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ABSTRACT

The effect of resonant magnetic perturbations on heat transport in DIII-D H-mode plasmas has been calculated by combining the TRIP3D field-line tracing code with the E3D two-fluid transport code. Simulations show that the divertor heat flux distribution becomes non-axisymmetric because heat flux is efficiently guided to the divertor along the three-dimensional invariant manifolds of the magnetic field. Calculations demonstrate that heat flux is spread over a wider area of the divertor target, thereby reducing the peak heat flux delivered during steady-state operation. Filtered optical cameras have observed non-axisymmetric particle fluxes at the strike-point and Langmuir probes have observed non-axisymmetric floating potentials. On the other hand, the predicted magnitude of stochastic thermal transport is too large to match the pedestal plasma profiles measured by Thomson scattering and charge exchange recombination spectroscopy. The Braginskii thermal conductivity overestimates the expected heat transport in the pedestal because the mean free path is longer than estimates of the parallel thermal correlation length, and collisionless transport models are probably required for accurate description. However, even the collisionless estimates for electron thermal transport are too large by one to two orders of magnitude. Thus, it is likely that another mechanism such as rotational screening of resonant perturbations limits the stochastic region and reduces transport inside of the pedestal.

1. INTRODUCTION

The strike point structure of a poloidally diverted tokamak has been predicted to become manifestly non-axisymmetric and develop helically striped patterns [1-6] when perturbed by magnetic fields due to external coils, field errors, and internal modes. There is potential to optimize this “strike-point splitting” in order to spread heat flux during steady-state operation in next-generation diverted reactors. Such patterns have been observed experimentally on DIII-D [7-9] during the application of three-dimensional magnetic perturbations and during locked modes. Non-axisymmetric heat flux deposition patterns during edge localized modes (ELMs) have also been observed on ASDEX-Upgrade [10-11] and during locked modes leading to disruption on MAST [12]. In addition, resonant magnetic perturbations (RMPs) have been shown to suppress [13-14] and eliminate [15-16] ELMs in DIII-D H-mode plasmas, so that true steady-state divertor operation can actually be achieved. This is important because at ITER values of pedestal collisionality, ELMs are predicted to release up to 20% of the pedestal stored energy on timescales fast enough to significantly erode the divertor target plates [17-18] and, thus, divertor lifetime.

Simulation of heat transport for DIII-D H-mode plasma discharge 122342 during the RMP ELM-suppressed phase is performed using the E3D Braginskii fluid transport code [19-20]. The E3D code, described in Section 2.2, performed the first calculations of non-axisymmetric heat flux deposition [19] for the circular limited TEXTOR tokamak’s Dynamic Ergodic Divertor [21]. In this work, we will use the E3D code to examine the heat flux patterns achieved in a poloidally diverted system and to address the question of whether stochastic transport can be responsible for the reduction in pedestal pressure gradient that led to the stabilization of Type-I peeling-ballooning modes as proposed in Ref. [16].

DIII-D’s strongly shaped magnetic fields are reconstructed using the TRIP3D code [22] which superimposes the fields from a given set of external coils upon the axisymmetric Grad-Shafranov EFIT [23] equilibrium reconstructed from experimental magnetic probes, flux loops, and motional Stark effect measurements. In order to reconstruct plasma profiles, kinetic EFIT [24] profile reconstructions also utilize information from Thomson scattering and charge exchange recombination spectroscopy, as well as calculations of the fast-ion pressure and bootstrap current. In addition to external perturbations from the MHD control “I-coil” and the field-error control “C-coil,” TRIP3D can also use a detailed model of intrinsic field errors constructed by the DIII-D field-error analysis team [25]. The I-coil consists of 6 upper and 6 lower sets of coils and is shown in Refs. [13-16]. All discharges in this study correspond to the up-down symmetric $n = 3$ “even-parity” configuration described in Refs. [15] and [16] that has 6 times larger resonant perturbation, $\delta b_{mn} / B$, than that of the up-down asymmetric “odd-parity” configuration described in Refs. [8] and [13].

A Poincarè plot of the $\phi = 0$ surface of section relative to the normalized poloidal magnetic flux surfaces, ψ , produced by TRIP3D for shot 123301 at 2170 ms is shown in Fig. 1(a). Field lines that escape to the divertor target have been traced for a maximum of 200 toroidal transits and are colored from yellow to black (color online) by the number of toroidal transits before escape in the forward direction (from 200 to 1). The Poincarè plot implies that many of the field lines in the outer 25% of the plasma (in normalized poloidal flux) can escape within ~ 1 -2 km. Remarkably, the measured plasma temperatures remain high enough ~ 1 -2 keV, that these connection lengths are of the same order of magnitude as the mean free path in this region. This implies that collisionless processes are important for determining parallel transport along field lines.

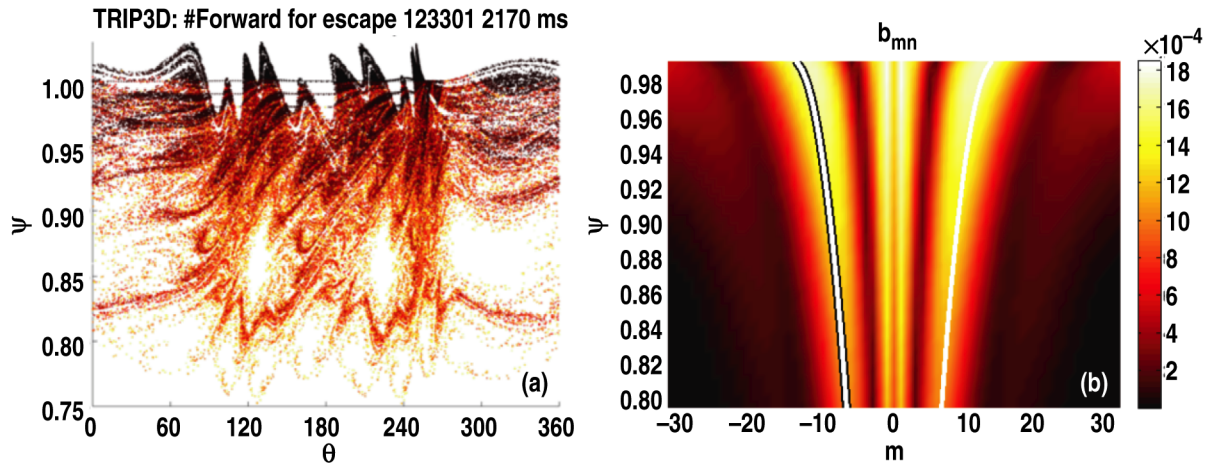


Fig. 1. (a) Poincarè plot of the $\phi = 0$ surface of section modeled for shot 123301 at 2170 ms for I-coil (3 kA-t), C-coil (12 kA-t) and intrinsic field errors. Field lines have been traced for a maximum of 200 toroidal transits and are colored from yellow to black by the number of toroidal turns before escape (200 to 1). Here, θ is not a straight-field lines angle, but the standard poloidal angle defined from the magnetic axis. (b) $n = 3$ Magnetic perturbation spectrum for shot 122342 at 4650 ms for I-coil (3 kA-t), but without C-coil and field errors. Black and white line indicates resonant left-handed modes $m = -3q$; white line indicates non-resonant right-handed $m = +3q$ modes.

Previous E3D simulations [9] have demonstrated greatly enhanced stochastic transport when all RMP sources are used. Because the C-coil and field errors introduce significant $n = 1$ perturbation components, the stochastic region is relatively broad and field lines from the edge can penetrate all the way to the location of the unperturbed $q = 2$ flux surface. However, an important caveat in the TRIP3D analysis is that the simple superposition of the equilibrium and external fields allows complete reconnection of magnetic flux. Unless the perturbation is large enough for the Lorentz force to overcome the viscous force, plasma rotation will tend to shield the resonant magnetic field components and limit the amount of stochasticity in the core [26-30]. In addition, the large diamagnetic flows at the edge of the H-mode plasma may limit the resonant fields at the edge. For simplicity, in this work we will not attempt to provide an accurate description of the plasma response fields. Instead, we will present results that assume that the TRIP3D analysis provides a first approximation of the

magnetic field sufficiently close to the separatrix. In order to limit the perturbation to the edge, in the following we study the effect of the I-coil perturbation alone. Although the fields in this case are relatively weakly stochastic, they have significant impact on the energetic balance in the simulation and the pattern of heat flux delivered to the divertor target.

In Section 2 we explore estimates for the stochastic enhancement of thermal diffusion and describe the computational technique required to accurately compute the parallel thermal transport in the fluid regime. In the third section we compare theoretical calculations of strike point splitting to experimental measurements. Finally, we conclude with a discussion of the relevance our results to experimentally determined transport and summarize our conclusions.

2. STOCHASTIC HEAT TRANSPORT

2.1. QUASI-LINEAR ESTIMATES

The dynamics of magnetic field lines can be estimated from the spectrum of the resonant magnetic field normal to a magnetic surface. If we define the flux surface averaged normal magnetic field perturbation via $\delta b_{mn} A = 2 \oint \sin(m\theta - n\phi + \chi_{nm}) \mathbf{B} \cdot d^2 \mathbf{a}$, so that the phase is χ_{nm} , then a set of perturbation parameters which simplify the formulae below are the Fourier series coefficients, $b_{mn} = \delta b_{mn} A / 2\pi \Psi_0$, normalized to the poloidal flux within the plasma $\Psi_0 = \Psi_{sep} - \Psi_{axis}$. Figure 1(b) displays the spectrum of the $n=3$ component of the I-coil perturbation at 3 kA-t as modeled by TRIP3D for plasma discharge 122342 at 4650 ms. Note that the spectrum has a ridge that follows the resonant value $m = -3q$, where $q = d\Psi_{tor} / d\Psi_{pol}$. Near the separatrix, the peak values are on the order of 1.8×10^{-3} . The spectrum determines the island width, $\delta\psi = 4\sqrt{b_{mn}/q'n}$, where $q' = dq/d\psi$, and since resonances are separated as $\Delta\psi = 1/q'n$, one can also estimate the Chirikov island overlap parameter, $\sigma = \delta\psi/\Delta\psi = 4\sqrt{q'n b_{mn}}$. As the separatrix is approached, the reconstructed profile is expected [3-4] to display logarithmic behavior of the form $q \rightarrow q_* \ell n(h_*/h)$, where we define $h = 1 - \psi$, and q_* , h_* are constants to be determined. The large shear $q' \rightarrow q_*/h$ forces island sizes to decrease as $h^{1/2}$ as the separatrix is approached, but since the width between resonances decreases in proportion to the shear, the island overlap still increases as $h^{-1/2}$. Thus, transition to stochasticity generically occurs sufficiently close to the separatrix at $h_{st} = 16q_* n b_{mn}$. A fit to the reconstructed q -profile produces $q_* = 0.56$, $\Delta_* = 24$, and therefore $h_{st} \sim 5\%$. Figure 2(a) shows that, for the I-coil perturbation alone, the overlap parameter exceeds unity over the outer 5%-10% of flux surfaces depending on the exact criterion one takes for stochastic transition.

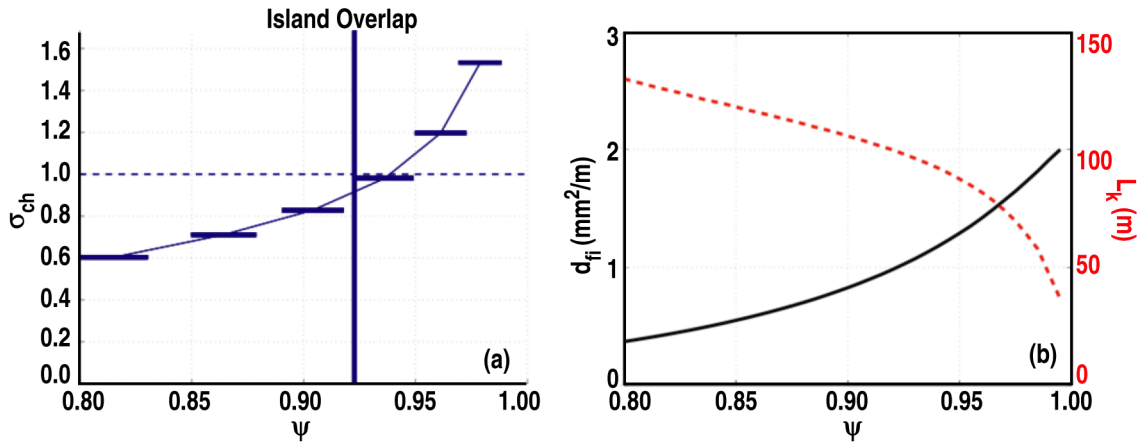


Fig. 2. (a) For the $n=3$ I-coil spectrum alone [Fig. 1(b)], the Chirikov island overlap parameter shows stochastic transition near $\psi = 0.92$. (b) The quasi-linear field line diffusivity and Kolmogorov length for the spectrum in Fig. 1(b) computed via Eq. (3).

Knowledge of the perturbation spectrum allows one to estimate the rate at which magnetic field lines wander across flux surfaces. For sufficiently ergodic motion, the field lines move across the unperturbed flux surfaces in a diffusive fashion so that $\langle \Delta x^2 \rangle \sim 2d_{fl} \ell$ along the length of a field line. The quasi-linear estimate [31] for the diffusion of poloidal flux in poloidal angle defined via $\langle \Delta \psi^2 \rangle = 2D_\psi \Delta \theta$,

$$D_\psi = \frac{\pi}{2} \sum_n b_{mn}^2 \delta_{m-qn} \quad , \quad (1)$$

grows quadratically with RMP amplitude. Here, δ_{m-qn} is shorthand for the Kronecker delta function $\delta_{m-qn,0}$. This, in turn, allows one to estimate the diffusion of field lines in real space

$$d_{fl} = \frac{B_T}{qRB} \frac{D_\psi}{|\nabla \psi|^2} \approx \frac{\pi q R}{2} \sum_n \left(\frac{\delta b}{B_T} \right)^2 \delta_{m-qn} \quad , \quad (2)$$

where B_T is the toroidal field, B is the total field strength and R is the major radius. Figure 2(b) shows that the characteristic diffusion coefficient is on the order of 1 mm²/m. In the collisionless regime, heat should diffuse at the thermal speed of the carrier particles, so that one can estimate the thermal diffusion coefficient to be $D_{st} = d_{fl} V_T$ where the thermal velocity $V_T = \sqrt{T/M}$ is defined in terms of temperature T and mass M .

In the collisional regime where the mean free path is shorter than the parallel thermal correlation length scale, $\lambda \ll L_T$, Rechester and Rosenbluth [32] estimated that the thermal transport coefficient would be reduced by a factor of λ/L_T , so that $D_{RR} = D_{st} \lambda/L_T = D_{\parallel} d_{fl}/L_T$. In equilibrium, the ratio of perpendicular (ρ_T) to parallel (L_T) correlation length scales must satisfy $\rho_T/L_T = \sqrt{D_{\perp}/D_{\parallel}}$, which reflects a balance of the diffusive time scales along and across magnetic field lines. At the same time, motion in the stochastic field causes these small perpendicular scales to stretch in the unstable Liapunov direction until they extend over a poloidal island length. Thus, the parallel thermal correlation length scale should be determined by the largest Liapunov exponent, or Kolmogorov length, up to a correction factor that only depends logarithmically on the diffusivity ratio, $L_{RR} = L_K \ell n(r/m\rho_T)$. The Kolmogorov length can be estimated via [33-34]

$$\frac{L_K}{\pi q R} = \frac{2\Gamma\left(\frac{1}{3}\right)}{\pi\Gamma\left(\frac{2}{3}\right)} (3D_K)^{-1/3} \approx 1.10 (D_K/2)^{-1/3} \quad , \quad (3)$$

where D_K represents the diffusion of neighboring trajectories. The quasi-linear estimate for D_K is given by a higher spectral weight of the perturbation spectrum,

$$D_K = \frac{\pi}{2} \sum_n (q' n b_{mn})^2 \delta_{m-qn} = \bar{n}^2 D_q = (q' \bar{n})^2 D_\psi \quad . \quad (4)$$

Since the Kolmogorov length is expected to scale inversely with perturbation strength, $L_K \sim b^{-2/3}$, the collisional diffusivity scaling, $D_{RR} \sim d_{fl} / L_K \sim b^{8/3}$, is even more rapid than the quadratic scaling in the collisionless case.

These estimates are clearly only relevant if a field line is long enough to sample the stochastic region, so that $\lambda \ll L_K \ll L_c$. If the connection length to the wall, L_c , becomes shorter than the Kolmogorov length, then the field lines exit the plasma ballistically, not diffusively, and this leads to greatly enhanced parallel transport [34]. For circular flux surfaces, the poloidal connection length, $L_c \sim \pi q R$, yields a reasonable estimate; however, in the stochastic case the connection length develops fractal structure [3-4,19]. Thus, we define the collisionality for parallel transport in terms of the ratio of mean free path to parallel thermal correlation length:

$$\lambda^* = \lambda / L_T \sim \min(\lambda / L_{RR}, \lambda / L_c) \quad , \quad (5)$$

where the asymptotic value is achieved in the appropriate regime. This definition is different from usual definitions of neoclassical collisionality [35] that compare the collision frequency to an effective bounce frequency.

2.2. COMPUTATIONAL METHOD

The E3D code [19-20] uses Monte-Carlo fluid elements to efficiently integrate the highly anisotropic advection-diffusion Braginskii fluid equations. Because the code has not yet implemented a model for neutral refueling, a key component of H-mode pedestal density physics, we focus on thermal transport alone, and keep the density fixed throughout the simulation. In this case, the solutions to the energy conservation equations

$$\partial_t \frac{3}{2} n_e T_e = \nabla \cdot n_e \chi_{||e} \hat{b} \hat{b} \cdot \nabla T_e + \nabla_{\perp} n_e \chi_{\perp e} \nabla_{\perp} T_e + Q_{ei} \quad , \quad (6a)$$

$$\partial_t \frac{3}{2} n_i T_i = \nabla \cdot n_i \chi_{||i} \hat{b} \hat{b} \cdot \nabla T_i + \nabla_{\perp} n_i \chi_{\perp i} \nabla_{\perp} T_i - Q_{ei} \quad , \quad (6b)$$

are essentially entirely determined by the boundary conditions and the geometry of the magnetic field. The parallel diffusivities are defined by their Braginskii values [36]

$$\chi_{||e} = 3.2 \tau_{ei} V_{Te}^2 \quad \chi_{||i} = 3.9 \tau_{ii} V_{Ti}^2 \quad , \quad (7)$$

and the nonlinear boundary conditions applied at the walls are the so-called Bohm sheath boundary conditions,

$$q_\alpha = \delta_\alpha T_\alpha \Gamma_\alpha \quad \Gamma_\alpha = n_e C_s \cos \beta_w \quad , \quad (8)$$

that require outflow of particles and energy at the ion sound speed, C_s . The boundary conditions depend on the angle between the field line and the wall β_w , and the flux coefficients δ_e and δ_i are determined from kinetic modeling studies in [37]. The plasma is assumed to be quasi-neutral so that $n_e = Z n_i$ with constant charge state $Z = 1$. The perpendicular diffusivities are assumed to be anomalous in origin and can be chosen to match experimental conditions. Experimentally inferred values for DIII-D H-mode plasma profiles typically range from 0.1-10.0 m²/s and vary significantly over the spatial extent of the edge plasma.

The Monte-Carlo elements are not particles, but heat packets which satisfy the equations of motion

$$\Delta \bar{x} = \sqrt{2\Delta t \bar{D}} \cdot \bar{\xi} + \bar{V} \Delta t \quad , \quad (9)$$

where $\bar{\xi}$ is a vector of random variables with unit standard deviation. In the limit of small times steps, the distribution function $f(x) = \sum_i w_i \delta(x - x_i)$ for the packets of heat, particles, etc. satisfies the ensemble-averaged $\langle f \rangle$ equation of motion

$$\frac{d\langle f \rangle}{dt} + \bar{\nabla} \cdot (\bar{V} - \bar{\nabla} \cdot \bar{D}) \langle f \rangle = S - \nu \langle f \rangle \quad . \quad (10)$$

The fluid equations of motion are reproduced with the choice $\bar{V}_{packet} = \bar{V}_{fluid} + \bar{\nabla} \cdot \bar{D}$ and sources represent the probability to inject or remove heat packets.

Because the thermal diffusivity is so anisotropic, $\chi_{\parallel} / \chi_{\perp} \sim 10^8 - 10^{11}$, tracking large parallel jumps of heat packets represents one of the major computational costs of the algorithm. E3D efficiently handles this cost by pre-computing field line following grids that trivialize the integration of the equations of motion. E3D uses the technique of “multiple local magnetic coordinate systems” to generate a series of field line following meshes that cover the entire domain. The RMP fields of interest are much smaller than the main toroidal field; by cutting the domain into enough toroidal sections, one can find a locally straight magnetic field line coordinate system in each subdomain. To make the method global, E3D generates a 3rd order spline mapping that interpolates between the faces of the subdomains. Thus, the large number of parallel numerical integration steps can be exchanged for a greatly reduced number of map evaluations. We find that six toroidal subdomains reproduces the field motion to sufficiently high accuracy. The mapping between subdomains typically has 80 radial x 360 poloidal grid points, while the plasma parameters within each subdomain are stored on a 32 or 64 point radial mesh x 360 poloidal x 16 toroidal mesh. A flexible definition of poloidal angle is used to focus enough resolution over the divertor region and on the divertor target to resolve the magnetic footprint.

2.3. EXPERIMENT

During DIII-D discharge 122342, the I-coils are energized to 3 kA-t in the $n = 3$ even parity configuration at 2000 ms, just after H-mode transition. The standard field-error correction algorithm was applied to the C-coil (maximum current of 12 kA-t) throughout the discharge. When the edge-safety factor reaches $q_{95} \sim 3.7$, particle transport is strongly affected, and the line-averaged density begins to decrease. The ELM frequency increases while the ELM size decreases until ELMs are completely suppressed at 2900 ms, when the target edge safety factor, $q_{95} = 3.5$, is achieved and the pedestal density is reduced to $n_{e,ped} = 2 \times 10^{13} \text{ cm}^{-3}$. Time-traces of similarly shaped discharges can be found in Refs. [15] and [16].

Figure 3(a) displays a set of fits to electron density, temperature, and ion density derived from Thomson scattering and charge exchange recombination data for discharge 122342 averaged over the ELM suppressed interval 4400-4900 ms. At 4650 ms, the total input power is $P_{NBI} + P_{Oh} = 5.1 \text{ MW}$ and the stored energy is essentially constant. The core radiated power is $P_{rad,core} = 0.5 \text{ MW}$, while the divertor radiates $P_{rad,div} = 0.9 \text{ MW}$. On axis, $n_e(0) = 4 \times 10^{13} \text{ cm}^{-3}$, and the low-density operation appears to increase the deposition of neutral beam energy into the ion channel: the ions reach 9 keV on axis while the electrons reach 3.5 keV. At the inside of the pedestal, $\psi = 0.85$, the ion temperature is 2.5 keV, while the electron temperature is 1.3 keV. Transport modeling using CORSICA determined that pedestal ions received close to twice as much power as pedestal electrons.

Figure 3(d)–(b) represent estimates of the parallel thermal diffusivity, mean free path, and correlation lengths based on these experimental profiles, using the expressions developed in Section 2.1. They will be discussed in detail in Section 2.5.

2.4. SIMULATION

We perform two numerical experiments that are intended to roughly match experimental conditions during the axisymmetric and RMP ELM-suppressed state. The protocol is to initialize E3D with axisymmetric profiles that are close to satisfying the correct boundary conditions and evolve until steady state. The density is not evolved, instead it is chosen to be a flux function that fits experimental Thomson scattering data, but becomes constant beyond the separatrix [Fig. 4(a),(b)]. Because E3D requires a good flux surface as an inner boundary condition, the inner surface is placed at $\psi = 0.86$ in the unperturbed case and $\psi = 0.82$ in the perturbed case. Since the stochastic field penetrates deeply into the plasma, a simple 1 or 2 level diffusivity model is not accurate enough to reproduce the experimental temperature profiles across the entire plasma domain. According to 1D analysis of the diffusivity of total pressure from the observed profiles, $D_{\perp} \sim 1 \text{ m}^2/\text{s}$ at the top of the pedestal and $D_{\perp} \sim 0.2 \text{ m}^2/\text{s}$ in the region of steep gradients. However, the steep gradient region is too narrow to accurately resolve in the simulation and qualitative results for the footprint structure are expected to be somewhat insensitive to the diffusivity profile; thus, we choose $D_{\perp} = 1 \text{ m}^2/\text{s}$

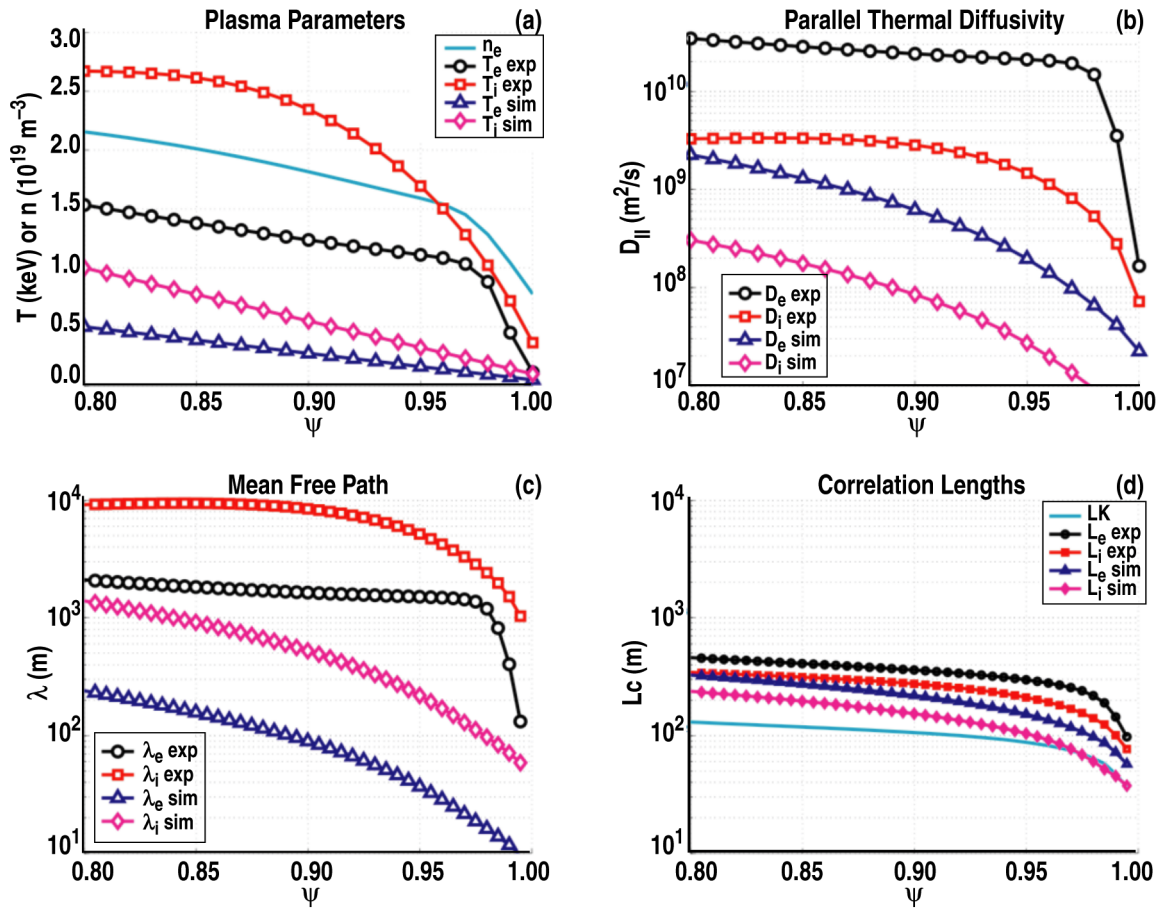


Fig. 3. Plasma parameters over the pedestal: (a) density and temperature, (b) parallel thermal diffusivity, (c) mean free path, (d) quasi-linear estimates of Kolmogorov length and thermal correlation lengths; *exp* = estimates based on measured H-mode profiles, *sim* = estimates based on simulation results for the I-coil (3 kA-t) perturbation.

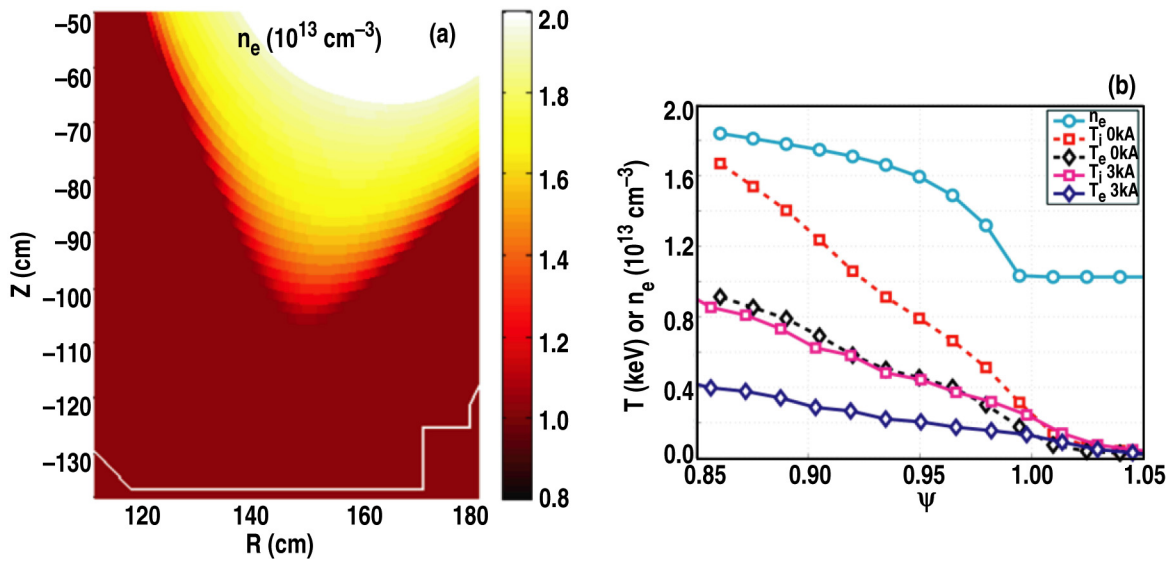


Fig. 4. Simulation input: (a) density contours, (b) density versus poloidal flux on the outer midplane. Simulation results: (b) temperature profiles for unperturbed (0 kA) and perturbed (3 kA) cases.

to be constant throughout the domain. In the simulation, a constant heat flux of 5 MW is applied to the inner boundary, and consistent with the CORSICA analysis above, 3.3 MW of the power is injected into the ions, while 1.7 MW is injected into the electrons.

Simulation results are shown in Figs. 4 and 5. The unperturbed cases are close to axisymmetric, while the perturbed cases clearly display three-dimensional structure (Fig. 5). In the next section it will be shown that this structure is primarily determined by the three-dimensional magnetic field line topology induced by the RMP. Figure 4(b) displays the simulation density and temperature profiles across the outer midplane. In the unperturbed case (0 kA), the profiles are roughly linear due to the choice of constant diffusivity and the temperatures achieved on the inner boundary are 1.7 keV for ions and 1 keV for electrons. The profiles in the perturbed case (3 kA) are linear as well, but have suffered a large drop in thermal confinement: the temperatures achieved on the inner boundary are 0.9 keV for ions and 0.4 keV for electrons.

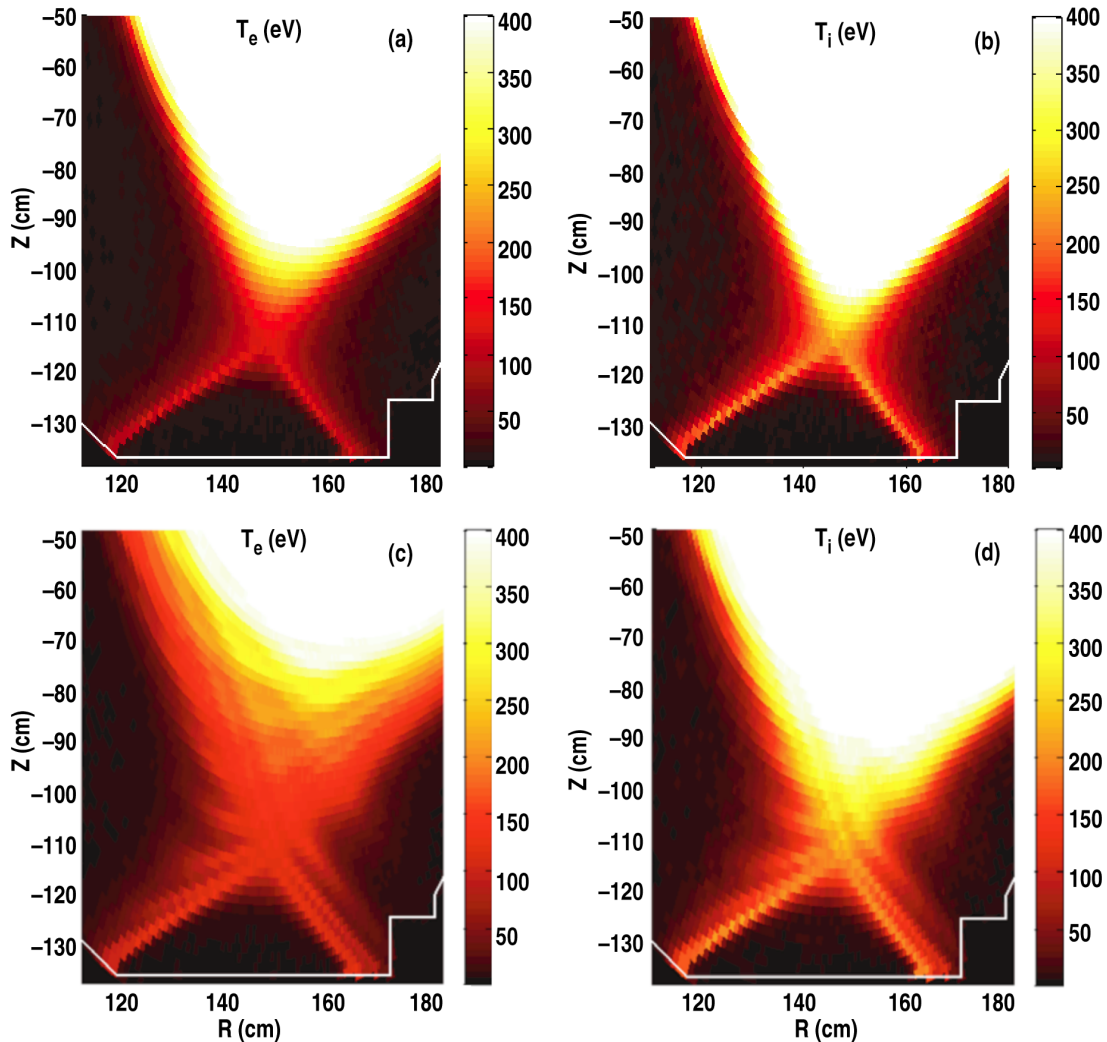


Fig. 5. Simulated temperatures at $\phi = 180^\circ$ toroidal location: (a) unperturbed T_e , (b) unperturbed T_i , (c) perturbed T_e , and (d) perturbed T_i .

2.5. THERMAL TRANSPORT COMPARISON

Considering the discussion of stochastic transport in the previous sections, it is surprising that the experimental thermal confinement remains high while particle confinement is reduced. In Refs. [15] and [16] it was demonstrated that the temperatures of both species in the steep gradient region are actually higher than the pre-RMP ELMing phase. In these experiments, the RMP reduces particle confinement at roughly constant stored energy. This implies a trade-off between higher density during the pre-RMP phase for higher temperature during the RMP phase. However, there appears to be large discrepancy between experiment and simulation in the RMP-induced change to the stored energy. The simulation results clearly show an enhancement to thermal conductivity in agreement with stochastic transport expectations.

To understand the source of the discrepancy qualitatively, let us examine the consequences of the quasi-linear transport estimates described in Section 2.1. Due to the relatively light mass of electrons, we expect electron thermal conduction to be 60 times larger than that of deuterium ions at fixed temperature. The Braginskii parallel thermal diffusivities in Fig. 3(b), defined via $D_{\parallel} = 2\chi_{\parallel}/3$, range from 10^{11} m²/s for electrons to 10^9 m²/s for ions over much of the observed plasma pedestal. The mean free paths for thermal conduction, defined via $\lambda = 2\chi_{\parallel}/3V_T$, for the experimental plasma are on the order of 1-4 km at the top of the pedestal as shown in Fig. 3(c). Due to the logarithmic correction factor, the thermal correlation lengths are close to 200-400 m, about 2-4 times larger than the Kolmogorov length [Fig. 3(d)]. Thus, even if we neglect the transition to short connection length at the plasma edge and use the approximation $\lambda^* = \lambda/L_{RR}$, Fig. 6(a) shows that the H-mode plasma is quite collisionless since $\lambda^*_e \sim 5$ and $\lambda^*_i \sim 30$. In fact, the ions are less collisional than the electrons due to their higher temperature.

Quasi-linear estimates for diffusive transport over the entire pedestal are shown in Fig. 6(b),(c). The best estimate of the actual value is the minimum of the collisional (D_{St}) and collisionless (D_{RR}) values and is indicated by open symbols. For the experimental H-mode profiles, the estimated collisionless electron thermal diffusivity reaches a maximum of ~ 20 m²/s in the steep gradient region near $\psi = 0.97$. Recall that the experimental result is closer to 0.2 m²/s, two orders of magnitude smaller, and both the observed electron and ion temperatures actually increase during the RMP [15-16]. The collisionless ion thermal diffusivity ~ 0.5 m²/s does have the correct order of magnitude to explain the increase in effective particle transport. However, such change in thermal conductivity is large enough to compete with neoclassical transport and should have observable consequences in the steep gradient region.

In contrast, for the simulated profile set, the temperatures of both species reach much lower values, and for the perturbed cases, this reduces the parallel diffusivities [Fig. 3(b)] and mean free paths [Fig. 3(c)] by one to two orders of magnitude. The electrons are cold enough to actually become collisional at these low densities and the ions are close to marginal,

$\lambda_{*i} \sim 1$, in the outer 5% of the plasma [Fig. 6(a)]. Thus, we can conclude that the fluid simulation is valid for electrons and, at best, marginal for ions. Figure 6(b),(c) show that the estimated stochastic enhancement in thermal diffusivity is roughly $D_{RRe} \sim 2 \text{ m}^2/\text{s}$ for electrons and $D_{RRi} \sim 0.5 \text{ m}^2/\text{s}$ for ions over much of the simulated pedestal. These order of magnitude estimates agree well with the change in diffusivity implied from the drop in the simulated temperatures between axisymmetric and perturbed cases; c.f. $\Delta D_e \sim 1.5 \text{ m}^2/\text{s}$ for electrons and $\Delta D_i \sim 0.7 \text{ m}^2/\text{s}$ for ions.

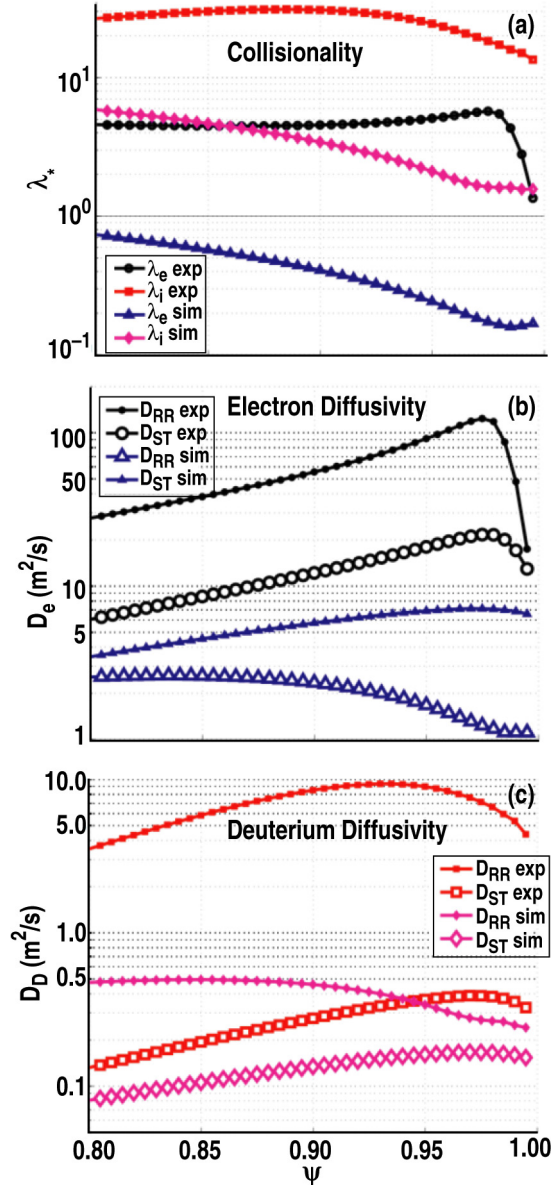


Fig. 6. Quasi-linear estimates for the effective (a) collisionality and (b) electron and (c) ion thermal diffusivity for the plasma profiles in Fig. 3. The best analytic estimates for the diffusivities, the minimum of the collisionless (*st*) and collisional (*RR*) values, are marked by open symbols.

3. STRIKE POINT SPLITTING

3.1. THE HOMOCLINIC TANGLE

In order to understand the way in which heat is transported across the separatrix, it is imperative to study the behavior of field lines in the vicinity of the separatrix and the X-point in particular. The X-point is constructed from four families of field lines: as we trace field lines in the forward toroidal direction, there are two entering families and two exiting families. In the axisymmetric case shown in Fig. 7(a), the entering and exiting field lines coincide and form the separatrix from a single self-intersecting, or homoclinic, orbit. Under perturbation, the X-point trajectory will deform, but it will survive. However, self-intersecting orbits are structurally unstable [38], and this topology will be destroyed by an arbitrarily small perturbation, as in Fig. 7(b). The four branches of the X-point can still be determined by locating the eigenvectors of the toroidal mapping of field lines near the fixed point and tracing the motion of field lines that enter/exit the X-point along those eigenvectors. However, “time reversal” symmetry in toroidal angle is fundamentally broken along the separatrix. Field lines that enter the X-point in the forward direction define the so-called *forward stable (backward unstable)* manifold, while the field lines that enter the X-point in the reverse direction define the *forward unstable (backward stable)* manifold, and these two manifolds no longer coincide.

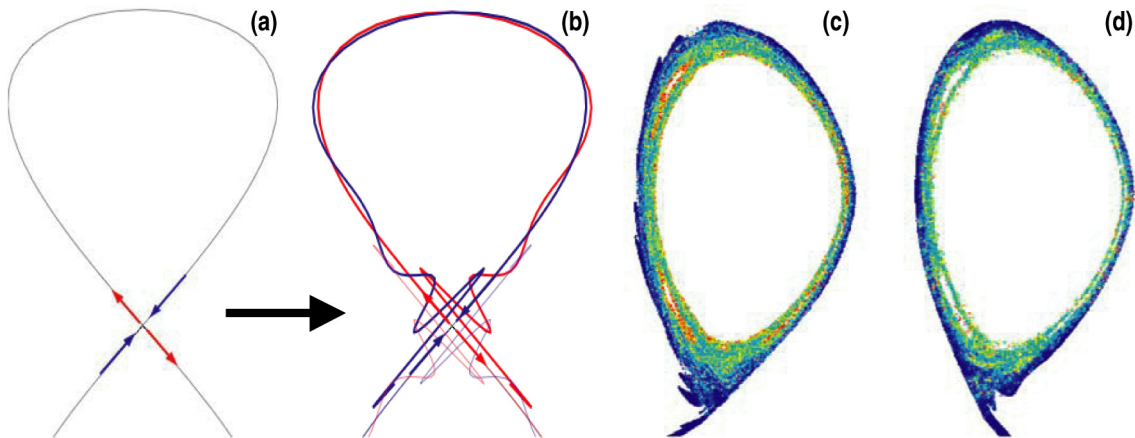


Fig. 7. (a) The axisymmetric separatrix is formed from a one-parameter family of homoclinic orbits that both exit (red) and enter (blue) the X-point in the forward direction. (b) Under perturbation, the family of exiting field lines (red) no longer coincides with the family of entering field lines (blue). Escaping field lines are still confined by these invariant manifolds as they exit in the (c) forward and (d) backward toroidal directions. The Poincaré plots in (c) and (d) use all TRIP3D magnetic field sources [as in Fig. 1(a)] and are colored from red to blue by the number of toroidal transits until escape (200 to 1).

No field line can ever cross such a manifold, because they are explicitly constructed from field lines and thus, must be invariant under parallel translations, $\vec{B} \cdot \vec{\nabla} \psi = 0$. However, in a chaotic field, these surfaces are “non-isolating” invariants of the motion, and they can

wander ergodically through the stochastic area of phase space. If we initialize points inside of the original separatrix and follow the field lines as they travel in the forward toroidal direction until they first strike the divertor target, Fig. 7(c) shows that they fill a large stochastic region, but the motion is clearly still bounded by a well-defined outer surface. Similarly, Fig. 7(d) shows that when traced in the opposite direction, a different outer bounding surface is developed. Neither manifold can intersect itself, but they generically intersect one another. If they intersect once, they must intersect an infinite number of times in either direction because the point of intersection can be mapped forward/backward along the stable/unstable manifold an infinite number of times, cf. Fig. 7(b). The lobes that lie between the stable and unstable manifolds transport flux along the boundary, and because the mapping is area preserving, both the forward and backward mapping of each lobe contains an equivalent amount of flux. The points of intersection of the manifolds must accumulate near the X-point, where the poloidal field vanishes, and, in order to preserve area, the lobes must then lengthen in order to counteract the decrease in width. As the lobes lengthen, their tips wander along an ever-increasingly complex self-avoiding path, eventually mixing with other lobes. This mixing is clearly ballistic at first, but after a close-encounter with the X-point, a field line will be scattered in an effectively random fashion.

Although the separatrix topology is “broken” by the perturbation, the invariant manifolds in the vicinity of the original separatrix still completely determine the fate of field lines. Melnikov [39] proved that small deformations of such manifolds can be treated linearly. To find the distance between the stable ψ_- or unstable ψ_+ manifold and the original separatrix ψ_0 , simply integrate along a field line from a point infinitesimally close to the X-point,

$$\psi_{\pm}(\phi, q\theta) = \psi_0 + \int_{\mp\pi}^{\theta} \frac{\vec{B} \cdot \vec{\nabla} \psi}{\vec{B} \cdot \vec{\nabla} \theta} d\theta \quad . \quad (11)$$

The difference in flux between the two manifolds, the Melnikov function,

$$\delta h(\phi_0) = \psi_+ - \psi_- = \int_{-\pi}^{\pi} \frac{\vec{B} \cdot \vec{\nabla} \psi}{\vec{B} \cdot \vec{\nabla} \theta} d\theta = 2\pi \sum_n b_{mn}(\psi_0) \delta_{m-qn} \sin(\chi_{mn} - n\phi_0) \quad , \quad (12)$$

depends upon the constant of motion $\phi_0 = \phi - q\theta$ alone. Note that although θ becomes singular as the separatrix is approached, the product $q\theta$ is simply the toroidal angle traversed, and thus, remains well behaved. The maxima of this function give the area between the lobes, while the zero crossings give the primary points of intersection between the manifolds. The distance in the direction normal to the original separatrix, increases as the X-point is approached $\hat{n} \cdot \delta \vec{x} = M/|\nabla \psi_0|$, but in order to preserve the area between the lobes, the distance between crossings decreases proportionately. Note that these distances are linear in the perturbation field.

The accessible stochastic region is asymmetric with respect to the separatrix: it is thicker on the interior than the exterior. The Melnikov layer, $M \sim 2\pi b_{m=qn} \sim 1\%$, is only 4 mm on the outer midplane, but due to the expansion of the unperturbed flux near the X-point, it creates a 2 cm footprint on the divertor floor. It is much thinner than the stochastic layer predicted by island overlap $h_{st} \sim 5\%$, and the ratio is

$$\delta h/h_{st} = \pi/8q*n \sim 1/5 . \quad (13)$$

Thus, as particles move along field lines, they leave the relatively wide stochastic layer, mix into the relatively thin homoclinic tangle, and eventually strike the divertor target. Upon reflection/re-injection through recycling processes they travel in the opposite direction, sampling the entire region between the two upper invariant manifolds. Just outside of the homoclinic tangle, field lines cannot mix with the interior, except through a perpendicular transport mechanisms such as collisions, cross-field convection, or neutral transport. Thus, the outer envelope of the tangle provides a precise definition of the inner boundary of the laminar scrape off layer (SOL). In the SOL, field lines do not close on themselves, and thus, a straight field line coordinate system can be found. One expects exponential decay in this region; e.g. for the collisional fluid regime, the SOL decay length should satisfy $\rho_{SOL}/L_c \sim \sqrt{D_{\perp}/D_{\parallel}}$. By similar reasoning, the original private flux region below the X-point is still magnetically well isolated, and will still have a rapid decay length due to the small connection length in this region. To verify this picture, in Fig. 8 we compare the electron temperature calculated by E3D with the invariant manifolds that enter/exit the X-point for the mapping that defines the E3D coordinate system. Strong correlation is found between the invariant manifold structure and the contours of constant temperature.

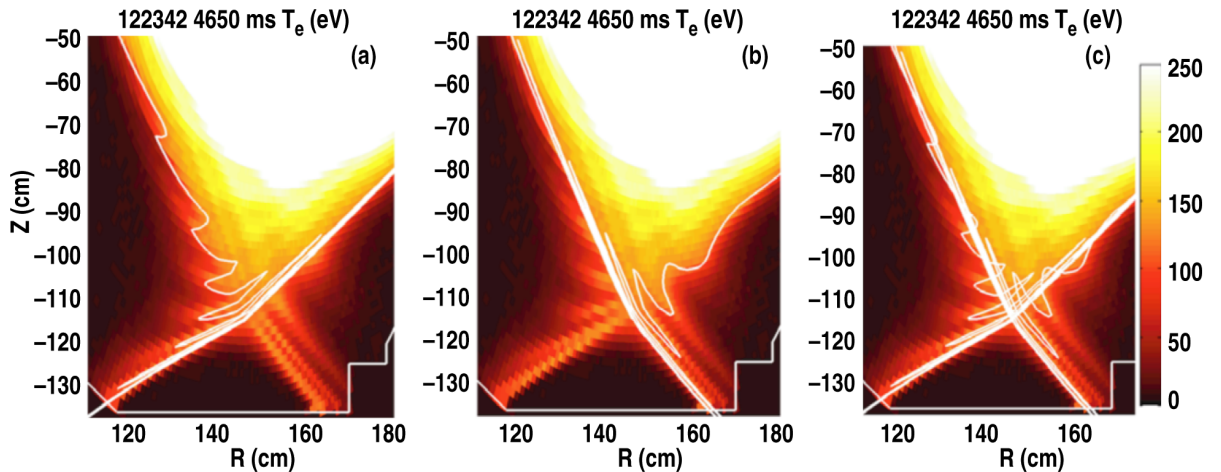


Fig. 8. The simulated electron temperature on the 0° toroidal plane demonstrates that heat flux is efficiently guided along the invariant manifolds of the magnetic field lines that connect to the X-point: (a) forward stable manifold, (b) forward unstable manifold, (c) the homoclinic tangle.

Note that if there is not enough input power into the stochastic layer, it could reach temperatures below ionization threshold, and retain only an exponentially small fraction of plasma. In this case, the plasma edge will be defined by the last dominant tangle of island chains above ionization threshold. Such behavior is commonly predicted and observed in limiter configurations such as TEXTOR [19,40]; however, in the diverted system, the homoclinic tangle still defines an outer boundary that geometrically confines the invariant manifolds of the island chain within. In this case, the heteroclinic intersection [38] of the invariant manifolds of the island chain and the remnant of the poloidal separatrix defines the chaotic web in which trajectories wander out to the divertor.

3.2. MAGNETIC FOOTPRINTS

During $n = 3$ even parity I-coil operation, both the inner and outer strike point (ISP/OSP) particle flux has been observed to split into multiple striations. For example, images of D_{α} -filtered recycling emission shown in Fig. 9(a) for shot 123301 clearly displays three striations, and this is also commonly observed in both CII and CIII filtered light. The detailed structure of the OSP has also been measured by slowly sweeping the OSP over a newly upgraded high-resolution Langmuir probe array (LPA) at the $\phi = 180$ deg toroidal location. Multiple peaks have been observed in the radial profiles of floating potential [41]. The distribution of field lines that are initialized on unperturbed flux surfaces inside the unperturbed separatrix as they first strike the divertor target is shown in Fig. 9(b) as calculated for shot 123301 including all RMP sources: I-coil, C-coil, and field-errors. In good agreement with observations, TRIP3D predicts that there should be three striations within the view of the tangential X-point TV, 120–240 deg. However, since the C-coil and field errors introduce significant $n = 1$ variations in the magnetic footprint, the IR camera view at 60 deg only observed a single striation, in agreement with the TRIP3D prediction. This result demonstrates the necessity of multiple measurements at different toroidal locations to verify that the observed structure is non-axisymmetric and has the predicted phase structure. In turn, the ability to take enough high-resolution measurements would allow one to use the detailed strike point structure as a sensitive new probe of the magnetic fields at the plasma edge.

The simulated thermal footprints for shot 122342 with 5 MW of input power and 3 kA-t of I-coil perturbation current (no C-coil or field errors) are shown in Fig. 10(a),(b). The $n = 3$ symmetry of the I-coil perturbations is apparent in the magnetic footprint structure. Because of the neglect of particle conservation, neutrals, and radiation, the computed heat fluxes are higher than expected for realistic conditions; the scales must be interpreted in light of the somewhat unphysical conditions of this numerical experiment. Although there was twice as much power injected into the ions 3.33 MW vs 1.67 MW, in both axisymmetric and perturbed cases, the heat flux to the divertor is more equally balanced between ions, 3 MW, and electrons, 2 MW, due to the collisional exchange of thermal energy. Since field lines that strike the inner divertor target are compressed to a smaller area, the heat flux is asymmetrically high even though only about 35% of the flux is channeled through the ISP

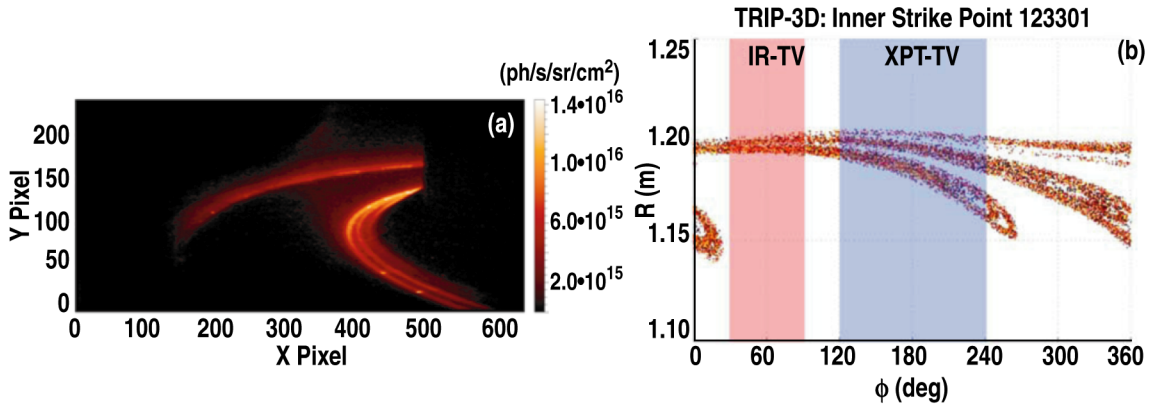


Fig. 9. (a) Tangential X-point TV image of filtered D_{α} light displays three striations along the inner strike point during I-coil operation (3 kA-t) in plasma discharge 123301. (b) The calculated first passage distribution of magnetic field lines as they strike the inner divertor target contains significant $n = 1$ and $n = 3$ components. The calculation includes C-coil, I-coil, and field errors. Shaded regions cover the approximate field of view of the current infrared camera centered on 60° (red) and the tangential X-point camera centered on 180° (blue).

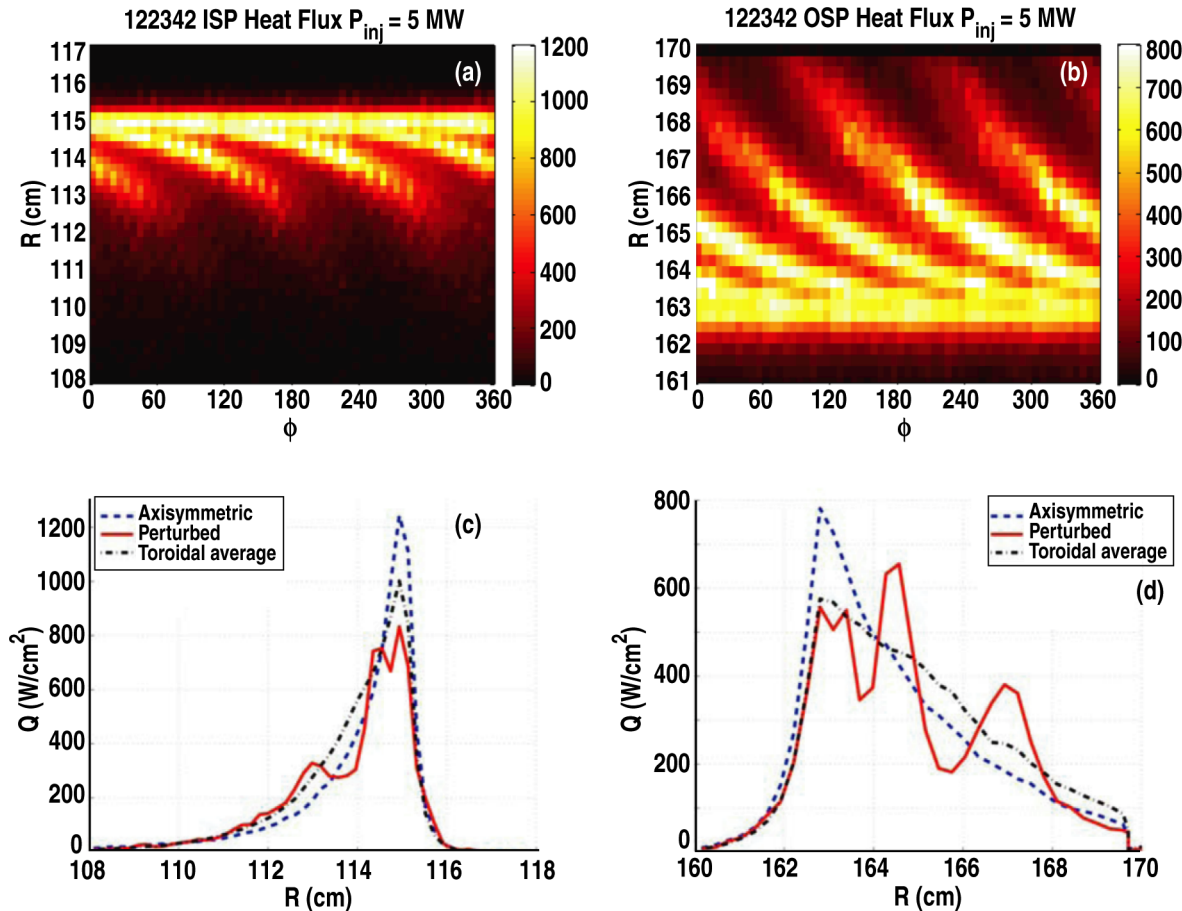


Fig. 10. Simulated heat flux deposition through the (a) inner and (b) outer strike points (ISP/OSP) due to the I-coil alone (3 kA-t). The peak of the heat flux near 180° (red —) for both (c) ISP and (d) OSP is reduced as compared to the axisymmetric case (blue --). The toroidal average of the perturbed profiles (black -.-) are wider than the axisymmetric cases indicating increased effective strike-point area.

both with and without RMP. Producing the correct inner/outer strike point asymmetry will eventually require drift physics and, perhaps, poloidal variation in the perpendicular transport coefficients. In fact, the ISP in DIII-D is typically detached, but during low-collisionality I-coil operation, the inner leg typically reattaches and delivers similar order of magnitude peak heat fluxes to the outer leg [42] as measured by infrared cameras.

In the simulation, the peak heat flux of the toroidally averaged profiles is reduced by 17% for the ISP and 25% for the OSP. The toroidally averaged profiles of heat flux were fitted to the approximate exponential form, $Q \sim Q_0 \exp(-\delta R/\rho)$, where δR is the radial distance from the separatrix. While the decay lengths are unchanged within the private flux region, $\rho_{ISP} \sim 0.35$ cm and $\rho_{OSP} \sim 0.57$ cm, on the scrape-off layer side, the decay length increases by 50% from 1.0 to 1.5 cm for the ISP and by 57% from 2.8 cm to 4.4 cm for the OSP. In fact, the toroidal average of the perturbed OSP profile appears to display an essentially linear, slower than exponential, decay.

Finally, a potential mechanism for enhanced convective transport is suggested by examining the heat flux sent directly to the entrance of the lower divertor cryopump. Simulated heat fluxes are delivered directly to the pump entrance at local levels of up to 10% of the peak value on the divertor. In addition, the mean position of the heat flux distribution, $\bar{R} = \int R \mathbf{q} \cdot d\mathbf{a} / P$, over the OSP is moved 0.4 cm toward the pump entrance relative to the axisymmetric case. This average movement of plasma toward the pump may increase the probability that a neutral will reach the opening. This could increase pumping efficiency and, thus, decrease the effective recycling of particles back into the bulk plasma.

4. CONCLUSIONS

In summary, we have calculated the non-axisymmetric distribution of heat flux to the DIII-D divertor under perturbation by the I-coil. The pattern is largely determined by the structure of the homoclinic tangle of invariant manifolds that guides field lines to the divertor target. The width of the magnetic footprint, the distribution of field lines escaping from the plasma region, can be thought of as the width of the effective separatrix. As the effective area for heat transport increases, the magnitude of the peak heat flux is reduced. The toroidal average of the perturbed profile decays slower than exponentially on the divertor target and indicates the increased efficiency with which heat flux is spread over the target. This also suggests that a linear decay of a “toroidally symmetric” strike point profile can potentially indicate toroidally rotating internal modes that produce an edge layer of stochastic field lines. The experimental observation of strike point splitting in particle flux appears to imply that the edge magnetic field has become stochastic enough to generate a homoclinic tangle. In addition, these observations coincide with changes to the pressure profile that are only produced during resonant perturbations. For instance, when magnetic perturbations with equivalent nonresonant $\delta b_{mn}/B$, but much weaker resonant terms are applied [8], proportionally smaller strike point splitting is predicted.

Paradoxically, the observed change in the electron temperature profile does not agree with the weakly stochastic fluid simulations presented here. Theoretical analysis and experimental results in L-mode and Ohmic plasmas [41,43-44] have consistently identified electron thermal conduction as the dominant transport mechanism. We have shown that H-mode plasma parameters are collisionless even in the presence of weak stochasticity, and transport simulations at these densities will typically require kinetic treatment for accuracy when extended into regions with \sim keV temperatures. However, the collisionless quasi-linear estimates for parallel electron transport are too large by an order of magnitude at the top of the pedestal, and two orders of magnitude too large in the steep gradient region [16].

In previous DIII-D RMP experiments, the largest factor in the reduction in pedestal pressure gradient was a drop in density due to increased particle transport [15-16]. Direct evidence for a factor of two reduction in the effective particle confinement time has been obtained by comparing pellet injection experiments in discharges with and without the RMP [45]. Ambipolar outflow aligned with the stochastic magnetic field should slow the net particle loss rate to that of the more massive ions [46-47]. The collisionless quasi-linear estimate for ion diffusivity in Section 2.5 does have the correct order of magnitude to explain the observed reduction in particle confinement; but this explanation requires a mechanism to shut off thermal transport, such as the extreme kinetic flux limits proposed in Ref. [47]. Many other explanations of particle transport have been proposed including: enhanced pumping efficiency (Section 3.2), enhanced neoclassical ion losses (Ref. [30]), static cross-

field $\vec{E} \times \vec{B}$ convection cells (cf. the single fluid MHD model in Ref. [48]), and broadband dynamic turbulence (observed experimentally in Ref. [49]).

Thus, it appears that the experimental results are inconsistent with a computational model of stochastic transport as well as quasi-linear estimates of thermal transport. It seems inevitable that another mechanism such as kinetic flux limits (cf. Ref. [47]) or the shielding of resonant perturbations by plasma rotation (cf. Ref. [30]) must play an important role in limiting stochastic transport. Because of the extreme sensitivity of the transport to the resonant perturbation strength, it is critical to understand the response of the plasma to the applied perturbations in order to predict the location and width of the resonant layer.

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