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Energy absorption and exposure build-up factors in hydroxyapatite

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ABSTRACT

The effective atomic number (Z_{eff}) and electron density (N_{el}) of hydroxyapatite (HA) and cortical bone have been computed for total photon interaction in the wide energy range of 1 keV–100 GeV using WinXCom. The variations of effective atomic number and electron density with energy of HA are compared with that of cortical bone. GP. fitting method has been used to compute energy absorption and exposure build-up factor of HA for wide energy range (0.015 MeV–15 MeV) up to the penetration depth of 40mean free path. The computed absorption build-up factor is used to estimate specific absorbed fraction of energy (Φ) and relative dose of photon in HA. Build-up factor increases with increase of penetration depth. The results of the present paper will also help in estimating safe dose levels for radiotherapy patients and also will be useful in dosimetry and diagnostics.

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1. Introduction

Gamma and X-radiation are widely used in medical imaging and radiation therapy. The user of radioisotopes must have knowledge about how radiation interacts with matter, especially with the human body, because when photons enter the medium/body, they degrade their energy and build-up in the medium, giving rise to secondary radiation which can be estimated by a factor which is called the 'build-up factor'. Calculations of the energy absorbed in a medium include not only the contribution of the uncollided photons from the source, but must also include the contributions from collided and secondary photons. In practice, this is done by multiplying the contribution of the uncollided photons by the energy absorption build-up factor. The energy absorption build-up factor is also defined as the build-up factor in which the quantity of interest is the absorbed or deposited energy in the interacting material and the detector response function is that of absorption in the interacting medium. Whereas the exposure build-up factor is defined as that build-up factor in which the quantity of interest is the exposure and the detector response function is that of absorption in air.

Singh et al. (2008) studied the variation of energy absorption build-up factors with incident photon energy and penetration depth for some solvents. In this study, the exposure build-up factors are computed on the basis of Z_{eq} which is calculated using the following interpolation formula:

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$$Z_{eq} = \frac{Z_1(\log R_2 - \log R) + Z_2(\log R - \log R_1)}{(\log R_2 - \log R_1)}$$
(1)

where Z_1 and Z_2 are the elemental atomic numbers corresponding to the ratios $(\mu_{comp} | \mu_{total}) R_1$ and R_2 respectively. R is the ratio for the chosen biological sample at particular energy. Then the GP fitting parameters were computed by interpolation method. The generated energy absorption build-up factor data was studied as a function of penetration depth and incident photon energy. Previous workers [Singh et al. (2008)] used the equivalent atomic numbers, Z_{eq} (which is obtained from interpolation method) to compute the build-up factors. The variation of Z_{eq} with photon energy is not similar to the variation of effective atomic number (Z_{eff}). Hence this computed build-up factors may not be accurate. Manjunatha and Rudraswamy (2011a) computed the exposure build-up factors in the different regions of teeth enamel and dentin based on the accurate values of effective atomic number (Z_{eff}). Manjunatha and Rudraswamy (2011b) studied the specific fraction of absorbed energies in the energy range 0.015-15 MeV. The build-up factor data were computed by different codes such as PALLAS-PL [Takeuchi (1973)], RADHEAT-V4 [Yamano et al. (1989)], ADJMOM-1 [Simmons (1973)] and ASFIT [Gopinath and Samthanam, 1971]. American National Standards ANSI/ANS 6.4.3 (1991) used GP fitting method and provided build-up factor data for 23 elements, water, air and concrete at 25 standard energies in the energy range 0.015-15 MeV with suitable interval up to the penetration depth of 40mean free paths. The ANSI/ANS 6.4.3 (1991) standard for buildup factors has been administratively withdrawn, but work is in progress for updating this standard which is much used. For the time being there are no new reference data for build-up factors.



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Meanwhile, it should be all right to use the ANSI/ANS 6.4.3 (1991) standard, since the possible discrepancies are expected to be small for the low-Z materials [(Ryman et al. (2008) and Ruggieri and Sanders (2008)]. The geometric progression (GP) fitting seems to reproduce the build-up factors with better accuracy when compared with other available approximations such as Berger. Taylor and three exponential [Harima (1993) and Harima et al. (1986)]. The absolute value of the maximum deviation of buildup factors in the GP fitting is within 0.5-3%, in the threeexponential approach it is within 0.4-9.3%, in the Berger approach it is within 0.9-42.7%, and in the Taylor approximation it is within 0.4-53.2% (Harima, 1993). Recently, Asano and Sakamoto (2007) have compared their build-up factors of two typical heavy concretes evaluated by using Monte Carlo simulations code (EGS4) with ANSI/ANS-6.4.3 standard reference database, and concluded that there is good agreement between both, except occasional slight differences. These differences may be due to the fact that ANSI/ANS data is based on the calculations using the moment method [Eisenhauer and Simmons (1975)] with parallel beam source and the Monte Carlo code EGS4 with isotropic emission source. Shimizu et al. (2004) have reported that when using the invariant embedding, GP fitting and Monte Carlo methods agree well for 18 low-Z materials with small discrepancies. All the materials used in the present study consist of low-Z materials.

Hydroxyapatite (HA) is the main mineral constituent of human bone, and also used clinically for many years. It has good biocompatibility in bone contact as its chemical composition is similar to that of bone material. The primary purpose of tissue engineering is repair, regeneration, and reconstruction of lost, damaged or degenerative tissues. Bone tissue itself shows an excellent ability of regeneration, but for big bony defect, healing process is difficult, so that bone grafts are required. At this point, it is very crucial to match the osteoconductive properties of porous ceramic scaffold in one side with the osteoinductive or osteogenic properties of living bone cells in the other side. Theoretically, a degradation rate of the implant similar to the rate of tissue formation is expected. In bone tissue engineering, Hydroxyapatite (HA) has been applied as filling material for defects and augmentation, artificial bone graft material, and prosthesis revision surgery. Its high surface area leads to excellent osteoconductivity and resorbability providing fast bone in growth (Frieb and Warner, 2002; Agarwala and Bhagawat, 2005; Sopyan et al., 2007). Their chemical composition is close to the mineral phase of bone and it is an origin of their excellent biocompatibility to bone tissue. This meets the requirement of any materials designed for bone repair and augmentation (Hench, 1998). The benefits of HA as bone graft are predominantly its safety, biocompatibility and osteoconductivity so that it can be used as a substitution biomaterial for bone in many indications clinically (Damien and Revell, 2004).

Porous HA has been applied for cell loading (Ohgushi and Caplan, 1999; Banfi et al., 2000; Aoki et al., 2004), drug releasing agents (Krajewski et al., 2000; Byrne and Deasy, 2002), chromatography analysis (United States Patent 6210715, 2001), and the most extensively for hard tissue scaffolds (Moore et al., 2001; Muraglia et al., 2000). In drug delivery systems, it has been recognized that, a system for the slow, local and continuous release of drugs would be a decided advantage for the treatment of many ailments. One of potential candidates for such controlled drug delivery systems is porous ceramics; much attention has been paid to porous HA. Owing to their physicochemical and biological properties, porous HAs have been proven as a potential candidate for bone drug delivery system (Komlev et al., 2003). In the present work an attempt has been made to compute energy absorption and exposure build-up factors of HA for wide energy range (0.015 MeV–15 MeV) up to the penetration depth of 40mean free path using GP fitting method. Such data will be prime importance in accurate dose calculations which is useful in medical dosimetry.

2. Present work

The computations of build-up factor have been divided into three parts, which are as follows.

2.1. Computation of effective atomic number (Z_{eff}) and effective electron density (N_{el})

For computation of Z_{eff} , firstly the values of mass attenuation coefficients were computed from WinXCom computer program (Gerward et al., 2004). Z_{ef} and N_{el} can be computed from the following equations:

$$Z_{eff} = \frac{\left(\frac{\left(\frac{\mu}{\rho}\right)\sum\limits_{bio}in_{i}A_{i}}{\sum\limits_{i}n_{i}}\right)}{\left(\sum\limits_{i}\left(\frac{f_{i}A_{i}}{Z_{i}}\right)\left(\frac{\mu}{\rho}\right)_{i}\right)}$$
(2)

$$N_{el} = \frac{N}{\sum_{i} n_i A_i} Z_{eff} \sum_{i} n_i \tag{3}$$

where n_i is the number of atoms of *i*th element in a given molecule, $(\mu/\rho)_{bio}$, the mass attenuation coefficient of biomolecule, N, the Avogadro's number, A_i , the atomic weight of element *i*. $(\mu/\rho)_{bio}$ was estimated based on the chemical composition [(Ca₁₀(PO₄)₆(OH)₂)] and f_i is the molar fraction. The nominator in the equation (2) gives atomic crosssection and denominator of this equation gives electronic crosssection. Similarly Z_{eff} and N_{el} of cortical bone are computed based on their composition (ICRU-44). The computed Z_{eff} and N_{el} are given in Figs. 1 and 2.

2.2. Computation of GP fitting parameters

We have evaluated the GP fitting parameters (b, c, a, X_k and d) using following expression which is based on Lagrange's interpolation technique:



Fig. 1. Variation of effective atomic number Z_{eff} of hydroxyapatite and cortical bone with photon energy for total photon interaction.



Fig. 2. Variation of effective electron density N_{el} of hydroxyapatite and cortical bone with photon energy for total photon interaction.

$$P_{Z_{eff}} = \sum \left(\frac{\prod_{Z' \neq Z} \left(Z_{eff} - Z \right)}{\prod_{z \neq Z} \left(z - Z \right)} \right) P_{Z}$$

$$(4)$$

where lower case *z* is the atomic number of the element of known GP fitting parameter P_z adjacent to the effective atomic number (Z_{eff}) of the given material whose GP fitting parameter $P_{Z_{eff}}$ is desired and upper case *Z* are atomic numbers of other elements of known GP fitting parameter adjacent to Z_{eff} . GP fitting parameters (*b*, *c*, *a*, X_k and *d*) for element adjacent to Z_{eff} are provided by the standard data available in literature [*ANSI/ANS* 6.4.3 (1991)]. The computed energy absorption and exposure GP fitting parameters for HA is given in Table 1.

Table 1

GP	fitting	parameters	of	HA
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2.3. Computation of build-up factors

The computed GP fitting parameters (*b*, *c*, *a*, X_k and *d*) were then used to compute the energy absorption and exposure build-up factors in the energy range 0.015 MeV–15 MeV up to a penetration depth of 40mean free path with the help of GP fitting formula, as given by the equations:

$$B(E,X) = 1 + \frac{b-1}{K-1} \left(K^X - 1 \right) \text{ for } K \neq 1$$
(5)

$$B(E,X) = 1 + (b-1)X \quad \text{for } K = 1$$

$$K(E,X) = CX^{a} + d \frac{\tanh\left(\frac{X}{X_{K}} - 2\right) - \tanh\left(-2\right)}{1 - \tanh\left(-2\right)} \quad (6)$$

where *X* is the source-detector distance for the medium in mean free paths (mfp) and *b* is the value of exposure build-up factor at 1 mfp. *K* (*E*, *X*) is the dose multiplication factor and *b*, *c*, *a*, X_k and *d* are computed GP fitting parameters that depend on attenuating medium and source energy.

3. Results and discussions

The variation of Z_{eff} and N_{el} with photon energy for total photon interactions are as shown in Figs. 1 and 2 and this variation is because of dominance of different photon interactions. In lower energy region, photoelectric interaction dominates, hence Z_{eff} varies similar to photoelectric absorption. There is a slight increase in the Z_{eff} up to 15 keV and becomes maximum then decreases sharply. It remains constant from 0.2 MeV to 2 MeV which shows that coherent and incoherent processes increases. From 2 MeV to 300 MeV, there is regular increase in the Z_{eff} with photon energy. This is due to the increase in incoherent and pair production processes. From 300 MeV onwards Z_{eff} remains constant which is due to dominance in pair production processes. It is found that Z_{eff}

Energy(MeV)	GP fitting parameters for energy absorption build-up factors				GP fitting parameters for exposure build-up factors					
	b	С	а	X_k	d	b	С	а	X_k	d
0.015	1.010	0.457	0.171	26.008	-0.262	1.010	0.457	0.171	26.008	-0.262
0.020	1.026	0.428	0.177	30.134	-0.350	1.026	0.428	0.177	30.134	-0.350
0.030	1.097	0.364	0.234	13.661	-0.134	1.097	0.365	0.234	13.661	-0.134
0.040	1.245	0.403	0.213	14.652	-0.121	1.245	0.403	0.213	14.652	-0.121
0.050	1.538	0.509	0.164	15.047	-0.089	1.538	0.509	0.164	15.047	-0.089
0.060	2.073	0.567	0.155	13.636	-0.083	2.073	0.567	0.155	13.636	-0.083
0.080	3.286	0.891	0.043	14.070	-0.038	2.780	0.889	0.045	13.710	-0.018
0.100	4.090	1.198	-0.031	13.195	-0.002	2.941	1.154	-0.019	13.592	0.006
0.150	4.094	1.603	-0.105	13.301	0.038	3.046	1.464	-0.077	15.048	0.015
0.200	3.638	1.715	-0.121	13.718	0.044	2.891	1.565	-0.093	15.566	0.023
0.300	3.042	1.733	-0.125	14.034	0.045	2.626	1.595	-0.099	15.127	0.025
0.400	2.736	1.675	-0.118	14.332	0.041	2.459	1.564	-0.097	15.272	0.026
0.500	2.545	1.617	-0.111	14.342	0.039	2.333	1.527	-0.094	15.414	0.027
0.600	2.409	1.557	-0.102	14.570	0.036	2.238	1.486	-0.088	15.353	0.026
0.800	2.232	1.460	-0.088	14.841	0.031	2.109	1.412	-0.078	15.395	0.024
1.000	2.113	1.383	-0.076	14.975	0.028	2.014	1.353	-0.070	15.695	0.023
1.500	1.938	1.251	-0.054	14.387	0.020	1.873	1.234	-0.049	14.889	0.017
2.000	1.840	1.159	-0.035	14.588	0.013	1.791	1.155	-0.034	15.254	0.012
3.000	1.700	1.056	-0.011	13.026	0.000	1.678	1.061	0.003	13.937	-0.001
4.000	1.609	0.989	0.007	14.040	-0.010	1.601	0.995	0.005	12.968	-0.009
5.000	1.548	0.927	0.027	12.943	-0.025	1.538	0.944	0.022	11.277	-0.021
6.000	1.475	0.929	0.025	15.484	-0.028	1.485	0.932	0.025	11.936	-0.020
8.000	1.380	0.909	0.032	12.115	-0.023	1.404	0.903	0.034	13.827	-0.028
10.000	1.309	0.915	0.031	14.507	-0.027	1.340	0.890	0.040	13.113	-0.033
15.000	1.229	0.838	0.061	14.182	-0.055	1.248	0.859	0.053	14.300	-0.054





Fig. 3. Variation of energy absorption build-up factor with photon energy for hydroxyapatite.

values of HA vary from the element with lowest *Z* to the highest *Z* present in their composition.

The variation of energy absorption and exposure build-up factors with incident photon energy for HA is shown in Figs. 3 and 4. From these figures it is observed that energy absorption and exposure build-up factors increases up to the E_{pe} and then decreases. Here E_{pe} is the energy value at which the photoelectric interaction coefficients matches with Compton interaction coefficients for a given value of effective atomic number (Z_{eff}). E_{ne} is almost equal to 0.1 MeV and for both exposure and absorption build-up factors. The variation of build-up factors with energy is due to dominance of photoelectric absorption in the lower end and dominance of pair production in the higher photon energy region. In the lower energy end photoelectric absorption is dominant photon interaction process; hence energy absorption build-up factor values minimum. As the energy of incident photon increases, Compton scattering overtakes the photoelectric absorption. It results multiple Compton scattering events which increases the energy absorption build-up factor up to the E_{pe} and becomes



Fig. 4. Variation of exposure build-up factor with photon energy for hydroxyapatite.

Fig. 5. Variation of energy absorption build-up factor with penetration depth for hydroxyapatite.

maximum at E_{pe} . Thereafter (above E_{pe}), pair production starts dominating (absorption process) which reduces the energy absorption build-up factor to a minimum value. The variation of energy absorption and exposure build-up factors with penetration depth of HA at 0.02 MeV, 0.1 MeV, 1 MeV, 4 MeV and 15 MeV is shown in Figs. 5 and 6. The build-up factor of HA increases with penetration depth. With increase in penetration depth, thickness of the interacting material has been increased which results in increasing the scattering events in the interacting medium. Hence it results in large energy absorption build-up factor values. So that the degree of violation of Lambert-Beer ($I = I_0 e^{-\mu t}$) law is less for least penetration depth.

The specific absorbed fraction of energy Φ is calculated the using the point source kernel method. In this method, the specific absorbed fraction of energy at distance *x* from the point source monoenergetic photon emitter is



Fig. 6. Variation of exposure build-up factor with penetration depth for hydroxyapatite.



Fig. 7. The variation of specific fraction of absorbed energy (Φ) with incident photon energy in hydroxyapatite at r = 0.01 mm and for various penetration depths up to 40mfp.

$$\Phi(\mathbf{x}) = \frac{\mu_{en} \exp\left(\mu \mathbf{x}\right) B_{en}}{4\pi \mathbf{x}^2 \rho} \tag{7}$$

Here μ_{en} is linear absorption coefficient of photons of given energy, μ is linear attenuation coefficient of photons of given energy, B_{en} is energy absorption build-up factor; ρ is density of the medium. The computed energy absorption build-up factors may be useful to evaluate Φ which intern helps for accurate dose calculation in HA. The variation of specific absorbed fraction of energy (g⁻¹) in HA at 5 mfp, 10 mfp, 15 mfp, 20 mfp and 40 mfp for various interacting thickness of the medium (0.01 mm, 0.1 mm, 1 mm) are shown in Figs. 7–9. From these figures it is observed that the specific absorbed fraction of Φ with energy is due to dominance of photoelectric absorption in the lower end and



Fig. 8. The variation of specific fraction of absorbed energy (Φ) with incident photon energy in hydroxyapatite at r = 0.1 mm and for various penetration depths up to 40mfp.



Fig. 9. The variation of specific fraction of absorbed energy (Φ) with incident photon energy in hydroxyapatite at r = 1 m and for various penetration depths up to 40mfp.

dominance of pair production in the higher photon energy region. In the lower energy end photoelectric absorption is dominant photon interaction process; hence Φ values minimum. As the energy of incident photon increases, Compton scattering overtakes the photoelectric absorption. It results multiple Compton scattering events which increases the value of Φ up to the E_{pe} and becomes maximum at E_{pe} . Thereafter (above E_{pe}), pair production starts dominating (absorption process) which reduces the value of Φ to minimum. The variation of specific absorbed fraction of energy (g^{-1}) of HA with penetration depth for various interacting thickness of the medium (0.01 m and 0.1 m) at 0.01 MeV, 0.1 MeV, 10 MeV, and 15 MeV is shown in Figs. 10 and 11. The specific absorbed fraction of energy for HA increases with penetration depth. With increase in penetration depth, thickness of the interacting material has been increased which results in increasing the scattering events in the interacting medium. Hence it results in large Φ values. The



Fig. 10. The variation of specific fraction of absorbed energy (Φ) with penetration depth in hydroxyapatite at r = 0.01 mm and for various incident energies up to 15 MeV.



Fig. 11. The variation of specific fraction of absorbed energy (Φ) with penetration depth in hydroxyapatite at r = 0.1 mm and for various incident energies up to 15 MeV.

specific absorbed fraction of energy decreases with the increase of thickness of the interacting medium.

The radial dependence of dose can be represented by $exp(-\mu r)$ B/r^2 . Here μ is denotes the linear attenuation coefficient for the appropriate photon energy and *B* is an absorption build-up factor. Hence photon dose at a distance r is given by $D_r = D_0 \exp(-\mu r)B/r^2$. Here D_0 is initial dose delivered by the point gamma ray emitter. The relative dose is $D_r/D_0 = \exp(-\mu r)B/r^2$. Hence relative dose of photon in HA is calculated from the computed absorbed build-up factor. The product of D_0 and relative dose gives actual photon dose at a distance *r*. The variation of relative dose (D_r/D_0) with photon energy in HA at 40mfp for various distances (r = 0.01 m to 1 m) is shown in Fig. 12. From this figure it is observed that relative dose (D_r/D_0) also increases up to the E_{pe} and then decreases. The variation of relative dose (D_r/D_0) with distance (r) in HA at 40mfp for various energies is shown in Fig. 13. Calculation of the dose distribution around point gamma ray emitters is useful in clinical dosimetry.



Fig. 12. Variation of relative dose (D_r/D_0) with photon energy in HA at 40mfp at various distances.



Fig. 13. Variation of relative dose (D_r/D_0) with distance (r) in hydroxyapatite at 40mfp at various energies.

Phantoms are constructed from materials having good tissue equivalence with respect to absorption of ionizing radiation. The fundamental advantage of such materials is that they allow the absorbed dose to be determined when information on the energy and nature of the charged particles at the point of interest is incomplete. For a given radiation type and energy, these materials should absorb and scatter radiation to the same extent, within acceptable limits, as irradiated tissue. Hydroxyapatite (HA) has been applied as filling material for bone defects and augmentation, artificial bone graft material, and prosthesis revision surgery. Its high surface area leads to excellent osteoconductivity and resorbability providing fast bone in growth. It is seen that the energy behavior of the effective atomic number of cortical bone is similar to hydraxyapatite (HA). When bone/HA is exposed to X-rays and gamma rays, then the maximum radiation dose to the tissue may not be at its surface but somewhere inside, due to the build-up of degraded photons by multiple scattering within the tissue. With proper knowledge of build-up factors of bone/HA, energy absorption can be carefully controlled. The results of the present paper will also help in estimating safe dose levels for radiotherapy patients and also will be useful in dosimetry and diagnostics.

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