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## **Hydrostatic, Uniaxial, and Triaxial Compression Tests on Unpoled “Chem-prep” PZT 95/5-2Nb Ceramic Within Temperature Range of –55 to 75°C**

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# **Hydrostatic, Uniaxial, and Triaxial Compression Tests on Unpoled “Chem-prep” PZT 95/5-2Nb Ceramic Within Temperature Range of $-55$ to $75^{\circ}\text{C}$**

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## **ABSTRACT**

Sandia is currently developing a lead-zirconate-titanate ceramic 95/5-2Nb (or PNZT) from chemically prepared (“chem-prep”) precursor powders. Previous PNZT ceramic was fabricated from the powders prepared using a “mixed-oxide” process. The specimens of unpoled PNZT ceramic from batch HF803 were tested under hydrostatic, uniaxial, and constant stress difference loading conditions within the temperature range of  $-55$  to  $75^{\circ}\text{C}$  and pressures to 500 MPa. The objective of this experimental study was to obtain mechanical properties and phase relationships so that the grain-scale modeling effort can develop and test its models and codes using realistic parameters. The stress-strain behavior of “chem-prep”

PNZT under different loading paths was found to be similar to that of “mixed-oxide” PNZT. The phase transformation from ferroelectric to antiferroelectric occurs in unpoled ceramic with abrupt increase in volumetric strain of about 0.7 % when the maximum compressive stress, regardless of loading paths, equals the hydrostatic pressure at which the transformation otherwise takes place. The stress-volumetric strain relationship of the ceramic undergoing a phase transformation was analyzed quantitatively using a linear regression analysis. The pressure ( $P_{T1}^H$ ) required for the onset of phase transformation with respect to temperature is represented by the best-fit line,  $P_{T1}^H$  (MPa) = 227 + 0.76 T (°C). We also confirmed that increasing shear stress lowers the mean stress and the volumetric strain required to trigger phase transformation. At the lower bound (-55°C) of the tested temperature range, the phase transformation is permanent and irreversible. However, at the upper bound (75°C), the phase transformation is completely reversible as the stress causing phase transformation is removed.

# ACKNOWLEDGEMENTS

The authors would like to acknowledge Rebecca Brannon and David Holcomb for their critical review of this report. The authors also thank Jeffrey Keck for overseeing fabrication of the PNZT specimens. Diane Meier assisted in the preparation of the specimens and Robert Hardy provided advice in setting up the control system for the loading machine. The managerial support received from Jaime L. Moya, Justine E. Johannes and Laurence S. Costin is also gratefully appreciated.

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# 1. Introduction

Sandia is currently developing a new PNZT ceramic sintered from a chemically precipitated, calcined and agglomerated powder (Voigt *et al.* 1998; Voigt *et al.* 1999). Lead-zirconate-titanate 95/5-2Nb ceramic (PZT 95/5-2Nb, or, simply, “PNZT”) is the active electrical element in ferroelectric explosive power supplies (Lysne and Percival, 1975; Bauer *et al.*, 1989). Under explosive loading, poled ferroelectric (FE) PNZT transforms to an antiferroelectric (AFE) polymorph, rapidly releasing its bound surface charge and producing very large voltages and currents (Fritz and Keck, 1978). Thus, the electromechanical response of PNZT must be understood and modeled under complex, dynamic loading conditions.

The ASCI (Advanced Simulation and Computing Program) Project “Grain-Scale Shock Response of PZT 95/5-2Nb Ceramic” is developing microstructural-scale models and codes (Brannon *et al.*, 2001) to accomplish this goal. Currently, the grain-scale modeling effort is working almost exclusively with phase relationships and electromechanical properties that have been measured for PNZT fabricated using a “mixed-oxide” process, in which lead, zirconium, titanium and niobium oxide powders were mixed, calcined, milled and agglomerated; the resulting PNZT powder was dry-pressed and sintered. However, to date there has also been no systematic characterization of the electromechanical properties and phase relationships for a single formulation of the “chem-prep” ceramic even within the limited temperature and pressure range over which some ferroelectric power supplies must reliably function.

The objective of this project is to obtain those properties and phase relationships so that the grain-scale modeling effort can develop and test its models and codes using realistic parameters obtained from a single formulation of the “chem-prep” PNZT within the temperature range of -55 to 75°C, and pressures to 500 MPa. The laboratory hydrostatic compression (HC) experiments were conducted on specimens instrumented to acquire data on transformation strains, strain anisotropy, and quasistatic bulk modulus as functions of temperature, pressure and phase (FE vs. AFE). The hydrostatic compression tests were supplemented with uniaxial compression (UC) experiments within the specified pressure and temperature ranges to quantify the interaction of transformation and dipole reorientation strains as a function of temperature. These interactions profoundly affect strain anisotropy under non-hydrostatic loading, which has been only superficially examined thus far. Constant-Stress-Difference (CSD) experiments were also conducted to determine the effects of non-hydrostatic compression on the mean stress for transformation.

**Task 1.** A series of HC experiments across the FE-AFE boundary was conducted on unpoled PNZT specimens in 10°C increments from -55 to 75°C. This density of experiments was necessary to investigate the curved structure of the boundary determined by Fritz and Keck (1978) for “mixed-oxide” ceramic. Strain measurements were performed on all experiments, which yielded a quasistatic bulk modulus and transformation strains.

**Task 2.** A series of UC experiments was conducted on unpoled ceramic at -55, 20 and 75°C. Acoustic velocity and strain measurements were used to measure changes in elastic properties and strains associated with stress induced dipole reorientation (Fritz and Keck, 1978; Fritz, 1979), the results of which can be used to test and calibrate models for stress-induced dipole reorientation. These experiments were carried to failure to observe the effect of a change of temperature (Zeuch *et al.*, 1999b) on the manner in which dipole switching strains interact with transformation strains.

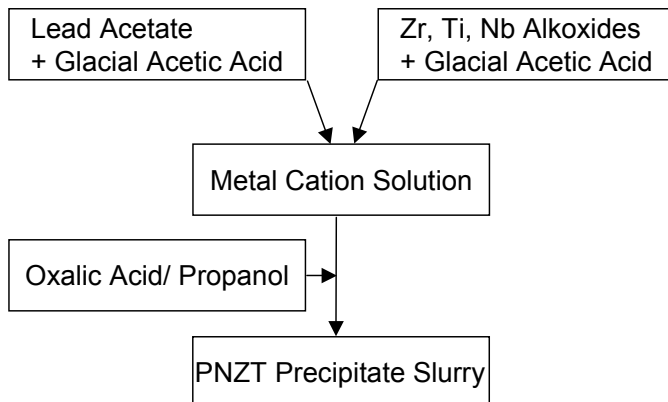
**Task 3.** A series of CSD experiments were conducted at four stress differences ( $\sigma_d = \sigma_1 - \sigma_3 = 50, 100, 150, \text{ and } 200 \text{ MPa}$ ) at each of three different temperatures (-55, 25, and 75°C). These experiments characterized the effects of nonhydrostatic loading on phase transformation of the unpoled “chem-prep” ceramic. Nonhydrostatic loading has been shown to lower the mean stress for onset of the transformation in “mixed-oxide” ceramic.

## 2. Sample Preparation and Characterization

### 2.1 Sample materials

The PNZT ceramic specimens were produced based on Sandia National Laboratories TSP (Transferred Sandia Process). This is an upscaled SP (Sandia Process) chemical preparation process for the synthesis of PNZT powder (U.S. Patent No. 5,908,802 by Voigt *et al.*, 1999). Figure 1 shows the flow diagram for key steps in solution synthesis of PNZT.

Our specimens came from sintering Lot HF803. The calcinated TSP38 powder was mixed with 0.9 w% of Lucite poreformer. The average density of the material from Lot HF803 was 7.358 g/cm<sup>3</sup>. The general electromechanical characteristics of the ceramic from HF803 are shown in Table 1. The average depoling pressure of the ceramic from Lot HF803 is approximately 303 ( $\pm 2$ ) MPa and falls in the upper range of the depoling pressure. The average charge release of the ceramic from Lot HF803 was 31.9 ( $\pm 0.2$ )  $\mu\text{C}/\text{cm}^2$ .



**Figure 1.** Overview of powder synthesis processing of PNZT (after Voigt *et al.*, 1999, U.S. Patent #5,908,802).

**Table 1. Electromechanical characteristics of “chem.-prep” PNZT-HF803.  
(from Pin Yang, 2003)**

<b>Serial no.</b>	<b>Depoling pressure (MPa)</b>	<b>Charge release (<math>\mu\text{C}/\text{cm}^2</math>)</b>
X10774	304	32.1
X10825	302	31.7
X10827	303	31.8
X10837	306	32.1
X10845	303	31.9
X10865	301	31.8
X10927	301	32.0
X10939	299	31.5
X10942	305	32.3
X10978	306	32.2
<b>Average:</b>	303	31.9
<b>Standard Deviation:</b>	2	0.2
<b>High:</b>	306	32.3
<b>Low:</b>	299	31.5

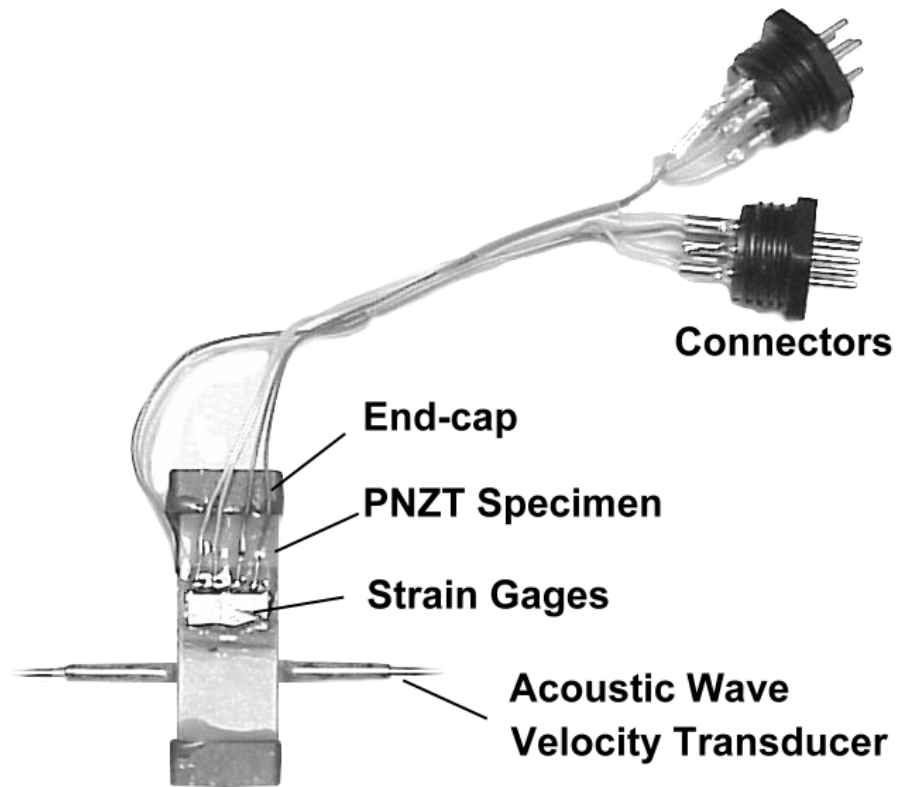
## 2.2 Sample preparations

The unpoled PNZT test specimens were instrumented to acquire data on the strains due to phase transformation as a function of temperature during quasistatic loading. We fabricated rectangular parallelepipeds of PNZT. The specimens have nominal dimensions of  $10.8 \times 10.8 \times 25.4$  mm. The dimensions fall within the range of nominal length-to-diameter ratio (2 to 2.5). The ends of the specimen were ground flat within 0.003 mm tolerance. Samples were visually inspected for significant flaws and general straightness of the surfaces. The physical dimensions of each specimen are listed in Table 2 with assigned test type and conditions.

Two pairs of orthogonal sets of axial and lateral strain gages were mounted on opposite sides of the specimen ( $180^\circ$  apart) at mid-height of the specimen. The axial and lateral gages were oriented to be parallel and perpendicular to the axis of the specimen, respectively. The axial ( $\epsilon_a$ ) and lateral ( $\epsilon_l$ ) strains were measured as the average strain from two respective strain gages. The volumetric strain,  $\epsilon_v$ , was calculated as  $\epsilon_v = \epsilon_a + 2\epsilon_l$ .

The instrumented specimen was placed between the upper and lower tungsten carbide end-caps. The strain-gaged specimen with two end-caps was coated with an approximately 1 mm thick impervious polyurethane membrane. To maintain uniform thickness of the membrane during curing, the specimen assembly was turned on a lathe along the axial centerline of the assembly. The flexible membrane allowed the confining pressure to be applied uniformly on the specimen and at the same time prevented the confining fluid from infiltrating into the specimen. In UC tests, a pair of acoustic wave velocity transducer is mounted on the opposite side of the specimen to measure the compressive (or P) wave velocity across the

specimen perpendicular to the loading axis. A typical PNZT specimen, ready to be tested, is shown in Figure 2.



**Figure 2.** A typical PNZT specimen instrumented with two pairs of axial and lateral strain gages and piezoelectric crystals for measuring wave velocities. The specimen is placed between two tungsten carbide end-caps and the assembly is coated with polyurethane membrane to prevent the confining fluid from infiltrating into the specimen.

**Table 2. List of mechanical tests conducted for “chem-prep” PNZT-HF803 specimens.**

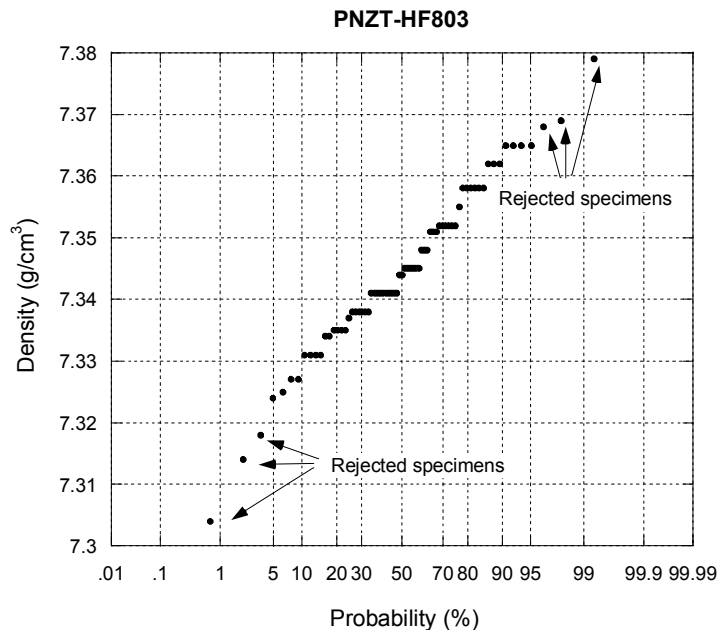
Specimen no.	Test type	Temperature (° C)	$\sigma_1$ - $\sigma_3$ (MPa)	Length (cm)	Width (cm)	Height (cm)	Weight (g)	Density (g/cm <sup>3</sup> )	Note
PNZT-01	UC	25	$\sigma_1$	1.077	1.080	2.540	21.75	7.365	
PNZT-02	UC	25	$\sigma_1$	1.080	1.080	2.540	21.74	7.345	
PNZT-03				1.080	1.080	2.540	21.76	7.352	
PNZT-04	UC	-55	$\sigma_1$	1.080	1.080	2.540	21.71	7.335	
PNZT-05				1.080	1.080	2.540	21.78	7.358	
PNZT-06	UC	77	$\sigma_1$	1.080	1.080	2.540	21.72	7.338	
PNZT-07	CSD	25	150	1.080	1.080	2.540	21.73	7.341	
PNZT-08	CSD	-55	100	1.080	1.080	2.540	21.71	7.335	
PNZT-09				1.077	1.080	2.543	21.75	7.358	Damaged
PNZT-10	CSD	25	50	1.080	1.080	2.543	21.73	7.334	
PNZT-11	CSD	25	200	1.080	1.080	2.540	21.74	7.345	
PNZT-12				1.080	1.080	2.543	21.78	7.351	
PNZT-13	CSD	25	50	1.080	1.080	2.543	21.75	7.341	
PNZT-14	CSD	25	150	1.082	1.080	2.540	21.75	7.331	
PNZT-15	CSD	25	100	1.080	1.082	2.540	21.75	7.331	
PNZT-16				1.080	1.080	2.543	21.67	7.314	Rejected
PNZT-17	CSD	25	50	1.080	1.080	2.543	21.73	7.334	
PNZT-18	CSD	25	100	1.080	1.080	2.540	21.73	7.341	
PNZT-19	CSD	25	150	1.080	1.080	2.543	21.76	7.344	
PNZT-20				1.080	1.080	2.540	21.73	7.341	
PNZT-21				1.080	1.080	2.543	21.78	7.351	
PNZT-22	CSD	-55	50	1.082	1.080	2.543	21.75	7.324	
PNZT-23	CSD	-55	200	1.080	1.080	2.543	21.71	7.327	
PNZT-24	CSD	-55	100	1.080	1.080	2.543	21.75	7.341	
PNZT-25	CSD	-55	100	1.080	1.080	2.543	21.78	7.351	
PNZT-26	CSD	-55	150	1.080	1.082	2.543	21.76	7.327	
PNZT-27	CSD	-55	150	1.082	1.080	2.540	21.79	7.345	
PNZT-28	CSD	-55	150	1.080	1.080	2.540	21.76	7.352	
PNZT-29				1.082	1.080	2.540	21.78	7.341	
PNZT-30	CSD	75	50	1.080	1.082	2.543	21.77	7.331	
PNZT-31	CSD	75	100	1.080	1.080	2.543	21.76	7.344	
PNZT-32	CSD	75	150	1.080	1.080	2.540	21.80	7.365	
PNZT-33	CSD	75	200	1.080	1.080	2.540	21.76	7.352	
PNZT-34	HC	25	0	1.080	1.080	2.540	21.75	7.348	
PNZT-35	CSD	75	50	1.080	1.080	2.540	21.68	7.325	
PNZT-36	CSD	75	150	1.080	1.080	2.543	21.74	7.338	
PNZT-37	HC	75	0	1.077	1.077	2.540	21.70	7.365	
PNZT-38				1.080	1.080	2.540	21.77	7.355	
PNZT-39				1.080	1.080	2.543	21.74	7.338	
PNZT-40				1.080	1.080	2.540	21.74	7.345	
PNZT-41				1.080	1.080	2.540	21.78	7.358	
PNZT-42				1.080	1.080	2.543	21.74	7.338	
PNZT-43				1.080	1.080	2.540	21.76	7.352	
PNZT-44	HC	58	0	1.080	1.080	2.540	21.78	7.358	
PNZT-45	HC	41	0	1.080	1.080	2.540	21.74	7.345	
PNZT-46				1.080	1.080	2.540	21.62	7.304	Rejected

PNZT-47				1.080	1.080	2.540	21.72	7.338	
PNZT-48				1.080	1.080	2.543	21.74	7.338	
PNZT-49	HC	15	0	1.080	1.080	2.540	21.74	7.345	
PNZT-50				1.077	1.080	2.538	21.77	7.379	Rejected
PNZT-51				1.080	1.080	2.540	21.76	7.352	
PNZT-52	HC	-55	0	1.077	1.080	2.540	21.76	7.369	Rejected
PNZT-53	HC	-25	0	1.080	1.080	2.540	21.70	7.331	
PNZT-54				1.080	1.080	2.543	21.77	7.348	
PNZT-55	HC	5	0	1.080	1.080	2.540	21.71	7.335	
PNZT-56	HC	-5	0	1.080	1.080	2.540	21.73	7.341	
PNZT-57	HC	-15	0	1.080	1.080	2.540	21.79	7.362	
PNZT-58	HC	-10	0	1.080	1.080	2.540	21.78	7.358	
PNZT-59	HC	-5	0	1.080	1.080	2.540	21.73	7.341	
PNZT-60	HC	75	0	1.080	1.077	2.540	21.66	7.335	
PNZT-61	HC	58	0	1.080	1.077	2.540	21.75	7.365	
PNZT-62				1.080	1.080	2.540	21.81	7.368	Rejected
PNZT-63	HC	-35	0	1.080	1.080	2.540	21.70	7.331	
PNZT-64	HC	-45	0	1.080	1.080	2.543	21.75	7.341	
PNZT-65	HC	15	0	1.080	1.080	2.540	21.73	7.341	
PNZT-66				1.080	1.080	2.540	21.79	7.362	
PNZT-67				1.080	1.080	2.540	21.78	7.358	
PNZT-68				1.080	1.080	2.540	21.76	7.352	
PNZT-69				1.080	1.080	2.540	21.79	7.362	
PNZT-70				1.080	1.080	2.540	21.66	7.318	Rejected
PNZT-71	UC	-55	$\sigma_1$	1.080	1.080	2.540	21.75	7.348	

UC-Uniaxial Compression; CSD-Constant Stress Difference; HC-Hydrostatic Compression

$\sigma_1$ -major principal stress;  $\sigma_3$ -minor principal stress

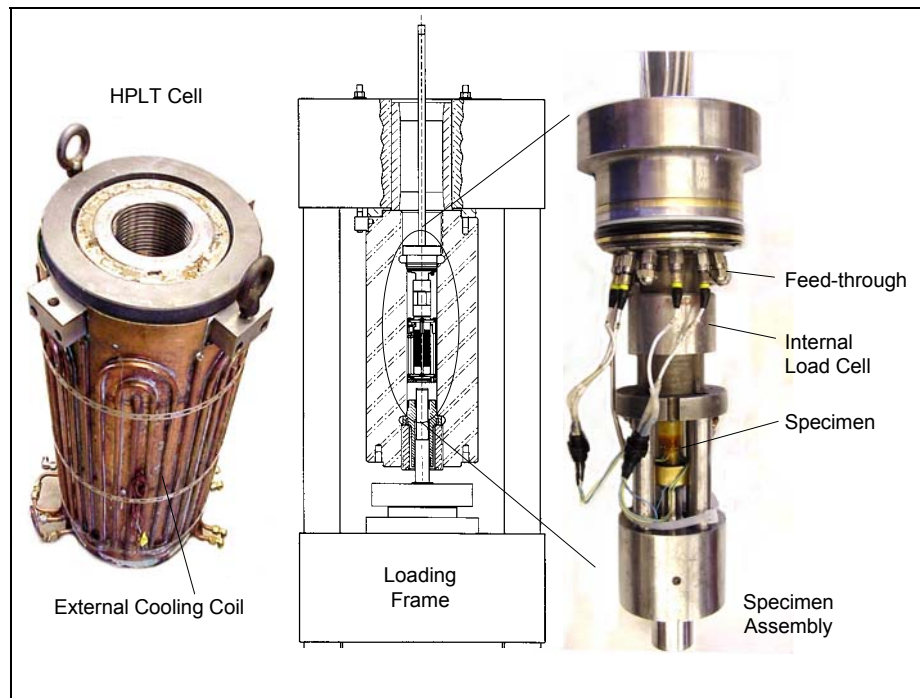
The following figure shows that six PNZT-HF803 specimens fell in the <5% or >95% “tail” regions of the density distribution plot. These specimens were considered as “outliers” and rejected for further experimental analyses.





## 2.3 Experimental set-up

A High-Pressure Low-Temperature (HPLT) triaxial cell (Zeuch *et al.*, 1999d) was designed and built to characterize the electromechanical properties of PNZT and other materials such as ALOX (Alumina Loaded Epoxy) and frozen soil (Lee *et al.*, 2002). It is capable of operating at temperature ranges from  $-65$  to  $150^{\circ}\text{C}$  and confining pressures up to 500 MPa. The HPLT triaxial cell has a bore diameter of 82 mm and length of 200 mm. The cell is able to accept specimens, in the form of cylinder or rectangular parallelepiped, having diameters (or face diagonals) up to 25 mm and lengths up to 50 mm. Figure 3 shows the schematic of the load frame and instrumented PNZT specimen integrated with the HPLT triaxial cell. In addition to the fundamental operating conditions of temperature, pressure and large specimen size required for the test cell, additional requirements and restrictions imposed serious constraints upon the design. These additional requirements included, for example, the necessity to: (1) fit in an existing, 1.9 MN servo-controlled load frame; (2) operate within an otherwise normal laboratory setting (*i.e.*, not in a cold room); and (3) use a liquid confining medium for safety and system controllability. Owing to the extreme operating conditions and the likelihood of high piston-seal friction, we also decided that internal load and strain measurements, and hence, numerous high-pressure feed-throughs, would be necessary. Nevertheless, despite these and other restrictions, it was deemed feasible to use an externally cooled pressure vessel composed of HP9-4-20 alloy steel and equipped with twelve coaxial feed-throughs. Two specially designed load cells have been built for internal force measurements. Strains were measured using the strain gages mounted on the specimen.



**Figure 3. Externally cooled High-Pressure-Low-Temperature (HPLT) cell and an assembly of PNZT specimen.**

## 2.4 Experimental procedure

Three different loading paths were used for uniaxial compression, hydrostatic compression, and constant stress difference testing. Appropriate loading paths are shown in Figures 4 and 5.

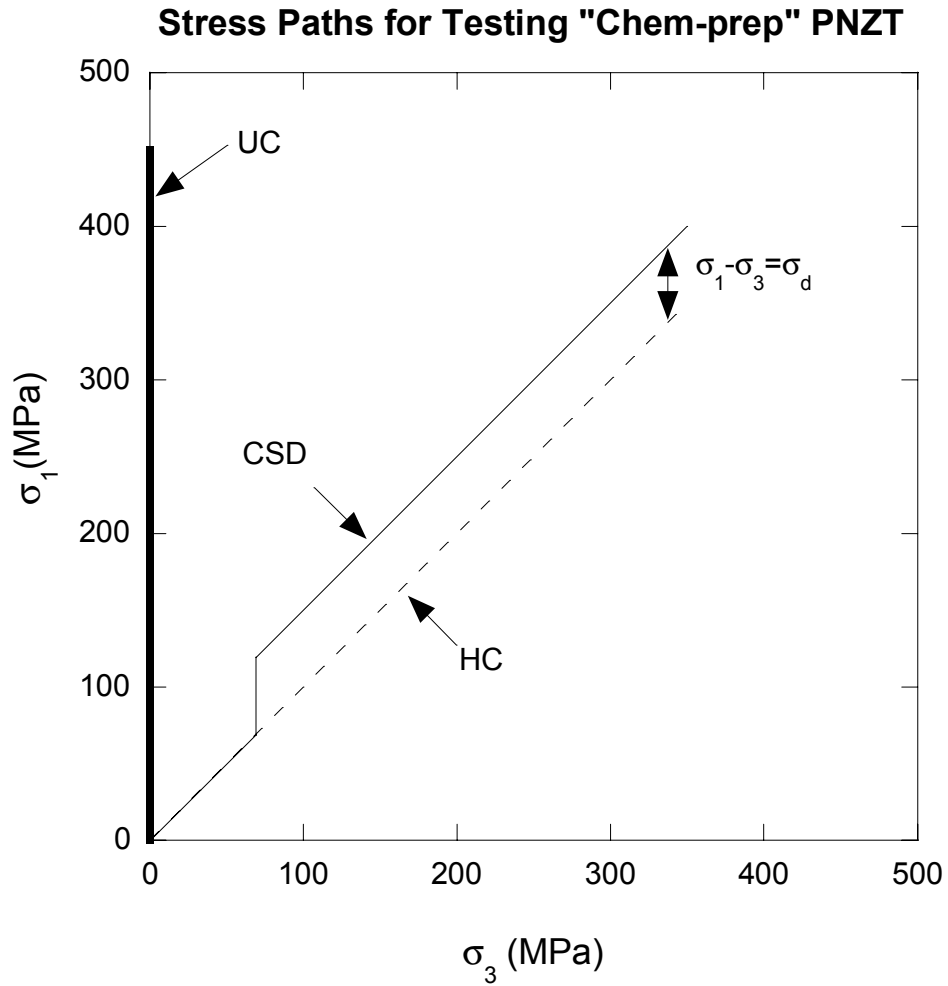
For hydrostatic compression, the piston, used for applying the axial load to the specimen, was pulled back so as not to apply any deviatoric stress to the specimen. The confining pressure,  $P$ , was increased at the rate of 0.69 MPa/s all around the specimen to apply all three principal stresses  $\sigma_1=\sigma_2=\sigma_3=P$  to the specimen past the hydrostatic pressure for transformation,  $P_T^{HC}$ . The loading history of the hydrostatic compression is represented by the dotted straight line in Figure 4.

For uniaxial compression, the axial load was applied without confining pressure ( $\sigma_2 = \sigma_3 = P = 0$ ). The piston was moved at a constant rate of  $2.54 \times 10^{-4}$  mm/s which corresponds to the strain rate of  $10^{-5}$ /s. The loading history of the uniaxial compression is shown as the thick vertical line UC in Figure 4.

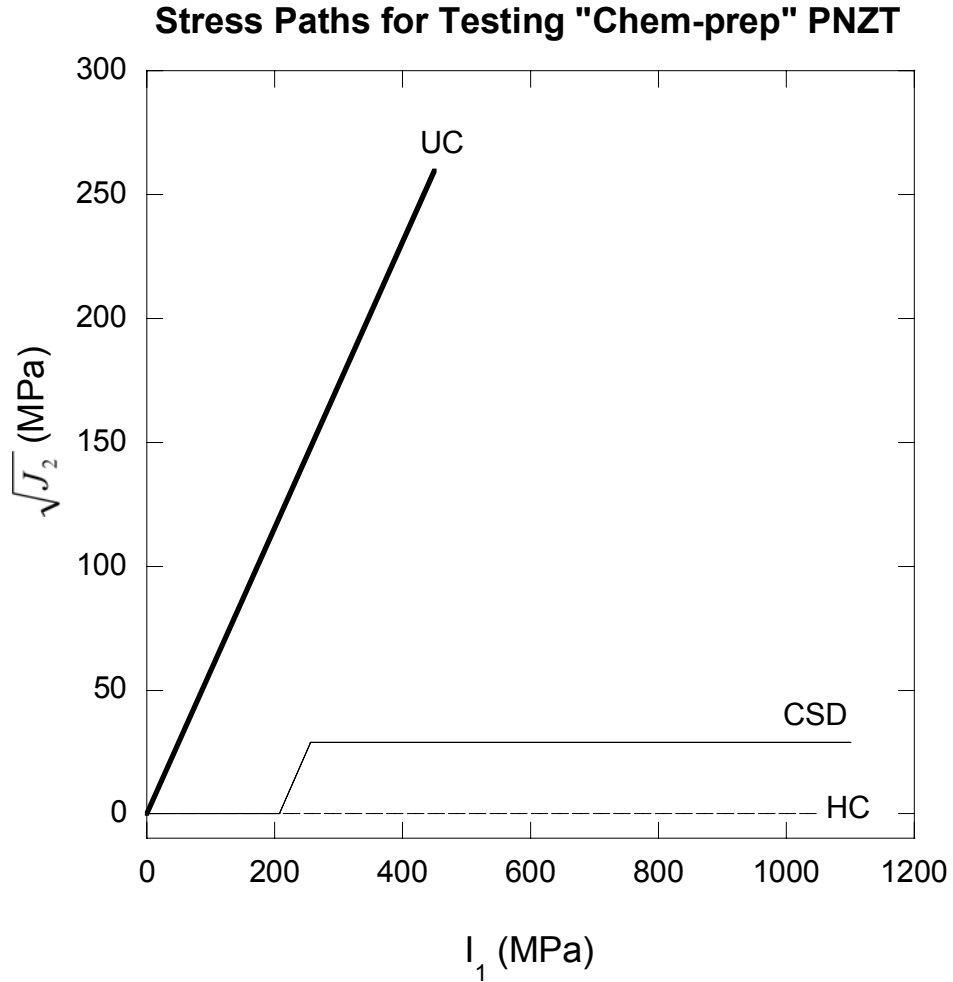
For constant stress difference testing, the specimen was hydrostatically compressed at about 69 MPa which is below the expected pressure for transformation,  $P_T^{HC}$ . At that pressure the piston was moved to make a contact with the specimen. Then additional load was applied to the specimen creating the stress difference ( $\sigma_1-\sigma_3=\sigma_d$ ). The axial stress ( $\sigma_1$ ) and the confining pressure ( $P=\sigma_3$ ) were increased simultaneously at the same rate to maintain the stress difference ( $\sigma_d$ ) constant. This loading path created a constant increase of the mean stress while maintaining the stress difference constant. The loading path of the constant stress difference testing is shown as CSD in Figure 4.

Figure 5 shows three stress paths plotted in domain of stress invariants:  $I_1=(\sigma_1+\sigma_2+\sigma_3)$  and  $J_2=\frac{(\sigma_1-\sigma_2)^2+(\sigma_2-\sigma_3)^2+(\sigma_3-\sigma_1)^2}{6}$ . During HC and CSD testing, the deviatoric

component of stresses shown in terms of  $J_2$  was kept constant throughout the test except for the stress difference  $\sigma_d$  set for CSD. For UC testing, deviatoric component of stresses increased linearly with hydrostatic component of stresses.



**Figure 4.** Three different loading paths are shown in the principal stress domain ( $\sigma_1$ - $\sigma_3$ ): UC for Uniaxial Compression, HC for Hydrostatic Compression, and CSD for Constant Stress Difference. The stress difference,  $\sigma_1 - \sigma_3$ , is shown as  $\sigma_d$ .



**Figure 5. Three different loading paths are shown in the stress invariant domain of  $(I_1, \sqrt{J_2})$ : UC for Uniaxial Compression, HC for Hydrostatic Compression, and CSD for Constant Stress Difference.  $I_1 = (\sigma_1 + \sigma_2 + \sigma_3)$  is the first invariant of stress and**

$$J_2 = \frac{(\sigma_1 - \sigma_2)^2 + (\sigma_2 - \sigma_3)^2 + (\sigma_3 - \sigma_1)^2}{6} \text{ is the second invariant of stress.}$$

## 3. Material Testing

### 3.1 Hydrostatic compression tests

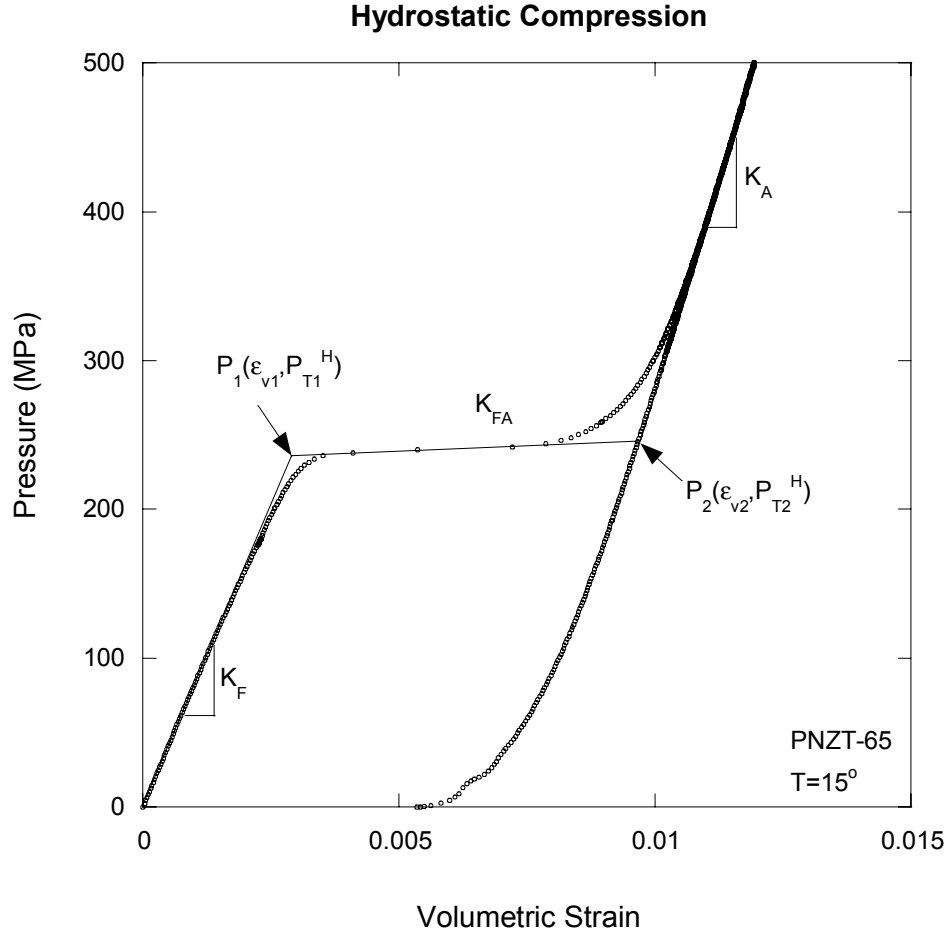
The mechanical behavior of “chem-*prep*” PNZT under hydrostatic loading was studied using a pressure (*P*)-volumetric strain ( $\epsilon_v$ ) plot. Figure 6 shows a typical record obtained from specimen PNZT-65 at 15°C. At a hydrostatic pressure of approximately 236 MPa, the unpoled PNZT underwent a phase transformation from a ferroelectric rhombohedral perovskite structure ( $F_{R1}$  or FE) to an antiferroelectric orthorhombic ( $A_o$  or AFE) structure. In order to characterize the phase transformation quantitatively, the *P*- $\epsilon_v$  plot was divided into three segments represented by three straight lines.

$$\begin{aligned} P_F &= a_1 + K_F \epsilon_v \quad (\text{where } 0 < \epsilon_v < \epsilon_{v1}) \\ P_{FA} &= a_2 + K_{FA} \epsilon_v \quad (\text{where } \epsilon_{v1} \leq \epsilon_v < \epsilon_{v2}) \\ P_A &= a_3 + K_A \epsilon_v \quad (\text{where } \epsilon_{v2} \leq \epsilon_v) \end{aligned} \quad (1)$$

The first segment, defined by a straight line with bulk modulus  $K_F$  as a slope, represents the mechanical behavior of PNZT in a FE phase. This linear increase of  $\epsilon_v$  as a function of *P* continues until the hydrostatic pressure reaches the phase transformation pressure  $P_{T1}^H$  at  $P_1$ . The volumetric strain at that pressure is represented by  $\epsilon_{v1}$ . The phase transformation is marked by a sudden increase in volumetric strain (or reduction in volume) shown as a nearly horizontal line with a slope of  $K_{FA}$ . The completion of phase transformation is shown as the abrupt increase of the slope at  $P_2$ . The volumetric strain and hydrostatic pressure at this point is represented as  $\epsilon_{v2}$  and  $P_{T2}^H$ , respectively. The remaining segment represents an AFE phase showing the higher bulk modulus  $K_A$ .

The unknown parameters of the three straight lines were obtained using a linear regression analysis applied to the linear portion of the segments (0 to 150 MPa for  $P_F = a_1 + K_F \epsilon_v$ ; the arbitrarily selected linear portion for  $P_{FA} = a_2 + K_{FA} \epsilon_v$ ; and the unloading portion of the data from the maximum pressure to 200 MPa for  $P_A = a_3 + K_A \epsilon_v$ ). The linear representation of the transitional segment,  $P_{FA} = a_2 + K_{FA} \epsilon_v$ , is subjective and is largely dependent on the selection of data to be analyzed.

Hydrostatic compression experiments were performed on large test specimens ( $10.8 \times 10.8 \times 25.4$  mm) across the FE-AFE boundary in 10°C increments within the temperature range of -55 to 75°C, and pressures up to 500 MPa. A total of thirteen specimens were tested mostly at 10°C increment. Each pressure (*P*)-volumetric strain ( $\epsilon_v$ ) plot is shown in Appendix A. Effects of temperature on the behavior of *P*- $\epsilon_v$  during phase transformation are shown in Figure 7. A detailed quantitative description of phase transformation in PNZT-HF803 under hydrostatic loading is summarized in Table 3.



**Figure 6. Quantitative description of phase transformation in “chem-prep” PNZT under hydrostatic loading. The initiation of phase transformation is represented by  $P_1$ . The volumetric strain and hydrostatic pressure at  $P_1$  is  $\epsilon_{v1}$  and  $P_{T1}^H$ , respectively.  $K_F$  represents the bulk modulus of the ceramic in FE phase. The completion of phase transformation is represented by  $P_2$ . The volumetric strain and hydrostatic pressure at  $P_2$  is  $\epsilon_{v2}$  and  $P_{T2}^H$ , respectively.  $K_A$  represent the bulk modulus of the ceramic in AFE phase. The phase transformation is represented by a straight line connecting  $P_1$  and  $P_2$  with slope  $K_{FA}$**

$$\left( = \frac{P_{T2}^H - P_{T1}^H}{\epsilon_{v2} - \epsilon_{v1}} \right).$$

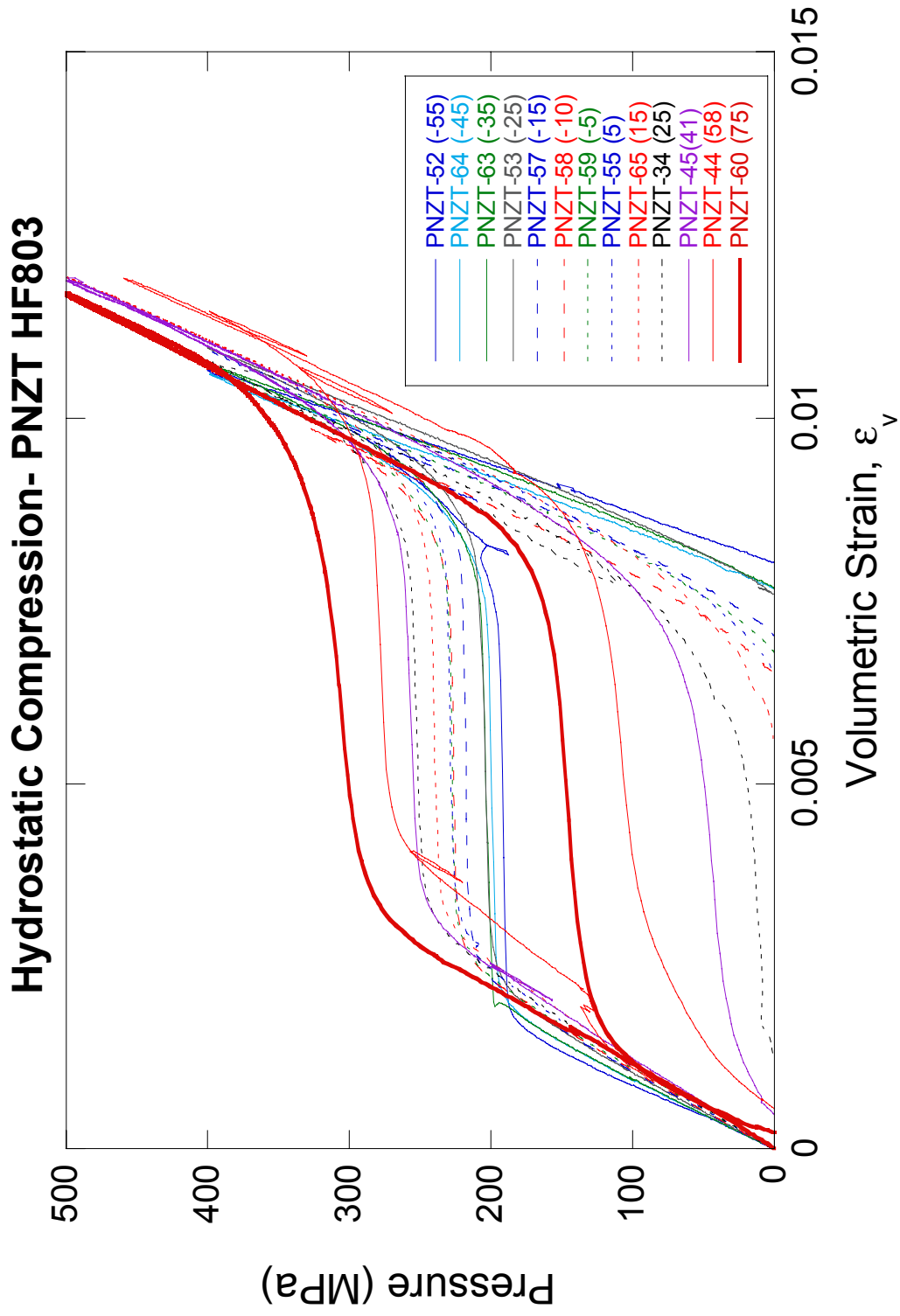


Figure 7. Pressure-Volumetric strain plot for hydrostatic compression tests on PNZT-HF803 specimens under different temperature conditions ranging from -55 to 75°C.

**Table 3. Summary of phase transformation in “chem-prep” PNZT-HF803 under hydrostatic compression (HC).**

Specimen no.	Temperature (°C)	$a_1$ (MPa)	$K_F$ (GPa)	$a_2$ (MPa)	$K_{FA}$ (GPa)	$a_3$ (MPa)	$K_A$ (GPa)	$\epsilon_{v1}$	$P_{T1}^H$ (MPa)	$\epsilon_{v2}$	$P_{T2}^H$ (MPa)	$\epsilon_{v2} - \epsilon_{v1}$ *	$P_{T2}^H - P_{T1}^H$ ** (MPa)
PNZT-52	-55	-1.0	115.3	187.2	1.0	-1220.4	151.7	0.0016	189	0.0093	196	0.0077	7.6
PNZT-64	-45	0.8	104.2	193.5	1.3	-1107.8	142.2	0.0019	196	0.0092	205	0.0074	9.5
PNZT-63	-35	1.1	103.2	196.5	1.4	-1103.5	139.9	0.0019	199	0.0094	210	0.0075	10.7
PNZT-53	-25	1.8	93.8	197.4	1.3	-1024.3	129.9	0.0021	200	0.0095	210	0.0074	9.8
PNZT-57	-15	1.9	92.1	214.3	0.8	-940.7	125.7	0.0023	216	0.0092	221	0.0069	5.4
PNZT-58	-10	1.8	90.6	222.3	0.8	-883.5	122.8	0.0025	224	0.0091	230	0.0066	5.5
PNZT-59	-5	1.1	89.5	222.8	1.0	-906.8	122.0	0.0025	225	0.0093	232	0.0068	6.6
PNZT-55	5	2.1	85.7	222.9	1.1	-865.5	115.6	0.0026	226	0.0095	234	0.0069	7.8
PNZT-65	15	0.9	80.9	232.7	1.3	-845.7	112.6	0.0029	236	0.0097	245	0.0068	8.9
PNZT-34	25	2.0	84.1	242.9	1.7	-769.0	108.8	0.0029	248	0.0095	259	0.0065	11.3
PNZT-45	41	-0.3	80.8	244.4	2.1	-803.7	109.1	0.0031	251	0.0098	265	0.0067	14.1
PNZT-44	58	2.0	82.7	262.1	2.4	-863.0	111.0	0.0032	270	0.0104	287	0.0071	17.0
PNZT-60	75	-1.5	87.4	271.9	5.8	-679.4	101.0	0.0033	291	0.0100	329	0.0066	38.2

$K_F$  - bulk modulus in FE (ferroelectric) phase

$K_{FA}$  - bulk modulus in transition from FE to AFE phase transformation

$K_A$  - bulk modulus in AFE (antiferroelectric) phase

$a_1$  - extrapolated pressure corresponding to zero volumetric strain in FE phase

$a_2$  - extrapolated pressure corresponding to zero volumetric strain during transition from FE to AFE phase

$a_3$  - extrapolated pressure corresponding to zero volumetric strain in AFE phase

$P_{T1}^H$  - pressure for initiation of FE to AFE phase transformation under hydrostatic compression

$P_{T2}^H$  - pressure for completion of FE to AFE phase transformation under hydrostatic compression

$\epsilon_{v1}$  - volumetric strain at  $P_{T1}^H$

$\epsilon_{v2}$  - volumetric strain at  $P_{T2}^H$

\* - Increase in volumetric strain during FE to AFE phase transformation

\*\* - Pressure increase during FE to AFE phase transformation



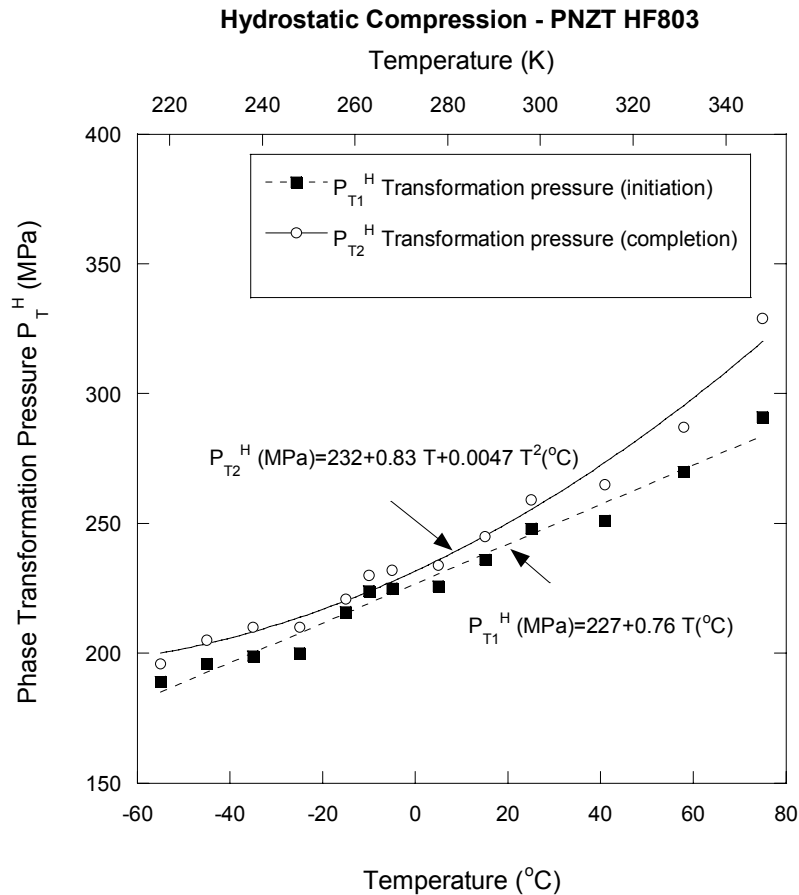
## Effects of Temperature on the Phase Transformation Pressures

The variations of pressures required for the onset ( $P_{T1}^H$ ) and completion ( $P_{T2}^H$ ) of FE to AFE phase transformation depend on temperature. As shown in Figure 8,  $P_{T2}^H$  data are well represented by a second-order polynomial function of temperature. However, the onset of transition  $P_{T1}^H$  is well represented by a simple straight line. The best-fit curves are:

$$P_{T1}^H \text{ (MPa)} = 227 + 0.76 T \text{ (}^\circ\text{C)} \quad (2)$$

$$P_{T2}^H \text{ (MPa)} = 232 + 0.83 T \text{ (}^\circ\text{C)} + 0.0047 T^2 \text{ (}^\circ\text{C)} \quad (3)$$

where the phase transformation pressures  $P_{T1}^H$  and  $P_{T2}^H$  are in MPa and T is temperature in degree C. The curved shape of the phase boundary, especially for the completion pressure  $P_{T2}^H$ , corroborates well with the previous findings in “mixed-oxide” ceramic in the phase diagram (Fritz and Keck, 1978).



**Figure 8. Phase transformation pressures plotted as a function of temperature. Both initiation ( $P_{T1}^H$ ) and completion ( $P_{T2}^H$ ) pressures for phase transformation increase with temperature under hydrostatic pressure.**

## Effects of Temperature on the Phase Transformation Strains

The volumetric strains at phase boundaries are plotted as a function of temperature (Figure 9). The volumetric strains for the onset of FE to AFE transformation increase with temperature in degree C:

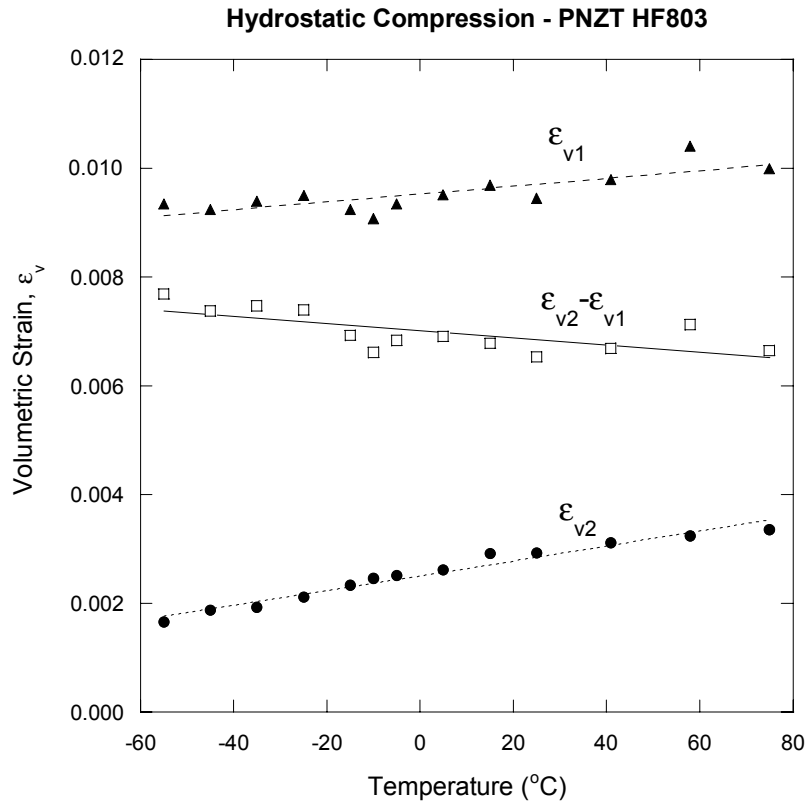
$$\varepsilon_{v1} = 0.0025 + 1.4 \times 10^{-5} T \text{ (}^\circ\text{C)} \quad (4)$$

The volumetric strains for the completion of FE to AFE transformation also increase with temperature:

$$\varepsilon_{v2} = 0.0095 + 7.2 \times 10^{-6} T \text{ (}^\circ\text{C)} \quad (5)$$

The difference between  $\varepsilon_{v2}$  and  $\varepsilon_{v1}$  corresponds to the sudden volume reduction during phase transformation. The amount of volume reduction decreases with temperature and can be represented as follows:

$$\varepsilon_{v2} - \varepsilon_{v1} = 0.007 - 6.6 \times 10^{-6} T \text{ (}^\circ\text{C)} \quad (6)$$



**Figure 9. Variations of volumetric strains ( $\varepsilon_v$ ) with temperature during FE to AFE phase transformation.**

## Effects of Temperature on the Bulk Moduli

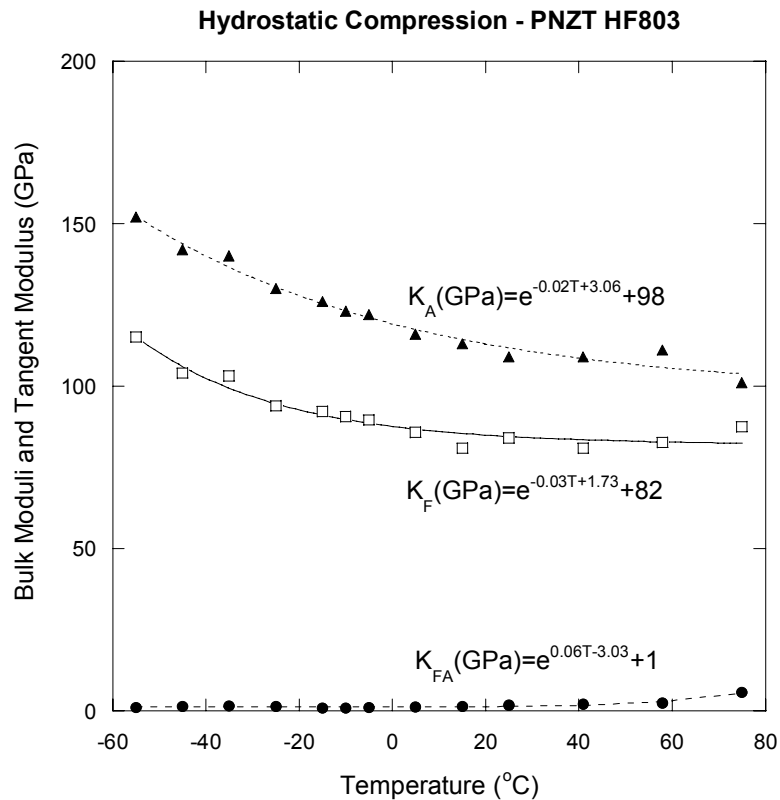
Figure 10 shows the variations of bulk moduli  $K_A$  and  $K_F$  and a tangent modulus  $K_{FA}$  of the “chem-prep” PNZT-HF803 with temperature. The results clearly show that, within experimental uncertainty the bulk moduli,  $K_A$  and  $K_F$ , decrease with increasing temperature

$$K_F \text{ (GPa)} = e^{-0.03T \text{ (}^\circ\text{C)} + 1.73} + 82 \quad (7)$$

$$K_A \text{ (GPa)} = e^{-0.02T \text{ (}^\circ\text{C)} + 3.06} + 98 \quad (8)$$

where  $T$  is temperature in degree C. It also shows that the bulk modulus  $K_A$ , after the completion of FE to AFE transition, becomes about 34 % higher than  $K_A$  in AFE phase ( $K_A \approx 1.35K_F$ ). The tangent modulus during transition remains constant or slightly increases with the rise of the temperature.

$$K_{FA} \text{ (GPa)} = e^{0.06T \text{ (}^\circ\text{C)} - 3.03} + 1 \quad (9)$$



**Figure 10. Variations of bulk moduli ( $K_A$  and  $K_F$ ) and transitional tangent modulus ( $K_{FA}$ ) with temperature for “chem-prep” PNZT-HF803 under hydrostatic compression.  $K_A$  and  $K_F$ , are bulk moduli for AFE and FE phases, respectively. The tangent modulus  $K_{FA}$  represents the slope of volumetric strain vs. pressure data during AFE to FE transition phases.**

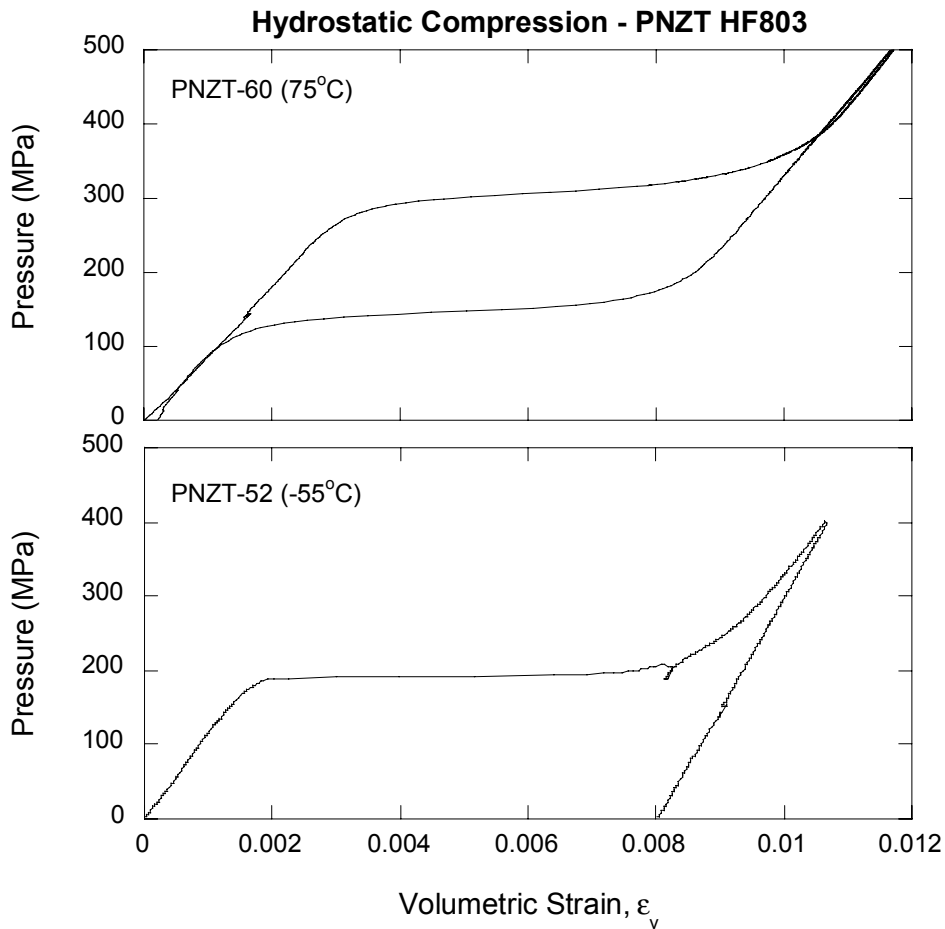
The results described above are consistent with previous observations on specimens of unpoled “mixed-oxide” PNZT ceramic from batch HF453 tested under quasi-static conditions using hydrostatic, uniaxial compression, and constant strain different loading paths. However, a comparison of properties  $K_F$  and  $K_A$  obtained from the hydrostatic loading indicate that material from HF803 appears significantly stiffer than material from HF453. In particular, the value of  $K_F$ , at room temperature, is  $\sim 80$  GPa (see Table 3) for material from HF803 and 64.4 GPa (Zeuch *et al.*, 1999d) for material from HF453. This variation in bulk modulus is significantly larger than would be expected by changing from a “mixed-oxide” to a “chem-prep” process for fabricating the ceramic and is being investigated. As described below, the larger values of the bulk modulus observed for HF803 could possibly be attributed to the material being in a mixed phase, i.e. having both FE and AFE phases present.

The usefulness of PNZT ceramic as sources of shock activated electrical power sources is due to the close proximity of the free energies of the FE and AFE phases. It is quite possible to fabricate material as a mixture of the two phases due to the close proximity of the free energies. Because the free energy of the AFE phase is so close to the free energy of the FE phase it is relatively easy to induce an AFE-to-FE phase transformation by the application of an electric field. Consequently, the poling process used to prepare the PNZT material for use as shock activated electrical power sources can convert a mixed phase unpoled ceramic material into a single phase poled FE ceramic. The electromechanical characteristics for HF803 listed in Table 1 indicate that this material is entirely in the FE phase after electrical poling.

It is useful to examine the volume strain on transform from the FE to the AFE phase. Unit cell volumes for the FE and AFE phases are  $71.32 \text{ \AA}^3$  and  $70.59 \text{ \AA}^3$  (Tuttle *et al.*, 2000), consequently the volume strain associated with the phase transformation should be approximately 1 % in solid material. However, the “mixed-oxide” and “chem-prep” materials are porous with the average densities of HF453 and HF803 being about 7.3 and 7.4  $\text{gm/cm}^3$ . Based in a theoretical solid density of about 8.0  $\text{g/cm}^3$  the initial distention ratios for HF453 and HF803 are about 1.096 and 1.081. The initial distention ratio,  $\alpha_0$ , for a material is calculated as the ratio of its theoretical solid density and initial porous density. If we assume that the distention ratio does not significantly change when the material transforms from the FE to the AFE phase, it would be expected that both materials exhibit similar volumetric transformation strains of roughly 1 %. The volumetric transformation strains observed at room temperature for HF453 and HF803 are roughly 0.9 % and 0.7 %. The smaller value of transformation strain observed for HF453 and HF803 indicates the possible presence of some material in the AFE phase

## Phase Reversal and Temperatures

After the transformation was completed at pressure  $P_{T2}^H$ , the hydrostatic pressure was increased up to 500 MPa following the upward slope of bulk modulus  $K_A$  of the ceramic in AFE phase. Upon depressurization, the volumetric strain was partially recovered following the downward slope of  $K_A$ . At high temperatures above the ambient condition, the phase transformation was reversible from AFE to FE. At low temperatures, the FE to AFE transition became permanent and the ceramic did not reverse to FE phase even after the hydrostatic pressure had been removed. Figure 11 shows an example of the P- $\epsilon_v$  plots from two hydrostatic compression experiments for bounding temperature range of -55 to 75°C.



**Figure 11. Examples of reversibility of phase transformation (AFE to FE) under hydrostatic loading for bounding temperature range of -55 to 75°C. At 75°C PNZT-60 specimen shows a complete reversal of the phase transformation. In contrast at -55°C, the transformation strain (about 0.8%) and the FE to AFE phase transformation were permanent.**

## 3.2 Unconfined uniaxial compression tests

Uniaxial compression experiments were conducted on unpoled PNZT specimens at three different temperatures of -55, 25 and 75°C. Acoustic velocity and strain measurements were used to measure changes in elastic properties and strains associated with dipole reorientation (or domain switching) and also phase transformation. The stress-strain records and the acoustic velocity data for all UC experiments are shown in Appendix B.

The specimens were prepared in the form of rectangular parallelepipeds with the same specifications used for other types of testing (HC and CSD). The uniaxial compression tests were carried out in an environmental chamber adapted to a 0.1 MN servo-controlled loading machine (Figure 12). The temperature changes in the chamber were controlled by heating elements and a forced circulation of liquid nitrogen. The thermocouple, placed inside the chamber close to the specimen, constantly measured the air temperature and provided feedback signal to the temperature controller. Two through-wall ports, opened in the vertical direction of the chamber, accommodated the loading pistons.

The instrumented specimen (see Figure 2 in Chapter 1) was placed between the upper and lower loading pistons and loaded until it failed. The axial and lateral deformations were measured from a pair of axial and lateral strain gages, respectively. A pair of acoustic transducers measured changes of P-wave velocities perpendicular to the loading direction. The data acquisition system for measuring P-wave velocities was based on an 8-bit waveform digitizer at sampling rate up to  $5 \times 10^9$  samples/s.

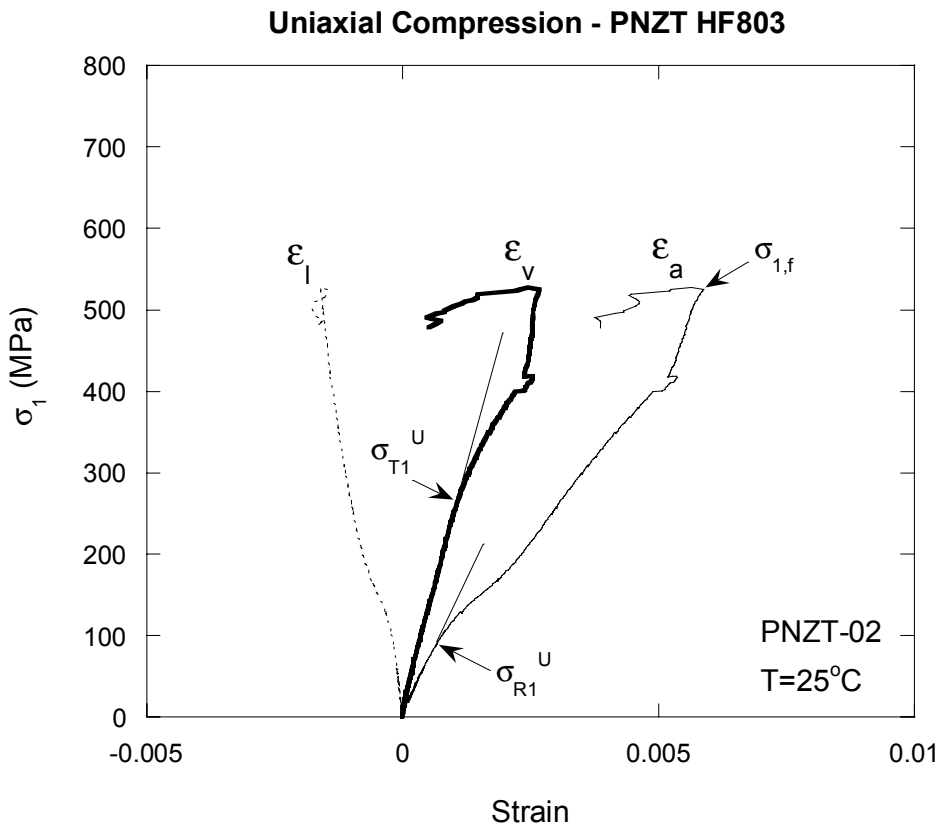


**Figure 12.** A uniaxial compression test set-up consisting of a 0.1 MN load-frame and an environmental chamber for temperature control.

## Stress-Strain Relationships during UC

A typical uniaxial compression experiment conducted on unpoled PNZT ceramic from batch HF803 is shown in Figure 13. The major principal stress,  $\sigma_1$ , applied axially to the specimen is plotted against axial ( $\epsilon_a$ ) and lateral ( $\epsilon_l$ ) strains, respectively. The volumetric strain ( $\epsilon_v = \epsilon_a + 2\epsilon_l$ ) is also plotted. The failure of the specimen is indicated as the peak of the stress-strain curve and the corresponding major principal stress is shown as  $\sigma_{1,f}$ .

As the axial stress is increased,  $\epsilon_a$  and  $\epsilon_l$  behave linearly up to the onset of nonlinear behavior indicated as  $\sigma_{R1}^U$ . The stress level corresponding to  $\sigma_{R1}^U$  is well below the stress level required for phase transformation,  $\sigma_{T1}^U$ , identified as the onset of deviation in the linear trend of  $\sigma_1$  vs.  $\epsilon_v$ . The stress-strain behavior past  $\sigma_{R1}^U$  is that  $\epsilon_a$  becomes more compressive and  $\epsilon_l$  becomes more tensile compared to elastic responses of the “chem-prep” PNZT specimen. However, each axial and lateral component of strains behaves proportionally, therefore, overall linear trend of the volumetric strain is maintained until the phase transformation initiates at  $\sigma_{T1}^U$  as shown in Figure 13.



**Figure 13. Typical uniaxial compression experiment on unpoled PNZT-HF803 ceramic. The major principal stress,  $\sigma_1$ , is plotted against axial ( $\epsilon_a$ ), lateral ( $\epsilon_l$ ) and volumetric ( $\epsilon_v$ ) strains, respectively. The major principal stress corresponding to the failure of the ceramic is indicated as  $\sigma_{1,f}$ . The major principal stress required for dipole reorientation under uniaxial compression is shown as  $\sigma_{R1}^U$ . The major principal stress for the initiation of FE to AFE phase transformation under uniaxial compression is indicated as  $\sigma_{T1}^U$ .**

According to Fritz (1979), uniaxial compression results of this nature indicate dipole reorientation in a low stress regime before phase transformation occurs. Our experimental observation in PNZT-02 shown in Figure 13 is in excellent accordance with the characteristics of isovolumetric phenomenon of dipole reorientation. Moreover, as the axial stress is increased past dipole reorientation in PNZT-02, the phase transformation is indicated as the onset of nonlinear response in the  $\sigma_1$ - $\epsilon_v$  plot. However, the volume reduction at the phase transformation in UC tests is not as significant as in HC or in CSD tests. The volume change in UC tests at phase transformation is the net result of volume reduction caused by phase transformation superimposed on the dilatation of the specimen caused by shear stress.

## **Effects of Temperatures in UC**

The summary of uniaxial compression tests at different temperatures is shown in Table 4. As indicated in Table 4 and Figure 14, the phenomenon of dipole reorientation is not evident in the stress-strain plot at low temperatures. Our uniaxial compression tests based on stress-strain ( $\epsilon_a$ ,  $\epsilon_l$  and  $\epsilon_v$ ) results show that at low temperatures (-55°C) dipole reorientation starting at lower stress levels than phase transformation is effectively suppressed and only the phase transformation occurs. We could not observe any nonlinear behavior in  $\epsilon_a$  and  $\epsilon_l$  at lower stress levels before the phase transformation occurring at  $\sigma_{T1}^U$ .

Figure 15 shows the P-wave velocity normalized to the baseline P-wave velocity measured for the unstrained PNZT ceramic. Although acoustic velocity measurements during UC tests (Appendix B) did not show consistent data, with a significant amount of scatter in them, it appears that the effect of dipole reorientation in P-wave velocity can be seen in test PNZT-01 at an ambient temperature of 25°C. At low stress level below 200 MPa of axial stress, P-wave velocity begins to decrease as observed by Fritz (1979). At high stress level above 200 MPa of axial stress, P-wave velocity starts to increase due to FE to AFE phase transformation.

**Table 4. Summary of phase transformation and dipole reorientation in “chem-prep” PNZT-HF803 under uniaxial compression (UC).**

Specimen no.	Temperature (°C)	$\sigma_{1,f}$ (MPa)	$\sigma_{R1}^U$ (MPa)	$\sigma_{T1}^U$ (MPa)	$\sigma_{Tm}^U$ (MPa)	$P_{T1}^H$ (MPa)	$P_{T2}^H$ (MPa)
PNZT-04	-55	754	NA	160	53	189	196
PNZT-71	-55	703	NA	160	53	189	196
PNZT-01	25	536	110	250	83	248	259
PNZT-02	25	527	90	250	83	248	259
PNZT-06	75	495	85	310	103	291	329

$\sigma_{1,f}^U$  - major principal stress corresponding to the peak of the stress-strain curve

$\sigma_{R1}^U$  - major principal stress required for dipole reorientation under uniaxial compression

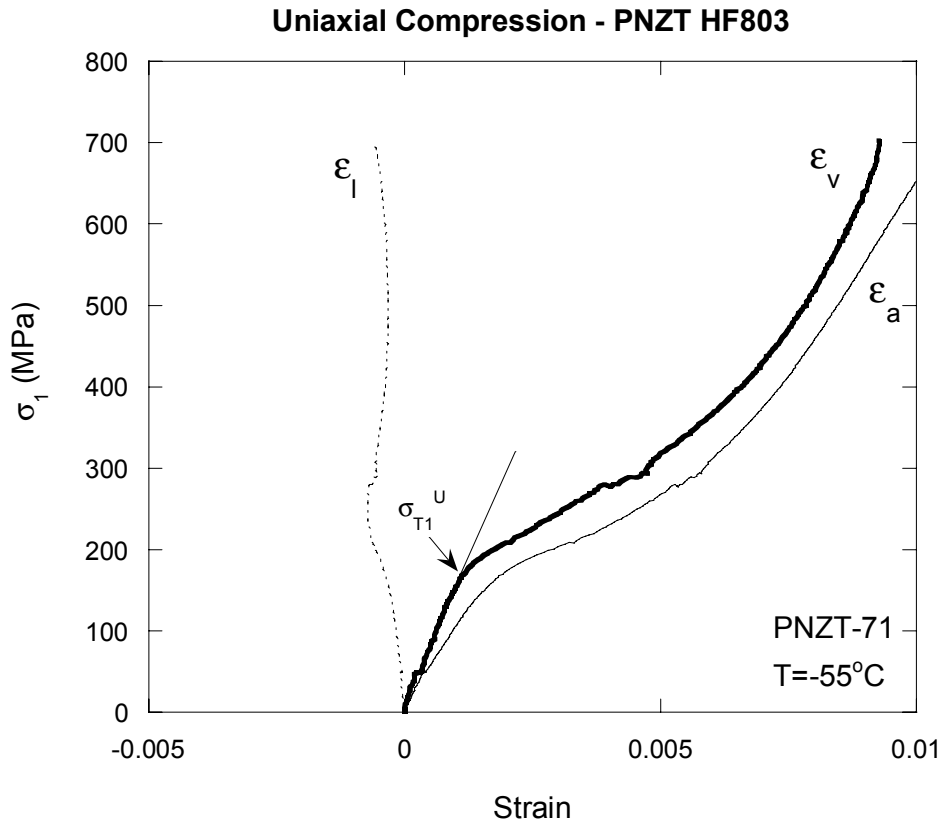
$\sigma_{T1}^U$  - major principal stress required for FE to AFE phase transformation under uniaxial compression

$\sigma_{Tm}^U$  - mean stress required for FE to AFE phase transformation under uniaxial compression

$P_{T1}^H$  - pressure for initiation of FE to AFE phase transformation under hydrostatic compression

$P_{T2}^H$  - pressure for completion of FE to AFE phase transformation under hydrostatic compression





**Figure 14. Typical uniaxial compression experiment on unpoled PNZT-HF803 ceramic at low temperature (-55°C). The major principal stress,  $\sigma_1$ , is plotted against axial ( $\epsilon_a$ ), lateral ( $\epsilon_l$ ) and volumetric ( $\epsilon_v$ ) strains, respectively. The major principal stress for the initiation of FE to AFE phase transformation under uniaxial compression is indicated as  $\sigma_{T1}^U$ .**

For the PNZT-04 specimen at a low temperature (-55°C), it appears that dipole reorientation is suppressed and the P-wave velocity remains unchanged until FE to AFE phase transformation. The other three tests display discontinuous responses in P-wave velocity with large scatter. Therefore, the significance in test results is in doubt (see Appendix B). A definite conclusion in dipole reorientation may be obtained if the uncertainties in identifying the P-wave arrival time are reduced.

Figure 16 shows variation of failure strength, phase transformation, and dipole reorientation with respect to temperature in uniaxial compression of “chem-prep” PNZT-HF803. The uniaxial compressive strength of PNZT-HF803 ranges from 500 to 750 MPa and is inversely related with temperature.

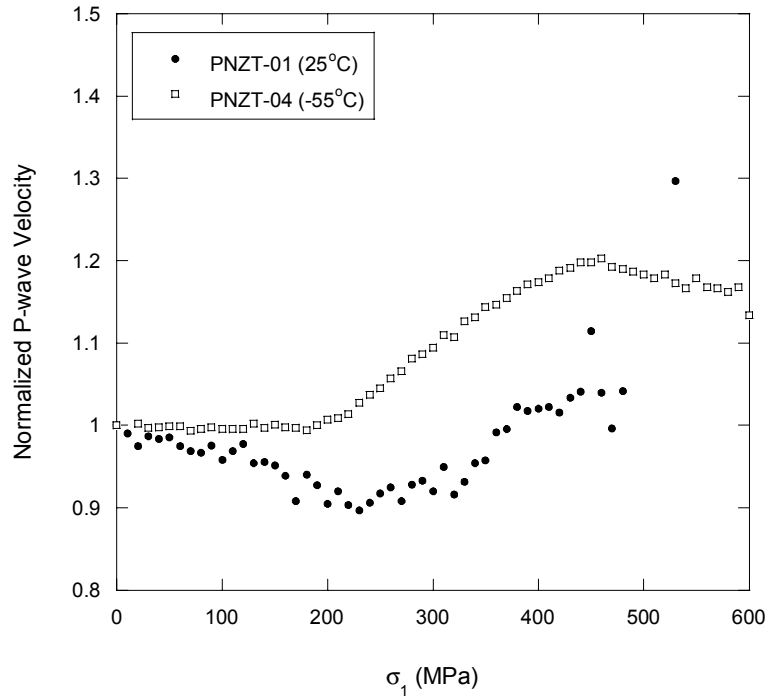


Figure 15. Changes in P-wave velocities with respect to applied axial stress ( $\sigma_1$ ) on unpoled PNZT-HF803 ceramic. The normalized P-wave velocities are the ratio of P-wave velocities to the baseline P-wave velocities measured at zero stress.

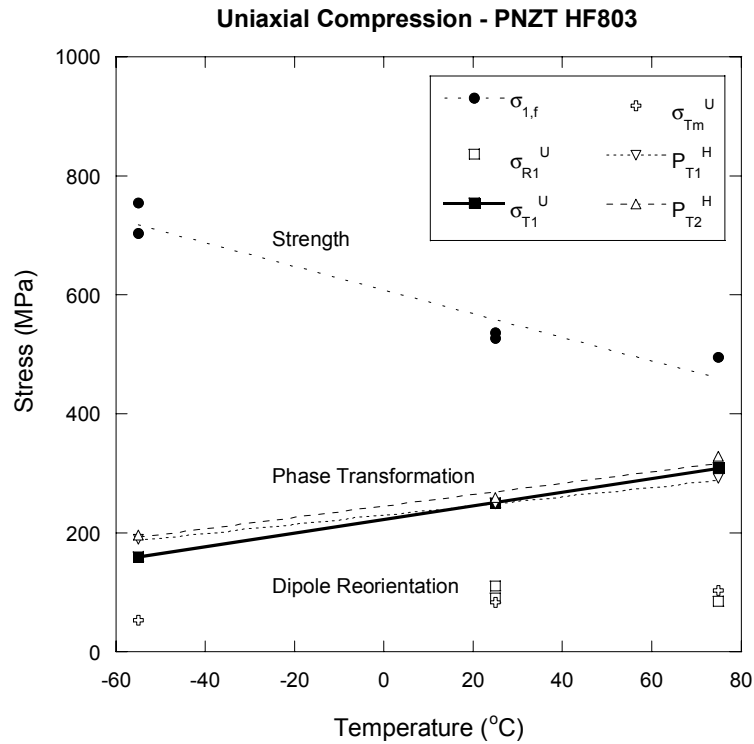


Figure 16. Effects of temperature on failure strength ( $\sigma_{1,f}$ ), phase transformation pressures ( $P_{T1}^H$ ,  $P_{T2}^H$ ,  $\sigma_{T1}^U$  and  $\sigma_{Tm}^U$ ) and dipole reorientation pressures ( $\sigma_{R1}^U$ ) in uniaxial compression of “chem-prep” PNZT-HF803.

## Maximum Stress Criterion for Phase Transformation

For comparison purposes, the pressures required for the onset ( $P_{T1}^H$ ) and completion ( $P_{T2}^H$ ) of FE to AFE phase transformation under hydrostatic compression are shown in the same plot. Also the mean stresses ( $\sigma_{Tm}^U = \sigma_{T1}^U/3$ ) for phase transformation under uniaxial compression are plotted. The maximum principal stress at phase transformation ( $\sigma_{T1}^U$ ) under uniaxial compression is in good accordance with the phase transformation pressures ( $P_{T1}^H$  and  $P_{T2}^H$ ) under hydrostatic compression. Figure 16 also shows that the stress at dipole reorientation ( $\sigma_{R1}^U$ ), is approximately one third of the phase transformation stress ( $\sigma_{T1}^U$ ). Therefore,  $\sigma_{R1}^U$  is in general agreement with  $\sigma_{Tm}^U$ .

Figures 17 and 18 compare  $\sigma$ - $\epsilon_v$  behavior in uniaxial compression on unpoled PNZT and hydrostatic compression on the same material at the same temperature. In Figure 17 the phase transformation data are plotted in terms of the mean stress and the volumetric strain. In Figure 18, the same data are plotted in terms of the major principal stress and the volumetric strain. The comparison of these two plots clearly demonstrates that in unpoled “chem-prep” PNZT-HF803, the phase transformation occurs when the major principal stress equals the hydrostatic pressure at which the transformation otherwise takes place.

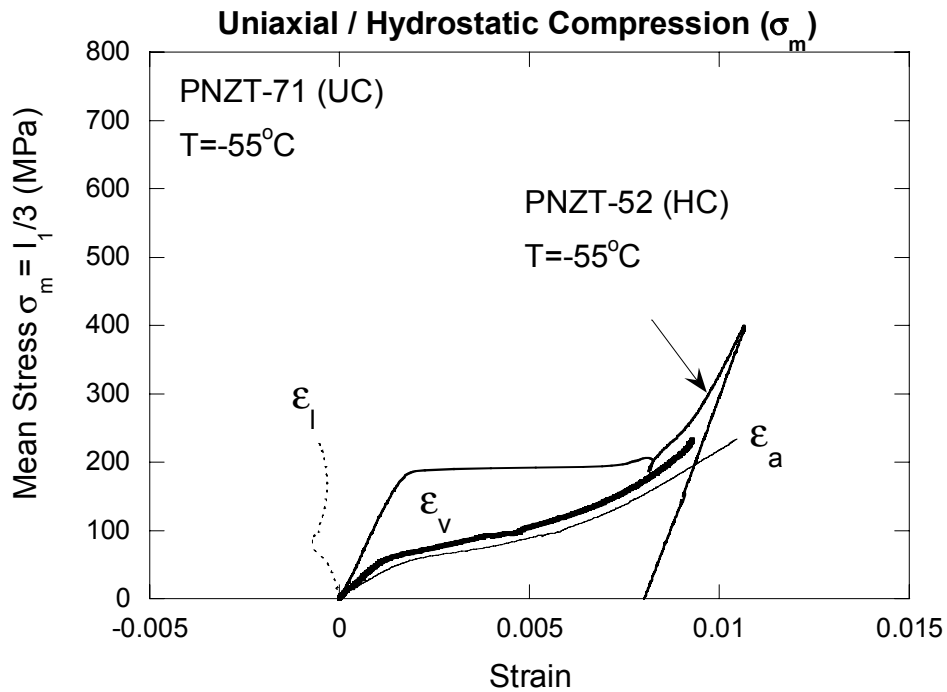
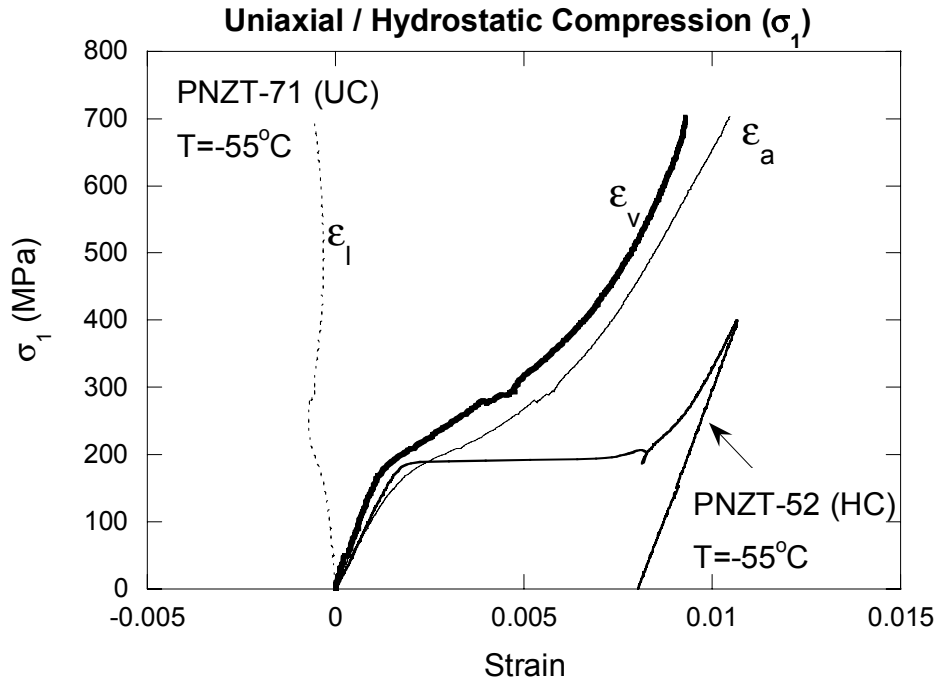


Figure 17. Comparison of stress-strain plots obtained during uniaxial compression with hydrostatic compression experiment using mean stress ( $\sigma_m = \frac{\sigma_1 + \sigma_2 + \sigma_3}{3}$ ). Shown are the axial strain ( $\epsilon_a$ ); lateral strain ( $\epsilon_l$ ); and volumetric strain ( $\epsilon_v$ ).



**Figure 18. Comparison of stress-strain plots obtained during uniaxial compression with hydrostatic compression experiment using major principal stress ( $\sigma_1$ ). Shown are the axial strain ( $\epsilon_a$ ); lateral strain ( $\epsilon_l$ ); and volumetric strain ( $\epsilon_v$ ).**

### 3.3 Constant stress difference tests

Constant-Stress-Difference experiments (Zeuch *et al.*, 1999a) were conducted to characterize the effects of nonhydrostatic loading on the phase transformation of the “chem-prep” PNZT-HF803. The sample preparation procedures and test equipment for the CSD tests were identical to those used for the HC and UC tests described in previous Chapter 2.4.

The typical loading path for the CSD test is shown in Figure 19. The PNZT-10 specimen was hydrostatically compressed to 69 MPa which is far below the expected transformation pressure under hydrostatic loading ( $P_T^{HC} \sim 250$  MPa). While the confining pressure,  $\sigma_3$ , was kept constant at 69 MPa, the axial stress,  $\sigma_1$ , was increased to 119 MPa creating the stress difference ( $\sigma_d = \sigma_1 - \sigma_3 = 50$  MPa). Then, both  $\sigma_1$  and  $\sigma_3$  were increased simultaneously at the same rate. As the mean stress was increased without changing the shear stress, the maximum principal stress reached the critical stress for FE to AFE phase transformation under CSD condition.

Appendix C shows the loading paths used for the CSD testing. Four levels of stress differences 50, 100, 150, and 200 MPa were used. Figures 20 and 21 show the complete  $\sigma_3$ - $\epsilon$  and  $\sigma_1$ - $\epsilon$  plots obtained from PNZT-10 experiment, respectively. As in the HC tests, the phase transformation is indicated as the abrupt increase in strains approximately at 250 MPa of  $\sigma_1$  or 200 MPa of  $\sigma_3$ .

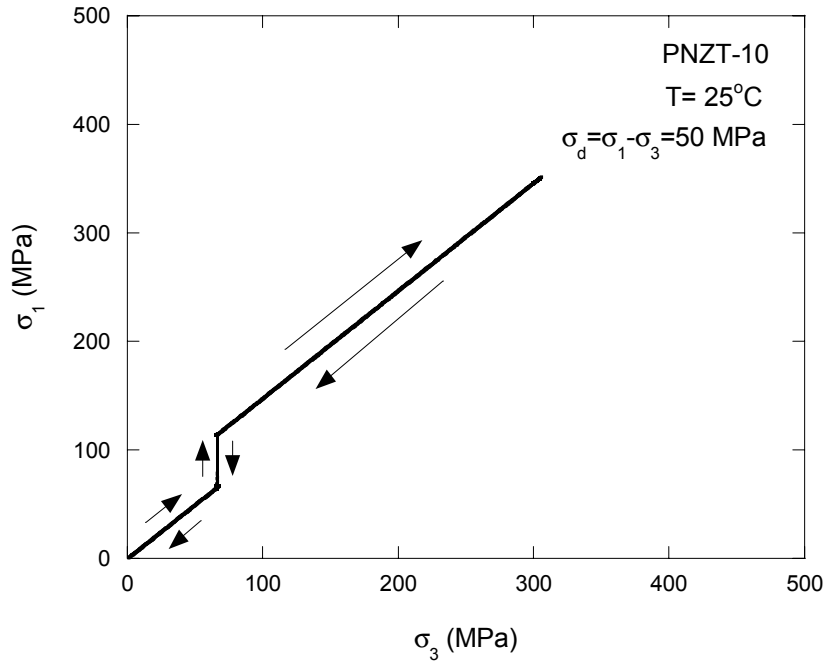


Figure 19. A loading path obtained from the Constant Stress Difference test PNZT-10 conducted at 50 MPa stress difference ( $\sigma_d = \sigma_1 - \sigma_3$ ). The unloading path is not discernable from the loading path since the unloading path exactly followed over the loading path in reverse direction.

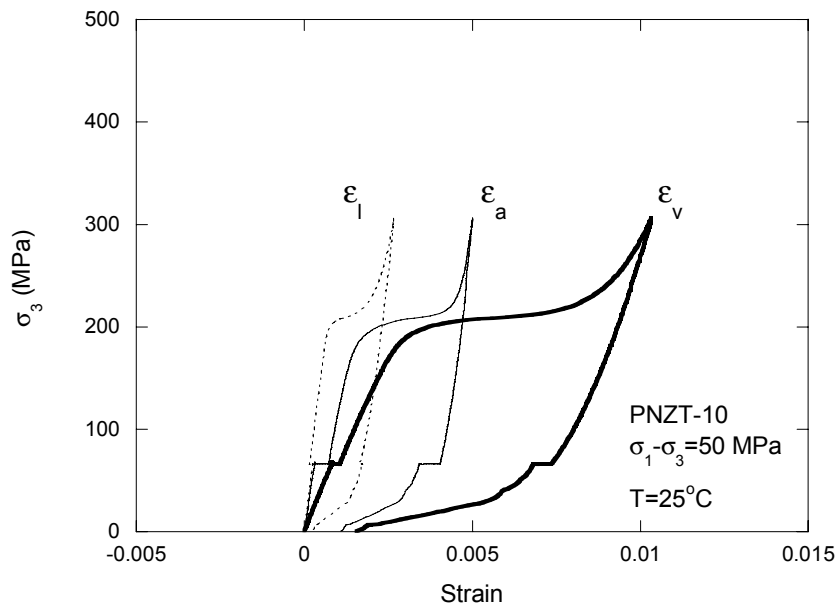
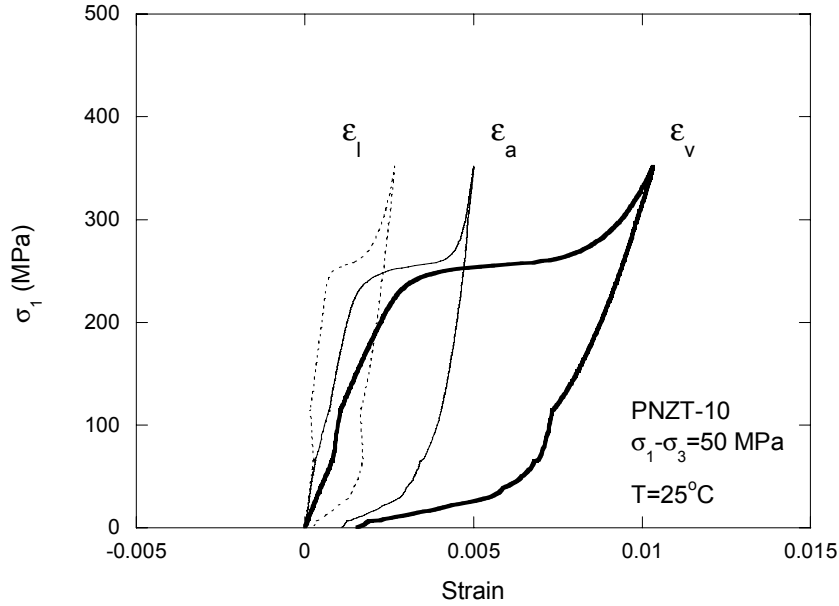


Figure 20. Minimum compressive stress ( $\sigma_3$ )-strain responses of the unpoled “chem-prep” PNZT-HF803 under CSD experiment. Initiation of phase transformation is represented by increase in axial ( $\epsilon_a$ ), lateral ( $\epsilon_l$ ), and volumetric ( $\epsilon_v$ ) strains around 200 MPa of  $\sigma_3$ .



**Figure 21. Maximum compressive stress ( $\sigma_1$ )-strain responses of the unpoled “chem-prep” PNZT-HF803 under CSD experiment. Initiation of phase transformation is represented by increase in axial ( $\epsilon_a$ ), lateral ( $\epsilon_l$ ), and volumetric ( $\epsilon_v$ ) strains around 250 MPa of  $\sigma_1$ .**

In order to study the effects of temperature in the CSD testing, we conducted a series of CSD tests for the temperature range of  $-55$  to  $75^\circ\text{C}$ . Figures 22, 23, and 24 show the mean stress-volumetric strain plots of the CSD testing conducted at three different levels of temperatures (low  $-55^\circ\text{C}$ , ambient  $25^\circ\text{C}$ , and high  $75^\circ\text{C}$ ), respectively. For each temperature group, a HC test ( $\sigma_d = \sigma_1 - \sigma_3 = 0$ ) is also shown to compare with data obtained with the stress differences from 50 to 200 MPa. The results are summarized in Table 5 and Figures 22, 23, and 24.

A comparison of bulk moduli,  $K_F$  and  $K_A$ , obtained under identical temperature and  $\sigma_d$  condition shows that the scatters of  $K_F$  and  $K_A$  are large. This may indicate the amount of sample to sample variation of the phase mixture. The cause of sample to sample variations in bulk moduli is the subject of further investigation.

As in the HC tests, the phase transformation of the “chem-prep” PNZT-HF803 under CSD condition was identified as the sudden increase in volumetric strain of the specimen ranging from 0.3 to 0.8 %. At low temperature, the volumetric strain at phase transformation was about 0.8 %. The volumetric strain was slightly reduced to 0.7 % for ambient temperature. At high temperature, FE to AFE transition was gradual with indistinct onset of phase transformation. As a result, the range of corresponding volumetric strain reduction varied widely from 0.3 to 0.7 %.

At the low temperature bound ( $-55^\circ\text{C}$ ), FE to AFE phase transformation was permanent under set temperature condition. Even though the stresses on the specimen returned to the initial condition, the ceramic did not revert to FE phase. Figure 22 shows that approximately 0.75% of irreversible volumetric strain remained even after the specimen was completely

unloaded. However, at ambient temperature (25°C) and at the upper temperature bound (75°C), the FE to AFE phase transformation became reversible. Figures 23 and 24 show that an insignificant amount of permanent volumetric strain remained after the stresses were removed. As the stresses were reversed, the AFE to FE phase transformation occurred with a gradual decrease in volumetric strain.

Figure 25 shows the effect of temperature on the levels of critical stresses required for the phase transformation of the “chem-*prep*” PNZT-HF803 under CSD condition. Both the maximum stress ( $\sigma_{T1}^{CSD}$ ) and the mean stress ( $\sigma_{Tm}^{CSD}$ ) for FE to AFE phase transformation increased with temperature under CSD loading conditions. It also shows that the critical pressure,  $P_{T1}^H$ , for FE to AFE phase transformation under hydrostatic loading increased in parallel with  $\sigma_{T1}^{CSD}$  and  $\sigma_{Tm}^{CSD}$ . The results shown in Figure 25 clearly indicate that  $\sigma_{Tm}^{CSD}$  underestimates  $P_{T1}^H$ . The results also confirm the previous findings in uniaxial compression that transformation occurs when the maximum compressive stress reaches  $P_{T1}^H$  (Zeuch *et al.*, 1999c).

If we assume that the transformation occurs when the maximum compressive stress reaches the hydrostatic pressure at which transformation would otherwise take place, then the mean stress,  $\sigma_{Tm}^{CSD}$ , at transformation can be represented as follows (Zeuch *et al.*, 1999c):

$$\begin{aligned}
 \sigma_{Tm}^{CSD} &= \frac{(\sigma_{T1}^{CSD} + 2\sigma_3)}{3} \\
 &= \frac{\sigma_{T1}^{CSD} + 2(\sigma_{T1}^{CSD} - \sigma_d)}{3} \\
 &= \sigma_{T1}^{CSD} - \frac{2\sigma_d}{3}
 \end{aligned} \tag{10}$$

Equation 10 shows that the mean stress for transformation will be lowered by two-thirds of the increasing shear stress or stress difference from  $\sigma_{T1}^{CSD}$ . Under HC loading,  $\sigma_{T1}^{CSD}$  becomes same as  $P_{T1}^H$ , pressure required for FE to AFE phase transformation under HC loading. Figure 26 shows the effects of shear stress and temperature on the volumetric strain at the onset of phase transformation. Increasing the temperature from -55 to 75°C clearly increases the volumetric strain at the onset of transformation. Sometimes this phenomenon is described as retardation of transformation. Under set temperature conditions, increasing shear stress linearly decreases the volumetric strain required to trigger FE to AFE phase transformation.

**Table 5. Summary of phase transformation in “chem-prep” PNZT-HF803 under Constant Stress Difference (CSD) loading.**

Specimen no.	Temperature (°C)	$\sigma_d$	$a_1$ (MPa)	$K_F$ (GPa)	$a_2$ (MPa)	$K_{FA}$ (GPa)	$a_3$ (MPa)	$K_A$ (GPa)	$\epsilon_{v1}^{CSD}$	$\sigma_{Tm1}^{CSD}$ (MPa)	$\epsilon_{v2}^{CSD}$	$\sigma_{Tm2}^{CSD}$ (MPa)	$\epsilon_{v2}^{CSD} - \epsilon_{v1}^{CSD}$	$\Delta\sigma_m$ (MPa)	$\sigma_{T1}^{CSD}$	$\sigma_{T2}^{CSD}$
PNZT-52	-55	0	-1.0	115.3	187.2	1.0	-1220.4	151.7	0.0016	189	0.0093	196	0.0077	8	189	196
PNZT-22	-55	50	0.2	101.5	160.0	2.1	-1089.6	140.9	0.0016	163	0.0090	179	0.0074	16	197	212
PNZT-25	-55	100	-0.8	125.0	123.9	5.8	-1364.8	176.1	0.0010	130	0.0087	175	0.0077	45	197	241
PNZT-08	-55	100	-4.4	144.0	124.3	7.0	-1342.2	176.8	0.0009	131	0.0086	185	0.0077	54	198	251
PNZT-27*	-55	150	1.3	106.0	122.8	-0.4	-1328.1	165.9	0.0011	122	0.0087	120	0.0076	-3	222	220
PNZT-28*	-55	150	-1.4	121.8	121.9	-0.2	-1229.4	158.6	0.0010	122	0.0085	120	0.0075	-1	222	220
PNZT-23*	-55	200	0.3	99.5	107.1	5.3	-1395.0	177.8	0.0011	113	0.0087	153	0.0076	40	246	286
PNZT-34	25	0	2.0	84.1	242.9	1.7	-769.0	108.8	0.0029	248	0.0095	259	0.0065	11	248	259
PNZT-17	25	50	4.1	72.8	206.4	3.1	-662.0	99.7	0.0029	215	0.0090	234	0.0061	19	249	268
PNZT-10	25	50	2.5	75.9	207.8	2.9	-749.4	103.4	0.0028	216	0.0095	236	0.0067	20	249	269
PNZT-18	25	100	13.8	78.3	164.5	10.4	-738.7	113.5	0.0022	188	0.0088	255	0.0065	68	254	322
PNZT-15	25	100	6.4	75.8	176.3	7.3	-720.4	103.3	0.0025	194	0.0093	245	0.0069	50	261	311
PNZT-19	25	150	3.7	64.9	148.0	10.1	-736.8	100.3	0.0026	175	0.0098	247	0.0072	72	275	347
PNZT-07	25	150	0.2	93.3	132.2	13.2	-500.1	91.8	0.0016	154	0.0080	238	0.0064	84	254	338
PNZT-11*	25	200	1.6	61.4	51.0	23.6	-535.6	91.0	0.0013	82	0.0087	256	0.0074	174	215	389
PNZT-60	75	0	-1.5	87.4	271.9	5.8	-679.4	101.0	0.0033	291	0.0100	329	0.0066	38	291	329
PNZT-30	75	50	1.2	80.2	250.9	8.1	-512.5	101.0	0.0035	279	0.0082	317	0.0048	38	312	351
PNZT-35	75	50	7.8	69.8	218.3	15.8	-140.6	66.0	0.0039	280	0.0071	331	0.0033	51	313	364
PNZT-31	75	100	-1.6	86.7	230.4	12.6	-400.5	83.2	0.0031	270	0.0089	343	0.0058	73	336	409
PNZT-32	75	150	1.0	85.4	188.8	20.2	-383.0	88.9	0.0029	247	0.0083	357	0.0054	110	347	457
PNZT-36**	75	150	5.4	78.4	71.6	47.3	-199.7	100.1	0.0021	172	0.0051	315	0.0030	142	272	415
PNZT-33**	75	200	1.9	87.3	177.5	21.0	-444.0	86.4	0.0027	233	0.0095	377	0.0068	144	367	510

$K_F$  - bulk modulus in FE (ferroelectric) phase;  $K_A$  - bulk modulus in AFE (antiferroelectric) phase;  $K_{FA}$  - tangent modulus in transition from FE to AFE phase

$a_1$  - extrapolated pressure corresponding to zero volumetric strain in FE phase

$a_2$  - extrapolated pressure corresponding to zero volumetric strain during transition from FE to AFE phase

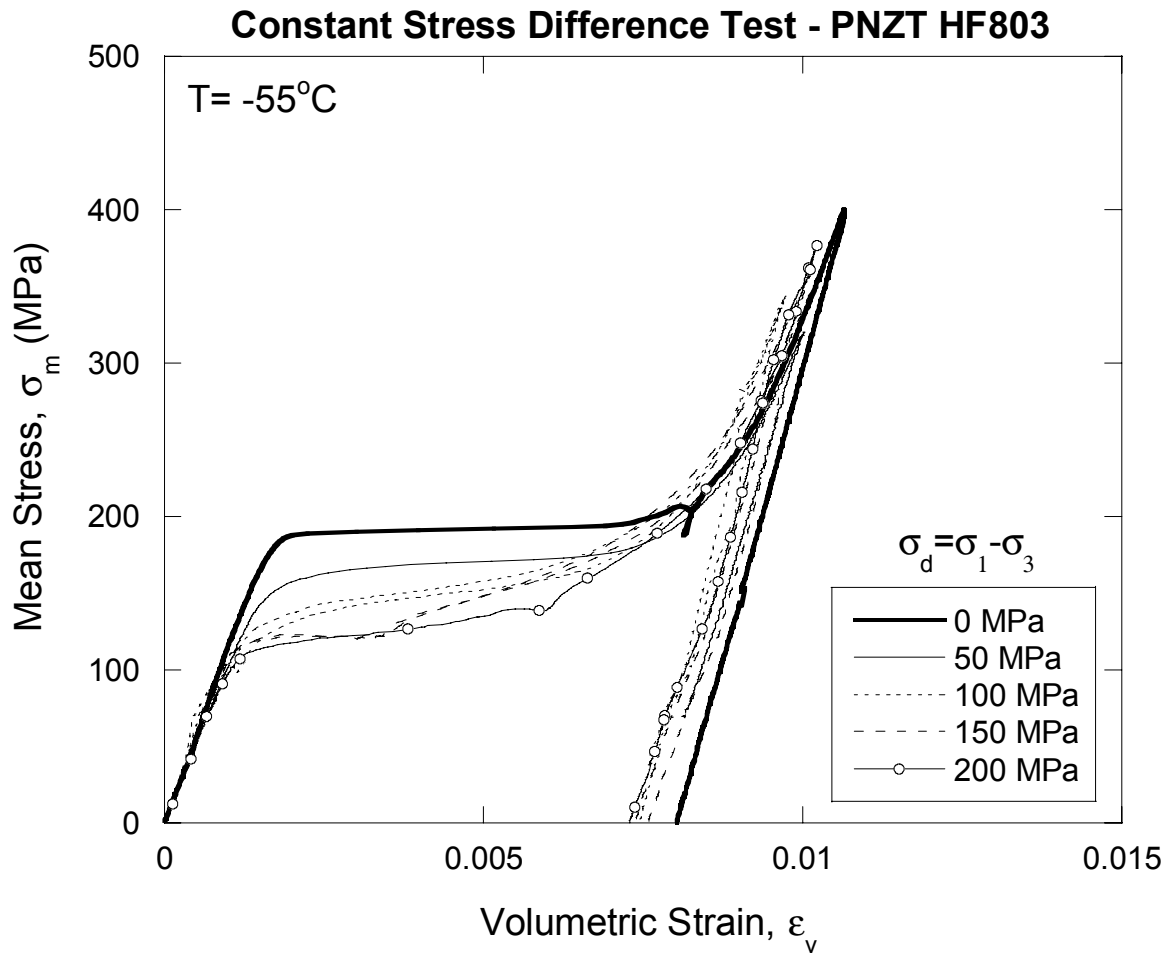
$a_3$  - extrapolated pressure corresponding to zero volumetric strain in AFE phase

$\sigma_{Tm1}^{CSD}$  - mean stress at initiation of FE to AFE phase transformation under CSD compression

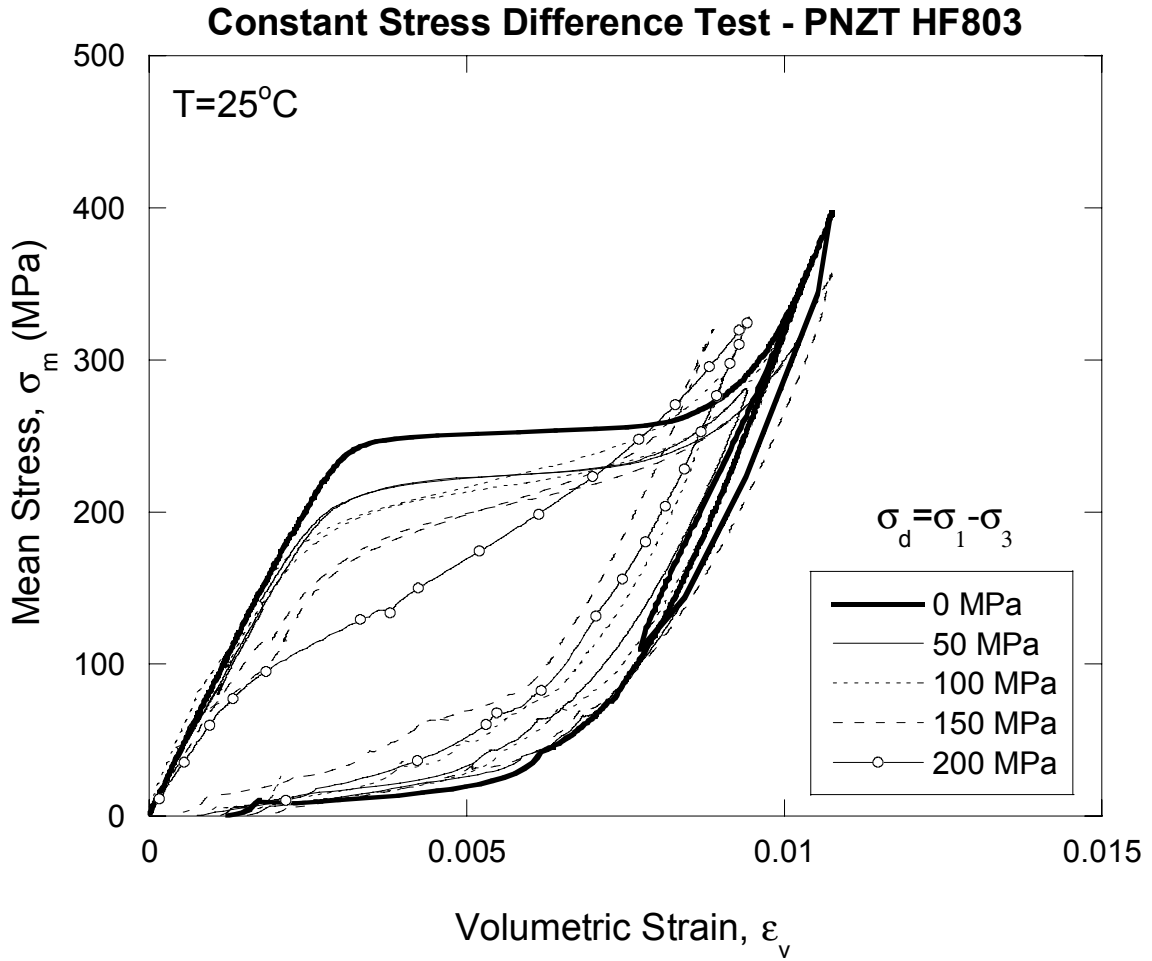
$\sigma_{Tm2}^{CSD}$  - mean stress at completion of FE to AFE phase transformation under CSD compression

$\epsilon_{v1}^{CSD}$  - volumetric strain at  $\sigma_{Tm1}^{CSD}$ ;  $\epsilon_{v2}^{CSD}$  - volumetric strain at  $\sigma_{Tm2}^{CSD}$

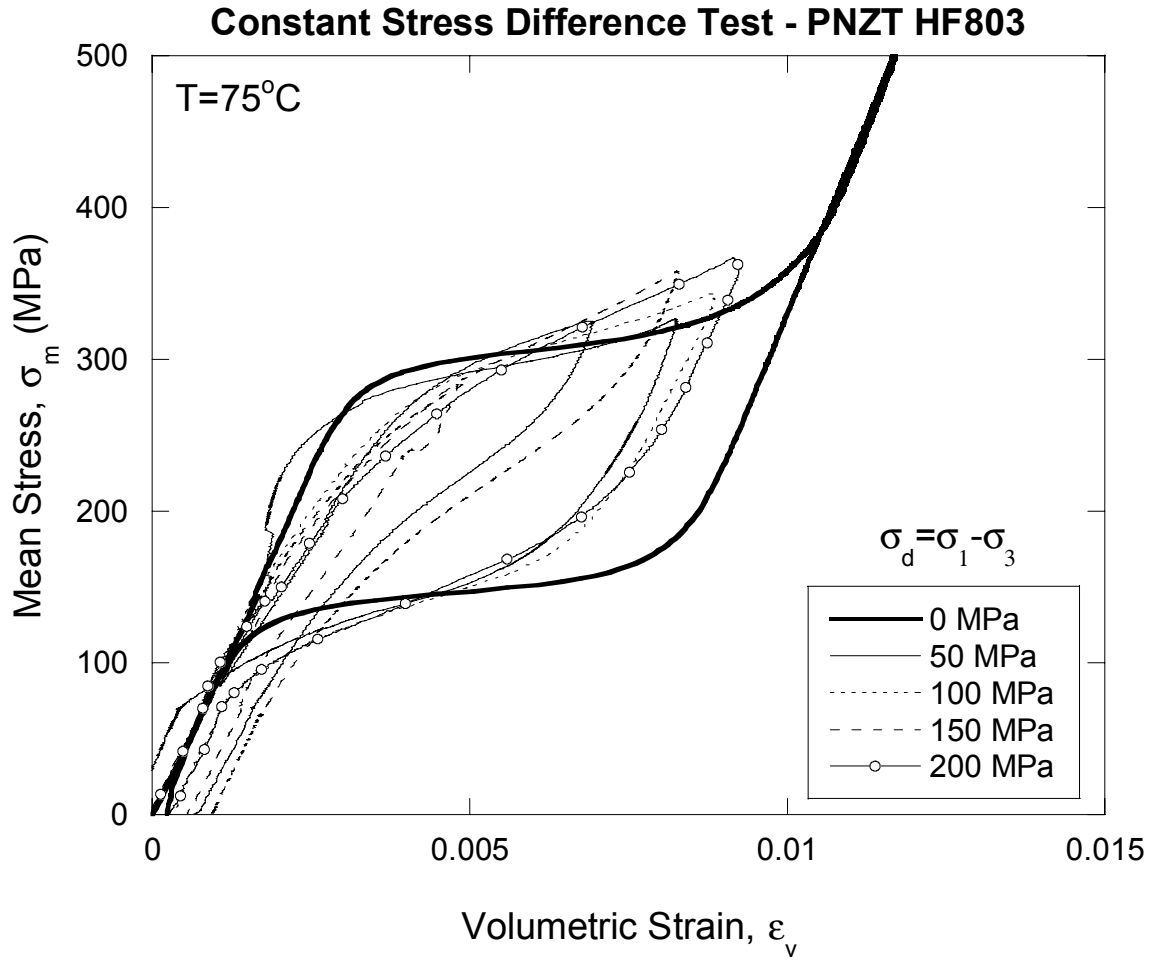




**Figure 22. Mean Stress-volumetric strain plot during constant stress difference test for unpoled “chem-prep” PNZT-HF803 ceramic at low temperature (-55°C).**



**Figure 23. Mean Stress-volumetric strain plot during constant stress difference test for unpoled “chem-prep” PNZT-HF803 ceramic at ambient temperature (25°C).**



**Figure 24. Mean Stress-volumetric strain plot during constant stress difference test for unpoled “chem-prep” PNZT-HF803 ceramic at elevated temperature (75°C).**

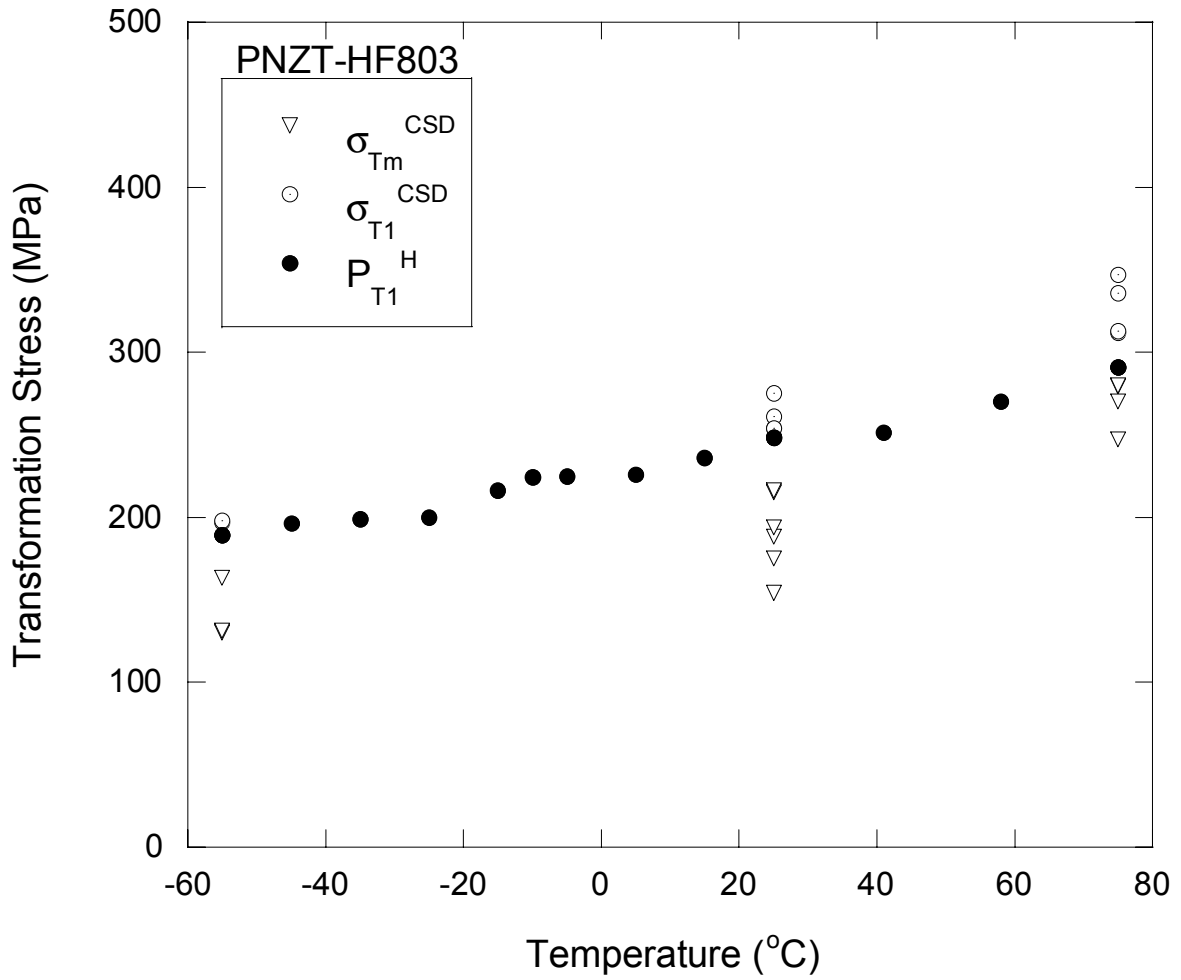
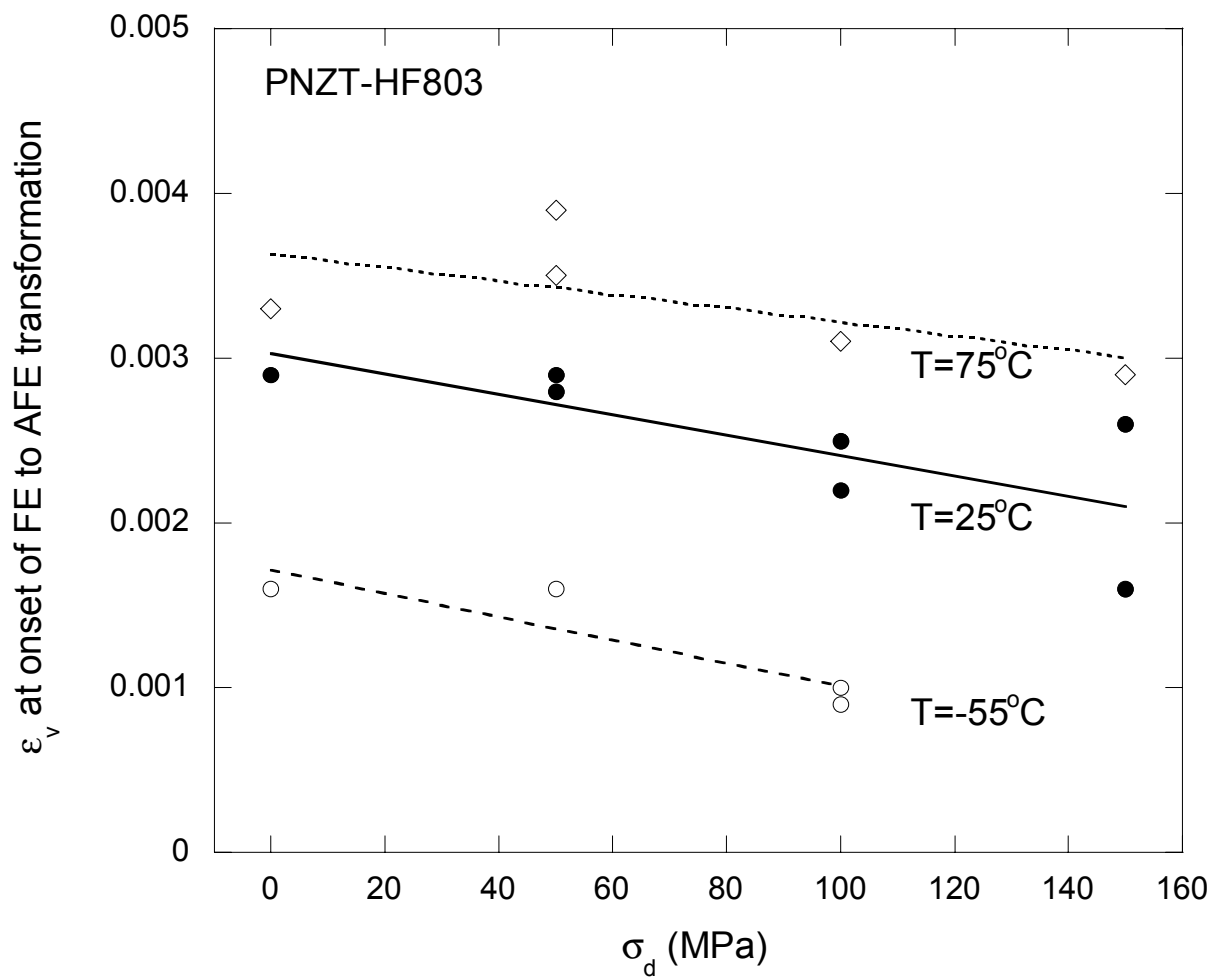


Figure 25. Critical stresses required for phase transformation of “chem-prep” PNZT- HF803 under constant stress difference (circles) and hydrostatic (diamonds) tests.  $\sigma_{Tm}^{CSD}$  is the mean stress for FE to AFE phase transformation under CSD loading,  $\sigma_{T1}^{CSD}$  is the maximum compressive stress for FE to AFE phase transformation under CSD loading, and  $P_{T1}^H$  is the pressure for FE to AFE phase transformation under hydrostatic loading



**Figure 26.** Effects of shear stress and temperature on the volumetric strain,  $\varepsilon_v$ , of “chem-prep” PNZT at the onset of phase transformation.

## 4. Conclusions

The specimens of unpoled “chem-prep” PNZT ceramic from batch HF803 were tested under quasi-static conditions using hydrostatic, uniaxial compression, and constant strain difference loading paths. The stress-strain behavior during the FE to AFE phase transformation was investigated within the temperature range (-55 to 75°C). The results from the laboratory experiments can be summarized as follows:

- The phase transformation occurs when the maximum compressive stress equals the hydrostatic pressure at which the transformation otherwise takes place.
- The pressure required for the onset ( $P_{T1}^H$ ) of the FE to AFE phase transformation under hydrostatic loading is represented by the following linear relationship:

$$P_{T1}^H \text{ (MPa)} = 227 + 0.76 T \text{ (}^\circ\text{C)}$$

- The curved structure in the phase boundary is shown in the completion ( $P_{T2}^H$ ) of the FE to AFE phase transformation. The relationship is:

$$P_{T2}^H \text{ (MPa)} = 232 + 0.83 T + 0.0047 T^2$$

- The volumetric strain for the onset of the FE to AFE transformation increases with temperature.
- The uniaxial compression test shows the isovolumetric phenomenon of dipole reorientation (or domain switching).
- At the low temperature bound (-55°C), the FE to AFE phase transformation is permanent and irreversible. However, at the upper temperature bound (75°C), the phase transformation is reversible from AFE to FE as the stress causing the phase transformation is removed.
- Under constant temperature conditions, increasing shear stress lowers the mean stress and the volumetric strain required to trigger phase transformation.

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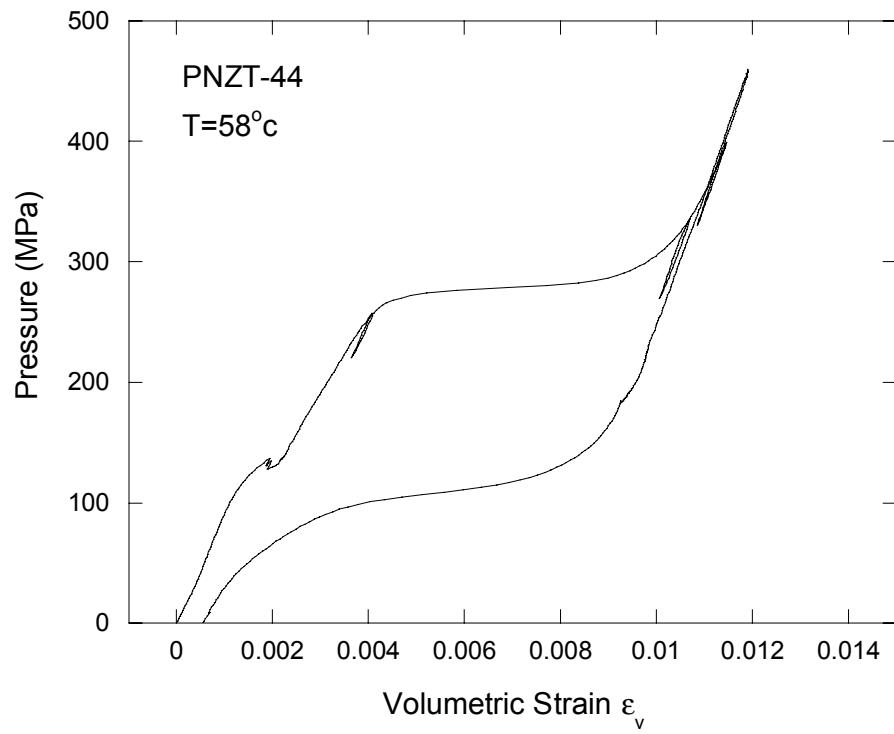
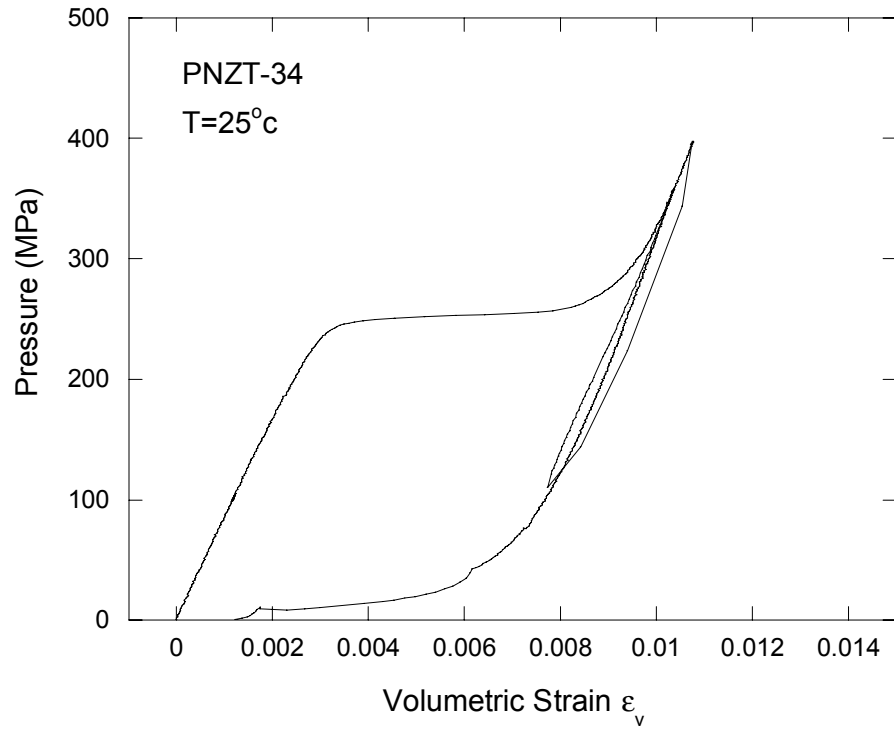
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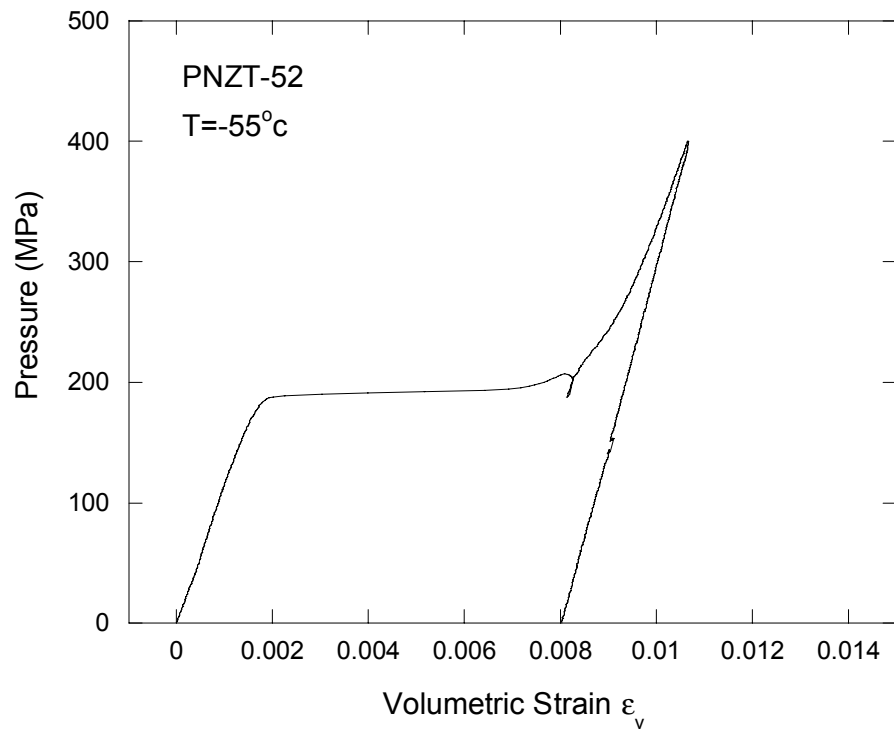
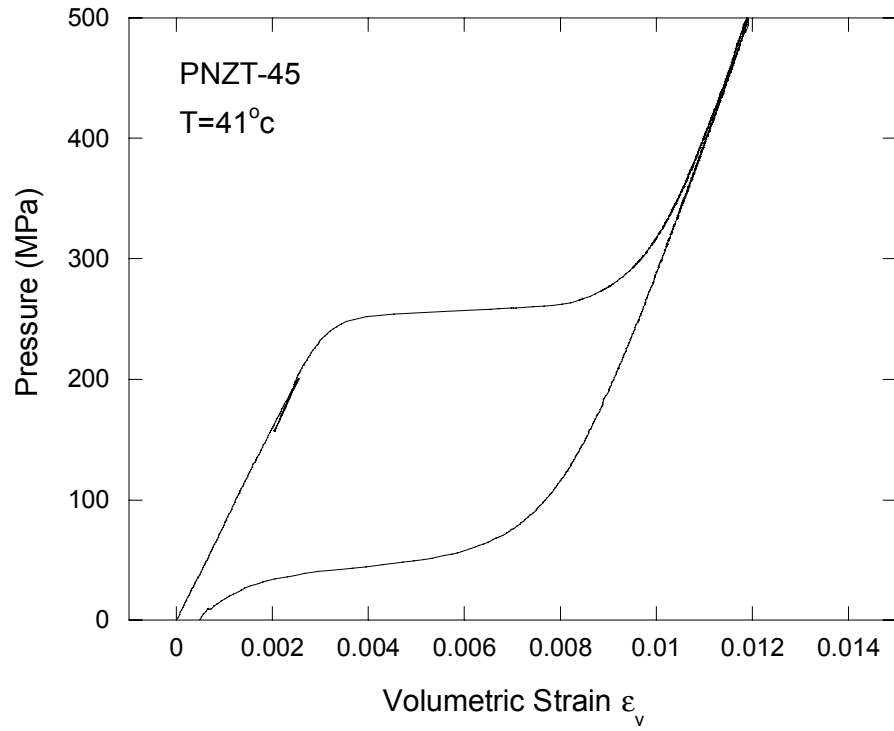
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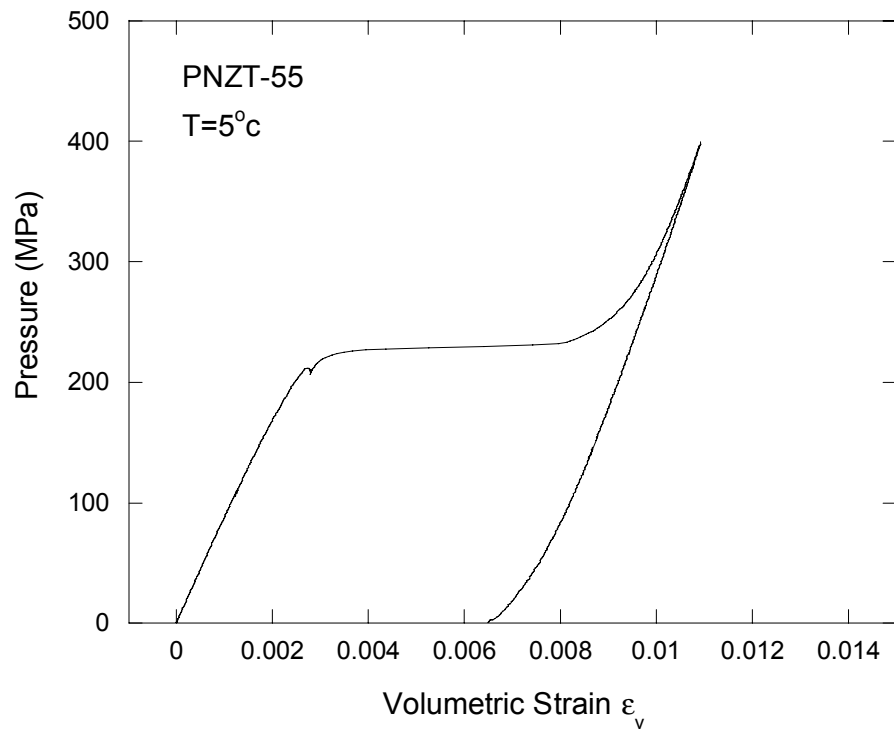
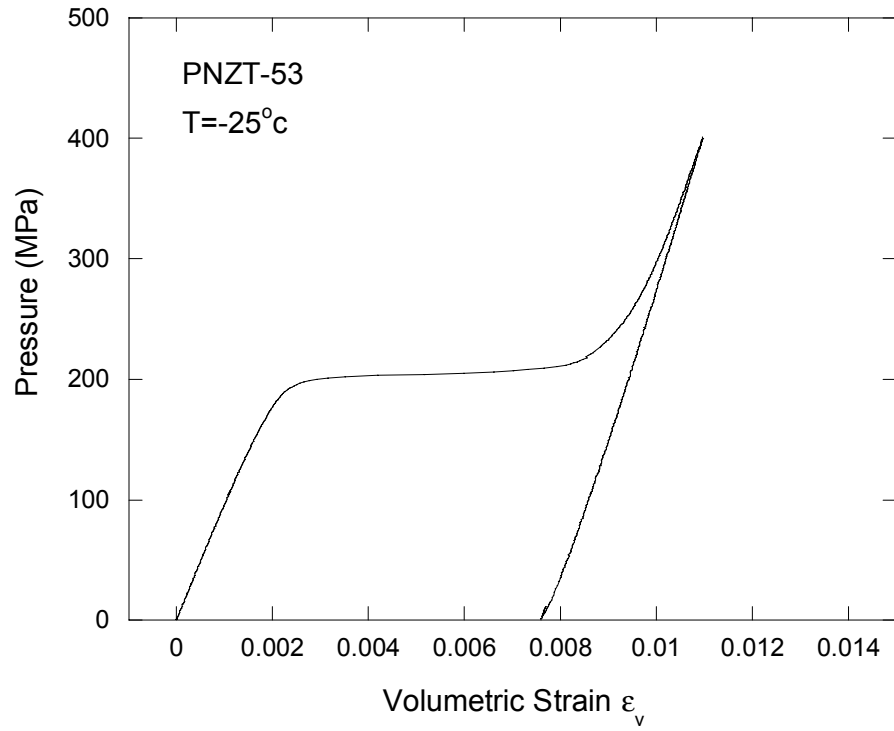


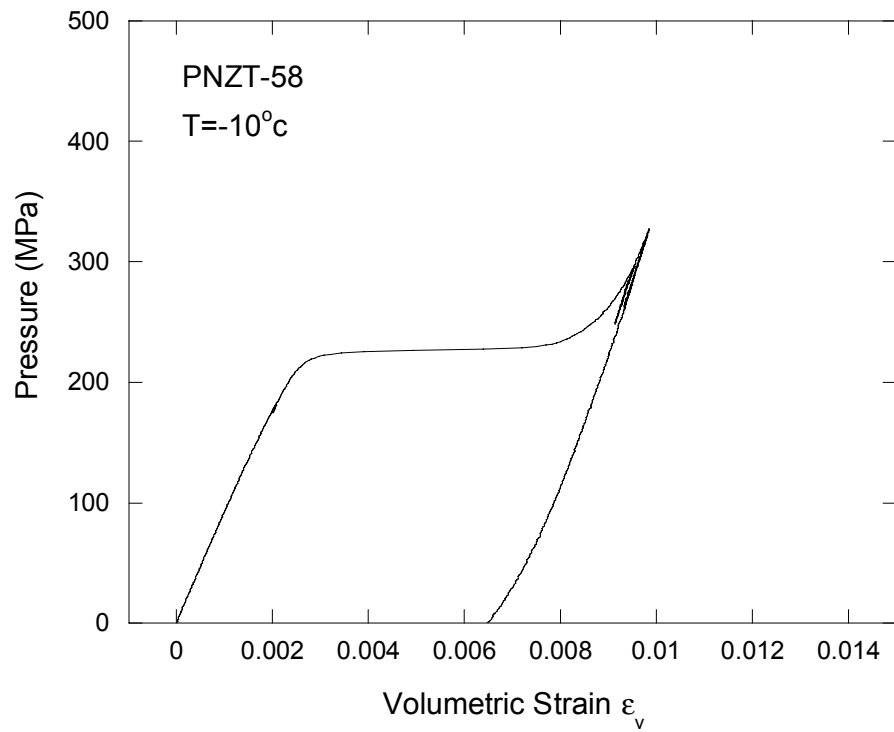
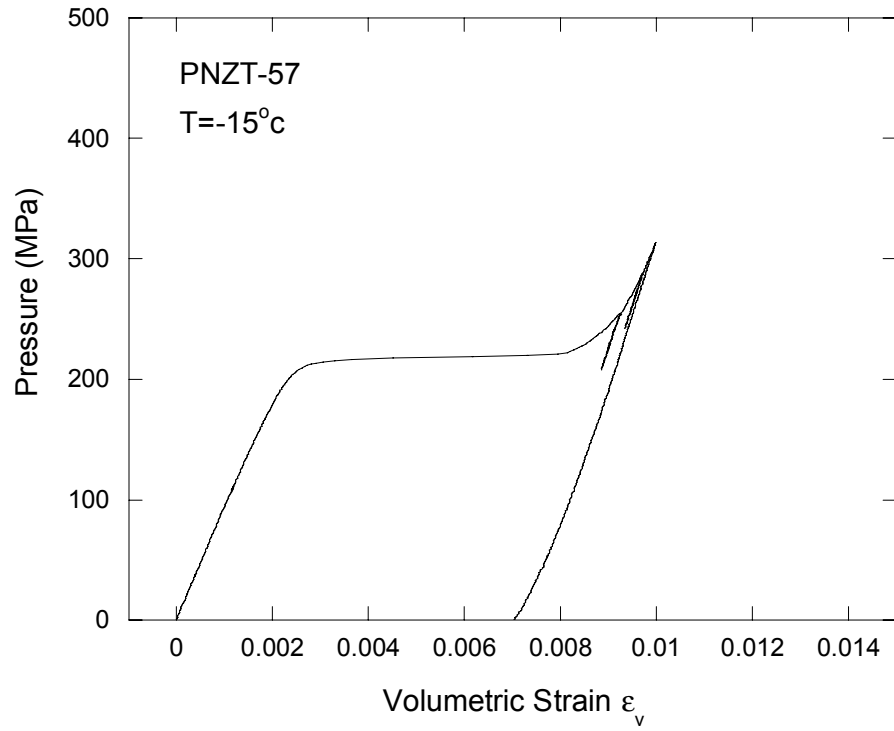
## **APPENDIX A**

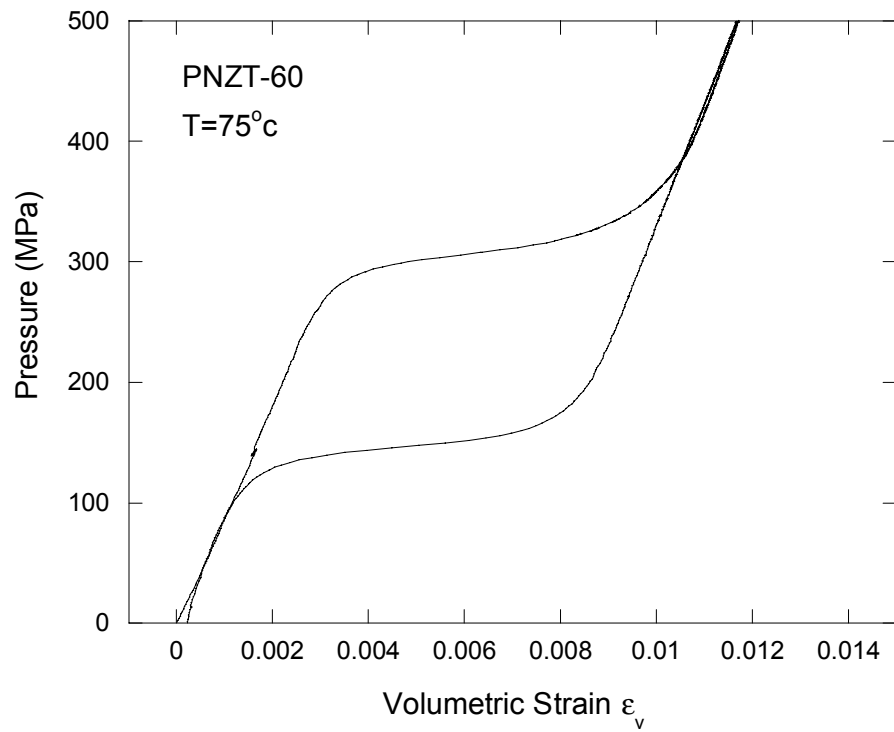
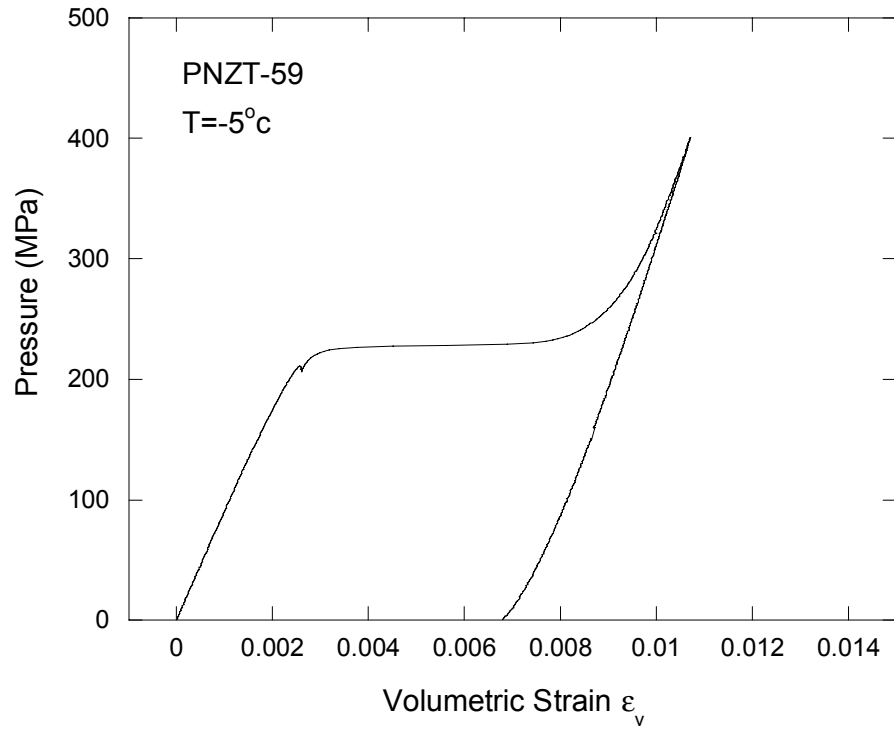
### **Hydrostatic Compression (HC) Test Plots for PNZT-HF803 ( $\epsilon_v$ -volumetric strain and T-temperature)**

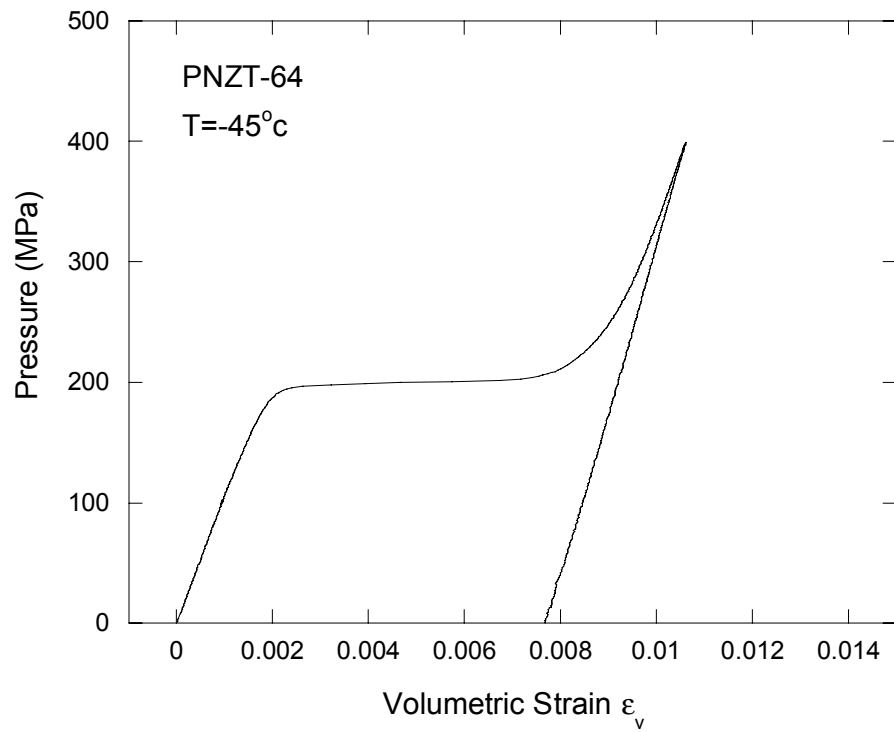
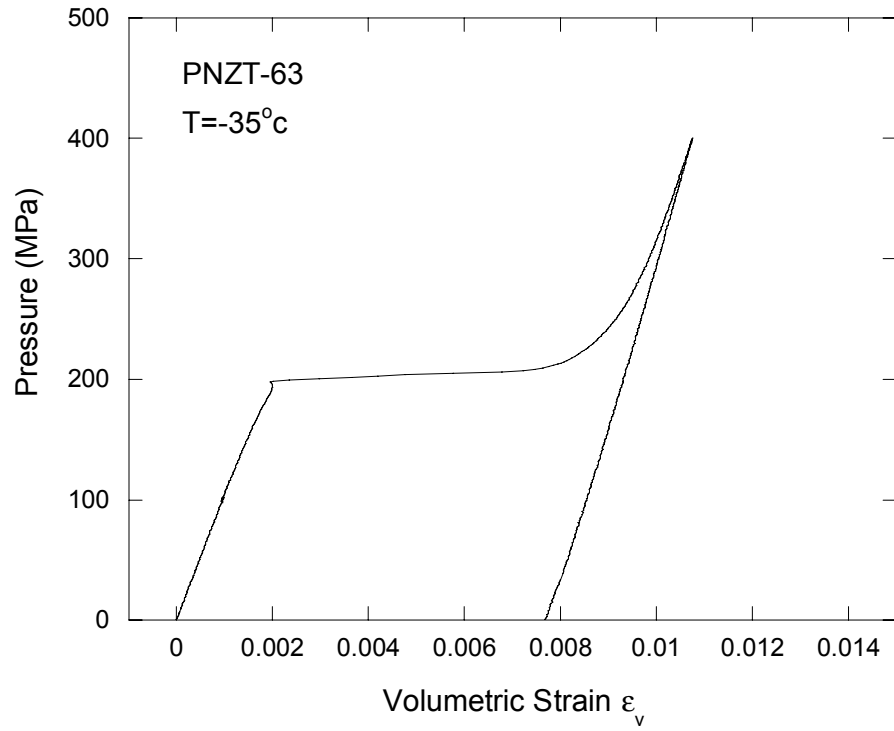


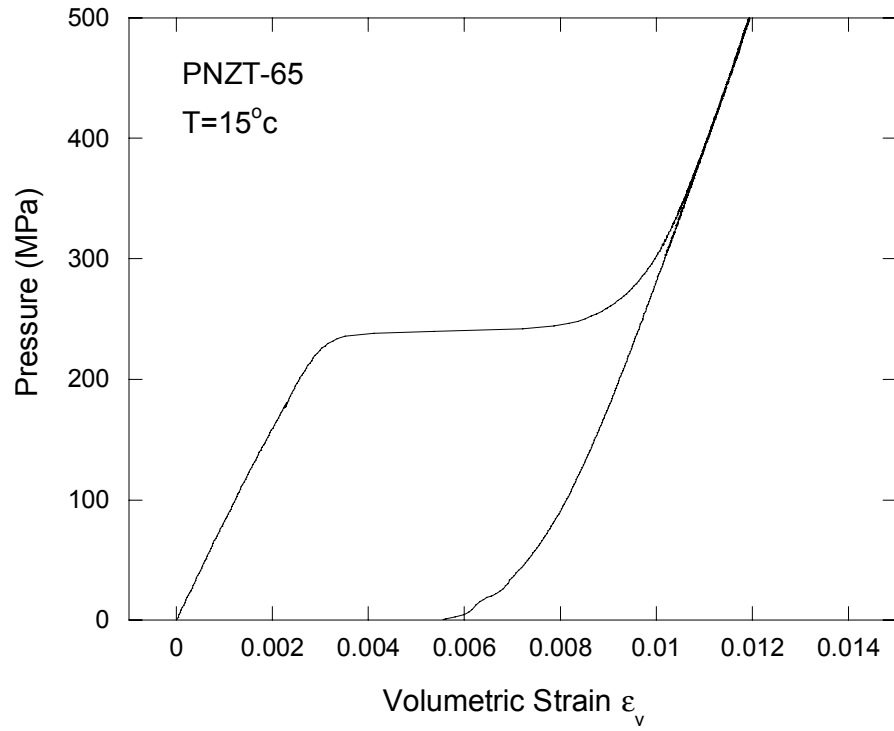










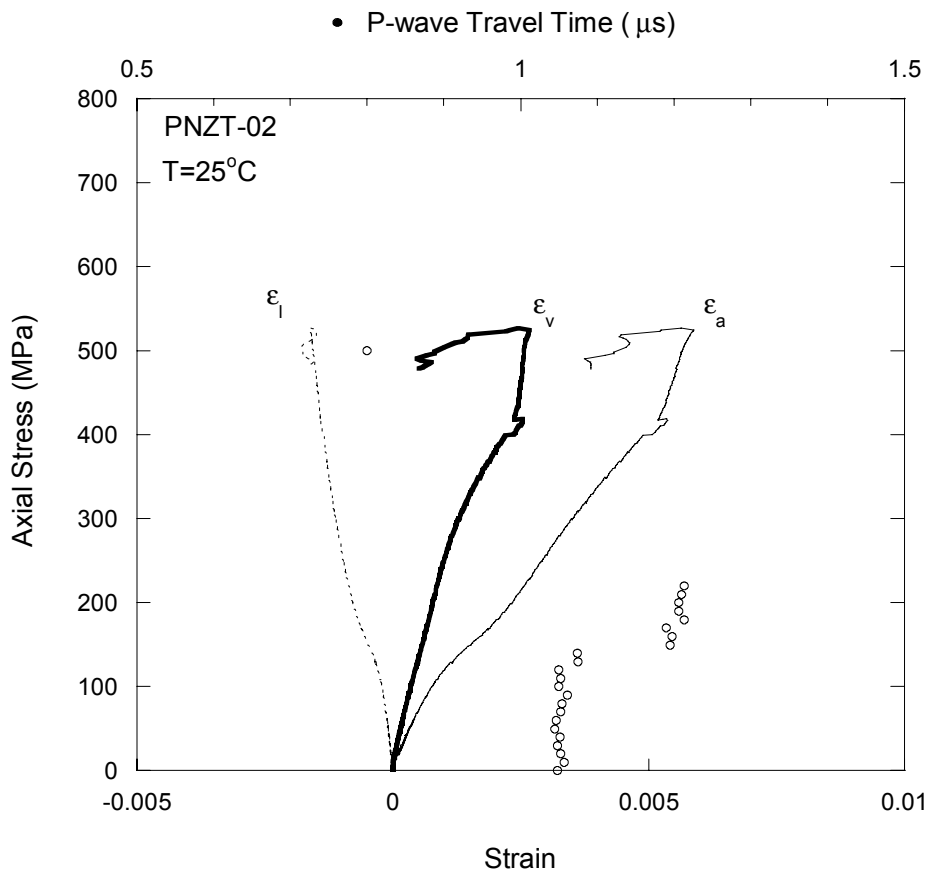
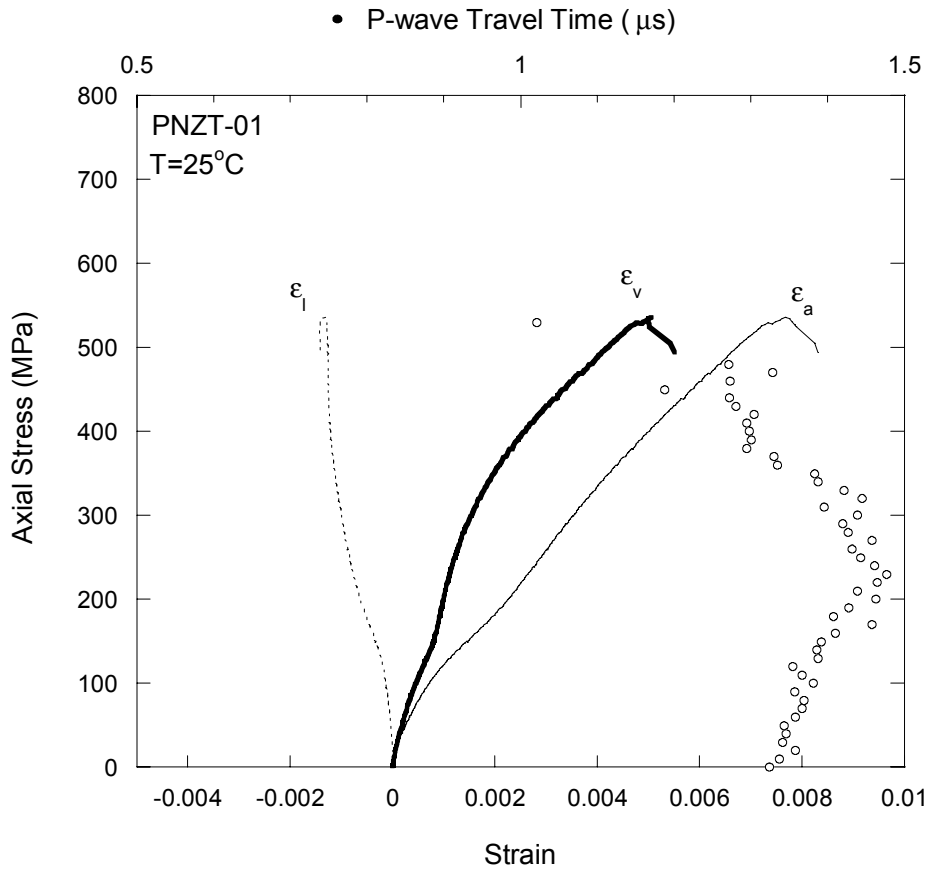


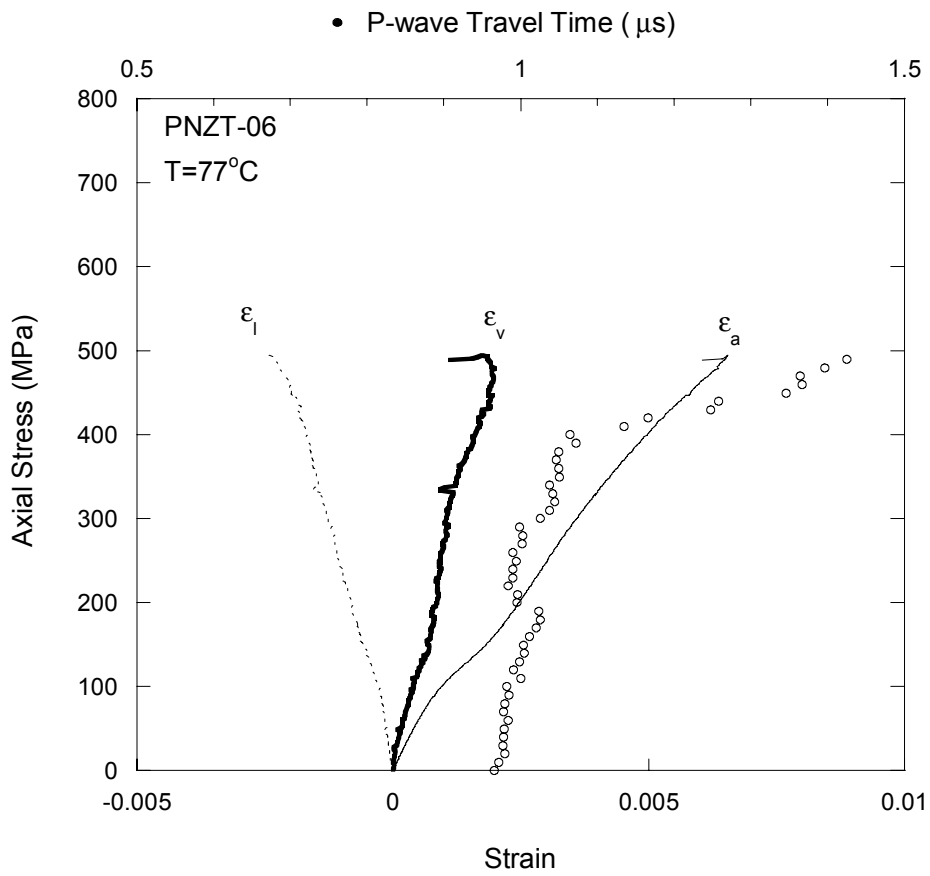
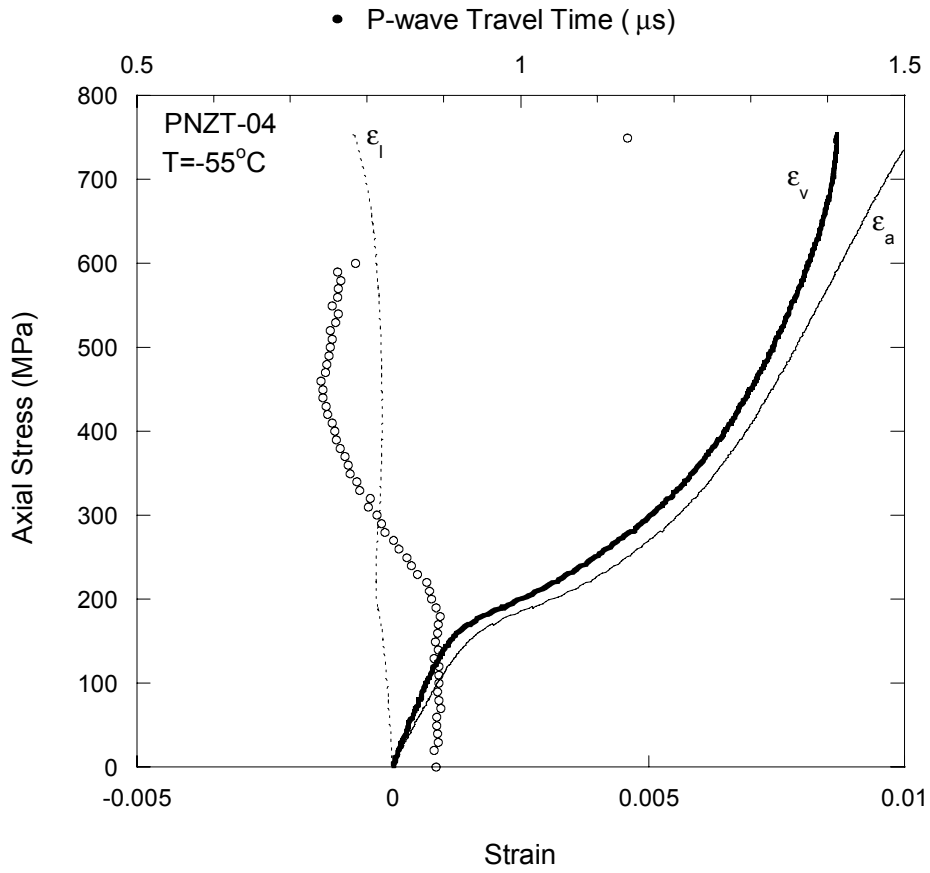


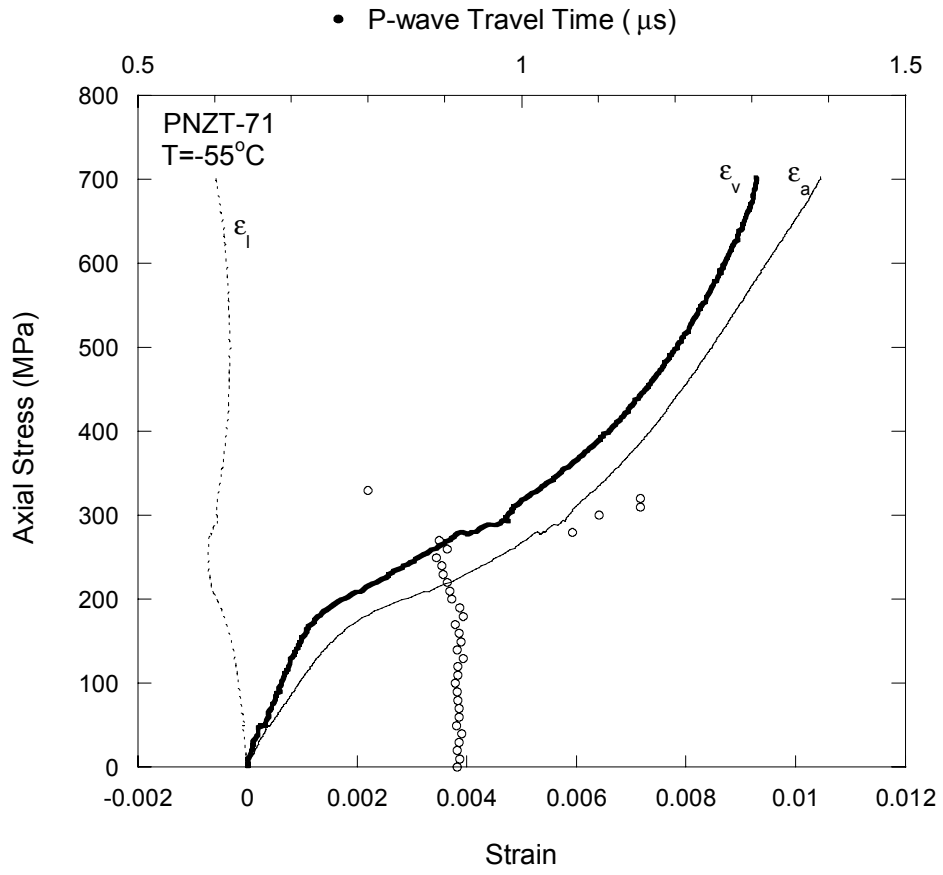
## **APPENDIX B**

### **Uniaxial Compression (UC) Test Plots for PNZT-HF803**

**( $\sigma_1$ -axial stress,  $\varepsilon_a$ -axial strain,  $\varepsilon_l$ -lateral strain,  
 $\varepsilon_v$ -volumetric strain and T-temperature)**



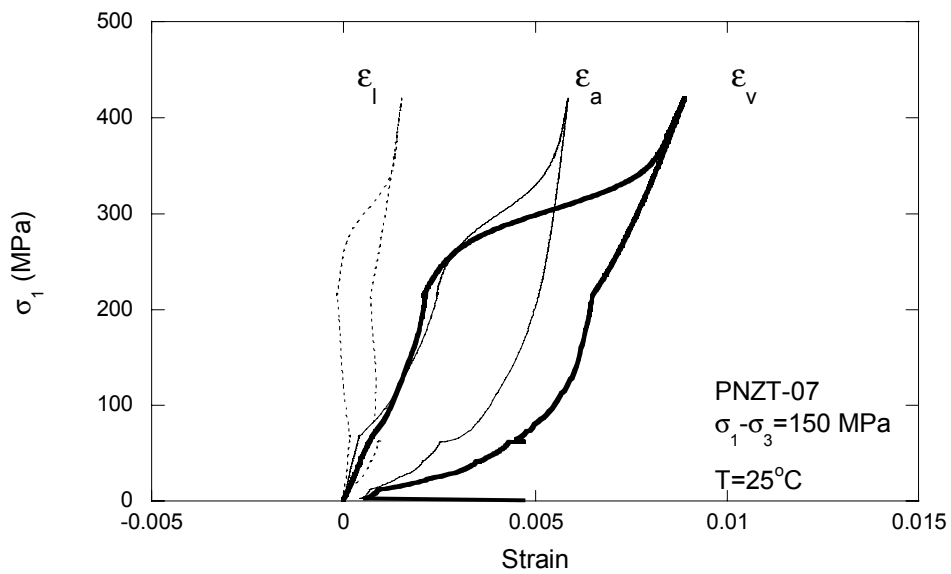
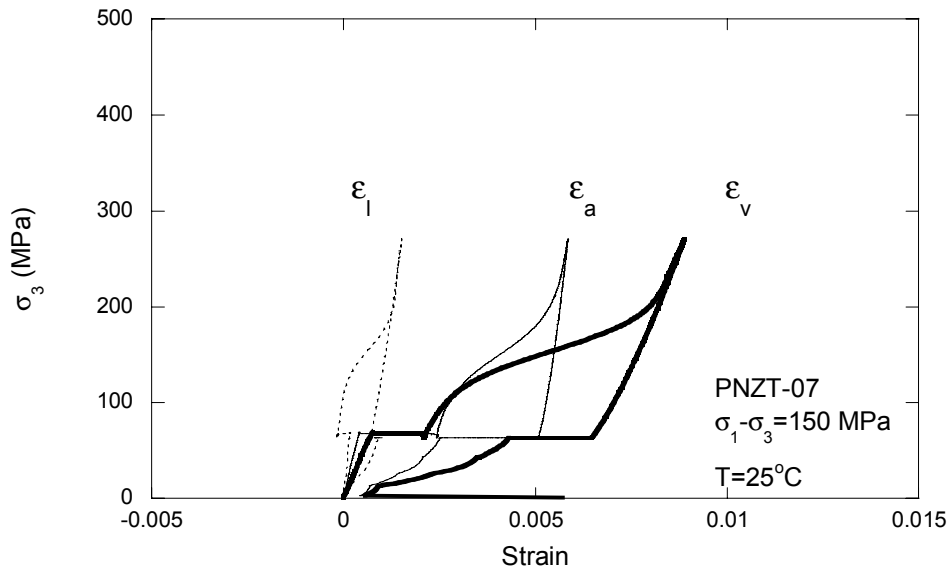
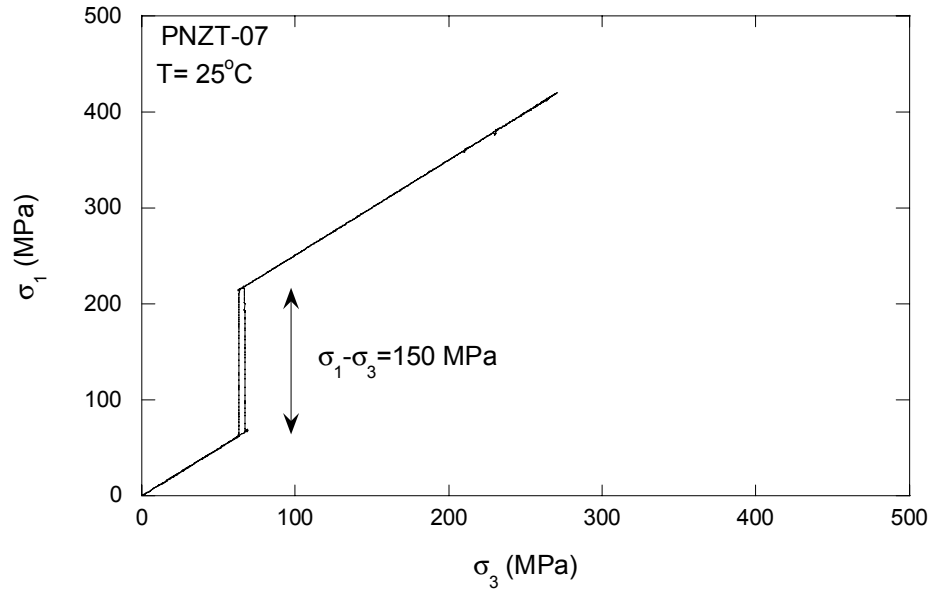


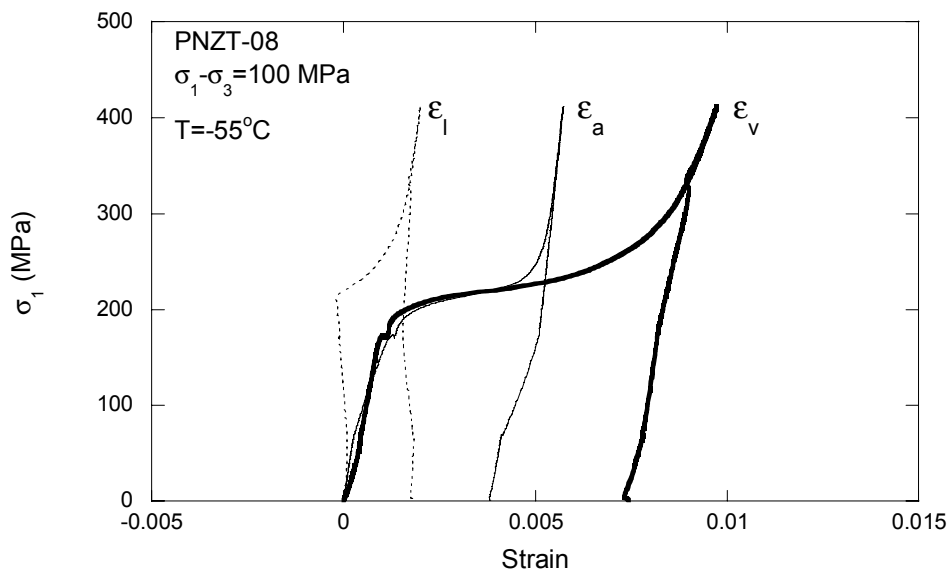
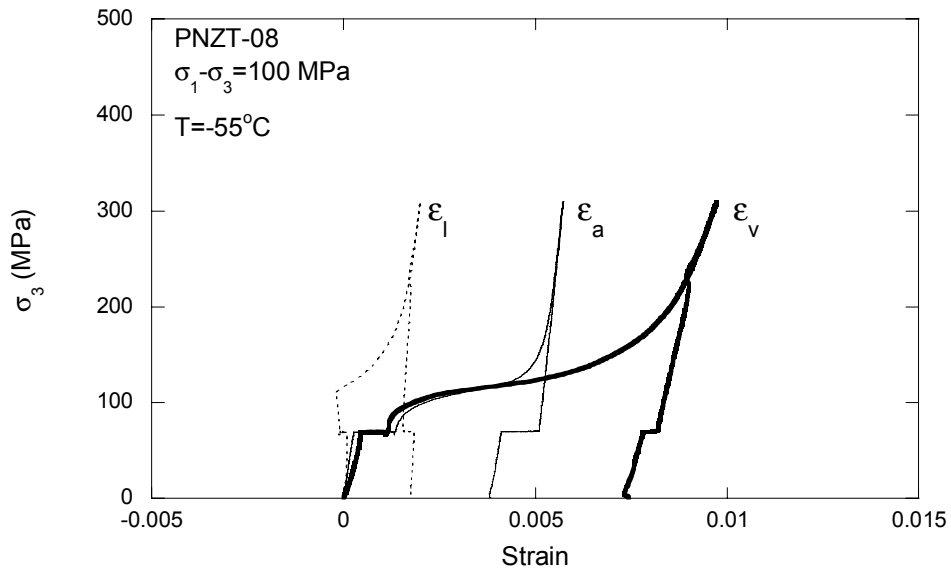
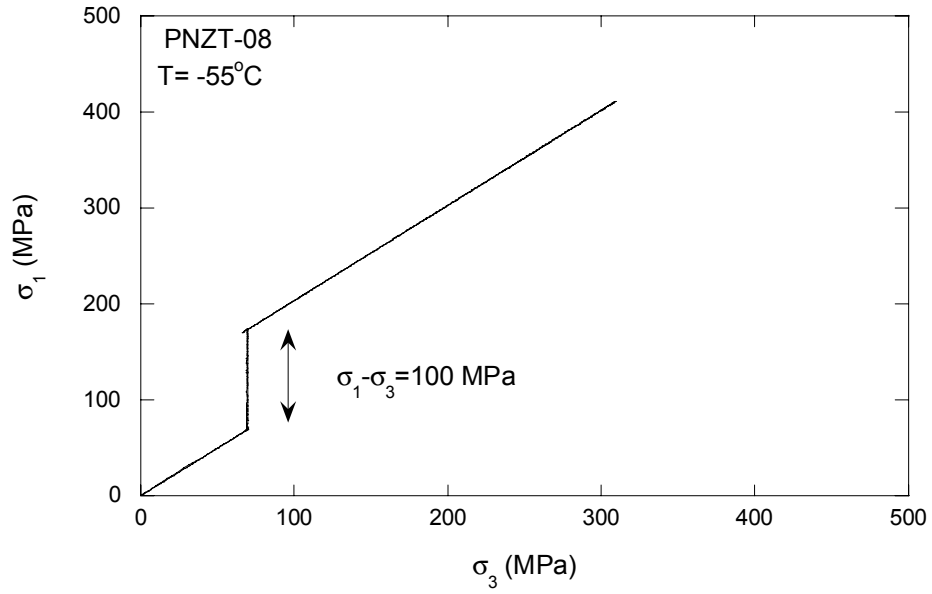


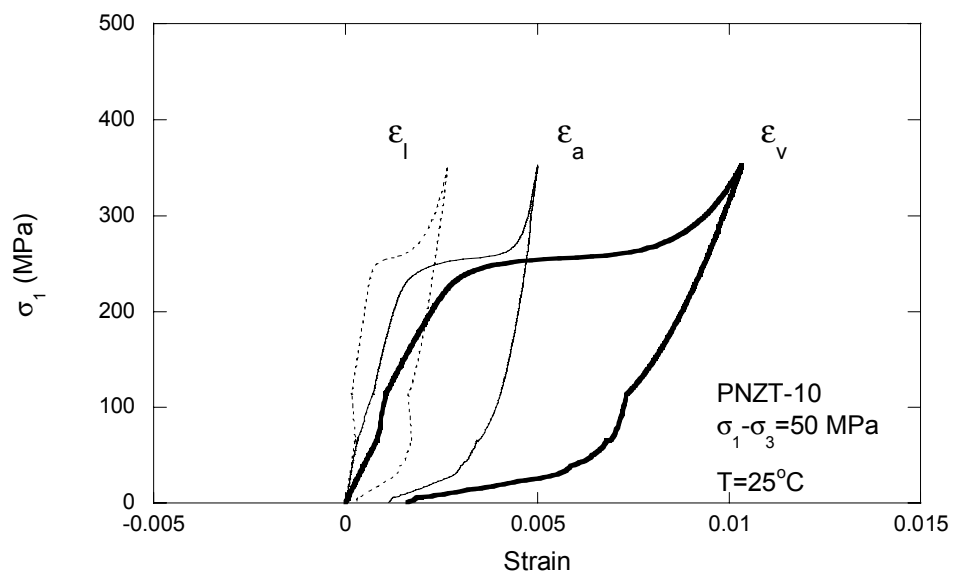
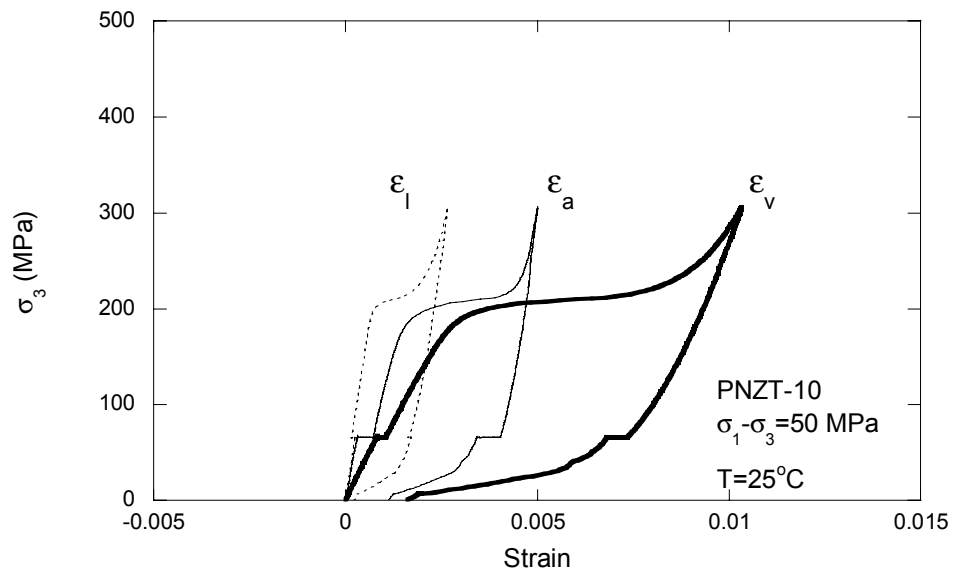
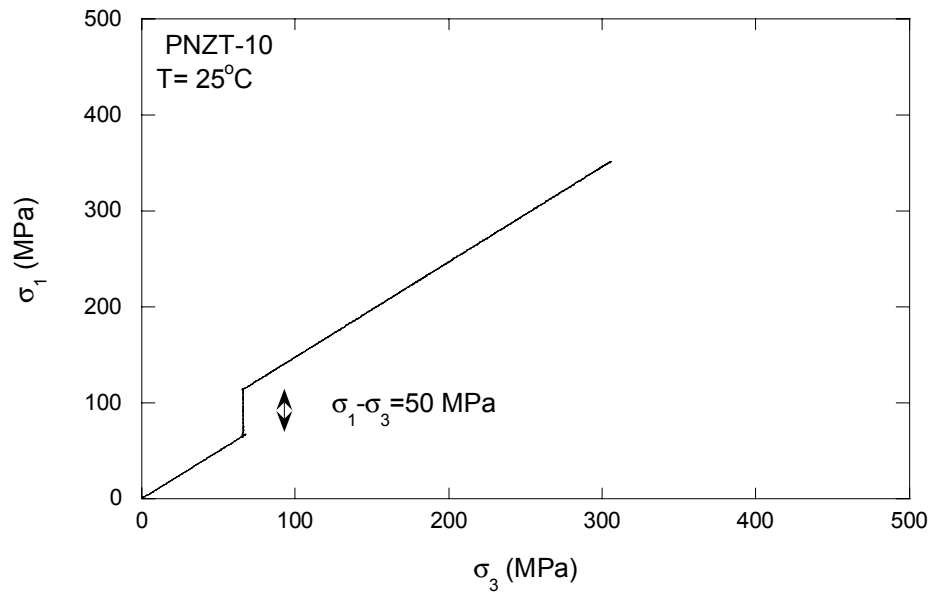
## **APPENDIX C**

### **Stress Paths and Stress-Strain Test Plots for Constant Stress Difference (CSD) Test for PNZT-HF803**

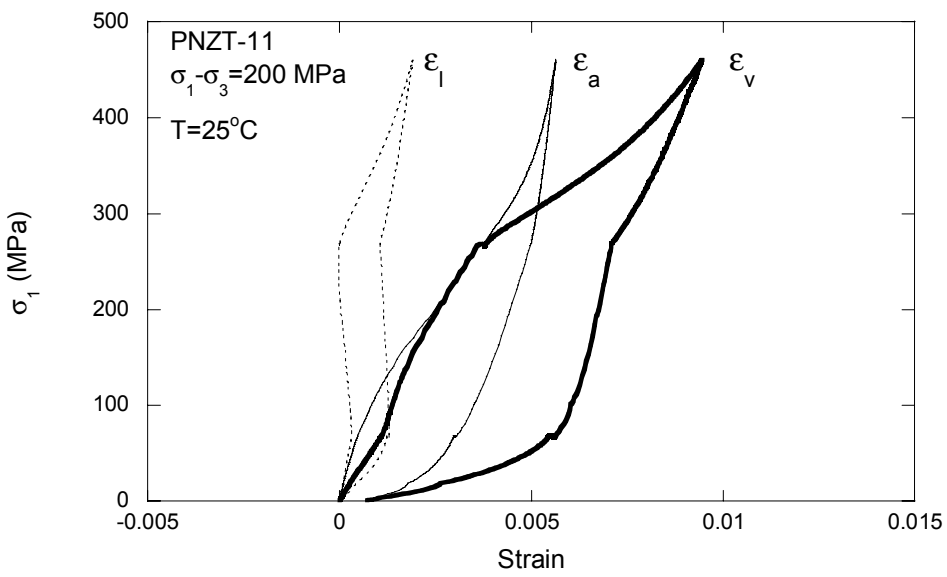
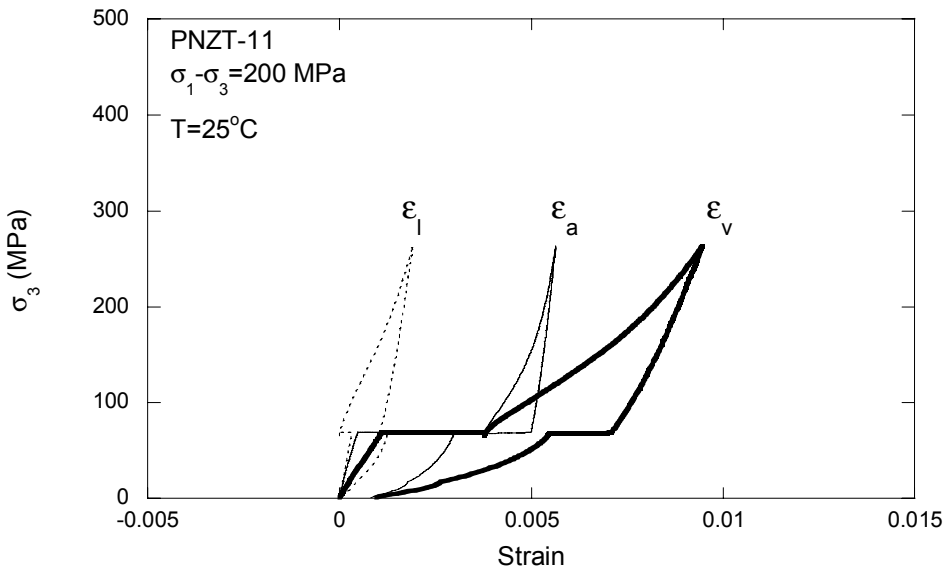
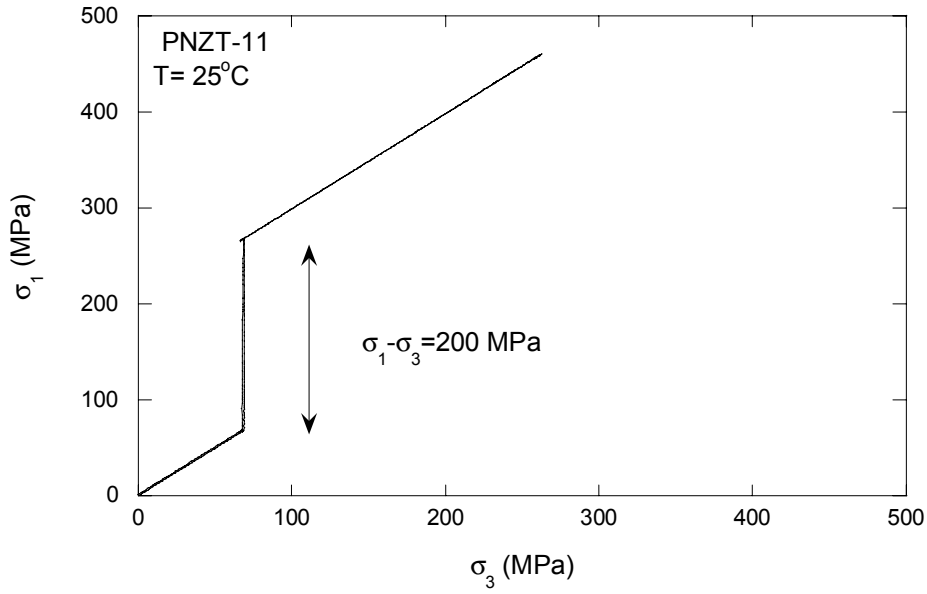
**( $\sigma_1$ -axial stress,  $\sigma_3$ -confining stress,  $\varepsilon_a$ -axial  
strain,  $\varepsilon_l$ -lateral strain,  $\varepsilon_v$ -volumetric strain and  
T-temperature)**

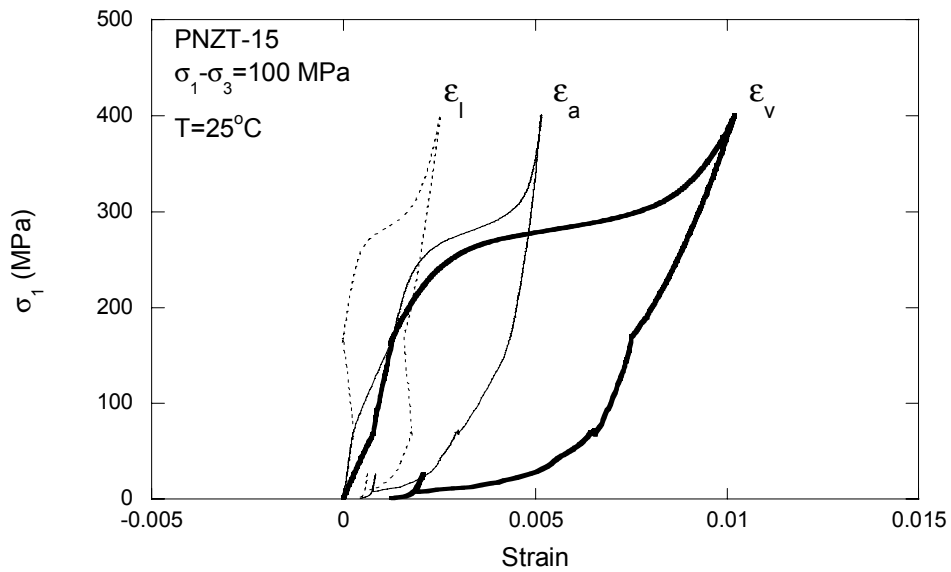
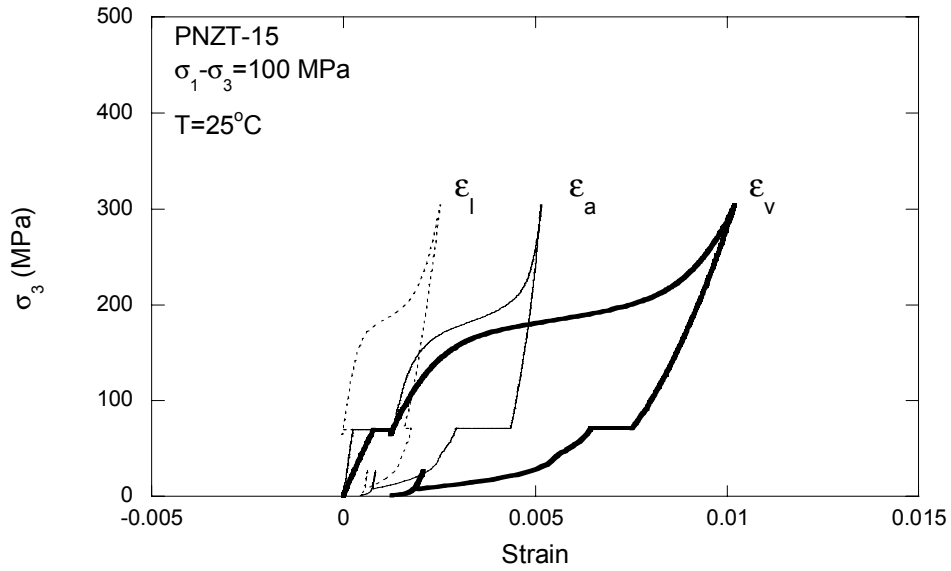
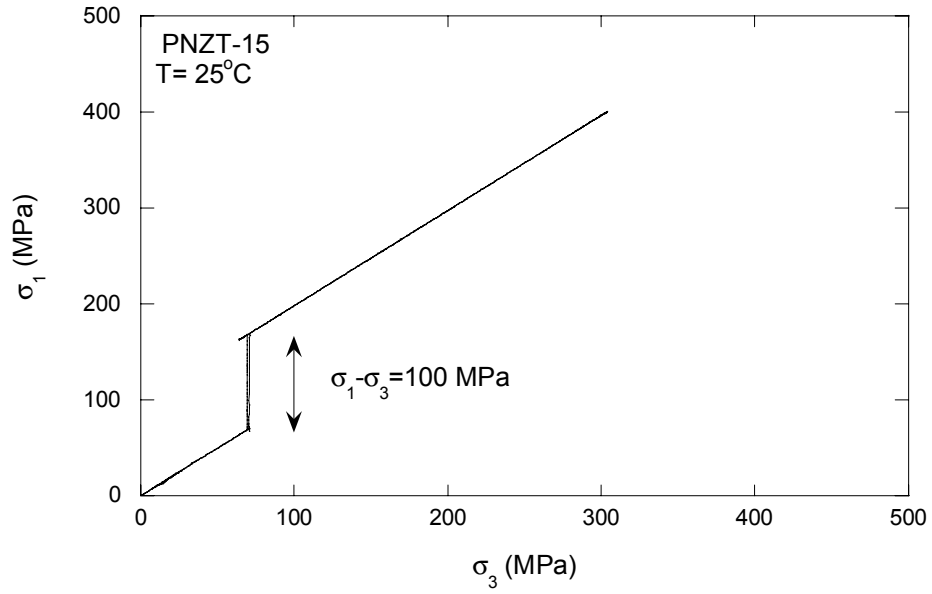


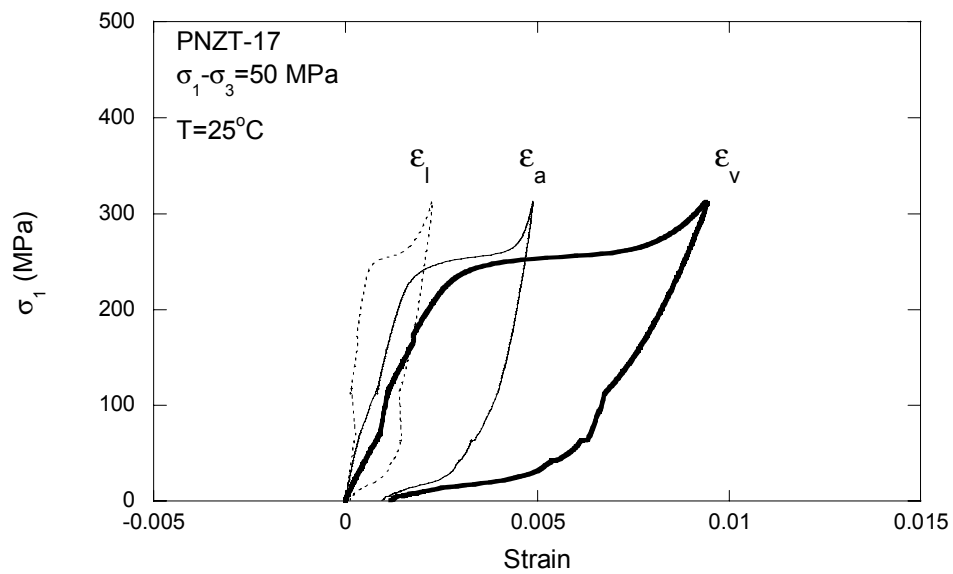
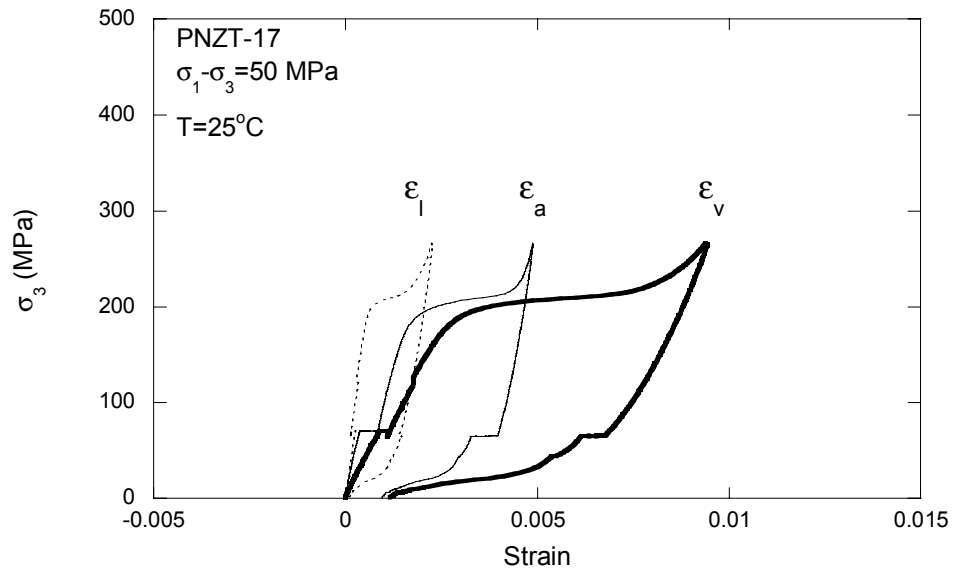
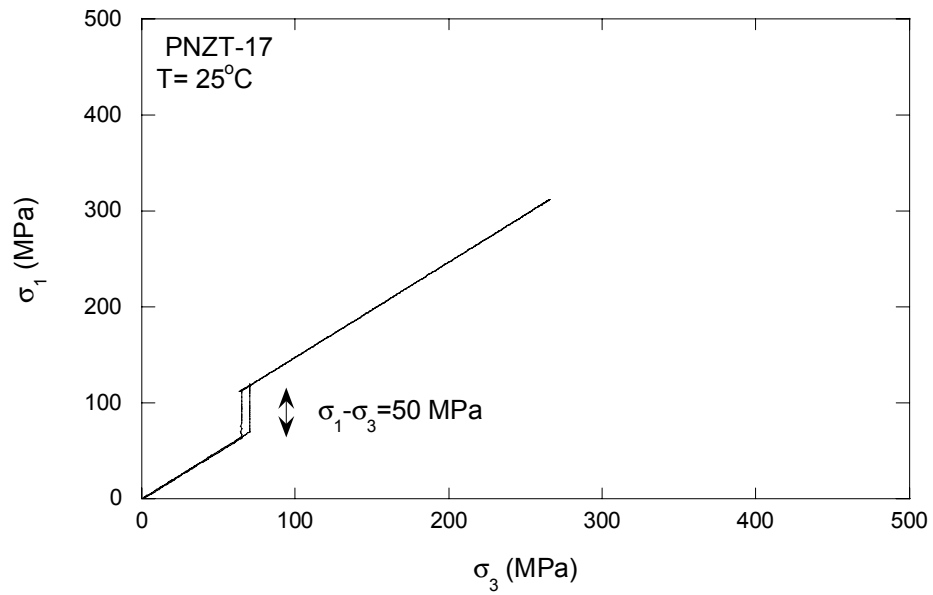


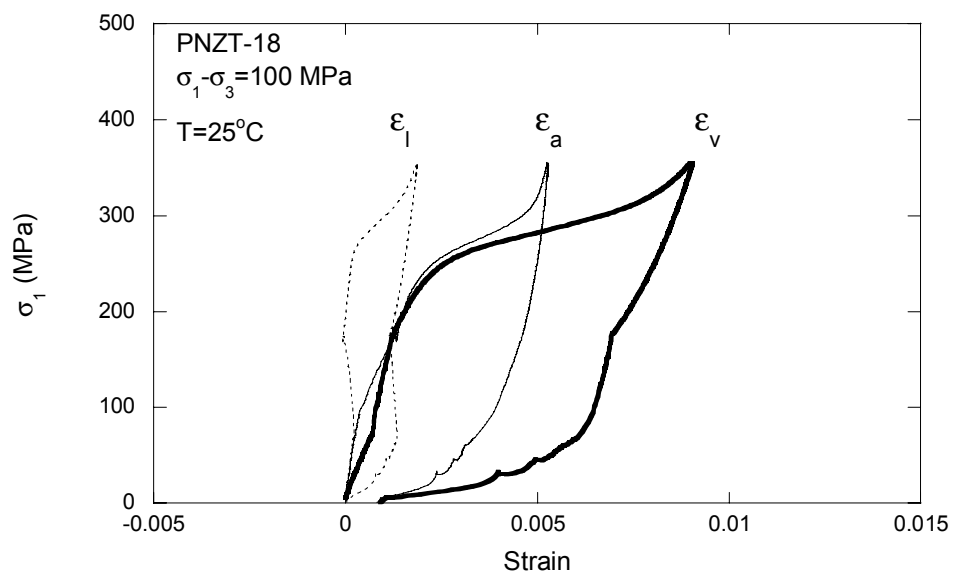
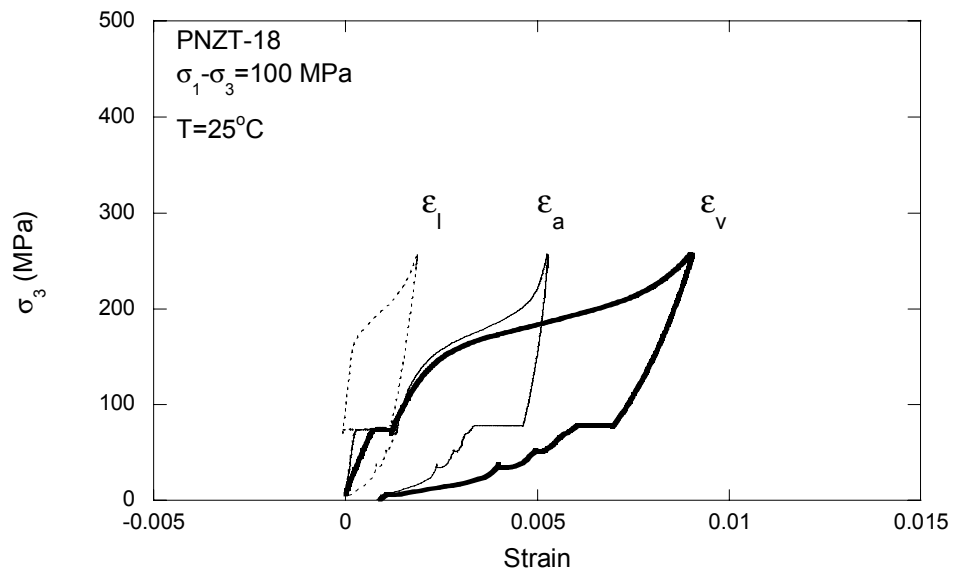
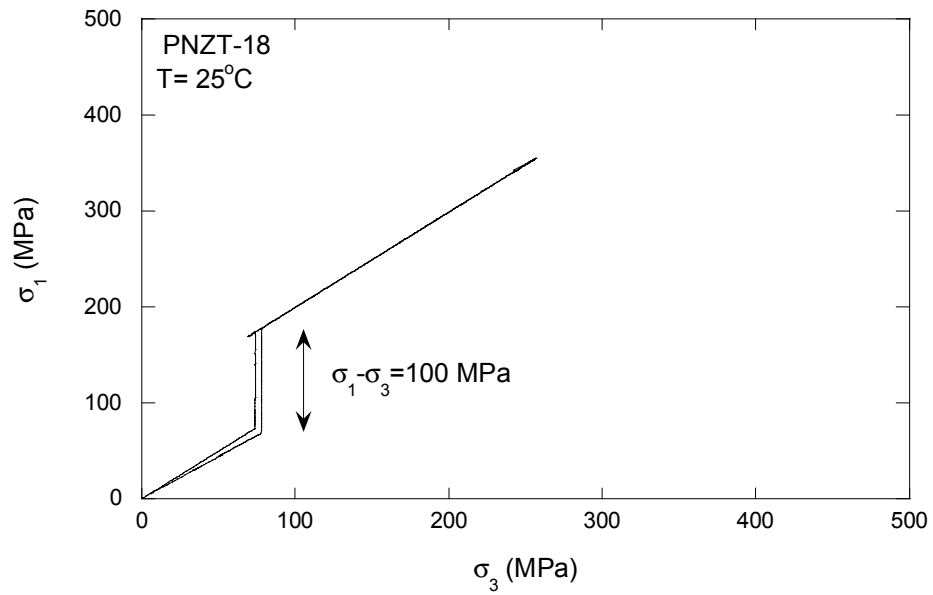


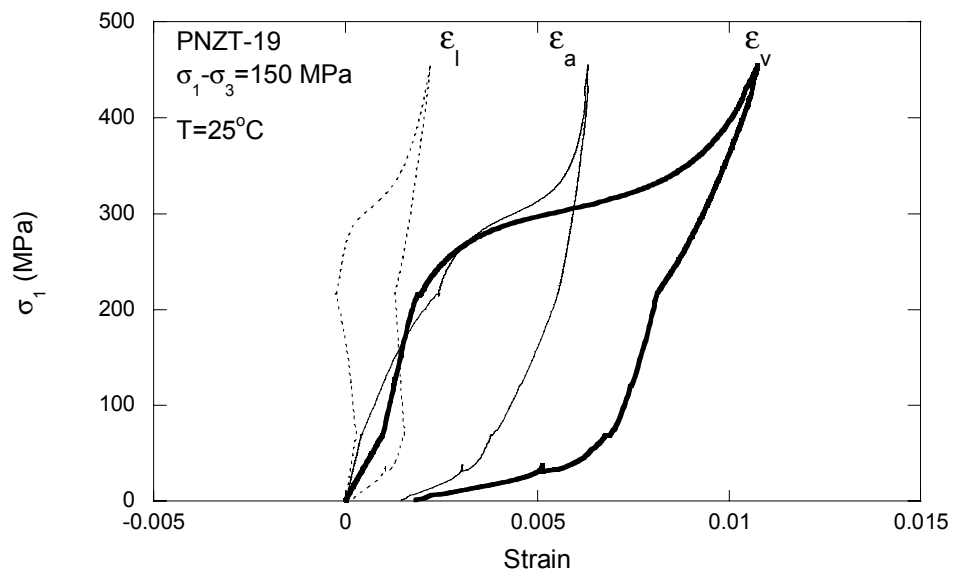
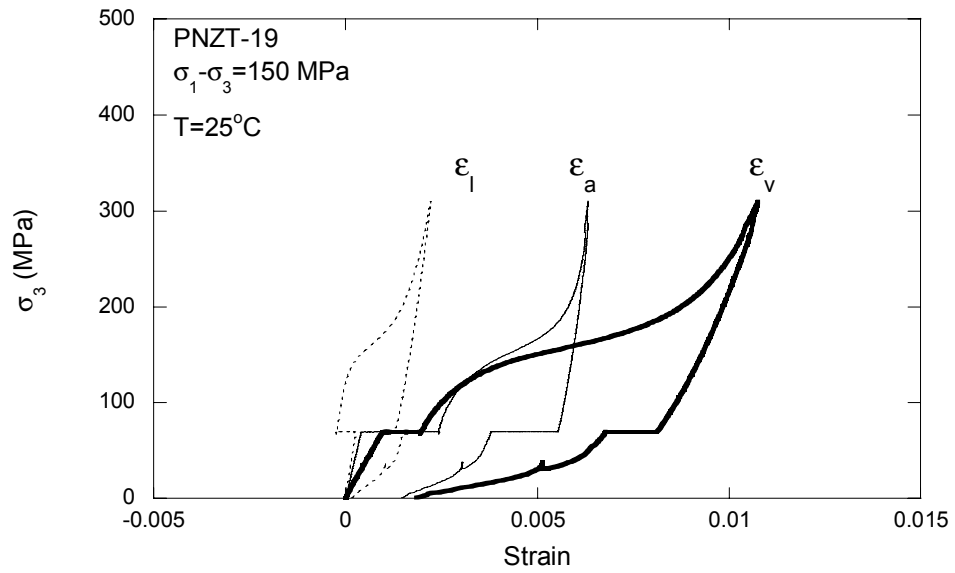
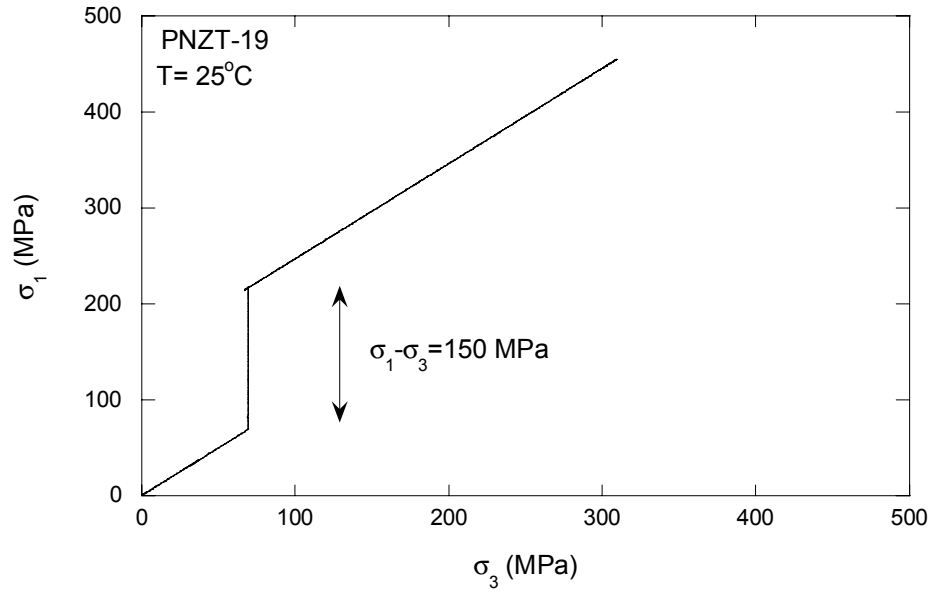


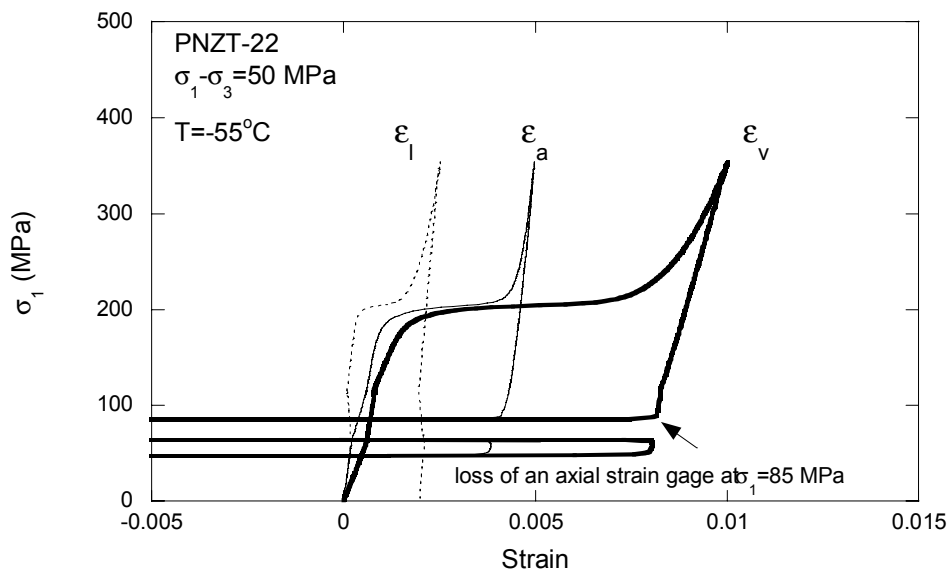
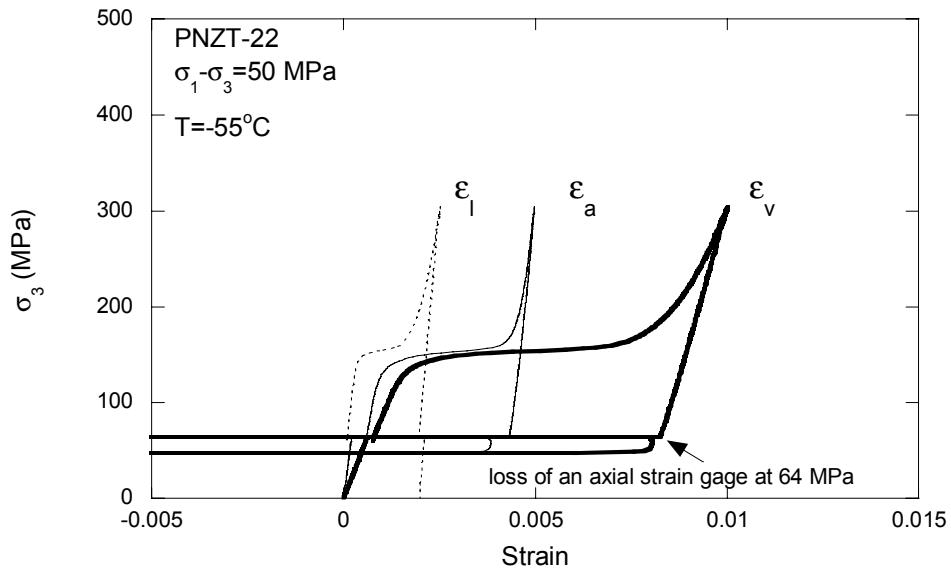
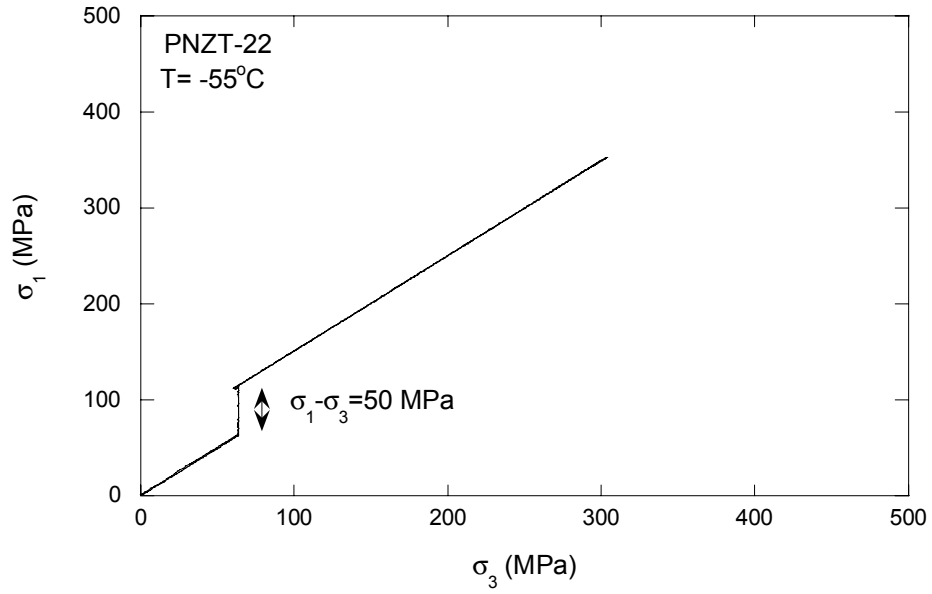


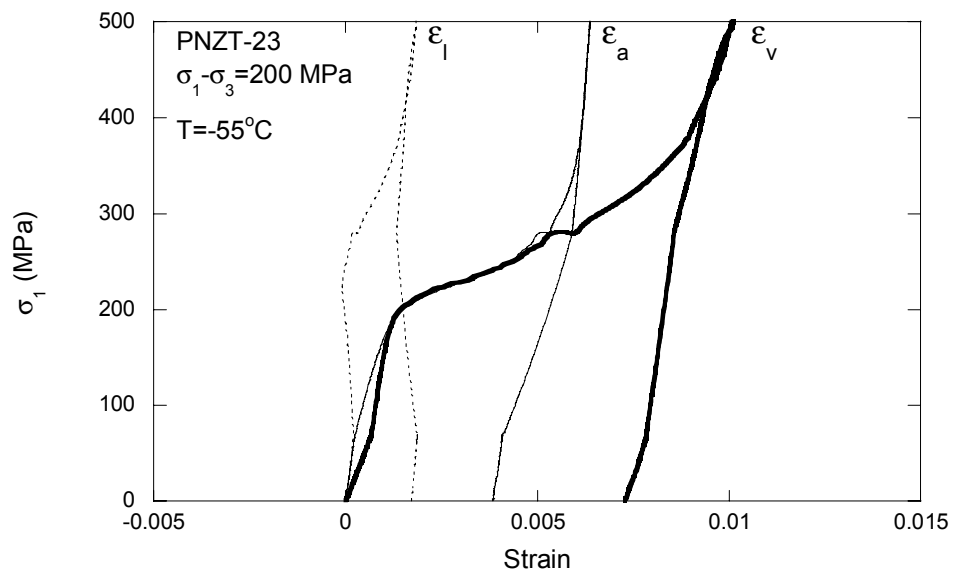
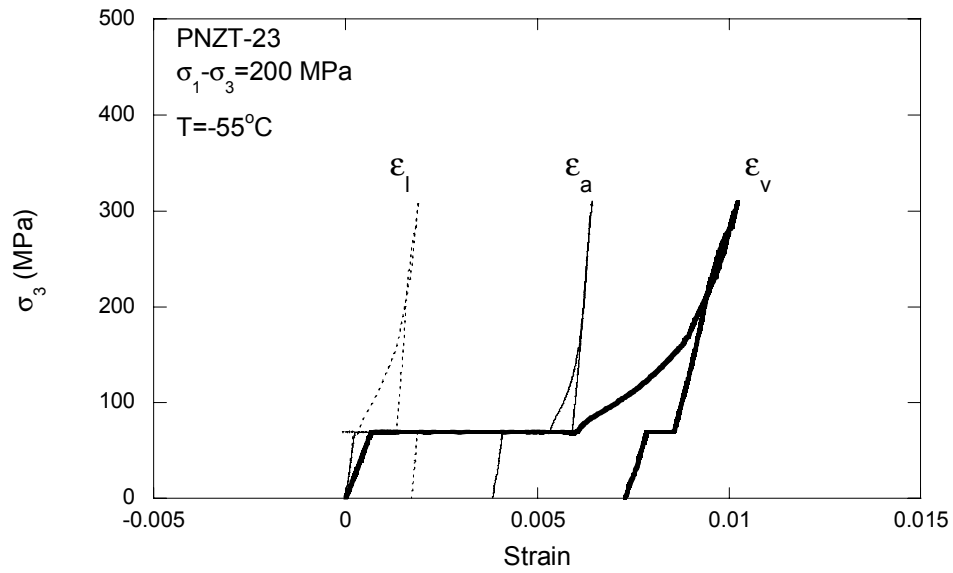
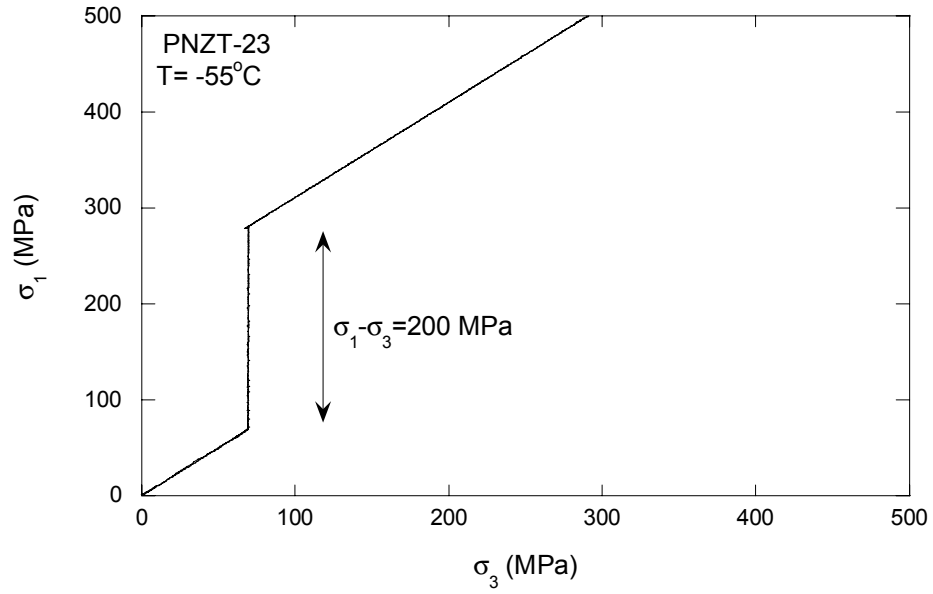


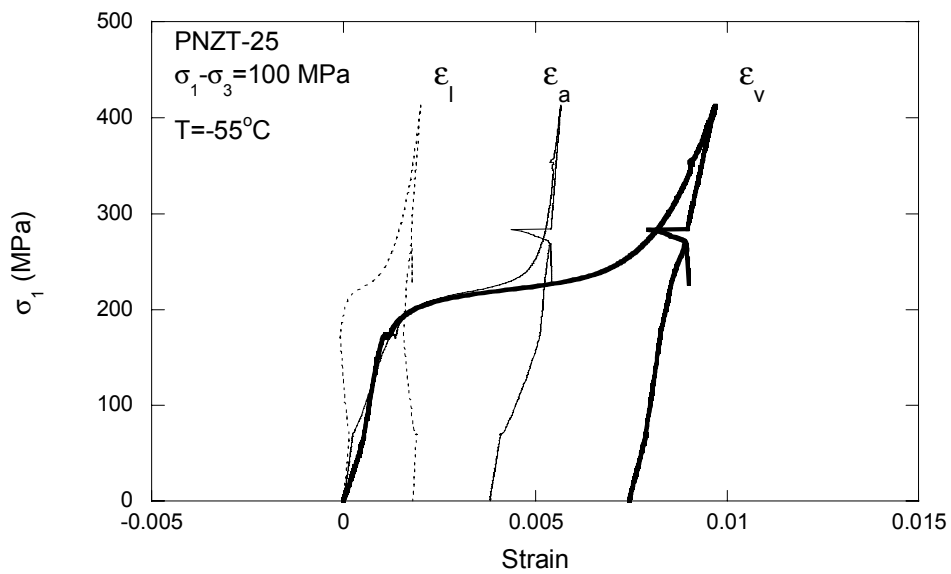
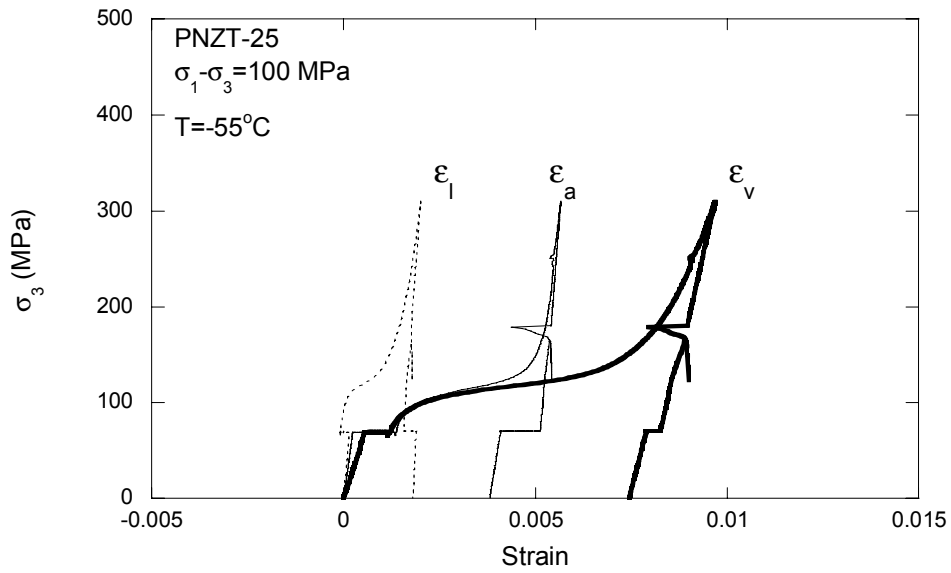
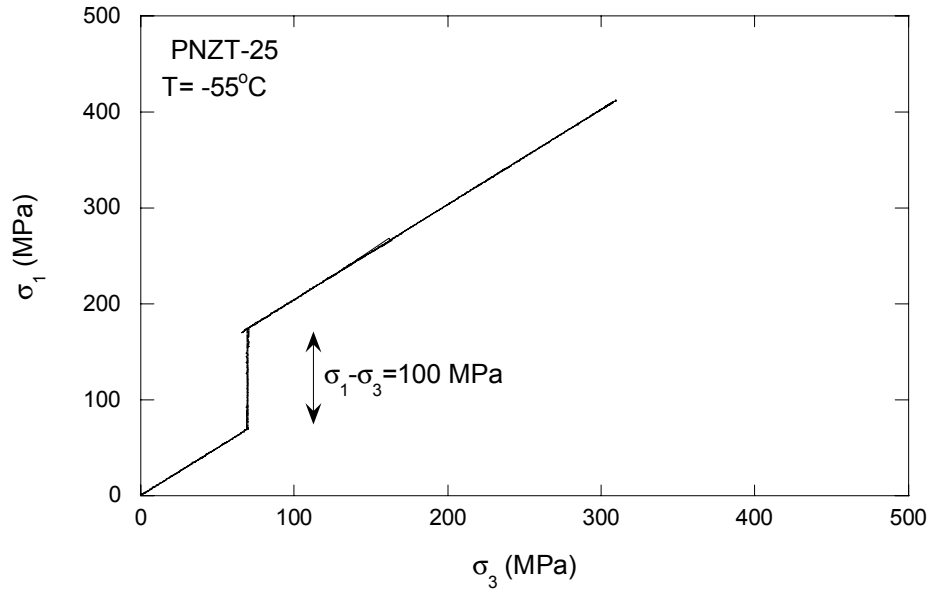




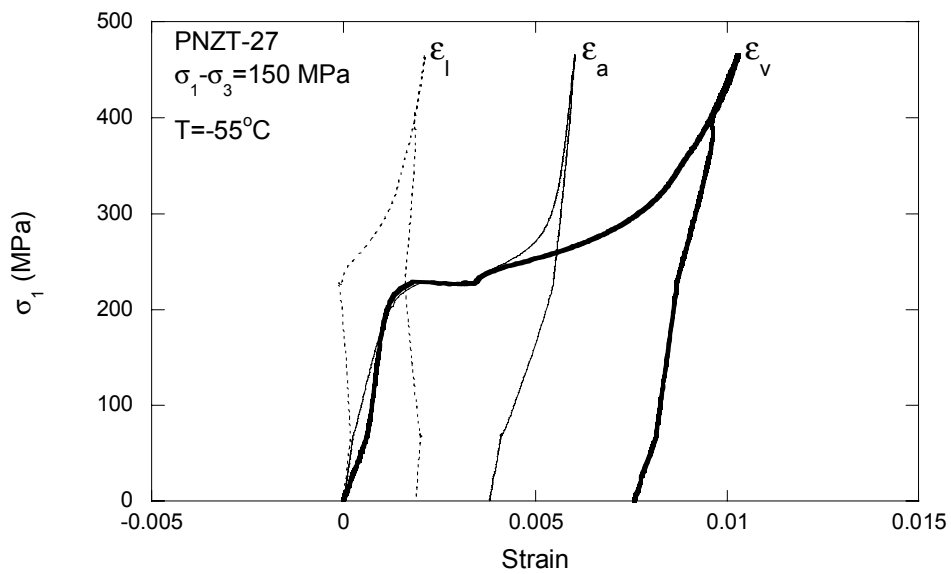
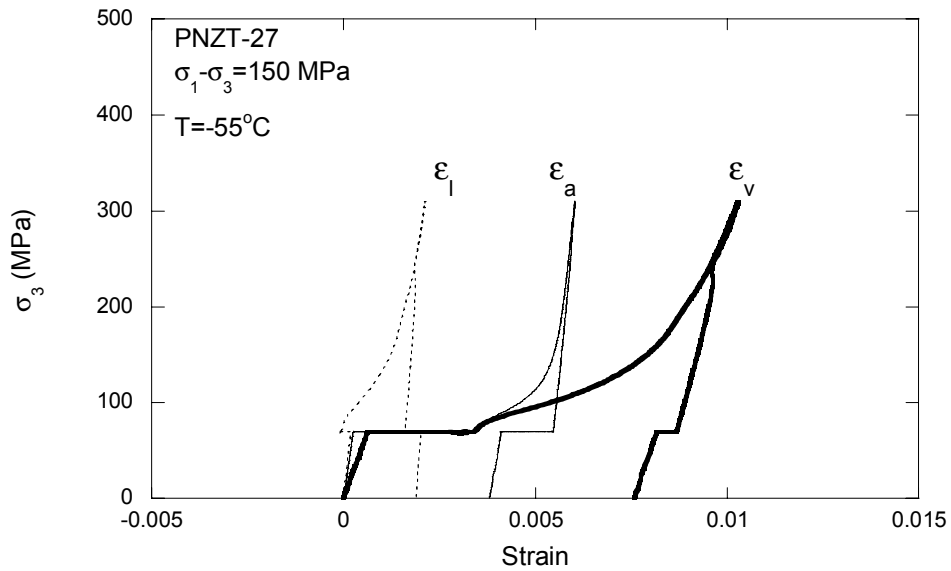
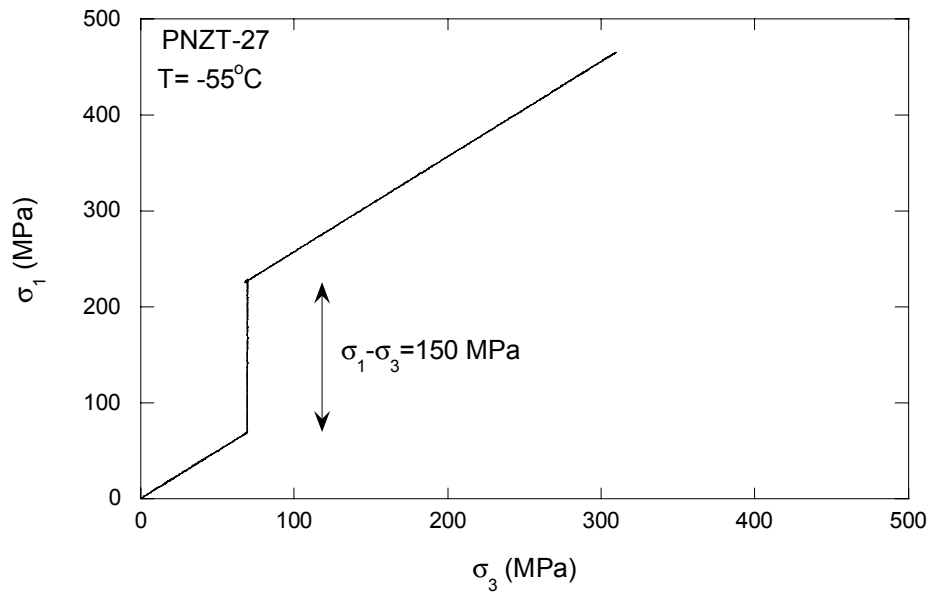


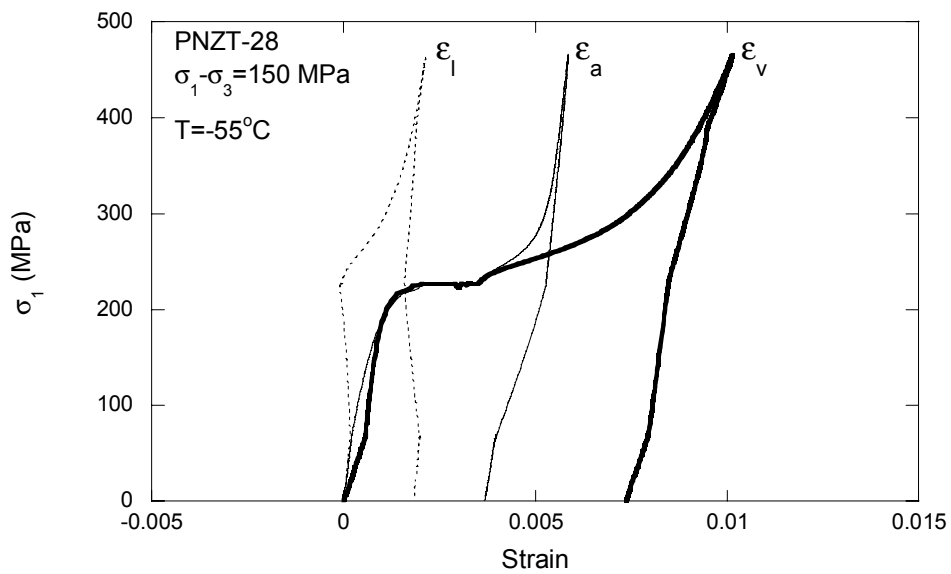
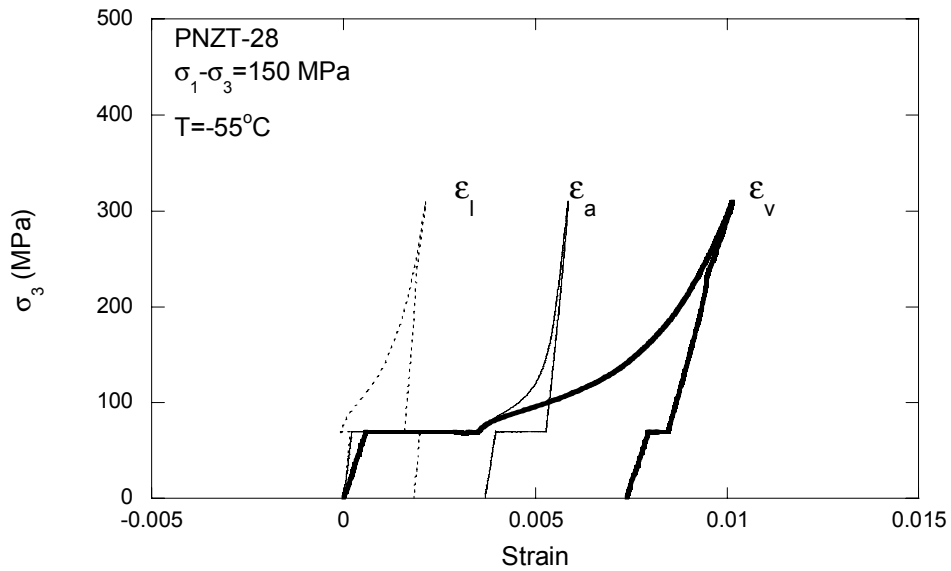
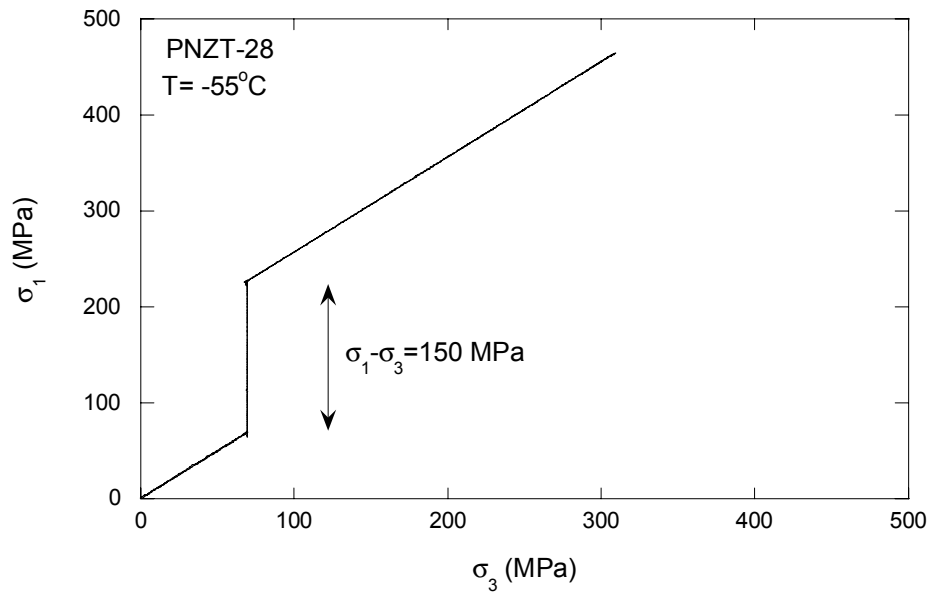


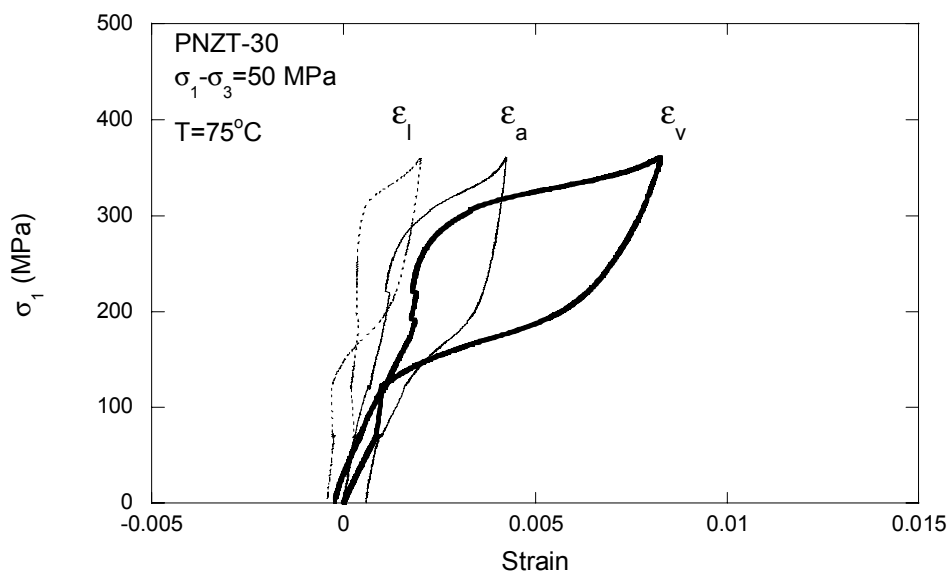
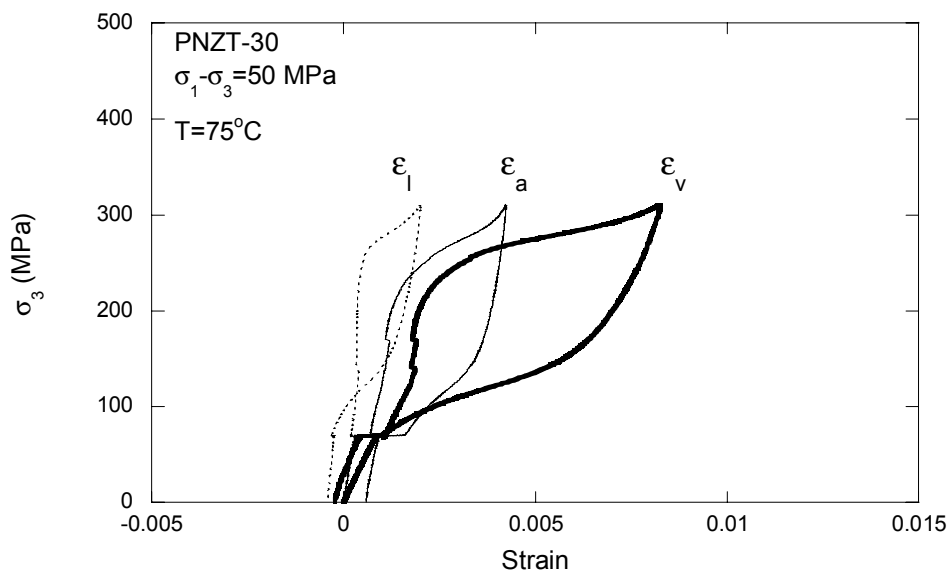
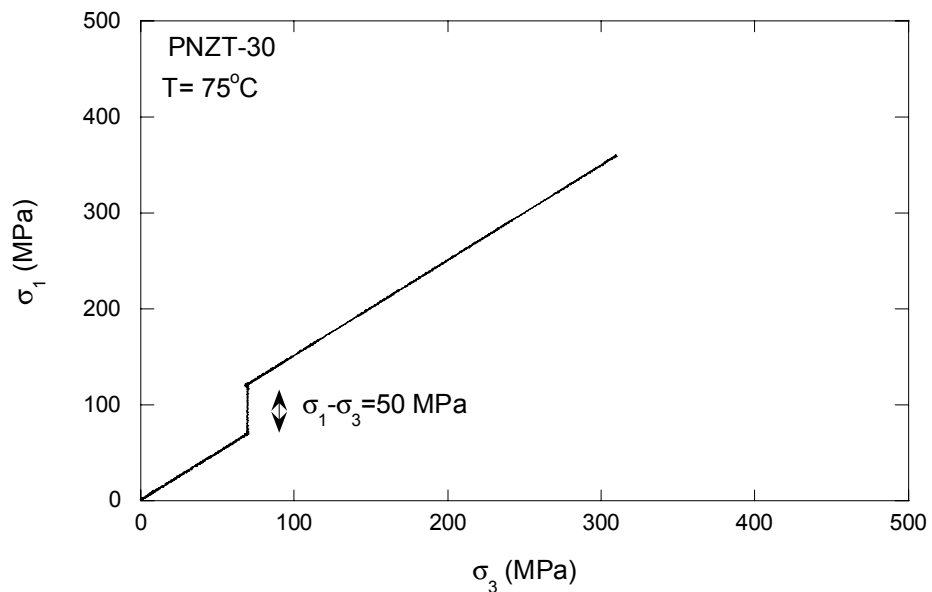


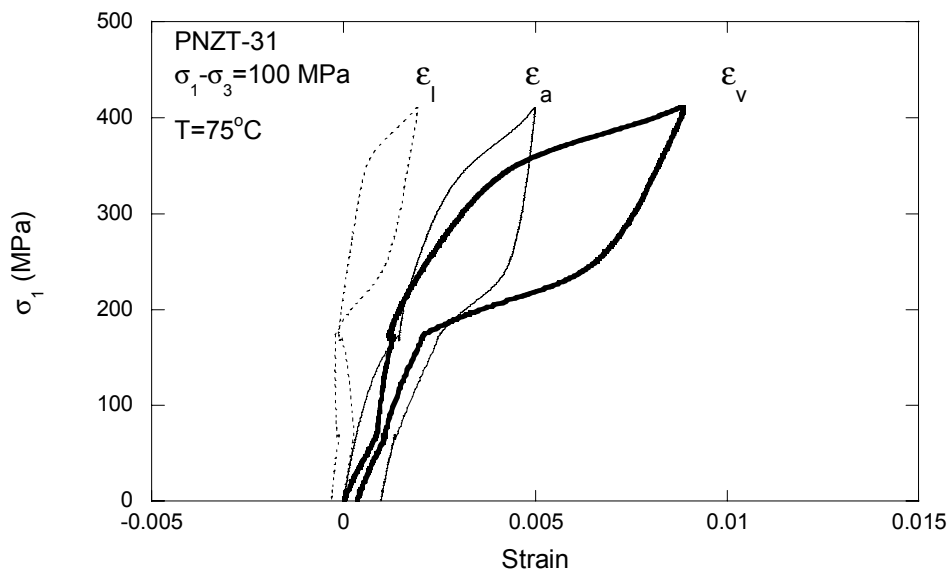
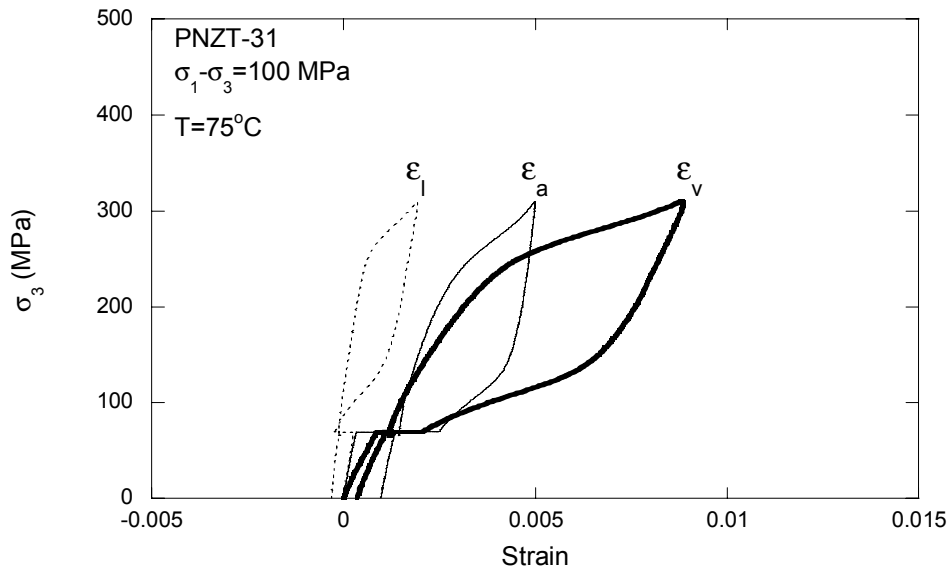
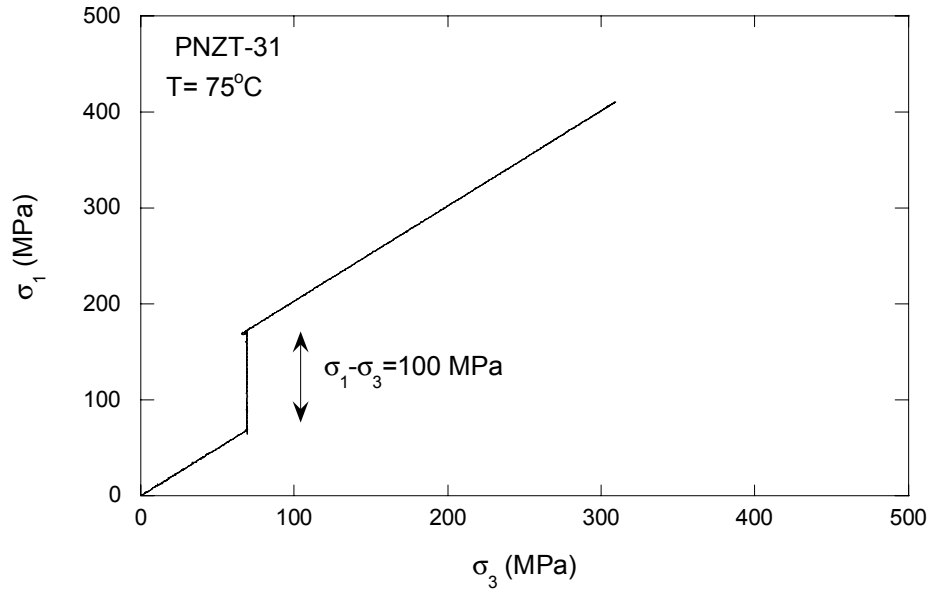


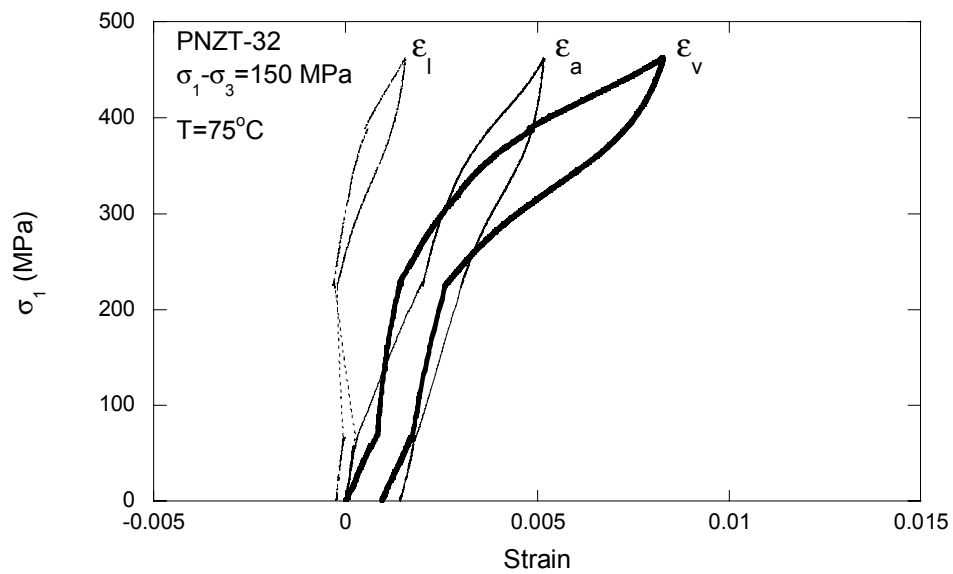
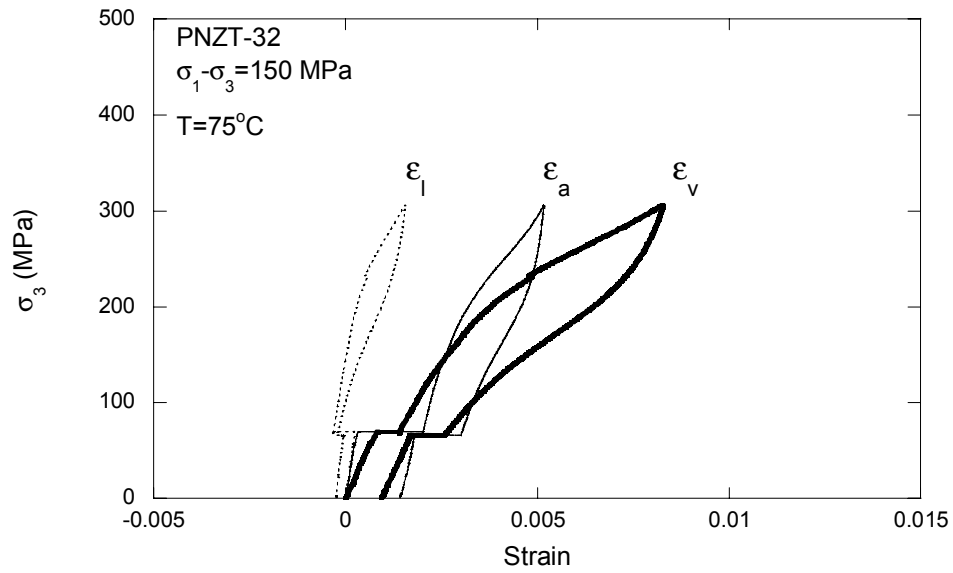
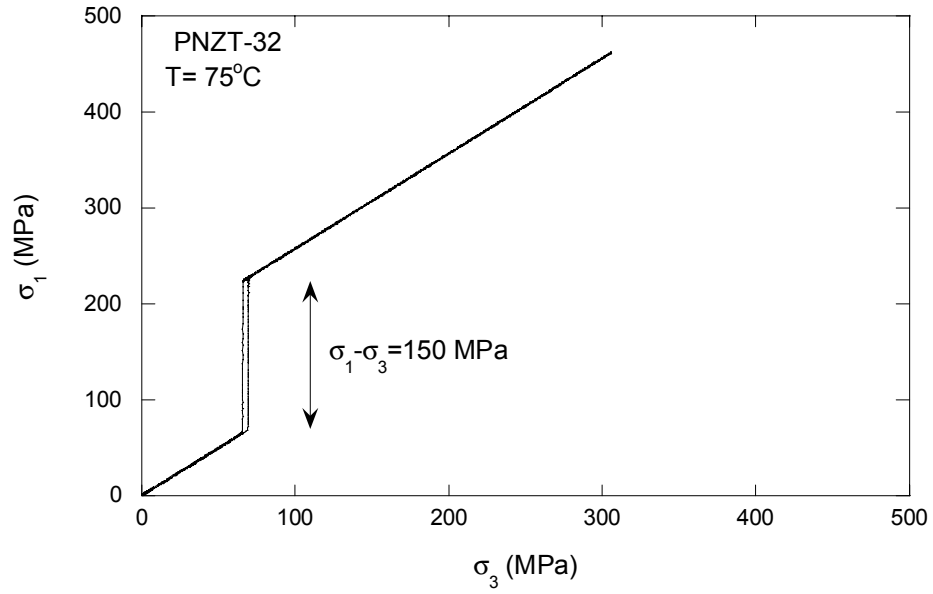


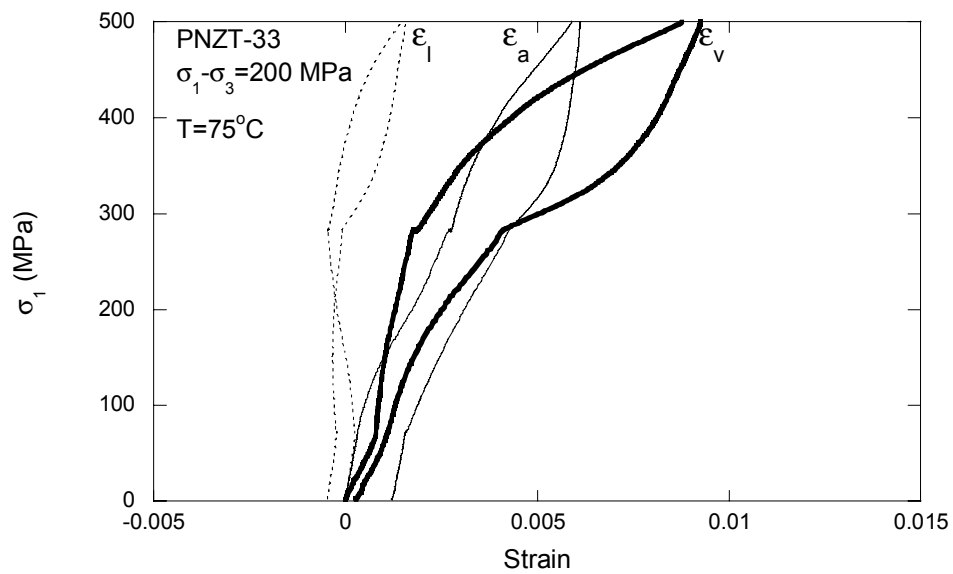
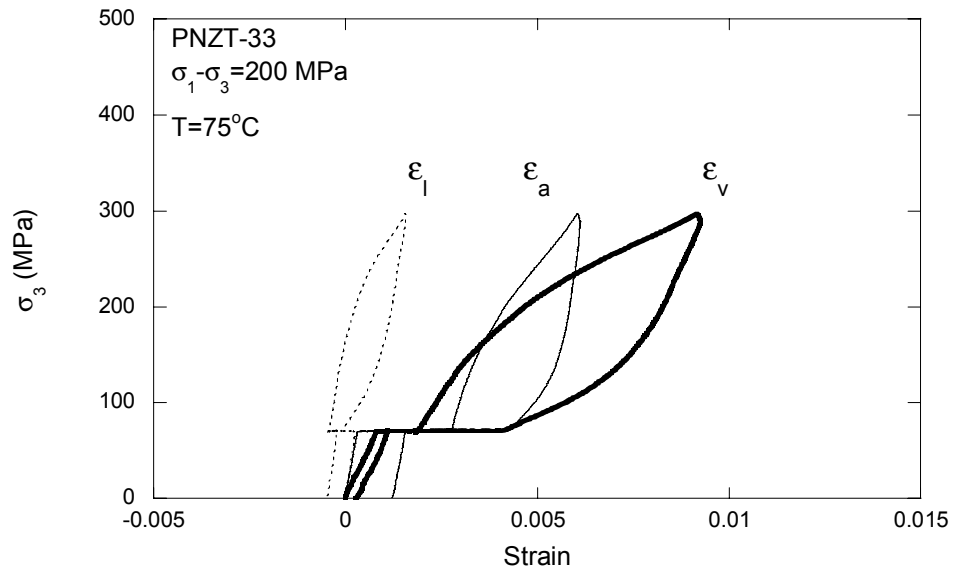
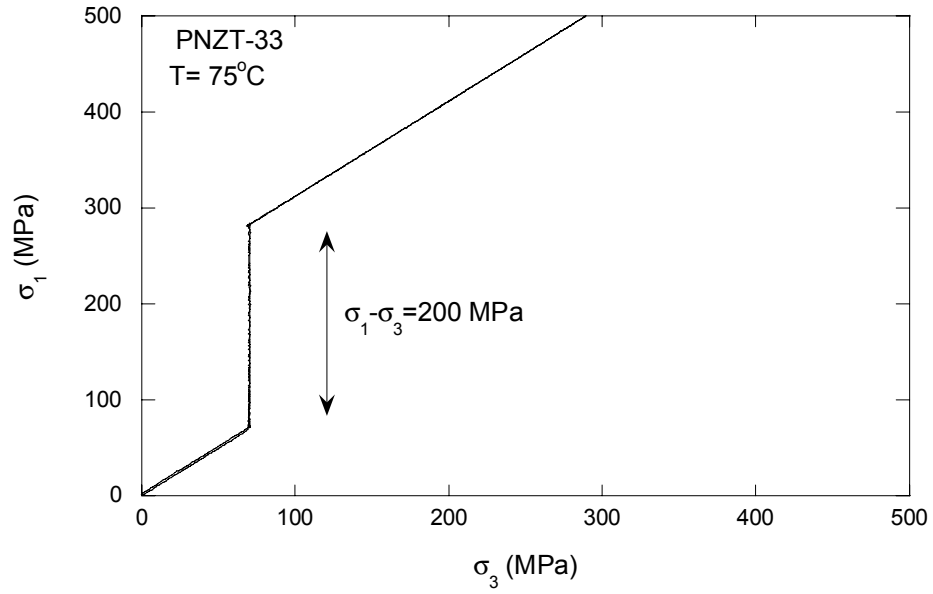


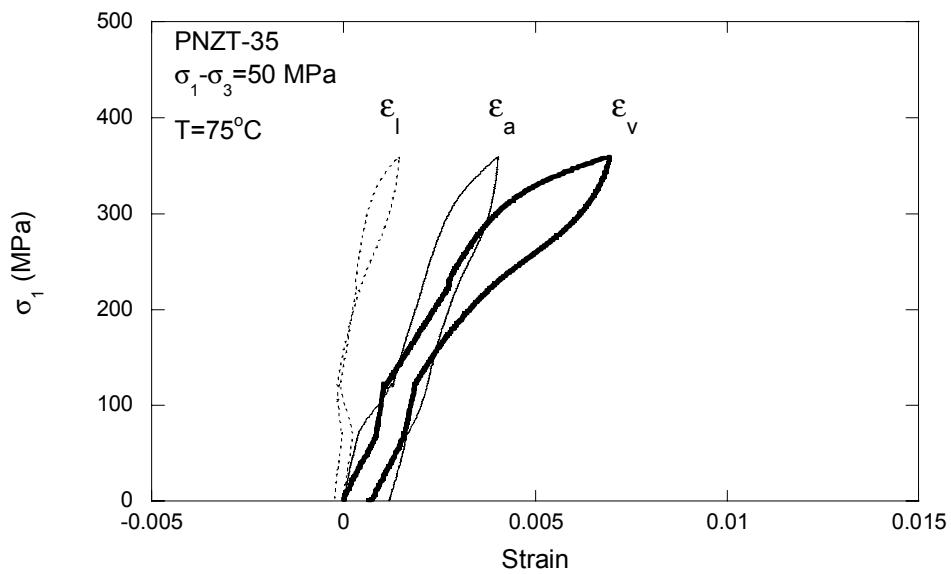
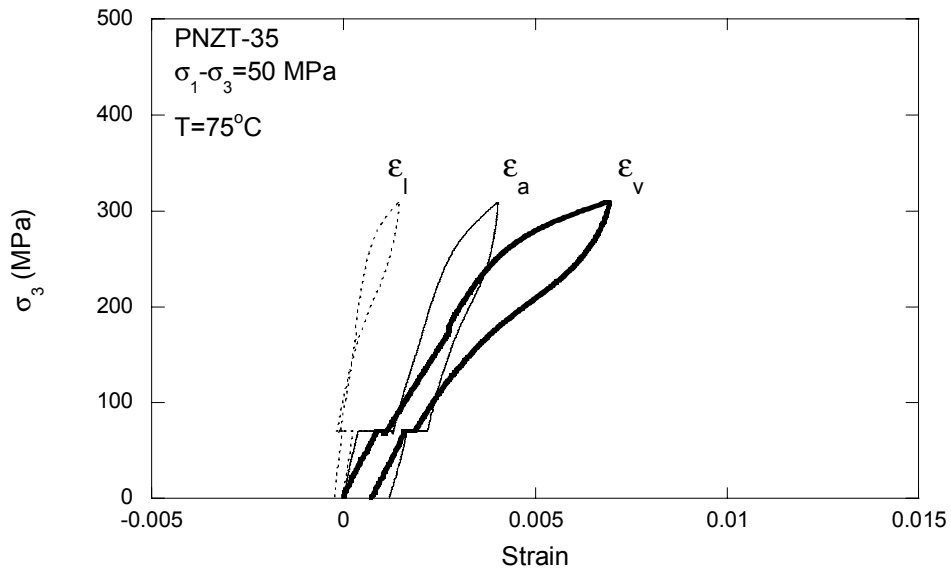
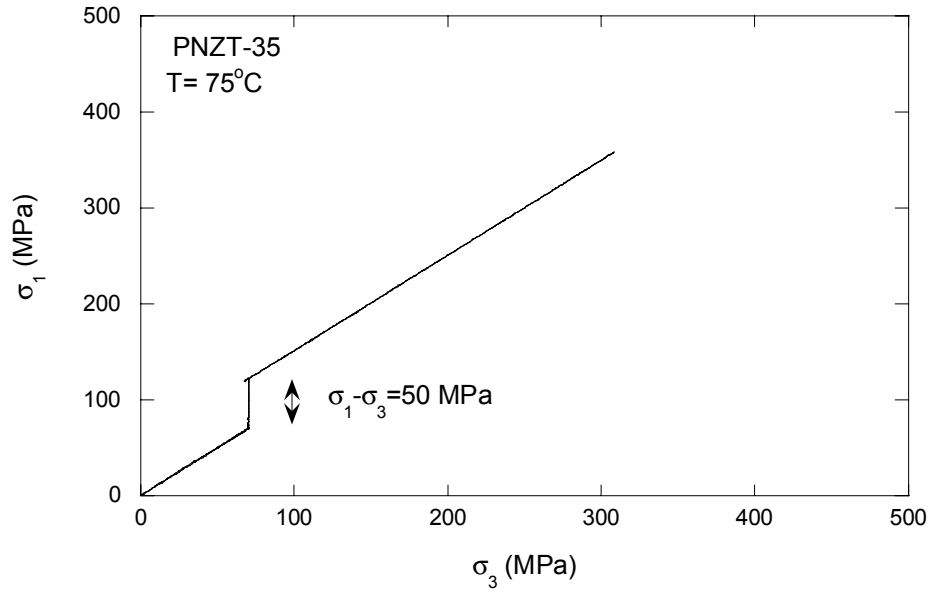


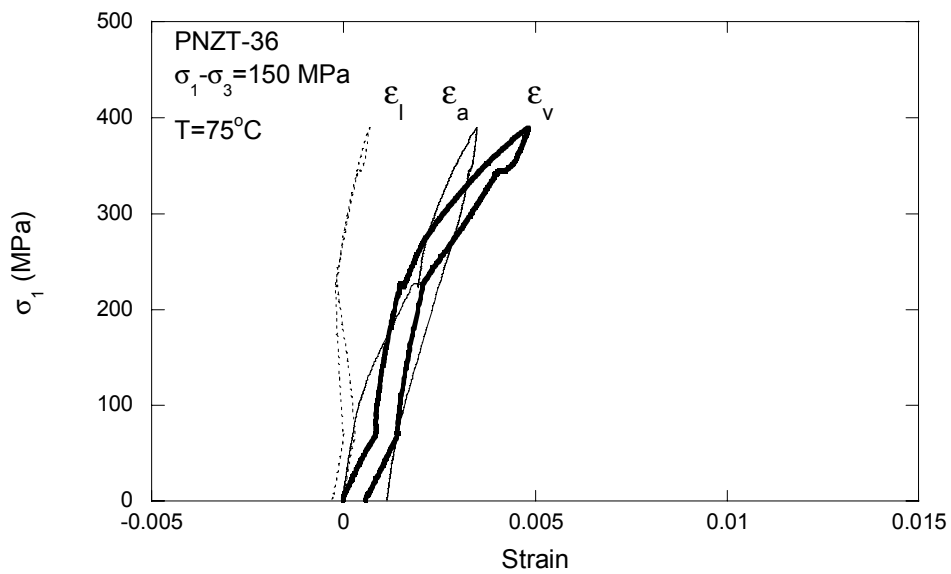
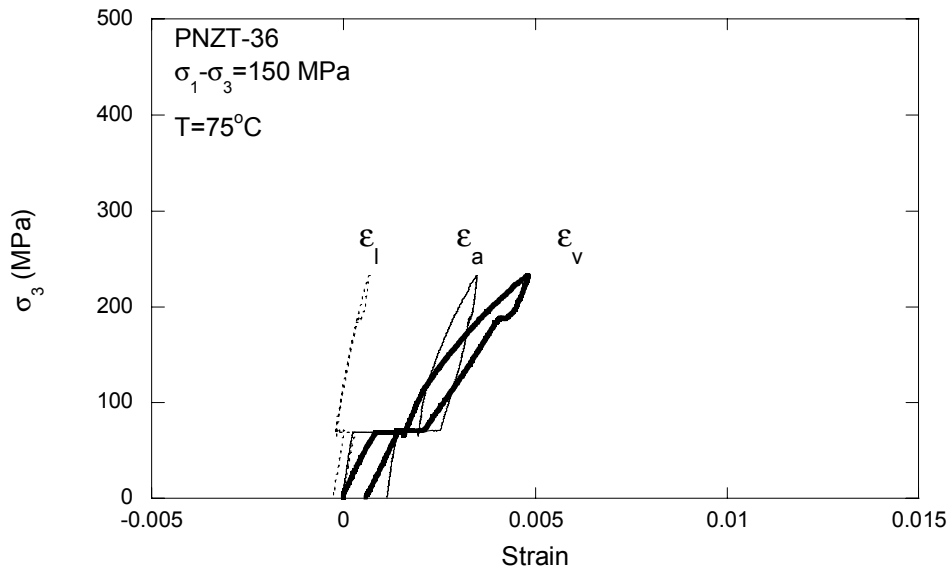
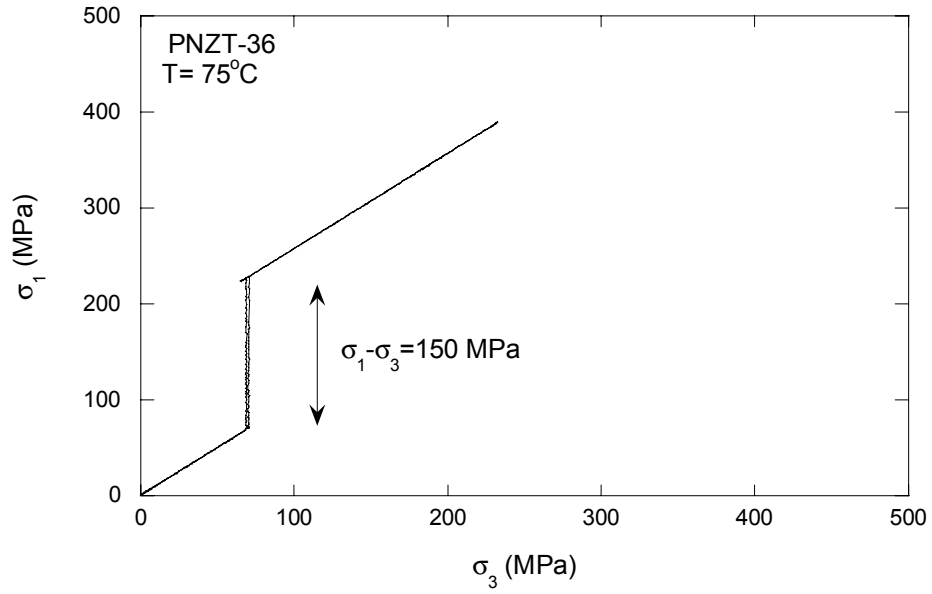














## **APPENDIX D**

### **List of Data and Supplemental Files Archived in Webfileshare System for PNZT-HF803**

List of files archived in the WEBFILESHARE system (<https://wfsprod01.sandia.gov>).

<b>Folder Name</b>	<b>File Name</b>	<b>Description</b>
/TARGET/PNZT-803	PNZT-SAND03.doc	This SAND report
/TARGET/PNZT-803	PNZT-master.xls	<p>Master data file consists of the following nine worksheets:</p> <p><b>HF803:</b> HF803 lot information  <b>Specimen:</b> PNZT specimen dimensions  <b>UC-Test matrix:</b> Test matrix and results for Uniaxial Compression tests  <b>HC-Test matrix:</b> Test matrix and results for Hydrostatic Compression tests  <b>CSD-Test matrix:</b> Test matrix and results for Constant Stress Difference tests  <b>UC-data:</b> Uniaxial compression test data (Time, <math>\sigma_a</math>, <math>\epsilon_a</math>, <math>\epsilon_l</math>, and <math>\epsilon_v</math>)  <b>UC-P velocity:</b> Compressive wave velocity data during uniaxial compression tests (Time, <math>\sigma_a</math>, Input, Output, and Delay time)  <b>HC-data:</b> Hydrostatic Compression test data (<math>\epsilon_v</math> and Pressure)  <b>CSD-data:</b> Constant Stress Difference test data (Time, <math>\sigma_1</math>, <math>\sigma_3</math>, <math>\epsilon_a</math>, <math>\epsilon_l</math> and <math>\epsilon_v</math>)</p>
/TARGET/PNZT-803	PNZT-ds.zip	Laboratory data sheets for the following tests: PNZT-01, 02, 04, 06, 07, 08, 10, 11, 15, 17, 18, 19, 22, 23, 25, 27, 28, 30, 31, 32, 33, 34, 35, 36, 44, 45, 52, 53, 55, 57, 58, 59, 60, 63, 64, 65 and 71
/TARGET/PNZT-803	PNZT-pic.zip	Miscellaneous pictures taken during constitutive testing of PNZT.

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