

# **Electron Transfer at the Cytochrome / Mineral Interface:**

## **An Overview of the EMSL BGC Modeling Component**

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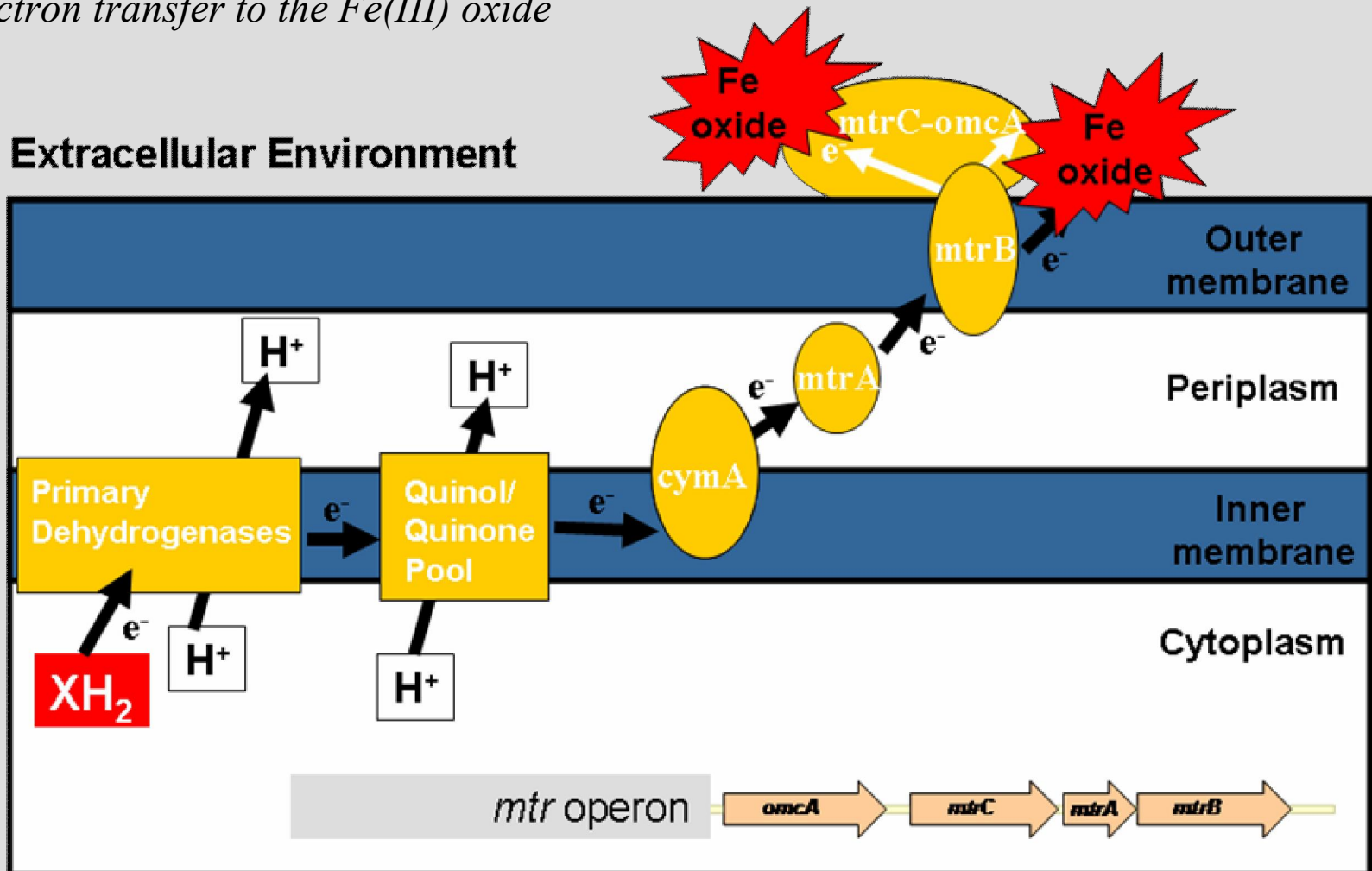
*Pacific Northwest National Laboratory*

**ERSD PI Meeting – April 2006**

Acknowledgements: US-DOE-OBBER-ERSD-EMSL  
EMSL Molecular Sciences Computing Facility  
EMSL NWChem Project

# Current Conceptual Model for Electron Transfer to Extracellular Substrates in *Shewanella*

*BGC Hypothesis: Outer membrane cytochromes OmcA/MtrC are responsible for direct electron transfer to the Fe(III) oxide*

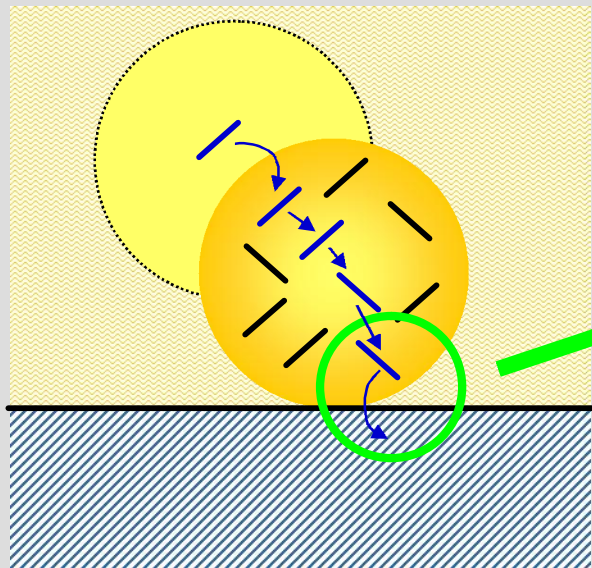


Courtesy - D. Richardson

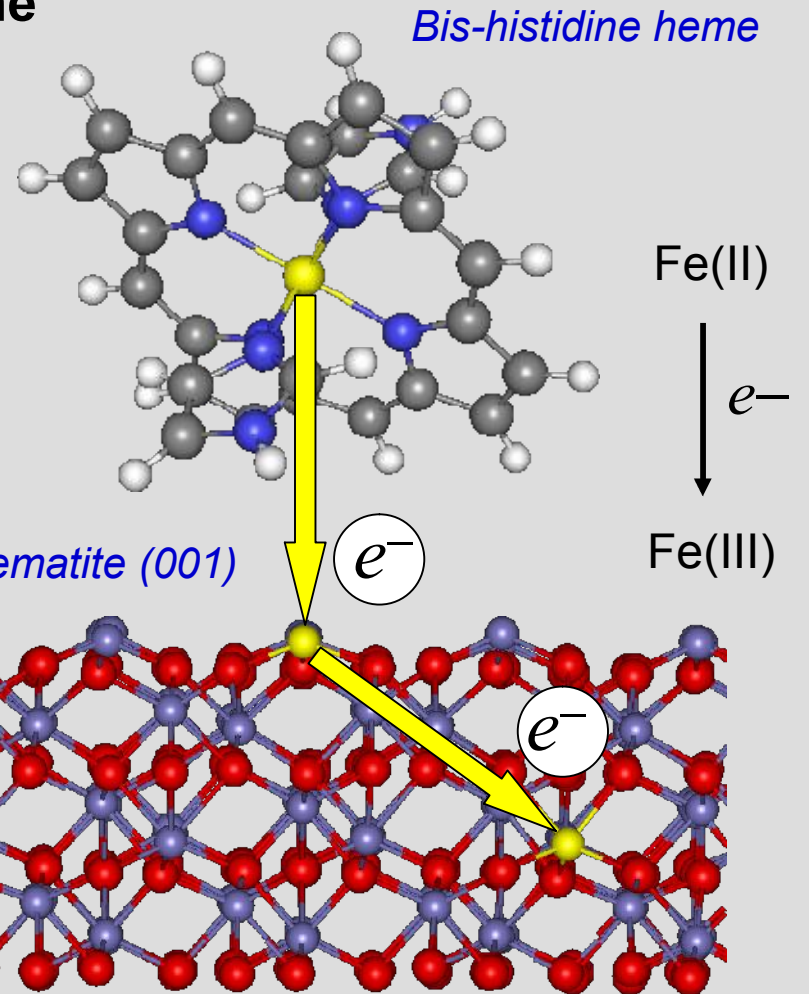
# Science Questions

What regulates the ET rate across the cytochrome/Fe(III)-oxide interface?

How are Fe(III) acceptor sites 'regenerated' and how fast?



*Fe-terminated hematite (001)*

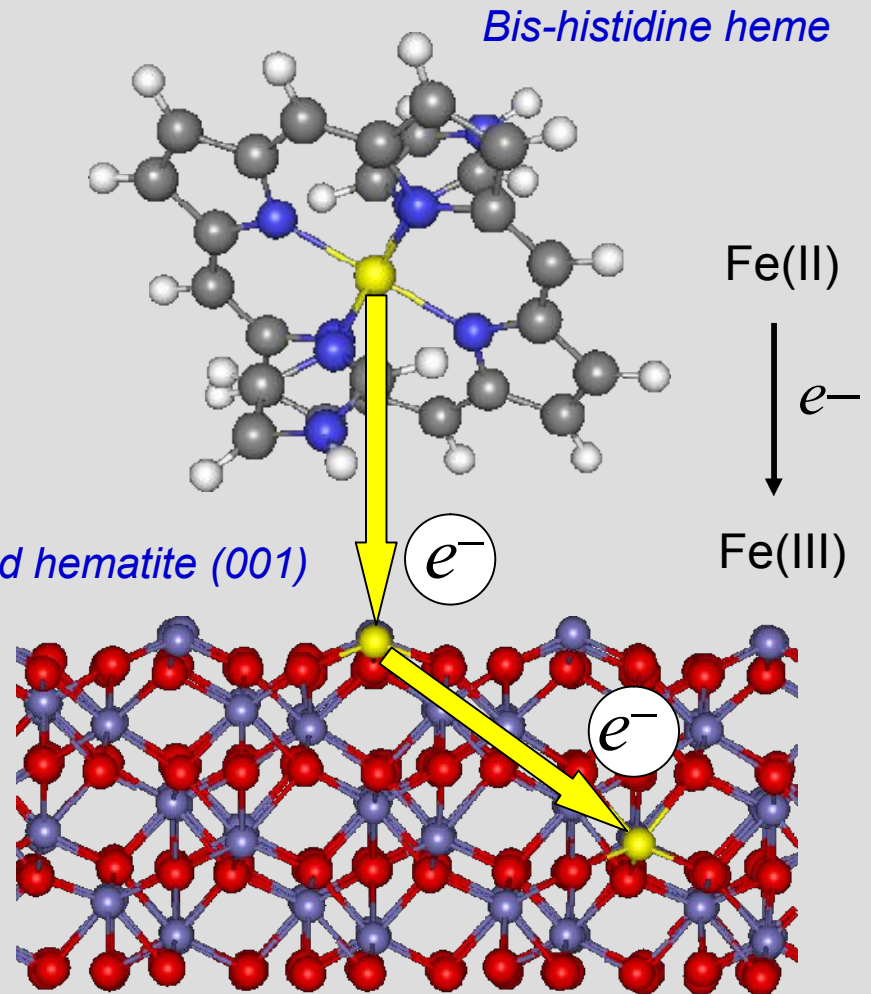


# Obstacles / Challenges

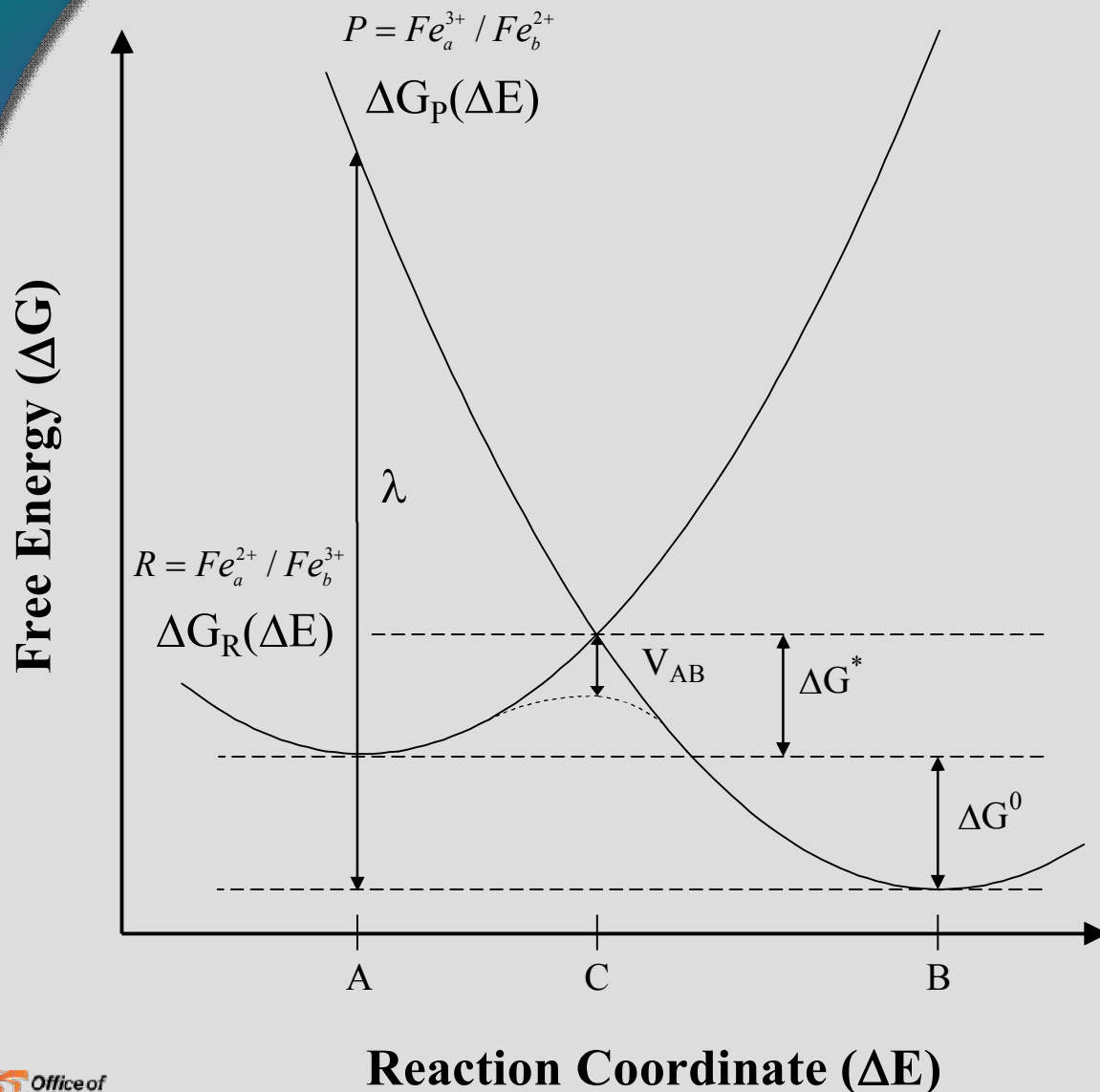
## Aspects influencing the ET kinetics at the molecular scale:

- electron transfer distance
- heme electronic structure
- axial ligand orientation
- heme orientation
- porphyrin distortion
- intervening / bridging molecules
- surface atomic structure
- surface electronic structure

- electron transfer distance
- crystallographic direction
- proximity to surface plane
- surface termination
- surface hydration
- defects



# Basic Electron Transfer Theory



$\Delta E$ : Reaction coordinate or energy gap

$$\Delta E = E_P - E_R$$

$\lambda$ : Reorganization energy

$V_{AB}$ : Electronic coupling

$\Delta G^*$ : Diabatic activation free energy

$\Delta G^0$ : Free energy of ET

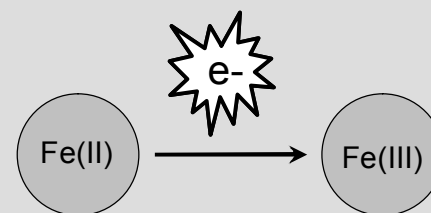
# Basic Electron Transfer Theory

ET rate = electronic part + nuclear part

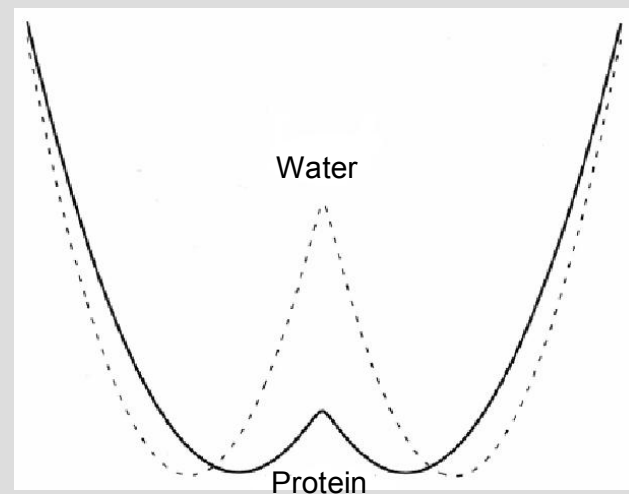
electronic

$$k_{et} = \frac{2\pi}{\hbar} V_{AB}^2 \frac{1}{\sqrt{4\pi\lambda k_B T}} \exp\left[-\frac{\Delta G^*}{k_B T}\right]$$

nuclear



Details of the molecular environment strongly influence the PES's and electronic coupling



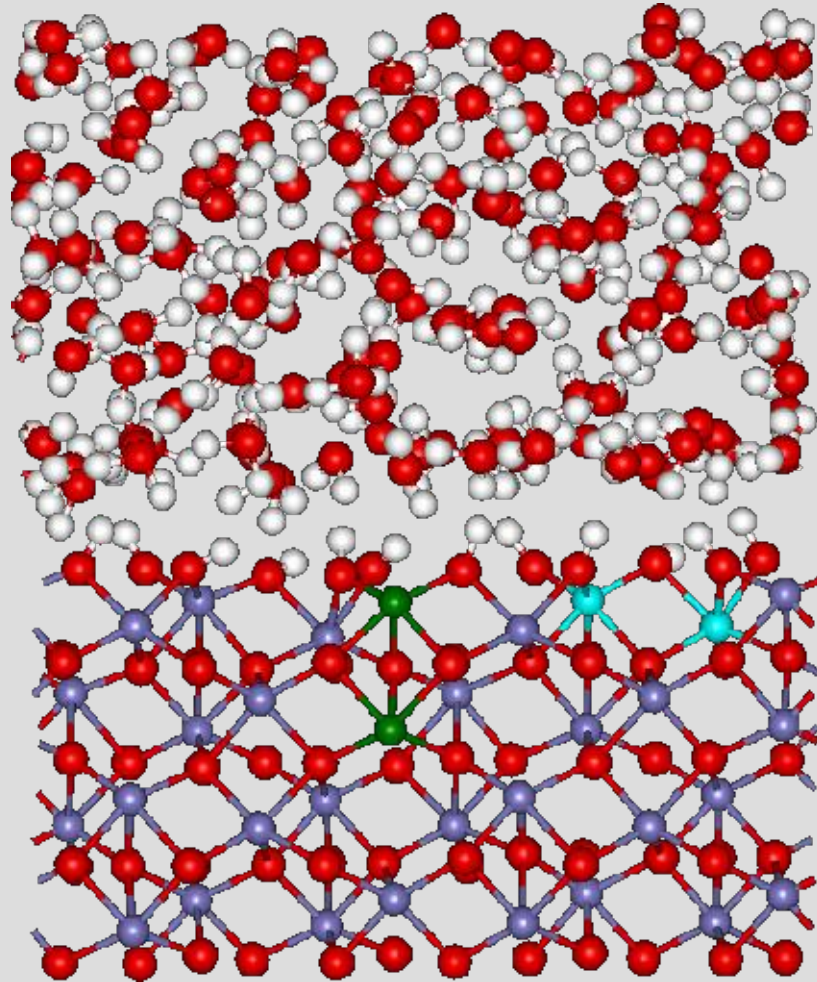


# Electron Migration at Hematite Surfaces

Hematite surfaces examined

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Fe-terminated (001)  
O(H)-terminated (001)  
(012)



Hydroxylated hematite (001)

# Approach to Model the Interatomic Interactions

The method is based on the **Born model of solids**.

$$V(r_{ij}) = \frac{q_i q_j}{r_{ij}} + \phi(r_{ij})$$

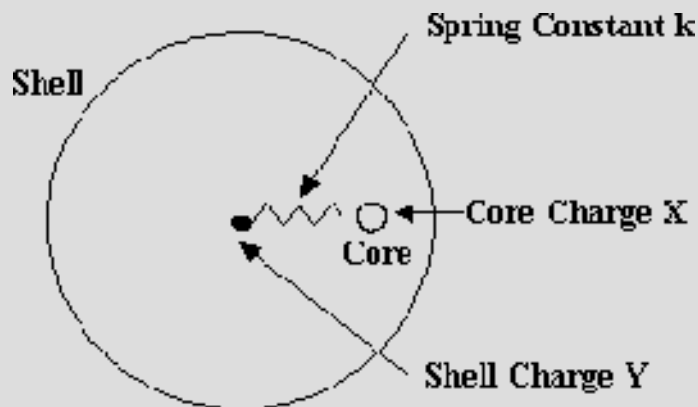
## 1<sup>st</sup> Term - Long range interactions

Coulombic energy

## 2<sup>nd</sup> Term - Short range interactions

Electron cloud repulsion,  
Van der Waals, bond stretch,  
angle bend, torsion...

## Shell Model<sup>1</sup>:



## Buckingham Potential:

$$\phi(r_{ij}) = A_{ij} * \exp\left(\frac{-r_{ij}}{\rho_{ij}}\right) - \frac{C_{ij}}{r_{ij}^6}$$

<sup>1</sup>Dick and Overhauser *Phys. Rev.*, 112, 90, 1958.



# Approach to Compute the PES's: MD + Umbrella Sampling

300 Kelvin  
 $\lambda_{\text{TOTAL}}$  is obtained directly

Run MD collecting configurations

$\Delta E$  is calculated for each configuration

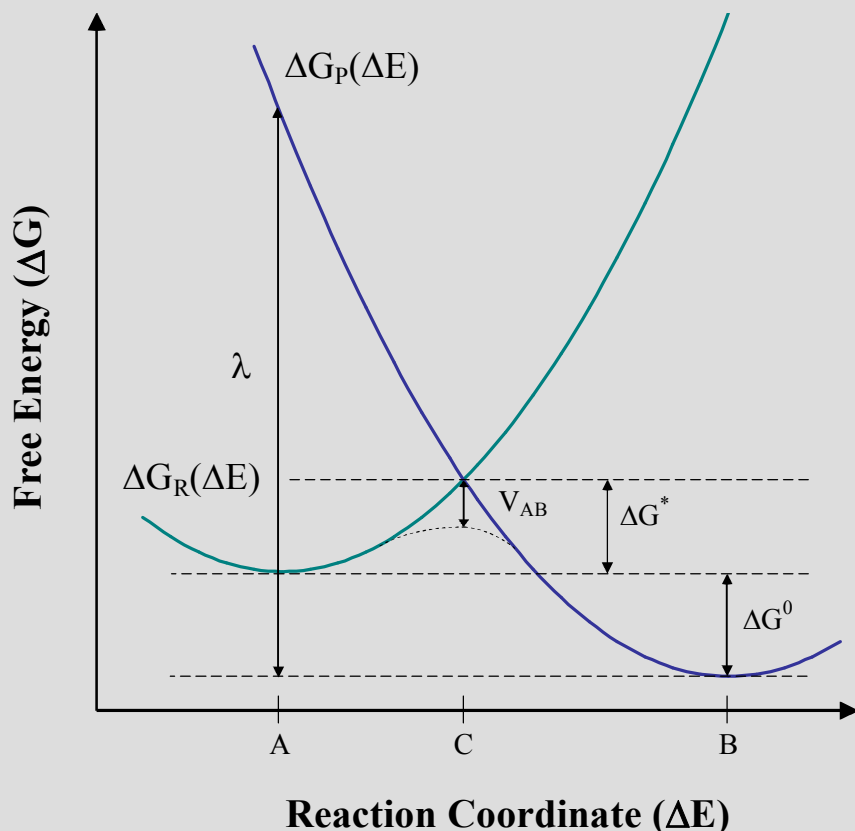
$$\Delta G(\Delta E) = -RT \ln \left[ \frac{P(\Delta E)}{P(\langle \Delta E \rangle)} \right]$$

As configurations with  $\Delta E \sim 0$  are rare, umbrella sampling technique is used to obtain a complete distribution.

$$V_{\theta} = \theta V_A + (1 - \theta) V_B$$

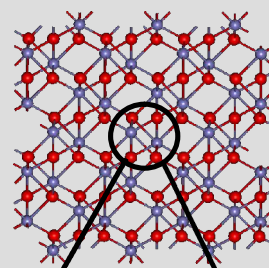
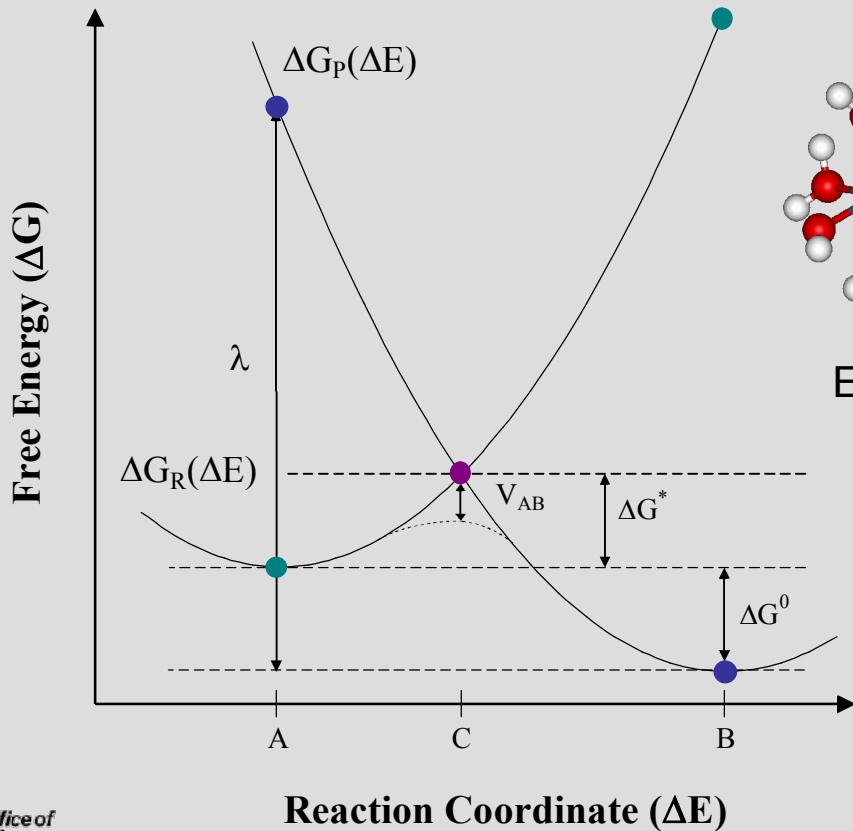
Calculations are carried out for several values of  $\theta$  (from 0 to 1).

Kerisit and Rosso, JCP, 123, 224712, 2005

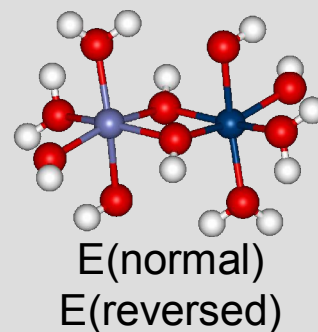
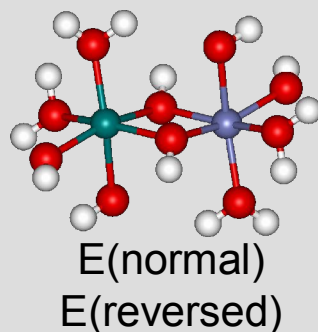


# Approach for Computing the Electronic Coupling

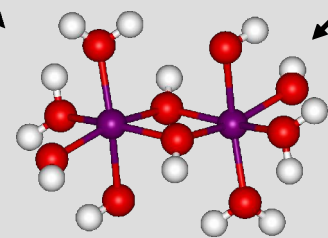
Zero Kelvin – without ZPE  
 $\lambda_I$  and  $\lambda_E$  obtained separately



Minimize reactant and product configurations



$$q = \theta q_A + (1 - \theta) q_B$$



# {01.2} Hematite Surface - Hydrated

Lower activation energy at the surface

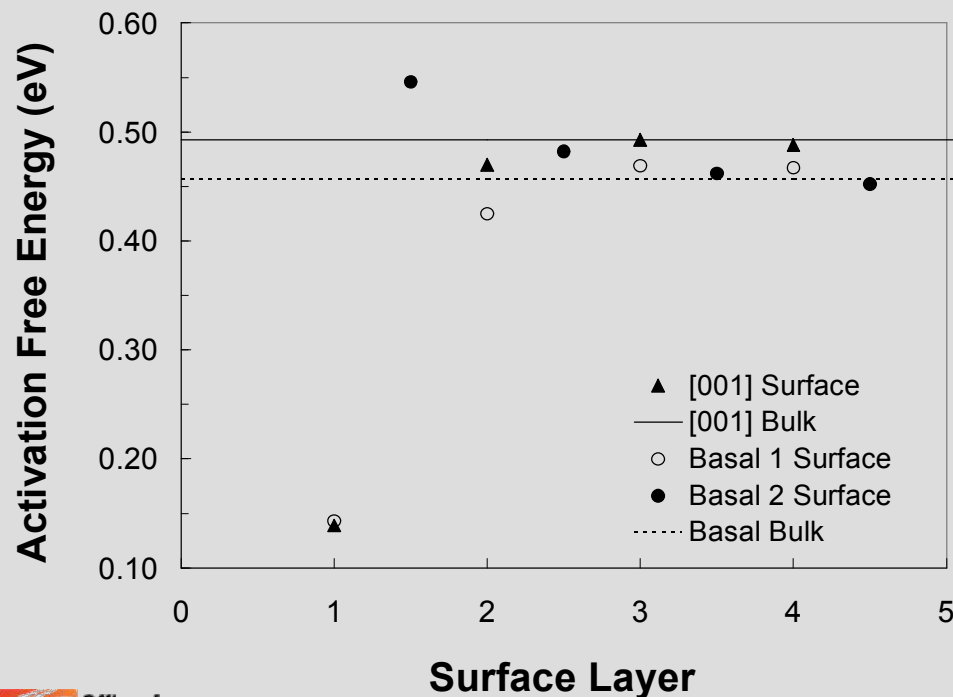
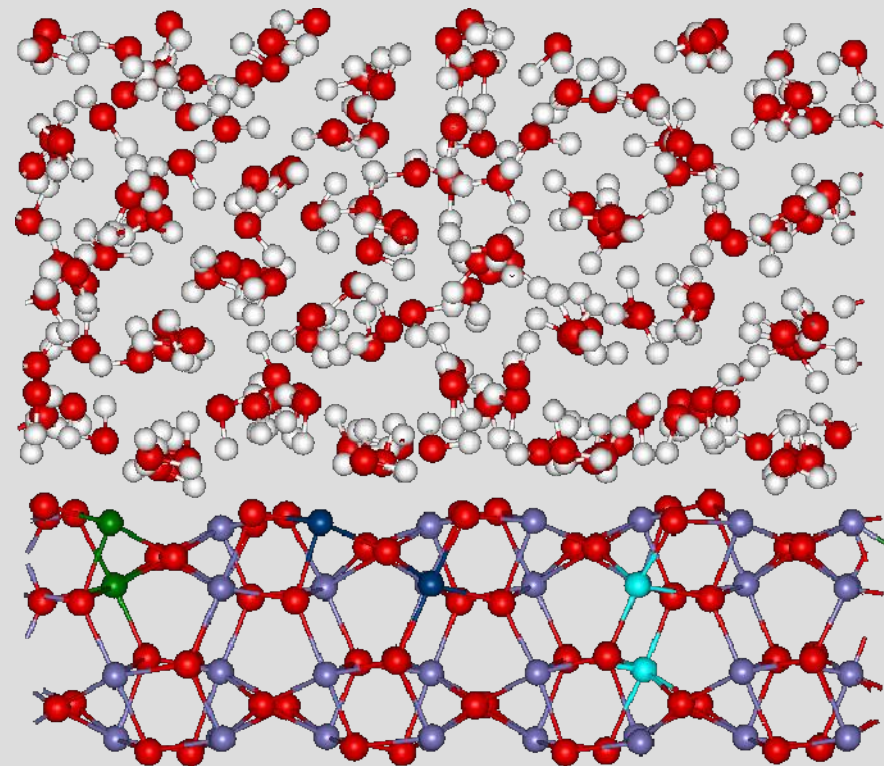
Great driving force at the surface

First interlayer transfer is uphill

Rapid convergence to bulk value

Water molecules: ~350

Water slab thickness: ~25 Å



# Electron Transfer at the {01.2} Hematite Surface

## LAYER 1

Direction	$\Delta G^0$ (eV)	$\Delta G^*$ (eV)	$V_{AB}$ (eV)	i	$k_{et}$ (s <sup>-1</sup> )
Basal 1	-1.04	0.14	0.031	2	4.9E+11
Basal 2	0.20	0.55	0.184	1	1.5E+07
Basal (bulk)	0.00	0.46	0.184	3	1.5E+09
C direction	-1.07	0.14	0.028	1	2.5E+11
C dir. (bulk)	0.00	0.49	0.028	1	6.6E+07

# Summary of Hematite Surface Results

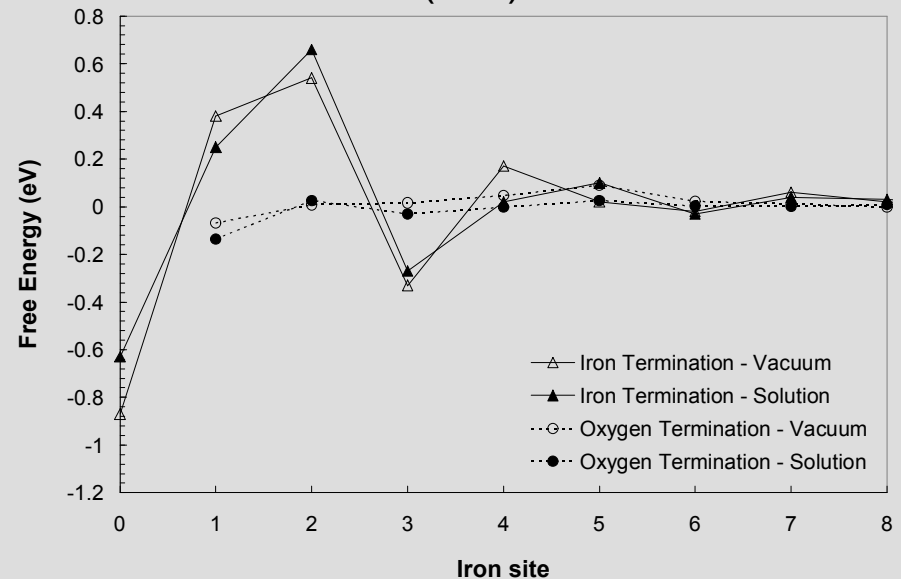
Water significantly affects the free energy when in direct contact with Fe(III) electron transfer centers and is able to form a short bond with the surface (e.g. (012) surface).

Different surfaces exhibit different behaviors due to different orientations.

Surface termination affects electron transfer some distance down into the surface.

Undercoordinated terminal iron atoms can act as electron traps at the surface.

(001) Hematite Surface



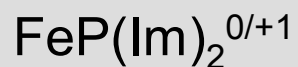
Electrons migrate through the surface of hematite no slower than  $10^7 \text{ s}^{-1}$ .

The details of the mineral surface structure are critical for controlling the electron migration rate

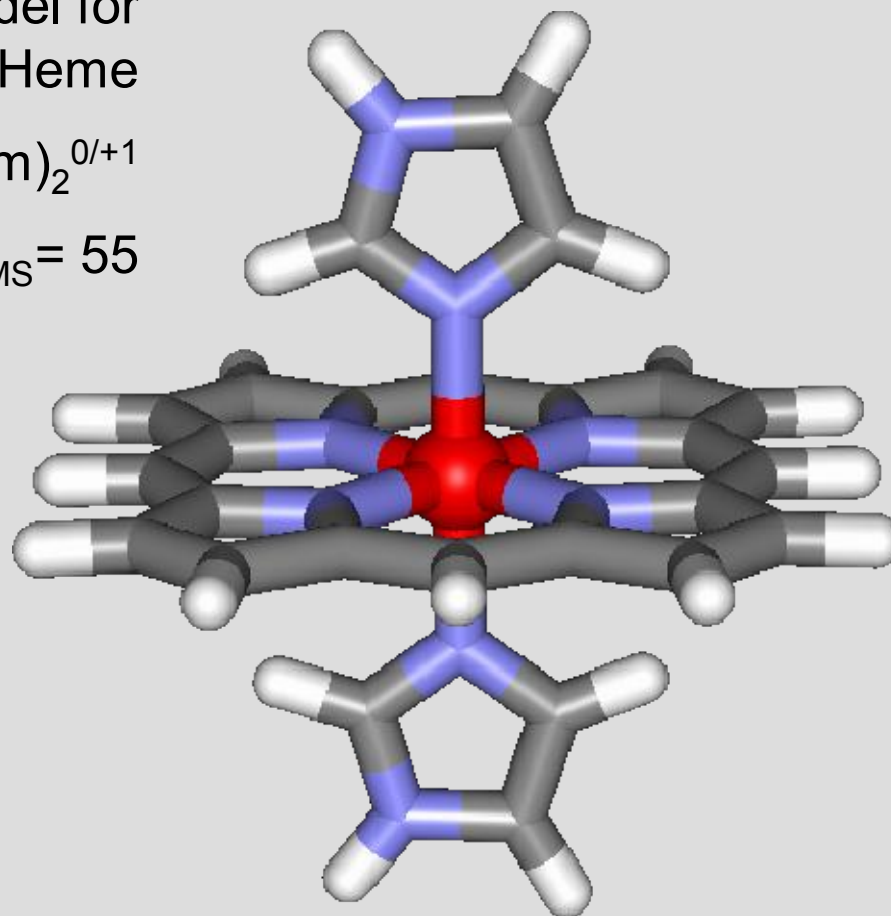


# Heme / Hematite Electron Transfer

Cluster model for  
Bis(histidine) Heme



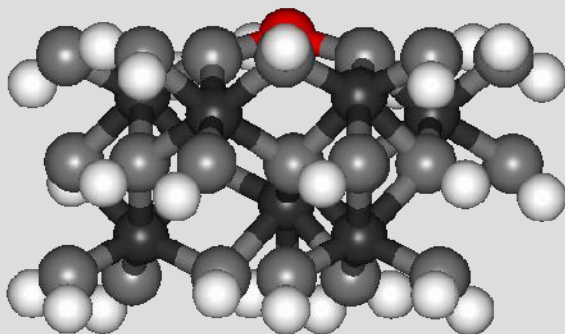
$$N_{\text{ATOMS}} = 55$$



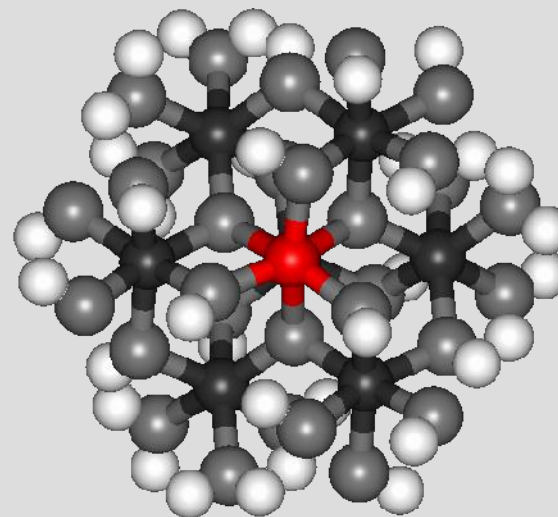
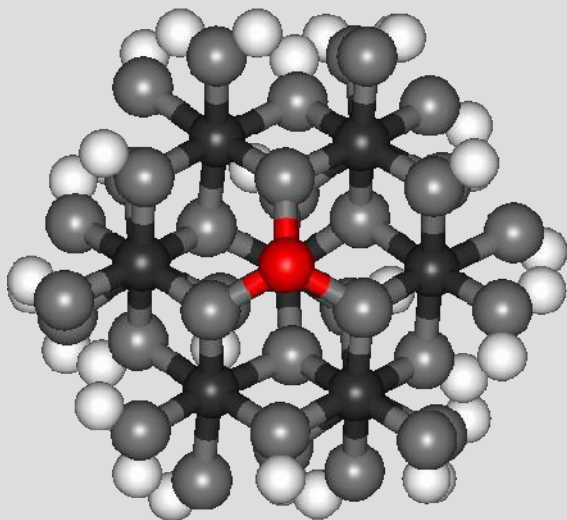
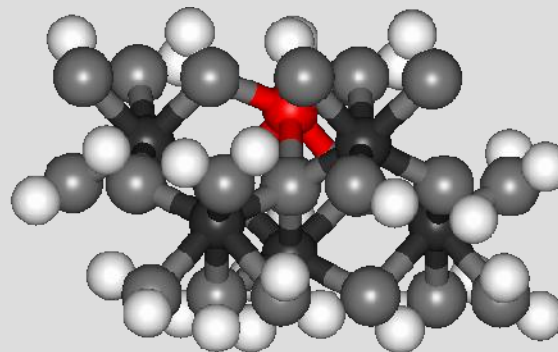
# Heme / Hematite Electron Transfer

Hematite surface cluster models:

Iron Termination:  $[\text{Fe}_{11}\text{O}_{33}\text{H}_{33}]^{0/-1}$

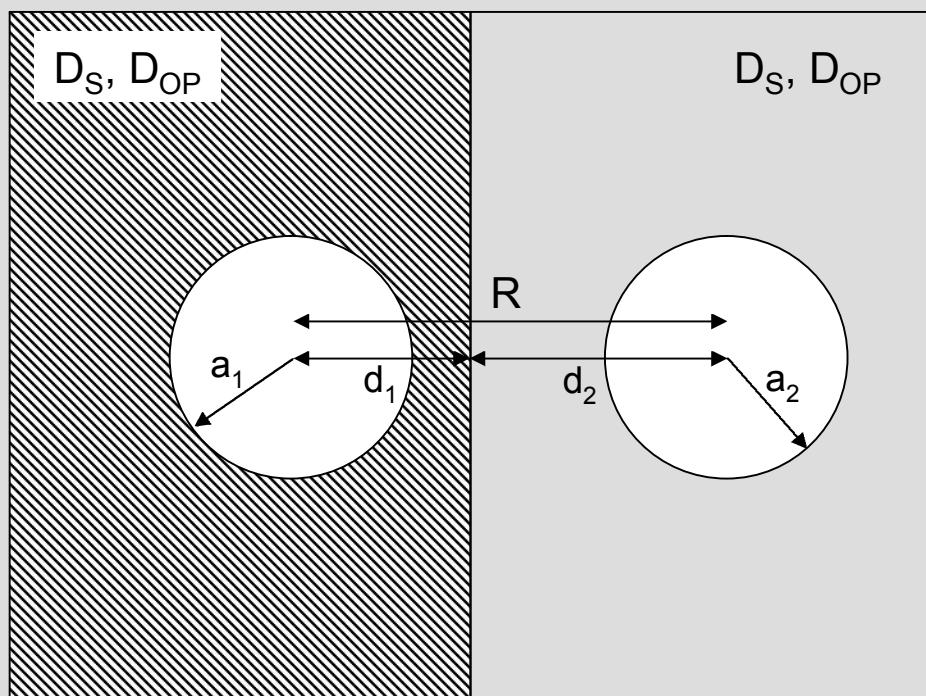


Hydroxyl Termination:  $[\text{Fe}_8\text{O}_{30}\text{H}_{36}]^{0/-1}$



# Heme / Hematite Electron Transfer

Need a simple approach to simulate the repolarization behavior of the surrounding protein and mineral at the interface:



$$\lambda_{TOT.} = \lambda_{INT.} + \lambda_{EXT.}$$

## External Part: Continuum Model

Marcus' equation for ET across interfaces\*

$$\lambda_{EXT.} = 0.46-0.71 \text{ eV (7-14 \AA range)}$$

$$\lambda_{TOT.} = 1.91-2.16 \text{ eV}$$

\* Marcus JPC (1990)

# Heme / Hematite Electron Transfer

Estimation of the Free Energy of Electron Transfer:

**Heme operation potentials of OmcA from *S. Oneidensis***

-66 mV, -149 mV, -212 mV in 3:3:4 heme ratio

(B.J.N. Jepson et al.)

**Flat band potential of hematite anodes in 2 M NaOH solution**

-426 mV v NHE at pH 13.6

(Quinn et al. J. Mater. Res. Bull. 11, 1011-1017, 1976)

**“59 mV per unit pH change”**

(J.K. Leland and A.J. Bard J. Phys. Chem. 91, 5076-5083, 1987)

**pH of point of zero charge of hematite ~ 8**

(L. Cromieres et al. Colloids Surfaces A: Physicochem. Eng. Aspects 202, 101-115, 2002)

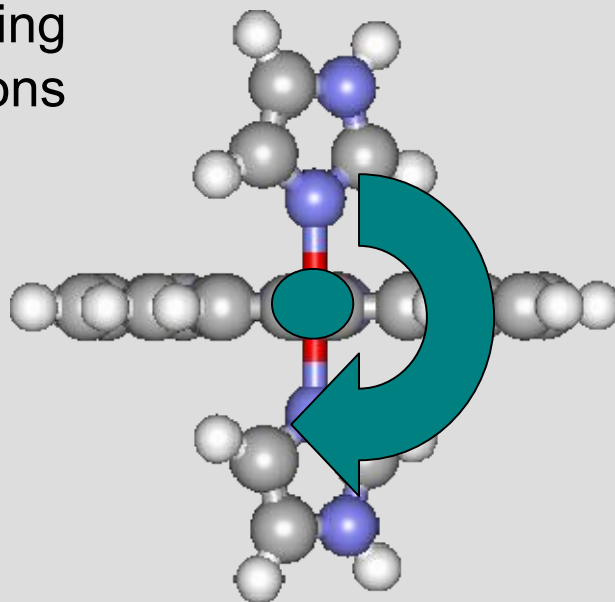
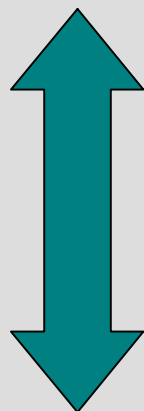
**Hematite redox potential v NHE at  $\text{pH}_{\text{PZC}} = -95 \text{ mV}$**

Free Energy of ET (Heme=>Hematite)	
Heme Potential (mV)	$\Delta G^0$ (mV)
-66	29
-149	-54
-212	-117

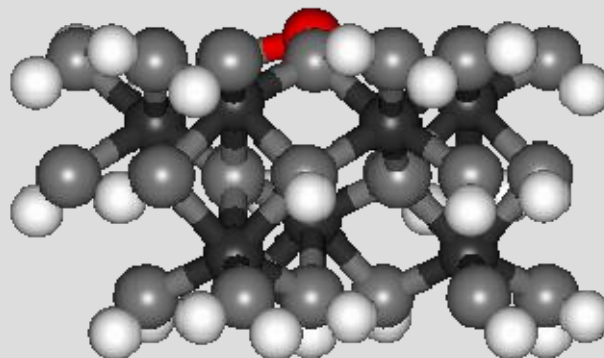
# Heme / Hematite Electron Transfer

Electronic coupling  
calculations

7 to 14 Å



0, 45 and 90°

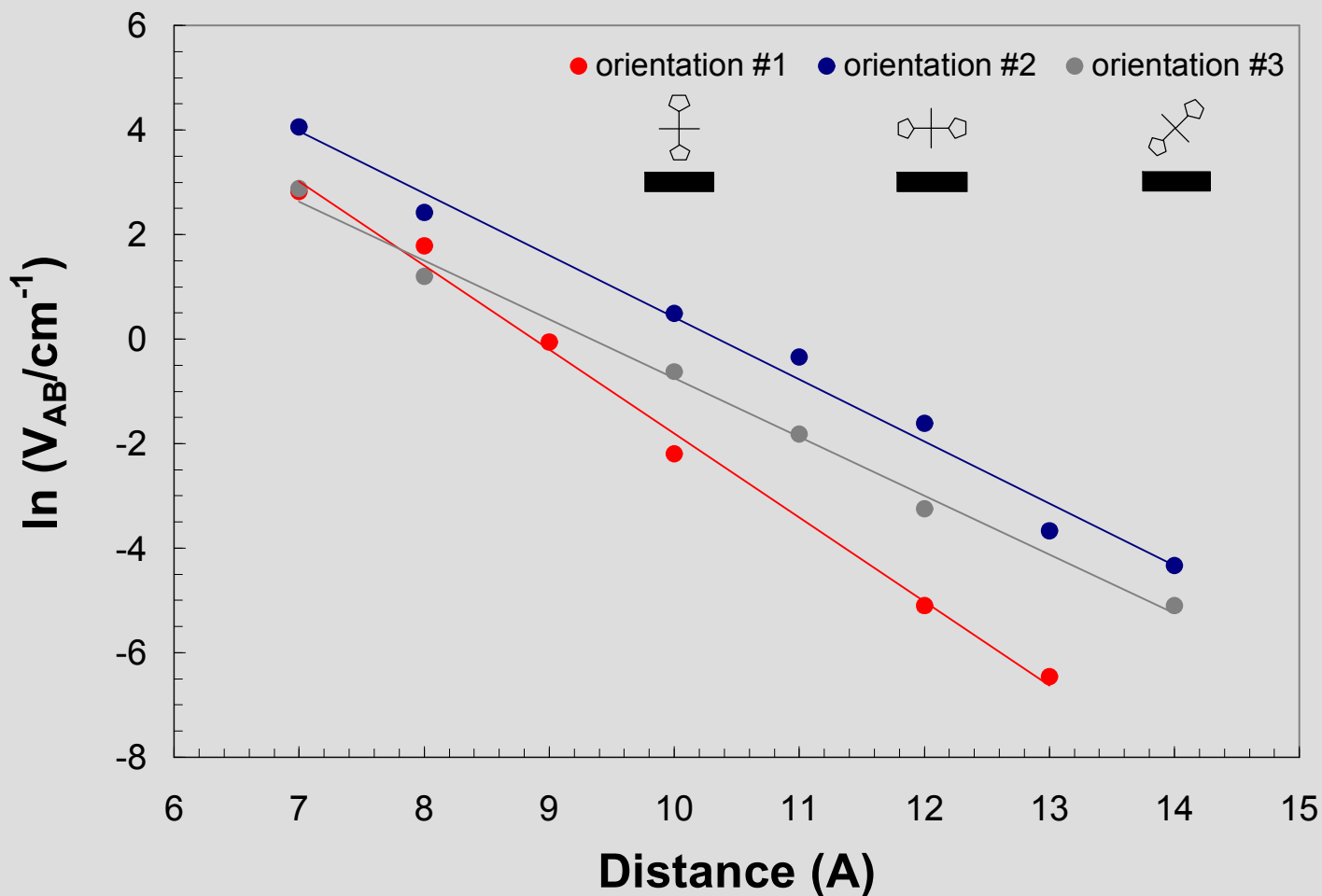


NWChem  
Unrestricted Hartree-  
Fock Level  
Fe Ahlrichs VTZ  
C,O,N,H 6-31G\*  
 $N_{\text{ATOMS}} = 129$  or  $132$



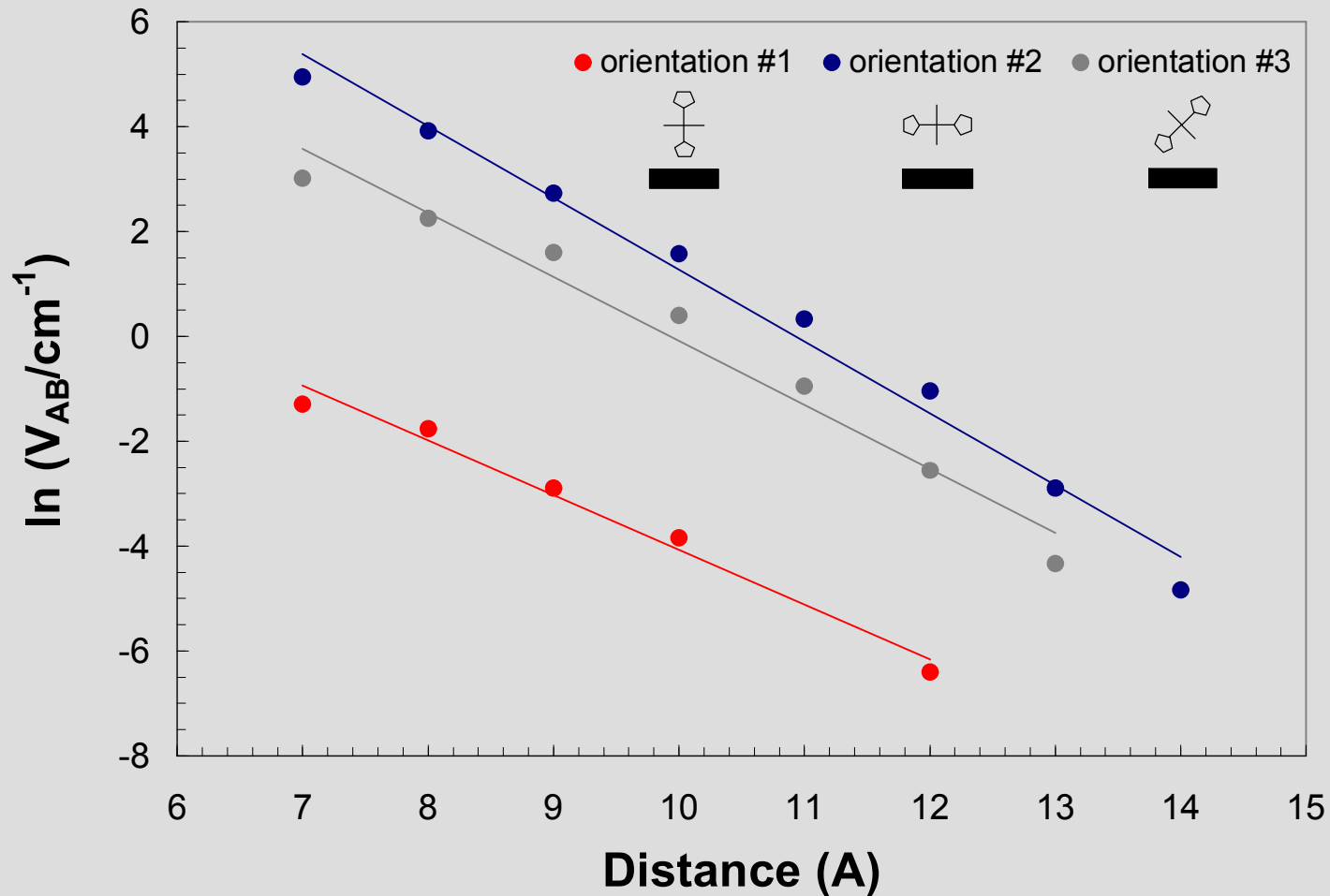
# Heme / Hematite Electron Transfer

Hydroxylated hematite (001)



# Heme / Hematite Electron Transfer

Fe-terminated hematite (001)



# Heme / Hematite Electron Transfer

$$k_{ET} = \frac{2\pi}{\hbar} |V_{AB}|^2 \frac{1}{\sqrt{4\pi\lambda k_B T}} \exp\left\{-\frac{(\Delta G^0 + \lambda)^2}{4\lambda k_B T}\right\}$$

Rate (s<sup>-1</sup>) for  $\Delta G^0 = -54$  mV

Hematite (001) surface

Distance	Hydroxyl Termination			Iron Termination		
	1	2	3	1	2	3
7	1.5E+03	1.8E+04	1.7E+03	4.0E-01	<b>1.0E+05</b>	2.2E+03
8	9.8E+01	3.5E+02	3.1E+01	8.1E-02	<b>7.0E+03</b>	2.5E+02
9	1.5E+00	1.3E+01	7.6E-01	5.1E-03	<b>4.0E+02</b>	4.1E+01
10	1.4E-02	3.1E+00	3.3E-01	5.3E-04	<b>2.7E+01</b>	2.6E+00
11	-	4.3E-01	2.3E-02	-	<b>1.7E+00</b>	1.3E-01

# Heme / Hematite Summary

Electronic coupling is weak except at very short distances.

Electron transfer is fastest when the edge of the porphyrin ring is orientated towards the surface.

The electron transfer rate decays an order of magnitude with every Å increase in distance.

Surface termination affects the rate: for most orientations, electron transfer is faster for Fe-termination.

Delivery of electrons to the hematite surface is slower than electron migration through the surface.

More protein-specific information is needed to select conditions appropriate for comparison with experimental results.

# Current Directions – KMC Models

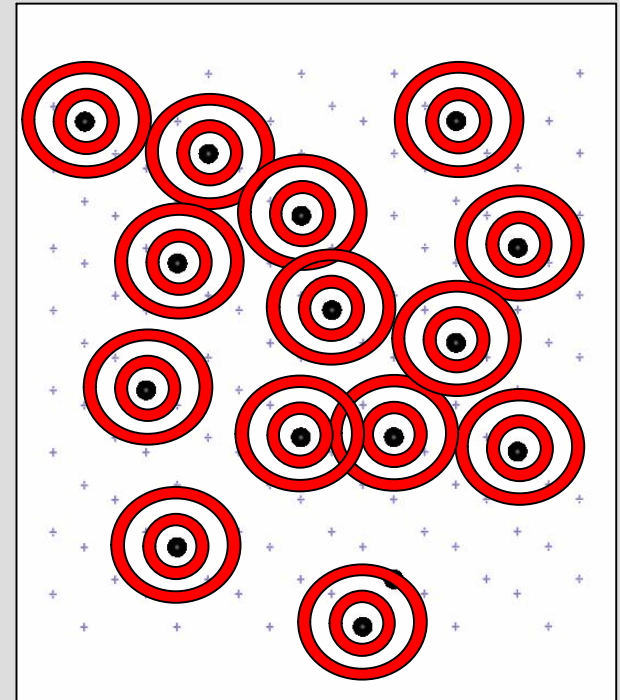
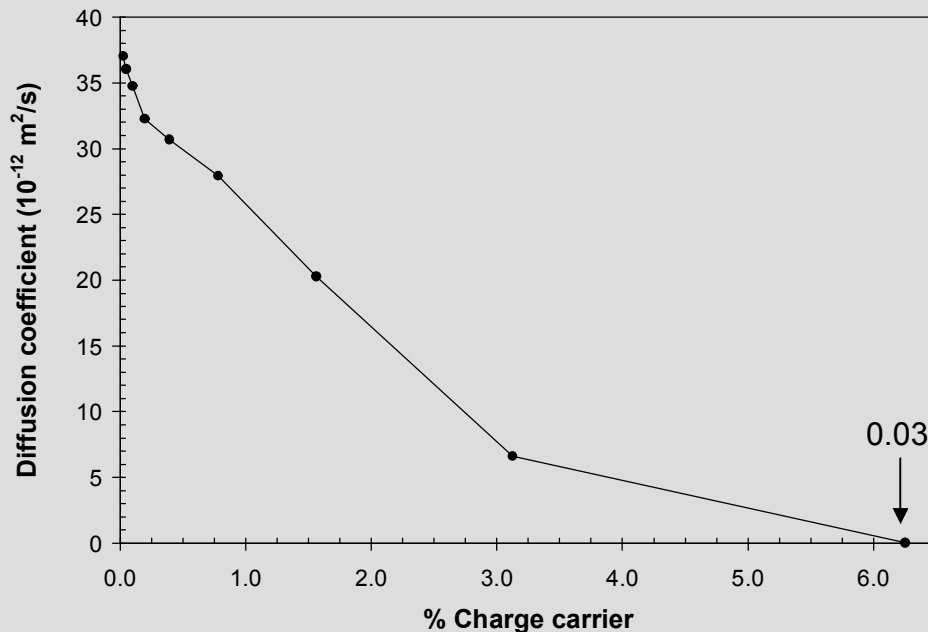
Effect of charge carrier concentration

1,000,000 KMC steps - 3D periodic boundary conditions

Temperature = 300 K

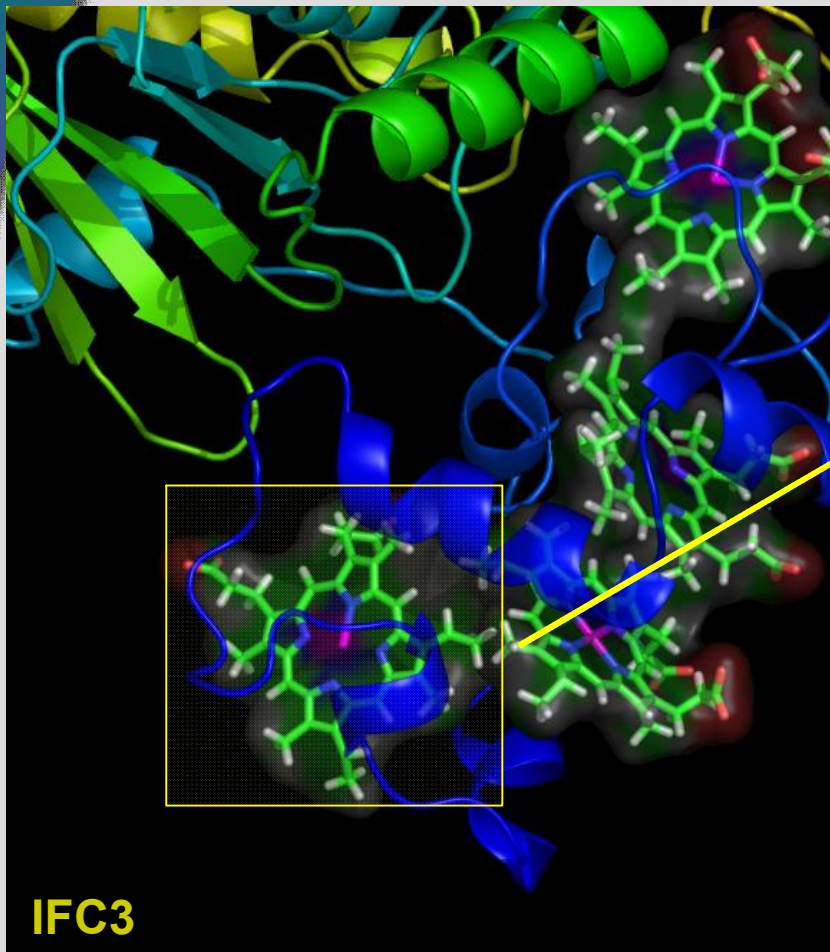
4096 iron sites: 1, 2, 4, 8, 16, 32, 64, 128 and 256 charge carriers

$$k_{et} = \nu_n \exp\left(-\frac{(\lambda + \Delta G^0)^2 / 4\lambda - V_{AB}}{k_B T}\right)$$

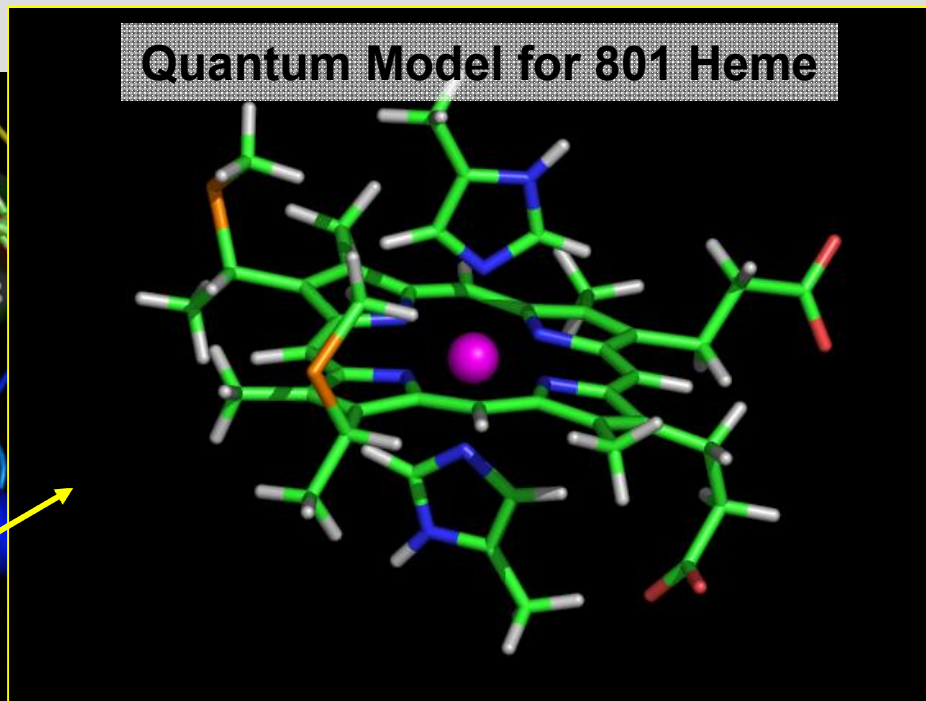




# Current Directions – Heme Environment



IFC3 – flavin domain → STC



- NWChem QM/MM module (M. Valiev)
- QM region - 109 atoms (DFT/B3LYP)
- MM region ~ 77000 atoms
- Separate calculation for each of four hemes
- Structural and electronic properties
- Redox potentials
- IR spectra, ....