# Azimuthal anisotropy: the higher harmonics 

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#### Abstract

We report the first observations of the fourth harmonic ( $v_{4}$ ) in the azimuthal distribution of particles at RHIC. The measurement was done taking advantage of the large elliptic flow generated at RHIC. The integrated $v_{4}$ is about a factor of 10 smaller than $v_{2}$. For the sixth $\left(v_{6}\right)$ and eighth $\left(v_{8}\right)$ harmonics upper limits on the magnitudes are reported.


Anisotropic flow, an anisotropy of the particle azimuthal distribution in momentum space with respect to the reaction plane, is a sensitive tool in the quest for the quark-gluon plasma and the understanding of bulk properties of the system created in ultrarelativistic nuclear collisions. It is commonly studied by measuring the Fourier harmonics $\left(v_{n}\right)$ of this distribution [1]. Elliptic flow, $v_{2}$, is well studied at RHIC and is thought to reflect conditions from the early time of the collision. Recently, Kolb [2] reported that the magnitude and even the sign of $v_{4}$ are more sensitive than $v_{2}$ to initial conditions in the hydrodynamic calculations. Besides one early measurement at the AGS [3], reports of higher harmonics have not previously been published. Some of the present work has already appeared (4).

Experiment - The data come from the reaction $\mathrm{Au}+\mathrm{Au}$ at $\sqrt{s_{\mathrm{NN}}}=200 \mathrm{GeV}$. The STAR detector main time projection chamber (TPC) was used in the analysis of two million events. The main TPC covered pseudorapidity $(\eta)$ from -1.2 to 1.2 and the low transverse momentum $\left(p_{t}\right)$ cutoff was $0.15 \mathrm{GeV} / c$. In the present work all charged particles were analyzed, regardless of their particle type. The errors presented in the figures are statistical.

Analysis - The difficulty is that the signal is small and the non-flow contribution to the two-particle azimuthal correlations can be larger than the correlations due to flow. To suppress the non-flow effects the current analysis uses the knowledge about the reaction plane derived from the large elliptic flow. One method for eliminating the non-flow contribution in a case when the reaction plane is known was proposed in [1]. Results obtained with this method we designate by $v_{4}\left\{E P_{2}\right\}$. The analysis for $v_{4}$ was also done with three-particle cumulants [5] by measuring $\left\langle\cos \left(2 \phi_{a}+2 \phi_{b}-4 \phi_{c}\right)\right\rangle$.
$P_{t}$-dependence - The results as a function of $p_{t}$ are shown in Fig. ⿴囗 (left) for minimum bias collisions ( $0-80 \%$ centrality). Shown for $v_{4}$ are both the analysis relative to the second harmonic event plane, $v_{4}\left\{E P_{2}\right\}$, and the three-particle cumulant, $v_{4}\{3\}$. § For the full author list and acknowledgments see Appendix "Collaborations" in this volume.

Both methods determine the sign of $v_{4}$ to be positive. As a function of $p_{t}, v_{4}$ rises more slowly from the origin than $v_{2}$, but does flatten out at high $p_{t}$ like $v_{2}$. The $v_{6}\left(p_{t}\right)$ values are consistent with zero. Ollitrault has proposed [6] for the higher harmonics that $v_{n}$ might be proportional to $v_{2}^{n / 2}$ if the $\phi$ distribution is a smooth, slowly varying function of $\cos (2 \phi)$. In order to test the applicability of this $v_{2}$ scaling we have also plotted $v_{2}^{2}$ and $v_{2}^{3}$ in the figure as dashed lines. The proportionality constant has been taken to be 1.2 in order to fit the $v_{4}$ data. The ratio, $v_{4} / v_{2}^{2}$, is shown in Fig. 1 (right) as a function of $p_{t}$.


Figure 1. (left) The minimum bias values of $v_{2}, v_{4}$, and $v_{6}$ with respect to the second harmonic event plane as a function of $p_{t}$ for $|\eta|<1.2$. The $v_{2}$ values have been divided by a factor of two to fit on scale. Also shown are the three particle cumulant values (triangles) for $v_{4}\left(v_{4}\{3\}\right)$. The dashed curves are $1.2 \cdot v_{2}^{2}$ and $1.2 \cdot v_{2}^{3}$. (right) The ratio $v_{4} / v_{2}^{2}$ is plotted against $p_{t}$. The dashed line is at the value of 1.2 .

Parton coalescence - Assuming a simple parton coalescence model, for mesons one gets [7]

$$
\begin{equation*}
v_{4} / v_{2}^{2} \approx 1 / 4+1 / 2\left(v_{4}^{q} /\left(v_{2}^{q}\right)^{2}\right) \tag{1}
\end{equation*}
$$

Since experimentally this ratio is $1.2, v_{4}^{q}$ must be greater than zero. If one assumes that the hadronic $v_{2}^{2}$ scaling results from partonic $v_{2}^{2}$ scaling [8], then

$$
\begin{equation*}
v_{4}^{q}=\left(v_{2}^{q}\right)^{2} \tag{2}
\end{equation*}
$$

and

$$
\begin{equation*}
v_{4} / v_{2}^{2}=1 / 4+1 / 2=3 / 4 . \tag{3}
\end{equation*}
$$

But this is still less than 1.2. Therefore either $v_{4}^{q}$ is even greater than simple parton $v_{2}^{2}$ scaling would indicate, or the simple parton coalescence model is inadequate.

Waist - Kolb [2] points out that for $v_{2}>10 \%$, which occurs at high $p_{t}$, and no other harmonics, the azimuthal distribution is not elliptic, but becomes "peanut" shaped. He calculates the amount of $v_{4}$ (which looks like a four-leaf clover) needed to eliminate this waist. Our values of $v_{4}$ as a function of $p_{t}$ are about a factor of two larger than needed to just eliminate the waist.

Centrality-dependence - The values of $v_{4}\left(p_{t}\right)$ for eight centrality bins are shown in Fig. 2 (left). Integrating these values weighted with the yield gives Fig. 2 (right) which shows the centrality dependence of $v_{2}, v_{4}$, and $v_{6}$ with respect to the second harmonic event plane and also $v_{4}$ from three-particle cumulants $\left(v_{4}\{3\}\right)$. The $v_{6}$ values are close to zero for all centralities. To again test the applicability of $v_{2}^{n / 2}$ scaling we have also plotted $v_{2}^{2}$ and $v_{2}^{3}$ in the figure as dotted histograms. The proportionality constant has been taken to be 1.4 to approximately fit the $v_{4}$ data. The larger constant here compared to that used in Fig. $\square$ is understood as coming from the use of the square of the average instead of the average of the square, and because the integrated values weighted by yield emphasize low $p_{t}$, where the best factor is slightly larger.


Figure 2. (left) $v\left(p_{t}\right)$ for the centrality bins (bottom to top) 5 to $10 \%$ and 10,20 , $30,40,50,60$, and 70 up to $80 \%$. (right) The $p_{t^{-}}$and $\eta$ - integrated values of $v_{2}, v_{4}$, and $v_{6}$ as a function of centrality. The $v_{2}$ values have been divided by a factor of four to fit on scale. Also shown are the three particle cumulant values for $v_{4}\left(v_{4}\{3\}\right)$. The dotted histograms are $1.4 \cdot v_{2}^{2}$ and $1.4 \cdot v_{2}^{3}$.

The $v_{n}\left\{E P_{2}\right\}$ values averaged over $p_{t}$ and $\eta(|\eta|<1.2)$, and also centrality (minimum bias, $0-80 \%$ ), are (in percent) $v_{2}=5.18 \pm 0.01, v_{4}=0.44 \pm 0.01, v_{6}=0.043 \pm 0.037$, and $v_{8}=-0.06 \pm 0.14$. Since $v_{6}$ is essentially zero, we place a two sigma upper limit on $v_{6}$ of $0.1 \%$. Also, $v_{8}$ is zero, but the error is larger because the sensitivity decreases as the harmonic order increases.

Blast Wave fits - We have fitted the data with a modified Blast Wave model 9 :

$$
\begin{align*}
& \rho(\phi)=\rho_{0}\left(1+2 f_{2} \cos (2 \phi)+2 f_{4} \cos (4 \phi)\right)  \tag{4}\\
& v_{n}\left(p_{t}\right)=\frac{\int_{-\pi}^{\pi} d \phi \cos (n \phi) I_{n}\left(\alpha_{t}\right) K_{1}\left(\beta_{t}\right)\left(1+2 s_{2} \cos (2 \phi)+2 s_{4} \cos (4 \phi)\right)}{\int_{-\pi}^{\pi} d \phi I_{0}\left(\alpha_{t}\right) K_{1}\left(\beta_{t}\right)\left(1+2 s_{2} \cos (2 \phi)+2 s_{4} \cos (4 \phi)\right)} \tag{5}
\end{align*}
$$

where $I_{n}$ and $K_{1}$ are modified Bessel functions, and $\alpha_{t}(\phi)=\left(p_{t} / T\right) \sinh (\rho(\phi))$ and $\beta_{t}(\phi)=\left(m_{t} / T\right) \cosh (\rho(\phi))$. In these equations, $\rho_{0}$ is the transverse expansion rapidity $\left(v_{0}=\tanh \left(\rho_{0}\right)\right)$ of the cylindrical shell. The parameters $f_{2}$ and $f_{4}$ are the harmonic amplitudes of the azimuthal variation of $\rho$, and $s_{2}$ and $s_{4}$ describe the spatial anisotropy of the source.

The Blast Wave fits to $v_{2}$ and $v_{4}$ are shown in Fig. 3 (left) and expanded in Fig. 3 (right), showing the approximate agreement with the ratio. A temperature of 0.1 GeV was assumed giving the fit parameters $\rho_{0}=0.49, f_{2}=1.4 \%, s_{2}=9.1 \%, f_{4}=0.0 \%$, and $s_{4}=4.4 \%$. It is interesting that in this large $p_{t}$ range the $s$ values are considerably larger than the $f$ values.


Figure 3. (left) $v_{2}$ and $v_{4}$ as a function of $p_{t}$ with the lines showing the Blast Wave fits. (right) The ratio $v_{4} / v_{2}^{2}$ as a function of $p_{t}$ with the line showing the ratio of the Blast Wave fits.

Conclusions - We have measured $v_{4}$ as a function of $p_{t}$, and centrality. This is the first measurement of higher harmonics at RHIC. It is expected that these higher harmonics will be a sensitive test of the initial configuration of the system, since they provide a Fourier analysis of the shape in momentum space which can be related back to the initial shape in configuration space.

## References

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