## §15. EUV Wavelength Calibration for SOXMOS Spectrometer

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Recently Xe spectrum from LHD were measured by Soft X-ray spectrometer(SOXMOS) ${ }^{1)}$. Coverage of wavelength is from $116(\AA)$ to $164(\AA)$, and central wavelength is $141.2(\AA)$ in our measurement. In order to identify the measured wavelength of Xe ions, the wavelength calibration was performed.

Firstly, we derived coefficients $b$ and $a$ assuming $\lambda=b+a \times p$ by the least squares method where $\lambda$ is wavelength and $p$ is pixel number. We used six observed values for wavelengths of FeXXI(128.73 $\AA$ ), FeXXII(135.774 $\AA), \quad \operatorname{FeXXII}(155.92 \AA)$, FeXXIII(132.8 $\AA), \operatorname{CVI}(134.9 \AA), \operatorname{CrXXI}(149.87 \AA)$ ions as references. We obtained

$$
\begin{equation*}
\lambda(\AA)=0.0481458 p+118.259 \tag{1}
\end{equation*}
$$

which is shown in Fig. 2 as a solid line. The range of wavelength is from 118.308 to 167.682 and the central wavelength is $142.9(\AA)$. This value is different from given the central wavelength(141.2( $\AA$ )).

To calibrate wavelength as a function of pixel theoretically, we calculated wavelength by using following two equations.

$$
\begin{equation*}
\pm m \lambda=d(\sin \alpha-\sin \beta) \tag{2}
\end{equation*}
$$

where $m$ is the diffraction order, $1,2,3, \cdots$ and $\lambda$ is wavelength $(\AA), d$ is the distance of the grating and is $10^{7} / N$ where N is the grating groove density per $\mathrm{mm}(600 \mathrm{~g} / \mathrm{mm}), \alpha$ is the incidence angle, $\beta$ is the diffraction angle ${ }^{2)}$ as shown in Fig.l.


Fig. 1 The incidence angle and the diffraction angle
$k \lambda[\AA]=\frac{10^{\prime}}{N}\left\{\cos \alpha^{\prime}-\cos \left[\beta_{0}^{\prime}+\cot ^{-1} \times\left(\cot \beta_{0}^{\prime}+\frac{R n}{\left(p-p_{0}\right) M}\right)\right]\right\}$
where $k=1,2,3, \cdots \cdots . \mathrm{R}$ is the Rowland circle diameter $(2 \mathrm{~m}), \mathrm{n}$ is the number of pixel per unit length
$(40 / \mathrm{mm}), \mathrm{p}$ is the pixel number(from 1 to 1024$), p_{0}$ is the central pixel(512), M is the fiber-optic taper magnification. We used the value $\mathrm{M}=2$. In eq(2), the angle $\alpha^{\prime}=\pi / 2-\alpha$ and $\beta^{\prime}=\pi / 2-\beta . \beta_{0}^{\prime}$ is the diffraction angle for the central pixel $p_{0}$,

We have calculated the diffraction angle $\beta$ in the case of both $141.2(\AA)$ and $142.9(\AA)$ by using eq.(2). For the central wavelength $\lambda=141.2 \AA, \beta$ is derived as $82.386^{\circ}$ for $\alpha=88.5^{\circ}$, and for $\lambda=142.9$ $\AA, \beta$ is $82.34^{\circ}$. Then $\beta_{0}^{\prime}=7.164^{\circ}$ for $\beta=82.386^{\circ}$ and $\beta_{0}^{\prime}=7.657^{\circ}$ for $\beta$ is $82.34^{\circ}$.

From eq.(3), for the central wavelength $\lambda$ $=141.2(\AA)$, range of wavelength is from $114.456(\AA)$ to $165.788(\AA)$ when $M=2$ and $R=2.2(m)$. For the central wavelength $\lambda=142.9(\AA)$, range of wavelength is from $116.007(\AA)$ to $167.629 \AA$ when $M=2$ and $\mathrm{R}=2.2(\mathrm{~m})$.

We show in Fig. 2 the relation between wavelength and pixel calculated by eq.(3). We also plotted the measured wavelengths of six obserbed spectral lines in Fig.2. Comparing calculations by eq.(3) with experimental values, we find that the difference from the observed points becomes smaller towards long wavelength range. Finally we will use the derived relation eq.(1) in our spectral analysis.


Fig. 2 Theoretical wavelength calibration curve are measured wavelength
Reference

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2) JAMES A. R. SAMSON, Techniques of VACUUM ULTRAVIOLET SPECTROSCOPY, John Wiley \& Sons, inc., NEW YORK(1967)
