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4 Species-Occupancy Distribution Removes Excessive Parameter from Species-Area Relationship

5 **Short Title:**

6 SOD removes excessive SAR Parameter

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23 **ABSTRACT**

24 **Aim** Although species-occupancy distributions (SODs) and species-area relationships (SARs)
25 arise from the two marginal sums of the same presence/absence matrices, the two biodiversity
26 patterns are usually explored independently. Here, we aim to unify the two patterns for isolate-
27 based data by constraining the SAR to conserve information from the SOD.

28 **Location** Widespread

29 **Methods** Focusing on the power-model SAR, we first developed a constrained form that
30 conserved the total number of occupancies from the SOD. Next, we developed an additive-
31 constrained SAR that conserve the entire shape of the SOD within the power-model SAR
32 function, using a single parameter (the slope of the endemics-area relationship). We then relate
33 this additive-constrained SAR to multiple-sites similarity measures, based on a probabilistic view
34 of Sørensen similarity. We extend the constrained and additive-constrained SAR framework to
35 23 published SAR functions. We compare the fit of the original and constrained forms of 12
36 SAR functions using 154 published datasets, covering various spatial scales, taxa and systems.

37 **Main conclusions** In all 23 SAR functions, the constrained form had one parameter
38 less than the original form. In all 154 datasets the model with the highest weight based on the
39 corrected Akaike Information Criteria (wAICc) had a constrained form. The constrained form
40 received higher wAICc than the original form in 98.79% of valid pairwise cases, approaching the
41 wAICc expected under identical log-likelihood. Our work suggests, both theoretically and
42 empirically, that all SAR functions may have one unnecessary parameter, which can be excluded
43 from the function without reduction in goodness-of-fit. The more parsimonious constrained
44 forms are also easier to interpret as they reflect the probability of a randomly chosen occupancy

45 to be found in an isolate. The additive-constrained SARs accounts for two complimentary turn-
46 over components of occupancies: turnover between species and turnover between sites.

47

48 **Keywords** Biodiversity patterns; islands; Jaccard; landscape; macroecology; multiple-sites
49 similarity; Sørensen; spatial ecology; occupancy-frequency distribution; patches.

50

51 INTRODUCTION

52 Studying biodiversity distribution patterns characterizes a major exploration line in
53 contemporary ecology due to both basic and applied needs. This exploration requires
54 biodiversity data collection of diverse species located at different spatial extents. Consequently,
55 most biodiversity studies end up with a species-by-site table filled with presence/absence data
56 (hereafter we refer to a presence of a species in a site as occupancy). Summing this community
57 matrix for each site over all species yields the total number of species sampled within each site
58 (Fig. 1A). Similarly, when summed for each species over all sites, the marginal sums yield the
59 number of sites in which a species occurred (i.e., the species occupancy level). These two sets of
60 marginal sums give rise to two important biodiversity patterns -- the species occupancy
61 distribution (SOD, the number of species that occurred in each occupancy level, e.g. McGeoch &
62 Gaston, 2002; Jenkins, 2011) and the species-area relationship (SAR, the change in species
63 richness with a change in area).

64 SARs and SODs can be constructed from data collected in various ways, including nested
65 quadrats, quadrats in a contiguous grid, quadrats in a non-contiguous grid, and non-overlapping
66 areas of various sizes (types I-IV sensu Scheiner, 2003, respectively). Here we focus on type IV
67 SARs, and following Tjørve & Turner (2009), we refer to the sites as isolates (non-overlapping

68 sites with biologically or environmentally defined borders that differ from one another in various
69 attributes such as area, shape, heterogeneity and spatial context). Most SOD studies focused on
70 contiguous or non-contiguous equal-sized quadrat (type II or III), in which SOD shape is highly
71 dependent upon the choice of grain size, while type IV SOD, on which we focus here, has the
72 advantage of working on naturally occurring grains: the isolates. Despite numerous studies of
73 SARs in island-like systems, we are not aware of any manuscript that focused on type IV SODs.

74 Indeed, among the two biodiversity patterns, SARs have received the most attention, with at
75 least 23 mathematical functions suggested to describe the pattern (Tjørve, 2003, 2009; Williams
76 *et al.*, 2009). In fact, SARs are one of the most fundamental patterns of ecology. Empirically,
77 SARs have been explored in numerous study systems, covering a wide range of scales, focusing
78 on diverse taxa, and using various methods (Rosenzweig, 1995; Scheiner, 2003; Drakare *et al.*,
79 2006; Triantis *et al.*, 2012). SARs exhibit a consistent pattern: the number of species increases
80 with area, thus considered as a general law of ecology (Rosenzweig, 1995). SARs have also been
81 the subject of extensive theoretical research, either aiming to explain their properties or as a
82 starting rule from which other patterns emerge (e.g., Rosenzweig & Ziv, 1999). The generality
83 and centrality of SARs triggered their usage in applied ecology. Among others, SARs are used to
84 estimate extinction debts (Brooks *et al.*, 2002; Kuussaari *et al.*, 2009), identify biodiversity
85 hotspots (Myers *et al.*, 2000; Gavish, 2011), and optimize reserve design (Bascompte *et al.*,
86 2007; Tjørve, 2010; Gavish *et al.*, 2012).

87 In contrast, SODs remained relatively unexplored, perhaps due to the complexity of shapes
88 they can take. Unlike SARs, which are usually described by convex functions with no asymptote
89 (Triantis *et al.*, 2012), SODs may be unimodal, bimodal, random, or uniform, and their modes
90 may occur for satellite (rare), central, or core (common) species (McGeoch & Gaston, 2002;

91 Jenkins, 2011; Hui, 2012). Furthermore, bimodal SODs may be symmetrical or asymmetrical,
92 and if asymmetric they may have a stronger or weaker mode for rare or common species. Until
93 recently, only one method (Tokeshi, 1992), based on comparison of the size of the satellite and
94 core modes to an expected null model, was used to describe SOD's shape. Recently, Jenkins
95 (2011) introduced the ranked species-occupancy curves (rSOC) as an alternative method and Hui
96 (2012) clarified the direct link between the two patterns. Similar to species-abundance
97 distribution and ranked abundance curves, SOD and rSOC are two alternative ways to present
98 the same information.

99 Although SODs and SARs arise from the two marginal sums of the same presence/absence
100 table, the two patterns were rarely explored simultaneously (but see: Hui & McGeoch, 2014;
101 Pan, 2015). In fact, in most cases they were explored simultaneously only when both were
102 derived from species abundance data, either through null models (Coleman, 1981), neutral
103 models (Hubbell, 2001), or metapopulation-based models (Ovaskainen & Hanski, 2003). The
104 aim of this paper is to develop the direct link between SODs and SARs for island-like systems
105 within a single framework. Within this framework, the shape of the SOD itself can be explored
106 in relation to species traits, thereby providing a more mechanistic understating of the SAR.
107 Furthermore, mechanistic SAR hypotheses such as the transient hypothesis (MacArthur &
108 Wilson, 1967), rescue effects (Brown & Kodric-Brown, 1977), target area effects (Gilpin &
109 Diamond, 1976) and small island effects (Lomolino, 2000), are mediated through changes in
110 species occupancy levels.

111

112 **MATERIAL AND METHODS**

113 **Mathematical developments**

114 We develop the direct link between SOD and SAR by constraining the SAR to conserve the data
115 encompassed by the SOD. Starting with the power-model (Arrhenius, 1921), we first developed
116 the constrained-SAR model, by forcing the SAR to conserve the observed total number of
117 occupancies (thereby canceling-out one of the power-model parameters). Then, in the additive-
118 constrained SAR model, we fit a separate constrained-SAR model to the species of each
119 occupancy level, and then sum the results over all occupancy levels. By describing the change in
120 SAR parameters with occupancy level we provide a novel one-parameter SAR function that
121 predicts not only the shape of the global SAR, but also the SAR of each occupancy level, while
122 conserving the entire shape of the SOD. The parameter of this additive model is the slope of the
123 endemics area relationship. Subsequently, we relate the SOD to multiple-sites similarity indices
124 and generalize to 23 known SAR functions.

125 **The power-model SAR**

126 We start with a presence/absence matrix of M species in N isolates (Fig. 1A, see notations in Fig.
127 1F). Each species is notated with m (in the range $\{1,2,\dots,M\}$), each isolate with i $\{1,2,\dots,N\}$ and
128 each entry as $O_{i,m}$ (that can take the value of 1 or 0). The observed number of species in isolate i
129 (hereafter, S_i) is the sum of $O_{i,m}$ over all M species, and if A_i is the area of isolate i , the global
130 SAR can be constructed (Fig. 1D). The occupancy level of species m (hereafter, j_m) is the sum of
131 $O_{i,m}$ over all N isolate (thus j_m is in the range $\{1,2,\dots,N\}$). The SOD explores how the number of
132 species in occupancy level j (hereafter R_j) changes with j (Fig. 1C). Thus, summing R_j over all
133 occupancy levels (all j in the range $\{1,2,\dots,N\}$) yields M . The presence/absence matrix can be
134 restructured as a square $N \times N$ matrix, with the number of presences from each occupancy-level
135 that were found in each isolate (hereafter $S_{i,j}$, Fig. 1B). The total number of occupancies can be

136 estimated in three ways: by summing $O_{i,m}$ over all M species, by summing S_i over all N isolates,
 137 and by summing $j \cdot R_j$ over all occupancy levels.

138 Given the observed S_i and A_i , the original power-model SAR (Arrhenius, 1921) takes the form:

$$139 \quad E(S_i)_{orig.} = c \cdot A_i^z \quad (E1)$$

140 With $E(S_i)_{orig.}$ as the number of species predicted for isolate i by the power-model AND c and z
 141 as scaling parameters. The total number of occupancies predicted by the power-model is the sum
 142 of equation 1 over all n isolates. To constrain the power-model SAR such that it will conserve
 143 the observed total number of occupancies, we set $\sum_j(j \cdot R_j) = \sum_i c \cdot A_i^z$ and multiply equation 1 by

$$144 \quad \sum_j(j \cdot R_j) / \sum_i c \cdot A_i^z:$$

$$145 \quad E(S_i)_{cons.} = c \cdot A_i^z \times \frac{\sum_{j=1}^N (j \cdot R_j)}{\sum_{i=1}^N (c \cdot A_i^z)} = \sum_{j=1}^N (j \cdot R_j) \cdot \frac{A_i^z}{\sum_{i=1}^N A_i^z} \quad (E2)$$

146 with $E(S_{i,j})_{cons.}$ being the expected number of species in isolate i according to the constrained
 147 power-model. Adding the total number of occurrences constraint to the power-model SAR
 148 eliminates parameter c , which allows the predicted sum of occupancies to differ from the
 149 observed one, leaving only parameter z . Furthermore, $A_i^z / \sum_i A_i^z$ is the probability of a single
 150 occupancy to be found in isolate i . Although this constrain can be employed with no knowledge
 151 of the SOD, we base it on the SOD's arguments to exemplify the effect of focusing only on
 152 species from a single occupancy level. In fact, when equation 2 is fitted only to the subset of
 153 species from occupancy level j (Fig. 1E), we get:

$$154 \quad E(S_{i,j})_{cons.} = (j \cdot R_j) \cdot \frac{A_i^{z_j}}{\sum_{i=1}^n A_i^{z_j}} \quad (E3)$$

155 with $E(S_{i,j})_{cons.}$ being the expected number of species from occupancy level j in isolate i , and z_j
 156 the slope of the SAR of occupancy level j . If we assume that the SAR of all occupancy levels can

157 be described by a power-model (see below) then equation 3 can be summed to produce a second
 158 approximation of the global SAR:

$$159 \quad E(S_i)_{add.cons.} = \sum_{j=1}^N [(j \cdot R_j) \cdot \frac{A_i^{z_j}}{\sum_{i=1}^N A_i^{z_j}}] \quad (E4)$$

160 with $E(S_i)_{add.cons.}$ being the expected number of species in isolate i according to the additive-
 161 constrained power-model. We are not aware of any publication that explores the change of z_j
 162 with j , which we term ‘ z -occupancy curves’. However, endemics-area relationships (the SAR
 163 when including only species that are endemic to a single isolate, i.e., $j=1$) usually have relatively
 164 high z_j values (Rosenzweig, 1995; Triantis *et al.*, 2008). Eventually, z_j values for $j=N$ are, by
 165 definition, zero (the species occur on all isolates, Fig. 1E)). In addition, equation 2 and 3 can
 166 estimate the maximal value of z that will ensure that none of the isolates contains more species
 167 than the actual size of the species pool ($\sum_j R_j$), or the number of species in occupancy level j (R_j),
 168 denoted as z_{max} and $z_{j,max}$, respectively. When setting the monotonically increasing (for $z>0$)
 169 equation 2 and 3 to equal $\sum_j R_j$ or R_j (respectively) and solving for the largest isolate (here, isolate
 170 $i=N$) we get:

$$171 \quad \frac{A_N^{z_{max}}}{\sum_{i=1}^N A_i^{z_{max}}} = \frac{\sum_{j=1}^N R_j}{\sum_{j=1}^N (j \cdot R_j)} \quad (E5)$$

$$172 \quad \frac{A_N^{z_{j,max}}}{\sum_{i=1}^N A_i^{z_{j,max}}} = \frac{R_j}{(j \cdot R_j)} = \frac{1}{j} \quad (E6)$$

173 This means that z_{max} is the value of z for which the probability of randomly drawn occupancy to
 174 be in the largest isolate equals the inverse of the mean occupancy level. Although z_j is
 175 unbounded for $j=1$, z_j of all other occupancy levels have a maximal value ($z_{j,max}$) that is
 176 independent of the number of species and depends mainly on the area distribution (A_i values,
 177 equation 6). The maximal values result in a decreasing function when plotting $z_{j,max}$ against j .

178 Therefore, we expect z_j to decrease with j in a predictable manner, according to a function $F(z_j|j)$
 179 that intersects the abscissa at $j=n$. Consequently, we get:

$$180 \quad E(S_i)_{add.cons.} = \sum_{j=1}^N [(j \cdot R_j) \cdot \frac{A_i^{F(z_j|j)}}{\sum_{i=1}^N A_i^{F(z_j|j)}}] \quad (E7)$$

181 Although various functions may describe the shape of the z -occupancy curve, we focused here
 182 on the form given in equation 8, and when plugging it into equation 7 we get:

$$183 \quad F(z_j|j): \quad z_j = a \cdot (1 - \log_N j) \quad (E8)$$

$$184 \quad E(S_i)_{add.cons.} = \sum_{j=1}^N \left[(j \cdot R_j) \cdot \frac{A_i^{a \cdot (1 - \log_N j)}}{\sum_{i=1}^N A_i^{a \cdot (1 - \log_N j)}} \right] \quad (E9)$$

185 We chose equation 8 for three main reasons. First, it is an exponential decay function $z_j = a - b \cdot \ln(j)$
 186 that intersects the point $(N, 0)$ (such that $b = a / \ln(N)$), and thus always predict z_j values of 0 when
 187 $j = N$. Second, preliminary analysis of several datasets revealed it to be a good candidate model.
 188 Third, its only parameter (a) is biologically meaningful- it is the z value of the endemic-area
 189 relationship. In fact, equation 9 is a SAR function that incorporates the entire observed shape of
 190 the SOD into the SAR, provides predictions for the overall SAR, as well as for the SAR of each
 191 occupancy level and has a single, ecologically-meaningful parameter (a). Other $F(z_j|j)$ functions
 192 with more complex shapes or with better theoretical grounds can be developed, perhaps after
 193 more detailed exploration of the shape of z -occupancy curves is carried.

194 Finally, if the constrained and additive-constrained model provide comparable predictions,
 195 and equation 2 and 9 are divided by the total number of occupancies, we get:

$$196 \quad \frac{S_i}{\sum_{j=1}^N [(j \cdot R_j)]} = \frac{A_i^z}{\sum_{i=1}^n A_i^z} \cong \sum_{j=1}^N \left[\left(\frac{j \cdot R_j}{\sum_{j=1}^N [(j \cdot R_j)]} \right) \cdot \left(\frac{A_i^{a \cdot (1 - \log_N j)}}{\sum_{i=1}^N A_i^{a \cdot (1 - \log_N j)}} \right) \right] \quad (E10)$$

197 so that the probability of a randomly chosen occupancy to be found in isolate i is similar (up to
 198 the error associated with the models) to the sum over all occupancy levels of the multiplication

199 of two probabilities. The first is the probability of a randomly chosen occupancy to be from
 200 occupancy level j . The second is the conditional probability of this occupancy to be found in
 201 isolate i , given the SAR of occupancy level j . The two probabilities reflect the two marginal
 202 sums of the presence/absence data table. In fact, the first probability is the generalization of
 203 Sørensen probabilities to multiple-sites, as explained in the next section.

204 **Similarity indices, SODs and weighted SODs**

205 The most commonly used pairwise similarity indices of binary data are *Jaccard* and *Sørensen*.
 206 Let S_1 and S_2 be the number of species in isolates 1 and 2, respectively, and let S_{shared} be the
 207 number of species shared by the two isolates. *Jaccard* similarity can be expressed as
 208 $S_{shared}/(S_1+S_2-S_{shared})$, while *Sørensen* similarity is $2 \cdot S_{shared}/(S_1+S_2)$ (Chao *et al.*, 2005). Therefore,
 209 *Jaccard* similarity is the ratio of the number of species in occupancy level $j=2$ and the total
 210 number of species. *Sørensen* similarity is the ratio of the number of occupancies in occupancy
 211 level $j=2$ and the total number of occupancies. When viewed as probabilities, *Jaccard* is the
 212 probability of randomly selecting a species that is shared by the two isolates. *Sørensen* is the
 213 probability of randomly selecting an occupancy from a species shared by two isolates. That is,
 214 when $n=2$, *Jaccard* can be expressed as $R_2/(R_1+R_2)$, while *Sørensen* can be expressed as
 215 $2 \cdot R_2/(1 \cdot R_1 + 2 \cdot R_2)$. *Jaccard* and *Sørensen* dissimilarities are the complimentary of the indices to 1,
 216 which can be expressed as $R_1/(R_1+R_2)$ and $1 \cdot R_1/(1 \cdot R_1 + 2 \cdot R_2)$, respectively. Thus, when there are
 217 only two isolates, the additive-constrained SAR (equation 10) explicitly contains *Sørensen*
 218 similarity and dissimilarity as weights.

219 The SOD summarizes the change in R_j with j . If we standardize the SOD by dividing it by
 220 $\sum_j R_j$, we get for each occupancy level the term $R_j/\sum_j R_j$, which is the generalization of *Jaccard*
 221 probabilities into multiple isolates. A weighted form of the SOD (wSOD, Fig. 1C) summarizes

222 the change in $j \cdot R_j$ with j . When standardizing the wSOD by dividing it with $\sum_j(j \cdot R_j)$, we get for
 223 each occupancy level the term $j \cdot R_j / \sum_j(j \cdot R_j)$, which is the generalization of *Sørensen* probabilities
 224 to multiple isolates. Since the basic unit of type IV SARs is occupancy and not species, *Sørensen*
 225 probabilities are more relevant to the study of type IV SARs. Therefore, when there are more
 226 than two sites, equation 10 incorporates the generalization of *Sørensen* probabilities into the
 227 general SAR framework.

228 We suggest that summary statistics of the standardized SOD and wSOD can be considered as
 229 measures of beta diversity, since their constituting values may serve as the building blocks for
 230 multiple-sites similarity indices. Such multiple-sites similarity measures may differ from one
 231 another in their treatment of the difference between species in occupancy level. For example, the
 232 strictest definition of *Jaccard* multiple-sites similarity may be the proportion of species that are
 233 found in all isolates from the total number of species, i.e., $R_n / \sum_j R_j$, and for *Sørensen*, the
 234 equivalent proportion of occupancies from the total number of occupancies, i.e., $n \cdot R_n / \sum_j(j \cdot R_j)$.
 235 The least strict may be the proportion of species/occupancies that are found in at least two
 236 isolates, i.e., $\sum_{j \neq 1} [R_j / \sum_j R_j]$ for *Jaccard*, and $\sum_{j \neq 1} [j \cdot R_j / \sum_j j \cdot R_j]$ for *Sørensen*. In fact, if w_j is the
 237 weight given to occupancy level j in the multiple-sites similarity measure (such that $0 \leq w_j \leq 1$),
 238 then a general multiple-sites similarity of *Jaccard* and *Sørensen*, which still conserves the 2
 239 isolates interpretation as the proportion of species or occupancies may be:

$$240 \quad Jac_{mult} = \frac{\sum_{j=1}^N [w_j \cdot R_j]}{\sum_{j=1}^N [R_j]} \quad (E11)$$

$$241 \quad Sør_{mult} = \frac{\sum_{j=1}^N [w_j \cdot j \cdot R_j]}{\sum_{j=1}^N [j \cdot R_j]} \quad (E12)$$

242 with $w_1=w_2=\dots=w_{N-1}=0$ and $w_N=1$ for the most strict example while $w_1=0$ and $w_2=w_3=\dots=w_N=1$
 243 for the least strict example. A more interesting option for the weights may be the proportion of
 244 isolates pairs in which a species co-occur, resulting with

$$245 \quad Jac_{mult} = \sum_{j=1}^N \left[\frac{j(j-1)}{N(N-1)} \cdot \frac{R_j}{\sum_{j=1}^N [R_j]} \right] \quad (E13)$$

$$246 \quad Sør_{mult} = \sum_{j=1}^n \left[\frac{j(j-1)}{N(N-1)} \cdot \frac{j \cdot R_j}{\sum_{j=1}^N [j \cdot R_j]} \right] \quad (E14)$$

247 which converges to *Jaccard* and *Sørensen* similarities for $n=2$, while satisfying $w_1=0$ and $w_N=1$
 248 and keeping the original probabilistic interpretation of the indices. We note though, that the
 249 multiple-sites similarity indices themselves are not incorporated directly into the SAR, but rather
 250 they are built by the same building blocks as the SAR. We further note that published multiple-
 251 sites versions of *Jaccard* (Baselga, 2012) and *Sørensen* similarities (Baselga, 2010) can also be
 252 restructured using terms from the SOD as:

$$253 \quad Jac_{mult,Bas} = \frac{[\sum_{j=1}^N (j \cdot R_j) - \sum_{j=1}^N R_j]}{[\sum_{j=1}^N (j \cdot R_j) - \sum_{j=1}^N R_j] + \sum_{j=1}^N (R_j \cdot j \cdot (N-j))} = \frac{\sum_{j=1}^N [(j-1) \cdot R_j]}{\sum_{j=1}^N [(j-1+j(N-j)) \cdot R_j]} \quad (E15)$$

$$254 \quad Sør_{mult,Bas} = \frac{2 \cdot [\sum_{j=1}^N (j \cdot R_j) - \sum_{j=1}^N R_j]}{2 \cdot [\sum_{j=1}^N (j \cdot R_j) - \sum_{j=1}^N R_j] + \sum_{j=1}^N (R_j \cdot j \cdot (N-j))} = \frac{\sum_{j=1}^N [(2j-2) \cdot R_j]}{\sum_{j=1}^N [(2j-2+j(N-j)) \cdot R_j]} \quad (E16)$$

255 yet, such extensions to multiple sites do not conserve the total number of species or occupancies
 256 in the denominator, and therefore loses the probabilistic interpretation of *Jaccard* and *Sørensen*
 257 similarities. Furthermore, although the contribution to the similarity measure increases with
 258 occupancy level in the numerators of $Jac_{mult,Bas}$ and $Sør_{mult,Bas}$, the denominator reaches a
 259 maximum value for $j=(N+1)/2$ and $j=(N+2)/2$, respectively. If the SOD is indeed the unifying
 260 concept between beta-diversity and SARs, we suggest focusing on multiple-sites similarity
 261 indices that conserve the probabilistic interpretation of the SOD and the wSOD. In addition to
 262 the ecological meaning that of the probabilities, it opens a possible direction to incorporate the

263 effect of unsampled species to multiple-site similarity indices and SARs, as shown for pairwise
264 similarity by Chao *et al.* (2005).

265 **Other SAR functions**

266 Constrained SARs and additively constrained SARs can be based on any SAR function (Tjørve,
267 2003, 2009; Williams *et al.*, 2009; Triantis *et al.*, 2012). Repeating the steps that led from
268 equation 1 to 2 for other SAR functions has a similar effect – all SAR functions lose one of their
269 parameters (Table 1). Similar additive forms to those shown here for the power-model can be
270 developed for all other SAR functions. Therefore, all SAR functions may have one unnecessary
271 parameter that can be excluded, apparently, without loss of statistical power.

272 **Empirical analysis of 154 datasets**

273 We explored 154 published datasets (see Appendix S2) to examine whether a parameter can be
274 dropped without loss of goodness-of-fit if the SAR is constrained. The datasets cover various
275 spatial scales (from 6 m² isolates to inter-provincial SARs), taxa (fungi, plants, invertebrates and
276 vertebrates) and systems (inter-provincials, ecoregions, true islands, fragmented terrestrial
277 landscapes, etc.). Before fitting any model and to ease the search for appropriate starting values
278 for parameters, we first standardized the area units to relative area: $P_i = A_i / \sum_i A_i$ (and $\sum_i P_i = 1$). We
279 fitted each dataset with the original and constrained forms of the twelve functions given in bold
280 face in Table 1, a total of 24 functions. Non-linear least square regressions (using the Levenberg-
281 Marquardt convergence algorithm) were used to fit each dataset with the 24 models, and various
282 parameter-starting values were used to avoid local minima. After convergence, for the original
283 and constrained forms of each SAR function, the estimated parameters of the form that resulted
284 with lower residuals sum-of-squares (RSS) were used as the starting parameters of the second

285 form in an additional non-linear regression and the newly estimated parameters were kept if the
286 fit was improved.

287 After fitting the 24 models, we calculated for each model the corrected Akaike Information
288 Criteria (AICc; Burnham & Anderson, 2002; see Appendix S1 in Supporting Information). Next,
289 AICc weights ($wAICc_g$, with g being the name of the model out of G models) were calculated for
290 the entire set of 24 models (i.e., $G=24$). We then focused on each of the 12 SAR functions
291 separately and estimated the $wAICc_g$ of the functions's original and constrained forms of each
292 SAR function (i.e., 12 different sets, each with $G=2$). For the 12 sets, we estimated the expected
293 $wAICc$ for the special case in which the original and constrained form have identical log-
294 likelihood and only differ in the number of parameters (Appendix S1). Finally, we applied a
295 least-square linear regression of the observed $wAICc$ of the constrained form against the
296 expected value under identical log-likelihood and explored whether the confidence intervals of
297 the intercept and slope overlapped with zero and one, respectively.

298 The 154 datasets were also used to explore the shape of z -occupancy curves. Firstly, for each
299 dataset, we fitted equation 3 separately for the species from each occupancy level. This yielded
300 the observed z_j values for every j for which some species were observed. Next, we fitted the
301 observed z -occupancy curve with equation 8, while recording the explained variance and
302 significance. For the datasets presented in Fig.3, we fitted equation 9 as well, and compared the
303 predicted z occupancy curve to the fitted one. We further compared the AICc values and weights
304 of the original power-model (equation 1), constrained power-model (equation 2) and additive-
305 constrained power-model (equation 9).

306 Finally, for the 154 datasets we estimated the *Sørensen* multiple-sites similarity index based
307 on equation 14. We used linear regression to explore the relation between the power-model z

308 values and the multiple-sites similarity value. For this analysis we use only dataset where the
309 power-model explained variance was larger than 0.25. All regression analyses were carried out
310 with the `minpack.lm` package in R (R Development Core Team, 2014).

311

312 RESULTS

313 When comparing the 24 models, in all 154 datasets the model with the highest wAICc had a
314 constrained form. In general, SAR functions with the highest wAICc usually had only two
315 parameters in the original form (80% of datasets), had a convex shape (63%) and had no
316 asymptote (64%). Indeed, in 32% of the datasets, the best SAR function had all three of these
317 characters. The power-model had the highest wAICc for 25.4% of the datasets.

318 From a total of 1848 (12×154) combinations of SAR models and datasets, the non-linear
319 regression achieved convergence for both the original and constrained forms in 1811 analyses.
320 The constrained form received a higher wAICc than the original form in 1789 out of 1811
321 pairwise comparisons (98.79%, Table S3 in Appendix S2, Fig. 2). The wAICc of the constrained
322 form approached the expected weight for the special case in which the original and constrained
323 forms had identical log-likelihood (Fig. 2). For ten of the twelve SAR functions the confidence
324 intervals of the intercept and slope of the linear regression between the observed and expected
325 AICc weight of the constrained form overlapped with 0 and 1, respectively (Table S3). The two
326 exceptions were the Monod and Negative Exponential SAR functions. However, in these two
327 SAR functions, large deviation from the expected wAICc occurred in datasets that were not
328 adequately described by the SAR function (Fig. S1 in Appendix S3).

329 The non-linear regression of observed z_j values against j according to the exponential decay
330 function (equation 8) was statistically significant ($p < 0.05$) for 138 of the 154 datasets. In some

331 cases, a very clear decay pattern was evident (see a few examples in Fig. 3), while in others the
332 pattern was not that clear. The decay of z_j with j was less well defined when the SAR pattern
333 itself was weak or when the number of species was very low relative to the number of isolates
334 (resulting in poor representativeness in many occupancy levels). The 25th, 50th, and 75th
335 percentiles of parameter a of equation 8 – i.e., the slope of the endemic area relationship – were
336 0.43, 0.65, and 1.12, respectively. The explained variance of the regressions had a 25th, 50th and
337 75th percentiles of 0.29, 0.65, and 0.81, respectively. For the datasets presented in Fig. 3, the z
338 values predicted for each occupancy level by fitting equation 9 as the general SAR function (red
339 line) was highly correlated to the z values when fitting each occupancy level separately (black
340 diamonds, equation 3). The predicted z values according to equation 9 was very similar to those
341 achieved by fitting equation 8 to the fitted z values (black line). The additive-constrained SAR
342 received higher AICc weights than the original power-model in 6 out of 9 datasets (table 2), and
343 in two of these cases, it also out-performed the constrained power-model.

344 We found a statistically significant negative correlation between the power-model z (equation
345 2) and *Sørensen* multiple-sites similarity index (equation 14, Fig. 4). We observed a strong effect
346 of the number of isolates on the z -similarity trend. Dataset with large number of isolates tended
347 to have lower z values, and lower similarity values, probably since most species remain rare even
348 when a large number of isolates are sampled.

349

350 **DISCUSSION**

351 We developed the constrained form of 23 known SAR functions, which forces the SAR to
352 conserve the total number of occupancies (Table 1). For all SAR functions, constraining the
353 SAR resulted in a decrease of one parameter in the number of function parameters. The meta-

354 analysis of the 154 datasets revealed that the constrained forms outperformed the original
355 ones. This is evident for the 154 datasets in the wAICc of the constrained form approaching
356 its expected value for the special case in which the original and constrained forms have
357 identical log-likelihood (Fig. 3). In the two SAR functions (Monod and Negative Exponential)
358 for which some deviation from linear correlation were observed, the deviations mainly
359 occurred in datasets for which the SAR function did not describe the pattern well, relative to
360 other SAR function (Fig. S1, Appendix S3). Therefore, the deviations probably resulted from
361 failure to converge to the same global minima, since many local minima have very similar
362 log-likelihoods.

363 Consequently, for any given SAR function we have two competing models having similar
364 predictions and log-likelihoods, with one of the models having fewer parameters than the
365 other. The basic principle of parsimony requires us to prefer the model with fewer parameters,
366 and therefore for each SAR function to prefer the constrained forms over the original ones.
367 Considering the most common power-model SAR, the parameter which is canceled-out is
368 parameter c , the ‘politically ignored’ parameter (sensu, Gould, 1979; Triantis *et al.*, 2012).
369 Our results suggest that it is correctly ignored since it is an unnecessary fitting parameter that
370 comes on the expense of the more informative, process-based component of the SOD. This
371 parameter can be isolated from equation 2, to get: $c = \sum_j (j \cdot R_j) / \sum_i (A_i^z)$. Therefore, Lomolino
372 (2000) statement that parameter c “*varies in a poorly understood manner among taxa and*
373 *types of systems*” is not surprising, given that even when the area units are standardized, it is a
374 function of the total number of occupancies, the number of isolates, the distribution of area
375 between isolates and the second parameter z . Parameter c (and its above approximation) is
376 usually interpreted as the number of species in one unit of area. The general SAR is then

377 constructed by multiplying the number of species in one unit area by an area dependent
378 function. This is still true for the constrained SAR (equation 2). However, we show here that
379 it is also true for the constrained SAR of all other SAR models (table 1).

380 Removing a parameter from a widely used function may seem to present a small technical
381 improvement. However, given its broad use and the importance of SARs for various
382 applications, simplification of SAR models is crucial to understanding patterns and processes,
383 since simpler models are easier to interpret. Although having more parameters allows better
384 fit to data, parameters should be added if the additional goodness-of-fit is needed to better
385 understand the pattern. For SARs, this does not seem to be the case. In fact, the proximity of
386 the wAICc to the expected AICc weight under identical log likelihood (Fig. 2) suggest that the
387 two forms have very similar goodness-of-fit.

388 By constraining the SAR we have shown that SAR represents the turnover of occupancies
389 between isolates. Although SARs predict the number of species in each isolate, it is more
390 correct to treat occupancy as their basic unit. To claim that the unit of SARs is species is
391 similar to claiming that the unit of the abundance-area relationship (i.e., the total number of
392 individuals per isolate) is species and not individuals. Accepting that SARs represent the
393 turnover of occupancies between isolates suggests that SARs may also be affected by the
394 second occupancies turnover component – i.e., the turnover of occupancies between species.
395 This second component is captured by the SOD and the additive-constrained SAR.

396 The additive-constrained SAR (equations 7 and 9) sums over all occupancy levels the
397 multiplication of two probabilities. The first is the probability that a random occupancy is
398 from occupancy level j , and the second is the probability of this occupancy being in isolate i ,
399 given its occupancy level. The two probabilities represent the two turnover components of

400 occupancies: *i.* turnover of occupancies between species, and *ii.* turnover of occupancies
401 between isolates. The first turnover component relates to the shape of the wSOD, and as such
402 to the extended Sørensen probabilities. The effect of this turnover component on the SAR's
403 shape is evident in the relation between z and the multiple-sites similarity index (Fig. 4). The
404 second relates to the shape of the z -occupancy curves.

405 Here we explored a very specific additive-constrained SAR that assumes a power-model at
406 all occupancy levels. Of-course, similar to the general SAR, this might not be correct in all
407 datasets. However, even under this strict assumption, the additive-constrained SAR
408 outperformed the original power-model in six out of nine datasets (table 2), while providing
409 excellent prediction to the actual shape of the z -occupancy curves (Fig. 3). Furthermore, even
410 within a given dataset, different models may best describe SARs of different occupancy
411 levels. Unfortunately, occupancy-specific SARs have never been explored before, with the
412 exception of the endemics-area relationship that was mainly explored using a power-model
413 (Triantis *et al.*, 2008). We predict that the best fitting SAR model will change in a consistent
414 manner with occupancy level, (e.g., from a sigmoid curve, to power-law and then to linear
415 models as occupancy increases). Alternatively, additive-constrained SARs can be based on
416 single models with greater flexibility such as the two models suggested by Tjørve (2012).

417 The constrained form does not suggest any clear ecological interpretation of z , yet it is still
418 unclear if any such interpretation will ever arise (Connor & McCoy, 2001; but see: Rosindell
419 & Cornell, 2007; O'Dwyer & Green, 2010; Grilli *et al.*, 2012). Mathematically, z is a scaling
420 parameter that changes the proportion $A_i^z / \sum_i (A_i^z)$, relative to $z=1$, for which each isolate
421 receives a proportion from the total occupancies that is identical to its relative area. Therefore,
422 the ecological interpretation added in the constrained form is not in the meaning of z , but

423 rather in the meaning of the proportion $A_i^z/\sum_i(A_i^z)$. Since equation 2 is structured as the total
424 number of occupancies multiplied by this proportion we can interpret it as the probability of a
425 randomly drawn occupancy to be from isolate i . The proportion also explains why z has
426 maximal values (equation 5), as no isolate can receive more occupancies than the number of
427 species. This restriction on the values of z may be the reason why various theories, in spite of
428 their very different underlying assumptions, also predict it to have a restricted range (e.g.,
429 Preston, 1962). Note, that z_{max} cannot be estimated from the original form of SAR, since many
430 different combinations of c and z may satisfy the maximal proportion criteria. Similar
431 maximal values for parameters can be found for six other SAR functions that have a single
432 parameter in their constrained form (table 1).

433 In a wider perspective, we used the SOD as a pre-defined pattern that is plugged into the
434 SAR. However, species occupancy levels may be explored in relation to any of the species
435 traits. For example, species dispersal ability is likely to effect the intensity of rescue effects
436 and recolonization rates. Thus, species with higher dispersal abilities are likely to be found in
437 more isolates than species with lower dispersal ability. Alternatively, species with high
438 competitive ability are likely to persist longer in isolates once they are colonized. Thus,
439 species with high competitive abilities are also likely to occur on more isolates than species
440 with poor competitive abilities. Now, if we can model the probability of a species to have a
441 certain occupancy level (j) based on its' dispersal and competitive abilities, we can sum these
442 probabilities over all species for a given j to represent R_j . These R_j can then be used in
443 equation 2 , 4 or 9 above. In such analyses, the parameters linking species occupancy levels to
444 species dispersal and competitive abilities (or any other relevant trait) can be estimated
445 simultaneously with the parameters of the SAR, thereby allowing a more mechanistic

446 understanding of SARs. The incorporation of species traits directly into SAR functions may
447 compliment other relations between SARs and traits, such as exploring SAR's slope for
448 various trait values (Franzen *et al.*, 2012), substituting species richness with functional trait
449 diversity as the dependent variable (Whittaker *et al.*, 2014) or building SARs from species-
450 specific incidence functions (Ovaskainen & Hanski, 2003). The advantage here is that one
451 does not need to know in advance the effect of these traits on the probability to occur on j
452 isolates, and can learn on it from the SAR function.

453 Similarly, SARs are only one of the biodiversity patterns that relate the number of species
454 per isolate with one of the isolate's attributes. Other attributes may include, for example,
455 habitat heterogeneity, degree of isolation or the availability of resources (e.g., species energy
456 relationship). Probably, many of the mathematical functions used to describe SARs (Table 1)
457 may be used to describe other biodiversity patterns, such as species-connectivity relationships
458 and species-heterogeneity relationships. The constrained and additive-constrained forms may
459 be used to explore any of these biodiversity patterns.

460 Here we show, both theoretically (Table 1) and empirically (Fig. 2), that all known SAR
461 functions have one unnecessary parameter. Simplification of models is crucial to understanding
462 patterns and processes, since simpler models are easier to interpret. By constraining the SAR, we
463 have clarified its basic units, united all functions to a similar general structure (Table 1),
464 introduced Sørensen probabilities into the SAR framework and linked the two sides of
465 presence/absence tables (Fig. 1). SARs are fundamental to the development and testing of many
466 ecological theories (McGill, 2010) and play an important role in conservation and management,
467 including identifying biodiversity hotspots (Guilhaumon *et al.*, 2008) and predicting the effect of

468 habitat loss on species richness (Rosenzweig *et al.*, 2012; Keil *et al.*, 2015). Hopefully, our work
469 will shed new light on this important biodiversity pattern.

470

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478

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584 **Supporting Information**

585 Additional Supporting Information may be found in the online version of this article:

586 **Appendix S1** – AICc, wAICc and expected AICc

587 **Appendix S2** – references and information on datasets.

588 **Appendix S3** – Linear regressions of *wAICc*.

589

590 **BIOSKETCH**

591 **Yoni Gavish** – Is currently a research fellow at the University of Leeds, working on the development of biodiversity
592 analysis tools under the EU-BON project. He is interested in species-distribution models, biodiversity-patterns,
593 community modeling and habitat-classification models.

594 **Yaron Ziv** - a spatial and community ecologist, heading the Spatial Ecology Lab at Ben-Gurion University. He is
595 interested in the effect of habitat heterogeneity on processes and patterns of biodiversity at different spatiotemporal
596 scales. In particular, he strives to explore how scale-dependent and multi-scale effects define species occurrence and
597 distribution at various levels of organization. He also involves in conservation activities, through applied research on
598 habitat restoration and management.

599

600 **EDITOR:** François Guilhaumon

601

602 **Table 1:** The original and constrained forms of 23 known species-area relationship (SAR)
 603 functions (c, z, f , and k are function parameters). The parameters column indicate the change in
 604 the number of parameters when moving from the original to the constrained form. Functions
 605 given in bold face were used in the empirical analysis of the 154 datasets.

Name	Original form ($S_i=$)	Constrained form ($S_i=$)	Parameters
608 Lin.	$c + z \cdot A_i$	$\sum_j(j \cdot R_j) \cdot \frac{(1+z' \cdot A_i)}{\sum_i[1+z' \cdot A_i]}$	$2 \rightarrow 1$ ($z'=z/c$)
609 Pow.	$c \cdot A_i^z$	$\sum_j(j \cdot R_j) \cdot \frac{A_i^z}{\sum_i[A_i^z]}$	$2 \rightarrow 1$
610 Pow.Ros.	$f + c \cdot A_i^z$	$\sum_j(j \cdot R_j) \cdot \frac{(1+c' \cdot A_i^z)}{\sum_i[1+c' \cdot A_i^z]}$	$3 \rightarrow 2$ ($c'=c/f$)
611 Ext.P1	$c \cdot A_i^{z \cdot A_i^{-f}}$	$\sum_j(j \cdot R_j) \cdot \frac{A_i^{z \cdot A_i^{-f}}}{\sum_i[A_i^{z \cdot A_i^{-f}}]}$	$3 \rightarrow 2$
612 Ext.P2	$c \cdot A_i^{z-f/A_i}$	$\sum_j(j \cdot R_j) \cdot \frac{A_i^{z-f/A_i}}{\sum_i[A_i^{z-f/A_i}]}$	$3 \rightarrow 2$
613 P1	$c \cdot A_i^z \cdot \exp(-f \cdot A_i)$	$\sum_j(j \cdot R_j) \cdot \frac{A_i^z \cdot \exp(-f \cdot A_i)}{\sum_i[A_i^z \cdot \exp(-f \cdot A_i)]}$	$3 \rightarrow 2$
614 P2	$c \cdot A_i^z \cdot \exp(-f/A_i)$	$\sum_j(j \cdot R_j) \cdot \frac{A_i^z \cdot (1 - \exp(-f/A_i))}{\sum_i[A_i^z \cdot (1 - \exp(-f/A_i))]}$	$3 \rightarrow 2$
615 Exp.	$c + z \cdot \log(A_i)$	$\sum_j(j \cdot R_j) \cdot \frac{(1+z' \cdot \log(A_i))}{\sum_i[1+z' \cdot \log(A_i)]}$	$2 \rightarrow 1$ ($z'=z/c$)
616 Kob.	$c \cdot \log(1 + A_i/z)$	$\sum_j(j \cdot R_j) \cdot \frac{\log(1+A_i/z)}{\sum_i[\log(1+A_i/z)]}$	$2 \rightarrow 1$
617 Mon.	$c/(1 + z/A_i)$	$\sum_j(j \cdot R_j) \cdot \frac{(1/(1+z/A_i))}{\sum_i[1/(1+z/A_i)]}$	$2 \rightarrow 1$
618 MMF	$c/(1 + f \cdot A_i^{-z})$	$\sum_j(j \cdot R_j) \cdot \frac{(1/(1+f \cdot A_i^{-z}))}{\sum_i[1/(1+f \cdot A_i^{-z})]}$	$3 \rightarrow 2$
619 Arc.Log.	$c/(f + A_i^{-z})$	$\sum_j(j \cdot R_j) \cdot \frac{(1/(f+A_i^{-z}))}{\sum_i[1/(f+A_i^{-z})]}$	$3 \rightarrow 2$
620 Neg.Exp.	$c \cdot (1 - \exp(-z \cdot A_i))$	$\sum_j(j \cdot R_j) \cdot \frac{(1 - \exp(-z \cdot A_i))}{\sum_i[1 - \exp(-z \cdot A_i)]}$	$2 \rightarrow 1$
621 Chp.Ric.	$c \cdot (1 - \exp(-z \cdot A_i))^f$	$\sum_j(j \cdot R_j) \cdot \frac{(1 - \exp(-z \cdot A_i))^f}{\sum_i[1 - \exp(-z \cdot A_i)]^f}$	$3 \rightarrow 2$

622	Wei.3	$c \cdot (1 - \exp(-z \cdot A_i^f))$	$\sum_j(j \cdot R_j) \cdot \frac{(1 - \exp(-z \cdot A_i^f))}{\sum_i[1 - \exp(-z \cdot A_i^f)]}$	$3 \rightarrow 2$
623	Wei.4	$c \cdot (1 - \exp(-z \cdot A_i^f))^k$	$\sum_j(j \cdot R_j) \cdot \frac{(1 - \exp(-z \cdot A_i^f))^k}{\sum_i[1 - \exp(-z \cdot A_i^f)]^k}$	$4 \rightarrow 3$
624	Asy.	$f - c \cdot z^{-A_i}$	$\sum_j(j \cdot R_j) \cdot \frac{(1 + c' \cdot z^{-A_i})}{\sum_i[1 + c' \cdot z^{-A_i}]}$	$3 \rightarrow 2$ ($c' = c/f$)
625	Rat.	$(c + z \cdot A_i)/(1 + f \cdot A_i)$	$\sum_j(j \cdot R_j) \cdot \frac{(1 + z' \cdot A_i)/(1 + f \cdot A_i)}{\sum_i[(1 + z' \cdot A_i)/(1 + f \cdot A_i)]}$	$3 \rightarrow 2$ ($z' = z/c$)
626	Gom.	$c \cdot \exp(-\exp(-z \cdot (A_i - f)))$	$\sum_j(j \cdot R_j) \cdot \frac{\exp(-\exp(-z \cdot (A_i - f)))}{\sum_i[\exp(-\exp(-z \cdot (A_i - f)))]}$	$3 \rightarrow 2$
627	Beta.P	$c \cdot (1 - (1 + (A_i/z)^f)^{-k})$	$\sum_j(j \cdot R_j) \cdot \frac{(1 - (1 + (A_i/z)^f)^{-k})}{\sum_i[e(1 - (1 + (A_i/z)^f)^{-k})]}$	$4 \rightarrow 3$
628	Com.Log.	$c/(1 + \exp(-z \cdot A_i + f))$	$\sum_j(j \cdot R_j) \cdot \frac{(1/(1 + \exp(-z \cdot A_i + f)))}{\sum_i[1/(1 + \exp(-z \cdot A_i + f))]}$	$3 \rightarrow 2$
629	EVF.	$c \cdot (1 - \exp(-\exp(z \cdot A_i + f)))$	$\sum_j(j \cdot R_j) \cdot \frac{(1 - \exp(-\exp(z \cdot A_i + f)))}{\sum_i[1 - \exp(-\exp(z \cdot A_i + f))]}$	$3 \rightarrow 2$
630	Lom.	$c/(1 + (z^{\log(f/A_i)}))$	$\sum_j(j \cdot R_j) \cdot \frac{(1/(1 + (z^{\log(f/A_i)})))}{\sum_i[1/(1 + (z^{\log(f/A_i)}))]}$	$3 \rightarrow 2$

631
632 **Pow.** – Power; **Pow.Ros.** – Power Rosenzweig; **Ext.P1**– Extended Power 1; **Ext.P2**– Extended Power 2; **P1** –
633 Persistence Function 1; **P2** – Persistence Function 2; **Exp.** – Exponential; **Kob.** – Kobayashi Logarithmic; **Mon.** –
634 Monod; **MMF.** – Morgan-Mercer-Flodin; **Arc.Log.** – Archibald Logistic; **Neg.Exp.** – Negative Exponential;
635 **Chp.Ric.** – Chapman-Richards; **Wei.3** – Weibull-3; **Wei.4** – Weibull-4; **Asy.** – Asymptotic; **Rat.** – Rational. **Gom.**
636 – Gompertz; **Beta.P.** – Beta-P; **Com.Log.** - Common Logistic; **EVF.** – Extreme-Value Function; **Lom.** – Lomolino
637 function.

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642 **Table 2:** Corrected Akaike Information Criteria (AICc) values and weights of the original
 643 power-model (equation 1), the constrained power-model (equation 2) and the additive-
 644 constrained power-model (equation 9) for the nine datasets presented in figure 2. Values in
 645 parentheses are the ranking of each model according to the AICc weights.

646

647	Data set	AICc			AICc weights		
		Equation 1	Equation 2	Equation 9	Equation 1	Equation 2	Equation 9
648	DS49	135.89	133.01	135.90	0.161 (2)	0.679 (1)	0.160 (3)
649	DS104	50.04	45.79	53.27	0.104 (2)	0.875 (1)	0.021 (3)
650	DS125	107.16	103.49	106.00	0.111 (3)	0.692 (1)	0.197 (2)
651	DS16	208.25	205.47	207.81	0.160 (3)	0.642 (1)	0.199 (2)
652	DS38	108.49	101.49	101.26	0.014 (3)	0.465 (2)	0.521 (1)
653	DS64	114.13	111.39	113.72	0.162 (3)	0.639 (1)	0.199 (2)
654	DS115	232.96	230.64	236.1	0.227 (2)	0.725 (1)	0.047 (3)
655	DS136	58.69	53.91	51.19	0.018 (3)	0.201 (2)	0.781 (1)
656	DS117	1135.18	1133.04	1133.90	0.172 (3)	0.501 (1)	0.326 (2)

658

659

660 **Figure 1.** General framework for species-occupancy distributions (SODs) and species-area
661 relationships (SARs). The marginal sums of presence/absence tables (A) yields the number of
662 species per isolate which can be used to plot the general SAR (D). The second marginal sums
663 yields the number of isolates per species (i.e., the species occupancy level), which can be used to
664 produce the SOD (C). However, the presence/absence table can be rearranged by grouping
665 species from the same occupancy level (B). From the resulting $N \times N$ square matrix the
666 occupancy-specific SARs can be produced (E) as well as a weighted version of the SOD (wSOD,
667 C). The additive-constrained SAR develop here is based on this square matrix. The notations
668 used here and in text are given in (F).

669
670 **Figure 2.** The corrected Akaike Information Criteria weight (wAICc) of the constrained species-
671 area relationships (SAR) form for 154 datasets and 12 SAR functions. For 1789 of 1811 valid
672 combinations of 154 datasets and 12 functions, the (wAICc of the constrained form (red, shown
673 here against the number of isolates), was higher than that of the original form. The observed
674 wAICc of the constrained form approaches the expected weight, if the two forms have identical
675 log-likelihood (and as such similar goodness-of-fit) and only differ in the number of parameters
676 (solid black line). As the number of isolates increases, the wAICc approach the expected values
677 under identical log likelihood and infinite number of isolates (horizontal dashed line). See
678 appendix 1 for details.

679
680 **Figure 3.** A few examples of z -occupancy curves. The predicted z values in each occupancy
681 level as predicted when fitting equation 9 (red line), compared to the z value obtained when
682 fitting each occupancy level separately with a constrained power-model (equation 3, black
683 diamonds). The dashed black line was obtained by fitting equation 8 to the fitted z values. Each
684 panel is for one dataset (DS), numbered according to Table S2 (Appendix S2).

685
686 **Figure 4.** The relation between z and *Sørensen* multiple-sites similarity index. The power-
687 model's z values decrease with increase in multiple-sites similarity index ($y = 0.53 - 0.61 \times x$,
688 $F_{113,1} = 14.491$, $p < 0.001$). The size of the points is relative to the square root of the number of
689 isolates in the dataset.

690

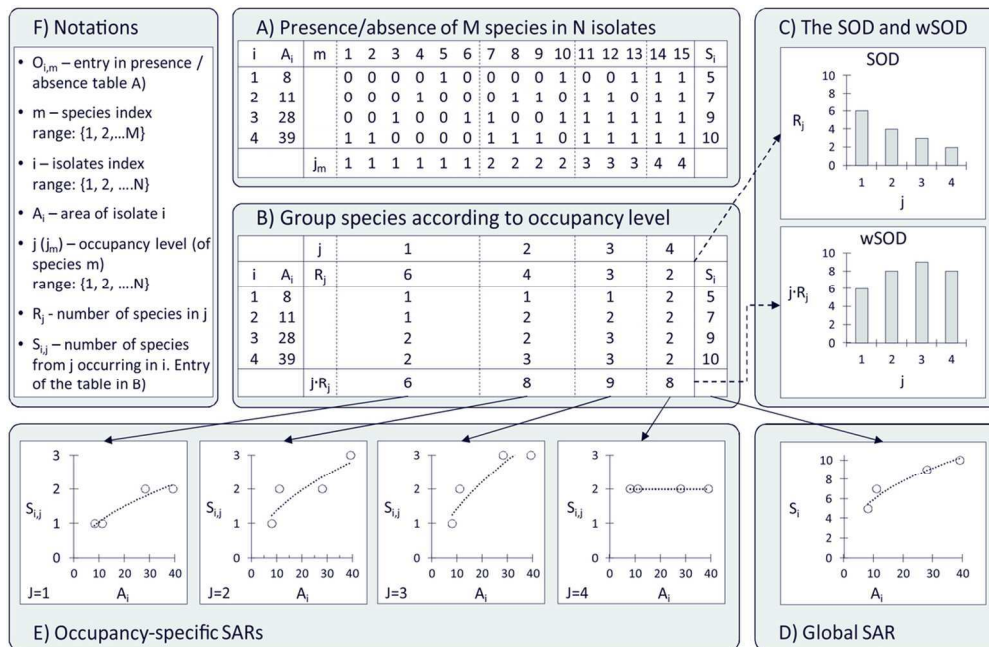
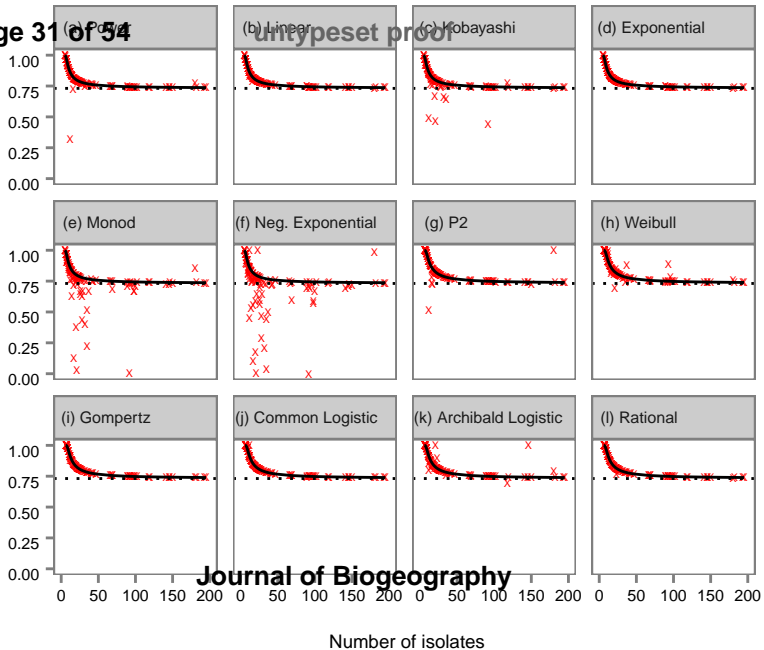
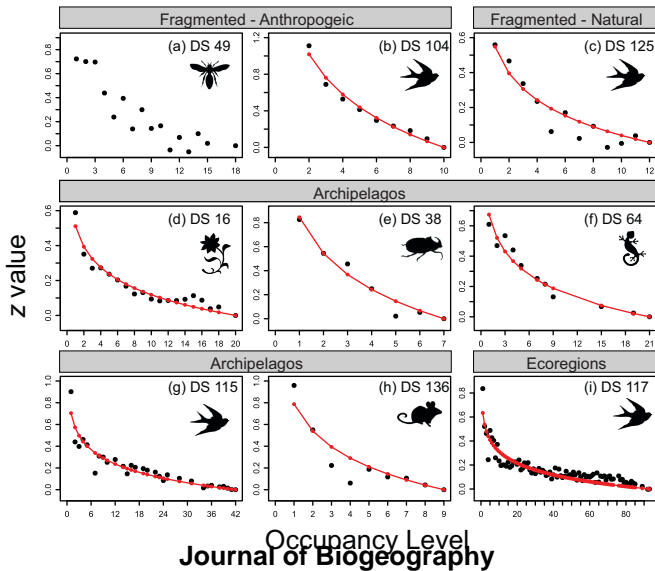


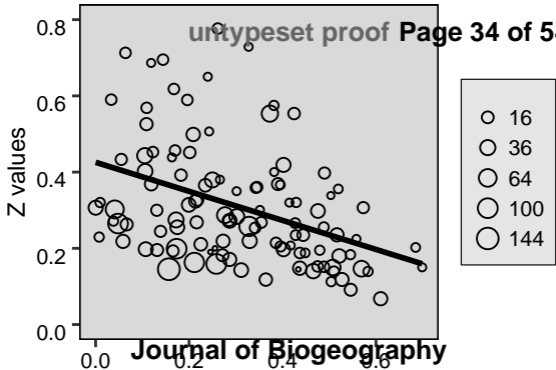
Figure 1. General framework for species-occupancy distributions (SODs) and species-area relationships (SARs). The marginal sums of presence/absence tables (A) yields the number of species per isolate which can be used to plot the general SAR (D). The second marginal sums yields the number of isolates per species (i.e., the species occupancy level), which can be used to produce the SOD (C). However, the presence/absence table can be rearranged by grouping species from the same occupancy level (B). From the resulting $N \times N$ square matrix the occupancy-specific SARs can be produced (E) as well as a weighted version of the SOD (wSOD, C). The additive-constrained SAR develop here is based on this square matrix. The notations used here and in text are given in (F).

109x71mm (300 x 300 DPI)









Multiple site Sørensen (eq. 14)

SUPPORTING INFORMATION**Species-occupancy distribution removes excessive parameter from species-area relationship**

Yoni Gavish and Yaron Ziv

Supplementary Information

Appendix S1 – explaining the AICc, wAICc and expected AICc

Appendix S2 – Reference list of all datasets used in the analysis (Table S1) and basic information on each dataset (table S2).

Appendix S3 – Linear regression between the expected and observed *wAICc* of the constrained form (table S3) with additional focus on the Monod and negative exponential functions (figure S1).

Appendix S1

Explaining the AICc, wAICc and expected AICc

Empirical datasets - data analysis. Non-linear least square regressions (using the Levenberg-Marquardt algorithm) were used to fit each dataset with 24 models (two forms of the 12 functions in Table 1). We used various parameter starting values to avoid local minima. All analyses were carried out with the function nlsLM (Minpack.lm Package) in R (R Development Core Team, 2011). After fitting the 24 models, we calculated Log-likelihood as:

$$LL = -(n/2) \cdot \ln(2\pi) - (n/2) \cdot \ln(RSS/n) - (n/2) \tag{SI1.1}$$

where *RSS* is the residuals sum of square and *n* is the number of isolates. Next, AICc values were calculated as:

$$-2 \cdot LL + 2 \cdot F + 2 \cdot F \cdot (F+1)/(n-F-1) \tag{SI1.2}$$

with *F* being the number of parameters of the model plus one for the residuals variance (Burnham & Anderson, 2002). As such, original and constrained forms of SAR function with two function parameters add *F*=3 and *F*=2, respectively. Original and constrained forms of SAR function with three function parameters add *F*=4 and *F*=3, respectively. We then calculated delta AICc and AICc weights. To avoid mixing the frequentist approach with the model-selection approach we employed in this study, we have not checked for normality with commonly used methods (e.g., Kolmogorov-Smirnov). Instead, we repeated the entire analysis using a Poisson error distribution, with: $LL = \sum_{i=1}^n \ln[\exp(-\mu_i) \cdot \mu_i^{y_i} / y_i!]$

(where *y_i* and *μ_i* are the observed and expected number of species for isolate *i*). Using the Poisson error had no qualitative effect on the results shown in the paper.

Empirical datasets - expected AICc weights. If constraining the SAR has no effect on the model's goodness-of-fit, the log-likelihood of the two forms should be identical. Under identical log-likelihoods, the constrained form (with one parameter less) will have a lower AICc value than the original form. Therefore, the delta AICc of the constrained form will be 0, and that of the original form will be:

$$\Delta AICc_{reg} = AICc_{reg} - AICc_{con} = \left[2 \cdot F + \frac{2 \cdot F \cdot (F+1)}{(n-F-1)} \right] - \left[2 \cdot (F-1) + \frac{2 \cdot (F-1) \cdot F}{(n-F)} \right] \tag{SI1.3}$$

The expected AICc weight of the constrained form (solid black line in Fig. 2) can then be calculated as:

$$wAICc_{con} = \frac{\exp(-0.5 \cdot 0)}{(\exp(-0.5 \cdot 0) + \exp(-0.5 \cdot \Delta AICc_{reg}))} \tag{SI1.4}$$

depending only on the number of isolates (*n*) and the number of parameters of the original form (*F*). When the number of isolates approaches infinity, the second term within the brackets of equation SI1.3 can be omitted,

$\Delta AICc_{reg} = 2$, and $wAICc_{con} = 0.731$ (dashed horizontal line in Fig. 1 of the main text). Finally, for each of the 12 SAR functions we explored the relation between the observed and expected $wAICc_{con}$ using linear regressions. If no information is lost, we expected the 154 datasets to fall on the unity line (Supplementary Table S3).

Burnham K.P. & Anderson R. (2002). Model selection and multimodel inference - A practical information - theoretic approach. Second edn. Springer Press.

R Development Core Team (2011). R: A Language and Environment for Statistical Computing. R Foundation for Statistical Computing, Vienna, Austria, <http://www.R-project.org>.

Appendix S1

Reference list of all datasets used in the analysis (Table S1) and basic information on each dataset (table S2).

The 154 dataset explored in this manuscript were collected using several methodologies. Our criteria for inclusion in the meta-analysis was that the reference:

- Reported the entire presence/absence data and not only the total number of species per site
- The area of the isolates was reported or can be extracted from online sources such as the island directory (<http://islands.unep.ch/isldir.htm>).
- Sampling effort increased with area.
- The pdf was available online or was received from the authors upon request.

We looked for dataset using several sources:

1. Manuscript known by the authors from there general reading in the fields.
2. Data collected by the authors
3. Dataset lists of other meta-analyses, mainly:
 - a. Triantis et al., 2012, The island species-area relationship: biology and statistics, *Journal of Biogeography*, 39 (2): 215-231
 - b. Drakare et al., 2006, The imprint of the geographical, evolutionary and ecological context on species–area relationships, *Ecology Letters* 9 (2): 215-227
 - c. Boecklen, W. J., 1997, Nestedness, biogeographic theory, and the design of nature reserves, *Oecologia*, 112 (1): 123-142
4. General google scholar/web of knowledge search using different crossing of the terms (and closely related terms):

System term	Crossed with	Data type
fragmentation	X	species list
fragmented landscapes		presence/absence
patchy landscape		occurrence
islands		abundance
archipelagos		Species atlas

Table S1 contains the list of references for all the datasets (with some references providing more than 1 dataset), while table S2 provides additional information (as well as some analytical results for each dataset)

Table S1:

Reference details for the 154 datasets used in the analysis. Reference number in supplementary table 2 refers to the numbers here.

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Table S2: Basic information on each dataset used in the analysis. The best model is the model that received the highest AICc weight from the 24 models (the constrained and regular forms of 12 functions). Abbreviations: *n* – number of isolates; Models abbreviations follow table 1 and are given below; Ori – original form; Con – constrained form; Ref^o – the reference number according to supplementary table S1. A version of the table in .xls format is available from the authors upon request (YG at gavishyoni@gmail.com).

	Major Taxon (Taxon)	system	Location	n	Area range (units)	Species (endemics, % endemics)	Number of occupancies	mean occupancy level	Best Model (Ori/Con)	Ref^o
1	Fungi	Archipelago	Andaman and Nicobar Islands	6	127-1536 (km ²)	63 (24 , 38.1%)	180	2.86	Lin. (Con)	14
2	Fungi	Archipelago	Canary islands	7	290.5-2007 (km ²)	1825 (963 , 52.8%)	3599	1.97	Lin. (Con)	5
3	Fungi	Archipelago	Cape-Verde	12	1.4-991 (km ²)	58 (36 , 62.1%)	93	1.60	Pow. (Con)	4
4	Fungi (Lichens)	Archipelago	Canary islands	7	290.5-2007 (km ²)	1438 (618 , 43%)	3364	2.34	Lin. (Con)	5
5	Fungi (Lichens)	Archipelago	Cape-Verde	12	1.4-991 (km ²)	244 (77 , 31.6%)	773	3.17	Pow. (Con)	4
6	Plants (Bryophyta)	Archipelago	Canary islands	7	290.5-2007 (km ²)	351 (88 , 25.1%)	1263	3.60	Lin. (Con)	5
7	Plants (Bryophyta)	Archipelago	Cape-Verde	12	1.4-991 (km ²)	139 (45 , 32.4%)	323	2.32	Neg.Exp. (Con)	4
8	Plants (Ferns)	Other	Sub-Saharan Africa	27	17-311040 (km ²)	687 (180 , 26.2%)	3115	4.53	Pow. (Con)	1
9	Plants (Marchantiophyta)	Archipelago	Canary islands	7	290.5-2007 (km ²)	138 (27 , 19.6%)	502	3.64	Lin. (Con)	5
10	Plants	Anthropogenic fragmented landscape	Lachish, Israel	40	0.06-7.93 (ha)	408 (77 , 18.9%)	6012	14.74	Exp. (Con)	32
11	Plants	Archipelago	Leros islets' group, east Aegean, Greece	17	0.6-124 (ha)	290 (99 , 34.1%)	958	3.30	Neg.Exp. (Con)	46
12	Plants (Pteridophyta)	Archipelago	Canary islands	7	290.5-2007 (km ²)	49 (5 , 10.2%)	218	4.45	Mon. (Con)	5
13	Plants (Pteridophyta)	Archipelago	Cape-Verde	12	1.4-991 (km ²)	35 (11 , 31.4%)	118	3.37	P2 (Con)	4

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	<i>Major Taxon (Taxon)</i>	<i>system</i>	<i>Location</i>	<i>n</i>	<i>Area range (units)</i>	<i>Species (endemics, % endemics)</i>	<i>Number of occupancies</i>	<i>mean occupancy level</i>	<i>Best Model (Ori/Con)</i>	<i>Ref'</i>
14	Plants (Spermatophyta)	Archipelago	Canary islands	7	290.5-2007 (km ²)	1314 (416 , 31.7%)	4461	3.39	Lin. (Con)	5
15	Plants (Spermatophyta)	Archipelago	Cape-Verde	12	1.4-991 (km ²)	757 (195 , 25.8%)	3196	4.22	Pow. (Con)	4
16	Plants (Vascular)	Archipelago	Sea of Cortes	20	0.6-1223 (km ²)	707 (281 , 39.8%)	2734	3.87	Kob. (Con)	12
17	Plants (Vascular)	Archipelago	Sea of Cortes, Bahia de Los Angeles	14	0.02-9.13 (km ²)	99 (23 , 23.2%)	396	4.00	Kob. (Con)	12
18	Plants (Vascular)	Archipelago	Sea of Cortes, small gulf islands	10	0.02-2.26 (km ²)	153 (96 , 62.8%)	271	1.77	Lin. (Con)	12
19	Invertebrates	Archipelago	mangrove islands, Florida Bay, USA (1969)	9	264-1263 (m ²)	205 (75 , 36.6%)	732	3.57	P2 (Con)	50
20	Invertebrates	Archipelago	mangrove islands, Florida Bay, USA (1970)	9	104-779 (m ²)	179 (67 , 37.4%)	652	3.64	Kob. (Con)	50
21	Invertebrates (Freshwater invertebrates)	Inland water bodies	Connecticut, USA	14	6.03-8318 (m ²)	89 (43 , 48.3%)	232	2.61	Pow. (Con)	53
22	Invertebrates (Mollusca)	Archipelago	Canary islands	7	290.5-2007 (km ²)	259 (219 , 84.6%)	354	1.37	Lin. (Con)	5
23	Invertebrates (Mollusca)	Archipelago	Cape-Verde	12	1.4-991 (km ²)	50 (13 , 26%)	192	3.84	Pow. (Con)	4
24	Invertebrates (Mollusca-Land snails)	Archipelago	Aegean Islands	34	3.4-842 (km ²)	152 (47 , 30.9%)	996	6.55	Pow. (Con)	34
25	Invertebrates (Acarina)	Archipelago	Canary islands	7	290.5-2007 (km ²)	391 (236 , 60.4%)	620	1.59	Neg.Exp. (Con)	5
26	Invertebrates (Araneae)	Anthropogenic fragmented landscape	Dvir, Israel	12	0.11-3.90 (ha)	114 (43 , 37.7%)	389	3.41	Exp. (Con)	30
27	Invertebrates (Araneae)	Anthropogenic fragmented landscape	Galon, Israel	8	0.16-4.24 (ha)	99 (39 , 39.4%)	308	3.11	Mon. (Con)	31
28	Invertebrates (Araneae)	Anthropogenic fragmented landscape	Lachish, Israel	12	0.06-2.81 (ha)	115 (35 , 30.4%)	447	3.89	Pow. (Con)	30
29	Invertebrates (Araneae)	Anthropogenic fragmented	Tokyo, Japan	7	0.2-27	34 (12 ,	103	3.03	Mon. (Con)	44

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	<i>Major Taxon (Taxon)</i>	<i>system</i>	<i>Location</i>	<i>n</i>	<i>Area range (units)</i>	<i>Species (endemics, % endemics)</i>	<i>Number of occupancies</i>	<i>mean occupancy level</i>	<i>Best Model (Ori/Con)</i>	<i>Ref'</i>
		landscape			(ha)	35.3%)				
30	Invertebrates (Araneae)	Anthropogenic fragmented landscape	Yokohama, Japan	9	0.4-15.1 (ha)	52 (12, 23.1%)	223	4.29	Pow. (Con)	44
31	Invertebrates (Araneae)	Archipelago	Canary islands	7	290.5-2007 (km ²)	455 (258, 56.7%)	962	2.11	Lin. (Con)	5
32	Invertebrates (Araneae)	Archipelago	Cape-Verde	12	1.4-991 (km ²)	114 (44, 38.6%)	233	2.04	Kob. (Con)	4
33	Invertebrates (Crustacea)	Archipelago	Canary islands	7	290.5-2007 (km ²)	99 (63, 63.6%)	170	1.72	Arc.Log. (Con)	5
34	Invertebrates (Crustacea-Land isopods)	Archipelago	Aegean Islands	23	3.4-476 (km ²)	67 (14, 20.9%)	569	8.49	Pow. (Con)	34
35	Invertebrates (Chilopoda)	Archipelago	Canary islands	7	290.5-2007 (km ²)	30 (11, 36.7%)	90	3.00	Lin. (Con)	5
36	Invertebrates (Diplopoda)	Archipelago	Canary islands	7	290.5-2007 (km ²)	67 (56, 83.6%)	91	1.36	Rat. (Con)	5
37	Invertebrates (Nematoda)	Archipelago	Canary islands	7	290.5-2007 (km ²)	98 (61, 62.2%)	195	1.99	Rat. (Con)	5
38	Invertebrates (Coleoptera)	Archipelago	Canary islands	7	290.5-2007 (km ²)	1926 (950, 49.3%)	4638	2.41	Lin. (Con)	5
39	Invertebrates (Coleoptera)	Archipelago	Cape-Verde	12	1.4-991 (km ²)	474 (171, 36.1%)	1408	2.97	Lin. (Con)	4
40	Invertebrates (Coleoptera, Tenebrionidae)	Archipelago	Aegean Islands	32	3.8-8260 (km ²)	165 (92, 55.8%)	514	3.12	Lin. (Con)	26
41	Invertebrates (Coleoptera, Tenebrionidae)	Archipelago	Sea of Cortes	18	0.004-9.13 (km ²)	31 (12, 38.7%)	120	3.87	Pow. (Con)	12
42	Invertebrates (Collembola)	Archipelago	Canary islands	7	290.5-2007 (km ²)	113 (53, 46.9%)	249	2.20	Rat. (Con)	5
43	Invertebrates (Diptera)	Archipelago	Canary islands	7	290.5-2007 (km ²)	989 (350, 35.4%)	2439	2.47	Lin. (Con)	5
44	Invertebrates (Diptera)	Archipelago	Cape-Verde	12	1.4-991 (km ²)	220 (97, 44.1%)	546	2.48	Pow. (Con)	4

	<i>Major Taxon (Taxon)</i>	<i>system</i>	<i>Location</i>	<i>n</i>	<i>Area range (units)</i>	<i>Species (endemics, % endemics)</i>	<i>Number of occupancies</i>	<i>mean occupancy level</i>	<i>Best Model (Ori/Con)</i>	<i>Ref'</i>
45	Invertebrates (Hemiptera)	Archipelago	Canary islands	7	290.5-2007 (km ²)	725 (254 , 35%)	2052	2.83	Lin. (Con)	5
46	Invertebrates (Hemiptera)	Archipelago	Cape-Verde	12	1.4-991 (km ²)	308 (105 , 34.1%)	937	3.04	Pow. (Con)	4
47	Invertebrates (Hymenoptera)	Archipelago	Canary islands	7	290.5-2007 (km ²)	960 (434 , 45.2%)	2086	2.17	Rat. (Con)	5
48	Invertebrates (Hymenoptera)	Archipelago	Cape-Verde	12	1.4-991 (km ²)	229 (142 , 62%)	370	1.62	Rat. (Con)	4
49	Invertebrates (Hymenoptera-Ants)	Anthropogenic fragmented landscape	south-eastern Brazil	18	3-299 (ha)	120 (26 , 21.7%)	535	4.46	Gom. (Con)	49
50	Invertebrates (Hymenoptera-Ants)	Archipelago	Sea of Cortes	13	0.02-8.68 (km ²)	24 (9 , 37.5%)	84	3.50	Kob. (Con)	12
51	Invertebrates (Lepidoptera)	Anthropogenic fragmented landscape	Southern Spain	13	3.6-2115 (ha)	81 (21 , 25.9%)	481	5.94	Mon. (Con)	9
52	Invertebrates (Lepidoptera)	Archipelago	Aegean Islands	31	9-9254 (km ²)	127 (41 , 32.3%)	1052	8.28	Com.Log. (Con)	22
53	Invertebrates (Lepidoptera)	Archipelago	Canary islands	7	290.5-2007 (km ²)	606 (222 , 36.6%)	1576	2.60	Lin. (Con)	5
54	Invertebrates (Lepidoptera)	Archipelago	Cape-Verde	12	1.4-991 (km ²)	163 (68 , 41.7%)	450	2.76	Lin. (Con)	4
55	Invertebrates (Lepidoptera)	Archipelago	Italian islands	10	40-22352 (ha)	76 (18 , 23.7%)	307	4.04	Pow. (Con)	20
56	Invertebrates (Lepidoptera)	Archipelago	Sardinian–Corsican islands	11	40-11559 (ha)	32 (5 , 15.6%)	175	5.47	Kob. (Con)	20
57	Invertebrates (Lepidoptera)	Archipelago	Sicilian islands	10	250-24600 (ha)	30 (5 , 16.7%)	160	5.33	Pow. (Con)	20
58	Invertebrates (Lepidoptera)	Archipelago	Tuscan islands	8	220-6030 (ha)	67 (23 , 34.3%)	198	2.96	Mon. (Con)	19
59	Invertebrates (Orthoptera)	Anthropogenic fragmented landscape	Small steppe patches, Buda Hills, Hungary	26	0.018-10.117 (ha)	32 (7 , 21.9%)	224	7.00	Lin. (Con)	8
60	Invertebrates (Orthoptera)	Anthropogenic fragmented	south-eastern Brazil	18	3-299	16 (9 ,	43	2.69	Kob. (Con)	49

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	<i>Major Taxon (Taxon)</i>	<i>system</i>	<i>Location</i>	<i>n</i>	<i>Area range (units)</i>	<i>Species (endemics, % endemics)</i>	<i>Number of occupancies</i>	<i>mean occupancy level</i>	<i>Best Model (Ori/Con)</i>	<i>Ref'</i>
		landscape			(ha)	56.3%)				
61	Invertebrates (Orthoptera)	Archipelago	Canary islands	7	290.5-2007 (km ²)	82 (26, 31.7%)	236	2.88	Lin. (Con)	5
62	Invertebrates (Thysanoptera)	Archipelago	Canary islands	7	290.5-2007 (km ²)	68 (28, 41.2%)	189	2.78	Pow. (Con)	5
63	Vertebrates (Herpatofauna)	Archipelago	Abaco Cays, West-Indian islands	21	0.05-16.4 (km ²)	8 (3, 37.5%)	56	7.00	Pow. (Con)	47
64	Vertebrates (Herpatofauna)	Archipelago	Anguilla bank, West-Indian islands	21	0.007-90.7 (km ²)	40 (19, 47.5%)	129	3.23	Com.Log. (Con)	47
65	Vertebrates (Herpatofauna)	Archipelago	Baubyan islands, Northern Philippines	5	0.7-196 (km ²)	44 (20, 45.5%)	83	1.89	Exp. (Con)	45
66	Vertebrates (Herpatofauna)	Archipelago	Berry Islands, West-Indian islands	15	0.09-25.9 (km ²)	18 (4, 22.2%)	69	3.83	Pow. (Con)	47
67	Vertebrates (Herpatofauna)	Archipelago	Bimini Islands, West-Indian islands	15	0.003-8.8 (km ²)	22 (9, 40.9%)	71	3.23	Lin. (Con)	47
68	Vertebrates (Herpatofauna)	Archipelago	Caicos Cays, West-Indian islands	29	0.01-144 (km ²)	14 (2, 14.3%)	130	9.29	Pow. (Con)	47
69	Vertebrates (Herpatofauna)	Archipelago	Central Exuma Cays, West-Indian islands	26	0.018-12.3 (km ²)	16 (2, 12.5%)	108	6.75	Com.Log. (Con)	47
70	Vertebrates (Herpatofauna)	Archipelago	Crooked-Acklins bank, West-Indian islands	11	0.03-497 (km ²)	10 (2, 20%)	35	3.50	Pow. (Con)	47
71	Vertebrates (Herpatofauna)	Archipelago	Grenada bank, West-Indian islands	35	0.01-32 (km ²)	28 (10, 35.7%)	160	5.71	Com.Log. (Con)	47
72	Vertebrates (Herpatofauna)	Archipelago	Guadeloupe bank, West-Indian islands	14	0.005-22 (km ²)	17 (8, 47.1%)	45	2.65	Pow. (Con)	47
73	Vertebrates (Herpatofauna)	Archipelago	Hispaniola bank, West-Indian islands	17	0.09-692 (km ²)	65 (29, 44.6%)	154	2.37	Pow. (Con)	47
74	Vertebrates (Herpatofauna)	Archipelago	Jamaica bank, West-Indian islands	14	0.02-2.2 (km ²)	10 (3, 30%)	27	2.70	Com.Log. (Con)	47
75	Vertebrates (Herpatofauna)	Archipelago	Keys of the northern coast of Cuba, West-	35	0.02-680	59 (15,	346	5.86	Pow. (Con)	47

	<i>Major Taxon (Taxon)</i>	<i>system</i>	<i>Location</i>	<i>n</i>	<i>Area range (units)</i>	<i>Species (endemics, % endemics)</i>	<i>Number of occupancies</i>	<i>mean occupancy level</i>	<i>Best Model (Ori/Con)</i>	<i>Ref'</i>
			Indian islands		(km ²)	25.4%)				
76	Vertebrates (Herpatofauna)	Archipelago	Martinique bank, West-Indian islands	28	0.002-0.8 (km ²)	41 (4, 9.8%)	77	1.88	Pow. (Con)	47
77	Vertebrates (Herpatofauna)	Archipelago	Mediterranean sea	14	84.9-25662 (km ²)	89 (40, 44.9%)	234	2.63	Exp. (Con)	16
78	Vertebrates (Herpatofauna)	Archipelago	Puerto-Rico bank, West-Indian islands	92	0.001-137 (km ²)	57 (20, 35.1%)	581	10.19	Pow. (Con)	47
79	Vertebrates (Herpatofauna)	Archipelago	Sea of Cortes, major islands	23	0.6-1173 (km ²)	85 (49, 57.7%)	212	2.49	Pow. (Con)	12
80	Vertebrates (Herpatofauna)	Archipelago	Southern Exuma Cays, West-Indian islands	20	0.019-9.26 (km ²)	18 (8, 44.4%)	68	3.78	Lin. (Con)	47
81	Vertebrates (Herpatofauna)	Archipelago	Turks bank, West-Indian islands	10	0.01-17.39 (km ²)	13 (6, 46.2%)	42	3.23	Lin. (Con)	47
82	Vertebrates (Herpatofauna)	Political	Sonora, Mexico and adjoining states	7	58238-315194 (km ²)	416 (169, 40.6%)	994	2.39	Neg.Exp. (Con)	25
83	Vertebrates (Herpatofauna-Amphibia)	Ecoregions	Australasia	66	1600-823000 (km ²)	528 (211, 40%)	1712	3.24	Mon. (Con)	56
84	Vertebrates (Herpatofauna-Amphibia)	Ecoregions	Indo-Malaysia	89	2600-663600 (km ²)	711 (382, 53.7%)	2220	3.12	Lin. (Con)	56
85	Vertebrates (Herpatofauna-Amphibia)	Ecoregions	Neoartic	102	3900-753800 (km ²)	267 (87, 32.6%)	1640	6.14	Neg.Exp. (Con)	56
86	Vertebrates (Herpatofauna-Amphibia)	Ecoregions	Neotropics	141	100-1916900 (km ²)	2167 (919, 42.4%)	8190	3.78	Pow. (Con)	56
87	Vertebrates (Herpatofauna-Amphibia)	Ecoregions	Paelearctic	182	2900-4639900 (km ²)	377 (117, 31%)	1920	5.09	Neg.Exp. (Con)	56
88	Vertebrates (Herpatofauna-Amphibia)	Ecoregions	Sub-Saharan Africa	96	1000-3053200 (km ²)	629 (237, 37.7%)	2669	4.24	Pow. (Con)	56
89	Vertebrates (Herpatofauna-Amphibia)	Inter-provincial	Global	9	16800-52731900 (km ²)	4587 (4355, 94.9%)	4826	1.05	P2 (Con)	56
90	Vertebrates (Herpatofauna-Reptiles)	Archipelago	Canary islands	7	290.5-2007 (km ²)	15 (5, 33.3%)	27	1.80	P2 (Con)	5

	<i>Major Taxon (Taxon)</i>	<i>system</i>	<i>Location</i>	<i>n</i>	<i>Area range (units)</i>	<i>Species (endemics, % endemics)</i>	<i>Number of occupancies</i>	<i>mean occupancy level</i>	<i>Best Model (Ori/Con)</i>	<i>Ref'</i>
91	Vertebrates (Herpatofauna-Reptiles)	Archipelago	Islands, north-eastern Adriatic coast	14	15-410 (km ²)	28 (6 , 21.4%)	170	6.07	Lin. (Con)	39
92	Vertebrates (Herpatofauna-Reptiles)	Ecoregions	Australasia	69	100-823000 (km ²)	1216 (412 , 33.9%)	6042	4.97	Gom. (Con)	56
93	Vertebrates (Herpatofauna-Reptiles)	Ecoregions	Indo-Malaysia	92	100-663600 (km ²)	1252 (537 , 42.9%)	5978	4.77	Pow. (Con)	56
94	Vertebrates (Herpatofauna-Reptiles)	Ecoregions	Neoarctic	89	100-753800 (km ²)	474 (135 , 28.5%)	3226	6.81	Mon. (Con)	56
95	Vertebrates (Herpatofauna-Reptiles)	Ecoregions	Neotropics	145	100-1916900 (km ²)	2164 (771 , 35.6%)	11768	5.44	Pow. (Con)	56
96	Vertebrates (Herpatofauna-Reptiles)	Ecoregions	Paelearctic	180	1400-4639900 (km ²)	789 (242 , 30.7%)	4931	6.25	Mon. (Con)	56
97	Vertebrates (Herpatofauna-Reptiles)	Ecoregions	Sub-Saharan Africa	98	200-3053200 (km ²)	1330 (478 , 35.9%)	6913	5.20	Wei.3 (Con)	56
98	Vertebrates (Herpatofauna-Reptiles)	Inter-provincial	Global	9	16800-52731900 (km ²)	6856 (6168 , 90%)	7607	1.11	Neg.Exp. (Con)	56
99	Vertebrates (Herpatofauna-Lizards)	Anthropogenic fragmented landscape	Reserves, Western Australia	23	34-5119 (ha)	69 (22 , 31.9%)	384	5.57	Mon. (Con)	37
100	Vertebrates (Herpatofauna-Lizards)	Anthropogenic fragmented landscape	Western Australia	26	0.5-174 (ha)	15 (2 , 13.3%)	106	7.07	Pow. (Con)	51
101	Vertebrates (Herpatofauna-Lizards)	Archipelago	Sea of Cortes	9	0.6-187 (km ²)	13 (1 , 7.7%)	77	5.92	Neg.Exp. (Con)	12
102	Vertebrates (Aves)	Anthropogenic fragmented landscape	Brazil	12	0.09-1.02 (ha)	19 (4 , 21.1%)	73	3.84	Lin. (Con)	2
103	Vertebrates (Aves)	Anthropogenic fragmented landscape	Canyon habitats, San Diego County, California, USA	37	0.4-102 (ha)	9 (1 , 11.1%)	73	8.11	Lin. (Con)	52
104	Vertebrates (Aves)	Anthropogenic fragmented landscape	Forest islands, central New-Jersey, USA	10	0.01-24 (ha)	35 (0 , 0%)	205	5.86	Pow. (Con)	29
105	Vertebrates (Aves)	Anthropogenic fragmented landscape	Sewage works, Britain	12	3-400 (ha)	24 (5 , 20.8%)	109	4.54	Mon. (Con)	28
106	Vertebrates (Aves)	Anthropogenic fragmented	Singapore	17	7-935	166 (26 ,	1234	7.43	Mon. (Con)	13

	<i>Major Taxon (Taxon)</i>	<i>system</i>	<i>Location</i>	<i>n</i>	<i>Area range (units)</i>	<i>Species (endemics, % endemics)</i>	<i>Number of occupancies</i>	<i>mean occupancy level</i>	<i>Best Model (Ori/Con)</i>	<i>Ref'</i>
		landscape			(ha)	15.7%)				
107	Vertebrates (Aves)	Anthropogenic fragmented landscape	Small woodlots, Wisconsin, USA	9	0.2-4.41	26 (8 , 30.8%)	108	4.15	Neg.Exp. (Con)	36
108	Vertebrates (Aves)	Anthropogenic fragmented landscape	Urban parks, Madrid, Spain	25	1-118.2	32 (6 , 18.8%)	293	9.16	Exp. (Con)	27
109	Vertebrates (Aves)	Archipelago	Baubyan islands, Northern Philippines	5	0.7-196	137 (46 , 33.6%)	332	2.42	Kob. (Con)	45
110	Vertebrates (Aves)	Archipelago	Canary islands	7	290.5-2007	78 (9 , 11.5%)	364	4.67	Lin. (Con)	5
111	Vertebrates (Aves)	Archipelago	Cape-Verde	12	1.4-991	55 (4 , 7.3%)	344	6.25	Pow. (Con)	4
112	Vertebrates (Aves)	Archipelago	Dahlak Archipelago	26	2-2143	38 (16 , 42.1%)	162	4.26	Com.Log. (Con)	6
113	Vertebrates (Aves)	Archipelago	Northern islands, Sea of Cortes	16	0.03-15.03	32 (10 , 31.3%)	147	4.59	Rat. (Con)	12
114	Vertebrates (Aves)	Archipelago	Southern islands, Sea of Cortes	16	0.05-187	28 (0 , 0%)	218	7.79	Kob. (Con)	12
115	Vertebrates (Aves)	Archipelago	Thousand Island lake, china	42	0.3-1289	93 (25 , 26.9%)	1193	12.83	Arc.Log. (Con)	54
116	Vertebrates (Aves)	Ecoregions	Australasia	69	100-823000	1605 (409 , 25.5%)	16038	9.99	Mon. (Con)	56
117	Vertebrates (Aves)	Ecoregions	Indo-Malaysia	93	300-663600	1781 (161 , 9%)	30768	17.28	Exp. (Con)	56
118	Vertebrates (Aves)	Ecoregions	Neoartic	118	100-1032800	728 (74 , 10.2%)	21702	29.81	Com.Log. (Con)	56
119	Vertebrates (Aves)	Ecoregions	Neotropics	150	100-1916900	3687 (569 , 15.4%)	54165	14.69	Exp. (Con)	56
120	Vertebrates (Aves)	Ecoregions	Palaearctic	195	1400-4639900	1570 (159 , 10.1%)	46043	29.33	Mon. (Con)	56
121	Vertebrates (Aves)	Ecoregions	Sub-Saharan Africa	100	100-3053200	2046 (239 , 11.7%)	36905	18.04	Exp. (Con)	56

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	<i>Major Taxon (Taxon)</i>	<i>system</i>	<i>Location</i>	<i>n</i>	<i>Area range (units)</i>	<i>Species (endemics, % endemics)</i>	<i>Number of occupancies</i>	<i>mean occupancy level</i>	<i>Best Model (Ori/Con)</i>	<i>Ref'</i>
122	Vertebrates (Aves)	Inland water bodies	Bogs, Wetland habitats, SW Sweden	47	8-66 (ha)	13 (0, 0%)	161	12.38	Neg.Exp. (Con)	33
123	Vertebrates (Aves)	Inland water bodies	Wet meadows, Wetland habitats, SW Sweden	15	2-22 (ha)	11 (2, 18.2%)	60	5.45	Neg.Exp. (Con)	33
124	Vertebrates (Aves)	Inter-provincial	Global	9	16800-52731900 (km ²)	9008 (6965, 77.3%)	11861	1.32	Neg.Exp. (Con)	56
125	Vertebrates (Aves)	Naturally fragmented	Forest patches, Southern Brazil	12	0.5-840 (ha)	189 (36, 19.1%)	938	4.96	Com.Log. (Con)	3
126	Vertebrates (Aves)	Naturally fragmented	Oaxaca, Mexico	17	2-159246 (ha)	60 (0, 0%)	478	7.97	Gom. (Con)	55
127	Vertebrates (Aves- Birds of prey)	Archipelago	Mediterranean sea	43	143-25662 (km ²)	25 (0, 0%)	307	12.28	Pow. (Con)	23
128	Vertebrates (Mammals)	Anthropogenic fragmented landscape	Atlantic forest fragments, Brazil	8	1.2-13.3 (ha)	12 (1, 8.3%)	62	5.17	Neg.Exp. (Con)	21
129	Vertebrates (Mammals)	Anthropogenic fragmented landscape	Reserves, Western Australia	23	34-5119 (ha)	24 (5, 20.8%)	171	7.13	Neg.Exp. (Con)	38
130	Vertebrates (Mammals)	Anthropogenic fragmented landscape	Temperate rain forest, Olympic Peninsula, Washington, USA	20	0.93-58.91 (ha)	18 (2, 11.1%)	142	7.89	Lin. (Con)	42
131	Vertebrates (Mammals)	Archipelago	Alexander archipelago, Alaska	24	10.1-5777 (km ²)	23 (4, 17.4%)	199	8.65	Com.Log. (Con)	15
132	Vertebrates (Mammals)	Archipelago	Baubyan islands, Northern Philippines	5	0.7-196 (km ²)	20 (13, 65%)	35	1.75	Pow. (Con)	45
133	Vertebrates (Mammals)	Archipelago	Great Salt Lake, Utah, USA	7	9-10767 (ha)	27 (11, 40.7%)	63	2.33	Lin. (Con)	17
134	Vertebrates (Mammals)	Archipelago	Islands, Gulf of Maine, USA	8	1.243-279 (km ²)	35 (11, 31.4%)	122	3.49	Lin. (Con)	18
135	Vertebrates (Mammals)	Archipelago	Islands, north-eastern Adriatic coast	14	15-410 (km ²)	13 (2, 15.4%)	86	6.62	Lin. (Con)	39
136	Vertebrates (Mammals)	Archipelago	Philippine Trench	9	22-99078 (km ²)	35 (15, 42.9%)	123	3.51	Lin. (Con)	35
137	Vertebrates (Mammals)	Archipelago	Sea of Cortes	28	0.32-1173	77 (75,)	79	1.03	Arc.Log. (Con)	12

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	<i>Major Taxon (Taxon)</i>	<i>system</i>	<i>Location</i>	<i>n</i>	<i>Area range (units)</i>	<i>Species (endemics, % endemics)</i>	<i>Number of occupancies</i>	<i>mean occupancy level</i>	<i>Best Model (Ori/Con)</i>	<i>Ref'</i>
					(km ²)	97.4%)				
138	Vertebrates (Mammals)	Archipelago	Thousand Islands Region, New-York, USA	20	0.04-591 (ha)	10 (0, 0%)	50	5.00	Gom. (Con)	40
139	Vertebrates (Mammals)	Ecoregions	Australasia	67	100-823000 (km ²)	674 (166, 24.6%)	3684	5.47	Com.Log. (Con)	56
140	Vertebrates (Mammals)	Ecoregions	Indo-Malaysia	93	300-663600 (km ²)	830 (126, 15.2%)	11697	14.09	Exp. (Con)	56
141	Vertebrates (Mammals)	Ecoregions	Neoarctic	119	100-1032800 (km ²)	481 (65, 13.5%)	7658	15.92	Neg.Exp. (Con)	56
142	Vertebrates (Mammals)	Ecoregions	Neotropics	146	100-1916900 (km ²)	1227 (127, 10.4%)	23383	19.06	P2 (Con)	56
143	Vertebrates (Mammals)	Ecoregions	Palaearctic	193	2900-4639900 (km ²)	905 (120, 13.3%)	14046	15.52	Mon. (Con)	56
144	Vertebrates (Mammals)	Ecoregions	Sub-Saharan Africa	98	200-3053200 (km ²)	1039 (195, 18.8%)	10964	10.55	Pow. (Con)	56
145	Vertebrates (Mammals)	Inter-provincial	Global	9	16800-52731900 (km ²)	4541 (3846, 84.7%)	5295	1.17	Neg.Exp. (Con)	56
146	Vertebrates (Mammals)	Naturally fragmented	Mountain-tops, great basin of north America, USA	17	31.1-3051 (km ²)	13 (1, 7.7%)	97	7.46	Com.Log. (Con)	11
147	Vertebrates (Mammals)	Naturally fragmented	Montane islands, American Southwest	27	6.89-11134 (km ²)	23 (5, 21.7%)	154	6.70	Kob. (Con)	41
148	Vertebrates (Mammals-Bats)	Archipelago	Antillean islands	22	13-105805 (km ²)	57 (31, 54.4%)	189	3.32	Kob. (Con)	7
149	Vertebrates (Mammals-Bats)	Archipelago	Islands, Bahamas	23	2.18-5959 (km ²)	13 (4, 30.8%)	117	9.00	Pow. (Con)	48
150	Vertebrates (Mammals-Bats)	Archipelago	Islands, Greater Antilles	19	5.2-105805 (km ²)	37 (13, 35.1%)	209	5.65	P2 (Con)	48
151	Vertebrates (Mammals-Bats)	Archipelago	Islands, Lesser Antilles	23	5.49-1628 (km ²)	24 (7, 29.2%)	225	9.38	Pow. (Con)	48
152	Vertebrates (Mammals-Rodents)	Anthropogenic fragmented landscape	Coastal Southern California	24	0.41-84 (ha)	9 (0, 0%)	67	7.44	Neg.Exp. (Con)	10

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	<i>Major Taxon (Taxon)</i>	<i>system</i>	<i>Location</i>	<i>n</i>	<i>Area range (units)</i>	<i>Species (endemics, % endemics)</i>	<i>Number of occupancies</i>	<i>mean occupancy level</i>	<i>Best Model (Ori/Con)</i>	<i>Ref'</i>
153	Vertebrates (Mammals-Rodents)	Archipelago	Virginia barrier islands, USA	9	29-2197 (ha)	5 (0, 0%)	19	3.80	Pow. (Con)	24
154	Vertebrates (Mammals-Monkeys)	Anthropogenic fragmented landscape	Udzungwa Mountains of Tanzania	22	0.06-526.32 (km ²)	7 (1, 14.3%)	69	9.86	Kob. (Con)	43

Pow. – Power; **Pow.Ros.** – Power Rosenzweig; **Ext.P1**– Extended Power 1; **Ext.P2**– Extended Power 2; **P1** – Persistence Function 1; **P2** – Persistence Function 2; **Exp.** – Exponential; **Kob.** – Kobayashi Logarithmic; **Mon.** – Monod; **MMF.** – Morgan-Mercer-Flodin; **Arc.Log.** – Archibald Logistic; **Neg.Exp.** – Negative Exponential; **Chp.Ric.** – Chapman-Richards; **Wei.3** – Weibull-3; **Wei.4** – Weibull-4; **Asy.** – Asymptotic; **Rat.** – Rational. **Gom.** – Gompertz; **Beta.P.** – Beta-P; **Com.Log.** - Common Logistic; **EVF.** – Extreme-Value Function; **Lom.** – Lomolino function.

Appendix S3

Linear regression between the expected and observed $wAICc$ of the constrained form (table S3) with additional focus on the Monod and negative exponential functions (figure S1).

Table S3:

For each of the twelve functions, the result of linear regression of the observed $wAICc$ of the constrained form against its expected $wAICc$, if the original and constrained forms have identical log likelihoods. N is the number of datasets used for the regression, while 'Low' and 'High' stand for the lower and higher values of the 95% confidence intervals around the intercept and slope. Cases in which the confidence interval of the intercept or slope did not overlap with 0 and 1 (respectively) are given in bold face.

<i>Model</i>	<i>N</i>	<i>R</i> ²	<i>Sig.</i>	<i>Constant</i>			<i>Slope</i>		
				<i>Estimate</i>	<i>Low</i>	<i>High</i>	<i>Estimate</i>	<i>Low</i>	<i>High</i>
Power	154	0.772	<0.001	-0.002	-0.076	0.071	0.997	0.910	1.084
Linear	154	0.998	<0.001	-0.001	-0.007	0.005	1.000	0.993	1.008
Kobayashi	154	0.755	<0.001	-0.069	-0.152	0.014	1.068	0.970	1.165
Exponential	154	1.000	<0.001	0.000	-0.001	0.000	1.000	1.000	1.001
Monod	149	0.441	<0.001	-0.329	-0.538	-0.120	1.338	1.092	1.584
Negative Exponential	151	0.389	<0.001	-0.470	-0.726	-0.214	1.481	1.180	1.782
P2	151	0.820	<0.001	0.021	-0.044	0.086	0.972	0.898	1.045
Weibull	151	0.951	<0.001	0.011	-0.021	0.043	0.988	0.952	1.025
Gompertz	145	0.999	<0.001	0.000	-0.004	0.005	0.999	0.994	1.004
Common Logistic	149	0.994	<0.001	-0.003	-0.014	0.008	1.004	0.991	1.017
Archibald Logistic	151	0.903	<0.001	0.035	-0.009	0.080	0.961	0.910	1.012
Rational	148	0.998	<0.001	-0.002	-0.008	0.004	1.002	0.994	1.009

Figure S1: The difference between the observed and expected (under identical log-likelihood) AICc weight of the constrained form, plotted against the cumulative AICc weight of the SAR function in the 24 SAR models analysis, for the (a) Monod and (b) Negative Exponential SAR functions. Note that deviation from zero difference occurs when the model poorly describes the empirical data (relative to other SAR functions).

