10^4$  mol/m<sup>3</sup>, yields  $t^*=6$  hours  $V_{Mg}^{MgB_2} = 5.6 \times 10^4$  mol/m<sup>3</sup>. Similarly, to ensure completion of reaction at 900°C at 4 hours (When time taken for completion of stage 1 and 2 ~ 1 hours), a uniform particle size of ~14 μm would be required for this process.

As the  $MgB_2$  layer forms on the surface of particle, it almost doubles in volume, leading to impingement of particles on one another. A large contact area between the particles presents clear evidence of sintering between the particles.<sup>6</sup> Critical current density is essentially a function of  $MgB_2$  phase fraction and degree of sintering between the particles. These two factors together form  $A_f$ , the effective cross-sectional area<sup>30</sup>. Therefore,  $J_c$  increases almost linearly with the reaction temperature, as expected. Similarly, it can be argued that bulk hardness (HV20) is a strong function of sintering and individual phase fraction.<sup>31,32</sup> Thus an observed increase in hardness of these samples with temperature gives another independent evidence of sintering between the  $MgB_2$  particles.

## 5 | CONCLUSION

It can be concluded that  $MgB_2$  phase formation in IG process is a three stage process that can be summarized by the following chemical equations.





With the formation of intermediate phase  $\text{Mg}_2\text{B}_{25}$  and associated volume expansion, cracks were initiated in all boron particles. These cracks propagated radially inwards, originating from crack tip stresses, resulting fracture and disintegration in a number of particles, and thereby offering better kinetics by exposing large surface area for reaction. Mg infiltration in the precursor was rapid, aided probably by vapor phase transport. This was followed by  $\text{MgB}_2$  layer growth, limited by diffusion of Mg atoms, and simultaneous sintering together to form grain boundaries. Despite reaction at high temperature (900°C, 4 hours), the samples contained residual intermediate boride. Therefore, an optimized particle size, of sufficient size to create pore geometries to facilitate Mg(l) infiltration, yet small enough to ensure complete diffusion of Mg atoms to the center and to provide grain-boundary pinning, could be the way forward for the fabrication of high-performance IG processed  $\text{MgB}_2$  bulk superconductors.

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