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1 **Factors affecting the spatial pattern of bedrock groundwater recharge at the**  
2 **hillslope scale**

3

4

5 Running head: Spatial patterns of bedrock groundwater recharge

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7

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17

18

19 **Abstract**

20 The spatial patterns of groundwater recharge on hillslopes with a thin soil mantle overlying bedrock are  
21 poorly known. Complex interactions between vertical percolation of water through the soil,  
22 permeability contrasts between soil and bedrock, and lateral redistribution of water result in large  
23 spatial variability of water moving into the bedrock. Here, we combine new measurements of saturated  
24 hydraulic conductivity of soil mantle and bedrock of the well-studied Panola Mountain experimental  
25 hillslope with previously collected (sub)surface topography and soil depth data to quantify the factors  
26 affecting the spatial pattern of bedrock groundwater recharge.

27 We use geostatistical characteristics of the measured permeability to generate spatial fields of saturated  
28 hydraulic conductivity for the entire hillslope. We perform simulations with a new conceptual model  
29 with these random fields and evaluate the resulting spatial distribution of groundwater recharge during  
30 individual rainstorms and series of rainfall events. Our simulations show that unsaturated drainage from  
31 soil into bedrock is the prevailing recharge mechanism and accounts for 60% of annual groundwater  
32 recharge. Therefore, soil depth is a major control on the groundwater recharge pattern through available  
33 storage capacity and controlling the size of vertical flux. The other 40% of recharge occurs during  
34 storms that feature transient saturation at the soil-bedrock interface. Under these conditions, locations  
35 that can sustain increased subsurface saturation due to their topographical characteristics or those with  
36 high bedrock permeability will act as hotspots of groundwater recharge when they receive lateral flow.

37

38 **1. Introduction**

39 The hierarchy of controls on patterns of groundwater recharge at varying spatial scales is poorly  
40 understood (Scanlon *et al.*, 2002). At the regional and watershed scale, where groundwater recharge is  
41 the renewable resource of large aquifers, recent research has demonstrated the vulnerability of  
42 groundwater recharge due to land use and climate change (Barron *et al.*, 2012; Flint *et al.*, 2014; Mair  
43 *et al.*, 2013). At smaller spatial scales of 1-10 m<sup>2</sup>, lysimeter and tracer studies have shown large  
44 temporal variation in such point scale recharge fluxes under different climate regimes (Pangle *et al.*,  
45 2014; Allison *et al.*, 1994).

46

47 Few investigations have yet examined hillslope-scale controls on the spatio-temporal variability of  
48 groundwater recharge. This is problematic because hillslopes are the fundamental hydrological unit  
49 (Troch *et al.*, 2013) and the scale at which flow accumulation occurs in the landscape. Therefore a key  
50 challenge in groundwater recharge research is the prediction and assessment of its variability at the  
51 hillslope scale (Allison *et al.*, 1994; De Vries and Simmers, 2002). Though spatial variability of  
52 groundwater recharge at hillslope scale may not be critical for water resource management (Flint *et al.*,  
53 2012), it may have profound implications for solute and contaminant transport. Zones of focused  
54 recharge can allow contaminants to move quickly from the unsaturated zone to underlying aquifers and  
55 streams (Scanlon *et al.*, 2002). Here we define hillslope groundwater recharge as all water that is  
56 transferred from the soil into the bedrock, where it is no longer available for root water uptake. At the  
57 hillslope scale, such recharge may feed aquifers through deep percolation, but also fast flow through  
58 fractures that may contribute to catchment streamflow farther down-valley (Torres *et al.*, 1997;  
59 Montgomery *et al.*, 2002; Gleeson *et al.*, 2009; Graham *et al.*, 2010; Gabrielli *et al.*, 2012).

60

61 Groundwater recharge can be a substantial part of the water balance partitioning between vertical and  
62 lateral flow. Heppner *et al.* (2007) measured a range of 21% to 52% of annual rainfall under a grass  
63 lysimeter during five years of natural rainfall conditions. Experiments on small hillslopes have  
64 estimated groundwater recharge of 34-41% (Ontario, Canada; Buttle and McDonald, 2002), 41%  
65 (Oregon, USA; Graham *et al.*, 2010), 35-55% (Japan; Kosugi *et al.*, 2006) and 94% (Georgia, USA;  
66 Tromp-van Meerveld *et al.*, 2007), while runoff ratios on these hillslopes have been estimated to be  
67 respectively 30-43% (Peters *et al.*, 1995), 13% (Gabrielli *et al.*, 2012), 3.5-7.4% (Kosugi *et al.*, 2006)  
68 and 5% (Tromp-van Meerveld and McDonnell, 2006a).

69 In other words, depending on the nature and variability of the soil-bedrock interface, the volume of  
70 water that moves vertically past the soil-bedrock interface can be equal to or larger than the volume of  
71 water that is routed laterally downslope along that interface. These relative values depend mainly on  
72 bedrock permeability, soil depth and slope angle (Asano *et al.*, 2002; Hopp and McDonnell, 2009; Ebel  
73 and Loague, 2008). While experimental studies have shown that return flow from bedrock into soil can  
74 be caused by variability of bedrock conductivity (Wilson and Dietrich, 1987; Shand *et al.*, 2007) and  
75 hillslopes rarely experience a uniformly rising and falling perched groundwater table at the soil-bedrock  
76 interface (Salve *et al.*, 2012), the effects of spatial variability of hydraulic conductivity on groundwater  
77 recharge have not been quantified. The filling, leakage and lateral spilling of the hillslope-scale patches  
78 of transient saturation at the soil-bedrock interface are now seen as a common behavior across many  
79 environments (Bachmair and Weiler, 2011; McDonnell, 2013). However, the groundwater recharge  
80 consequences of this behavior have not yet been examined.

81

82 We present new measurements and new model results from the well-described Panola experimental  
83 hillslope (see Tromp-van Meerveld and McDonnell (2009) for a site review) to examine the hierarchy  
84 of factors affecting the spatial pattern of bedrock groundwater recharge. Considering the known  
85 bedrock topography and bedrock permeability at this hillslope, we hypothesize that saturation at the  
86 soil-bedrock interface (SBI) is a driver of increased bedrock groundwater recharge (GWR). We further  
87 hypothesize that rainfall dynamics are an important on/off switch for groundwater recharge patterns.  
88 We developed a new model (building upon Appels *et al.* (2011)) to examine a number of specific  
89 questions:

90

- 91 • How do spatial patterns of soil- and bedrock hydraulic conductivity (derived from  
92 new point-scale measurements) influence hillslope-scale transient soil saturation and  
93 resulting bedrock groundwater recharge?
- 94 • What is the sequence of controls on the spatial pattern of groundwater recharge?
- 95 • How do within- and between-storm rainfall conditions influence this sequencing and  
96 ultimate process hierarchy?

## 97 **2. Study Site**

98 The study hillslope is part of the Panola Mountain Research Watershed (PMRW), located in the  
99 Georgia Piedmont, southeast of Atlanta (GA, USA). In 1995, a 29x51 m hillslope was instrumented  
100 with 135 crest-stage gauges, 29 recording wells, and a 20 m wide trench at the downhill boundary,  
101 excavated down to competent bedrock. Detailed site and instrumentation descriptions can be found

102 elsewhere (Freer *et al.*, 2002; Tromp-van Meerveld and McDonnell, 2006a; 2006b; 2007; 2009). Here,  
103 we only describe the soil and bedrock characteristics that are relevant for the current modeling study.

104

105 The PMRW is underlain by Panola Granite bedrock, a 300 to 360 Ma old biotite-oligoclase-quartz-  
106 microcline granite formation. The primary conductivity of the granite matrix is estimated to be  $7 \times 10^{-6}$   
107  $\text{m yr}^{-1}$ , with a secondary regolith conductivity of  $1 \times 10^{-3} \text{ m yr}^{-1}$  (White *et al.*, 2001). The effective  
108 hydraulic conductivity of the weathered granite was found to be in the range of  $8.8 \times 10^{-8}$  to  $5.1 \times 10^{-6} \text{ m}$   
109  $\text{s}^{-1}$  in falling head experiments (White *et al.*, 2002) and  $1.6 \times 10^{-6} \text{ m s}^{-1}$  in an area-average sprinkling  
110 experiment (Tromp-van Meerveld *et al.*, 2007).

111 Throughout the watershed, the top 2 to 4 m of the bedrock is weathered to porous soft disintegrated  
112 granite (saprolite) that has retained the original granodiorite texture (White *et al.*, 2001). Tromp-van  
113 Meerveld *et al.* (2007) did not find saprolite at the monitored hillslope site, except at the deepest soil  
114 section, 20-22 m upslope from the trench face (Fig. 1).

115

116 The soil depth ranges from 0.0 to 1.8 m (average 0.63 m) and consists of hillslope sediments and  
117 colluvium from upslope erosion (Freer *et al.*, 1997; White *et al.*, 2001; Tromp-van Meerveld *et al.*,  
118 2007). The coarse sandy loam does not have pronounced layering or discernible structure except for a  
119 0.15 m thick organic horizon (Tromp-van Meerveld and McDonnell, 2006a). A large part of subsurface  
120 flow captured at the hillslope trench at the slope base takes place in macropores and soil pipes (Freer *et*  
121 *al.*, 2002; Tromp-van Meerveld and McDonnell, 2006b).

122

123 Average seasonal hillslope runoff coefficients for fall, winter, spring, and summer periods are 6, 10, 1,  
124 <1 % respectively, resulting in a yearly average hillslope runoff coefficient of 5 % (Tromp-van  
125 Meerveld and McDonnell, 2006a). Accounting for evapotranspiration by the oak-hickory forest,  
126 groundwater recharge losses to the bedrock are greater than 20% of precipitation during large storm  
127 events, reaching 90 to 95% during artificial sprinkling events (Tromp-van Meerveld *et al.*, 2007).

128 Overland flow does not occur on the hillslope, except on the small section of exposed bedrock.

129

### 130 **3. Methods**

#### 131 **3.1 Measurements of saturated hydraulic conductivity of soil and bedrock**

132 We measured vertical soil hydraulic conductivity in two transects of 240 and 285 m length with a  
133 Guelph permeameter at a maximum of four depths (0.19, 0.32, 0.46, 0.75 m). The transects were  
134 located perpendicular to the main stream channel downhill of the study site in a ridge and hollow on the  
135 hillslope. Each transect featured four measurement sites.

136

137 Lateral saturated hydraulic conductivity of the soil immediately above the bedrock was measured  
138 through falling head well tests in 135 wells, forming a very approximate 2x2 m grid (Fig. 1b). The  
139 wells were composed of 1.9 cm PVC pipes, augered to bedrock and screened over the bottom 0.10 m.  
140 A 1L bottle was fixed to the top of the well and the time needed to drain the 1L bottle was recorded.  
141 This experiment was repeated until steady state conditions were reached. Some wells were positioned  
142 in areas with either soil pipes or cracks and water could not be supplied at a rate high enough to  
143 quantify drawdown. No lateral saturated conductivity could be calculated from these wells.

144 The lateral conductivity was calculated by considering the drawdown from the bottles as a slug test:

145 
$$Q = \frac{2\pi L_I K_L}{\ln(R_E/R_W)} \quad (1)$$

146 The rate of water level change is related to the flux as:

147 
$$\frac{dy}{dt} = \frac{-Q}{\pi R_C^2} \quad (2)$$

148 Combining equation 1 and 2 and integrating between the limits  $y_0$  at time=0 and  $y_t$  at time = t, yields:

149 
$$K_L = R_C^2 \ln(y_0/y_t)/Ft \quad (3)$$

150 Where F is a shape factor depending on the well geometry. The calculated  $K_L$  combines both effects of  
151 conductivity and the local bedrock gradient. We analyzed the results to see if the local gradient  
152 systematically affected the measured K value. It was assumed that the soil permeability was greater  
153 than that of the bedrock, and the majority of flow would be lateral rather than vertical, leading to  
154 estimates of lateral rather than vertical hydraulic conductivity.

155

156 The bedrock hydraulic conductivity was measured during three sprinkling experiments. A 2 m wide  
157 line source upslope of the monitoring trench was sprinkled continuously until a steady state flux was  
158 achieved at the trench (3 to 5 days). The flux into the bedrock was determined as the difference  
159 between the steady state sprinkling flux and the flux into the trench at the bottom of the hillslope.

160 Under the assumption of unit head gradient, the saturated hydraulic conductivity of the bedrock was  
161 then calculated through dividing the bedrock flux by the area over which bedrock infiltration occurs  
162 (i.e. the product of the width of the line source and the distance between line source and trench).

163

164 This approach was repeated for three locations at each of 6 m, 9 m, and 14 m upslope of the trench. For  
165 the upslope sections, the loss was determined as the difference between the volume applied, the volume  
166 captured in the trench and the measured loss in the section downslope. Losses and derived bedrock  
167 hydraulic conductivities were determined for nine 16 m<sup>2</sup> sections of the hillslope (see positions shown  
168 in Fig. 1a). Despite high water application rates (0.29 l s<sup>-1</sup> or approximately 44 mm hr<sup>-1</sup>), no overland  
169 flow was observed.

170

171 To analyze the relationship between hydraulic conductivity and the bedrock topography that governs  
172 the direction of lateral subsurface flow, we calculated the flow accumulated area and topographic  
173 wetness index (TWI) of the bedrock topography. The cell size of the bedrock DEM was small  
174 compared to the size of the topographic depressions; hence we used a D8 algorithm to calculate flow  
175 accumulation. The topographic wetness index (TWI) was calculated with the following equation  
176 (Kirkby, 1975):

177

178 
$$TWI = \ln(\alpha/\tan \beta) \quad (4)$$

179 Where  $\alpha$  is the upslope area per unit contour length (m<sup>2</sup> m<sup>-1</sup>) and  $\beta$  is the local slope gradient (°). The  
180 unit contour length was 1 m in this study.

181

### 182 **3.2 Model setup**

183 We developed a distributed hydrological model to simulate the spatial distribution of groundwater  
184 recharge.

185 We assumed that all throughfall (the fraction of precipitation that is not intercepted by vegetation)  
 186 infiltrated into the soil. The throughfall volume was calculated with an empirical formula (eq. 5)  
 187 determined by Tromp-van Meerveld and McDonnell (2006a) from storm events at PMRW (Cappellato  
 188 *et al.*, 1995).

$$190 \quad T = 0.97P - 1.66 \quad (5)$$

191 Where  $T$  is the throughfall depth of a rainstorm (mm) and  $P$  is the depth of the rainstorm (mm). For  
 192 potential transpiration rate of the vegetation we used the average daily rate of  $2.6 \text{ mm d}^{-1}$  measured  
 193 during the 2002 growing season. In the model simulations, the actual transpiration per timestep from  
 194 each soil column was determined as the minimum of two volumes:

$$196 \quad T_{ACT} = \min(T_{POT}, S_{ACT}) \quad (6)$$

197 Where  $T_{ACT}$  is the actual volume of transpiration (m),  $T_{POT}$  is the potential volume of transpiration (m),  
 198 and  $S_{ACT}$  is the actual volume of water stored in the soil column (m). We assumed an immediate and  
 199 uniform distribution of moisture in the soil column. Where there was no soil present, water was  
 200 immediately added to the soil-bedrock interface reservoir.

201 The soil was represented by a single column above each bedrock topography cell. We assumed  
 202 unsaturated flow was a consequence of gravity drainage only (i.e. unit gradient flow) (eq. 7).

$$204 \quad q_V = -K_{eff} \quad (7)$$

205 Where  $q_V$  is the unsaturated flux ( $\text{m d}^{-1}$ ) and  $K_{eff}$  is the effective conductivity ( $\text{m d}^{-1}$ ). The effective  
 206 hydraulic conductivity (eq. 8) is calculated as a function of the saturated hydraulic conductivity and the  
 207 relative conductivity.

$$209 \quad K_{eff} = K_V K_r \quad (8)$$

210 Where  $K_V$  is the saturated hydraulic conductivity of the soil in vertical direction ( $\text{m d}^{-1}$ ) and  $K_r$  is the  
 211 relative conductivity (-), calculated with the van Genuchten-Mualem equation (van Genuchten, 1980):

$$213 \quad K_r = \sqrt{\frac{\theta_a - \theta_r}{\theta_s - \theta_r}} \left( 1 - \left( 1 - \left( \frac{\theta_a - \theta_r}{\theta_s - \theta_r} \right)^{\frac{1}{m}} \right)^m \right)^2 \quad (9)$$

214 Where  $\theta_a$  is the actual soil moisture content,  $\theta_s$  the saturated soil moisture content, and  $\theta_r$  the residual  
 215 soil moisture content. The  $m$  (-) parameter is related to the shape parameter  $n$  (-) from the Van  
 216 Genuchten water retention curve through:

$$218 \quad m = 1 - 1/n \quad (10)$$

220 Groundwater recharge (GWR) was determined as a direct loss from the soil-bedrock interface (SBI)  
 221 reservoir. If there is water present in this reservoir at any point of the hillslope, the recharge rate,  $q_{gwr}$   
 222 ( $\text{m d}^{-1}$ ) was determined as the minimum of two rates:

$$224 \quad q_{gwr} = \min(q_V, K_{BR}) \quad (11)$$

225 Where  $q_V$  is the drainage from the soil ( $\text{m d}^{-1}$ ) and  $K_{BR}$  ( $\text{m d}^{-1}$ ) is the saturated hydraulic conductivity of  
226 the bedrock. The storage capacity of the bedrock was assumed to be infinite.  
227 When the recharge rate into the bedrock was too small to drain the SBI reservoir during the timestep,  
228 water was routed along the SBI topography. The routing algorithm takes into account changes in flow  
229 directions caused by filling and spilling of depressions in the microtopography (Appels *et al.*, 2011).  
230 We replaced the original instantaneous water transfer in the redistribution algorithm with a kinematic  
231 wave approximation of the Boussinesq equation over a sloping boundary (eq. 12, Rupp and Selker  
232 (2006)) to account for the spatial variability of horizontal hydraulic conductivity.  
233

$$234 \quad Q_L = K_L b h \frac{dH}{dx} \quad (12)$$

235 Where  $Q_L$  is the lateral flux of water ( $\text{m}^3 \text{d}^{-1}$ ),  $K_L$  is the saturated hydraulic conductivity of the soil in  
236 lateral direction ( $\text{m d}^{-1}$ ),  $b$  is the width of flow (m),  $h$  is the height of the saturated layer (m), and  $dH/dx$   
237 is the hydraulic head gradient ( $\text{m m}^{-1}$ ), that is assumed to be equal to the gradient of the bedrock surface  
238 in the direction of flow. The flow direction along the SBI was determined for every timestep, based on  
239 the highest local gradient of the hydraulic head. The resulting flow was then calculated in a single  
240 direction (eq. 12).

241 The height of the saturated zone was transient and assumed to be unrelated to the soil column height,  
242 implying the presence of a transient thin soil layer for saturated flow at the locations where the bedrock  
243 was exposed. At the domain boundary, water was allowed to drain freely from the seepage face without  
244 outflow resistance. The conceptualization of soil and saturated zone above the SBI is illustrated in Fig.  
245 2.  
246

### 247 **3.3 Generation of fields of hydraulic conductivity**

248 Our model required three spatial distributions of hydraulic conductivity: vertical and lateral direction in  
249 the soil and vertical in the bedrock. Spatially variable fields of hydraulic conductivity were generated  
250 from the results of a geostatistical analysis of the conductivity measurements. The geostatistical  
251 analysis of the measurements was performed with the nlme and geoR packages of R statistical software  
252 (Pinheiro *et al.*, 2013; Diggle and Ribeiro, 2007) Based on the best-fitting models for the  
253 measurements, as presented in Table 1, random fields were generated with the RandomFields package  
254 (Schlather *et al.*, 2014) of R statistical software (R Core Team, 2014). The random field generation was  
255 performed with the log10 transformed measurement values due to non-normally distributed values (see  
256 results section 4.1).

257 The  $K_L$  dataset was large enough for a reliable estimate of the spatial distribution of the values, the  
258 number of measurements of  $K_V$  and  $K_{BR}$  was smaller and measurements represented a smaller part of  
259 the hillslope. This will likely have had consequences for the estimates of nugget and correlation length  
260 of the covariance model (Table 1). We decided to work with these estimates in the absence of larger  
261 data availability. The choice of covariance model, specifically the ratio between correlation lengths of  
262 the  $K_{BR}$  pattern versus that of the  $K_L$  and/or  $K_V$ , affects the simulations in terms of flow length along the  
263 SBI. We do not claim that the geostatistics we used in this study are the ‘right’ ones and varying  
264 correlation length will surely affect the results. However, performing a full sensitivity analysis with  
265 structures of various length fell outside the scope of this study.



266 Also,  $K_{BR}$  was measured at a larger spatial scale than the cell size of the generated spatial distributions  
267 of  $K_{BR}$ . However, we assumed that the variance of the measurements was equal to the variance of the  
268 smaller spatial scale.

269

### 270 **3.4 Parameterization and simulation scheme**

271 Model simulations were performed with 25 combinations of randomly generated hydraulic conductivity  
272 fields. We established with a jackknife resampling analysis that the standard deviation of the water  
273 balance components did not change when considering 20 simulations or more, suggesting that the  
274 results of our set of 25 simulations are not biased to a specific combination of hydraulic conductivity  
275 patterns.

276

277 The soil hydraulic parameters required for the calculation of the relative conductivity (eq. 9) were  
278 uniformly distributed ( $\theta_s = 0.45$ ,  $\theta_r = 0.30$ ,  $n=1.75$ ). These values were based on previous modeling  
279 studies (Hopp and McDonnell, 2009; James et al., 2010). The grid cell size of the domain was set at  
280 0.25 m, such that the heterogeneity of the bedrock topography could be distinguished.

281

282 We performed three sets of simulations of increasing complexity to address the effects of (1) spatial  
283 variability of hydraulic conductivity, (2) storm duration, and (3) transient precipitation on groundwater  
284 recharge on the hillslope. Table 1 presents the parameterization scheme of the simulation sets.

285 The rainfall event of simulation set 1 has been described and modelled before by Burns *et al.* (2001),  
286 Freer *et al.* (2002), Hopp *et al.* (2009), and James *et al.* (2010). The rainfall volume was corrected for  
287 throughfall (eq. 5), but transpiration was neglected as this event occurred before the growing season.

288 The first combination of conductivity values in this first simulation set (Table 2) was based on the  
289 average of the measured values of soil and bedrock hydraulic conductivity with a relatively small  
290 contrast between vertical hydraulic conductivity of the soil and bedrock (simulations a and d). For the  
291 second and third combination, the contrast between  $K_V$  and  $K_{BR}$  was increased by a factor of 10  
292 (simulations b and e) and a factor of 100 (simulations c and f). Initial conditions and spin up period  
293 were the same as used by James *et al.* (2010).

294 The intensity and lag time used in simulation set 2 were the average storm intensity and the average lag  
295 time between storms at Panola, calculated from the 147 storm record (Tromp-van Meerveld and  
296 McDonnell, 2006a). In these simulations, transpiration was neglected and the rainfall events were  
297 treated as effective throughfall events.

298 The precipitation series of simulation set 3 was corrected for throughfall (eq. 5) and the potential  
299 transpiration rate was set at  $2.6 \text{ mm d}^{-1}$  during the growing season (1 May to 1 October).

300

## 301 **4. Results**

### 302 **4.1 Spatial patterns of soil and bedrock saturated hydraulic conductivity**

303 The measured hydraulic conductivity values of the three zones showed a large variability (Fig. 3 and  
304 Table 3). The  $K_V$  profiles measured with the Guelph permeameter showed a general tendency of  
305 decreasing variability of hydraulic conductivity with depth. However, large values were found at 45  
306 and 72 cm depth (Fig. 3). These may be attributed to the presence of macropores or other vertical  
307 preferential flow paths in the soil as identified as important transport mechanisms by Freer *et al.*

308 (2002). We did not find a statistically significant relation between soil depth and saturated hydraulic  
309 conductivity, neither in the vertical nor in the lateral direction.

310

311 The ranges of the measured values of saturated hydraulic conductivity of the soil and bedrock  
312 overlapped. A Kolmogorov-Smirnov test showed that the lateral saturated hydraulic conductivity ( $K_L$ )  
313 of the soil was significantly larger than the vertical saturated hydraulic conductivity of the soil ( $K_V$ ) and  
314 the bedrock ( $K_{BR}$ ), but there was no significant difference between the datasets of  $K_V$  and  $K_{BR}$  at a  $p$ -  
315 value of 0.10. The size of the  $K_L$  values could also have been affected by the local slope of the SBI,  
316 reflecting differences in hydraulic head instead of variability of  $K_L$ . An analysis of measured  $K_L$  values,  
317 grouped by soil depth, versus slopes determined from the bedrock DEM did not reveal a correlation  
318 between saturated hydraulic conductivity and local slope. In addition, Fig. 4a and 4b show no  
319 meaningful correlations of measured  $K_L$  values and flow accumulation or topographic wetness index  
320 (TWI) based on the bedrock DEM.

321

322 Geostatistical analysis of the data showed that a lognormal distribution fitted the observed spatial  
323 clustering of hydraulic conductivity better than a normal distribution. An exponential covariance model  
324 provided the best fit to all three datasets (Table 3). The coefficient of variation of measured hydraulic  
325 conductivity of both  $K_V$  and  $K_{BR}$  was larger than that of  $K_L$ . The correlation length of the fitted  
326 covariance models was shortest for the soil hydraulic conductivity in the vertical direction.

327

#### 328 **4.2 Effects of uniform and spatially variable hydraulic conductivity**

329 In the simulations with uniform parameters (Figs. 5a, b, c) only soil depth and bedrock topography  
330 control the spatial pattern of GWR that results after a rainstorm. When the contrast between  $K_V$  and  $K_{BR}$   
331 was small (Fig. 5a),  $q_V$  from the soil exceeded  $K_{BR}$  only at locations with soil depths smaller than 0.05  
332 m and lateral flow along the soil-bedrock interface did not extend further than 1 m before reinfiltration.  
333 Shallow soil zones were more saturated than deep soil zones and therefore higher amounts of GWR  
334 occurred in these zones during the course of the storm. In the uniform simulations with a larger contrast  
335 between  $K_V$  and  $K_{BR}$  (Fig. 5 b and c),  $q_V$  from the soil exceeded the  $K_{BR}$  early on in the rainstorm and as  
336 a result zones with shallow soils now generated lateral flow along the SBI. Zones of high flow  
337 accumulation and depression storage in the bedrock topography developed a larger transient saturated  
338 layer that provided high GWR in the drainage phase after the storm. Due to the formulation of the  $q_L$  in  
339 one direction and the lack of detailed topography of the bedrock, the lateral flowpaths along the SBI  
340 appear as ribbons of increased GWR in the final maps.

341

342 Though the cumulative bedrock groundwater recharge did not exceed the event precipitation at the  
343 hillslope scale, local values of groundwater recharge could be much higher as a result of lateral flow  
344 and slow recharge from the stagnating saturated layer after the storm: up to a factor three for the  
345 uniform conductivity fields and a factor five for the spatially variable conductivity fields.

346

347 In the simulations with spatially variable values of  $K_V$ ,  $K_L$ , and  $K_{BR}$ , we found that firstly the rate at  
348 which water was delivered to the SBI was affected: some deeper soil zones now received more GWR  
349 than others in the low-contrast simulation (Fig. 5d). Secondly, the spatial distribution of  $K_L$  created a

350 more varied pattern of lateral flow. So while the GWR ribbons were still visible in Figs. 5e and 5f, the  
351 GWR pattern surrounding these hotspots of GWR was less smooth.

352

353 The low contrast parameter set underestimated subsurface flow at the bottom of the domain most: no  
354 flow in the uniform scenario and only  $0.05 \text{ m}^3$  cumulative in the spatially variable version. The higher  
355 contrast parameter sets all generated significant subsurface flow with a first peak already occurring  
356 during the first rain period of the storm. This was an artefact of the model structure that just considered  
357 one soil layer and therefore simulated a fast movement of the infiltration front. The spatial distribution  
358 of  $K_V$  partly mitigated this artefact, because it caused a slight delay of the first runoff peak and a more  
359 prolonged drainage phase of the hydrographs after the storm (Figs. 5e and 5f). Simulations c and f  
360 resulted in cumulative runoff volumes closest to the observed total runoff of  $13.5 \text{ m}^3$ , suggesting that  
361 this conductivity contrast approaches reality best.

362

### 363 **4.3 Effects of storm duration**

364 Fig. 5 showed a clear negative relationship between soil depth and groundwater recharge when  
365 hydraulic conductivities were uniformly distributed; the pattern became more varied with spatially  
366 variable fields of  $K$ . In Fig. 6, the variation of the GWR pattern is explored as a function of storm  
367 duration. The coefficient of variation (CV) was determined for all cells that fell within the same soil  
368 depth range. The lines in each panel show that though there were considerable differences between the  
369 individual combinations of fields (a result of  $K_V$  variability), they all display a similar increasing  
370 variability as a function of storm duration. In shallower soil classes the range of CV (i.e. the bandwidth  
371 of the lines in Fig. 6) increased due to effects of  $K_{BR}$  variability: the flux from the soil columns was  
372 larger than the flux into the bedrock. In the deeper soil classes the range of CV increased more slowly,  
373 because the soil did not reach similar levels of saturation. Increased CV could be attributed to run-on  
374 from shallower soil zones.

375 In all the scenarios, the total amount of rain applied was the same and so was the total amount of  
376 groundwater recharge. However, the fraction of total recharge occurring during the storms increased  
377 disproportionately with the size of an individual storm event from 7% in the 1-hour storms to 78% in the  
378 20-hour storm. In accordance with this increase, the spatial variability of GWR increased with an  
379 increase of storm duration (moving from top to bottom in Fig. 6). In hillslope areas with a soil depth  
380 shallower than the critical depth that variability was caused by the spatial distribution of  $K_{BR}$ . In  
381 hillslope areas with deeper soil depths that variability increased due to increased differences in wetness  
382 and induced vertical flux during the storms and run-on from shallow soil depth zones.

383

384 The extent of lateral flow can be illustrated by comparing the actual saturated SBI area with the area  
385 where SBI was generated because  $q_V$  was larger than  $K_{BR}$ . Fig. 7 illustrates the increasing extent of run-  
386 on with increasing storm duration. The loops in the panels are hysteretic: the saturated area increases  
387 during the storm and then sustains saturation during the drainage phase both because percolation rates  
388 from wet shallow soil zones are still high and because drainage from the saturated layer continues after  
389 the storm. Longer storms resulted in a larger saturated SBI area and more deviation from the 1:1 line,  
390 indicating a larger travel distance of lateral flow. The differences between the loops of the individual  
391 combinations of  $K$  fields show that the exact size and position of the run-on affected areas depends on  
392 the particular realization of  $K_L$  and  $K_{BR}$  fields.

393

#### 394 **4.4 Analyzing the groundwater recharge pattern – annual precipitation dynamics**

395 The spatial patterns of soil and bedrock conductivity mainly affected yearly cumulatives of subsurface  
396 runoff and storage change in the transient saturated layer at the SBI, as indicated in Table 3 by the high  
397 coefficients of variation for these water balance components. Since throughfall solely depended on  
398 precipitation characteristics, this volume was identical for all simulations.

399

400 Figure 8 shows the empirical cumulative distribution function of groundwater recharge and cumulative  
401 rainfall as a function of event throughfall. Events were defined as the duration of the rainstorm and 24  
402 dry hours after a storm. Our simulations showed that 25% of annual groundwater recharge occurred  
403 during events with 9.7 mm throughfall or less, 50% of annual GWR during events with throughfall of  
404 37 mm or less, and 75% of annual GWR during events with throughfall of 84 mm or less (Fig. 8). A  
405 total of 40% of annual groundwater recharge occurred during events that exceeded the precipitation  
406 threshold for subsurface flow of 52 mm throughfall (Tromp-van Meerveld and McDonnell, 2006a).  
407 Groundwater recharge under saturated areas accounted for 40% of the annual total GWR.

408

409 Maps of cumulative GWR during various periods of the simulation and of different realizations of *K*  
410 fields are shown in Fig. 9. These maps show that GWR hotspots (in red) changed with storm  
411 magnitude. In a lag period (Fig. 9a), the zones with deep soil depth received the largest amounts of  
412 GWR, whereas in an event period with the same average amount of groundwater recharge (Fig. 9b)  
413 more recharge occurred in zones with a shallow soil. Events needed to be of a considerable size to have  
414 increased GWR occur along lines of higher flow accumulation (Fig. 9d). The relative contribution of  
415 GWR hotspots to the total volume varied per event between 12 and 90%, depending on the extent of  
416 lateral flow. On a yearly timescale (Fig. 10), the hotspots received 30% of the bedrock groundwater  
417 recharge.

418

419 When the yearly cumulative groundwater recharge at each point of the hillslope was plotted as a  
420 function of the duration of saturation at the soil-bedrock interface (Fig. 10), three zones could be  
421 distinguished: 1) a zone without a strong correlation between duration of saturation and amount of  
422 GWR, 2) a zone where long durations of saturation corresponded to high yearly GWR, 3) a zone  
423 displaying the same correlation, but at a steeper slope.

424

## 425 **5 Discussion**

### 426 **5.1 A perceptual model of the spatial hierarchy of groundwater recharge at the** 427 **hillslope scale**

428

429 Our simulations suggest that the relative importance of each of the structural and dynamic controls on  
430 groundwater recharge into bedrock at the hillslope scale varies with rainstorm size and the duration of  
431 dry periods between events. The structural aspects of the hillslope include its bedrock topography, soil  
432 depth, soil hydraulic properties - characteristics that are assumed to be constant on the recharge  
433 timescale. The dynamic aspects include the rate at which water is delivered to, and the extent to which  
434 lateral flow is present at, the soil-bedrock interface – characteristics that are transient on the recharge  
435 timescale.

436 Dynamic aspects drive the hierarchy of controls, expressed as a flow chart in Fig. 11. Firstly, the ratio  
437 between rain depth ( $\Sigma P$ ) and soil water storage capacity ( $V_{soil}$ ) determines the size of the vertical flux of  
438 water through the soil. Secondly, the ratio between this vertical flux ( $q_V$ ) and the flux into the bedrock  
439 ( $q_{gwr}$ ) determines the level of saturation at the soil-bedrock interface (SBI). Thirdly, the ratio between  
440 the lateral flux ( $q_L$ ) from saturated areas at the soil-bedrock interface and the flux into the bedrock  
441 ( $q_{gwr}$ ) determines the run-on distances along the SBI. When the first and second ratio are small, the  
442 spatial pattern will reflect the spatial distribution of soil depth. Conversely, when widespread SBI  
443 saturation occurs, run-on distances are large and increased GWR will occur within zones of high flow  
444 accumulation and depression storage in the bedrock topography (SBI<sub>topo</sub>). The transition phase between  
445 soil depth and topography controlled recharge occur under lower soil-bedrock interface saturation,  
446 when the  $K_L$  patterns on the hillslope control run-on distances and resulting increased bedrock  
447 groundwater recharge. This is an example of structural hillslope characteristics influencing a dynamic  
448 control.

449 We found that the spatial variability of soil depth trumped the spatial variability of  $K_V$  as an influential  
450 factor, because the spatial variability of the delivery rate was mainly determined by the soil moisture  
451 content. Shallow soil zones not only delivered more water to the soil-bedrock interface, but also at a  
452 higher rate, because they reach a state of higher saturation than their deeper soil counterparts during  
453 average rainstorms. The spatial variability of  $K_V$  played a smaller role, but affects the variation around  
454 the groundwater recharge-soil depth relationship

455 The presence of fractures or another type of variety of bedrock permeability is a structural aspect for  
456 increased bedrock groundwater recharge potential (as opposed to an average value of bedrock  
457 permeability as estimated by Tromp-van Meerveld *et al.*, 2007). Fractures will act as hot spots for  
458 groundwater recharge, due to their large potential loss rate. Though our model does not explicitly  
459 account for fracture flow, the randomly generated fields of  $K_{BR}$  contained points with values large  
460 enough to be considered as fractures. Our results show that the combined vertical and lateral flux is not  
461 always large enough for the actual loss rate to equal the potential loss rate. Instead, increased bedrock  
462 groundwater recharge will also occur at locations with smaller  $K_{BR}$ , but with accompanying prolonged  
463 saturation at the soil-bedrock interface. In general, lateral flow ceases within 24 hours after rainfall  
464 events and the saturated layer is drained by vertical recharge into the bedrock. Recharge from this  
465 saturated layer occurs faster than drainage from the soil and is the main reason why the fraction of  
466 recharge occurring during rain storms increases non-linearly with storm size.

467 The storm throughfall amount determined the extent over which saturation at and lateral flow along the  
468 SBI occurred. Lateral flow occurred during virtually all rainfall events in this conceptual model, but it  
469 did not always reach further than cells directly neighboring locations where it was generated.  
470 Therefore, the timescale over which we made the groundwater recharge and the selection of an event or  
471 lag period determined the spatial pattern of the GWR maps.

472  
473 In our simulations, high flow accumulation zones were the main control on GWR patterns during  
474 rainstorms larger than 50 mm throughfall or smaller storms on a very wet (>60% saturation) soil. This  
475 50 mm is fairly consistent with the 52 mm throughfall threshold for subsurface flow at Panola as found  
476 by Tromp-van Meerveld and McDonnell (2006b).

477 In the hydrological year we investigated 10% of the annual throughfall occurred in events larger than  
478 that threshold. These events provided 40% of the simulated annual groundwater recharge. On an annual  
479 basis, 23% of simulated GWR occurred in the lags between storms, during which soil depth is the main  
480 control on the GWR pattern. The remaining 33% of GWR occurred in ‘transition phase’ rainstorms,  
481 with relatively short run-on distances. In this transition phase, sections of the hillslope are in different  
482 stages of the hierarchy in Fig. 11 during the same event.

483  
484 Consistent with Hopp and McDonnell (2009) and Harman and Sivapalan (2009) the average soil depth,  
485 bedrock permeability, soil hydraulic conductivity and lower boundary conditions determine the  
486 hillslope integrated water balance. However, individual spatial distributions of these hillslope  
487 characteristics strongly determine the spatial pattern of bedrock groundwater recharge hotspots. When  
488 defined as locations with groundwater recharge greater than the 90-percentile value, 30% of annual  
489 GWR occurs in hotspots (i.e. 10% of the hillslope area receives 30% of the hillslope recharge).  
490 However, the contribution and the position of hotspots depends on the timescale that is chosen to  
491 analyze GWR and also between events, depending on the presence and extent of lateral flow at the soil-  
492 bedrock interface.

493 Our perceptual model of bedrock groundwater recharge illustrates that the dynamic aspects driving the  
494 spatial pattern of bedrock groundwater recharge, i.e. rainstorm size in proportion to soil water storage  
495 capacity, are key factors in the occurrence and positioning of recharge hotspots. Our perceptual model  
496 of groundwater recharge occurring at short distances downslope of the original point of infiltration of  
497 throughfall fits well into the interflow framework proposed by Jackson *et al.* (2014). It accounts for  
498 saturated zones developing in a fragmented fashion along the hillslope, converging along lines of flow  
499 accumulation when storms are large. This model is consistent with the fill-and-spill of bedrock  
500 topography in the sense that in order to generate subsurface stormflow at the lower boundary of the  
501 hillslope, the fill zones need to be fully saturated and connected. However, these zones do not map one  
502 to one to hotspots of groundwater recharge, due to the heterogeneity that is created by short distance  
503 run-on during events below the threshold.

## 504 505 **5.2 On groundwater recharge and measurement scale**

506 We caution that the results presented in this paper are simulation results. The overlap of simulated  
507 patches of transient saturation at the soil-bedrock interface with increased groundwater recharge was  
508 promising, but we cannot evaluate our model with measured values of bedrock groundwater recharge at  
509 the site—a notoriously difficult measurement to make (Shand *et al.*, 2005; Heppner *et al.*, 2007;

510 Gleeson *et al.*, 2009; Salve *et al.*, 2012). That said, experimental studies at other hillslope sites have  
511 reported both the distinctive slow, widespread recharge during dry periods versus fast, localized  
512 recharge in wet periods (Anderson *et al.*, 1997; Gleeson *et al.*, 2009) and large differences in magnitude  
513 of response in individual wells to events (Salve *et al.*, 2012).

514 In this study, we have shown how spatially variable distributions of conductivity play a role in creating  
515 a recharge flux that is highly variable in space and time. We combined two sets of point-scale  
516 measurements (Guelph permeameter and well-based falling head measurements) with more integrated  
517 measurements (sprinkling experiment) to generate spatial distributions of conductivity on our hillslope.  
518 We worked from the premise that these experiments provided a range of values of soil and bedrock  
519 conductivity and a first quantitative measure of their spatial correlation; but not a set of exact values at  
520 each point of the hillslope.

521  
522 The sprinkling experiments at various sections of the hillslope above the trench showed a large range of  
523  $K_{BR}$  variability (consistent with the sprinkling experiment performed by Tromp-van Meerveld *et al.*  
524 (2007)), even though the section areas were still rather large and individual fractures were not mapped  
525 or instrumented. In order to estimate the actual locations of increased bedrock recharge (e.g. everything  
526 higher than the 90-percentile value as per Fig. 10), quantifying the local extent of lateral flow along the  
527 soil-bedrock interface is an important step. Our work suggests that due to the higher frequency of small  
528 rainstorms and the resulting occurrence of lateral flow over short distances at the site, the spatial  
529 distribution of  $K_L$  was as important as that of  $K_{BR}$ . The well-based falling head experiment, as simplistic  
530 as it was, provided some insights into that distribution. The experimental method had some drawbacks:  
531 (1) the direction of flow was not well defined (saturation around the wells most likely occurred as a  
532 “bulb” of wetting) and (2) it was a combined measurement of soil and bedrock permeability so that  
533 neither could be individually resolved. The latter is not an issue if the contrast between soil and bedrock  
534 permeability is high. Notwithstanding these issues, one of the interesting measurement results was that  
535 these ranges of conductivity overlap. This may imply that local conductivity contrasts are smaller than  
536 generally acknowledged at the site until now (compare the high average contrast calculated by Tromp-  
537 van Meerveld *et al.*, 2007). It may further imply that some of the well-based falling head measurements  
538 were measuring the conductivity of the bedrock and not that of the soil. Since the soil consists of  
539 colluvium originating from upslope parent material, it is perhaps not surprising that the saturated  
540 hydraulic conductivity of soil and bedrock were not spatially correlated. However, given the occurrence  
541 of subsurface flow on the site, we expected that  $K_L$  above the SBI would be related to topographic  
542 characteristics of the bedrock that govern lateral flow. Where lateral flow accumulates, more  
543 weathering could result in eroded soil pipes or, conversely, clogging due to flushing and accumulation  
544 of fine materials. Hence, we expected a correlation of  $K_L$  with flow accumulation or topographic  
545 wetness index (TWI). The lack of such a correlation (Fig. 4) illustrates the need of separate spatial  
546 surveys of conductivity at other sites instead of using bedrock topography or soil depth as a proxy for  
547 the distribution of  $K_L$ .

548  
549 A logical follow up would be a detailed survey of distributions of hydraulic conductivity at a site such  
550 as Rivendell (Salve *et al.*, 2012; Kim *et al.*, 2014) to see if these can be used to explain the lack of  
551 uniformly rising and falling perched groundwater table at the site. It is intuitive to focus measurement  
552 campaigns on large events that feature subsurface runoff at the toe of a hillslope, but for improving our

553 understanding of spatial variability of groundwater recharge more emphasis should be put on  
554 measuring flow distances during smaller events.

555

### 556 **5.3 On the value of a simple modeling approach**

557 The results of this study show that the location of hotspots of bedrock groundwater recharge is  
558 determined largely by the spatial distribution of lateral soil hydraulic conductivity, bedrock hydraulic  
559 conductivity and the extent of lateral flow that is generated on the hillslope during a multi-storm  
560 timeseries.

561

562 The first weakness of our modeling approach is that we do not simulate flow through the bedrock  
563 matrix and fractures. The unlimited unit gradient flux into the bedrock likely overestimates recharge  
564 under unsaturated drainage conditions and underestimates such fluxes during periods of transient  
565 saturation at the soil-bedrock interface. Also, we did not simulate return flow from upslope fractures  
566 into the soil further downslope and thus ignore feedbacks between bedrock and soil as for instance  
567 observed by Montgomery *et al.* (1997) and Shand *et al.* (2007). Secondly, we restricted lateral flow to  
568 the soil-bedrock interface, where a more sophisticated physical model could simulate perched  
569 groundwater flow. The rationale for the assumption of restricted lateral flow is found in previous field  
570 and modeling studies at the site that have shown that saturated flow mainly occurs at this interface.

571

572 The lack of bedrock flow simulation is more difficult to defend as we do not have data to support our  
573 modeling choices. The shallow bedrock geology of the hillslope likely contains connected fractures  
574 parallel to the land surface since it is constructed from granite blocks (Tromp-van Meerveld *et al.*,  
575 2007). Connected fractures in the bedrock may produce return flow from the bedrock into the hillslope,  
576 but there is no experimental evidence confirming or negating this. Previous modeling studies of the  
577 Panola hillslope by Hopp and McDonnell (2009) and James *et al.* (2010) contained hydrologically  
578 active bedrock, but did not consider fracture flow either.

579

580 Incorporating both the spatial variability of saturated hydraulic conductivity of soil and bedrock, and  
581 bedrock topography on a hillslope while running a model that deals with matrix and fracture flow  
582 remains a computational challenge. Modeling studies of similar hydrogeological systems with more  
583 sophisticated numerical tools (e.g. HydroGeoSphere by Gleeson *et al.*, 2009) are therefore necessarily  
584 restricted to a simpler description of their modeling domain. In a recent study with a 3D Richards'  
585 solver by Liang and Uchida (2014), soil depth and TWI were found to be first-order controls on  
586 transient saturation at the SBI in a steep catchment with a high intensity rainstorm. As shown in this  
587 study, this is an extreme scenario; on gentle hillslopes and during shorter rain events local flow  
588 heterogeneities are likely more important controls. Alternatively, instead of using more powerful  
589 Darcy-Richards solvers for this type of problem that feature non-Darcian flow in both soil and bedrock,  
590 different conceptual approaches to fast recharge such as the one proposed by Mirus and Nimmo (2013)  
591 may be a successful way forward.

592

## 593 **6. Conclusions**

594 We examined the spatiotemporal distribution of bedrock groundwater recharge at the hillslope scale at  
595 the well-studied Panola experimental hillslope. We used new measurements of spatially variable soil



596 and bedrock hydraulic conductivity and a multi-event precipitation series to perform simulations of  
597 groundwater recharge with a new, simple, spatially distributed model.

598

599 We found that the major part of simulated groundwater recharge during a hydrological year occurred  
600 under unsaturated drainage. Soil depth was a main control on amounts and rates through available  
601 storage capacity and controlling the size of vertical flux. During rain storms transient saturation  
602 occurred at the soil-bedrock interface and lateral flow started to affect groundwater recharge patterns.  
603 There were two aspects to that: firstly, hillslope SBI locations that received more lateral flow and had  
604 increased saturation at the end of a storm received more groundwater recharge. Secondly, increased  
605 lateral flow transported water to locations where the bedrock permeability was higher.

606 We have shown that under the rainfall regime found at Panola and the specific distribution of soil and  
607 bedrock hydraulic properties, hillslope-wide SBI saturation only occurred during extreme rainfall  
608 events. While these contributed a large amount of water, the main controls on an annual scale were  
609 therefore not just soil depth and bedrock topography, i.e. the factors that control fill and spill areas in  
610 the subsurface. Instead, hydraulic conductivity, both that of bedrock and the ‘lateral’ soil, determined  
611 the activation and extent of lateral flow along the SBI.

612

613 The results of this study highlight the importance of 3D modeling and simulation of multi-storm time  
614 series when investigating groundwater recharge distributions. Point-scale modeling by definition  
615 underestimates the variability of the process and cannot account for variation in location and timing of  
616 increased bedrock groundwater recharge as does modeling at the watershed scale. This is in accordance  
617 with results of subsurface stormflow studies. We propose that in order to improve our understanding of  
618 the spatiotemporal dynamics of groundwater recharge at the hillslope scale, we go back to subsurface  
619 runoff hillslopes and try to quantify the characterizing ratios between delivery and loss rate and rain  
620 storm size and extent of lateral flow.

621

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Simulation scheme – Effect of:			
	1. Uniform and spatial variability of hydraulic conductivity	2. Storm duration	3. Transient precipitation
$K_V, K_L, K_{BR}$	3 realizations of spatially variable K and 3 realizations of spatially uniform K. Values presented in Table 2.	25 realizations of spatially variable K generated with geostatistics presented in Table 3.	25 realizations of spatially variable K generated with geostatistics presented in Table 3.
Forcing	A single long rainfall event that occurred on 6 and 7 March 1996, during which 87 mm of rain precipitated following a dry period of seven days.	100 mm rain precipitated at a rate of 5 mm hr <sup>-1</sup> in 1, 2, 5, 10, or 20 rainfall events. Each event is followed by a 4.5 day dry spell.	A full year of precipitation, measured in 1997.
Initial condition	$\theta_i = 0.375$	$\theta_i = 0.38$ and $\theta_i = 0.32$	$\theta_i = 0.38$

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748 Table 2. Saturated hydraulic conductivity values used in the simulations presented in Fig. 5. Simulations a-c were  
749 parameterized with the mean values of the spatially variable fields of simulations d-f.

	Spatially uniform	Spatially variable	Soil vertical ( $K_V$ ) (cm hr <sup>-1</sup> )	Soil lateral ( $K_L$ ) (cm hr <sup>-1</sup> )	Bedrock ( $K_{BR}$ ) (cm hr <sup>-1</sup> )
Simulation a	a	d	2.5	67	0.83
b	b	e	2.5	67	0.083
c	c	f	25	67	0.083

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752 Table 3. Statistics of saturated hydraulic conductivity of the soil and bedrock.

	Measured (log10 transformed values of cm hr <sup>-1</sup> )			Fitted exponential covariance model (log10 transformed values of cm hr <sup>-1</sup> )			
	Mean	Variance	Min-Max range	Mean	Variance	Nugget	Correlation length (m)
Soil vertical ( $K_V$ )	-0.17	0.34	-1.2 – 1.3	-0.05	0.59	0.0	15.6
Soil lateral ( $K_L$ )	1.5	0.36	-1.1 – 2.3	1.5	0.38	0.26	20.6
Bedrock ( $K_{BR}$ )	-0.11	0.078	-0.64 – 0.21	-0.11	0.078	0.0	30.5

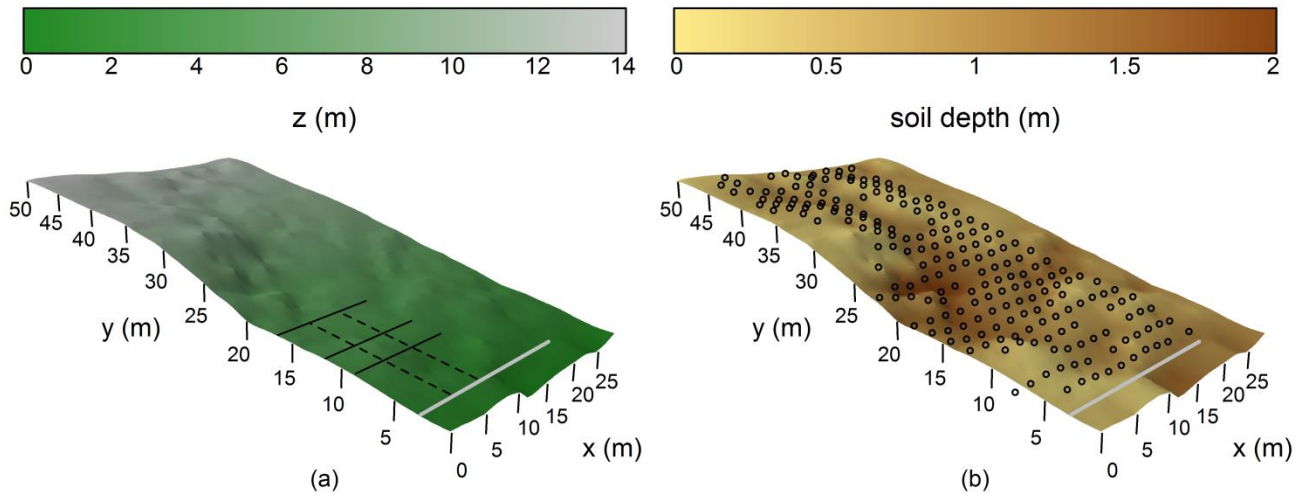
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754 Table 4. Water balance components of full year simulation mean (standard deviation) of the 25 random realization  
755 combinations.

	Throughfall	Transpiration	Groundwater recharge	Runoff	Storage change unsaturated soil	Storage change saturated layer
Yearly mean and standard deviation (m <sup>3</sup> )	1800 (0)	419 (0.7)	1337 (7)	47 (7)	-7.2 (1)	4.2 (3)
Percentage of yearly throughfall (%)	100	23	74	2.6	-0.4	0.2

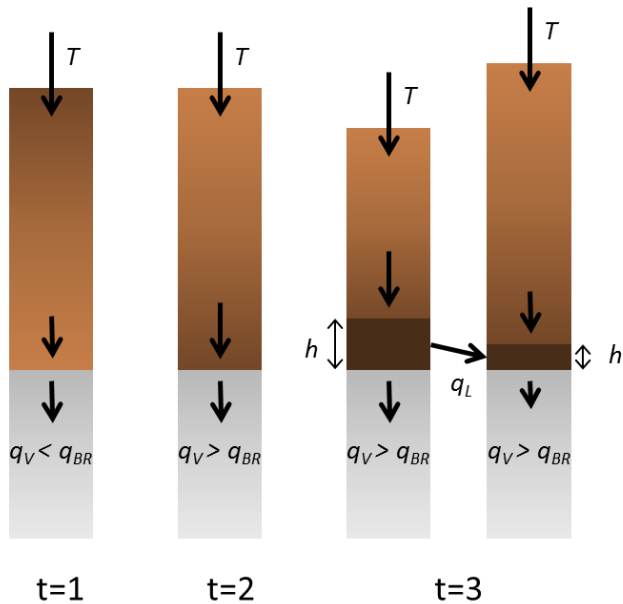
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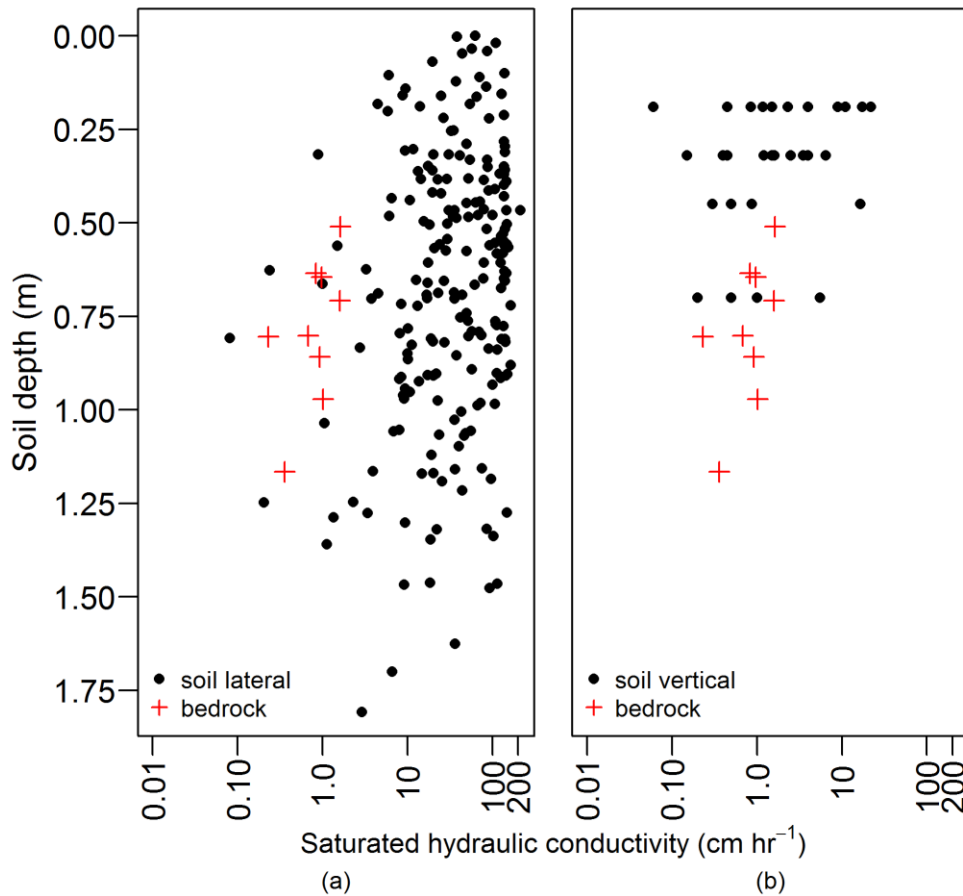
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Fig. 1. (a) Bedrock topography of the Panola hillslope, interpolated to a 0.25x0.25 m grid. The grey line indicates the position of the trench. The black solid lines indicate the position of the sprinkling lines, the dashed lines indicate the projected trench sections for which bedrock losses could be determined (b) Soil depth distribution of the Panola hillslope, interpolated to a 0.25x0.25 m grid. The circles indicate the location of the wells (piezometers). The grey line indicates the position of the trench. The actual values of hydraulic conductivity are shown in Fig. 2 and Table 1.

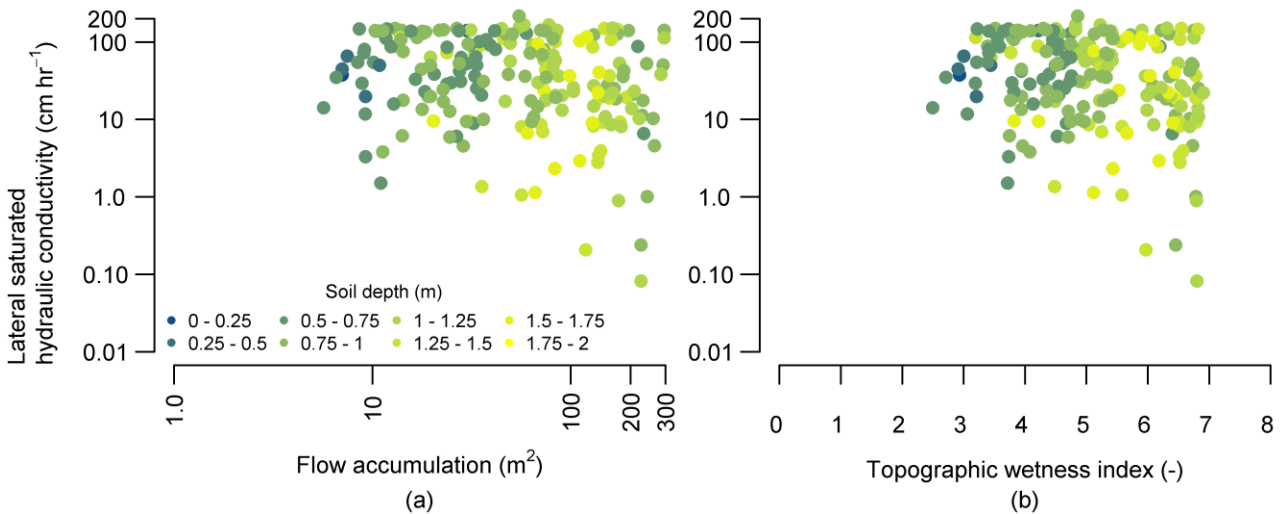


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Fig. 2. Illustration of the subsurface conceptualization at three subsequent timesteps during a rainstorm. At  $t=1$ , the soil is still unsaturated and the vertical flux from the soil is smaller than the maximum  $K_{BR}$ . Due to the wetting of the soil column at  $t=2$ , the vertical flux from the soil is now larger than the flux into the bedrock and a saturated layer starts to form at the soil-bedrock interface. At  $t=3$ , water in the saturated layer moves laterally from one column to its neighboring soil column.

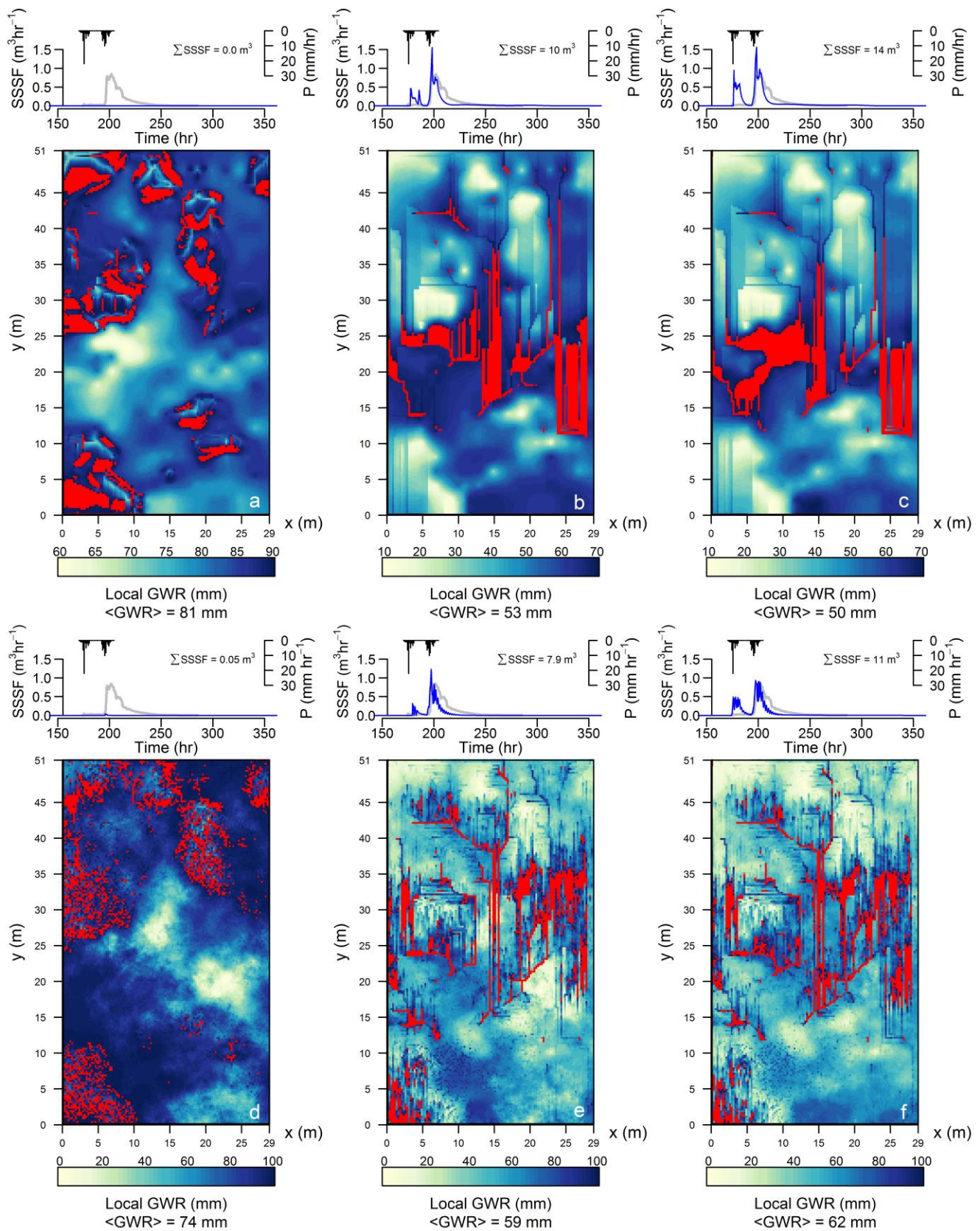


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 771 Fig. 3. Measured values of saturated hydraulic conductivity plotted against soil depth: a) conductivity of the soil in lateral  
 772 direction and bedrock conductivity, b) conductivity of the soil in vertical direction and bedrock conductivity. Note the  
 773 logarithmic *x*-axis.



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 775 Fig. 4. Lateral soil saturated hydraulic conductivity plotted versus (a) the flow accumulation area of the bedrock topography  
 776 and (b) topographic wetness index (TWI) of the bedrock topography. For both flow accumulation area and TWI, the 80-  
 777 percentile value of all points within 1 m radius of each well was used. The color coding indicates average soil depths around  
 778 the wells.  
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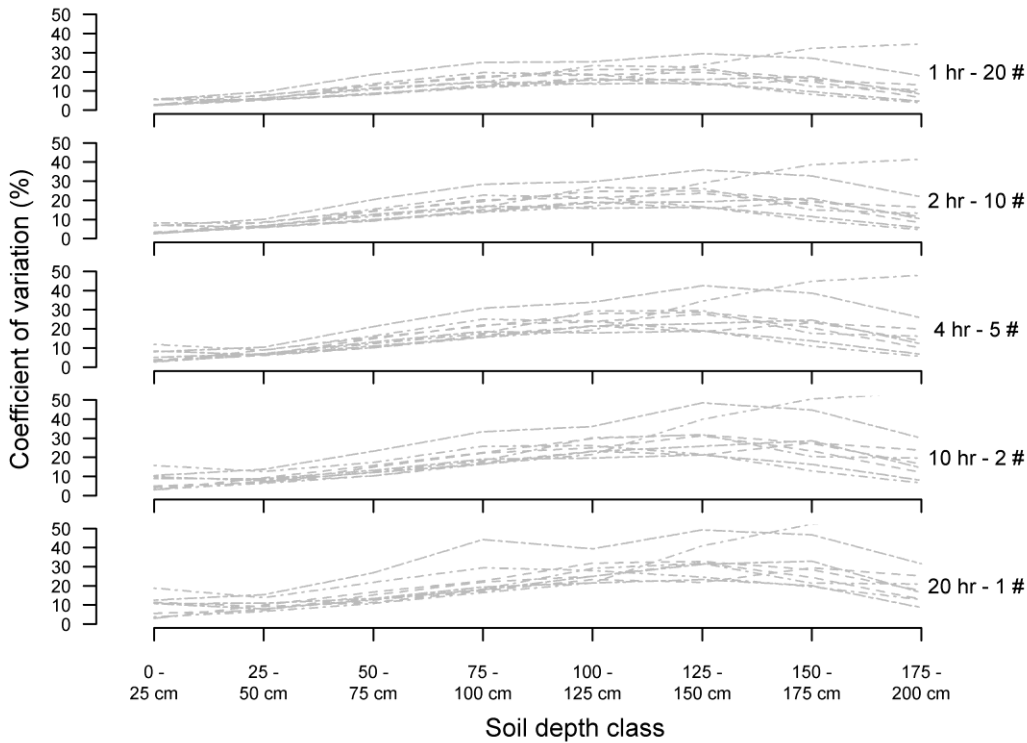


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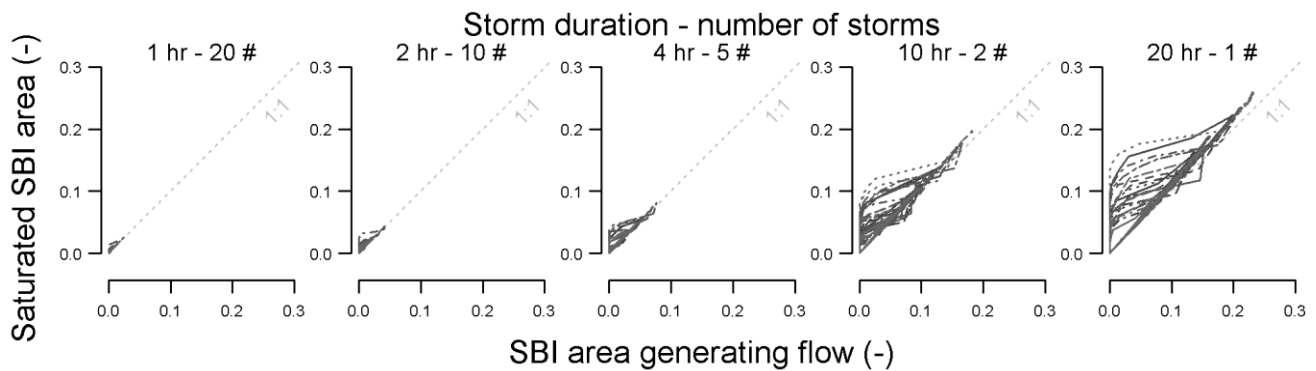
Fig. 5. Hydrographs and maps of bedrock groundwater recharge after the 6-7 March 1996 rain storm. The grey line is the observed hydrograph in the trench, the black line the input precipitation and the blue line the hydrograph of subsurface flow at the bottom of the model domain. The maps show cumulative bedrock groundwater recharge from the start of the rain storm until the end of the simulation (7 days) in every grid cell. The color scales vary between the simulations. The red dots



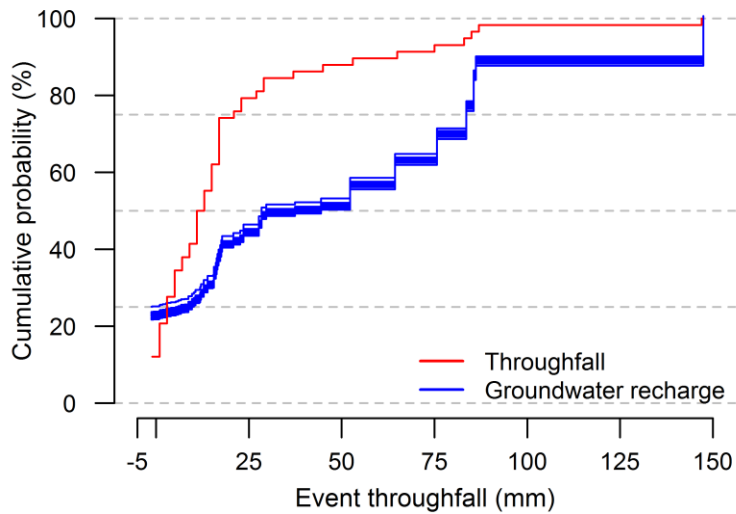
785 indicate locations with bedrock groundwater recharge higher than the 90-percentile value. The simulations of panels a-c  
 786 were performed with spatially uniform  $K_V$ ,  $K_L$ , and  $K_{BR}$  (values presented in Table 2), those of panels d-f with spatially  
 787 variable fields of  $K_V$ ,  $K_L$ , and  $K_{BR}$  (values presented in Table 2).  
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 791 Fig. 6. Coefficient of variation of groundwater recharge (%) determined in 8 classes of soil depth. Each panel contains the  
 792 results of a precipitation scenario presented in Table 1 (forcing of simulation set 2). A precipitation scenario consists of 100  
 793 mm rain applied at a rate of 5 mm hr<sup>-1</sup>, but in a varying number of storms within the simulation (with storm duration  
 794 increasing while the number of storms in the simulation decreases). Each grey line represents one of 25 simulations with a  
 795 random combination of  $K_V$ ,  $K_L$ , and  $K_{BR}$ . For clarity only twelve out of 25 simulations have been plotted.  
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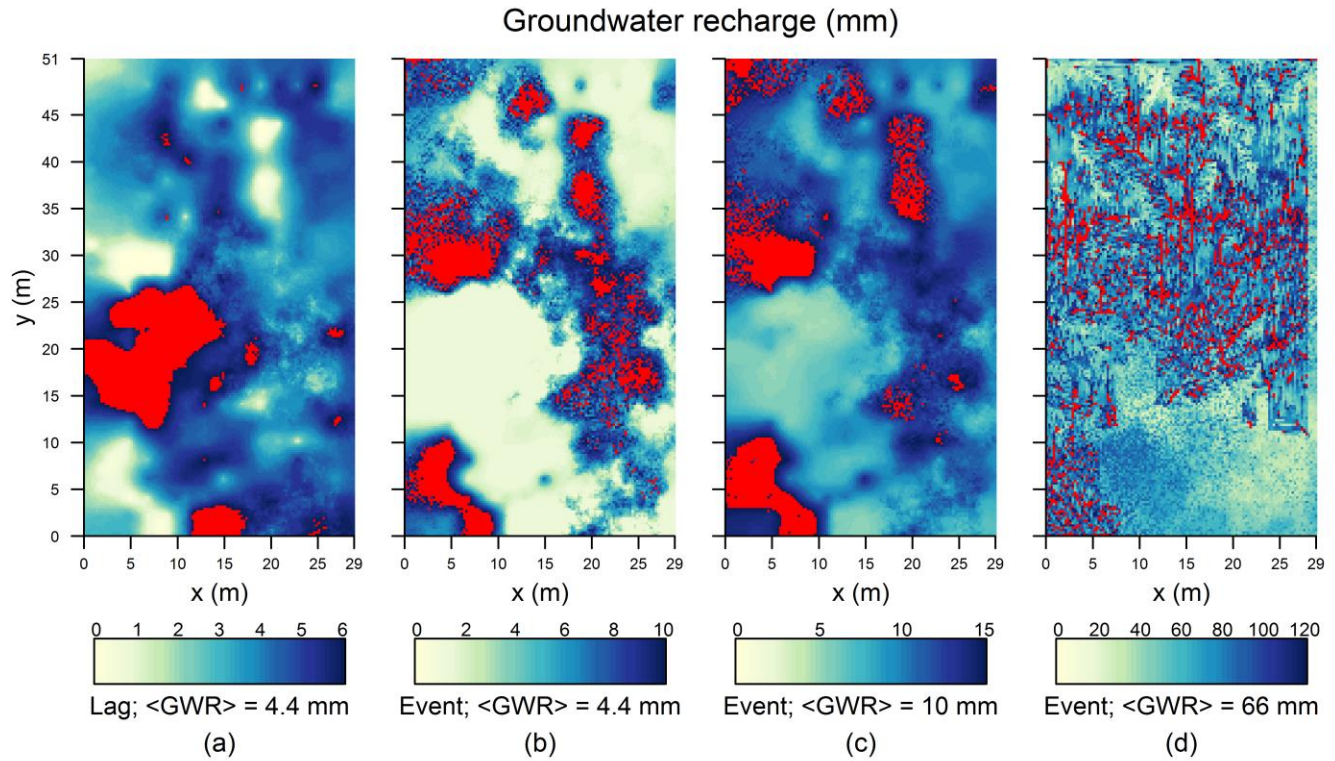


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 798 Fig. 7. Saturated areal fraction of SBI plotted against the areal fraction of SBI where the percolation rate is larger than  $K_{BR}$   
 799 and subsurface lateral flow is generated. Each line represents one of 25 simulations with a random combination of  $K_V$ ,  $K_L$ ,  
 800 and  $K_{BR}$ .  
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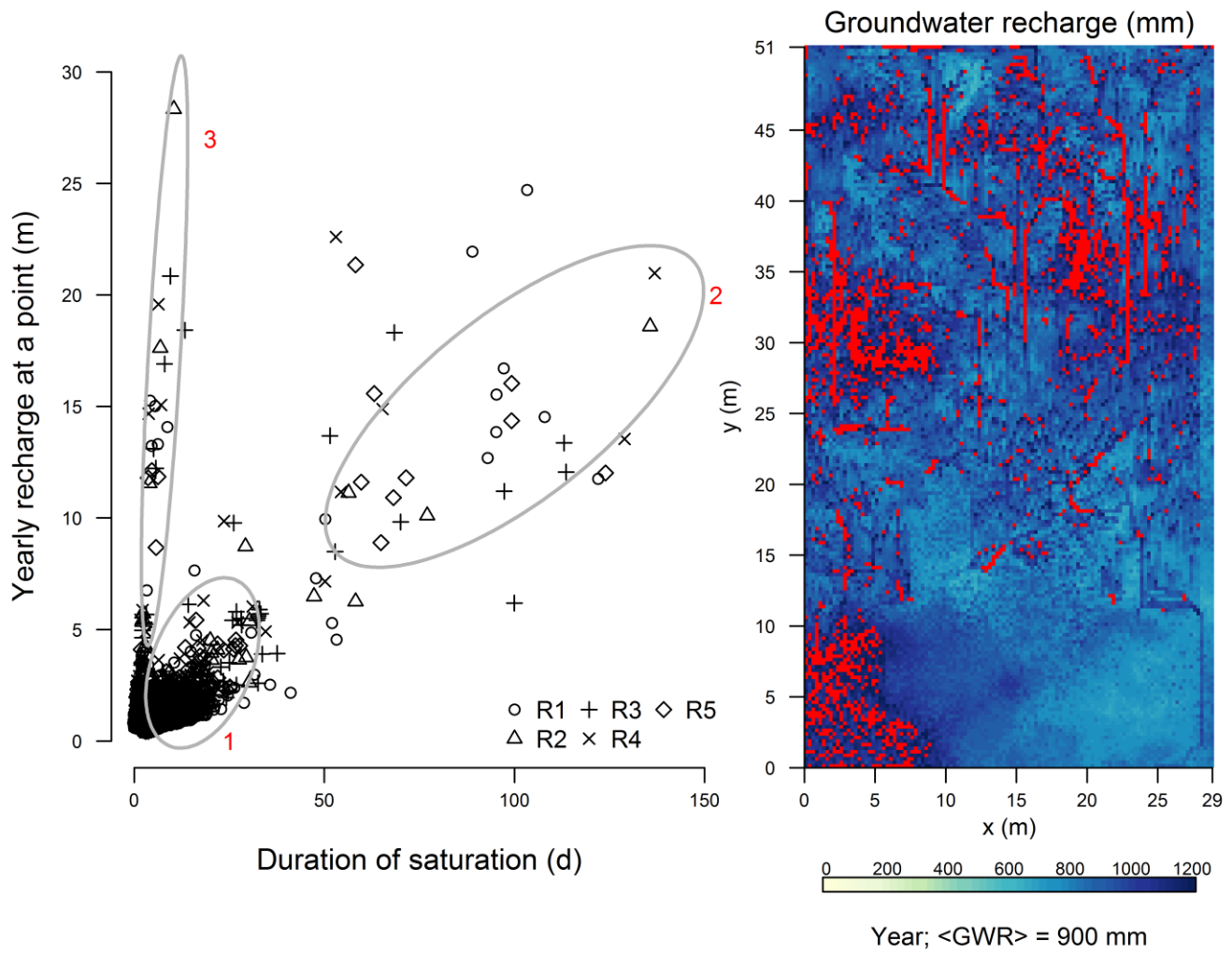
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Fig. 8. Cumulative distribution of annual bedrock groundwater recharge and throughfall as a function of event throughfall amount for all 25 simulations. A negative event throughfall indicates net transpiration in the current event definition.



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Fig. 9. Maps of cumulative groundwater recharge of one lag between rain events and three events of increasing size (a-d). Every color scale is cut off at the 90-percentile value of groundwater recharge during the specific period. The locations in red are the locations where GWR is larger than the 90-percentile value. An event was defined as rainstorm duration plus the following 24 dry hours. A lag was defined as a dry period beyond those 24 hours until the start of the subsequent rainstorm.

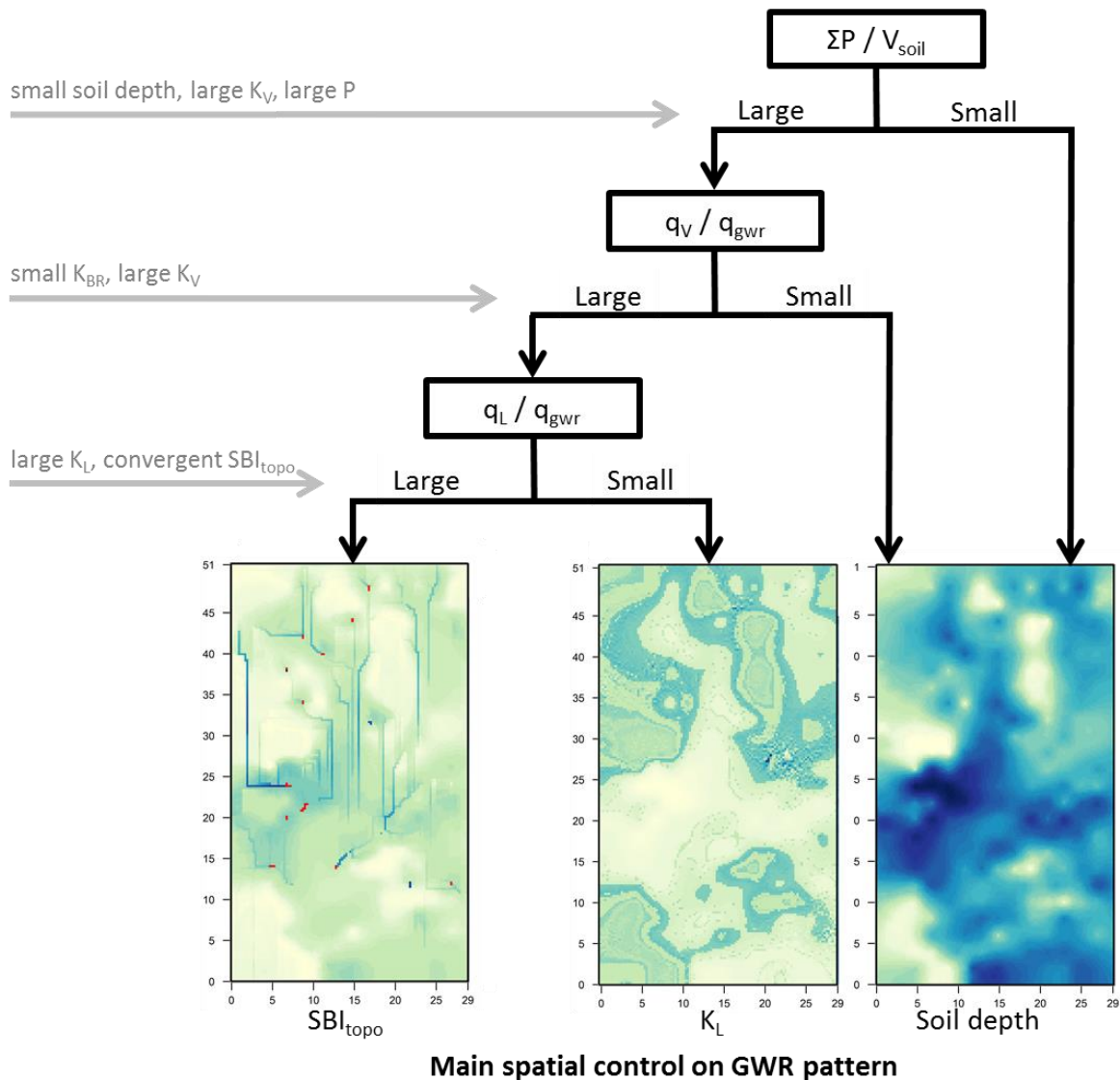


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Fig. 10. Cumulative groundwater recharge at a point as a function of the duration of saturation for five random realizations (left, realizations indicated with different symbols. Map of yearly cumulative groundwater recharge (right). The color scale was cut off at the 90-percentile value of groundwater recharge and the locations with higher GWR colored red.

Structural characteristics enhance  
dynamic controls locally

Dynamic characteristics drive  
hierarchy of controls



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Fig. 11. Conceptual model of generation of a spatial pattern of groundwater recharge at the Panola hillslope. The structural characteristics that reinforce the effect of a dynamic control are indicated in grey on the left side of the figure.