

# The Turbulent Wake of a Monopile Foundation

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## Abstract

An experimental programme is presented, examining the turbulent wake of a monopile foundation in a current. Velocity was recorded across an extensive domain downstream of a model monopile in a 0.5 m deep basin, using an acoustic Doppler velocimeter array. The distribution of turbulent kinetic energy ( $TKE$ ) is examined across the entire domain. Tests were undertaken using several combinations of pile diameter ( $D = 0.1$  and  $0.2$  m) and mean flow velocity ( $\bar{u}_0 = 0.08$  to  $0.24$  m/s), representing typical prototype conditions at a scale of 1:50. It is shown that turbulence can be predicted using the distance downstream ( $x$ ) and off axis ( $y$ ), the pile diameter, and the mean flow velocity. Two new parameters are introduced to simplify assessment of proposed structures. Relative Excess Turbulence ( $RET$ ) is the extra turbulence generated by the pile, normalised by the ambient turbulence. Turbulence Recovery Lengthscale ( $TRL$ ) is the distance downstream (normalised by  $D$ ) required for  $RET$  to fall below a given threshold. Results show that  $RET$  decays exponentially with distance downstream. Across the wake,  $RET$  fitted a Gaussian function with peak values at the wake centreline.  $TRL$  is estimated at 40 for an  $RET$  threshold of 1.0 and 400 for an  $RET$  threshold of 0.1.

*Keywords:* monopile, turbulence, windfarm, monopile array, windfarm environmental impact, current

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## 1. Introduction

Monopile foundations are by far the most common design for offshore wind turbines, comprising 91% of all European installations completed in 2014 (EWEA, 2015). They are well suited to shallow and transitional water depths, due to their simplicity of installation. At existing installations, piles are typically around 5 m in diameter. The UK is currently the world leader in terms of offshore wind installed capacity, with further growth in the sector forming a key component of the government's renewables 2020 strategy (DECC, 2013, Esteban et al., 2011).

As installations move into deeper water and turbine diameters increase, the greater horizontal loads and bending moments will necessitate the use of ever larger piles (Byrne and Houlby, 2003). There are plans for turbines of 6 MW capacity, in as much as 30 m of water depth. Such installations will require monopiles of up to 7.5 m diameter (Achmus et al., 2008). With a greater number of ever larger monopiles anticipated in the coming years, it is important that we understand their impact.

The flow structure close to the base of a monopile has already been extensively studied (Dargahi, 1989, García-Hermosa et al., 2014, Sumer et al., 1997, Unger and Hager, 2006). Three distinct flow structures can be identified close to the base of the pile. A horseshoe vortex forms at the upstream face, contraction of streamlines occurs as the flow accelerates around the sides of the pile, and lee wake vortices are formed immediately downstream of the pile.

These flow structures lead to enhanced bed scour and the formation of a scour hole around the pile. This is of great concern to the structural integrity of the foundation. Much work has been done to quantify the depth of the scour hole (Roulund et al., 2005, Sumer et al., 2001, Whitehouse et al., 2011), and its rate of development (McGovern et al., 2014).

In addition to the flow structures described above, the monopile's presence will cause increased turbulence in the flow downstream. Elevated turbulence enhances the carrying capacity of the flow, leading to increased sediment transport (Butt et al., 2004, Gyr and Hoyer, 2006). This increases the distance that scoured sediments can be transported downstream of the pile.

The environmental impacts of suspended sediments are numerous. Increased turbidity can affect the productivity of plankton (Kocum et al., 2002), as well as influencing the behaviour of predatory fish (Abrahams and Kattenfeld, 1997) and marine mammals (Weiffen et al., 2006). These

38 are related to economic concerns, as any changes could impact on fisheries.  
39 Sediment transport regimes also govern sedimentation processes downstream  
40 (Yin et al., 2014).

41 Techniques exist for estimating the turbidity downstream of existing mono-  
42 piles, by analysing satellite images (Gerace et al., 2013). Turbid wakes have  
43 been observed transporting sediment for hundreds of metres downstream of  
44 monopiles (Vanhellemont and Ruddick, 2014).

45 Ideally, numerical modelling would be used to predict the likely impact  
46 of a proposed wind farm on sediment transport during the planning phase.  
47 However, the flow structures governing the increased turbulence are typically  
48 on the same scale as the monopile. These cannot be resolved by existing  
49 sediment transport models, which typically have cell sizes on the order of  
50 hundreds of meters in order to cope with the large regions of interest (Magar  
51 et al., 2013).

52 This paper presents the results of a series of laboratory experiments,  
53 performed at a scale of 1:50, examining the wake structure downstream of  
54 a monopile foundation. In particular, the influence on turbulence of flow  
55 velocity, pile diameter and location relative to the pile were measured. Two  
56 new parameters are introduced to simplify turbulence assessment of planned  
57 monopile structures in terms the relative position and flow velocity.

58 Empirical relationships are presented predicting the turbulent character-  
59 istics of the wake. These have been validated to show that turbulence in  
60 the wake of a monopile can be described by a small number of parameters.  
61 These parameterisations will allow the monopile’s influence on turbulence to  
62 be implemented in regional sediment transport models.

## 63 **2. Materials and Methods**

### 64 *2.1. Experimental Design*

65 The experimental programme was carried out in the Coastal basin at  
66 Plymouth University. The basin measures 10 m long by 7.2 m wide, with a  
67 water depth of 0.5 m. The pile was fixed to the floor of the basin, centred  
68 4.5 m from the downstream tank wall and 3.5 m from the side (Figure 1).  
69 The floor of the tank is fibre reinforced plastic, with a roughness lengthscale  
70 of  $< 0.0001$  m.

71 Prototype values of water depth, pile diameter and flow velocity were cho-  
72 sen based on typical values at existing wind farm sites. Matutano et al. (2013)

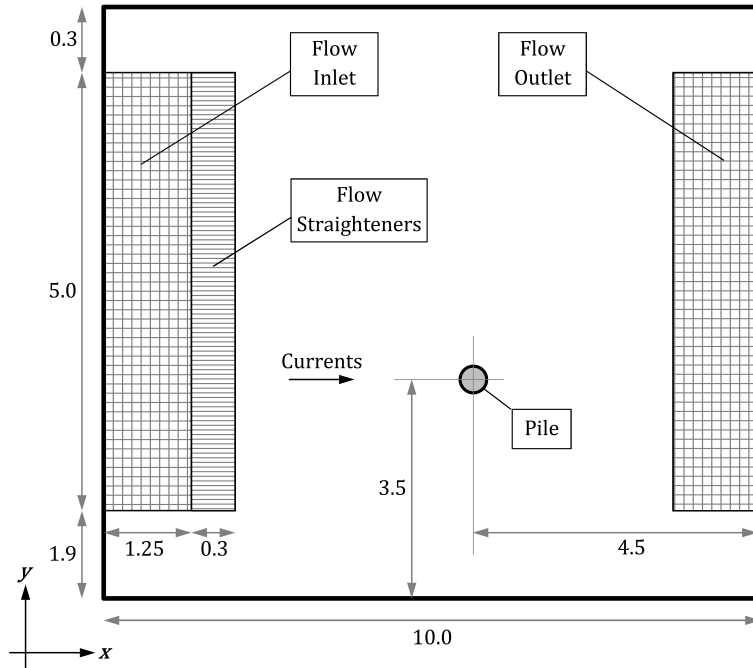


Figure 1: Plan view of the Coastal basin. Not to scale. All dimensions in metres.

73 provide information from several existing wind farms. Average monopile di-  
 74 ameter is just below 5 m, with the largest quoted at 6 m. Pile diameters are  
 75 expected to increase in the future as development moves into deeper water.  
 76 Peak current velocities range between 0.6 and 2.0 m/s, although the higher  
 77 values in this range correspond to particularly shallow sites. The experimen-  
 78 tal programme was designed to examine turbulence in the free stream flow,  
 79 and so an intermediate depth prototype was considered more appropriate.  
 80 This was confirmed by examination of proposed sites in the channel region,  
 81 using the ANEMOC offshore windfarm database (Benoit et al., 2008).

82 Prototype values were converted to model scale by applying Froude simil-  
 83 itude at a scale of 1:50 to derive appropriate scale factors ( $\lambda$ ). Measure-  
 84 ments were made at four model velocities ( $\bar{u}_0 = 0.08, 0.14, 0.18$  and  $0.24$  m/s), and  
 85 two model pile diameters ( $D = 0.1$  and  $0.2$  m), in water depth  $d$  of  $0.5$  m  
 86 (Table 1). Froude similitude is achieved between the model and prototype,  
 87 with Froude numbers ranging between  $8 \times 10^{-2}$  and  $2 \times 10^{-1}$ .

Table 1: Prototype vs Model parameters

Parameter	$\lambda$	Prototype	Model
$d$	50	25 m	0.5 m
$D$	50	5-10 m	0.1-0.2 m
$\bar{u}_0$	$\sqrt{50}$	0.6-1.6 m/s	0.08-0.24 m/s
$Re$	-	$2 \times 10^6$ to $2 \times 10^7$	$8 \times 10^3$ to $5 \times 10^4$

88 Measured water temperatures were around 20 °C throughout the experi-  
 89 mental program, with a corresponding kinematic viscosity of approximately  
 90  $10^{-6}$  m<sup>2</sup>/s. For the current experimental program, model Reynolds numbers  
 91 range from  $8 \times 10^3$  to  $5 \times 10^4$ ; flow is fully turbulent.

92 To allow comparison of results with different prototype scales,  $x$  and  $y$   
 93 positions were normalised by the pile diameter to yield  $x^*$  and  $y^*$ :

$$94 \quad x^* = \frac{x}{D} \quad (1) \quad y^* = \frac{y}{D} \quad (2)$$

95 *2.2. Data*

96 Three components of velocity were measured using a Nortek Vectrino  
 97 profiler Acoustic Doppler Velocimeter (ADV), referred to here as ‘ADV1’.  
 98 ADVs are very suitable for experimental measurements of this kind and are  
 99 widely used, (Graf and Istiarto, 2002, Qi et al., 2012). Nikora and Goring  
 100 (1998) provide a summary of their operation.

101 Detailed velocity measurements were made downstream of the model pile  
 102 under steady flow conditions, with the goal of parameterising the wake struc-  
 103 ture. Velocity time series data were recorded using ADV1 positioned along  
 104 transverse and longitudinal wake profiles (Figure 2). At each location, 500  
 105 seconds of velocity time series data were recorded at a sample frequency of  
 106 64 Hz, for each flow condition. The instrument was positioned vertically to  
 107 record point velocity within the free stream, 35 cm from the tank floor.

108 The longitudinal profile extended 2.7 m downstream of the pile centre,  
 109 with nine measurement positions spaced logarithmically along its length.  
 110 Table 2 summarises the eight transverse profiles, aligned perpendicular to  
 111 the mean flow. Values of  $x$  and  $D$  were chosen so that the eight profiles  
 112 converged to four in the  $x^*$  domain. Each profile extended 50 cm either side  
 113 of the wake centreline.

Table 2: Summary of transverse profiles

$D$	$x$	$x^*$	$\bar{u}_0$
(m)	(m)	-	(m/s)
0.1	0.25	2.5	0.08-0.18
0.1	0.50	5.0	
0.1	0.75	7.5	
0.1	1.00	10.0	
0.2	0.50	2.5	0.08-0.24
0.2	1.00	5.0	
0.2	1.50	7.5	
0.2	2.00	10.0	

114 Velocity time series data from ADV1 was used to calculate Turbulent  
 115 Kinetic Energy per unit volume ( $TKE$ ), using equation 3.

$$116 \quad TKE = \frac{1}{2}\rho(\bar{u}'^2 + \bar{v}'^2 + \bar{w}'^2) \quad (3)$$

117 Where  $u$ ,  $v$  and  $w$  are the components of velocity in the  $x$ ,  $y$  and  $z$  direc-  
 118 tions, respectively, and the apostrophe indicates the fluctuating component.  
 119  $\rho$  is the density of water. For these experiments,  $x$  is defined as the mean  
 120 flow direction,  $y$  is the other horizontal dimension perpendicular to this, and  
 121  $z$  is the vertical direction.

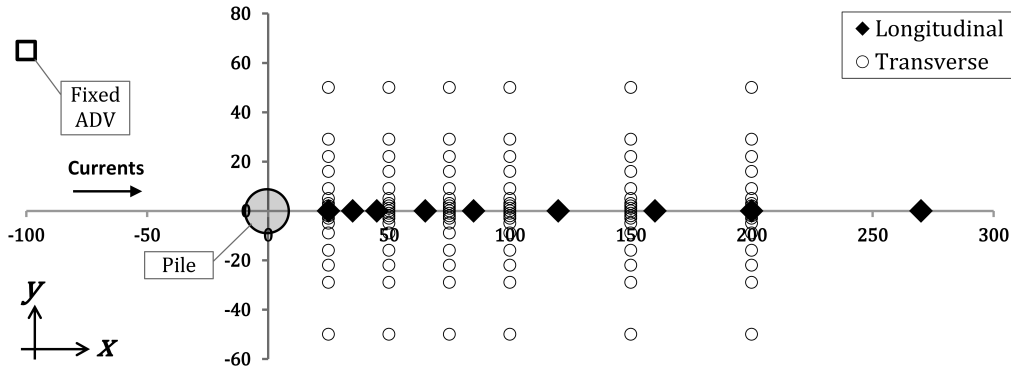


Figure 2: Experimental setup: plan view showing longitudinal and transverse measurement profiles. All dimensions in cm.

122 A point measurement ADV (Nortek Vectrino+) was used to measure the  
123 undisturbed mean flow velocity upstream of the pile ( $\bar{u}_0$ ). This instrument,  
124 referred to as ‘ADV2’, was positioned 100 cm upstream of the pile centre  
125 and +65 cm off axis. The two instruments had the same sample frequency,  
126 and were electronically synchronised to record over the same time period.  
127 Both instruments were positioned vertically so as to measure within the free  
128 stream, 35 cm from the tank floor.

### 129 *2.3. Control Measurements*

130 A series of control measurements were also made with the pile removed  
131 from the tank. These covered the same range of pump settings as used in  
132 the wake measurements. Control  $TKE$  values ( $TKE_0$ ) were calculated from  
133 the velocity time series data according to equation 3.

### 134 *2.4. Flow Conditioning*

135 Flow entering the tank passed through a flow straightener structure to  
136 minimise pump turbulence. Design of this structure was informed by the  
137 findings of Markus et al. (2015). Flow is impounded near the inlet, before  
138 passing through a bank of honeycomb blocks to enter the basin. Each block  
139 measures 0.5 m tall by 0.3 m thick by 1.25 m wide, with a bank of four  
140 blocks extending across 5.0 m of the inlet grills. The blocks are made from  
141 polycarbonate with a cell size of 12 mm diameter. Whilst Markus et al. used  
142 tubes aligned both parallel and perpendicular to the main flow direction,  
143 all of the cells in the current work were aligned parallel to the flow. Visual  
144 examination of the flow with fine seeding particles confirmed that turbulence  
145 is not significant once the flow has passed through the honeycomb.

### 146 *2.5. Data Pre-Processing*

147 In order to reduce the potential problems of instrument noise and en-  
148 sure that genuine turbulent fluctuations were identified, raw measurements  
149 were subjected to rigorous processing to ensure high quality data. Data  
150 were assessed manually to check for low correlation, low signal to noise ratio,  
151 reflections from the bed, or phase wrapping - all indications of poor measure-  
152 ment accuracy. Acceptable data were then filtered using a 3D phase space  
153 algorithm to remove noise. This technique was originally proposed by Goring  
154 and Nikora (2002), and modified by Wahl (2003). A concise description of  
155 the algorithm can be found in Mori et al. (2007).

156 *2.6. New Parameters*

157 In assessing the environmental impact of a proposed monopile founda-  
158 tion, a fundamental consideration is the increase in turbulence relative to  
159 the ambient level in the undisturbed flow ( $TKE_0$ ). To this end, a new pa-  
160 rameter is introduced to express the increased turbulence in the pile wake -  
161 the Relative Excess Turbulence ( $RET$ ):

$$162 \quad RET = \frac{TKE - TKE_0}{TKE_0} \quad (4)$$

163 Another useful parameter for impact assessment is the spatial extent of  
164 the pile's region of influence. A second new parameter is introduced to sim-  
165 plify comparisons between proposed installations. The Turbulence Recov-  
166 ery Lengthscale ( $TRL$ ) is defined as the normalised distance required down-  
167 stream, along the wake centreline, for turbulence to recover. Recovery can  
168 be considered to have taken place when  $RET$  falls below a threshold ( $\Delta$ ).

$$169 \quad TRL = x^* \quad (5)$$

170 when

$$171 \quad y^* = 0 \quad \text{and} \quad RET = \Delta$$

172 **3. Results**

173 Data from the experimental programme were analysed, with the aim of  
174 quantifying a surface that defines  $RET$  in the domain downstream of a pile  
175 in terms of  $x^*$  and  $y^*$ .

176 *3.1. Control Measurements*

177 The data from the control measurements is presented in Table 3. These  
178 values are the mean of three measurements made using ADV1 at each of  
179 four pump settings. As expected, pump power correlates with both  $\bar{u}_0$  and  
180  $TKE_0$ . Following the quadratic relationship between velocity and kinetic  
181 energy,  $TKE_0$  was normalised by  $\rho\bar{u}_0^2$ . Values of  $TKE_0/\rho\bar{u}_0^2$  show close  
182 agreement across the range of flow conditions tested, supporting this method  
183 of normalising  $TKE$ .



Table 3: Summary of control data

Pump Power (%)	$\bar{u}_0$ (m/s)	$TKE_0$ ( $\text{kg m}^{-1} \text{s}^{-2}$ )	$TKE_0/\rho\bar{u}_0^2$ -
20	0.0963	0.1289	0.0139
32	0.1531	0.3694	0.0158
40	0.1886	0.5459	0.0153
50	0.2357	0.8471	0.0153

184 *3.2. Longitudinal Characteristics*

185 Figure 3a shows measured  $TKE$  values along the centreline of the wake  
 186 downstream of the 10 cm pile, at each of the three current velocities tested.  
 187 Turbulence decays exponentially with distance downstream of the pile in  
 188 all three datasets. As expected, higher mean flow velocity correlates with  
 189 higher values of  $TKE$ . These trends were also observed downstream of the  
 190 20 cm pile. Figure 3b shows trends with similar gradients, this time for four  
 191 different velocities tested. For a given value of  $x$  at or beyond 0.5 m,  $TKE$   
 192 values associated with the larger pile are greater by a factor of approximately  
 193 two.

194  $TKE$  and  $x$  can be normalised by  $\rho\bar{u}_0^2$  and  $D$  respectively. When this  
 195 was applied, data for both pile diameters and all four mean flow velocities  
 196 collapsed towards a common relationship, as shown in Figure 4. Data nor-

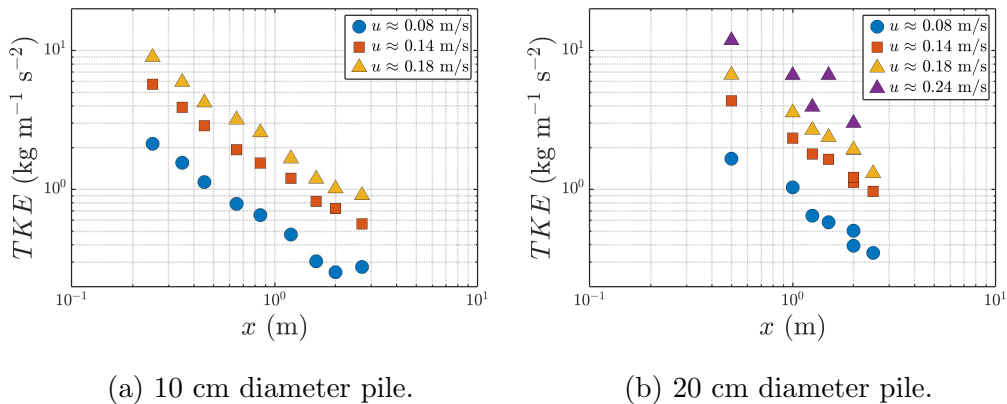


Figure 3: Centreline  $TKE$  Profiles

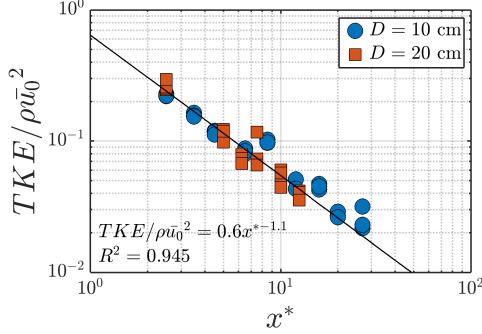


Figure 4: Normalised  $TKE$ : longitudinal profiles.  $\bar{u}_0 = 0.08$  to  $0.18$  m/s

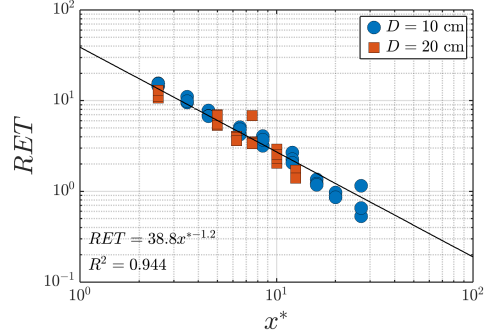


Figure 5:  $RET$ : longitudinal profiles.  $\bar{u}_0 = 0.08$  to  $0.24$  m/s

197 malised in this way were analysed using linear regression to yield equation 6,  
 198 which fits the data with an  $R^2$  of 0.945. The high  $R^2$  value indicates that the  
 199 equation is very representative of the process. This shows that turbulence  
 200 characteristics downstream of the pile centreline can be estimated using only  
 201  $\bar{u}_0$  and  $D$ , parameters that will be known at an early design stage.

$$202 \quad \frac{TKE}{\rho \bar{u}_0^2} = 0.6x^{*-1.1} \quad (6)$$

203 The wake  $TKE$  data from ADV1 were combined with undisturbed velocity  
 204 data from ADV2, to calculate  $RET$  (equation 4). When this was applied,  
 205 data for both pile diameters and all four mean flow velocities collapsed to  
 206 a single relationship (Figure 5). Equation 7 fits the measured data with  
 207 an  $R^2$  value of 0.944. Both equation 6 and equation 7 can be applied with  
 208 confidence over the experimental range of  $2.5 \leq x^* \leq 27$ .

$$209 \quad RET = 38.8x^{*-1.2} \quad (7)$$

### 210 3.3. Transverse Characteristics

211 Figure 6 shows a typical transverse profile of normalised  $TKE$ . Nor-  
 212 malised  $TKE$  was greatest along the wake's centreline, and rapidly dropped  
 213 to a constant background value on either side. Transverse  $TKE$  cross sec-  
 214 tions collapsed when normalised by mean  $\rho \bar{u}_0^2$  and  $D$ , as was the case with  
 215 the longitudinal profiles.

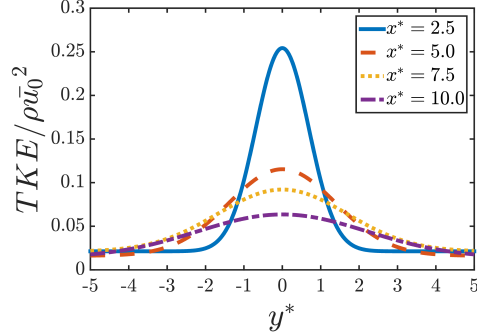
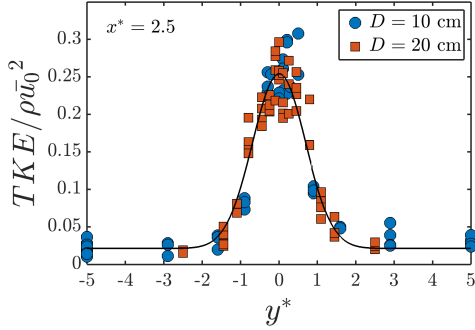


Figure 6: Normalised  $TKE$  cross section,  $2.5 D$  downstream. Data for different velocities and pile diameters collapsed to a common relationship.

Figure 7: Transverse profiles fitted to normalised  $TKE$  data at four different values of  $x^*$ . Cross sections become lower and wider with  $x^*$ .

216 The distribution of  $TKE$  in the cross sections was found to fit a function  
 217 of the form:

$$218 \quad \frac{TKE}{\rho \bar{u}_0^2} = \alpha_1 e^{-\alpha_2 y^{*2}} + \alpha_3 \quad (8)$$

219 Where  $\alpha_1$ ,  $\alpha_2$  and  $\alpha_3$  are regression constants. Non-linear regression was  
 220 used to determine the values of these constants for each of the four  $x^*$  profiles  
 221 (Table 4).

Table 4: Regression constants for normalised  $TKE$  cross sections.

$x^*$	$\alpha_1$	$\alpha_2$	$\alpha_3$	$R^2$
2.5	0.2330	1.0512	0.0212	0.9387
5.0	0.0992	0.2555	0.0162	0.7892
7.5	0.0711	0.1748	0.0209	0.5396
10.0	0.0497	0.1015	0.0138	0.5826
<i>Mean</i>	-	-	0.0180	0.7125

222 For a given cross section, the peak value of  $TKE$  is governed by the  
 223 constant  $\alpha_1$ . Given the distance downstream and the pile diameter, the  
 224 value of  $\alpha_1$  might be estimated using equation 6. Likewise, the width of the  
 225 wake is governed by the constant  $\alpha_2$ . Both constants tend towards zero as  $x^*$   
 226 increases and the wake profile becomes lower, wider and flatter (Figure 7).

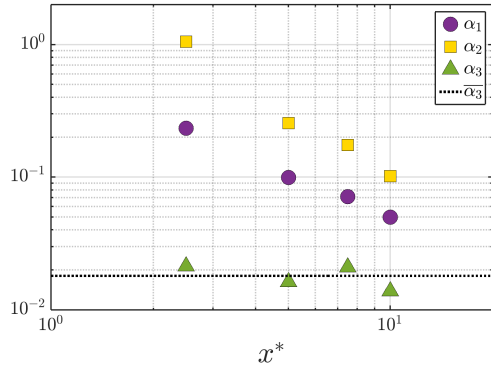


Figure 8: Regression constants  $\alpha_1$ ,  $\alpha_2$  and  $\alpha_3$  for normalised  $TKE$  cross sections.

227 Figure 8 plots the values of  $\alpha_1$ ,  $\alpha_2$  and  $\alpha_3$  against  $x^*$ , confirming the  
 228 trend identified in Table 4. Although  $\alpha_1$  and  $\alpha_2$  are constant for a given  
 229 cross section, these observations show that when considering the wake as a  
 230 whole they are functions of  $x^*$ .

231 The constant  $\alpha_3$  defines the ambient level to which turbulence decays  
 232 outside the wake. The fitted values were similar for all four cross sections.  
 233 Furthermore, the range of  $\alpha_3$  encompasses the control range of  $TKE_0/\rho\bar{u}_0^2$   
 234 presented in Table 3, with similar mean values.

235 Figure 9 plots  $RET$  against  $y^*$ , for each of the four values of  $x^*$  tested.  
 236 Each plot represents two different pile diameters and four different flow ve-  
 237 locities. As with the longitudinal profiles, the data collapse very well when  
 238 normalised in this way. Peak  $RET$  occurs along the centreline. The shape  
 239 of the wake becomes lower, flatter and wider as  $x^*$  increases.

Table 5: Regression constants for  $RET$  cross sections.

$x^*$	$\beta_1$	$\beta_2$	$R^2$
2.5	14.1747	0.9429	0.9309
5.0	6.7866	0.3028	0.8332
7.5	5.1888	0.1657	0.5292
10.0	2.8917	0.0928	0.4760
<i>Mean</i>	-	-	0.6923

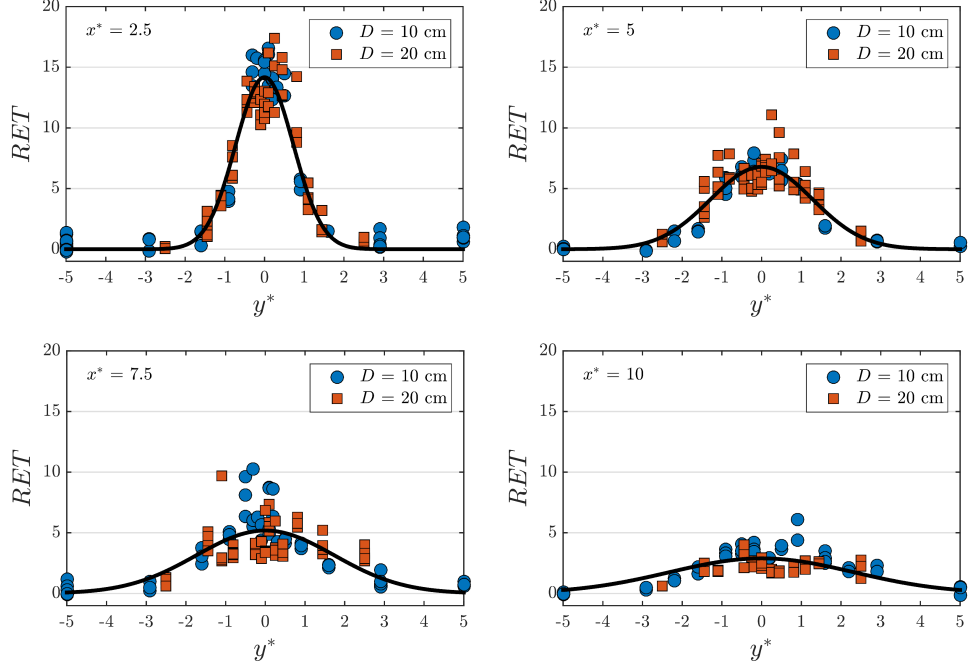


Figure 9:  $RET$  - transverse cross sections at different values of  $x^*$ . Black lines indicate equation 9 fitted to the measured data. Profiles become lower, flatter and wider as  $x^*$  increases.

240 Average  $RET$  values recover to approximately zero at the boundaries of  
 241 the wake. This allows equation 8 to be simplified to give equation 9:

242 
$$RET = \beta_1 e^{-\beta_2 y^{*2}} \quad (9)$$

243 Table 5 summarises the fitting of experimental data to this relationship.  
 244 As with Table 4, the values of the constants tend towards zero as  $x^*$  increases.  
 245 The general trend in both tables is for  $R^2$  to reduce with increasing values  
 246 of  $x^*$ . This might be attributed to the increasing influence of measurement  
 247 error as the turbulence signal decreases. Figure 9 indicates that equation 9  
 248 predicts the mean  $RET$  values at the crest of each profile.

### 249 3.4. Empirical model

250 Following the observations made in sections 3.2 and 3.3, a unifying rela-  
 251 tionship was sought to describe the distribution of turbulence over the entire

252 domain. The validity of such a relationship follows from dimensional analysis  
 253 of the parameters. As the peak *RET* in a given cross section occurs along  
 254 the centreline,  $\beta_1$  can be expressed by a term of the same form as equation  
 255 7;  $\beta_1 = \gamma_1 x^{*- \gamma_2}$ , where  $\gamma_1$  and  $\gamma_2$  are constants. Table 5 suggests an inverse  
 256 relationship between  $x^*$  and  $\beta_2$ , and so the term  $\gamma_3/x^*$  is substituted for  $\beta_2$ ,  
 257 where  $\gamma_3$  is a constant. *RET* can now be expressed in terms of both  $x^*$  and  
 258  $y^*$ :

$$259 \quad RET = \gamma_1 x^{*- \gamma_2} e^{-\frac{\gamma_3 y^{*2}}{x^*}} \quad (10)$$

260 Using non-linear regression, equation 10 was fit to the measured data to  
 261 yield the constants  $\gamma_1$ ,  $\gamma_2$  and  $\gamma_3$ . Equation 10 is valid with these constants  
 262 for the range of experimental values,  $2.5 \leq x^* \leq 27$  and  $-5 \leq y^* \leq 5$ .

$$\gamma_1 = 33.949$$

$$\gamma_2 = 0.9761$$

$$\gamma_3 = 1.9967$$

263 Along the centreline of the wake,  $\gamma_1$  and  $\gamma_2$  are analogous and similar in  
 264 magnitude to the fitted constants in equation 7, which gives confidence in  
 265 the result.

266 Figure 10 plots the measured data over the entire domain, against a sur-  
 267 face defined by the empirical relationship. Measured *RET* agrees closely with  
 268 calculated values. The function successfully explains both the exponential  
 269 decay of *RET* along the wake centreline and the spreading of the wake with  
 270 distance downstream.

271 Figure 11 plots the measured values of *RET* against those predicted using  
 272 equation 10 and the fitted values of  $\gamma_1$ ,  $\gamma_2$  and  $\gamma_3$ . Predicted values were found  
 273 to fit measured data with an  $R^2$  of 0.874. 23% of predicted values are within  
 274  $\pm 10\%$  of the measured data, with 70% falling within  $\pm 50\%$ .

### 275 3.5. Outputs

276 Equation 10 allows the calculation of *TRL* along the wake centreline.  
 277 By setting  $y^*$  equal to zero and *RET* equal to  $\Delta$ ,  $\gamma_3$  is eliminated and the  
 278 equation simplifies:

$$279 \quad \gamma_1 x^{*- \gamma_2} = \Delta \quad (11)$$

$$280 \quad x^* = e^{\frac{\ln \frac{\gamma_1}{\Delta}}{\gamma_2}} = TRL \quad (12)$$

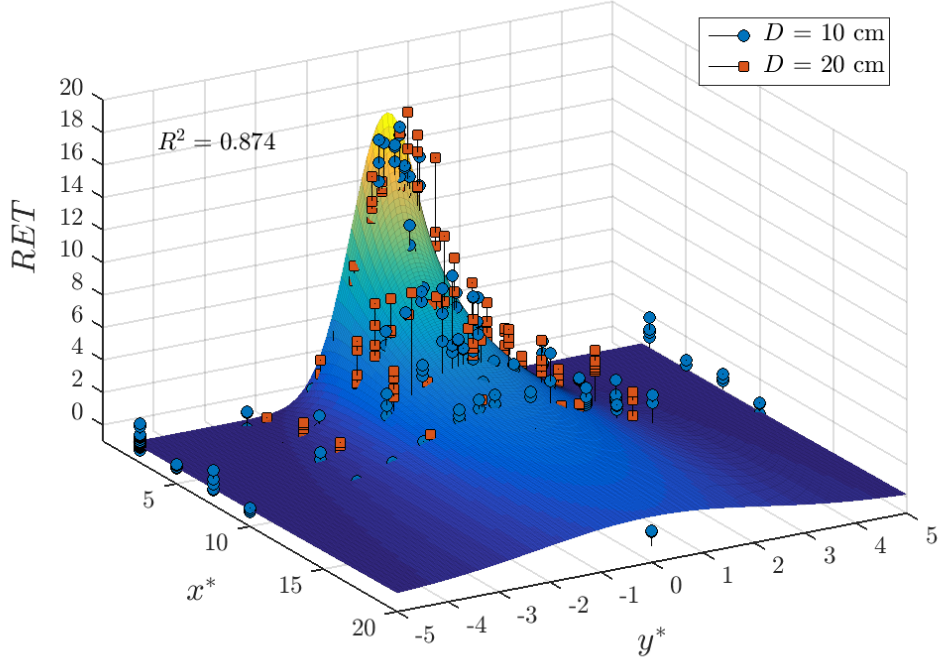


Figure 10: Distribution of Residual Excess Turbulence ( $RET$ ), against normalised distance downstream ( $x^*$ ) and off axis ( $y^*$ ) from the pile centre. Measured values against a surface defined by equation 10.

282 The value of the threshold  $\Delta$  is arbitrary in this definition, and differ-  
 283 ent values may be specified according to the purpose of the analysis. Two  
 284 examples serve to illustrate this point:

285 Given a receptor or process that is insensitive to variations in turbulence,  
 286  $\Delta$  might be set equal to 1.0. This implies  $TKE$  is twice that of the ambi-  
 287 ent conditions, and might signify that turbulence has returned to its original  
 288 order of magnitude. Inputting these values into equation 12 yields a value  
 289 of 37.01 for  $TRL$ , or approximately 40. Given a typical prototype diameter  
 290 of 5 m, this corresponds to a distance of 200 m. From an engineering per-  
 291 spective, 200 m is less than typical turbine spacing in existing and planned  
 292 offshore windfarms;  $RET$  will decay below a value of 1.0 before reaching a  
 293 neighbouring monopile.

294 If instead the process of interest is highly sensitive to changes in turbu-

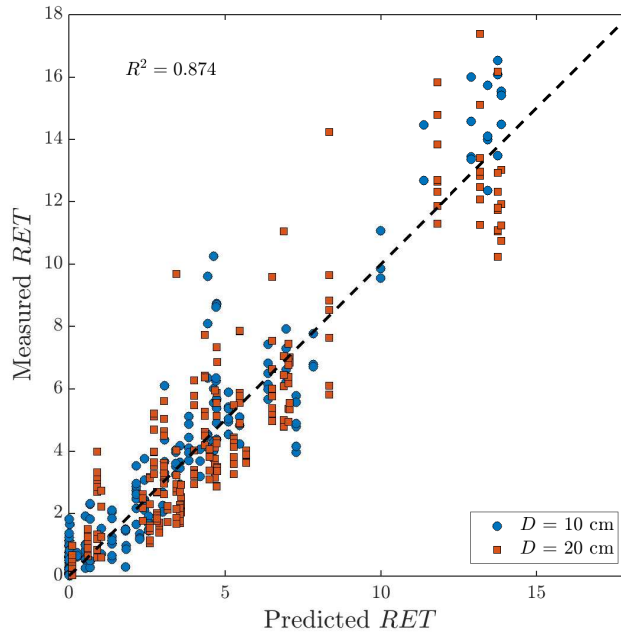


Figure 11:  $RET$  downstream of the pile. Measured values vs values predicted using equation 10.

295 lence, a value of 0.1 might be specified for the threshold  $\Delta$ . This implies  
 296 that  $TKE$  has decayed to only 10% above the ambient conditions - a much  
 297 tighter specification than above. Using this new threshold  $TRL$  is calculated  
 298 at 391.6, or approximately 400. This corresponds to 2,000 m downstream for  
 299 a typical 5 m diameter prototype, which is greater than typical pile spacing;  
 300  $RET$  will exceed 0.1 when the wake reaches the next pile downstream.

#### 301 4. Discussion

302 Model velocities covered the range from 0.08 to 0.24 m/s. These model  
 303 values represent prototype current velocities of 0.57 to 1.70 m/s, which are  
 304 typical of peak velocities measured at existing wind farms (Matutano et al.,  
 305 2013). The data may even be applicable to some less energetic tidal energy  
 306 sites.



307 Two pile diameters were tested during the experimental programme. The  
308 0.1 m model pile scales to a typical 5 m diameter prototype in a transitional  
309 water depth of 25 m. At the same scale, the 0.2 m pile represents a 10 m  
310 diameter prototype. This is significantly larger than the largest wind tur-  
311 bine monopiles currently being proposed, but may represent other types of  
312 offshore structure. In spite of this disparity in scale, *RET* values collapsed  
313 successfully (Figure 5, Figure 9, Figure 11). This suggests that the relation-  
314 ships identified hold true for the range of pile diameters scaled to represent  
315 existing and proposed offshore wind farms.

316 In general, the proposed equations were found to represent the data well.  
317 One group of *RET* values were found to lie above the main cluster of data in  
318 the cross section at  $x^* = 7.5$  (Figure 9). Closer examination did not reveal  
319 any underlying cause for this group of points. Despite these anomalous data,  
320 the range of *RET* values at the centre of the cross section is approximately  
321 8, which is similar to the range of *RET* values shown in the cross sections at  
322  $x^* = 2.5$  and  $x^* = 5$ .

323 The findings indicate that turbulence affects a substantial region down-  
324 stream of the pile, showing that turbulence is a much larger scale problem  
325 than scour. Changes to the turbulent characteristics of the flow may be  
326 significant for mixing, and could affect primary productivity and marine bio-  
327 diversity in the region of the pile (Kocum et al., 2002).

328 This is in good agreement with the findings of Vanhellemont and Ruddick  
329 (2014), who reported turbid plumes 30 to 150 m wide, extending for several  
330 kilometres downstream of wind farms. Translating *RET* values into quanti-  
331 ties of suspended particulate matter would require data on the characteristics  
332 of the suspended material and the ambient conditions at a specific site, as  
333 proposed by Rivier et al. (2014). However, heightened *TKE* at this distance  
334 from the pile will enhance the carrying capacity of the flow, and contribute  
335 to the persistence of the observed plumes.

336 Prototype pile spacing within existing and planned wind farms is typically  
337 500 to 1,000 m, with pile diameters of around 5 m. Given these dimensions,  
338 the *TRL* values estimated in section 3.5 imply that the *RET* reaching a  
339 monopile from its upstream neighbour will be somewhere between 1.0 and 0.1.  
340 This is small compared to the estimated *RET* of 33.9 at  $x^* = 1.0$  downstream  
341 of an individual pile (equation 10). These observations suggest that monopile  
342 foundations will behave as individuals with respect to turbulence in the pile  
343 wake, and group effects are expected to be small.

## 344 5. Conclusion

345 A detailed experimental programme was carried out in a laboratory to  
346 assess the levels of turbulence in the wake of a monopile foundation. TKE  
347 measurements were made up to 27 diameters downstream of the pile. Tur-  
348 bulence along the wake centreline was found to decay exponentially with  
349 distance downstream.

350 In this work, two new parameters have been introduced for characterising  
351 the turbulence downstream of a monopile foundation: the Relative Excess  
352 Turbulence (*RET*) and the Turbulence Recovery Lengthscale (*TRL*). These  
353 parameters will be useful for assessing the likely impact of monopile founda-  
354 tions on local flow conditions. Experimental data were used to infer *TRL*  
355 values of 40 pile diameters for an *RET* threshold of 1.0, or 400 pile diameters  
356 for an *RET* threshold of 0.1.

357 Profiles of turbulence across the wake fitted a Gaussian function. The  
358 lateral extent of the pile's impact increased with distance downstream of the  
359 pile. Measurements of TKE outside the wake were similar to ambient values.

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## 368 References

- 369 Abrahams, M. and Kattenfeld, M. (1997), 'The role of turbidity as a  
370 constraint on predatory-prey interactions in aquatic environments.', *Be-*  
371 *havioural Ecology and Sociobiology* **40**, 169 – 174.
- 372 Achmus, M., Abdel-Rahman, K. and Kuo, Y.-S. (2008), Design of Monopile  
373 Foundations for Offshore Wind Energy Converters, *in* '11th Baltic Sea  
374 Geotechnical Conference', Gdansk.

- 375 Benoit, M., Lafon, F. and Goasguen, G. (2008), ‘Constitution et exploita-  
376 tion d’une base de données d’états de mer le long des côtes françaises par  
377 simulation numérique sur 23 ans’, *European Journal of Environmental and*  
378 *Civil Engineering* **12**(February 2015), 35–50.
- 379 Butt, T., Russell, P., Puleo, J., Miles, J. and Masselink, G. (2004), ‘The  
380 influence of bore turbulence on sediment transport in the swash and inner  
381 surf zones’, *Continental Shelf Research* **24**, 757–771.
- 382 Byrne, B. W. and Houlby, G. T. (2003), ‘Foundations for offshore wind  
383 turbines’, *Philosophical Transactions of The Royal Society* **361**, 2909–2930.
- 384 Dargahi, B. (1989), ‘The turbulent flow field around a circular cylinder’,  
385 *Experiments in Fluids* **12**, 1–12.
- 386 DECC (2013), UK Renewable Energy Roadmap, Technical Report Novem-  
387 ber, Department of Energy and Climate Change.
- 388 Esteban, M. D., Diez, J. J., López, J. S. and Negro, V. (2011), ‘Why offshore  
389 wind energy?’, *Renewable Energy* **36**(2), 444–450.
- 390 EWEA (2015), The European offshore wind industry - key trends and statis-  
391 tics 2014, Technical Report January, European Wind Energy Association.
- 392 García-Hermosa, I., Brossard, J., Cohen, Z., Perret, G., Pinon, G., Abcha,  
393 N., Bennis, A. C., Ezersky, A., Mouazé, D., Rivier, A., Iglesias, G., Miles,  
394 J., Rogan, C., Simmonds, D., Gross, M. and Magar, V. (2014), Experi-  
395 mental characterisation of wave induced flow fields due to an offshore wind  
396 farm mast, *in* ‘Proceedings of the 1st International Conference on Renew-  
397 able Energies Offshore’, Lisbon.
- 398 Gerace, A. D., Schott, J. R. and Nevins, R. (2013), ‘Increased potential to  
399 monitor water quality in the near-shore environment with Landsat’s next-  
400 generation satellite’, *Journal of Applied Remote Sensing* **7**, 073558–1 –  
401 073558–18.
- 402 Goring, D. G. and Nikora, V. I. (2002), ‘Despiking acoustic doppler velocime-  
403 ter data’, *Journal of Hydraulic Engineering* **128**(1), 117–126.
- 404 Graf, W. H. and Istiarto, I. (2002), ‘Flow pattern in the scour hole around  
405 a cylinder Écoulement dans une fosse autour d’un cylindre’, *Hydraulic*  
406 *Research* **40**(1), 13–20.

- 407 Gyr, A. and Hoyer, K. (2006), *Sediment Transport*, Springer.
- 408 Kocum, E., Underwood, G. J. C. and Nedwell, D. B. (2002), ‘Simultaneous  
409 measurement of phytoplanktonic primary production, nutrient and light  
410 availability along a turbid, eutrophic UK east coast estuary (the Colne  
411 Estuary)’, *Marine Ecology Progress Series* **231**, 1–12.
- 412 Magar, V., Abcha, N., Bennis, A., Brossard, J., Conley, D., Ellis, E., Ezer-  
413 sky, A., Greaves, D., Gross, M. S., Iglesias, G., Littlewood, K., Miles,  
414 J., Mouazé, D., Perret, G., Pinon, G. and Simmonds, D. J. (2013),  
415 Laboratory-Scale Environmental Impact Assessment of a Monopile Founda-  
416 tion under Different Wave Conditions, *in* ‘EWEA Offshore 2013’, pp. 1–  
417 9.
- 418 Markus, D., Jakobsen, M., Bletzinger, K.-U. and Frigaard, P. (2015), ‘Damp-  
419 ing of unwanted turbulence in wave-current experiments’, *Coastal Engi-  
420 neering* **96**, 38–48.
- 421 Matutano, C., Negro, V., López-Gutiérrez, J.-S., Esteban, M. D. and del  
422 Campo, J. M. (2013), ‘Dimensionless wave height parameter for prelimi-  
423 nary design of scour protection in offshore wind farms’, *Journal of Coastal  
424 Research* **29**(65), 1633–1638.
- 425 McGovern, D. J., Ilic, S., Folkard, A. M., McLelland, S. J. and Murphy, B. J.  
426 (2014), ‘Time development of scour around a cylinder in simulated tidal  
427 currents’, *Journal of Hydraulic Engineering* **140**(6).
- 428 Mori, N., Suzuki, T. and Kakuno, S. (2007), ‘Noise of acoustic doppler  
429 velocimeter data in bubbly flows’, *Journal of engineering mechanics*  
430 **133**(1), 122–125.
- 431 Nikora, V. and Goring, D. (1998), ‘ADV measurements of turbulence: Can  
432 we improve their interpretation?’, *Journal of Hydraulic Engineering* .
- 433 Qi, W., Gao, F., Han, X. and Gong, Q. (2012), Local scour and pore-water  
434 pressure around a monopile foundation under combined waves and cur-  
435 rents, *in* ‘Proceedings of the Twenty-second International Offshore and  
436 Polar Engineering Conference’, Rhodes, pp. 159–165.

- 437 Rivier, A., Bennis, A. C., Pinon, G., Gross, M. and Magar, V.  
438 (2014), ‘Modelisation numerique regionale de l’impact des eoliennes off-  
439 shore sur l’hydrodynamique et le transport sedimentaire’, *Journées de*  
440 *l’hydrodynamique* **14**.
- 441 Roulund, A., Sumer, B. M., Fredsøe, J. and Michelsen, J. (2005), ‘Numerical  
442 and experimental investigation of flow and scour around a circular pile’,  
443 *Journal of Fluid Mechanics* **534**, 351–401.
- 444 Sumer, B., Christiansen, N. and Fredsøe, J. (1997), ‘The horseshoe vortex  
445 and vortex shedding around a vertical wall-mounted cylinder exposed to  
446 waves’, *Journal of Fluid Mechanics* **332**, 41–70.
- 447 Sumer, B., Whitehouse, R. J. and Tørum, A. (2001), ‘Scour around coastal  
448 structures: a summary of recent research’, *Coastal Engineering* **44**(2), 153–  
449 190.
- 450 Unger, J. and Hager, W. H. (2006), ‘Down-flow and horseshoe vortex char-  
451 acteristics of sediment embedded bridge piers’, *Experiments in Fluids*  
452 **42**(1), 1–19.
- 453 Vanhellemont, Q. and Ruddick, K. (2014), ‘Turbid wakes associated with  
454 offshore wind turbines observed with Landsat 8’, *Remote Sensing of Envi-*  
455 *ronment* **145**, 105–115.
- 456 Wahl, T. (2003), ‘Discussion of Despiking acoustic doppler velocimeter data  
457 by Derek G. Goring and Vladimir I. Nikora’, *Journal of Hydraulic Engi-*  
458 *neering* **128**(1), 484–488.
- 459 Weiffen, M., Möller, B., Mauck, B. and Dehnhardt, G. (2006), ‘Effect of water  
460 turbidity on the visual acuity of harbor seals (*Phoca vitulina*)’, *Vision*  
461 *Research* **46**, 1777–1783.
- 462 Whitehouse, R. J. S., Harris, J. M., Sutherland, J. and Rees, J. (2011), ‘The  
463 nature of scour development and scour protection at offshore windfarm  
464 foundations.’, *Marine pollution bulletin* **62**(1), 73–88.
- 465 Yin, Y., Christie, E., Li, M., Moulinec, C. and Emerson, D. (2014), ‘3d  
466 morphological impact modelling of offshore wind farms using les and hpc’,  
467 *Coastal Engineering Proceedings* **1**(34), sediment–48.