

Measurements and Modeling of Coherent Synchrotron Radiation and its Impact on the LCLS Electron Beam

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(Dated: December 2, 2008)

Abstract

In order to reach the high peak current required for an x-ray free electron laser, two separate magnetic dipole chicanes are used in the Linac Coherent Light Source (LCLS) accelerator to compress the electron bunch length in stages. In these bunch compressors, coherent synchrotron radiation (CSR) can be emitted either by a short electron bunch or by any longitudinal density modulation that may be on the bunch. In this paper, we report detailed measurements of the CSR-induced energy loss and transverse emittance growth in these compressors. Good agreement is found between the experimental results and multi-particle tracking studies. We also describe direct observations of CSR at optical wavelengths and compare with analytical models based on beam microbunching.

PACS numbers: 29.27.Bd, 41.60.Ap, 41.60.Cr, 41.75.Ht

Submitted to the Phys. Rev. ST Accel. Beams

Work supported in part by US Department of Energy contract DE-AC02-76SF00515

I. INTRODUCTION

Coherent synchrotron radiation (CSR) is one of the most challenging issues associated with the design of bunch compressor chicanes for advanced accelerators and x-ray facilities. In recent years, effects of CSR on electron beam quality have been studied extensively in theory and simulations (see, e.g., Ref. [1] for a recent review). Experimental studies of CSR effects are relatively sparse because adequate beam quality is not commonly available. Examples of previous measurements can be found in Refs. [2–6]. In this paper, we present detailed measurements of CSR effects at the Linac Coherent Light Source (LCLS) and compare the results with tracking studies. We also present direct observations of CSR at optical wavelengths, evidently due to the modulated beam current (microbunching).

Figure 1 shows a schematic of the LCLS linacs and two bunch compressors (BC1 & BC2), with nominal beam energy listed at selected locations. Both compressors are four-dipole chicanes and are motorized so that the central two dipoles can be horizontally translated to match the beam trajectory. The horizontal dispersion is corrected after the chicanes using a pair of tweaker quads in the chicanes (see, e.g., BC1 layout in Fig. 2). The injector through BC1 was successfully commissioned in 2007 [7], and some preliminary results of BC1 compression and emittance growth were reported in Ref. [8]. The commissioning of the entire accelerator including BC2 has just been concluded in 2008 [9]. A “laser heater” (shown in Fig. 1) to Landau damp the microbunching instability by increasing the uncorrelated energy spread in the beam [10] will not be installed until late 2008. A relatively low charge of 250 pC is used to tune up the machine and to perform these CSR measurements, although higher charge levels of 1 nC have also been explored. The nominal linac and bunch compressor parameters at 250 pC charge are listed in Tables I and II, where RF phases are defined with respect to the crest (with negative phase values indicating the beam is in front of the crest). Under typical operating condition, the (rms) bunch length is compressed from 750 μm to 100 μm after BC1, and then to 8 μm after BC2 to reach a final current of 2.5 kA.

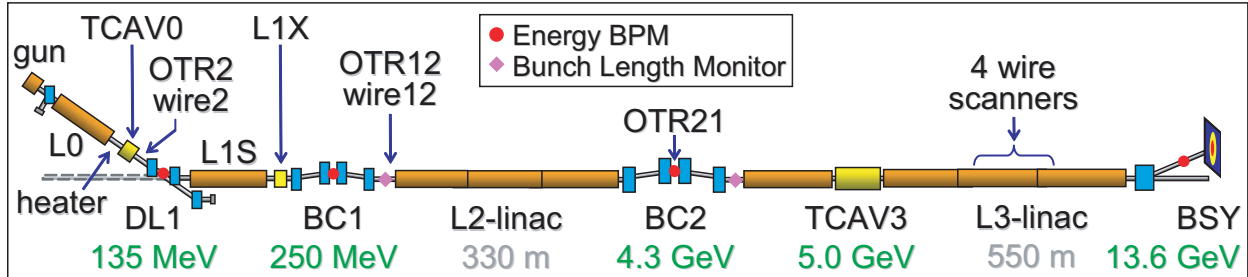


FIG. 1: LCLS accelerator layout showing BC1, BC2, both transverse RF cavities (TCAV0 and TCAV3), and screen at end of linac. The laser heater has not been installed for the experiments described in this paper.

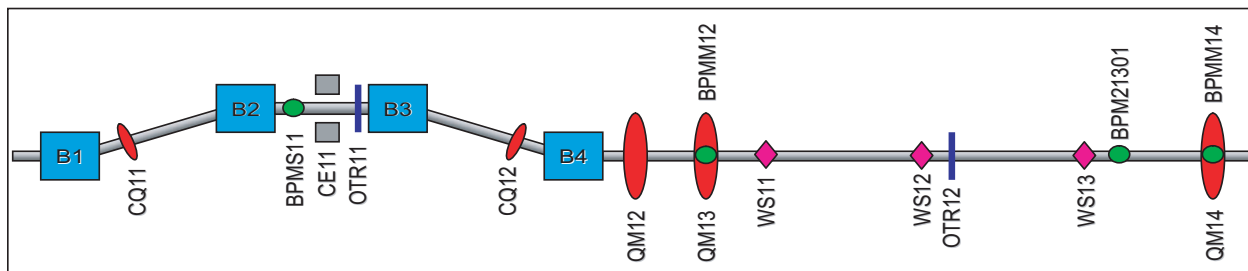


FIG. 2: Bunch compressor 1 (BC1) and its diagnostics section showing tweaker quads (CQ11 and CQ12) in the chicane for dispersion correction, BPMs, quadrupoles, OTR screens, and wire scanners (WS) for beam diagnostics.

II. BC1 RESULTS

A. Measurements

As is shown in Table I, at 250 pC charge (and 135 MeV energy), the measured (rms) bunch length is typically 750 μm and the normalized emittances (in x and y) are 0.7 μm . The bunch length is measured using a transverse deflecting cavity located in the injector area [11] (TCAV0 in Fig. 1), and the emittances are measured using an optical transition radiation (OTR) screen and a wire scanner before a 35° achromatic bend (DL1). In order to study the CSR effects on BC1 compression, the incoming energy chirp of the electron bunch is varied by adjusting the L1S RF phase from -20° to -30° while holding the BC1 energy constant at 250 MeV and the BC1 R_{56} constant at -45.5 mm. The short x-band section (L1X), a 4th harmonic RF system used to linearize the longitudinal phase space (by

TABLE I: Nominal measured beam and linac parameters for 250-pC bunch charge operation.

Parameter	Symbol	Value	Unit
Injector bunch length (rms)	σ_{z0}	~ 750	μm
Injector norm. emit. (x/y)	$\gamma\epsilon_0$	~ 0.7	μm
L1S RF phase (2856 MHz)	ψ_1	-22	deg-S
L1X RF phase (11.4 GHz)	ψ_X	-160	deg-X
L1X RF peak voltage	V_X	20	MV
L2 RF phase (2856 MHz)	ψ_2	-37	deg-S
L3 RF phase (2856 MHz)	ψ_3	0	deg-S
Final electron energy	E_f	13.6	GeV
Final bunch length (rms)	σ_{zf}	~ 8	μm
Final norm. emit. (x/y)	$\gamma\epsilon_f$	$\sim 1.3/0.7$	μm

TABLE II: BC1 and BC2 chicane parameters at 250 pC.

Parameter	Symbol	BC1	BC2	Unit
Electron energy	E_0	0.25	4.3	GeV
Energy spread (rms)	σ_E/E_0	1.4	0.38	%
Momentum compaction	R_{56}	-45.5	-24.7	mm
Chicane total length	L_T	6.5	23	m
Bend angle per dipole	$ \theta $	5.4	2.0	deg
Eff. length per dipole	L_B	0.20	0.54	m
Dipole bending radius	ρ	2.1	15.5	m
B1 to B2 (=B3 to B4)	ΔL	2.43	9.87	m
Dispersion at center	$ \eta $	247	363	mm
Translation range	Δx	0-30	0-52	cm

decelerating the bunch by about 19 MV), is also held constant in phase and amplitude.

To measure the absolute bunch length after BC1, the BC2 chicane is switched off and the bunch is vertically streaked using a transverse deflecting cavity located at 5 GeV (TCAV3 in Fig. 1). The phosphor screen located at the beam switchyard (BSY) after the L3 linac records the vertical beam size, which is then converted to bunch length due to the imposed

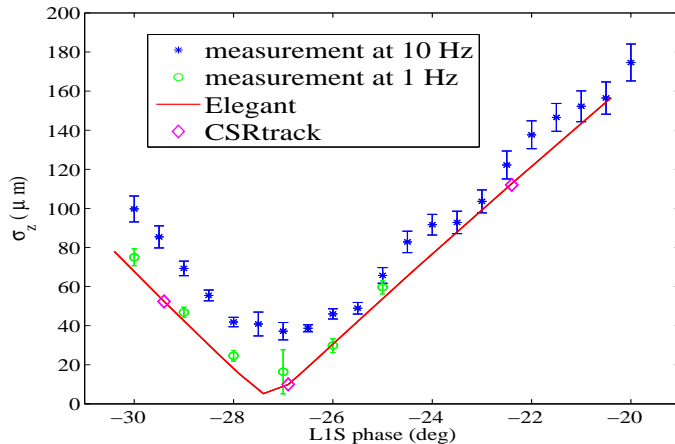


FIG. 3: BC1 compression measurements and simulations vs. L1S phase (zero phase is on crest). The 1-Hz (green) measurements are thought to be more accurate, due to a screen persistence problem at 10 Hz (blue).

$y - z$ correlation at TCAV3. The phosphor screen exhibits some persistence of beam images at higher bunch repetition rates. Because of vertical position jitters on the screen, the measured bunch lengths shown in Fig. 3 are usually reported longer at the 10-Hz repetition rate than at 1 Hz. Figure 3 also shows that the bunch is under-compressed above -27° and over-compressed below -27° , with the minimum measured rms bunch length of $15 \mu\text{m}$ at full compression. (The simulations shown here are taken from three separate computer codes, *Elegant*, *CSRtrack*, and *IMPACT-Z*), to be described below in Sec. II B.)

In a dipole magnet, coherent radiation of a Gaussian bunch entails an average energy loss per electron per unit length of [12]

$$\frac{dE}{ds} \approx \frac{1.8Ne^2}{\rho^{2/3}\sigma_z^{4/3}}, \quad (1)$$

where $N = 1.56 \times 10^9$ is total number of electrons (at 250 pC), and $\rho = 2.1 \text{ m}$ is the BC1 dipole bending radius (see Table II). A compressed bunch with rms length σ_z traversing the last dipole of BC1 (which is 0.2 m in length) can induce significant energy loss due to CSR (about 2 MeV for $\sigma_z = 10 \mu\text{m}$ at 250 pC). Since the energy loss occurs primarily in the last dipole, the bunch will be kicked horizontally and will execute a betatron oscillation after the bend. A BPM after BC1 (BPMM12 in Fig. 2) shows the expected horizontal steering effect due to CSR, which can be utilized in a quick scan to identify the full compression phase (see Fig. 4).

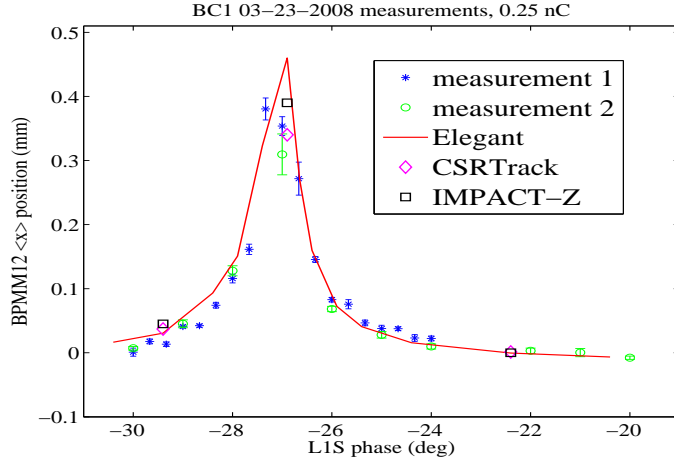
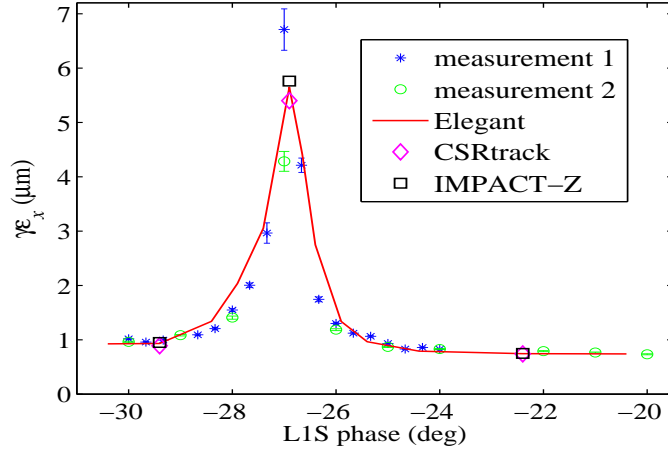


FIG. 4: Post-BC1 BPMM12 x -position vs. L1S phase to monitor CSR energy loss.

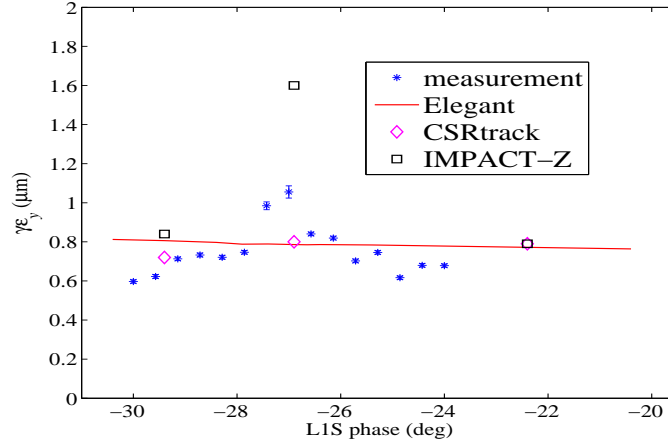
Also associated with the CSR energy loss, the bunch energy spread can increase in the chicane, giving rise to horizontal emittance growth after the chicane. A quadrupole magnet 1.0 meters after BC1 (QM13) and a wire scanner 2.2 meters after the quadrupole (WS12 in Fig. 2) are used to measure the projected emittances in both x and y using the “quad-scan” technique. Two separate sets of horizontal emittance measurements and one set of vertical emittance measurements are shown in Figs. 5(a) and 5(b). In addition to the pronounced peak in horizontal emittance at full compression (at -27° , as is shown in the simultaneous measurements of Fig. 3), a vertical emittance increase of 50% can also be seen. Note that BC1 normally operates at -22° (at a compression factor of ~ 7.5) where transverse emittances are unaffected by CSR. Note also that the emittances almost fully return to their uncompressed levels at phases below -29° , *i.e.* when the bunch is over-compressed. Figures 6(a) and 6(b) show measured horizontal profiles of the beam at the wire scanner, for the nominal phase (-22°) and at full compression (-27°), respectively. The horizontal profile at full compression is much larger and very much distorted due to CSR and shot-to-shot position jitter.

B. Simulations

Multi-particle simulations were used to compare with these measurements. First the injector (up to DL1 in Fig. 1) was modeled using the *IMPACT-T* [13] space charge code with one million macroparticles. The simulated normalized emittances and the rms bunch length



(a) Horizontal emittance after BC1 at 250 pC.



(b) Vertical emittance after BC1 at 250 pC.

FIG. 5: Measured and simulated transverse emittances after BC1 vs. L1S phase.

at the injector end were chosen to replicate the measured values shown in Table II. These macroparticles were used as input for *Elegant* [14] and for different L1S phases were tracked through BC1 with a 1-D CSR model that includes field transients. A phase shift of -0.4° was added in the simulation results of Fig. 3 to fit with measurements of the compressed bunch length. (This phase shift may come from RF drift during the measurements or for a small uncertainty in the initial phase.) The BPMM12 horizontal position readout due to CSR energy loss is in good agreement with *Elegant* simulations (see Figs. 4). In addition, the simulated emittances are compared with the measurements in Figs. 5(a) and 5(b). The validity of the 1-D CSR model was cross-checked using *CSRTrack* [15] with a 2-D (x - z) CSR algorithm (“g_to_m” method) to track the beam in the BC1 region for three L1S

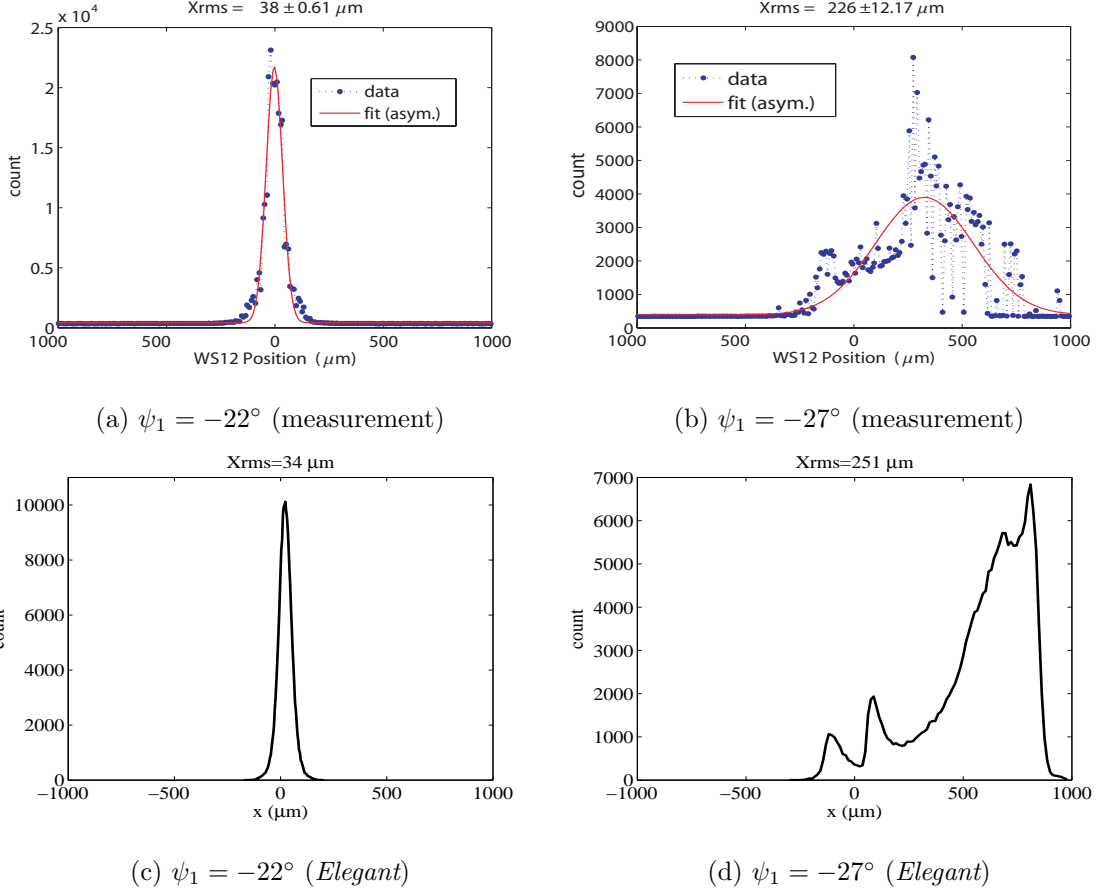


FIG. 6: Measured and simulated horizontal beam profiles at the post-BC1 wire scanner for two L1S phases.

phases as shown in Fig. 3 (when the beam is under-compressed, fully-compressed, and over-compressed). *CSRTrack* simulations yield the same rms bunch length (after applying the same -0.4° phase shift as in the *Elegant* case). Although the 2-D *CSRTrack* code predicts a somewhat different energy loss a few meters after the chicane, the energy loss up to the end of the last dipole is quite similar to that calculated by the 1-D *Elegant* code. As a result, the BPMM12 readout of CSR energy loss, which only responds to the loss up to the end of the last chicane dipole, is very well modeled by both codes (Fig. 4). Good agreement is also found between the simulated horizontal emittances from both *Elegant* and *CSRTrack* and the measurements. Figures 7(a)-(f) show *Elegant* simulations of the longitudinal phase space distributions and the current profiles at WS12 for three L1S phases, resulting in a beam that is under-compressed, fully-compressed, and over-compressed, respectively.

Since no vertical self-force is present in these two codes, *Elegant* and *CSRTrack* simulations

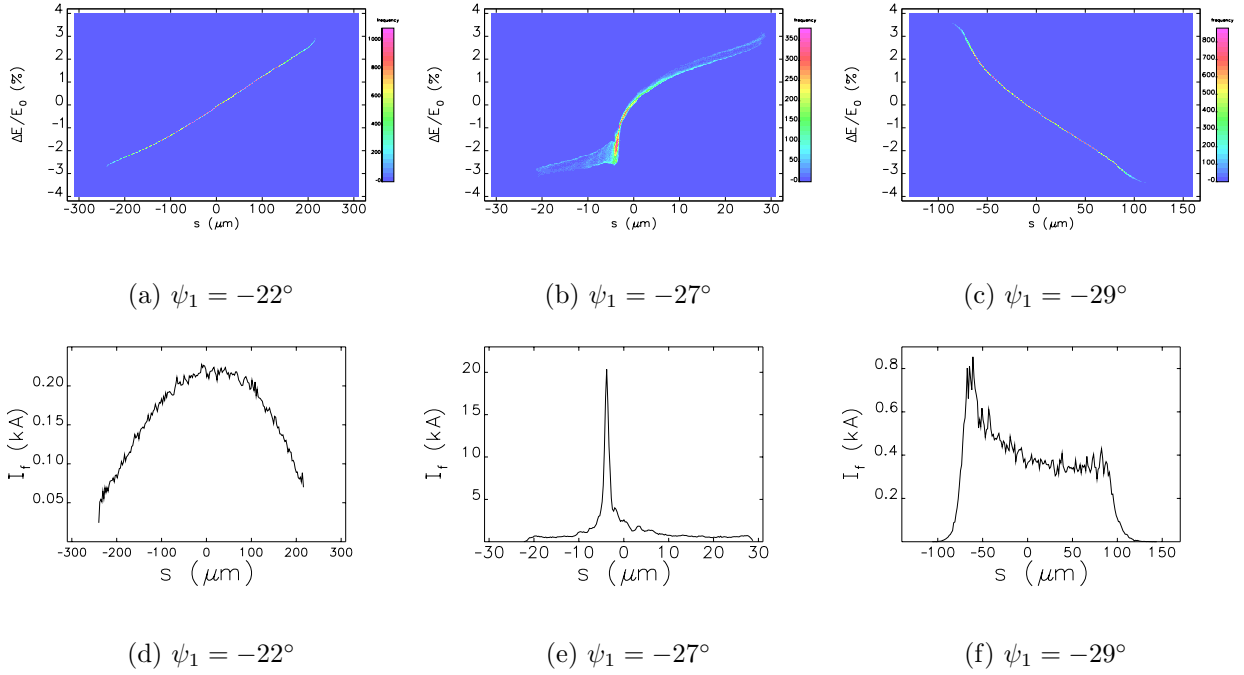
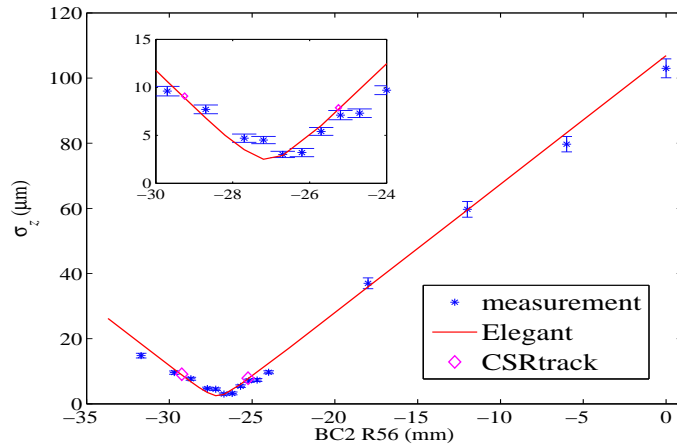
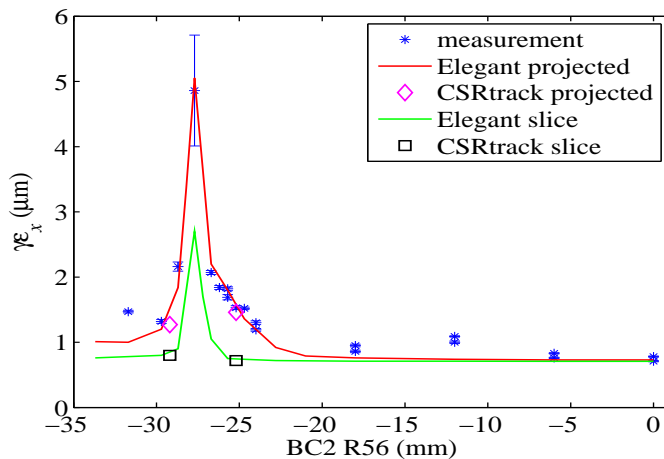


FIG. 7: *Elegant* simulations of the beam longitudinal phase space distributions (upper plots) and the current profiles (lower plots) after BC1 at 250 MeV for three L1S phases. The bunch head is to the left.

do not show any vertical emittance growth, in contrast with the vertical measurement at full compression. However, these simulations indicate that a current spike of ~ 20 kA is formed after BC1 at the full compression phase (see Figs. 7(b) and 7(e)). We suppose that the transverse space charge force at this high-current spike may increase the vertical emittance in the 3-m drift section after BC1 and before the beam reaches the wire scanner. Using a 3-D space charge code *IMPACT-Z* that incorporates the same 1-D CSR model as in *Elegant* [16], we simulate the three compression phases and plot the results in Figs. 4, 5(a), and 5(b). Figure 5(b) suggests that the increase in vertical emittance at full compression may be due to the vertical space charge effect after BC1. Finally, Figures 6(c) and 6(d) give the simulated horizontal profiles as obtained by *Elegant*, to be compared with the measurements.



(a) Compressed bunch length after BC2 at 250 pC.



(b) Horizontal emittance after BC2 at 250 pC.

FIG. 8: BC2 bunch length compression and emittance growth measurements and simulations.

III. BC2 RESULTS

A. Bunch length and emittance studies

When the BC2 chicane is switched on, the L2-linac phase (see Fig. 1) can also be varied to measure the bunch compression and its effect on the beam. The results are less reliable than those of the BC1 studies because the emittance can be sensitive to the RF phase of the 330-m L2 linac section. In order to avoid this problem, we instead vary the strength of the BC2 chicane while holding the L2 linac phase fixed at -37° , with BC1 in its nominal configuration as listed in Table II. The compressed bunch length is measured with the TCAV3 transverse

RF deflector (see Fig. 1) at a 1-Hz beam rate. The projected transverse emittances are measured with four wire scanners near the end of the linac (at about the 10 GeV point, see Fig. 1). Figures 8(a) and 8(b) show the measured bunch length and horizontal emittance as functions of the BC2 chicane strength (again at 250 pC charge). The rms bunch length measurements extend down to $\sim 2 \mu\text{m}$ near full compression (see inset plot in Fig. 8(a)). When BC2 is switched off, the horizontal emittance returns to the same level as the vertical emittance (not shown), both at the $0.7 \mu\text{m}$ level under nominal BC1 compression. This confirms the emittance preservation through the linac in the absence of BC2 compression. However, when BC2 operates at the nominal strength ($R_{56} = -24.7 \text{ mm}$ at 250 pC), the horizontal projected emittance is almost doubled due to CSR. *Elegant* tracking of the entire accelerator including wakefields, longitudinal space charge in the linac, and CSR in BC1 and BC2 confirms the CSR emittance growth in BC2 as a function of compression (red curve in Fig. 8(b)). The initial beam configurations are similar to the previous BC1 simulations, and -1° is added to the L2 phase in these simulations in order to match the bunch length measurements as shown in Fig. 8(a); again the discrepancies are likely due to small RF phase drifts during the experiment.

The longitudinal phase space of the compressed bunch is strongly affected by the longitudinal wakefield in the L2 linac, and the compressed bunch current profile is far from being a Gaussian or parabolic distribution. This is illustrated in *Elegant* simulations shown in Figs. 9(a)-(f) for three BC2 strengths, corresponding to a beam that is under-compressed, slightly over-compressed, and significantly over-compressed, respectively. These plots correspond to the 10 GeV point in the linac, where the projected emittances are measured by four wire scanners. The longitudinal phase space distributions may change after BC2 due to wakefields in the L3 linac but the current profiles remain the same as at the BC2 exit. When the bunch is under-compressed (see Figs. 9(a) and 9(d)), the simulated current profile has high-current leading and trailing spikes formed near the end of BC2. These high-current spikes contribute to most of the projected emittance growth. As *Elegant* simulations indicate, the slice emittance in the core part of the bunch is unaffected in this under-compressed regime (when $|R_{56}| < 25 \text{ mm}$, green curve in Fig. 8(b)). The bunch from the injector simulation is heavily smoothed to remove as much numerical noise as possible before the *Elegant* runs are begun; nevertheless, the beam after BC2 is clearly microbunched at wavelengths much shorter than the bunch length due to the very high gain of the LCLS accelerator system at these short

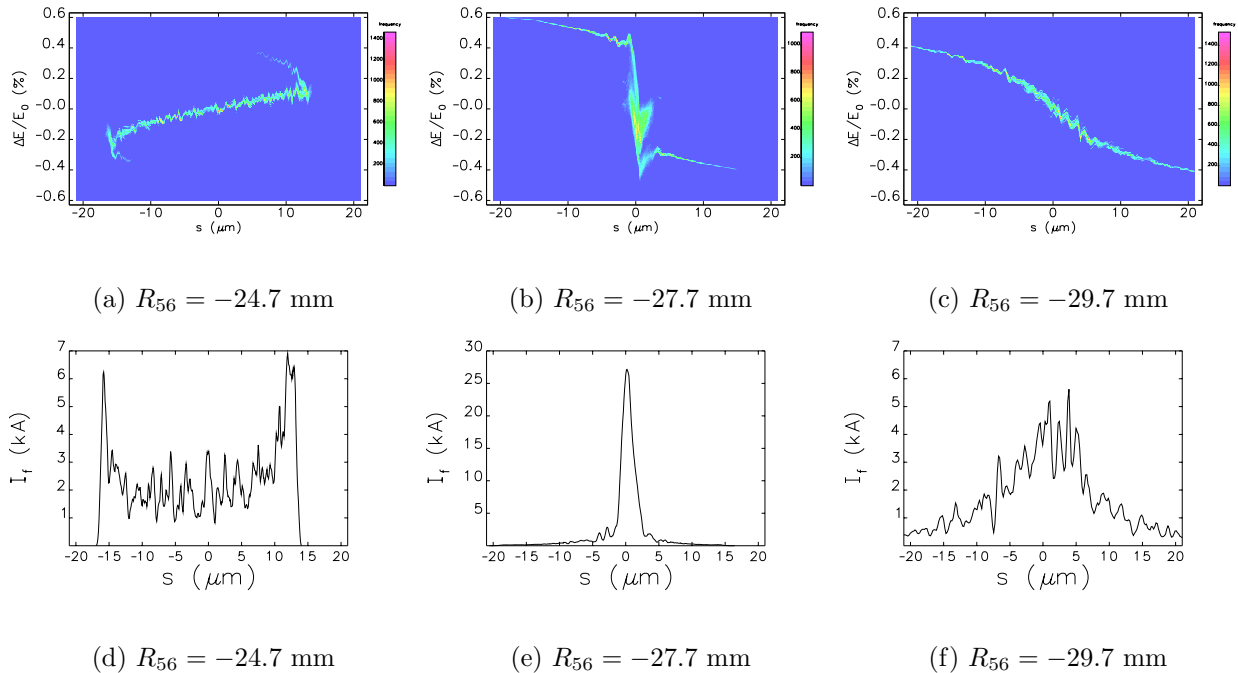


FIG. 9: *Elegant* simulations of the beam longitudinal phase space distributions (upper plots) and the current profiles (lower plots) in L3 linac at 10 GeV for three BC2 R_{56} settings. The bunch head is to the left.

wavelengths [10] (see Fig. 9). As is shown in Figs. 9(b) and 9(e), the bunch longitudinal phase space becomes even more complicated near full compression. The simulated peak current reaches a maximum of more than 25 kA when the bunch is slightly over-compressed (in terms of the rms bunch length), corresponding to the maximum projected emittance growth as shown in Fig. 8(b). *CSRtrack* results of bunch length and emittance growth at the end of BC2, for nominal compression (when $R_{56} = -24.7$ mm) and for an over-compressed case (when $R_{56} = -29.2$ mm), are also plotted in Figs. 8(a) and 8(b). We see that they agree with the *Elegant* results.

B. Direct observations of CSR on an OTR screen

As discussed above, wire scanners instead of OTR screens are used to measure the compressed beam profiles and transverse emittances. All OTR screens after DL1 are compromised by a strong coherent OTR (COTR) signal due to high-frequency longitudinal structure on the electron beam and hence these screens cannot be used for accurate beam profile mea-

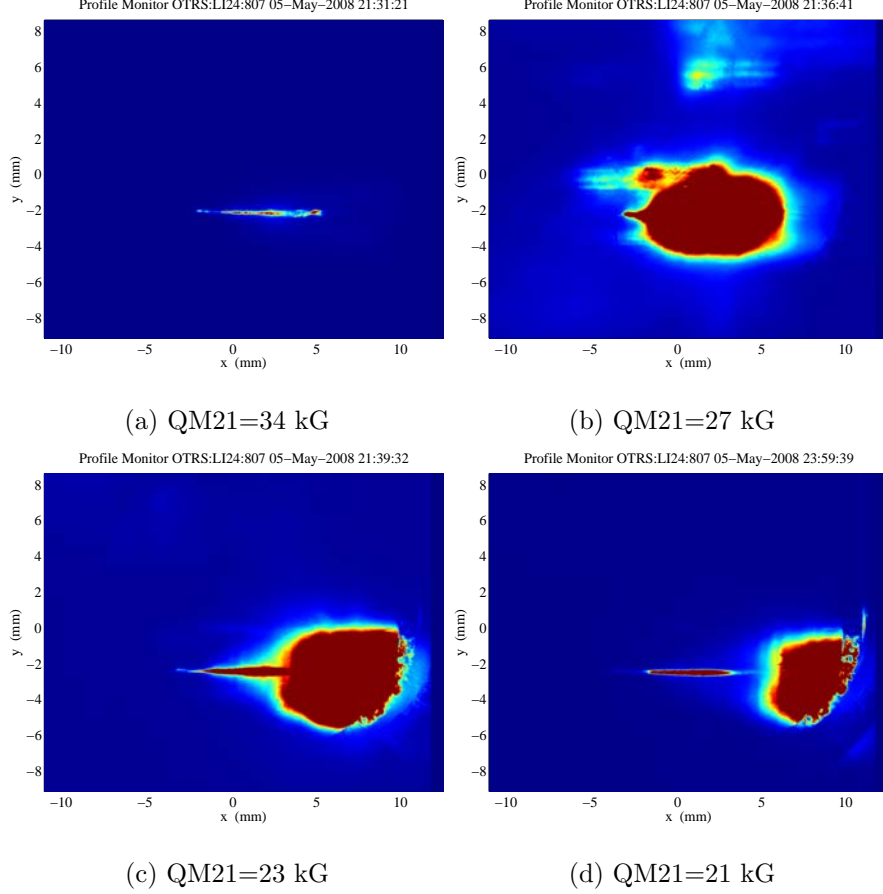


FIG. 10: Optical radiation pattern observed on an OTR screen upstream of the beginning of the third dipole in BC2 vs. pre-BC2 quadrupole strength (QM21).

surements [7, 17, 18]. Nevertheless, CSR signals generated inside a dipole, horizontally separated by the bend from COTR signals, are observed on an OTR screen (OTR21, shown in Fig. 1 as a red dot in the middle of BC2) while adjusting the strength of a horizontal-focusing quadrupole (QM21) a few meters upstream of BC2. The energy-chirped electron beam entering BC2 is dispersed horizontally in the middle of BC2. Thus, the OTR signal from OTR21 emitted by such a beam has a large aspect ratio in the transverse spot size as is shown in Fig. 10(a) (here QM21=34 kG, the nominal length-integrated quadrupole gradient). As we decrease the QM21 strength to 27 kG, a CSR signal with an enlarged and more rounded transverse spot appears on the screen (Fig. 10(b)). At even lower QM21 values, the CSR spot becomes (horizontally) separated from the OTR spot (Figs. 10(c) and 10(d)). In fact, a part of CSR signal is clipped off by the OTR screen frame in Fig. 10(d).

Since the OTR camera is sensitive to optical radiation from 350 nm to about 1 μm in

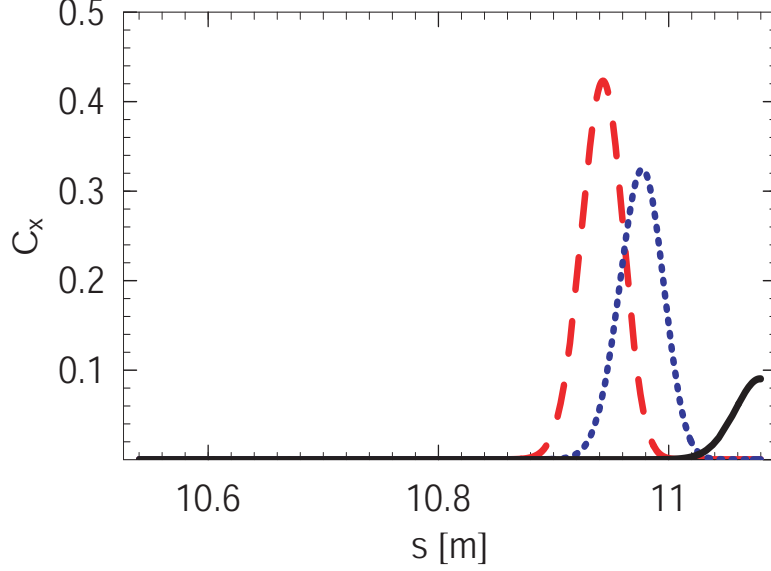


FIG. 11: Calculated transverse coupling factor in BC2 second dipole (from $s = 10.54\text{m}$ to $s = 11.08\text{m}$) for QM21=27 kG (black solid curve), 23 kG (blue dotted curve), and 21 kG (red dashed curve).

wavelength, the observed CSR signal most likely comes from longitudinal density modulation in the beam (microbunching) instead of from the overall bunch shape (the rms bunch length is $70\ \mu\text{m}$ in the middle of BC2). The evolution of a microbunched beam in a chicane under the influence of CSR can be described by an integral equation [19, 20]. Neglecting the small effect of CSR amplification of microbunching, the amplitude of density modulation in a chicane is coupled to the horizontal emittance by x - z (R_{51}) and x' - z (R_{52}) transport coefficients (as is shown in Eqs. (26) and (41) of Ref. [20]). Let us denote the transverse coupling factor as

$$C_x(k(s); s) \propto \exp \left[- \frac{k^2(s)\varepsilon_x\beta_0}{2} \left(R_{51}(s) - \frac{\alpha_0}{\beta_0} R_{52}(s) \right)^2 - \frac{k^2(s)\varepsilon_x}{2\beta_0} R_{52}^2(s) \right]. \quad (2)$$

Here $k(s) = k_0/(1+hR_{56}(s))$ is the modulation wave number at distance s from the beginning of BC2 (the initial point), k_0 is the initial modulation wave number, h is the initial (relative) energy chirp, α_0 and β_0 are the initial horizontal twiss parameters.

Thus, varying the upstream QM21 strength changes the initial beam divergence (*i.e.*, changes α_0 in Eq. (2)). In turn, this affects the microbunching amplitude through the R_{52} from the location of QM21 to the chicane center. If the maximum density modulation is reached inside the second dipole, a strong CSR signal emitted from that location will reach

the OTR screen (OTR21), but shifted in the $+x$ direction with respect to the OTR signal generated by the beam. This hypothesis was tested with numerical calculations based on Eq. (2) and the initial twiss parameters determined by the QM21 setting. We assume an initial modulation wavelength of $1.5 \mu\text{m}$, that is compressed to a wavelength $\lambda \leq 1 \mu\text{m}$ in the second dipole of BC2, so that optical radiation may be generated and observed by the OTR21 camera downstream. Figure 11 shows the evolution of the transverse coupling factor C_x in the second dipole for different QM21 strengths. When QM21=34 kG the transverse coupling factor is close to zero so that we do not observe any CSR signal on the screen (Fig. 10(a)). In this case, the microbunching is washed out by the large nominal horizontal beam divergence at QM21. When QM21=27 kG (black solid curve in Fig. 11), the divergence is reduced and the transverse coupling factor reaches a maximum at the end of the second dipole, hence CSR and coherent edge radiation are directed to the same horizontal screen location as the beam, as indicated in Fig. 10(b). When QM21=23 kG (blue dotted curve in Fig. 11), the transverse coupling factor reaches a maximum at ~ 10 cm before the end of the second dipole and strong CSR emitted from this location reaches the screen (which is 0.725 m downstream of the end of the second dipole), but now shifted horizontally from the beam center by ~ 5 mm. For QM21=21 kG (red dashed curve in Fig. 11), the transverse coupling factor reaches a maximum at ~ 13 cm before the end of the second dipole, and the calculated shift of the CSR center with respect to the beam center is 7 mm. The estimated horizontal shifts of CSR center from beam center agree well with the observed shifts seen in Figs. 10(c) and 10(d). Finally, we should point out that CSR is emitted with an opening angle on the order of $[\lambda/(2\pi\rho)]^{1/3}$, which explains the much larger vertical CSR spot size seen on the screen (~ 2 mm) than the vertical electron beam size.

IV. SUMMARY

We have presented detailed measurements of CSR-induced energy loss and transverse emittance growth in the two LCLS bunch compressors (which are at very different beam energies), and have observed CSR emission induced by a microbunched beam. These measurements and observations are consistent with simulations and analysis. The addition of a Landau-damping laser heater in late 2008 should suppress these high-frequency beam structures and may also reduce the horizontal emittance growth in BC2.

V. ACKNOWLEDGMENTS

We thank the SLAC engineering, lasers, controls, operations, and RF support groups for their help and dedicated support, and also thank J. Qiang in assisting us using both *IMPACT-T* and *IMPACT-Z* codes. This work was supported by Department of Energy Contract No. DE-AC02-76SF00515.

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