Study of low-lying resonant states in ¹⁶F using an ¹⁵O radioactive ion beam

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PACS: 27.20.+n, 25.40.Cm, 25.60.Bx, 21.10.Dr

Abstract

A 120 MeV ¹⁵O radioactive ion beam with an intensity on target of 4.5×10⁴ pps has been developed at the 88-inch cyclotron at the Lawrence Berkeley National Laboratory. This beam has been used to study the level structure of ¹⁶F at low energies via the p(¹⁵O,p) reaction using the thick target inverse kinematics method on a polyethylene target. The experimental excitation function was analyzed using R-matrix calculations. Significantly improved values for the level widths of the four low-lying states in ¹⁶F are reported. Good agreement with the theoretical spectroscopic factors is also obtained.

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I. INTRODUCTION

Among the nuclei in the A=16, T=1 isobaric triad, many states in ¹⁶N and ¹⁶O have been well established, but less has been reported on ¹⁶F. Four states of ¹⁶F below 1 MeV have been identified experimentally, and their energies are currently known to an accuracy of 4-6 keV (the next known state of ¹⁶F lies at 3.76 MeV) [Ti93]. Experimental studies with stable beams have also established spin-parity values for these low-lying states, but only upper limits or rough estimates of their level widths have been reported. The main difficulty in characterizing ¹⁶F has been that it can be broadly studied by relatively few reactions, primarily ¹⁴N(³He,n) [Za65, Bo73, Ot76], ¹⁶O(³He,t) [Pe65, Na77, St84, Fu02], ¹⁶O(p,n) [Mo71, Fa82, Or82, Oh87, Ma97], and ¹⁹F(³He, ⁶He) [Na77].

All the states in 16 F are unbound to 15 O+p. The spins and parities of the low-lying states have been found to be 15 O, 17 , 17 , and 15 in ascending order in energy, and are believed to have 15 O core-single proton configurations, namely $1p_{1/2}^{-1}$ $2s_{1/2}$ for the 15 O states and $1p_{1/2}^{-1}$ $1d_{5/2}$ for the 15 O, 15 states [Fa82, St84]. However, the variation in the $1d_{5/2}^{-1}$ - $2s_{1/2}^{-1}$ energy level difference across the members of the A=16, T=1 isobaric triad [Fo95, Og99] made initial 16 F spin assignments uncertain [Za65, Ot76] since 16 N showed 16 O, 16 O, 16 O, as is shown in Figure 1.

A recently developed ¹⁵O radioactive ion beam from the BEARS (Berkeley Experiments with Accelerated Radioactive Species) facility [Po00, Po03, Gu05] at the Lawrence Berkeley National Laboratory (LBNL) has been used to study the structure of ¹⁶F using ¹⁵O+p elastic resonance scattering and the Thick Target Inverse Kinematics (TTIK) method on a polyethylene target [Ar90, De92]. Of particular interest is

establishing the level widths of the low-lying ¹⁶F states, which can be compared to theoretical calculation for this proton unbound nucleus.

II. EXPERIMENT

The BEARS facility at LBNL's 88-inch cyclotron provides several proton-rich radioactive ion beams for studies of exotic nuclei and nuclear astrophysics [Gu05, Ka06]. Radioactive isotopes such as 11 C ($T_{1/2} = 20$ min.) and 14 O ($T_{1/2} = 71$ sec.) have been produced by bombarding 40 µA of 10 MeV protons from LBNL's Life Sciences Division's medical cyclotron onto a nitrogen gas target via $^{14}N(p,\alpha)$ and $^{14}N(p,n)$ reactions, respectively. These isotopes are then transferred in the form of volatile carbon dioxide (11CO₂ for 11C, and [14O]CO₂ for 14O) 350 meters via a capillary line to the 88inch cyclotron for injection into its Advanced Electron Cyclotron Resonance (AECR) ion source. Recently, an ^{15}O beam ($T_{1/2} = 122$ sec.) has been developed as the third radioactive ion beam in the BEARS system based on the process developed for the ¹⁴O beam. The nuclide ¹⁴O is produced in the form of H₂ ¹⁴O by adding a small amount of hydrogen to the nitrogen gas target, and this is then chemically converted in two rapid steps to [14O]CO2 [Po03]. For the case of 15O production, the gas target was loaded with ¹⁵N₂ instead of ¹⁴N₂. H₂¹⁵O was formed inside the gas target cell and chemically converted to [15O]CO2 for transfer to the 88-inch cyclotron. In addition, to conserve the ¹⁵N₂ gas using this batch type production process, it was stored and recycled into the gas target [Po06].

To set up the beam optics and eliminate the ¹⁵N component of the beam, a 160 MeV ²⁰Ne⁸⁺ beam was initially used as a pilot beam; then a weak 120 MeV ¹⁵N beam was

tuned into the experimental area, since the ¹⁵N⁶⁺ accelerating frequency is very close to that of the ²⁰Ne⁸⁺. Next, the ¹⁵N beam was fully stripped to its 7+ charge state by passing it through a thin aluminum stripper foil placed before an analysis magnet. The subsequent beam optics was then adjusted to focus the ¹⁵N⁷⁺ beam on the target. These adjustments were then changed to obtain ¹⁵O⁸⁺ from an accelerated and stripped ¹⁵O⁶⁺ beam. Finally, the cyclotron was carefully tuned to maximize a focused 120 MeV ¹⁵O⁸⁺ beam on the target position, eliminating ¹⁵N contamination as much as was possible. However, the cyclotron frequency difference between ¹⁵N⁶⁺ and ¹⁵O⁶⁺ is so small (1.2 kHz) that a residual amount of ¹⁵N contamination was still observed in the low energy region of the ¹⁵O spectrum. The measured amount of ¹⁵N contamination of the ¹⁵O beam was less than 2 % throughout the experiment. The ¹⁵O beam profile measured at 0° in the laboratory using a single silicon detector (see below) is shown in Figure 2.

Figure 3 shows the last stage of the experimental setup. At the beginning of the experiment, the ^{15}O beam was counted at 0° with a single silicon detector (1,000 µm), and scattered ^{15}O beam from a thin gold foil was measured simultaneously by a ΔE -E monitor telescope (25 µm and 300 µm, respectively) placed at 20° to the beam axis. The ratio between these two measurements allowed us to calculate that the average beam intensity of ^{15}O impinging on the target was 4.5×10^4 pps. The beam energy spread was measured to be 1.66 MeV FWHM at 0° after going through the aluminum stripper foil and the gold scattering foil (see Figure 3).

For the $^{15}\text{O+p}$ experiment, the 120 MeV ^{15}O beam[‡] was slowed down by a 3.81 μ m Ni degrader, and completely stopped in a thick 200 μ m (18.4 mg/cm²) CH₂ target. The

[‡] This beam energy was chosen to permit maximum ¹⁵O production by extracting the 6+ charge state from the AECR ion source, which has the maximum yield.

thickness of Ni degrader was chosen to stop the ^{15}O beam very close to the end of the target, minimizing the energy loss of emerging low energy protons within the CH₂ target. The main particle telescope was composed of ΔE (30 μ m), E1 (700 μ m), and E2 (5,000 μ m) silicon detectors, located at 0° at a distance of 10.9 cm from the target. The first two detectors were thick enough to detect protons from the four low-lying resonance states in ^{16}F , and the third one permitted the detection of high energy protons of up to 7 MeV in the center-of-mass (c.m.). The total energy resolution was found to be 28 keV c.m. (FWHM) for the energy region below 3 MeV c.m., including contributions from electronic noise, detector/setup geometry [Mo66], and beam straggling [Ma00] in the CH₂ target.

Figure 4 shows a typical two-dimensional particle identification spectrum recorded during the experiment using the ΔE -E1 part of the detector telescope. The proton band is clearly shown in this figure along with a lot of β^+ counts. A gate was drawn around this proton band, and the proton spectrum inside the gate was converted into a one-dimensional excitation function. This excitation function consisted of the sum of the ΔE and E1 detectors up to 2.7 MeV c.m. (see Figure 4 caption) and at higher energies was the sum of the ΔE , E1 and E2 detectors (in triple coincidence). The energy calibration for the ΔE -E1 and the ΔE -E1-E2 detector system was established by using the p(15 N,p) reaction [Ha57, Ba59, De62, Da84] before and after the main p(15 O,p) measurement because the energy levels of the relevant excited states in 16 O are well known. The measured laboratory energy of the protons at a given laboratory angle can then be converted to center-of-mass energy by using

$$E_{c.m.} = \frac{m_p + M(^{15}O)}{4M(^{15}O)\cos^2\theta_{lab}} E_{p,lab.}.$$
 (1)

Finally, proton counts were converted into cross-sections without any background subtraction, so that an arbitrary cross-section unit has been used for the excitation function. The experimental cross-section, $\frac{d\sigma}{d\Omega}$, was calculated by using an energy-dependent target thickness, Δx , which is inversely proportional to the stopping power, $\frac{dE}{dx}$ [Zi03]:

$$\frac{d\sigma}{d\Omega} = \frac{R}{\rho \times \Delta x \times I \times \Delta \Omega} = \frac{R}{\rho \times \left(\Delta E \times \frac{dx}{dE}\right) \times I \times \Delta \Omega},$$
(2)

where R is the proton yield, ρ is the target density [atoms/cm³], $\Delta\Omega$ is the detector solid angle, and I is the total ¹⁵O beam intensity [Ku01, Te03].

Figure 5 shows our measured $p(^{15}N,p)$ excitation function along with the results from the two previous $^{15}N(p,p)$ studies [Ba59, Da84]. The uncertainty of our energy calibration was estimated to be about \pm 15 keV in the center-of-mass frame. Figure 6 then shows the $p(^{15}O,p)$ excitation function up to 6.5 MeV, measured at 180° c.m. using the data from the complete detector telescope (ΔE , E1, E2) as described earlier.

III. DATA ANALYSIS

In this study, the level widths of the first four states in ¹⁶F were the main focus of the data analysis, so that only the low energy region below 3 MeV in the center-of-mass was selected for R-matrix analysis. As shown in Figure 7, the first four states in ¹⁶F are quite distinguishable, and the interference between potential and resonance scattering is clearly

observed. In order to compare these experimental results with theory, a resonance scattering analysis code, which is based on the R-matrix equations in Ref. [La58, Ru05], was written to calculate the theoretical excitation function. In order to perform the correct comparison with theory, background subtraction is necessary because protons from the reaction between the ¹⁵O beam and ¹²C in the CH₂ target may contribute to the measured proton spectrum. Due to the limited beam time, we did not measure the ¹²C(¹⁵O,p) spectrum. As a result, the earlier ¹²C(¹⁴O,p) reaction data using 120 MeV ¹⁴O were used to estimate this background contribution [Gu05]. This background proton spectrum is also shown in Figure 7, and the background is small in the region of the four low-lying resonances.

The J^{π} values of these four states are 0°, 1°, 2°, and 3° (as discussed earlier). To make the analysis simple, the 0° and 1° states are assumed to be pure $1p_{1/2}^{-1}$ $2s_{1/2}$ configurations, and only s-wave contributions to these resonances are considered. For the 2° and 3° states, only d-wave contributions are considered with a $1p_{1/2}^{-1}$ $1d_{5/2}$ configuration. Theoretical shell model calculations predict that the amplitudes of these simple configurations are well over 0.97 in these states (see Table III in Ref. [Fa82] and Table 4 in Ref. [St84]). The partial width of each combination of channel spin, s, and orbital angular momentum, ℓ , is represented as $\Gamma_{s\ell}$, which is a key parameter in the data fitting.

For the data fitting, the R-matrix calculation was convoluted with the experimental resolution function, and compared to the experimental cross section, after adding the background function discussed earlier whose shape was adopted from an earlier $^{12}\text{C}(^{14}\text{O,p})$ experiment. All the fitting parameters in both the R-matrix analysis (E_R and $\Gamma_{s\ell}$) and the background function (a simple Gaussian function) were iterated using a

minimization algorithm, MINUIT [Ja75], until the lowest chi-square per degree of freedom was obtained. This procedure was repeated, changing the initial values, upper/lower limits and step sizes of the fitting parameters, until the best χ^2 value was obtained.

A channel radius of 5 fm obtained by the conventional formula $r = 1.45 \left(A_1^{\frac{1}{3}} + A_2^{\frac{1}{3}} \right) fm$ was used in the all R-matrix calculations. Different values for the channel radius within a range from 4.5-5.5 fm were also tested, but no significant change in the results was observed. Finally, the level width and excitation energy of each state were obtained from the average value of these fitting results; the average χ^2 value was 1.08 per degree of freedom, which varied from 0.84 to 1.27.

IV. RESULTS AND DISCUSSION

The experimental cross section and the R-matrix calculations are shown in Figure 7, where the adopted background function is also shown. The level widths and excitation energies of the four states in this study are summarized in Table I. Spin-parity assignments were not tested in this work because data were only taken at one angle, but a different order of J^{π} values such as 0° , 2° , 1° , and 3° for the first four states in 16 F was found to create an excitation function whose χ^2 value was unacceptable. The excitation energies of these four states were also fitting parameters, and the results are in very good agreement with the known values [Ti93]. However, no improvement in the values was possible since these values are already known quite accurately with uncertainties less than 10 keV.

The level widths in Table I obtained from the $^{15}\text{O+p}$ data show new results compared to the compiled values from the previous studies. The level widths of the 0° , and 1° states were reported to be 40 ± 20 keV and less than 40 keV, respectively, in Ref. [Ti93]. Our study finds that the 0° state has a level width of 23.1 ± 2.2 keV, and that the broader 1° state has a width of 91.1 ± 9.9 keV (about twice the compiled value). However, the $^{14}\text{N}(^3\text{He,n})^{16}\text{F}$ data [Ot76] reported that the first two states are 1° , and 0° with level widths of 39 ± 20 keV, and 96 ± 20 keV, respectively (see Table I). Also note that the $^{16}\text{O}(^3\text{He,tp})$ data [St84] reported similar results (to ours) of ~ 25 keV and ~ 100 keV for the 0° and 1° state, respectively. The level width of the 2° state is found to be 3.3 ± 0.6 keV which is much narrower than the compiled value of 40 ± 30 keV, while 14.1 ± 1.7 keV for the 3° state is in good agreement with < 15 keV in Ref. [Ti93]. As reflected in the experimental results, the 0° and 1° states show relatively broad peaks as would be expected from s-wave scattering compared to the narrower 2° and 3° states from the d-wave scattering.

In order to compare these experimental level widths to theoretical expectations, the single particle width of each state, Γ_{sp} , was obtained from a potential model calculation for two different diffusion parameters, a, as is shown in Table II (also see Table III). This single particle width calculation allows us to estimate the proton partial width of each state using the equation $\Gamma_p = C^2 S \Gamma_{sp}$ if we know the single-particle spectroscopic factor, $C^2 S$. Experimental spectroscopic factors for ¹⁶N, which has the same core-single particle configuration as ¹⁶F, are available from a ¹⁵N(d,p)¹⁶N transfer reaction study [Bo72]. However, they are a factor of two less than theoretical prediction and this discrepancy has not been clearly explained (see discussion in Ref. [Bo72]). Theoretical

spectroscopic factors for the analogue states in ¹⁶N [Me96] are given in Table II for comparison.

As can be seen in Table II, the widths of all four levels are close to the single particle shell model predictions with either of the two diffusion parameters. This successful single particle approach was then applied to the level shifts between the mirror nuclei. We wanted to calculate the shifts with two goals: (1) to understand how the general features of the potential affect the isotopic shift for the s-states in ¹⁶N and ¹⁶F, and (2) to obtain an additional estimate of the single particle spectroscopic factors for the s-states. The isotopic shift of the levels depends primarily on the global radial distribution of the wave functions in the Coulomb field. It is well known [Th51, Eh51, No69] that the shift (to stronger binding) in the proton-rich nuclide is greatest for s-states due to the greater spacial extent of their wave functions.

The calculations were made with two sets of potential parameters (Table III) for the Woods-Saxon distribution, which mainly differ by two parameters. The first, the conventional calculation, had $r_0 = 1.2$ fm and the diffuseness parameter, a = 0.65 fm; the second, more diffuse potential had a smaller radius, which was compensated by a larger a = 0.75 fm. Then the well depths of the potentials were fixed by a fit to the excitation energies of the levels in 16 N, and the same parameters were used to calculate the excitation energies of the levels in 16 F. The only new factors in the calculations for 16 F were a small change of the reduced mass and the Coulomb potential of the uniformly charged sphere with radius parameter, $r_{\rm C}$, of 1.2 fm. (The change of this parameter to 1.17 fm resulted in ~ 10 keV shift toward less binding)

The "conventional" parameters in Table III result in a ¹⁶F ground state binding energy of -0.577 MeV, which is smaller than the experimental value of -0.535 MeV. We consider this disagreement as evidence of a need for a change of the parameters, which were fixed for stable nuclei [see also Go04]. Use of the diffuse potential provides 42 keV more binding than experiment for the 0° state and 58 keV more than for the 1° state (535 keV + 193 keV). In this case we can consider the differences as an indication that the spectroscopic factors of these states are less than the single particle limit. To estimate the needed changes of the spectroscopic factors, we took the ratio of the differences between the calculated and experimental level positions to the average difference between the excitation energies of the 2s_{1/2} states (0° and 1°) and the 1d_{5/2} states (2° and 3°) in ¹⁶N and ¹⁶F. As a result, we obtained 0.91 for the spectroscopic factor of the 0° state, and 0.88 for the 1° state (see Table II).

The absolute values of the spectroscopic factors are dependent upon the excitation energies of the $1d_{5/2}$ states in our approach. These excitation energies in their turn are dependent upon electromagnetic corrections and details of their nuclear structure (one can consider mixing with the nearest $d_{3/2}$ states, for example). These corrections could be as large as 100 keV, which would result in 2% corrections to the absolute values of the spectroscopic factors. In addition, the differences in the values of the spectroscopic factors for the 0^- and 1^- states can have physical meaning. The smaller spectroscopic factor for the 1^- state can be related to a possible admixture of the $1p_{1/2}^{-1}$ $1d_{3/2}$ configuration (it is much more difficult to find a possible admixture for the $1^{\pi} = 0^-$).

In conclusion, the experimental data on the widths and the excitation energies of the lowest states in ¹⁶F favor the more diffuse nuclear potential, as was observed earlier for

the ¹⁵F case [Go04]. The four low-lying states of ¹⁶F manifest remarkably clear single particle structure. In this sense the population of these levels in different nuclear reactions can be used as a test of nuclear reaction theory as was proposed recently in [Mu05].

V. SUMMARY

The energies and level widths of the first four states in ¹⁶F were measured with a ¹⁵O beam and proton elastic resonance scattering using the Thick Target Inverse Kinematics technique at 180° c.m. This study was made possible by the newly developed ¹⁵O radioactive ion beam using BEARS at the 88-Inch Cyclotron. The experimental data were analyzed with R-matrix calculations, and then compared to previous experimental results and theoretical predictions. This p(¹⁵O,p) experiment allows us to report more precise level widths with substantially less uncertainty than previously known values, and our experimental results also show very good agreement with theory.

ACKNOWLEDGEMENTS

This work was supported by the U.S. Department of Energy, Office of Nuclear Physics, under Contract No. DE-AC03-76SF00098 (Lawrence Berkeley National Laboratory). The authors also appreciate support by the U.S. Department of Energy Grants No. DE-FG02-93ER40773 and DE-FG52-06NA26207/A000. The authors would like to thank Mr. Mitch Andre Garcia for assistance with the experiment and Mr. Christopher Ramsey for his contributions at the medical cyclotron.

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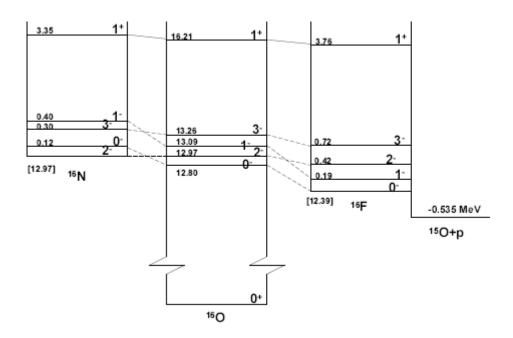


FIG. 1. An isobaric energy level diagram for the A=16, T=1 nuclear states [Ti93].

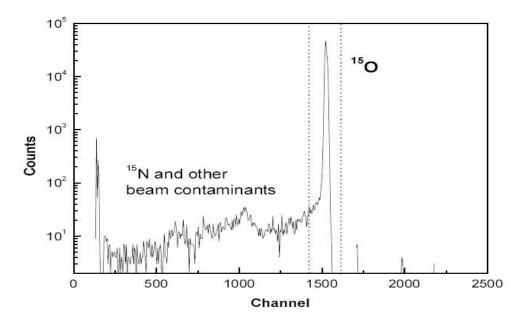


FIG. 2. The observed ¹⁵O beam profile at 0° in the laboratory without a Ni degrader and a target. A small tail consisting of ¹⁵N and other beam contaminants is observed. See text.

Detector Telescope at 0°

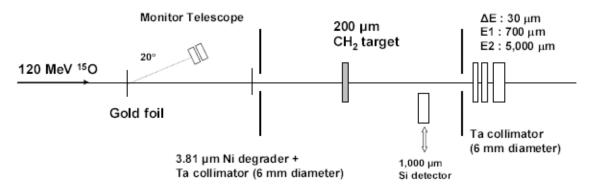


FIG. 3. The experimental setup for the ¹⁵O+p resonance scattering reaction. See text.

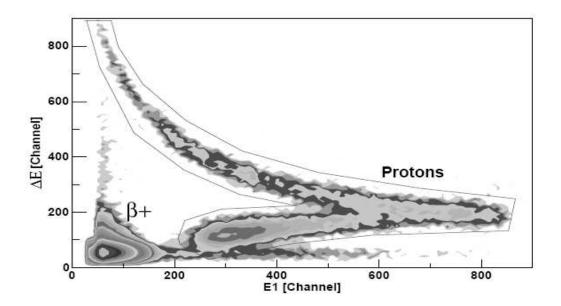


FIG. 4. A typical two-dimensional particle identification spectrum for ΔE -E1 coincidences. Protons with energies below 2.7 MeV c.m. (around channel number 850 in E1) stopped in the ΔE -E1 detector telescope. Protons above this energy punched through the E1 detector and were also recorded in coincidence in the E2 detector. Consequently, the deposited energy in both the ΔE and the E1 detectors starts decreasing after this point, as is shown. See text.

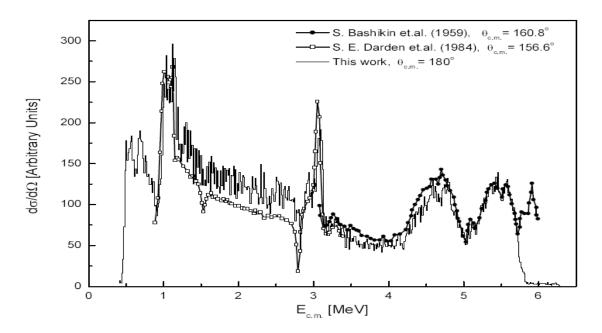


FIG. 5. The measured ¹⁵N+p excitation function at 180° c.m. without background subtraction used for the energy calibration. Experimental results from previous studies at different c.m. angles are also shown.

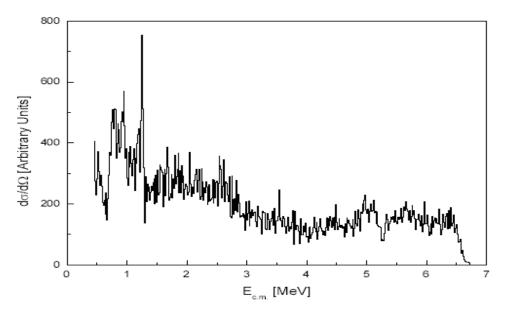


FIG. 6. The measured ¹⁵O+p excitation function at 180° c.m. up to 6.5 MeV c.m.

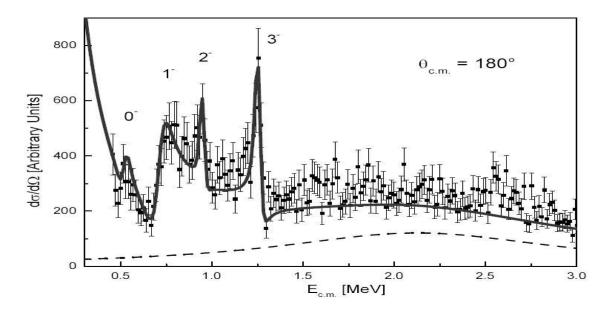


FIG. 7. The R-matrix fit for the low-lying states in ¹⁶F. The solid line represents the R-matrix calculation added to the background; the background function is shown as a dashed line. See text.

TABLE I. A comparison of previous experimental studies with our results for the level widths.

Compila	tion []	Гі93]		³ He,n) ¹⁶ F Za65]]		³ He,n) ¹⁶ F Ot76])(³ He,tp) [St84]	p(¹⁵ O,p) ^a		
E_x [MeV ± keV]	J^{π}	$\Gamma_p[\text{keV}]$	J^{π}	$\Gamma_p[\text{keV}]$	J	\int^{π}	$\Gamma_p[\text{keV}]$		ľπ	$\Gamma_p[\text{keV}]$	E_x^b [MeV ± keV]	J^{π}	$\Gamma_p[\text{keV}]$
0	0-	40±20	0-	50±30]	1-	39±20	()-	≈ 25	0	0-	23.1±2.2
0.19 3 ±6	1-	< 40	2-	< 40	()-	96±20		1-	≈ 100	0.190±20	1-	91.1±9.9
0.424±5	2-	40±30	1	40±30	≥	2	24±20	2	2-		0.422±19	2-	3.3±0.6
0.721±4	3-	< 15	3-	< 15	≥	2	24±20	3	3-		0.721±17	3-	14.1±1.7

^a This work.

^b The uncertainty primarily comes from the energy calibration (\pm 15 keV).

Table II. Comparison of ¹⁶F experimental results with the isobaric analog states in ¹⁶N and with theoretical calculations in the framework of the potential model.

	¹⁶ N			¹⁶ F		¹⁶ F Theory				
Ex	Ex		E_{x}	J^{π}	$\Gamma_p[\mathrm{keV}]^b$	Parameter set #1 (a=0.65 fm)	Parameter set #2 (a=0.75 fm)			
[MeV]	J^{π}	C^2S a	[MeV±keV]			$\Gamma_{\rm sp}[{ m keV}]$	$\Gamma_{\rm sp}$ [keV]	C^2S	C^2S	
. ,								(Exp.)	(Shift)	
0.120	0-	0.95	0	0-	23.1±2.2	21.8	22	1.05	0.91	
0.397	1-	0.96	0.190±20	1-	91.1±9.9	89.5	96	0.95	0.88	
0	2-	0.93	0.422±19	2-	3.3±0.6	3.6	4.3	0.77		
0.296	3-	0.87	0.721±17	3-	14.1±1.7	12.7	15.0	0.94		

^a OXBASH calculation reported in Ref. [Me96].

Table III. Woods-Saxon potential model parameters

	Parame	ter set #1	Parameter set #2			
	0-	1-	0-	1-		
V	-55.36 MeV	-54.42 MeV	-55.474 MeV	-54.455 MeV		
r _o	1.2 fm	1.2 fm	1.17 fm	1.17 fm		
a	0.65 fm	0.65 fm	0.75 fm	0.75 fm		
r _c	1.2 fm	1.2 fm	1.2 fm	1.2 fm		
V_{so}	7.64 MeV	7.64 MeV	7.64 MeV	7.64 MeV		
$a_{ m so}$	0.65 fm	0.65 fm	0.65 fm	0.65 fm		
r _{o so}	1.17 fm	1.17 fm	1.17 fm	1.17 fm		

^b This work.