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Evaluation of Neutron Cross Sections for Hafnium in the Resolved Resonance Range

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The international High Priority Request list notes: - "In the nuclear industry hafnium is used as neutron absorbing material to regulate the fission process. Interpretation of critical experiments with UOx fuel conducted by CEA in the AZUR zero-power reactors has shown systematic under-estimation of the reactivity worth that may be attributed to an overestimated natural hafnium capture cross section in the epi-thermal energy range"

To service the request for improved resonance data a PhD project has:-

a) Improved REFIT R-matrix evaluation code.

b) Obtained hafnium oxide samples enriched in Hf176, 177, 178, 179 isotopes.

c) Gained support from NUDAME and EUFRAT projects.

d) Prepared enriched and natural Hf samples.

e) Performed capture and transmission Time of Flight measurements at the GELINA linear accelerator.

f) Analysed the capture counts to generate yields using AGS and AGL codes.

g) Used REFIT to perform least squares analysis of GELINA measurements.

(Included previous ORNL, Harwell and RPI transmissions and capture yields.)

h) Submitted results to EXFOR.

i) Included resolved resonance parameters in JEFF evaluations taking the resolved range to over 1 keV.

j) Tested evaluations with suitable benchmarks.

k) Passed resolved resonance data to CEA Cadarache for unresolved analysis.

Resultant Hf evaluations will be included in JEFF3.2.

I. INTRODUCTION

The large absorption cross-section of hafnium makes it a candidate for use in reactor control rods to regulate the fission process. As it is a resonance absorber, it is favoured for use in thermal fission reactors with harder neutron spectra, such as those using MOX fuel. Hence, it is important to understand the hafnium cross-section in the resolved resonance energy range.

Calculations on the AZUR criticality experiments conducted by CEA, using the latest JEFF3.1 isotopic hafnium evaluations based on recent RPI measurements [1], indicate a measured rod worth of 7000 pcm being out by ∼30 pcm [2]. This may be due to an overesti-mate of the natural hafnium capture cross section. Res-onances below ∼180 eV are reasonably defined by recent measurements at RPI [2]. Above ∼250 eV unresolved resonances are present in JEFF3.1. The Hf isotope files can be improved by extending the resolved resonance range to higher energies, thereby negating uncertainties

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Table 1. Hafnium Enrichments.

Isotope	^{176}Hf	^{177}Hf	^{178}Hf	^{179}Hf	^{180}Hf
^{176}Hf	**65.0**	22.9	6.3	1.8	4.0
^{177}Hf	1.0	**85.4**	11.3	0.9	1.4
^{178}Hf	0.8	1.9	**92.4**	3.3	1.6
^{179}Hf	0.2	1.3	4.1	**72.1**	22.3

from the treatment of the unresolved resonance range. Ideally, this objective can be achieved through capture cross-section measurements on hafnium identified on the NEA Nuclear Data High Priority Request List [3].

II. NUDAME AND EUFRAT PROJECTS

The EUFRAT [4] project and predecessor NUDAME offer opportunities for researchers to access EC-JRC-IRMM accelerator facilities. Approved requests for Hf measurements allowed visits in 2007–2009 to measure Hf samples on the GELINA LINAC [5].

III. EXISTING MEASUREMENTS

The JEFF3.1 evaluation for Hf includes resolved resonance parameters from Trbovich [1]. His thesis reviews the status of Hf measurements prior to RPI's natural metal and enriched solution transmission and capture measurements. It highlights early transmission measurements by Harvey [6] plus capture and transmission measurements by Moxon [7]. All three authors kindly supplied transmissions/yields for potential inclusion in EXFOR [8]. Noguère [9] considers more recent cold and room temperature transmission measurements by Siegler [10]. Study of all these indicated the importance of using isotopically enriched samples to allocate resonances to isotopes.

IV. ENRICHED SAMPLES

Isotopically enriched samples were kindly loaned by INRNE Sofia [11]. The % enrichments of the Hf in the HfO_2 samples are given in Table 1. The samples were in thin walled aluminium cans. In all cases, ^{174}Hf was less than 0.05% abundant.

V. EXPERIMENTAL SETUP

The IRMM GEel pulsed LINear Accelerator (GELINA) [5] operates at frequencies of between 50 and 800 Hz. A compressed pulse of electrons with a width of ∼1 nanosecond strikes the rotating uranium target. The resulting Bremsstrahlung radiation produces a fission-like neutron spectrum via (γ,n) and (γ,f) reactions in the uranium. The fast neutrons are moderated by two adjacent water-filled beryllium

containers to give neutrons at energies between ∼1 meV and ∼20 MeV. These moderated pulsed neutrons are collimated into beams down the 12 flight paths arranged around the target. Stability and intensity are monitored by two BF_3 proportional counters.

Capture measurement stations are positioned at the 10, 30 and 60 m flight paths with interstitial fixed anti-overlap filters (^{10}B or ^{nat}Cd) and changeable background filters (Ag, Bi, Co, Na, S, and W). The γ-rays originating from the capture reaction are detected with C_6D_6-based liquid scintillators [12] of 10 cm diameter and 7.5 cm height. Capture events, and neutron time-of-flight, determined using the IRMM Fast Time Digitizer [13] with a 0.5 ns resolution, were recorded on the Geel DAC2000 data acquisition system [14].

VI. GEEL MEASUREMENTS

In April 2007, GELINA was used at 50 Hz to measure 0.026, 0.079 and 0.024 mm thick natural Hf samples at the 12.89 m measurement station. In October 2007, a 1 mm natural sample was measured at 800 Hz in the 58.586 m station introducing a ^{10}B overlap filter. In 2008, the enriched samples were prepared and ^{177}Hf (thickness 3.223 mm / 1.91×10^{-3} atoms/barn), ^{178}Hf ($2.502 / 1.80 \times 10^{-3}$), ^{178}Hf ($1.052 / 0.82 \times 10^{-3}$), ^{179}Hf ($2.452 / 2.14 \times 10^{-3}$) and ^{nat}Hf ($1.081 / 4.5953 \times 10^{-3}$) measurements were made at 800 Hz on the 12.95 m station retaining the ^{10}B filter. Next, the 28.82 m station was used to measure ^{176}Hf ($2.062 / 2.17 \times 10^{-3}$), ^{177}Hf ($3.223 / 1.91 \times 10^{-3}$), ^{178}Hf ($2.502 / 1.80 \times 10^{-3}$), ^{179}Hf ($2.452 / 2.14 \times 10^{-3}$) and ^{nat}Hf ($1.081 / 4.5953 \times 10^{-3}$) at 800 Hz with ^{10}B filter. In October 2008, ^{176}Hf ($2.062 / 2.17 \times 10^{-3}$) and ^{179}Hf ($2.452 / 2.14 \times 10^{-3}$) measurements were made at 50 Hz on the same station but with ^{nat}Cd filters. In all cases, the incident neutron flux was continuously measured with a ^{10}B ionisation chamber placed ∼1 m in front of the sample. The measurements were designed to optimise counts from 0.1 eV to several keV. Finally a thick (16 / 6.893×10^{-2}) natural Hf sample was measured at the 49.34 m station with a ^{nat}Cd filter to supplement other Siegler's 2001 transmission measurements [10] and to help understand some resolution problems and check the nuclei radii used in the analysis. As well as the main measurements, ancillary measurements were made with various filters present to deduce the background count.

VII. ANALYSIS OF THE MEASUREMENTS

The Analysis of Geel List-mode (AGL) code package [15] was used to bin the raw measurement data into 30720 variable width time-of-flight channels to cover the full energy range in sufficient detail. Each measurement is performed over a number of one hour cycles and AGL rejects any cycles with unstable beam conditions. It checks all results are meaningful relative to known crite-

ria regarding apparatus used. The code then outputs a spectrum (histogram) of reliable counts for each detector used in the measurement.

The Analysis of Geel Spectra (AGS) code package [16, 17] performs a dead time correction for each detector spectrum and merges them to form a single spectrum. This operation was repeated for the flux detectors and uncertainties in both are formed. Using the black resonances in the ancillary measurements, the time dependence of the background was manually fitted for both the capture and flux measurements. The capture spectrum is then divided by the flux spectrum after alignment. The resultant yields were normalised using the saturated, low energy ^{177}Hf resonances and will be available in EXFOR [8].

VIII. STABILISATION OF THE REFIT CODE

REFIT is a widely used Least-Square Fitting Program for Resonance Analysis of Neutron Transmission, Capture, Fission and Scattering Data. REFIT-2007 was consolidated during the initial Hf analysis. The code was then used at a summer school in Geel in 2008 and further modification suggested before application to the final analysis as REFIT-2009 [18].

IX. EVALUATION

The resonance analysis of the measured hafnium was performed in several stages. The allocation of resonances was primarily performed by overlaying plots of the capture yields from the Geel 30 m measurements of the enriched oxide and natural 1mm foil hafnium samples, plus Moxon's enriched sample measurements [7], particularly for ^{180}Hf. This process is demonstrated in Fig. 1 where a doublet in ^{177}Hf overlying a single ^{179}Hf resonance is replaced by doublets in both isotopes.

Using resonances in JEFF3.1 and ENDF/B-VI.8 evaluations, plus the new resonances, prior sets of resonance parameters evolved during the fitting process.

For ^{177}Hf and ^{179}Hf, where there are two possible s-wave resonance spins for each isotope, the spin value was arbitrarily assigned such that the distribution between the two spin values was approximately equal.

REFIT needs experimental parameters input. An effective temperature of 302.9 K was applied. The efficiency for the detection of neutron capture in a given isotope is proportional to the binding energy for the C_6D_6 detectors. Isotopic efficiencies were formed, relative to unity in ^{177}Hf, (including accounting for capture to the meta-stable state in ^{179}Hf). Quoted flight path lengths were adjusted by REFIT and the resultant values used. In the analysis of the capture, an energy dependent scattered neutron detection efficiency was included. Nuclear parameters for impurities, canning and sample holders were also included (Zr, O, Al, Br, Mn).

Average capture widths for each isotope were determined from a weighted average of fitted capture widths
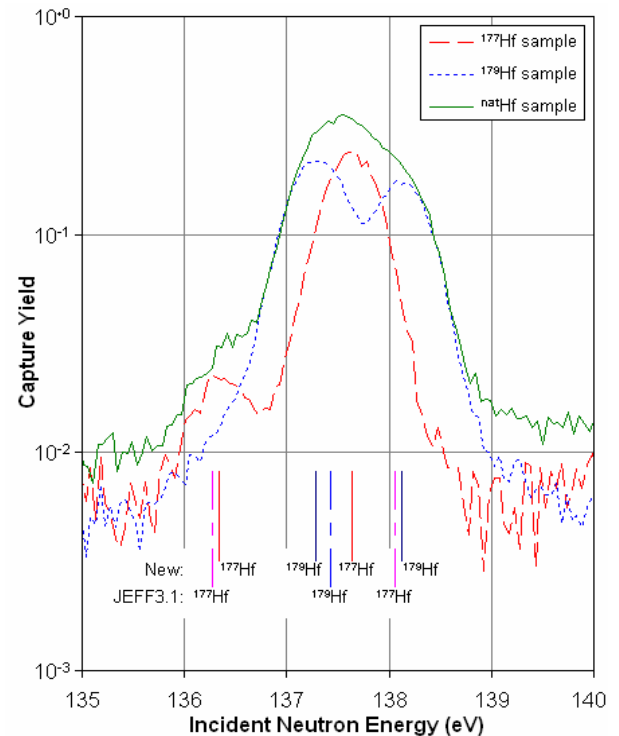

Fig. 1. (Color online) Comparison of capture yield curves of Hf sample measurements with resonance allocation from JEFF3.1 (long markers) and this work (short markers).

for that isotope. For resonances in the even-mass isotopes, they were used where Γ_n was much less than Γ_γ. They were used for all ^{177}Hf and ^{179}Hf resonances above 50 eV and for resonances below 50 eV where the resonance area was deemed insensitive to Γ_γ. In other cases individual Γ_γ's were treated as variables but it was found that if the calculation was insensitive to the parameter, the "fitted" value would differ with each run of REFIT without converging to any one value and have a high uncertainty associated with it and potentially be very different to the starting (JEFF3.1) value. This had to be manually detected.

Hafnium resonance parameters for the 0.5 eV to 1 keV neutron energy range were derived by the simultaneous analysis in $\sim$ 50 eV energy segments of several measurement data sets using the REFIT code.

Re-analysis of RPI's measurements using isotopically-enriched solution samples derived different parameters for the 7.8 eV doublet [19]. Using these as fixed input, resonance parameters within the 0.5 – 20 eV neutron energy range were derived using the Geel 12 m oxide and 1mm metal capture measurement data, together with the RPI transmission measurements of 0.001, 0.002, 0.004, 0.010, 0.020 and 0.050 inch natural hafnium metallic samples. Published thermal capture cross sections were reviewed, adjusted to modern standards and the inverse variance weighted results used to calculate bound levels; the REFIT run was repeated. The resonance parameters of 20 – 1000 eV energy range

Table 2. Resolved Resonance Statistics.

	RR Top limit (eV)		No. Resonances in RR	
	JEFF3.1	New file	JEFF3.1	New file
^{174}Hf	220	250	12	14
^{176}Hf	700	3000	19	74
^{177}Hf	250	1000	94	331
^{178}Hf	1500	3000	23	55
^{179}Hf	250	1000	50	219
^{180}Hf	2500	3000	16	21

were derived using the Geel capture yield data, together with the 16 mm natural Hf transmission measurement and those of Siegler [10]. The Geel 12 m capture data were not used above 250 eV due to poor experimental resolution.

The quality of the fit for a segment was assessed by visual inspection of the fitted curve relative to the experimental data, using REFIT's graphical output, the χ^2 values for individual data sets and the overall χ^2 value for the run.

At neutron energies around 1 keV, the experimental resolution and Doppler effects mean that the closely spaced ^{177}Hf and ^{179}Hf resonances cannot be resolved, but broad resonances of ^{176}Hf, ^{178}Hf and ^{180}Hf are still resolvable to around 3 keV. Further analysis of the $1 - 3$ keV neutron energy range took place within these constraints. Unfortunately, features in the Beer and Macklin [20,21] evaluation could not be seen in Geel measurements preventing use of their data at higher energies.

X. RESONANCE PARAMETERS

Resonance parameters in ENDF6 format were concatenated for each isotope and used to replace parameters in the current JEFF3.1 files giving the statistics in Table 2.

XI. TESTING

The new evaluations have been applied using the MONK Monte-Carlo code [22] to assess two integral benchmarks containing different size Hf blocks within enriched fuel. K-eff was reduced by 100 pcm for the case with the small block and 160 pcm for the large block leaving it supercritical by 100 pcm. Further study indicated improvement to be due to addition of resonances above 250 eV.

XII. CONCLUSION

New Hf resolved resonance evaluations have been generated and submitted to JEFF. Although our initial test-ing yields an improved prediction, a reduction in K-eff seems contrary to the initial indication in the request list. We await with interest the CEA's findings but also note we are reducing the resonance integral yet increasing absorption at higher energies due to adding resonances. A PhD thesis will fully describe the work [23].

ACKNOWLEDGMENTS

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