# Finite Element Simulation for Structural Response of U7Mo Dispersion Fuel Plates Via Fluid-Thermal-Structural Interaction

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#### FINITE ELEMENT SIMULATION FOR STRUCTURAL RESPONSE OF U7MO DISPERSION FUEL PLATES VIA FLUID-THERMAL-STRUCTURAL INTERACTION

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#### ABSTRACT

This article presents numerical simulation of dispersion fuel mini plates via fluid-thermal-structural interaction performed by commercial finite element solver COMSOL Multiphysics to identify initial mechanical response under actual operating conditions. Since fuel particles are dispersed in Aluminum matrix, and temperatures during the fabrication process reach to the melting temperature of the Aluminum matrix, stress/strain characteristics of the domain cannot be reproduced by using simplified models and assumptions. Therefore, fabrication induced stresses were considered and simulated via image based modeling techniques with the consideration of the high temperature material data. In order to identify the residuals over the U7Mo particles and the Aluminum matrix, a representative SEM image was employed to construct a microstructure based thermo-elasto-plastic FE model. Once residuals and plastic strains were identified in micro-scale, solution was used as initial condition for subsequent multiphysics simulations at the continuum level. Furthermore, since solid, thermal and fluid properties are temperature dependent and temperature field is a function of the velocity field of the coolant, coupled multiphysics simulations were considered. First, velocity and pressure fields of the coolant were computed via fluidstructural interaction. Computed solution for velocity fields were used to identify the temperature distribution on the coolant and on the fuel plate via fluid-thermal interaction. Finally, temperature fields and residual stresses were used to obtain the stress field of the plates via fluid-thermal-structural interaction.

**Keywords:** *dispersion fuel plates, multiscale, multiphysics, microstructure based fem* 

#### **1. INTRODUCTION**

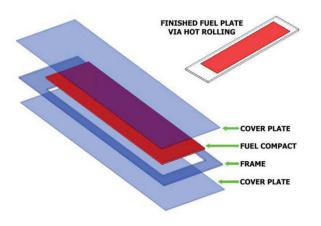
Initiated in late 1970, the primary objective of the Reduced Enrichment for Research and Test Reactors (RERTR) program is to develop the technology to minimize the use of Highly Enriched Uranium (HEU) for most civilian applications. RERTR fuel development program aims to develop fuel types that would substitute high enriched uranium with proliferation resistant, low enriched uranium (<20%<sup>235</sup>U) for research reactors [1]. However, once the amount of the enriched Uranium per unit volume is reduced, there will be a sudden drop in the fission rate. Consequently, higher densities should be employed to compensate for lower fission rate caused by the reduction of enriched Uranium per unit volume. Many research reactors can be satisfactorily operated with Silicon based  $(U_3Si_2-Al)$  dispersive fuels lower (up to 5 g/cm<sup>3</sup>) densities. However, several high performance reactors such as ATR (Advanced Test reactor), HFIR (High Flux Isotope Reactor), MITR Massachusetts Institute of Technology Reactor, NBSR (National Bureau of Standards Reactor) and MURR (Missouri University Research Reactor) require even higher densities (up to 10 g U/cm<sup>3</sup>). Challenge associated with this, the fuel with high-uranium density should remain stable during irradiation as well as during the fabrication process. Among several proposed alloys, U-Mo based fuels are found to be the most promising candidate for fuels with higher densities. Molybdenum extends the stability of the gamma phase of the domain, since this phase is known to be stable under the desired irradiation conditions. U-Mo has a low neutron caption cross-section, good irradiation behavior and acceptable swelling response [2-4].

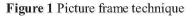
Dispersive fuel elements have been preferred in the research and test nuclear reactors due to their reliability, robust thermal and mechanical response [5]. For development of Molybdenum based dispersion fuels with higher densities, U-Mo particles are dispersed in the Aluminum matrix. An aggressive research has been carried out in Material and Fuel Complex (MFC) of Idaho

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National Laboratory (INL) to benchmark U-Mo based dispersion and monolithic fuel types. One of the major challenges of developing a new fuel type is to predict the structural response under thermo-mechanical loading. Number of irradiation experiments has been carried out to experimentally observe the structural response of the plates [6-9]. However, structural simulation of U-Mo alloy based dispersive fuel elements is in their early development stages.

Since fabrication of dispersive plates requires thermally driven procedures, this process should be understood well to accurately simulate the structural response under actual operating conditions. The process of producing of U-Mo based dispersion plates by Hot Rolling is as follows. Fabrication is according the well established picture-frame technique. This method has been used successfully for years for commercial fabrication of Aluminum-based dispersion fuel plates. The frame contains a compact that is assembled in a cavity machined into the frame plate. Fuel compact is prepared with atomization process as explained in elsewhere [10]. U-7Mo powder is mixed with 6061AL powder. The blended powder is then compacted under pressure and placed in a frame made of 6061 Al alloy. Cover plates are placed to the top and the bottom to form the cladding as illustrated schematically in Fig. 1.





Assembly is then welded together and rolled under pressure to form a plate to reach the targeted thickness. The miniplates are produced by hot and cold rolling. The plates are hot rolled where the plates are in the furnace approximately 100 min at 500 °C and 15 min outside the furnace during the actual rolling. The plates are then cold rolled further to achieve the targeted thickness [11]. Dimensions for finished product are shown in Fig. 2.

The final high-temperature process of the fuel plates are exposing them a blister annealing for testing purposes. This is a standard practice to ensure that no blisters develop on the surface, which would be an indication of poor bonding between the fuel meat and the cladding. During blister annealing, plates are exposed to 485°C for 60 minutes.

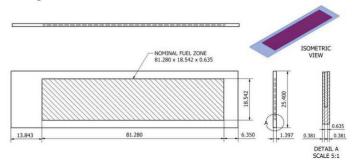
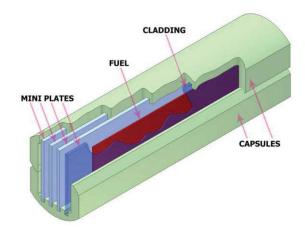
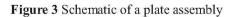


Figure 2 Dimensions [mm] of dispersion fuel plate

Once mini plates are fabricated as described, total 32 mini plates are then assembled into 4 capsules made of Al6061-T6. The capsules are positioned vertically in a basket and are cooled by direct contact with primary coolant. Flow velocities over the plates are 11 m/sec and 14 [m/sec] for outer and inner channels respectively. Approximate pressure of the primary coolant in ATR is 2.56 MPa. Representative schematic of plate assembly is shown in Fig. 3.





#### 2. MODELLING

There are numbers of published works investigating thermal stresses in multi-layered structures via thermo-structural coupling. However, available publications on multiscale-multiphysics simulations of multi-layered structures with consideration of residual stresses are still scarce. In addition, simulation efforts for structural response of newly developed U-Mo alloy based mini fuel plates are in very early stages. This article discusses the simulation efforts for U-Mo based fuel plates to provide in-depth understanding of Aluminum matrix-fuel particles stress/strain characteristics via microstructural based FE simulation techniques. The thermo-mechanical behavior of the plates and their initial response under actual

operating conditions with consideration of the residuals via fluid-thermal-structural interaction will be provided. The framework for the methodology and the techniques that were used for the multiscale-multiphysics simulations will be explained.

To provide an effective tool for assessment of structural response of the plates, it would be more realistic to use a simulation model as close as possible to the actual product. As explained previously, high temperatures are required during the fabrication process to achieve a proper thermo-mechanical bonding. Since multi layered structure has different components with different thermal and mechanical properties, residual stresses and stress gradients over the mechanical domain should be expected once the thermal transient is completed. It is important to emphasize that residual stresses are known to influence materials mechanical properties such as creep or fatigue life. Sometimes, the effect on mechanical properties is beneficial; and many other times, the effect is very deleterious. Improperly identified residuals would lead very deleterious results and consequently very poor conclusions. Therefore, identifying these stresses and including the residuals into subsequent simulations are crucial for accurate numerical results. However, considering fuel particles are dispersed in an Aluminum matrix, residuals cannot be simulated by simplified assumptions. Since location, size and orientation of the particles would greatly alter the mechanical response of the domain; involvement of microstructural characteristics should be considered. For this purpose, a non-linear thermomechanical simulation in micro-scale should be employed first.

It is well recognized that microstructure controls the physical and mechanical properties of a material. Since microstructures are such complex ensembles, correlating known microstructures with their physical and mechanical properties becomes very complicated task. Even single-phased materials may have such microstructural distribution and orientations that affect physical and mechanical properties and consequently structural response. Accurate representation of a microstructure is quite important across a wide range of disciplines for the prediction of properties and the simulation of structural response under mechanical and thermal loading. Analytical models and assumptions might provide acceptable predictions relatively simple configurations. However, these for approximations become very questionable in harsh environments for critical mechanical components such as reactor structures or nuclear fuels. Materials often contain defects and second phases in small fractions that can ultimately affect integrity and reliability. Because the two neighboring phases may have different thermal and mechanical properties. and these properties are dependent to orientation of the phases, other problems become quite significant such as residual stresses. Since, microstructural orientation and behavior is very difficult to predict, it is a challenging problem for scientists to quantify mechanical response at continuum level.

One way of computing the macroscopic behavior of a material sample with a complex microstructure is to construct a simulation model based on a micrograph of representative sectioning of the material. For this purpose, an effective numerical procedure, Image Based Finite Element has been developed by the scientists to implement mechanical and thermal properties and even determine structural response. This technique is very efficient and accurate for the numerical simulation of porous, composite and multi-phased materials with very complex geometries. The quality of the results produced with such a model obviously depends on the number of sections obtained from the material. To achieve desired accuracy, a microstructural characterization should be carried out. Then, representative microstructure can be used to produce realistic image-based finite element models [12-16]

There are several tools are available for image processing such as OOF2 with Abaqus interaction developed by NIST,  $\mu$ FEM with Ansys interaction developed by ORNL, LaGriT developed by LANL or iso2mesh with Matlab interaction. Benchmarking these tools is out of focus of this article. However, any of these tools can be successfully used for converting a microstructural image to a Finite element mesh. Since Comsol Multiphysics was employed for the multiphysics simulations presented in this article and Comsol has very effective Matlab interaction, image processing toolbox of Matlab and iso2mesh were found to be more effective.

Once residuals and plastic strains due to fabrication process are identified via microstructural based analysis, solution should be used as initial condition for subsequent multi-physics simulations in continuum level. In addition, since thermal response of the structure is mainly driven by amount of heat removed by primary coolant and heat removal rate is a function of the coolant velocity field and coolant temperature increases non-linearly while coolant travels along the path in the mini plate capsule and the heat generation rate has a non-uniform distribution along the plate width, fluid-structure interaction should be carefully coupled with fluid-thermal interaction before coupling them with structural mechanics. To achieve this, velocity and pressure fields of the coolant should be computed via fluid-structural interaction with thermal dependency. Computed velocity and pressure fields then should be used to identify temperature fields on both coolant and on the fuel plate via coupled fluid-thermal and thermal-structural interaction. Finally, computed temperature fields and residual stress distribution should be supplied to the solver to obtain the accurate mechanical response of a plate via coupled Fluid-Thermal-Structural interaction.

## 3. MATHEMATICAL PRELIMINARIES

#### 3.1. Structural Mechanics

Mechanical properties were assumed to be independent of direction but dependent of temperature. Hence, modulus of elasticity (E), Poisson's ratio (v) and shear modulus (G) were defined as follows,

$$E_x = E_y = E_z = E(T) \tag{1}$$

$$v_{xy} = v_{yx} = v_{xz} = v_{zx} = v_{yz} = v_{zy} = v(T)$$
(2)

$$G(T) = G_{xy} = G_{xz} = G_{yz} = \frac{E(T)}{2 \cdot [1 + \nu(T)]}$$
(3)

Assuming the material of interest undergoes small strains, linearized form of the strain tensor can be expressed as,

$$\varepsilon_{ij}^{total} = \frac{1}{2} \left( \frac{\partial u_i}{\partial u_j} + \frac{\partial u_j}{\partial u_i} \right)$$
(4)

Where,  $\mathcal{E}_{ij}$  and u strain tensor and displacements respectively. At each point of the plate, the total-strain components  $\mathcal{E}_{ij}^{total}$  are represented as the sum of the corresponding components of the elastic, plastic, thermal and initial ones. Such as,

$$\varepsilon_{ij}^{total} = \frac{1}{2} \left( u_{i,j} + u_{j,i} \right) = \varepsilon_{ij}^{el} + \varepsilon_{ij}^{pl} + \varepsilon_{ij}^{th} + \varepsilon_{ij}^{in} \tag{5}$$

Furthermore, thermal strain tensor  $\mathcal{E}_{kl}^{th}$  is expressed by,

$$\varepsilon_{kl}^{th} = \alpha_{kl} \left( T \right) \times \Delta T \tag{6}$$

 $\alpha_{kl}(T)$  is the tensor governing coefficient of thermal expansion, and  $\Delta T$  is the temperature change from the reference point. The mechanical constitution of the plate was assumed to be in the following form:

$$\sigma_{ij} = D_{ijkl} \times \varepsilon_{kl}^{el} + \sigma_{ij}^{in} \tag{7}$$

Where,  $D_{ijkl}$  is 6x6 temperature dependent elasticity matrix (i.e.  $D_{ijkl}(T)$ ),  $\varepsilon_{kl}^{el}$  elastic strain tensor, and  $\sigma_{ij}^{in}$  is initial or namely residual stresses. Substituting elastic strains into the mechanical constitution gives the stress distribution on the plate expressed as,

$$\sigma_{ij} = D_{ijkl} \times \left(\varepsilon_{kl}^{total} - \varepsilon_{kl}^{pl} - \varepsilon_{kl}^{th} - \varepsilon_{kl}^{in}\right) + \sigma_{ij}^{in} \tag{8}$$

Material flow was defined according to Von-Mises rule as follows,

$$F_d(\sigma_{ij},\bar{\varepsilon}) = \frac{1}{2}\sigma_{ij}'\sigma_{ij}' - \frac{1}{3}\sigma_s^2(\bar{\varepsilon})$$
<sup>(9)</sup>

#### 3.2. Fluid Flow

Generalized version of the Navier-Stokes equations was solved over the domain to allow for variable viscosity. Starting with the momentum balance in terms of stresses, the generalized equations in terms of transport properties and velocity gradients can be expressed in momentum transport equation defined as follows;

$$\rho \frac{\partial u}{\partial t} - \nabla \cdot \left[ \eta \left( \nabla u + (\nabla u)^T \right) \right] + \rho (u \cdot \nabla) u + \nabla p = F$$
(10)

Equation of continuity for incompressible fluids is;

$$\nabla \bullet u = 0 \tag{11}$$

Where  $\eta$  is the dynamic viscosity,  $\rho$  is the density, u is the velocity field, P is the pressure and F is volume force field. Temperature dependent data for viscosity and density was used to allow the thermal effects.

#### 3.3. Thermal Transport

The fundamental law governing heat transfer is the first law of thermodynamics, or the principle of conservation of energy. The basic law is usually expressed in terms of temperature for convenience. Following heat equation solved over the coolant domain;

$$\rho C_{p} \frac{\partial T}{\partial t} + \nabla \cdot \left(-k \nabla T\right) = Q - \rho C_{p} \mathbf{u} \cdot \nabla T$$
(12)

Where  $\rho$  is the density,  $C_p$  is the specific heat capacity at constant pressure, T is absolute temperature, k is the thermal conductivity, u is the velocity vector, Q is the heat sources other than viscous heating. For solid, u (velocity vector) is set to be zero and therefore, governing equation for pure conductive heat transfer in fuel foil and cladding is expressed as;

$$\rho C_p \frac{\partial T}{\partial t} + \nabla \cdot (-k \nabla T) = Q$$
<sup>(13)</sup>

Heat transfer coefficient between the bulk of the fluid and the cladding surface was computed via Dittus–Boelter correlation;

$$h = \frac{k_w}{D_H} N u \tag{14}$$

Where  $k_w$  thermal conductivity of the coolant,  $D_H - D_i$  is hydraulic diameter and Nu is Nusselt number formulated as;

$$Nu = 0.023 \cdot \operatorname{Re}^{0.8} \cdot \operatorname{Pr}^{n} \tag{15}$$

Where Re - Reynolds number, Pr - Prandtl number and n = 0.4

#### **4. MATERIAL PROPERTIES**

As the hot rolling temperature reaches 500°C, material properties at such high temperatures are crucial to obtain more accurate simulation results. These properties and experimental

details are available elsewhere [17-22]. For completeness, compilation of the material properties that were used in the multiphysics simulations is given in Table 1 below.

 Table 1 Material Property
 [17-22] (\*)

CLADDING (/	AT COCL TON ())
	1 6061-1(1)

CLAL	DDING (ALE	/												
Young	g Modulus	Poisson's Ratio		Yield Stress		Therr	Thermal Expansion		Conductivity		Specific Heat		Density	
[C]	[GPa]	[C]	[-]	[C]	[MPa]	[C]	[1/K]	[C]	$[W/m \cdot K]$	[C]	[J/kg·K]	[C]	[kg/m <sup>3</sup> ]	
21	69.63	21	0.330	24	55.15	100	$23.60 \times 10^{-6}$	0	177	17	896	23	2702	
93	66.39	100	0.334	149	55.15	200	24.30x10 <sup>-6</sup>	27	180	127	942	560	2702	
149	63.43	149	0.335	177	51.71	300	$25.40 \times 10^{-6}$	126	189	227	988			
204	59.63	204	0.336	204	44.81			227	191	327	1034			
260	54.12	260	0.338	232	36.54			327	190	427	1080			
287	49.92	316	0.360	260	27.57			426	185	527	1126			
316	47.17	371	0.400	288	22.06			526	179	581	1151			
371	43.51	427	0.410	315	17.92			581	175					
427	28.77	482	0.420	371	12.41									
482	20.20			560	6.89									

#### FUEL PARTICLES (U7Mo) (2)

Young	g Modulus	Poisson's Ratio		Yield Stress <sup>(3)</sup>		Thermal Expansion		Cor	Conductivity		Specific Heat		Density	
[C]	[GPa]	[C]	[-]	[C]	[MPa]	[C]	[1/K]	[C]	$[W/m \cdot K]$	[C]	[J/kg·K]	[C]	$[kg/m^3]$	
21	83.00	25	0.250	20	734.00	50	11.81x10 <sup>-6</sup>	23	11.30	23	145.2	23	17200	
126	80.00	560	0.250	100	644.73	100	$12.42 \times 10^{-6}$	100	13.23	100	152.9	560	17200	
				200	549.73	200	13.63x10 <sup>-6</sup>	200	15.16	200	160.6			
				300	464.82	300	$14.84 \mathrm{x} 10^{-6}$	300	18.16	300	168.8			
				400	424.58	400	$16.05 \times 10^{-6}$	400	21.66	400	177.0			
				500	306.53	500	17.26x10 <sup>-6</sup>	500	25.30	500	184.7			
				600	295.08	600	$18.47 \times 10^{-6}$	600	28.25	600	192.9			

MATRIX (40%U7Mo + 60%AL6061) (4)

Young	g Modulus	Poisson's Ratio		Yield Stress		Thermal Expansion		Cor	Conductivity		Specific Heat		Density	
[C]	[GPa]	[C]	[-]	[C]	[MPa]	[C]	[1/K]	[C]	[W/m·K]	[C]	[J/kg·K]	[C]	$[kg/m^3]$	
21	74.98	25	0.300	24	326.69	50	$18.4 \times 10^{-6}$	25	98	26	325	23	6711	
93	72.22	100	0.300	100	290.98	100	18.6x10 <sup>-6</sup>	100	103	102	343	560	6711	
149	70.06	149	0.300	149	272.36	200	$19.3 \text{x} 10^{-6}$	150	105	202	359			
204	67.78	204	0.300	200	247.39	300	$19.9 \mathrm{x} 10^{-6}$	200	106	302	371			
260	64.47	260	0.300	300	198.06	400	$20.6 \times 10^{-6}$	250	106	402	386			
287	61.95	316	0.320	371	181.95	500	$20.0 \times 10^{-6}$	300	107	451	402			
371	58.11	371	0.340	400	176.77	600	$20.4 \mathrm{x} 10^{-6}$	350	107	501	410			
427	49.26	427	0.350	500	127.80			400	107					
482	44 12	482	0.350	560	122.80			500	107					

#### COOLANT (5)

D	Density		Conductivity		Specific Heat		Heat Transfer Coef		Kin. Viscosity		Dyn. Viscosity	
[K]	[kg/m <sup>3</sup> ]	[K]	[W/mK]	[K]	[J/kgK]	[K]	$[W/(m^2 \cdot K)]$	[K	$[m^2/s]$	[K]	[Pa.s]	
274	1003.95	273	0.5562	274	4216.58	274	41346	274	$1.79 \times 10^{-6}$	273	$1.79 \mathrm{x} 10^{-3}$	
300	997.65	300	0.6056	300	4181.48	300	57303	30	$8.53 \times 10^{-7}$	300	$8.52 \times 10^{-4}$	
350	975.71	350	0.665	350	4191.84	340	78314	35	) $3.82 \times 10^{-7}$	350	$3.73 \text{x} 10^{-4}$	
400	940.67	400	0.687	400	4262.9	400	102745	40	) $2.32 \times 10^{-7}$	400	$2.17 \text{x} 10^{-4}$	
450	892.8	450	0.6777	450	4398.89	440	111376	45	) $1.77 \times 10^{-7}$	450	$1.55 \text{x} 10^{-4}$	
500	832.39	500	0.6431	500	4658.38	500	116649	50	) $1.46 \times 10^{-7}$	500	$1.23 \text{x} 10^{-4}$	

(1) Reference [17] claims that Poisson Ratio is independent of temperature. Data from [22] was used instead for both Poisson's Ratio and Young Modulus.

(2) Unreported particle properties for U7Mo were approximated with properties of U10Mo monolithic plates.

(3) Hardness data was used to approximate the yield level for U10Mo and U7Mo.

(4) Except conductivity and specific heat reported by Lee in [20] and [21], the matrix properties were computed by rule of mixture.

(5) Heat transfer coefficient was computed by using Dittus-Boelter correlation.

(\*) No extrapolation was performed for unknown data. Data for outside the bounds was approximated to the nearest neighbor.

Interpolations between the known temperatures were performed by piecewise cubic splines.

#### 5. HOT ROLLING and RESIDUALS 5.1. Microstructure Based FE Model

Since fuel particles are dispersed in an Aluminum matrix and location, size and orientation of the particles would alter the structural response of the domain; involvement of microstructural characteristics should be considered and consequently, numerical model should include these geometric characteristics. For this purpose, a non-linear thermomechanical simulation in micro-scale should be employed first. Then, solution of the micro-model can be used as initial condition for the subsequent simulations in the continuum level. Since every proceeding simulations is built on the residuals presented here, the accuracy of this simulation is quite important. At this point, the reader should be aware of the deterministic nature of this technique. It is quite important to note that the representative micro-structure and its location in the mechanical domain would alter the simulation results. However, since dispersion matrix has relatively simple configuration and the ultimate goal of this simulation is to obtain the structural response of the Aluminum matrix and the matrix material reaches to its yield level, results presented here are satisfactory for use in subsequent simulations. On the other hand, if the particle response alone is the concern, then, more detailed SEM investigations at various sections should be carried out to increase the accuracy via statistical approaches.

To calculate the fabrication induced residuals on the dispersion fuel compound (U7Mo+Al6061) after Hot Rolling process, general purpose commercial FE solver, Comsol Multiphysics was employed and computational clusters at Idaho National Laboratories was utilized. An image of representative microstructure was used to construct the model. SEM image of representative section is shown in Fig. 4a.

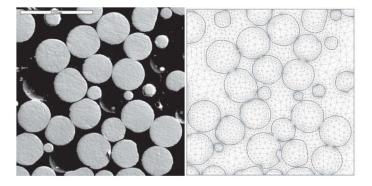


Figure 4 Microstructural image and resulting FE model

Image processing toolbox of Matlab and iso2mesh was employed to convert the microstructure to a Finite Element mesh. An appropriate number of seeds are assigned to the particle boundaries. First, the fuel particles were meshed; then, matching mesh was assigned to Aluminum matrix. At the particle boundaries, a denser mesh was used to increase the accuracy of the solution. Resulting finite element mesh is shown in Fig. 4b.

One node (lower left corner) of the model was fixed and horizontal boundary at the bottom was constrained to restrict the motion on the vertical direction. Fuel was represented by using quadratic triangular elements totaling 7408 elements, while cladding contains 4135 quadratic triangular elements. Elasto-thermo-perfectly-plastic material models were assigned to both 6061 Aluminum matrix and U7Mo fuel particles to simulate thermo-plasticity. Elasto-plastic parametric solver with reduced integration was used to minimize the computational expense. Since amount of time under temperature is small, thermal creep was assumed to have negligible effect. It was also assumed that complete mechanical bonding would be achieved at exact hot rolling temperature, and therefore 500°C was assumed to be reference point for the hot rolling simulation. From 500C, 20 sub-steps were used to reach the room temperature. Solution was stored for every 25°C temperature drop for mechanical history.

#### 5.2 Results and Discussions

Equivalent stress distribution over the domain is shown in Fig. 5. It was noted a complete plastic deformation of the matrix material (Al6061TO) with tensile residuals and compressive stresses on the particles (U7Mo). In Fig. 5, particles register stresses less than their yield level. However, existence of several hot spots was noted. It was understood that even though there are higher local residuals on the particles, matrix material holds approximately 55 MPa residuals at the end of hot rolling.

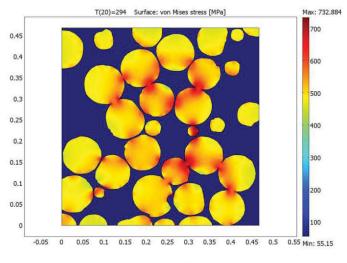


Figure 5 Equivalent stress distribution on the matrix

Once solution in micro level was obtained, a 2D symmetric model was constructed to solve the problem in macro level. Similarly, it was assumed 500°C is the perfect bonding temperature and 20 sub-steps were used to reach the room temperature. For every 25°C temperature drop solution was stored. Micro structure was assumed to be repetitive. Consequently, solution of micro model was supplied to the 2D continuum model as periodic condition. Similar meshing methodology and FE construction techniques were employed.

Equivalent stress distribution over the plate and the particles is shown in Fig. 6. Solution was compared with Fig. 5 for verification.

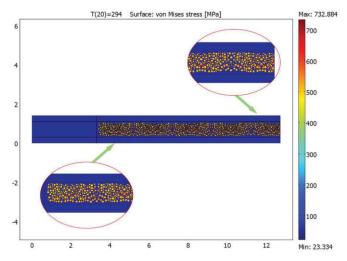


Figure 6 Equivalent stresses distribution in 2D

Mechanical response of the particles and the matrix with respect to temperature is shown in Fig. 7. Even though particles hold average 400 MPa compressive residuals, maximum values were presented also. Maximum values were captured from the particles regardless of their location. It was noticed that residuals on the articles are higher where mesh densities increase due to the sharp corners between the particles. One might use even finer mesh to get more precise results for the sharp corners of the particles, if particles alone are concern. Matrix material (Al6061-TO) follows the flow rule presented in material data previously and reaches to complete yielding. Consequently, 55 MPa residuals on the matrix at the end of the Hot Rolling should be expected.

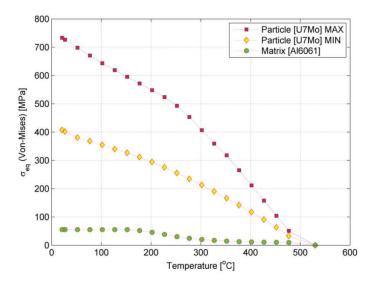


Figure 7 Stress history for the particles and the matrix

#### 6. BLISTER ANNEALING 6.1. FE Model

Blister annealing is a common practice to ensure that no blisters develop on the surface, which would be an indication of poor bonding between the fuel meat and the cladding. During blister annealing, plates are exposed to 485°C (758K) for 60 minutes. Since residual stresses were identified via microstructural based simulation, solution was used for subsequent simulations. Obviously, whole plate could be modeled by using a repetitive microstructure in 3D. However, this would be computationally very expensive. Therefore, two distinct simulations were considered. First one considers the overall response of the plates in 3D and second one investigates the particle response in microstructural level.

Because of the symmetry, only one-half of the plate was modeled. Since eight-node hexahedral elements produce more accurate results, brick elements with mapped meshing were used for discretization. Fuel was represented by using 3 layers totaling 2250 quadratic elements, while cladding was represented by 9 layers contains 8280 quadratic elements. Elasto-thermo-perfectly-plastic material models were assigned to both cladding material and fuel compound to simulate thermo-plasticity. One node (lower left corner) of the model was constrained in three directions to prevent rigid body motion. On the mid boundary, symmetry condition was assigned to corresponding nodes. Half symmetric FE model along with partial cut is shown in Fig. 8.

Residual stresses were introduced to the solver as an initial condition. Namely normal and shear components in all 3 directions were included on fuel compound. Elasto-plastic parametric solver with reduced integration was employed. Since amount of time under temperature is small, thermal creep was assumed to be zero. Fuel compound is mixture of 40%U7Mo and 60%Al6061. Material properties of the compound which was presented previously were assigned accordingly. 21 °C was assumed to be reference point for the blister annealing simulation. At this temperature, plate was assumed to be free of any defects. Since, blister annealing require the plates to be exposed to 485°C, 22 sub-steps with 25°C increase in each step were used to reach annealing temperature.

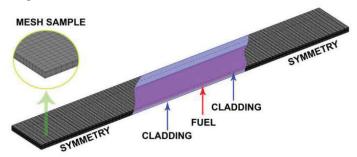


Figure 8 Half symmetric FE model

#### 6.2 Results and Discussions

Equivalent stress distribution and effective plastic strains are shown in Fig. 9 and Fig. 10 respectively.

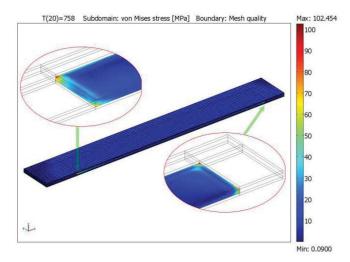


Figure 9 Equivalent stresses

It seems cladding material over the fuel region manifests further plastic deformations due annealing. However, blister acts as a stress relief on the plate body. Equivalent stress distribution on the fuel is more or less uniform; however, higher concentration was observed once closer to the fuel ends.

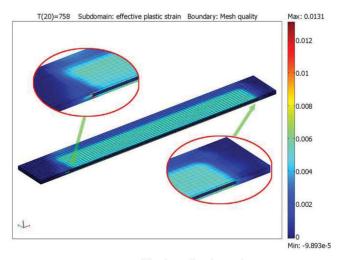
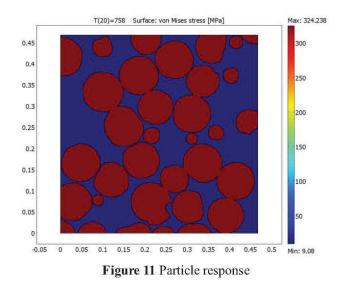


Figure 10 Effective plastic strains

To understand the response of the fuel region and fuel particles under blister annealing, microstructure based simulation was repeated. Same microstructural model presented before was modified to compute the response of the fuel region. Same boundary conditions and similar methodology were employed. Two stepped elasto-plastic parametric solver with reduced integration was used. Blister simulation was introduced as subsequent step for hot rolling simulation which was previously discussed. 21 °C was assumed to be reference point for the second step. Similarly, 22 sub-steps with 25°C increase in each step were created. Residual stresses from step 1 were introduced to the solver as an initial condition.



Plastic strains are significantly lower on fuel particles. However high stress gradients were noted. Aluminum matrix has approximately 9 MPa equivalent stresses while fuels register approximately 325 MPa. It seems blister acts as a stress relief on both matrix and particles.

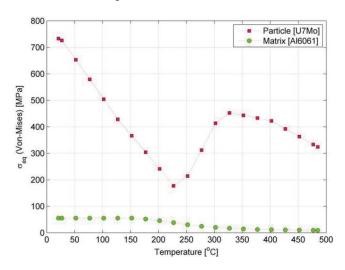


Figure 12 Blister Response of particles and matrix

Fig. 12 presents equivalent stress history calculated for the particles and matrix material. However, at approximately 225 °C, normal stresses change direction from compression to tension. Equivalent stresses drop to 325 MPa which is significantly lower than 730 MPa as computed for the Hot Rolling. Assuming there are no significant microstructural changes that would hinder the mechanical properties, then, the plate should overcome the thermal stresses under extreme temperatures occurs during the annealing step.

#### 7. IN-REACTOR RESPONSE 7.1 Multiphysics FE Model

To provide an effective tool for benchmarking of structural response of the mini plates, it would be more realistic to use a simulation model as close as possible to the actual operating conditions. For this purpose, multi-step coupled multiphysics simulations were carried out. Once residuals and plastic strains due to fabrication process are identified via image based FE analysis as discussed previously, computed residuals were used as initial condition for subsequent multi-physics simulations. Since thermal response of the structure is driven by the amount of the heat removed by the primary coolant and, the heat removal rate is a function of the coolant velocity field and, coolant temperature increases while the coolant travels along the path in the mini plate capsule, fluid-structure interaction was coupled with fluid-thermal interaction. To achieve this, velocity and pressure fields of the coolant was computed via fluid-structural interaction with thermal dependency. Computed velocity and pressure fields were used to identify temperature fields on both coolant and on the fuel plate via coupled fluidthermal and thermal-structural interaction. Finally, computed temperature fields and residual distribution were supplied to the solver to obtain the mechanical response of the plate via coupled Fluid-Thermal-Structural interaction.

Because of the symmetry, only one-half of the plate (cut through from the mid-plane, i.e. fuel core) was modeled. Since eight-node hexahedral elements produce more accurate results, brick elements with mapped meshing were used for domain discretization. Fuel was represented by using 3 layers totaling 7500 quadratic elements, while cladding contains 16656 quadratic elements distributed to 6 layers. Coolant was represented with 10 layers totaling 40260 quadratic elements. Resulted finite element model is shown in Fig. 13.

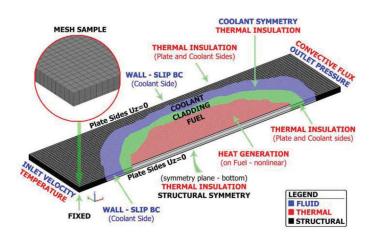


Figure 13 Coupled multi-physics FE setup

For fluid flow, temperature dependent viscosity and density were assigned to corresponding elements. Inlet velocity of 14 [m/sec] and outlet boundary condition was assigned to corresponding nodes. Initial pressure of 2.56 MPa was assigned to coolant section. Coolant sides were treated as wall boundaries and slip conditions were assigned accordingly. Similar with symmetry condition used for solid portion, due to the symmetry of the coolant, only half of the coolant was modeled and consequently, symmetry boundary condition was assigned to the nodes on the top of the coolant.

For thermal transport, temperature dependent thermal properties (conductivity, specific heat and density) were assigned to corresponding domains namely to fuel, cladding and coolant. Velocity fields from previous simulation were assigned to coolant. Inlet side was constrained with proposed inlet temperature (52 °C). Due to the small thickness of the plate, heat escape from the plate sides was assumed to be negligible and therefore, mini plate sides were treated as insulated boundaries. Symmetry/insulation boundary condition was assigned to the plate mid layer (i.e fuel core) as well as to symmetry plane for the coolant. Convective flux was assigned to the nodes located at outlet side. Heat source/sink condition was assigned to the nodes shared by solid and the coolant to handle the heat transfer between two. Due to non-uniform fission density, fuel matrix closer to ATR core has higher heat generation rate. For thermally accurate simulations, this nonlinearity should be considered. Heat generation rate was supplied to the solver via parametric formulation. Experimental data for fission density was used to compute the power profile shown in Fig. 14. Polynomial representation of the profile was multiplied with average heat generation rate of 10000 W/cm<sup>3</sup> to formulate the heat generation rate in space domain. Finally, relation shown in Eq. 16 was supplied to the solver to include this thermal non-linearity on the fuel compound.

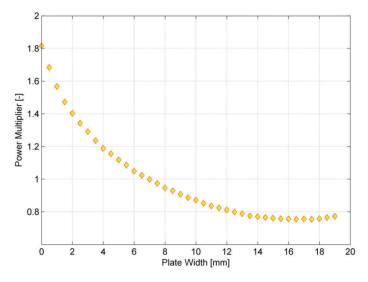


Figure 14 Power profile along the plate width

$$Q(x,t) = P_{av}(t) * (0.00002783 * x^{4} - 0.001278 * x^{3} + 0.02321 * x^{2} - 0.2231 * x + 1.785) [W/cm^{3}]$$
(16)

In Eq. 16, Q is the heat generation rate, P is average power (10000 W/cm<sup>3</sup> for this simulation) and x is the distance [mm] along the plate width.

For structural mechanics simulations, elasto-thermo-perfectlyplastic material models were assigned to both cladding and fuel materials to simulate thermo-plasticity. One node (lower left corner) of the model was constrained in three directions to prevent rigid body motion. Since fuel plate goes into a guided channel in fuel assembly, side nodes were constrained accordingly. On the mid boundary, symmetry condition was assigned to corresponding nodes. Residual stresses were introduced to the solver as initial condition. Namely normal and shear components in all 3 directions were added in to formulation. Thermal result of Fluid-Thermal interaction was assigned accordingly as loading to compute thermal displacements. Elasto-plastic parametric solver with reduced integration was employed. Since amount of time under temperature is small, thermal creep was assumed to have negligible effects. Fuel compound is mixture of 40% U7Mo and 60% Al6061 and material properties of the compound were assigned accordingly. The plate was assumed to be free of any defects at the room temperature (i.e. no premature cracks).

It should be noted that there exist possible convergence problems, once different physics with material non-linearity are coupled together and solved simultaneously. Making the coolant mesh unnecessarily dense would create equivalently dense structural mesh and therefore, structural mechanics might experience convergence problems, especially if solution goes in to plastic region. On the other hand, using too coarse mesh in solid section would lead to inaccurate temperature field and consequently wrong thermally driven stress fields. If the structural response is the ultimate goal, while still carefully considering other disciplines, several degrees of deviation in temperature field would not alter overall behavior of the plate dramatically. Optimizing the mesh density was left to reader's expertise and will not be discussed here. In addition, it is known that material properties degrade under irradiation and the plate experiences phenomenon such as particle swelling and irradiation induced creep. Since this article considers only initial response of the plates and data for these variables is not available yet, these phenomenon were not considered. However once degraded material properties are available, simulation results should be updated for full transient behavior.

#### 7.2 Thermal Response

Even though temperature of the ATR's primary coolant does not appear in structural calculations, it affects the thermal solution of the solid domain due to its interaction with it. Once fluid motion was computed via Fluid-Structural interaction, velocity field were used to thermal response of the coolant. Figure 15 shows computed temperature field of the coolant film layer. As expected, coolant has 52 °C on the inlet side. Temperature gradients due to non-linear heat generation rate were noted. In addition, coolant experiences temperature increase while it travels through the channel. These thermal gradients closer to the outlet side are more noticeable. Highest temperature for film layer of the coolant was computed as 92.8 °C as shown in the Fig. 15.

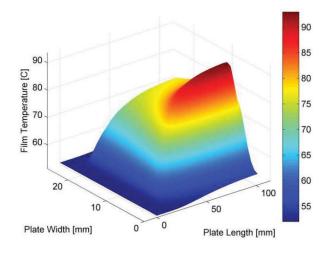


Figure 15 Temperature field of the primary coolant film

While cladding surface exhibits approximately 93°C, maximum temperature between the cladding material and the fuel compound is approximately 102 °C as shown in Fig. 16. Not surprisingly, highest temperature was recorded closer to the ATR core on the outlet side of the primary coolant.

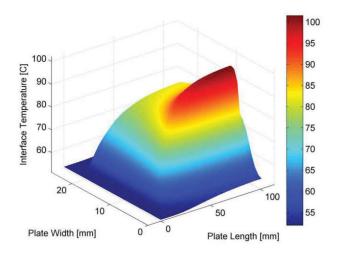


Figure 16 Temperature between cladding and fuel matrix

The temperature field for the fuel core (i.e. plate mid plane) is presented Fig. 17. Highest temperature computed for the fuel compound is approximately 108 °C on the outlet side of the coolant. Thermal gradients are more noticeable due to the non uniform heat generation rate as presented in Fig.14 and formulated in Eq. 16. Even though inlet side is considerably colder, plate experiences temperature increase closer to the outlet side due to the temperature increase of the ATR's primary coolant.

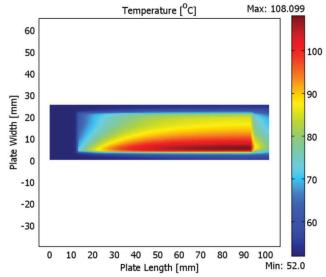


Figure 17 Temperature field at the fuel core (plate mid-plane)

#### 7.3 Structural Response

The final step of the multiphysics simulations is to couple previously computed results. Residual stresses which were computed via parametric structural-thermal interaction (presented in Section 5.2), and temperature fields which were computed via coupled fluid-structural and thermal-fluid interaction (presented in Section 7.2) were used to simulate the structural response of the plate via thermal-structural interaction. Computed temperature values were assigned to corresponding nodes as thermal loads and residuals due to fabrication process were assigned accordingly as initial loading.

Figure 18 shows displacement field of the dispersion mini plate. Maximum total displacement was computed as 0.109 mm, while directional displacements were 0.108 mm, 0.037 mm and 0.0012 mm on x, y and z respectively.

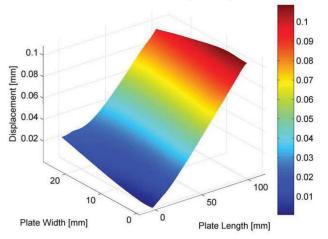


Figure 18 Total displacements on the plate

Corresponding strains to the directional displacements were computed as 0.0015, 0.0021 and 0.0020 on x, y, and z directions respectively.

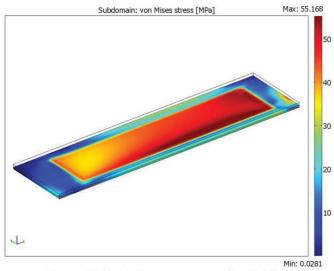


Figure 19 Equivalent stresses on the cladding

Equivalent stresses on the cladding material (Al6061-TO) are shown in Fig. 19. Cladding over the fuel region holds approximately 55 MPa due to the fabrication induced residuals. No further plastic strains were noted in addition to plastic strains developed during the fabrication.

Figure 20 shows equivalent stress distribution on the fuel matrix (40%U7Mo + 60%AL6061). While fuel compound holds approximately 50 MPa, equivalent stresses increase to approximately 145 MPa at regions close to the interface. Assuming there are no preexisted defects, fuel compound should not experience any problems due to the thermally driven stress gradients, if Von-Mises failure criteria is used.

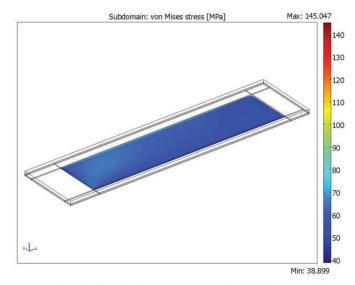


Figure 20 Equivalent stresses on the fuel compound

Figure 21 shows equivalent stresses distribution on the fuel cladding interface to further investigate the gradients. Fuel compound-cladding interface registers approximately 65 MPa.

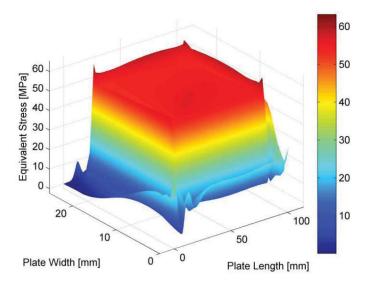


Figure 21 Equivalent stresses on the fuel cladding interface

Figure 22 shows equivalent stresses distribution on the cladding surface. Highest stresses were computed as 55 MPa and found to be closer to the outlet side of the reactor core.

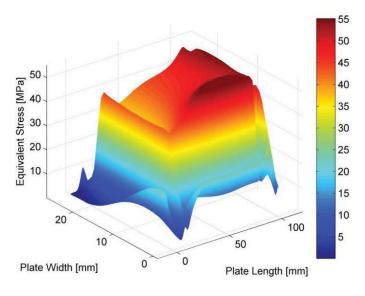


Figure 22 Equivalent stresses on the cladding surface

Obviously, whole plate can be modeled by using microstructure. However, this would be computationally very expensive. If particle response alone is a concern, similar methodology can be employed to simulate the particle responses in micro-scale. However, purpose of this article was overall response of the plate; therefore, this simulation will not be discussed here.

#### 8. CONCLUSIONS

Thermo-mechanical response of the dispersion fuel mini-plates under in-reactor conditions was investigated. The analysis demonstrated that residual stresses still govern the mechanical response of the plate. Compared to proposed monolithic fuel, dispersion plates showed significant compliance. Unless there is a micro failure (i.e. particle-Al matrix separation), in overall, plate demonstrated no structural weakness under in reactor conditions. Since this article considered initial response of the plate, particle swelling, creep and material degradation were not included. For full transient behavior, these variables should be included in micro scale when the material data becomes available.

#### 9. ACKNOWLEDGMENTS

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#### **10. NOMENCLATURE**

$C_p$	Specific heat capacity
$D_{ijkl}$	Elasticity matrix
$\mathrm{D}_{\mathrm{H}}$	Hydraulic diameter
E	Modulus of elasticity
F	Volume force field
G	Shear modulus
h	Heat transfer coefficient
k	Thermal conductivity
Nu	Nusselt number
Pr	Prandtl number
р	Pressure
Q	Heat source
Re	Reynolds number
Т	Temperature
$lpha_{\scriptscriptstyle kl}$	Tensor for coefficient of thermal expansion
${\cal E}_{ij}$	Strain tensor
$\eta$	Dynamic viscosity
$\sigma_{ij}$	Stress tensor
ρ	Density
$u_i$	Displacement
v	Poisson's ratio

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