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QUANTUM-BASED ATOMISTIC SIMULATION OF TRANSITION METALS

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Abstract. First-principles generalized pseudopotential theory (GPT) provides a fundamental basis for *transferable* multi-ion interatomic potentials in *d*-electron transition metals within density-functional quantum mechanics. In mid-period bcc metals, where multi-ion angular forces are important to structural properties, simplified *model* GPT or MGPT potentials have been developed based on canonical *d* bands to allow analytic forms and large-scale atomistic simulations. Robust, advanced-generation MGPT potentials have now been obtained for Ta and Mo and successfully applied to a wide range of structural, thermodynamic, defect and mechanical properties at both ambient and extreme conditions of pressure and temperature. Recent algorithm improvements have also led to a more general matrix representation of MGPT beyond canonical bands allowing increased accuracy and extension to *f*-electron actinide metals, an order of magnitude increase in computational speed, and the current development of temperature-dependent potentials.

Keywords: Atomistic simulation, MGPT potentials, tantalum, molybdenum, equation of state, strength
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INTRODUCTION

Accurate and predictive large-scale atomistic simulation of materials properties is a forefront challenge in condensed-matter physics. There currently exists a wide spectrum of atomic-scale calculational methods, extending from exact quantum-mechanical techniques to classical descriptions with totally empirical force laws. All of these methods fall into one of two distinct categories separated by a material-dependent gap. On one side of this gap are electronic-structure methods based on direct quantum-mechanical treatments. These include *quantum simulations* that attempt to treat electron and ion motion on an equal footing, solving on the fly for both the electronic states of the system and the forces on the individual ions. In transition metals, methods based on modern density-functional theory (DFT)

[1] can provide a highly accurate description of the system and are chemically very robust, but they come at the price of being severely limited in the size (≤ 1000 atoms) and duration (≤ 10 ps) of the simulation. On the other side of the gap are methods used in *atomistic simulations*, such as molecular dynamics (MD), that treat only the ion motion, allowing much larger ($\sim 10^8$ - 10^{10} atoms) and longer (~ 100 ns) simulations by solving classical Newtonian equations of motion with the forces derived from explicit interatomic potentials. Bridging the *electronic-atomistic gap* is possible through the development of first-principles *quantum-based potentials* based on a systematic coarse-graining of the DFT electronic structure. In this paper, we present an overview of recent work at LLNL on developing quantum-based interatomic potentials for transition metals from density-functional theory and widely applying these

potentials to the atomistic simulation of materials properties at both ambient and extreme conditions.

QUANTUM-BASED POTENTIALS

Within DFT quantum mechanics, first-principles generalized pseudopotential theory (GPT) provides a fundamental basis for *ab initio* interatomic potentials in transition metals [2]. In the GPT a mixed basis of plane waves and localized *d*-state orbitals is used to self-consistently expand the electron density and total energy of the system in terms of weak *sp* pseudopotential, *d-d* tight-binding, and *sp-d* hybridization matrix elements, which in turn are all directly calculable from first principles. For a bulk elemental metal, one obtains the real-space total-energy functional

$$E_{tot}(R_1 \dots R_N) = NE_{vol}(\Omega) + \frac{1}{2} \sum_{i,j} v_2(ij; \Omega) + \frac{1}{6} \sum_{i,j,k} v_3(ijk; \Omega) + \frac{1}{24} \sum_{i,j,k,l} v_4(ijkl; \Omega) \quad (1)$$

The leading volume term in this expansion, E_{vol} , as well as the two-, three-, and four-ion interatomic potentials, v_2 , v_3 and v_4 , are volume dependent, *but structure independent* quantities and thus *transferable* to arbitrary bulk ion configurations. The angular-force multi-ion potentials v_3 and v_4 reflect directional-bonding contributions from partially-filled *d* bands and are generally important

for the central transition metals. In the full *ab initio* GPT, however, these potentials are multidimensional functions, so that v_3 and v_4 cannot be readily tabulated for application purposes. This has led to the development of a simplified model GPT or MGPT, which achieves short-ranged, analytic potential forms that can be applied to large-scale atomistic simulations [3,4].

The MGPT is derived from the GPT through a series of systematic approximations applicable to mid-period transition metals. Canonical *d* bands are introduced to express the *d*-state components of v_2 and the multi-ion potentials v_3 and v_4 analytically in terms of a single radial function and three universal angular functions that depend only on *d* symmetry and apply to all transition metals and all volumes. To compensate for the approximations introduced into the MGPT, the *d*-state potential coefficients in v_2 , v_3 and v_4 together with E_{vol} are constrained by fundamental theoretical and/or experimental data. In our current preferred scheme, we fit a combination of first-principles DFT calculations and experimental data on the cold equation of state, shear elastic moduli, unrelaxed vacancy formation energy and Debye temperature. Optimized Ta MGPT potentials, so obtained to 1000 GPa [5,6], are displayed in Fig. 1 at equilibrium. Corresponding optimized Mo potentials, obtained to 400 GPa [7], are also shown, as are earlier first-generation 1994 Mo potentials [4]. The new MGPT Mo potentials correct known problems with the latter at short bond lengths.

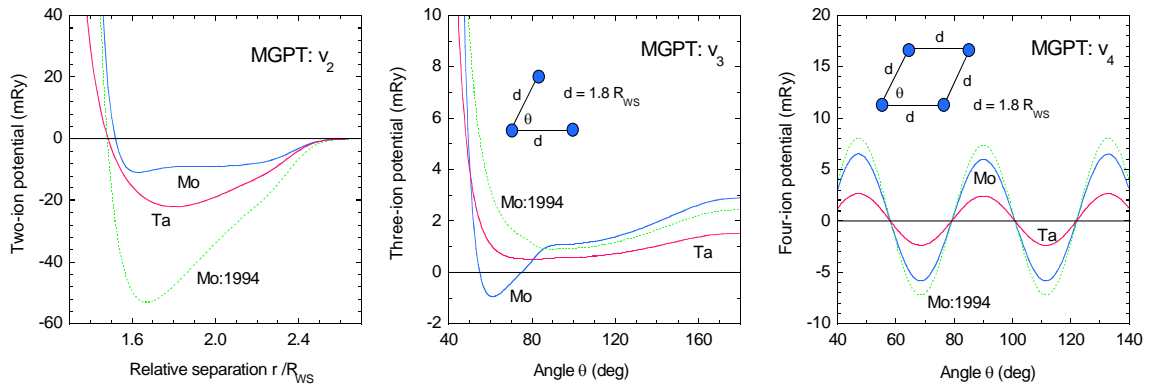


Figure 1. Optimized MGPT potentials v_2 , v_3 and v_4 for Ta and Mo at their respective equilibrium volumes. Shown for comparison are earlier 1994 MGPT potentials for Mo.

SELECTED APPLICATIONS

The MGPT potentials for Ta and Mo have been applied to a wide range of structural, thermodynamic, defect and mechanical properties at both ambient and extreme conditions. These properties include multiphase equation of state, melting and rapid resolidification, high-pressure elastic moduli and ideal strength, thermoelasticity and sound velocities, vacancy and self-interstitial formation and migration, grain-boundary structure, dislocation core structure and mobility, and the multiscale modeling of yield strength.

Multiphase equation of state and melt

We first discuss the quantum-based calculation of thermodynamics properties, with emphasis on the multiphase equation of state (EOS) and melting curve of Ta. In treating such properties, it is useful to break all thermodynamic quantities into cold (zero-temperature), ion-thermal and electron-thermal contributions. Thus for the total pressure of at volume Ω and temperature T we write:

$$P(\Omega, T) = P_0(\Omega) + P_{ion}(\Omega, T) + P_{el}(\Omega, T) \quad (2)$$

with similar expressions for the internal energy $E(\Omega, T)$ and the Helmholtz free energy $A(\Omega, T)$. We treat the observed bcc solid, the liquid and the metastable A15 phase. The cold bcc components of our Ta EOS are taken from accurate first-principles DFT electronic-structure calculations obtained with the FP-LMTO method in the 0-1000 GPa pressure range [8], and by construction, these components are exactly reproduced by the MGPT potentials. The ion-thermal EOS components are calculated from the MGPT potentials using quasiharmonic lattice dynamics in the low-T solid and MD simulation in the high-T solid and in the liquid. Good quality bcc phonons are obtained and these yield a Grüneisen parameter with a nonlinear volume dependence at high pressure. The remaining electron-thermal EOS components are obtained by using MD/MGPT snapshots of finite-T structure in small-cell (27 or 54-atom) FP-LMTO calculations and then configuration averaging. In both the high-T solid and in the liquid only 10-15

configurations are needed at each volume-temperature point to obtain well-converged and smoothly varying results. At temperatures as low as melt, there are very significant electron-thermal contributions arising from the large density of electronic states at the Fermi level in mid-period transition metals such as Ta. Through direct MGPT simulations, we have also shown that the A15 structure becomes competitive with bcc at low pressures and high temperatures in Ta, but over the entire 0-1000 GPa range from $T=0$ to melt, bcc is the predicted solid phase. A full two-phase bcc-liquid EOS and melt curve have been calculated over this pressure range and a temperature range of 0-35,000 K [5,9]. The calculated 300-K isotherm and Hugoniot from this EOS are shown in Fig.2 and compared against diamond-anvil-cell (DAC) and shock-compression experimental data [10,11]. Our corresponding equilibrium melt curve obtained from bcc and liquid free energies is displayed in Fig. 3 and compared against isobaric expansion data [12], the observed shock melting point [13] and recent laser-heated DAC measurements [14].

The pressure and temperature dependence of elastic moduli are closely related quantities with important implications for shock melting. As in Eq. (2), we calculate the single-crystal moduli C_{ij} as a sum of cold, ion-thermal and electron-thermal

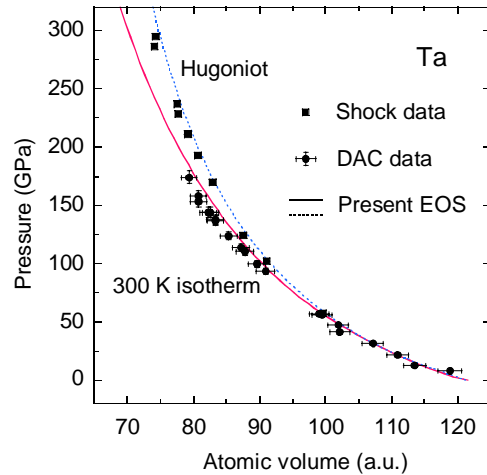


Figure 2. The 300-K isotherm and Hugoniot for Ta, as calculated with the present multiphase EOS and as measured in DAC [10] and shock [11] experiments.

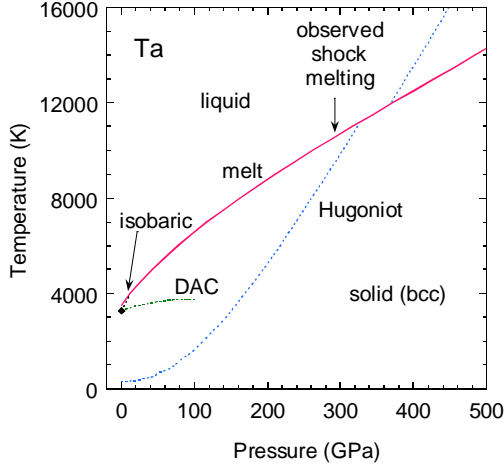


Figure 3. Present calculated melt curve (solid line) and predicted shock melting (intersection with dashed line) in Ta, as compared with experimental data [12-14].

components. The cold component is obtained from a blend of experimental data at low pressure and FP-LMTO calculations at high pressure and is reproduced by our MGPT potentials, while the electron-thermal component is calculated from FP-LMTO calculations at finite temperature. The remaining the ion-thermal component is obtained from either of two MGPT-based methods. The first involves the calculation of explicit strain derivatives of quasiharmonic phonons, while the second involves exact Monte Carlo simulation and thereby also includes anharmonic contributions to C_{ij} . We have used these methods to investigate the full thermoelastic behavior of Ta and Mo at high temperature and pressure [15].

High-pressure melting in transition metals has become controversial with unexpectedly flat melt curves recently obtained in laser-heated DAC experiments for Ta, Mo and other metals [14]. In contrast, we predict a steep melting curve for Ta, which is consistent with both isobaric expansion data near ambient pressure [12] and the observed shock melting point near 300 GPa [13]. Moreover, as shown in Fig. 4, our calculated sound velocities from high-T,P elastic moduli in bcc and liquid Ta are in good agreement with those measured along the Hugoniot in the shock melting experiments, confirming the interpretation of those experiments.

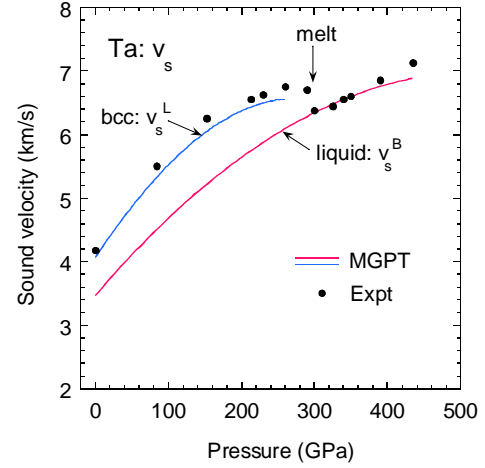


Figure 4. Calculated bcc and liquid Ta sound velocities from elastic moduli (solid lines) compared with values measured in shock melting experiments (points) [13].

Multiscale modeling of yield stress

The low-T and high-strain-rate plastic behavior of bcc transition metals is controlled by the intrinsic core properties of $a/2\langle 111 \rangle$ screw dislocations. Unlike the highly mobile edge dislocations in these metals, the motion of the screw dislocations is severely restricted by the non-planar atomic structure of its core, resulting in low mobility, thermal activated kink pairs and a temperature-dependent yield stress.

For the accurate atomistic simulation of dislocation core properties, we have developed an advanced Green's function (GF) simulation method that allows both static and dynamic calculations [6]. Extensive GF/MGPT simulations have been carried out in Ta and Mo over wide ranges of pressure on the core structure, the Peierls stress and its stress-orientation dependence, and kink-pair energetics of $a/2\langle 111 \rangle$ screw dislocations [6,16]. In general, the core structure exhibits a three-fold directional spreading, of variable magnitude or polarization. We predict an isotropic core structure for Mo and Ta near equilibrium and into expansion, but an increasingly polarized core under hydrostatic pressure.

Similarly, our calculated Peierls stress τ_p in Ta and Mo exhibits a strong dependence on the

orientation of the applied stress and large deviations from the well-known Schmid law. Our minimum τ_p in Mo at ambient pressure is close to the corresponding experimental estimate based on extrapolating the observed yield stress to zero temperature, and is a major improvement over that previously obtained with the 1994 MGPT potentials [17]. In the case of Ta, our minimum τ_p is still about a factor of two larger than the experimental estimate. In Ta and Mo we also find that both the ideal shear strength of the bcc perfect crystal and τ_p display approximate linear scaling with the $\langle 111 \rangle$ shear modulus $G_{111} = (2C' + C_{44})/3$ to 1000 and 400 GPa, respectively. Our results for Ta are displayed in Fig. 5. These findings support the linear scaling of yield strength with shear modulus, as is assumed in most of the constitutive models used in the shock-compression community.

At finite temperature, the motion of the bcc screw dislocations occurs by the thermally assisted formation and migration of kink pairs. In microscale dislocation dynamics (DD) simulations of single-crystal plasticity for bcc metals [18], a key input quantity is the stress-dependent activation enthalpy for kink-pair formation, $\Delta H(\tau)$. This quantity controls the dislocation

mobility, with the stress-dependent velocity of a screw dislocation given by

$$v_{screw}(\tau) \propto \exp[-\Delta H(\tau)/k_B T]. \quad (3)$$

We have now performed extensive GF/MGPT atomistic simulations of $\Delta H(\tau)$ for both Ta and Mo over a wide range of pressures. These results can then be fitted to the simple analytic form used in the DD simulations. One can thereby import the required atomistic information directly into DD simulations for real materials at any assumed pressure condition. In Fig. 6 we display atomistically-informed DD simulations of yield stress in Ta as a function of temperature for three selected pressures. In the latter, we have everywhere scaled down the Peierls stress by about a factor of two to account for the overestimate noted above. Otherwise, the temperature dependence of the yield stress at ambient pressure is in good accord with experiment [19]. Similar DD simulations have also been done for Mo [16].

BEYOND THE STANDARD THEORY

One of the advantages of the first-principles GPT formalism for interatomic potentials is that it is systematically improvable in a manner consistent

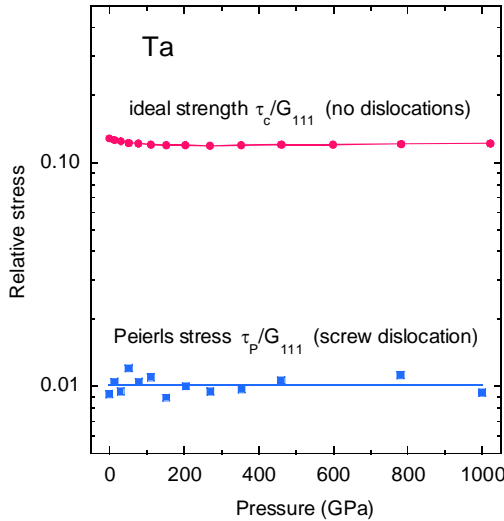


Figure 5. Calculated pressure scaling of the ideal shear strength and Peierls stress in Ta.

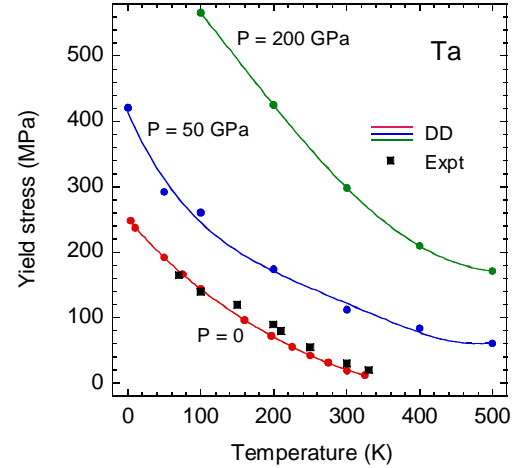


FIGURE 6. Atomistically-informed DD simulations of the single-crystal yield stress in bcc Ta at three pressures.

with quantum mechanics. Recently, we have made major strides in this direction by developing a more general matrix MGPT representation. In the matrix MGPT, the three- and four-ion angular functions are recast as matrix products that can be evaluated on the fly numerically during a simulation. In this representation, several major extensions of the standard MGPT are possible. First, the theory can be immediately generalized to treat non-canonical d -bands with arbitrary tight-binding coefficients. Second, one may further generalize from d states to f states to treat actinide metals by replacing 5×5 d -state matrices with 7×7 f -state ones.

A third major advance that has been facilitated by the matrix MGPT is algorithm improvements in the evaluation of energies and forces, most notably an optimized strategy to calculate the multi-ion energy terms in Eq. (1) and an explicit analytic treatment of the forces [20]. This has resulted in MGPT simulation codes that are 6-10 times faster and has dramatically increased the size and scope of problems that can be addressed on large parallel platforms. The most striking example of this is the recent large-scale MD/MGPT simulations of rapid resolidification of Ta that have been performed on LLNL's new BlueGene/L supercomputer [21].

Two other important areas we are currently pursuing are the use of non-canonical bands and the development of temperature-dependent MGPT potentials. In principle, non-canonical bands permit a more accurate characterization of the underlying electronic structure. In practice, we have found them useful in improving the overall quality of the calculated phonon spectrum in certain difficult cases such as Mo. Interestingly, the introduction of just two non-canonical band parameters seems to be able to improve *all* phonons at *all* volumes. The concept of temperature-dependent potentials for d - and f -electron metals is an important one because of the large electron-thermal effects at temperatures as low as melt. These effects are normally treated additively from the normal ion-thermal effects, as in Eq. (2), but we are now trying to capture them simultaneously and self-consistently by building MGPT potentials on the basis of the total electron free energy at finite temperature.

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