# C/ORNL/93-0191

# **Metals and Ceramics Division**

# Crada Final Report for CRADA ORNL 93-0191

# ENERGY EFFICIENCY STUDY OF SINGLE-WIDE MANUFACTURED HOMES

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# **Date Published- December 1999**

Prepared by the Oak Ridge National Laboratory Oak Ridge, Tennessee 37831-6092 Managed by LOCKHEED MARTIN ENERGY RESEARCH CORP. for the U.S. DEPARTMENT OF ENERGY under contract DE-AC05-96OR22464

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#### EXECUTIVE SUMMARY

This report covers a project that was carried out from 1994 to 1998. The project included laboratory characterization of the insulations used in the manufactured home test units, instrumentation of two full-size single-wide manufactured homes, and measurement of ceiling heat fluxes, roof-cavity temperatures, and electric power use. One of the full-size units that was studied contained the manufacturer's standard insulation package while the second unit contained an upgraded insulation package. A roof cavity test facility was constructed to test the use of a combination of vacuum insulation panels and loose-fill rock wool to insulate manufactured home roof cavities.

The performance of the installed roof cavity insulation compared favorably with that predicted by laboratory measurements. The standard unit had a time-average roof cavity insulation R-value of 17 ( $R_{SI}$ -3.0) versus the claimed value of R-14 ( $R_{SI}$ -2.4) while the upgraded unit showed R-23.5 ( $R_{SI}$ -4.1) versus the claimed value of R-21 ( $R_{SI}$ -3.6). The upgraded unit had nominal R-21 ( $R_{SI}$ -3.6) on the floor of the cavity and R-7 ( $R_{SI}$ -1.2) below the roof. The nominal or laboratory values are for an average temperature of 75 °F (24 °C) while the actual performance values reflect temperatures that vary over a relatively wide range.

The upgraded unit used less energy over the period of the project than the standard unit. The ratio of electric power use for the standard unit over the upgraded unit was 1.3. This difference cannot be explained totally by the insulation in the roof cavity since analysis showed that only about one-fourth of the electric power used for heating and cooling was due to heat loss or gain across the ceiling. Differences in air exchange rates and equipment efficiency also contribute to the units' energy use.

Computer simulations show that a significant savings in ceiling heat loss or gain would result from adding thermal resistance in the roof-cavity truss region. The thermal break in the truss region could be improved, for example, by using nominal 2x4s in place of 2x2s for the ceiling joists or by covering the tops of the joists with insulation.

A radiation control coating, white in color with a solar reflectance of 0.86, was

applied to the exterior roof surfaces of both units in August of 1996. Comparison of data collected before and after the coating was applied showed decreased attic temperatures for both the standard and upgraded unit. Energy savings are highly dependent on geographical location so computer simulations using DOE 2.1E were carried out for a set of cities across the United States. These computer simulations for nine cities were completed for a single-wide manufactured home configuration with R-14 ( $R_{sI}$ -2.4) roof cavity insulation, the standard package. Annual electric power savings ranged from 894 kWh for 346 ft<sup>2</sup> (32.2 m<sup>2</sup>) of roof in Rapid City to 2119 kWh for the same roof area in Los Angeles. In every location simulated there was a heating season penalty that partly off-set the reductions in air-conditioning load.

The field performance of vacuum insulation panels was compared with laboratory performance. The comparison was favorable for panels installed away from the edge of the roof cavity. Two of the three panels installed along the edge of the roof cavity exhibited performance well below the predicted level. One panel was observed to be soft, indicating a loss of vacuum. Panels can be installed between trusses and covered with conventional loose-fill. The panels will perform as expected if protected from puncture.

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# ENERGY EFFICIENCY STUDY OF SINGLE-WIDE MANUFACTURED HOMES

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# ABSTRACT

This Cooperative Research and Development Agreement (CRADA) was among Tennessee Technological University, Clayton Homes, Inc., and Oak Ridge National Laboratory(ORNL). Manufactured homes now make up a substantial portion of the new home market, and improving the energy efficiency of these homes would save significant amounts of energy. This project explored the impact of differing levels of attic insulation, the use of evacuated insulation panels, and the application of a solar reflective roof coating. The performance of the installed roof cavity insulation compared favorably with that predicted by laboratory measurements. The more heavily insulated of the two units used about 30% less energy over the period of the project than the standard unit. Based on the experimental data, computer simulations for nine cities were completed for a single-wide manufactured home with the solar reflective roof coating. Annual electric power savings ranged from 894 kWh in Rapid City to 2119 kWh for the same roof area in Los Angeles. The field performance of vacuum insulation panels was compared with laboratory performance. The panels will perform as expected if protected from puncture.

# **1. OBJECTIVE OF THE CRADA**

The objectives of this CRADA were to determine relative thermal performance of the roof cavities containing two levels of insulation, determine the relative overall performance of the two single-wide manufactured homes, determine the effect of coating the exterior roof surfaces with a solar reflecting paint, determine the feasibility and performance of vacuum insulation panels in a roof cavity, and predict performance of solar reflecting roof coating in different geographical locations by modeling.

## 2. BENEFITS OF CRADA TO DOE

ORNL has been performing extensive R&D on the development of evacuated panel superinsulation technology and on evaluating the long-term performance of reflective roof coatings for the DOE. The information developed in this CRADA had a synergistic effect on the superinsulation development program conducted by ORNL for DOE. The cooperative agreement provided valuable field data in both of these areas for comparison with existing laboratory results.

## 3. TECHNICAL DISCUSSION OF RESULTS

### **3.1. Introduction**

This report covers work done on two full-size manufactured homes and a roofcavity test facility during the period October 1, 1993 to March 1, 1999. The work was carried out at Tennessee Technological University in Cookeville, Tennessee using two full-size single-wide manufactured homes built by Clayton Homes in Maynardville, Tennessee. The single-wide units were instrumented with calibrated heat-flux transducers and thermocouples to monitor roof cavity temperatures and ceiling heat fluxes. This instrumentation was installed as the homes were built.

The third test unit consisted of a manufactured-home roof cavity positioned above four feet of conditioned space. This unit was constructed for the purpose of testing vacuum insulation panels as roof cavity insulation. Vacuum insulation panels have high thermal resistivities that can provide needed thermal resistance in limited space. The roof cavities of many types of manufactured homes have limited space, especially near the edges.

The full-size units used in the study had roof-cavity insulation at two levels. The first unit had a standard insulation package consisting of sufficient thickness of fiberglass batts to provide a nominal R-14 (ft<sup>2</sup>•h•°F/Btu) [ $R_{sI}$ -2.4 (m<sup>2</sup>•K/W)]. The second unit contained an upgraded insulation package consisting of nominal R-28 ( $R_{sI}$ -4.8) fiberglass batt insulation. The roof cavity test facility contained loose-fill rock wool insulation installed by an insulation contractor to a nominal R-19 ( $R_{sI}$ -3.3) level.

The broad objectives of this project are listed below:

- Determine relative thermal performance of the roof cavities containing two levels of insulation.
- Determine the relative overall performance of the two single-wide manufactured homes.
- Determine the effect of coating the exterior roof surfaces with a solar reflecting paint.

- Determine the feasibility and performance of vacuum insulation panels in a roof cavity.
- Predict performance of solar reflecting roof coating in different geographical locations by modeling.

The broad objectives were supported by a number of technical projects, the descriptions of which are contained in this report.

Construction guidelines for manufactured homes are set by the United States Department of Housing and Urban Development. These guidelines establish thermal and ventilation standards. As indicated above, a major objective of this project was to determine if the energy efficiency of a particular manufactured housing design could be improved with modifications to the standard roof-cavity insulation package. As more manufactured homes are built, it is important to explore the possibilities of energy conservation, especially in the lower cost homes.

## 3.2. Description of Test Units and Instrumentation

## 3.2.1 Full-Size Manufactured Homes

The test units for this project consisted of two 14-ft-wide by 52-ft-long (4.3 m wide by 16 m long) single-wide manufactured home units. Each manufactured home contained R-11 ( $R_{sr}$ -1.9) fiberglass batts for insulation in the 16-in. on center, 2x4-in. (0.41 m on center, 0.05x0.1 m) stud walls. The outside of the walls were covered with a thin cardboard sheet that is an air infiltration barrier. White aluminum siding was installed on the outside of this air infiltration barrier and attached to the wall framing with screws. The inside walls and ceiling were covered with nominal 3/8-in.-thick (0.01 m) gypsum board. The interior walls of the unit contained no thermal or acoustical insulation. Each unit had seven windows that were frame-type construction containing dual-pane glass. The windows remained closed throughout the study. Each unit had two exterior hollow wooden doors that were coated with a thin white plastic coating.

The flooring was made from 5/8-in.-thick (0.016 m) compressed particle board that rested on 16-in. on center, 2x6-in. (0.41 m on center, 0.05 x0.15 m) joists. The joists were supported by a chassis that was placed on concrete masonry blocks and anchored to the ground. Underpin skirting made of polyvinyl chloride sheets was used as a crawlspace wind barrier.

The roof joists and trusses were made of nominal 2x2-in. (0.05x0.05 m) wood lumber set 24-in. (0.61 m) on center. The joists are attached to the top of the ceiling gypsum board. The roof trusses are covered with a 0.012-in.-thick (0.0003 m) polished unpainted aluminum sheet. The roof cavity is unventilated.

The manufacturer's standard unit (at the time this project was initiated) contained two layers of R-7 ( $R_{SI}$ -1.2) fiberglass batts and the upgraded unit contained four layers of R-7 ( $R_{SI}$ -1.2) fiberglass batts. One of the R-7 ( $R_{SI}$ -1.2) batts in the upgraded unit was installed below the roof to form a "rumble" blanket. The other batts were all placed on the ceiling gypsum board, parallel to the ceiling joists and between these joists. The only design difference between the two manufactured homes was the additional two layers of

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R-7 ( $R_{SI}$ -1.2) fiberglass batts installed in the roof cavity of the upgraded unit.

Figure 1 contains a photograph of the single-wide units which shows the manufactured home skirting that was used for crawlspace wind barriers. The photograph shows the absence of shading by trees or buildings. These units were placed nine ft (2.7 m) apart on a gravel surface. The test site was located on the Tennessee Technological University campus in an undisturbed area that is unhindered by buildings or trees. The two units were positioned in an east to west orientation to avoid shading of one unit by the other.



Figure 1. End/side view of manufactured homes used in this project.

Two box-type fans were placed in each unit to provide air circulation and reduce interior air temperature variations. One computer operated continuously in the upgraded unit for heat flux transducer and thermocouple data collection for all units. Water heaters were powered in both units but there was no use of hot water. Minimal occupation of the units took place during the study. Interior lights were used a few hours each month while small exterior lights were on continuously for security reasons.

Thermocouples and heat flux transducers were placed in the insulated roof cavity at the time of manufacture to measure roof cavity temperatures and ceiling heat flows. Each heat flux transducer was placed on top of the ceiling, taped to prevent movement, and covered by the roof cavity insulation. Three of these heat flux transducers were



**Figure 2**. Heat flux transducer and thermocouple locations in the full-size manufactured homes.

placed along the centerline of the roof cavity in each unit. One heat flux transducer was placed on the edge of the roof cavity approximately one ft from the exterior wall in each unit. For this report, there are four labeled measurement positions within the attic space, A, B, C, and D, as shown in Figure 2. Although these positions vary by a few inches between the two homes, they are essentially the same. Heat flux transducer and thermocouple measurements are available for these locations. Multiple temperature measurements are made through the height of the attic assembly at the A and D locations, as shown in Table 1.

Each manufactured home unit was equipped with the same model heat pump system. The power to the heat pump and its fan were metered together, while the power to the backup resistive heater was metered separately. The meters were placed between the main circuit breaker and the heat pump. Electrical energy consumption for lights and computer equipment were not included in the submetered energy used for heating and cooling. The electrical energy consumption for the heat pump and resistive heaters were recorded several times per month.

The heat pump was controlled by a Honeywell Tradeline thermostat with an automatic changeover for heating and cooling requirements. The automatic changeover

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feature allows heating or cooling to take place upon demand and was needed in transient weather months when both heating and cooling were needed since the units were not occupied on a full-time basis.

Horizontal location (as shown on Fig. 2)	Label	Vertical location
А	TCA1	top ridge
А	TCA2	gypsum board (attic-side)
А	TCA3	near hft A
D	TCD1	near hft D
D	TCD2	gypsum board (attic-side)
D	TCD3	top of fiberglass
D	TCD4	top ridge <sup>a</sup>
D	TCD5	attic air

Table 1. Thermocouple Locations in the Full-size Manufactured Home Attics

<sup>a</sup> placed between the wood rafter and aluminum roof assembly covering to measure the roof temperature

The thermostats were mounted about five ft above the floor in the hallway. This placement minimized the effect of drafts and solar heating from windows. A check was made periodically with a digital thermometer to assure that the thermostat set points were remaining constant. This was accomplished by observing the temperatures at which the system would turn on and off during heating or cooling. While in normal operation, the interior temperature fluctuates  $\pm 2^{\circ}F (\pm 1^{\circ}C)$  from the thermostat set point. When the outer limit is reached, the heat pump will supply heating or cooling to return the temperature to the set point.

# 3.2.2 Roof Cavity Test Unit

The roof-cavity test facility was constructed by mounting standard 14-ft-wide (4.3 m) manufactured home roof trusses on a base made with 2x6-in. (0.05 x 0.15 m) stud

wall construction. The roof-cavity test facility is 24-ft-long with 4-ft-high (7.3 m long with 1.2 m high) walls. This base design was chosen to reduce the heat loss/gain to the interior conditioned space. The structure had a single access door and no windows. A through-the-wall heating/cooling unit was provided to maintain a constant temperature inside the test facility. Electric fans were positioned to move air inside the conditioned space and reduce interior temperature variations. Figures 3 and 4 show the details of the roof test facility.

The roof sheathing for the test facility was built in sections that were hinged near



Figure 3. Photograph of roof test facility.

the peak of the roof. The system permitted access to specific regions of the roof cavity for installation of insulation, thermocouples and heat-flux transducers. The middle section of the north half of the test facility was the primary site for the present study. This section contained three bays formed by four trusses set 24-in. (0.6 m) on center. Each of the three bays was instrumented with two calibrated heat flux transducers and thermocouples to measure temperatures in the roof cavity. The transducer positions are shown in Figure 5, which is not drawn to scale.



**Figure 4.** Photograph of roof test facility with one test section open.



Figure 5. Vacuum panel and heat flux transducer positions in the roof test facility (not to scale).

Loose-fill rock wool insulation was installed in all three bays by an insulation contractor. The rock wool insulation was installed on top of the vacuum insulation panels, thus filling the 22-in.-wide (0.56 m) space between trusses on the north half of the test facility. The panels were located as shown in Fig. 5 and Table 2. The panels were approximately 3/4-in. (0.02 m) thick. The rock wool insulation was manufactured by American Rock Wool Company located in Spring Hope, North Carolina. The target R-value for the installed rock wool was R-19 ( $R_{sI}$ -3.3). All of the bays in the roof test facility were insulated with loose-fill rock wool at the R-19 ( $R_{sI}$ -3.3) level to reduce the load on the heating/cooling equipment.

Location ID	Location	Transducer	Vacuum panel ID
1	Bay 1, North	ORNL - #R1	18240212
2	Bay 1, South	ORNL - #R2	18240217
3	Bay 2, North	ORNL - #R3	18240223
4	Bay 2, South	ORNL - #R4	18240210
5	Bay 3, North	ORNL - #R5	18240221
6	Bay3, South	ORNL - #R7	18240218

Table 2. Heat Flux Transducer and Vacuum Panel Locations in the Roof Test Facility

## 3.2.3 Heat Flux Transducers and Thermocouples

The collection and archival of heat flux transducer and thermocouple data were accomplished by using a data acquisition system that was designed and built by LaserComp, Inc. of Lynnfield, Massachusetts. The 8 x 8 in.  $(0.2 \times 0.2 \text{ m})$  heat flux transducers were constructed using a ceramic plate that contains embedded thermocouples to form a thermopile. These transducers react to a heat flow across the insulation batt and create an output voltage that is proportional to the heat flux. The heat flux transducers were calibrated (in the same configuration they were to be used) by placing them as test specimens in a heat flow meter built and operated in accordance with

ASTM C 518.<sup>1</sup> The output voltages were measured as a function of heat flux for three to five heat fluxes at a constant average temperature. The ratio of the heat flux to the output voltage is the calibration factor. Table 3 shows these calibration factors for the transducers used in this project.

Type-T thermocouples were used for temperature measurements. Heat flux and temperature data were read by the data acquisition system every 12 minutes. Every 60 minutes, these 12 minute readings were averaged and stored as one-hour averages.

Manufactured	l Home Units	Roof Test Facility		
Heat Flux Transducer Number	Calibration Factor (Btu/hr•ft <sup>2</sup> )/ (millivolt)	Heat Flux Transducer Number	Calibration Factor (Btu/hr•ft <sup>2</sup> )/ (millivolt)	
ORNL - #1	3.8196	ORNL - #R1	7.0918	
ORNL - #2	2.7866	ORNL - #R2	3.5128	
ORNL - #3	3.7066	ORNL - #R3	3.0326	
ORNL - #4	3.8940	ORNL - #R4	3.6499	
ORNL - #5	3.2980	ORNL - #R5	2.7853	
ORNL - #6	3.8420	ORNL - #R6	2.7403	
ORNL - #7	3.5385	ORNL - #R7	3.7086	
ORNL - #8	3.4335			

 Table 3. Calibration Factors for Heat Flux Transducers Installed in the Roof

 Cavities of the Manufactured Home Units and the Roof Test Facility

## 3.2.4 On-Site Weather Data Collection

On-site weather conditions were measured and collected from a weather station located approximately 30 ft from the manufactured home units. This weather station was capable of measuring and collecting dry bulb air temperature, wind speed and direction, relative humidity, and solar radiation on an hourly basis. Figure 1 shows the weather station instrumentation rising behind the manufactured homes. The weather station failed early in 1998 due to electrical storms. The station was repaired and reinstalled but did not function satisfactorily. Analysis using local weather data, therefore, are limited to the early part of the project.

### **3.3. HEAT FLOW IN THE FULL-SIZE MANUFACTURED HOMES**

### 3.3.1 Laboratory Measurements

The thermal resistance of batt insulation used in this project was measured using a heat-flow-meter apparatus built and operated in accordance with ASTM C 518<sup>1</sup>. These laboratory measurements were conducted to determine the apparent thermal conductivity of the fiberglass batts used in the manufactured home roof cavities. Sixteen measurements were made using the heat flow meter apparatus on single-thickness batt specimens. Tests were conducted at three average specimen temperatures at each of four insulation densities. Four tests were made at each density. The test temperatures were at 50, 75, and 100°F (10, 24, and 38 °C), and a repeated test at 75°F (24°C). An equation for apparent thermal conductivity, as a function of temperature and density, was developed from the heat-flow meter measurements.

The model used assumes that the thermal conductivity varies with density as shown in Eq. (1) where  $k_a$  is the apparent thermal conductivity, a,b,c are the model fit parameters, and  $\rho$  is the density.

$$k_a = a + b\rho + \frac{c}{\rho} \tag{1}$$

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The temperature dependence of  $k_a$  was taken to be linear and Eq. (2) follows from Eq. (1) where  $\alpha,\beta$  are model fit parameters and T is the mean specimen temperature.

$$k_{a}(\rho,\bar{T}) = (\alpha_{1} + (\beta_{1} * \bar{T})) + (\alpha_{2} + (\beta_{2} * \bar{T})) \rho + \frac{(\alpha_{3} + (\beta_{3} * \bar{T}))}{\rho}$$
(2)

The method of least squares was used to develop Eq. (3) where  $\overline{T}$  is in °F and  $\rho$  has units of lb/ft<sup>3</sup>.

$$k_{a} = (-0.070687 + 6.98879E - 04 * \bar{T}) + (0.060689 - 4.9234E - 4 * \bar{T})\rho + \frac{(0.031972 - 1.9602E - 4 * \bar{T})}{\rho}$$
(3)

The resulting fit is a thermal conductivity equation that is a function of both temperature and density. Table 4 shows results from laboratory heat flow measurements. Table 5 shows the deviation between the calculated, using Eq. (3), and measured values [the deviation is defined as  $(k_{experiment} - k_{calculated})/k_{calculated}$ ]. Eq. 3 describes the experimental  $k_a$  data to better than  $\pm 1.5$  %.

Specimen Mass Specimen Dimension	Specimen Mass0.1971 lbs (0.0894 kg)Specimen Dimensions12 x 12 in. (0.3 x 0.3 m) at several thicknesses					
Thickness (ft)	T (°F)	$k_a$ (Btu/hr•ft•°F)	ρ (lb/ft <sup>3</sup> )			
0.2917	50.02	0.0216	0.6757			
	75.04	0.0232				
	100.06	0.0254				
0.2789	50.02	0.0212	0.7067			
	75.04	0.0228				
	100.06	0.0249				
	75.04	0.0229				
0.2690	50.02	0.0211	0.7327			
	75.04	0.0226				
	100.06	0.0246				
	75.04	0.0226				
0.2624	50.02	0.0210	0.7513			
	75.04	0.0224				
	100.06	0.0244				
	75.04	0.0224				

Table 4. Apparent Thermal Conductivity Data for Fiberglass Batt Insulation as aFunction of Temperature and Density

Average Insulation Temp. (°F)	Density (lb/ft <sup>3</sup> )	$k_{calculated}$ (Btu/ft•h• °F)	k <sub>experiment</sub> (Btu/ft∙h•°F)	Deviation (%)
50.02	0.6757	0.0214	0.0216	0.93
75.04	0.6757	0.0233	0.0232	-0.43
100.06	0.6757	0.0252	0.0254	0.79
75.04	0.6757	0.0233	0.0232	-0.43
50.02	0.7067	0.0211	0.0212	0.47
75.04	0.7067	0.0230	0.0228	-0.87
100.06	0.7067	0.0248	0.0249	0.40
75.04	0.7067	0.0230	0.0229	-0.43
50.02	0.7327	0.0209	0.0211	0.96
75.04	0.7327	0.0227	0.0225	-0.88
100.06	0.7327	0.0249	0.0246	-1.20
75.04	0.7327	0.0227	0.0226	-0.44
50.02	0.7513	0.0209	0.0210	0.48
75.04	0.7513	0.0225	0.0224	-0.44
100.06	0.7513	0.0242	0.0244	0.83
75.04	0.7513	0.0225	0.0224	-0.44

Table 5. Comparison of Apparent Thermal Conductivity Measured to That Predicted byEq. 3 for Fiberglass Batt Insulation as a Function of Temperature and Density

### 3.3.2 Field Data Analysis - Ceiling Heat Flux Through the Insulation

One-dimensional heat transfer across insulation is described by Fourier's Law. Equation (4) shows that the rate of heat flow per unit area (q') through the insulation as a function of the apparent thermal conductivity (k) and the temperature gradient (dT/dx).

$$q' = \frac{Q}{A} = -k \left(\frac{dT}{dx}\right) \tag{4}$$

Where Q is the total heat flow and A is the insulation area. Equation (4) may be integrated with constant heat flow rate to obtain Eq. (5) which equates a resistance (R) to the ratio of the thermal driving force ( $\Delta$ T, the temperature difference) to the heat flux (q').

$$R = \frac{\Delta T}{q'} \tag{5}$$

Heat fluxes were measured in this project by calibrated heat flux transducers placed between the ceiling and the insulation in the roof cavity. Type-T thermocouples were used to measure temperature differences across the insulation batts in the roof cavity. Time averages of the heat flow and temperature data were used to calculate R-values for the roof-cavity insulation. Equation (6) shows the time averaging technique that was used for thermal resistance.

$$\bar{R} = \frac{\int_{t_1}^{t_2} \left| \frac{\Delta T}{q'} \right| dt}{t_2 - t_1}$$
(6)

Where  $\overline{R}$  is the average thermal resistance and t is the time. Upon integration over a onehour time interval, Eq. (6) reduces to Eq. (7) for  $\overline{R}_{hour}$ .

$$\bar{R}_{hour} = \overline{\left| \left( \frac{\Delta T}{q'} \right) \right|} \tag{7}$$

$$\bar{R}_{month} = \frac{\sum_{j=1}^{n} R_{hour_j}}{n}$$
(8)

Equation (4) was used to calculate hourly average R-values, and Eq. (8) was used to calculate the monthly average R-values from the hourly R-value data.Equation (5) shows that heat flux (q') values close to zero result in very large values for  $\overline{R}_{hour}$ . These low heat fluxes occur when indoor and outdoor temperatures differ by a few degrees or when the heat flow direction changes. Additional thermal resistance average calculations were made to determine the effect of excessively large thermal resistances on the monthly R-value average ( $\overline{R}_{month}$ ). In the first calculation, average hourly R-values that exceeded 30 hr•ft<sup>2</sup>•°F/ Btu (5.2 m<sup>2</sup>•K/W) were discarded from the set used to calculate  $\overline{R}_{month}$  using Eq. (8). A second calculation was made using the same procedure except that the Rvalues greater than 40 hr•ft<sup>2</sup>•°F/ Btu (6.7 m<sup>2</sup>•K/W) were discarded. A third calculation excluded  $\overline{R}_{hour}$  values greater than 50 hr•ft<sup>2</sup>•°F/ Btu (8.7 m<sup>2</sup>•K/W). Comparison of these three calculations determined that in most cases the anomalous R-values made less than 1 % difference in the calculated values for  $\overline{R}_{month}$ . Since the  $\overline{R}_{month}$  values between 30, 40, and 50 hr•ft<sup>2</sup>•°F/ Btu (5.2, 6.7, and 8.7 m<sup>2</sup>•K/W) differed only by 1 %,  $\overline{R}_{month}$  values calculated by the three methods were averaged.

The field data showed that there was a significant increase in the thermal resistance for the winter months. To compare this data to the laboratory data, four thickness measurements were made for the section of fiberglass batt that rests above each heat flux transducer. The average thickness of these four measurements was used to calculate a density. These four thickness measurements are contained in Table 6. Because the fiberglass batts are uniform (in terms of mass per unit area), these thickness values were transformed to density values using the data shown in Table 4. A thermal resistance for the insulation batt can then be determined as a function of temperature and density using Eq. (3). Figures 6 and 7 and Table 7 report results for the standard and

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Measurement	Position A		Position B		Position D	
Standard Manufactured Unit						
#1	4.5	(0.114)	4.5	(0.114)	4.6	(0.116)
#2	4.4	(0.113)	4.9	(0.124)	4.3	(0.108)
#3	5.0	(0.127)	5.1	(0.129)	4.6	(0.117)
#4	4.5	(0.114)	5.3	(0.135)	4.6	(0.118)
Average	4.6	(0.117)	5.0	(0.126)	4.5	(0.115)
	U	pgraded Mar	ufacture	d Unit		
#1	7.8	(0.197)	7.4	(0.189)	7.5	(0.190)
#2	7.8	(0.199)	7.6	(0.194)	7.4	(0.189)
#3	7.7	(0.195)	7.8	(0.197)	7.4	(0.188)
#4	7.8	(0.199)	7.5	(0.190)	7.3	(0.186)
Average	7.8	(0.198)	7.6	(0.193)	7.4	(0.188)

Table 6. Fiberglass Batt Field Thickness Measurements [in. (m)]



**Figure 6.** Comparison of field-measured roof cavity insulation thermal resistance to laboratory-measured data for the standard manufactured home unit.



**Figure 7.** Comparison of field-measured roof cavity insulation thermal resistance to laboratory-measured data for the upgraded manufactured home unit (batt installed against the roof not included here).

density using Eq. (3). Figures 6 and 7 and Table 7 report results for the standard and upgraded manufactured home units' measured thermal resistance. The standard unit monthly averages for November through March show a 21 % greater thermal resistance than the thermal resistance predicted by the laboratory thermal conductivity measured at the same temperature. Summer monthly averages show a 6 % greater thermal resistance than the thermal resistance calculated from the laboratory measurements.

The upgraded unit's winter monthly averages showed a 14 % greater thermal resistance than those predicted by the laboratory measurements. Summer monthly averages showed a 1% greater thermal resistance than those predicted by the laboratory measurements. (These measurements and comparisons for the upgraded unit are only for the three layers of insulation that were placed on the attic floor and do not reflect any additional thermal resistance due to the layer that was placed between the roof truss supports and the aluminum roofing.) Annual field results show an average of R-17.0 ( $R_{sI}$ -3.0) thermal resistance for the insulation in the standard unit and an insulation resistance of R-23.5 ( $R_{sI}$ -4.4) for the upgraded unit, both greater than the rated values for

these units.

	Standard Unit (R-14)			Upgraded Unit (R-28)		
Month	Field (hr•ft <sup>2</sup> • °F/Btu)	Lab (hr•ft <sup>2</sup> • °F/Btu)	Diff <sup>(a)</sup> (%)	Field (hr•ft <sup>2</sup> • °F/Btu)	Lab (hr•ft <sup>2</sup> • °F/Btu)	Diff <sup>(a)</sup> (%)
06/95	15.3	13.5	12.9	21.3	20.9	1.9
07/95				20.2	20.8	2.8
08/95	13.5	13.4	0.7	21.1	20.8	1.4
09/95	16.2	13.6	18.6	21.6	21.0	2.5
10/95	17.4	13.9	25.6	23.8	21.3	12.1
11/95	16.9	14.2	19.6	25.7	21.6	18.7
12/95	18.0	14.4	24.6	24.3	21.7	11.7
01/96	17.7	14.5	22.3	25.1	21.8	15.4
02/96	19.9	14.1	41.3	25.8	21.6	19.6
03/96	17.7	14.2	24.4	25.7	21.6	19.4
04/96	17.7	14.0	26.6	25.8	21.3	21.2
05/96	17.2	13.6	25.8	22.0	20.9	5.2

 Table 7. Variation of Actual Thermal Resistance (R-Value) of Roof Cavity Insulation on

 a Monthly Basis

(a) Difference (%) = Lab-Field \*100/Lab

As was shown in Fig. 2, one heat flux transducer was placed one ft from the edge of the exterior wall while the three remaining transducers were located along the center line of the roof assembly. Compression of an insulating material like fiberglass batts reduces the thickness which in turn reduces the thermal resistance. Yarbrough and Graves showed that in manufactured housing, the slope of the roof restricts space available for thermal insulation.<sup>3</sup> By taking the ratio of heat flux from the edge transducer to the center-line transducer, the reduction of insulation thermal resistance can be determined. By knowing the distance of the edge heat flux transducer from the wall,

the thickness of the insulation, and the roof slope, a calculation can be made to determine the amount of reduction of thermal resistance of the edge insulation. The height of the roof above the middle of the transducer in the standard unit is equal to 4.81 in. (0.12 m) and the thickness of the insulation above the middle of the transducer is 4.52 in. (0.11 m). This implies there is no compression of the edge insulation by the roof and therefore the ratio of the edge and center axis heat flux transducer measurements should be equal to 1.0. On an annual basis, the field data for the standard unit has a heat flux ratio from the edge to center transducers equal to 1.14. This small difference in the field and calculated heat flux ratios is attributed to wall edge effects. The wall edge effects are thermal bridges that exist at the eave edge where the roof trusses and ceiling joists are joined to the wall.

The height of the roof above the middle of the edge transducer in the upgraded unit is equal to 4.21 in. (0.11 m). The installed thickness of the insulation above the middle of the transducers located along the center of the attic space is about 7.4 in. (0.19 m) so the edge insulation must be compressed. By knowing the thickness of the compressed insulation and the mass per square foot, the density of the insulation can be calculated. The thermal conductivity of the compressed insulation is obtained from Eq. (3) using a temperature of 75°F (23.9°C) and the calculated density. [Note that the field compression is much greater than that used in the laboratory to produce the data that was used to derive Eq. (3)]. The thermal resistance of the compressed insulation is the measured thickness divided by the thermal conductivity calculated from Eq. (3). The thermal resistance for the center transducer insulation is calculated by the same procedure. If the temperature difference across the insulation were equal in both cases, the ratio of the thermal resistances would be equal to the ratio of the heat fluxes. The ratio of the heat flux measured by the edge transducer to the heat flux measured by the center axis transducer in the upgraded unit would equal 1.31 under this condition. However, the temperature difference across the insulation is not equal in both cases. The edge insulation is not only compressed, but is in direct contact with the roof surface, and thus directly linked with the external air temperature (via conduction through the roof and external convective heat transfer conditions). The center insulation is exposed to an

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enclosed air space at a buffered temperature and experiences natural convection heat transfer to this space. The field data show the combined effect of these factors. On an annual basis, field data show that the upgraded unit has a heat flux ratio from the edge to center axis transducers equal to 1.50.

By examination of Figure 8, a significant difference in ratios exists between the two manufactured home units. These results show that a considerable amount of reduction in thermal resistance is taking place in the edges of the roof cavity for the upgraded unit. The month of November gave an anomalous result in that the standard unit heat flux ratio was slightly greater than the upgraded unit.

Since there is no compression of the insulation in the standard unit, the average of the four heat flux transducers was used to represent a heat flux for the total insulation area. Because of the insulation compression in the upgraded unit, a different approach was taken to determine the heat flux for the total insulation area. The edge heat flux transducer represents 4 % of the total ceiling area. The average of the remaining three center axis heat flux transducers contributed 96 % of the total ceiling area. The average



Figure 8. Ratio of edge to center heat flux transducer energy gain/loss.

of the three center axis heat flux transducers is multiplied by 0.96 and the edge heat flux transducer is multiplied by 0.04. The sum of these products gives a weighted average for the total insulation area.

The total heat flowing through the insulation, excluding the wood joists, is then calculated by the product of the weighted average heat flux of the insulation area by the insulation area using Eq. (9).

$$q_{insulation} = q'_{insulation} * A \tag{9}$$

The total insulation heat loss or gain for a period of t hours was calculated by using Eq. (10).

$$Q_{insulation} = q_{insulation} * t$$
(10)

# 3.3.3 Field Data Analysis - Total Energy Consumption

The roof assemblies of the manufactured home units were constructed of wood trusses and insulated with layers of nominal R-7 ( $R_{st}$ -1.2) fiberglass batts. Wood joists were used as the support for the ceiling gypsum board and the fiberglass insulation. The fiberglass batts were placed between these wood joists. The fraction of ceiling area occupied by the wood joists was calculated by dividing the area of the wood attached to the ceiling by the total ceiling area. Each manufactured home unit contains 27 wood joists that are 0.125 ft wide by 14.0 ft long by 1.5 in. thick (0.038m by 4.27 m by 0.04 m). Total area of the ceiling of one unit is 728.0 ft<sup>2</sup> (67.7 m<sup>2</sup>). Therefore, the fraction of ceiling area covered by wood joists is 0.065. The fraction of ceiling area covered by insulation batts is 0.935. In order to calculate an overall thermal resistance of the attic floor, the thermal resistance of the wood joists and the thermal resistance of the insulation must be known. This overall attic floor thermal resistance was calculated using a series-parallel heat-flow equation from the ASHRAE Handbook of Fundamentals that reduces to Eq. (11) when the area fractions described above are used.<sup>2</sup>

$$\frac{1}{R_{atticfloor}} = \frac{0.935}{R_{insulation}} + \frac{0.065}{R_{wood}}$$
(11)

By calculating  $R_{attic floor}$  from Eq. (11), a series of calculations can then be made to determine the fraction of the total ceiling heat flow that comes through the roof cavity insulation. More heat will flow through the wood joists per square foot of area than the insulation batts due to the lower thermal resistance of the wood members. Heat flux transducers were placed between the ceiling and the insulation batt and, therefore, measured only the heat loss or gain through the insulation. The fraction of the total heat flow that is transported by the insulation was calculated using Eq. (12).

$$f_{insulation} = \frac{0.935}{R_{insulation}} * R_{atticfloor}$$
(12)

Using nominal R-values for the insulation and wood produces a  $f_{insulation}$  of 0.6 for the standard unit and 0.5 for the upgraded unit. In other words, 40 to 50% of the total ceiling heat flux is going through the wood joists in this arrangement. The soft pine wood used to construct the trusses has an R-value of approximately 1.0 hr•ft<sup>2</sup>•°F/Btu per in. of thickness, or R-1.5 (R<sub>sI</sub>-0.2).

An overall attic floor thermal resistance ( $R_{attic floor}$ ) was then calculated using Eq. (11) and the field-measured data for the fiberglass insulation. The calculated and field-measured attic floor thermal resistances are compared in Table 8. The wood trusses cause a significant reduction in the overall performance of the roof cavity. By examination of these results, larger reductions in the field-measured overall thermal resistances ( $R_{Total}$ ) exist for the upgraded unit than for the standard unit. Annual results showed overall thermal resistances of R-10.2 ( $R_{st}$ -1.8) for the standard manufactured home unit and an overall thermal resistance of R-12.0 ( $R_{st}$ -2.1) for the upgraded manufactured home unit.

Calculations were made to determine the increase of the overall thermal resistance for both manufactured home units if the thermal resistance of the wood joists were to be increased to R-3.5( $R_{si}$ -0.6). The thermal resistance of this portion of the attic floor could be increased by placing any type of insulating material on top of the joists or by increasing the wood joist thickness to 3.5 in. (0.09 m). These results are also included in Table 8 and show that a significant increase in the overall thermal resistance would result from increasing the thermal resistance of the joist area.

Assemblies with 1.5 in. and 3.5 in. Wooden Joists in Parallel Heat Flow - 1995-1996 Data $*$	Table 8. Overall Attic Floor Thermal Resistances of Standard and Upgraded Roof	
Data *	Assemblies with 1.5 in. and 3.5 in. Wooden Joists in Parallel Heat Flow - 1995-1996	5
	Data *	

Month	Standard Unit			Upgraded Unit		
	Field (insulation only)	1.5 in.	3.5 in.	Field (insulation only)	1.5 in.	3.5 in.
June	15.3	9.6	12.5	21.3	11.5	16.0
July				20.2	11.2	15.4
August	13.5	8.9	11.4	21.1	11.4	15.9
September	16.2	9.9	13.1	21.6	11.5	16.1
October	17.4	10.3	13.9	23.8	12.1	17.3
November	16.9	10.2	13.6	25.7	12.5	18.2
December	18.0	10.5	14.2	24.3	12.2	17.5
January	17.7	10.4	14.0	25.1	12.4	17.9
February	19.9	11.1	15.3	25.8	12.6	18.3
March	17.7	10.4	14.0	25.7	12.6	18.2
April	17.6	10.4	14.0	25.8	12.6	18.2
May	17.2	10.2	13.7	22.0	11.7	16.4

\*The units for the thermal resistances in this table are  $h \cdot ft^2 \cdot F/Btu$ .

Total heat flow across the ceiling  $(Q_{ceiling})$  is calculated from the total heat flux of the insulation system  $(Q_{insulation})$  divided by the fraction of the total heat flow that is transported by insulation [f<sub>insulation</sub> from Eq. (12)] as shown by Eq. (13).

$$Q_{ceiling} = \frac{Q_{insulation}}{f_{insulation}}$$
(13)
This calculated total ceiling heat flow contains both insulation and wood joist contributions.

Both of the manufactured home units used in this project were heated and cooled with electric heat pumps. Coefficient of performance for both heat pumps were calculated for several months of operation. A coefficient of performance is defined by Eq. (14). Where  $|Q_1|$  is the absolute value of the heat transferred to the higher temperature

$$COP = \frac{Refrigerant \ Effect}{Net \ Work \ Input} = \frac{|Q_2|}{|Q_1| - |Q_2|}$$
(14)

sink, and  $|Q_2|$  is the absolute value of the heat transferred from the lower temperature source. For example, if a heat pump has a coefficient of performance equal to 3.0, for every one kilowatt-hour of energy input into the heat pump, there will be three kilowatthours of output due to energy from the refrigerant thermodynamic cycle. The manufacturer of the heat pumps provided coefficients of performance of 1.97 and 3.0 at outdoor air temperatures of 17 and 47 °F (-8.3 and 8.3 °C), respectively. These two points were used to obtain a linear expression which is shown in Eq. (15). Average outdoor air temperatures for each month were provided by an on-site weather station. Using the monthly average air temperature, the coefficient of performance for each month of heating was calculated using Eq. (15).

$$COP = 0.0343 * \bar{T}_{air} + 1.39 \tag{15}$$

The electrical energy inputs to the heat pump and resistive heater were measured separately. The fraction of the total electrical energy for the heat pump and resistive heater were calculated. The heat pump fraction is multiplied by the coefficient of performance and the resistive heating fraction is multiplied by a coefficient of performance of 1.0. These products were summed to give a monthly heat pump coefficient of performance adjusted for resistive heating. Total thermal energy input

 $(Q_{total})$  to each manufactured home is calculated by the product of the total electrical energy  $(E_{total})$  (heat pump and resistive) and the coefficient of performance (COP) for the heat pump and resistive heater combined. The total electrical energy  $(E_{total})$  is converted from kilowatt-hours to BTUs by multiplying by 3412. Eq. (16) shows the calculation of  $Q_{total}$ .

$$Q_{total} = E_{total} * COP \tag{16}$$

The fractional amount of total input energy  $(Q_{total})$  that moved through the ceiling alone  $(Q_{ceiling})$  is calculated from Eq. (17).

$$f_{ceiling} = \frac{Q_{ceiling}}{Q_{total}}$$
(17)

Five separate calculations using Eq. (17) were performed to determine the quantity of the total energy input to the manufactured home that was transported through the ceiling. In each calculation, the present hour temperature difference determined by subtracting the temperature measured on the ceiling side from the temperature measured on top of the insulating batt is subtracted from the previous hour temperature difference. If this insulation temperature difference change was greater than  $1^{\circ}F$  (0.6°C), the heat flux measurement was discarded for that hour interval. Calculations were also made at insulation temperature difference changes of  $3^{\circ}F$ ,  $5^{\circ}F$ ,  $7^{\circ}F$ , and  $10^{\circ}F$  (1.7, 2.8, 3.9, and 5.6°C). By making these calculations, it was possible to determine if small insulation temperature variations affected the calculated heat loss or gain through the ceiling. Final results showed that only a 2 % difference in the overall fraction of ceiling energy loss was encountered when all heat fluxes were kept in the calculation.

Calculations were performed to determine the quantity of the total heat input into the manufactured home that was lost or gained through the ceiling. The purpose for this calculation was to determine if a significant fraction of the total heat input to the manufactured home was being lost or gained through the ceiling. These calculations were made using Eq. 17. Figure 9 shows the monthly fractional results for each unit. Table 9 gives the results in tabular form.



**Figure 9**. Fraction of total energy input into test homes that is lost or gained through the ceiling - 1995-1996 data.

Table 9. Fraction of Total Energy Input into Test Homes that is Lost or Gained through the Ceiling - 1995-1996 Data

	Standard Unit	Upgraded Unit		Standard Unit	Upgraded Unit
June	0.241	0.238	December	0.182	0.197
July		0.265	January	0.185	0.202
August	0.189	0.173	February	0.297	0.281
September	0.334	0.283	March	0.226	0.238
October	0.296	0.279	April	0.327	0.308
November	0.224	0.246	May	0.320	0.192
Annual Average	0.240	0.220			

The highest fractional results occurred in April, May, September, and October. This was due to the air temperature fluctuations from warm days to cool nights. After applying the fractional results for each month to that month's energy use, the annual fraction for the standard unit was 0.240 and for the upgraded unit was 0.220.

#### 3.3.4 Computational Fluid Dynamics Models

Another way to consider the complexities of heat flow through the attic is to use a computational fluid dynamics model. This method explicitly recognizes the effect of air movement within the closed attic space on heat transfer through the attic configuration. Using CFX-4.2 Solver, simplified two-dimensional models of the attic spaces were first constructed to correspond with the physical geometry of the attics described in Sect. 2.1.<sup>4</sup> The grid applied to this space is shown in Figs. 10 and 11. The computational models used a plane of symmetry down the centerline of the attic, so these grids represent one-half of the triangular attic space. The radiation heat transfer model is one included within the CFX code and is a discrete transfer method developed by Shah.<sup>4</sup> The equations solved at each grid node are the incompressible Navier-Stokes equations with a Boussinesq approximation to account for buoyancy. A k-epsilon turbulence model was used.

These two-dimensional models do not include the wooden attic joists, but are useful for bench marking the computer model and for determining the necessary grid spacing. Table 10 summarizes many of the assumptions used within the computer models. The boundary conditions were selected to match those of a relatively cold winter night, such as several nights that occurred during January 1997.

For comparison, several time periods were chosen from the weather data that met the criteria of relatively stable outdoor temperature (because the computational model assumes steady-state conditions) and with no incident solar radiation (because that was not included in the model). Figure 12 shows the air temperature measured during the selected time periods. The overall attic R-values for those time periods were calculated using the corresponding heat flux meter data and the temperature difference between the

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Figure 10. Grid used to calculate heat and mass flows for the standard insulation attic space.



Figure 11. Grid used to calculate heat and mass flows for the upgraded insulation attic space.

	Inside	70
Air Temperature (°F)	Outside	25
Air Film Resistance	Inside	0.61
(h-ft <sup>2</sup> -°F/Btu)	Inside70Outside25Inside0.61Outside0.17Gypsum board0.1335Insulation0.0238Wood0.0849	0.17
	Gypsum board	0.1335
Thermal Conductivity (Btu/h-ft-°F)	Insulation	0.0238
	Wood	0.0849

Table 10. Values of Parameters Used in Computational Fluid Dynamics Model

outdoor temperatures and an indoor temperature of 70°F (21°C). This value is the air-toair thermal resistance, that is, it includes the effect of indoor and outdoor surface film resistances and all the materials and air space within the attic construction, not just the insulation. For this calculation, the heat flux meter data was treated as described in Sect. 3.2, that is, (1) for the standard unit the average of all four meters was used and (2) for the upgraded unit, the average of the three central transducers was multiplied by 0.96 and



**Figure 12**. Air temperatures measured during January, 1997 for time periods used to bench mark two-dimensional computational fluid dynamics model.



**Figure 13.** Overall attic space R-values (including indoor and outdoor surface air resistances) calculated using measured heat fluxes and outdoor temperatures for comparison periods during January, 1997

added to 0.04 times the value from the edge transducer. The results of this calculation are shown in Fig. 13.

The average R-value for the standard unit for this period was 16.8 ( $R_{sI}$ -2.9) with a standard deviation of 2.7%. For comparison, the two-dimensional computational model predicted R-15.2 ( $R_{sI}$ -2.6) for the standard unit, or about 10% less.

The upgraded unit has lower heat flux values, leading to greater variability in the data, as shown by Fig. 13. The mean of the values shown is R-33.1 ( $R_{sI}$ -5.7), with a large standard deviation of 25%. For comparison, the two-dimensional computational fluid dynamics model predicted R-23.7 ( $R_{sI}$ -4.1) for the upgraded unit. Although this is 28% less than the mean measured value, it is very close to the values recorded for many of the selected time periods, again as shown in Fig. 13. Remember that these values are air-to-air thermal resistances that include the effect of surface film resistances and all the materials and air space within the attic construction, not just the insulation.

Computational models are also useful for expanding our understanding of the various heat transfer mechanisms at work in the attic space. Although the various heat transfer modes are highly interlinked, it is instructive to look at the effect of "turning off" one or more modes to see the effect on the total heat flux. This exercise is explored in Table 11. The effectiveness of still air as an insulator is demonstrated in the conduction only model, where the R-value of the standard model is greater than that of the upgraded model because the still air is less conductive than the insulation. When convection is allowed, the value of the insulation becomes apparent. While adding radiation heat transfer to the model, the effect of reflective surfaces was examined. The emissivity of the surfaces would be low for reflective surfaces, such as polished aluminum (0.05 was used for these cases) and higher for dull surfaces, such as the insulation attached to the underside of the roof in the upgraded unit. The reflective surface has a relatively small impact under the winter condition, i.e. heat flow up, modeled here. The effect would be greater under heat flow down, or summer, conditions.

	Standard           R-Value (h-ft²-°F/Btu)           32.63           16.64           15.20	Upgraded
Modeled Heat Transfer Mechanism(s) in Attic Space	R-Value (h-ft <sup>2</sup> -°F/Btu)	R-Value (h-ft <sup>2</sup> -°F/Btu)
Conduction only	32.63	32.29
Conduction + Convection	16.64	24.74
$\label{eq:conduction} \begin{array}{l} Conduction + Convection + Radiation \\ \epsilon_{attic \ floor} = 0.8, \ \epsilon_{attic \ ceiling} = 0.8 \end{array}$	15.20	23.69
$\begin{array}{l} Conduction + Convection + Radiation \\ \epsilon_{attic \ floor} = 0.8, \ \epsilon_{attic \ ceiling} = 0.05 \end{array}$	16.42	24.45

Table 11. Effect of Varying Heat Transfer Parameters on Heat Flow Through the Attic, Two-Dimensional Model\*

\*Average R-value, from the two-dimensional model and therefore not corrected for trusses.

The air flow patterns for both units (from two-dimensional models including all three heat transfer modes) are shown in Figs. 14 and 15. Note that the additional insulation in the upgraded model not only reduces the conductive heat transfer, but also



Figure 14. Air flow patterns predicted by computational model in standard insulation attic space.



Figure 15. Air flow patterns predicted by computational model in upgraded insulation attic space.



Figure 16. Temperature distributions predicted by computational model in standard insulation attic space.



Figure 17. Temperature distributions predicted by computational model in upgraded insulation attic space.

reduces the height of the air space within the attic. This reduced height in turn reduces the natural convection driving force. The effect of the reduced convective currents is apparent in the temperature profiles within the attic spaces, as shown in Figs. 16 and 17. The colder outside temperatures penetrate much deeper into the attic air space with the air circulation for the standard unit (Figs. 14 and 16) than for the upgraded unit (Figs. 15 and 17). The effect of the additional batt of insulation placed against the roof membrane is also illustrated in these temperature profiles, where the coldest attic air temperature is  $34^{\circ}F(1^{\circ}C)$  in the upgraded unit, compared to  $26^{\circ}F(-3^{\circ}C)$  in the standard unit. Remember that an outdoor air temperature of  $25^{\circ}F(-4^{\circ}C)$  was used for both models.

In the two manufactured homes tested here, the insulation was properly installed between and adjacent to the wood joists. However, sometimes when batt insulation is used, gaps can occur between the wood trusses and the insulation batts, allowing air to travel all the way down to the gypsum board surface of the attic floor. To explore this effect, computational models were created to reflect two extreme conditions. The first model represents poorly installed batt insulation with air gaps on each side of the joist and with no insulation above the joist. For comparison, the second model represents a 'perfect' insulation installation with no air gaps and with the joists fully covered. Examining this effect required a three-dimensional computational model. For both models, a plane of symmetry below the ridge line of the roof was used as for the two-dimensional model. Two additional planes of symmetry were also used to bound the computational domain. The first is parallel to the wood joist and travels down the center of a joist. The second is also parallel to the wood joist but travels down the centerline between two adjacent joists. These planes and the geometry used for the two comparison models are shown on Fig. 18. Both of these models reflect the standard insulation unit but modified to include either an air gap on each side of the joist or to include insulation covering the joist. The grid used for these models is shown in Figs. 19 and 20. Figure 20 is taken from a slice near the centerline of the attic and perpendicular to the wood joist. Note that the grid is somewhat coarser than that used for the two-dimensional model, although the total number of grid points is of course much greater. The air circulation within the gap combined with the uncovered wood joist increases the overall heat flux by

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almost 60%, decreasing the overall thermal resistance from the 'perfect' case's R-14.8 to R-9.3 ( $R_{sI}$ -2.5 to  $R_{sI}$ -1.6). Note that the value for the corresponding two-dimensional model without gaps or joists was R-15.2 ( $R_{sI}$ -2.6). This difference of 3% is attributable to the inclusion of the wood joist and to the slightly coarser grid used in the three-dimensional model. This calculation demonstrates the importance of careful installation procedures. Indeed, many of the later manufactured home models produced by this manufacturer use loose-fill insulation to preclude such gaps and to fully cover the wood joists.



Figure 18. Geometry used in three-dimensional computational models of attic space with and without air gaps parallel to each joist.



**Figure 19**. Grid used to calculate heat and mass flows for the three-dimensional model of the standard insulation attic space.

# 3.3.5 Effect of Air Infiltration on Energy Consumption

Air infiltration is a major contributor to energy loss or gain in buildings. With the use of a blower door, fan depressurization tests were conducted on both manufactured homes to determine the air infiltration rates.<sup>5</sup> Calculations were made to determine the number of air changes per hour (ACH) for each manufactured home. The volumetric flow rate of air across the building envelope was measured as a function of the pressure difference across the envelope. An equation relating log V with log  $\Delta P$  was derived from the data. A volumetric flow rate of air across the envelope for a pascals (ACH50) was then determined from the data. The volume of the manufactured



**Figure 20**. Grid slice parallel to the attic centerline, perpendicular to the wood attic joist, from the three-dimensional model of the standard insulation attic space.

home is divided by this volumetric flow rate and the resulting air change per hour is divided by 20 (ACH50/20) for a good estimate of average air infiltration rate<sup>6</sup>. Tables 12 and 13 give results from the blower door tests. A correlation coefficient is used to measure the goodness of fit of the equation with all data points in Tables 12 and 13. These results show that the two units had air infiltration rates that differed by only about

3.6%. Blower door results yielded 1.08 air changes per hour for the standard unit and 1.12 air changes per hour for the upgraded unit. These units had essentially the same air tightness.

Fan Pressure (Pascals)	Temp Corrected (Pascals)	Flow Rate (ft <sup>3</sup> /min)	Envelope ∆P (Pascals)
56.0	55.05	3558.06	172.1
52.1	50.95	3424.23	152.0
45.2	44.20	3191.92	137.0
40.2	39.31	3012.13	121.5
35.3	34.52	2824.63	104.8
28.8	28.16	2554.21	91.4
24.2	23.66	2343.60	81.7
20.5	20.04	2158.98	73.4
14.1	13.78	1794.22	50.4
10.5	10.26	1550.83	38.2
Logarithmic Fit Log V = 0.57335 * Lo Correlation Coefficie	$pg \Delta P + 2.27906$ nt = 0.997	CFM @ 50 Pascals = 1791.28 Effective Leakage Area = 120.4 in <sup>2</sup>	
$\frac{Power Fit}{V = 190.144 * \Delta P^{0.573}}$ Correlation Coefficie	$^{35}$ nt = 0.997	ACH50 = 21.49 ACH50/20 = 1.08	

Table 12. Tests Results from Minneapolis Blower Door Test for Standard Unit (Unit Volume 5000 ft<sup>3</sup>).

Calculations were made for each month to determine the quantity of energy loss/gain due to air infiltration. These calculations were made using Eq. (18) where  $Q_{air}$  is

$$Q_{air} = \dot{m}C_p \ \Delta T \tag{18}$$

the energy required to heat or cool the infiltrating air into the manufactured home per hour,  $C_p$  is the heat capacity of the air,  $\dot{m}$  is the mass flow rate of air, and  $\Delta T$  is the

temperature difference between the indoor and entering outdoor air. The mass flow rate of air was calculated by the product of the air density at the indoor temperature, the volume of the manufactured home and the air change per hour rate. The heat capacity for air was taken to be constant at 0.24 Btu/lb•°F (1.005 kJ/kg•°C). The change in temperature is calculated by subtracting the average monthly air temperature from an indoor temperature of 68°F (20°C) for the winter months. For the summer months, the

Fan Pressure (Pascals)	Temp Corrected (Pascals)	Flow Rate (ft <sup>3</sup> /min)	Envelope ∆P (Pascals)
57.5	56.23	3595.36	169.0
52.3	51.14	3430.72	159.9
49.9	48.80	3351.95	149.1
44.9	43.91	3181.43	140.0
41.2	40.29	3048.97	124.2
36.0	35.20	2852.19	114.2
32.4	31.68	2707.39	100.4
26.5	25.91	2451.21	83.0
21.7	21.22	2220.58	65.9
15.0	14.67	1849.96	50.3
9.9	9.68	1506.36	34.3
Logarithmic Fit Log V = 0.53586 * L Correlation Coefficie	$\log \Delta P + 2.35911$ nt = 0.9987	CFM @ 50 Pascals =1860.031 Effective Leakage Area = 137.8 in <sup>2</sup>	
$\frac{Power Fit}{V = 229.78 * \Delta P^{0.53586}}$ Correlation Coefficie	nt = 0.9989	ACH50 = 22.41 ACH50/20 = 1.12	

Table 13. Tests Results from Minneapolis Blower Door Test for Upgraded Unit (Unit Volume 4900 ft<sup>3</sup>).

indoor temperature of  $74^{\circ}F(23^{\circ}C)$  is subtracted from the average monthly air temperature. These calculations account for the sensible energy required to condition the infiltration air. The latent energy required to condition the air due to differences between

the indoor and outdoor humidity was not calculated.

In the winter months, large temperature differences exist between the indoor and average outdoor air temperatures. These large temperature differences caused the winter  $Q_{air}$  calculated using Eq. (18) to be much larger than the  $Q_{air}$  for summer conditions. The sensible energy loss due to air infiltration is more significant in the winter than in the summer. The latent load posed by humid summer conditions was not estimated.

The results in Figure 21 show a greater percentage energy loss for the upgraded unit than for the standard unit. Since energy consumption of the upgraded unit is less than the standard unit for each month, the percentage of total air infiltration energy loss is greater for the upgraded unit. Table 14 shows the comparison of monthly heat pump energy use and air infiltration energy loss/gain for the standard and upgraded manufactured home units. Annual calculations (excluding July) show 32.1 % of the energy use by the heat pump for the standard unit is due to air infiltration. The upgraded unit results show 41.0 % of the energy use by the heat pump is due to air infiltration.



**Figure 21.** Monthly percentage of air infiltration energy loss for standard and upgraded manufactured home units.

Month	Standard Unit (R-14)			Upg	graded Unit	(R-28)
	E <sub>total</sub> (kWh)	E <sub>air</sub> (kWh)	$E_{air}/E_{total}$	E <sub>total</sub> (kWh)	E <sub>air</sub> (kWh)	$E_{air}/E_{total}$
June	418	13	0.03	332	13	0.04
July				258	23	0.09
August	617	38	0.06	565	48	0.08
September	240	43	0.18	227	42	0.18
October	215	94	0.44	165	94	0.57
November	547	210	0.38	342	206	0.60
December	798	273	0.34	522	267	0.51
January	873	299	0.34	567	293	0.52
February	1070	590	0.55	826	578	0.70
March	567	208	0.37	358	204	0.57
April	256	91	0.35	180	89	0.49
May	280	34	0.12	258	33	0.13
Total	5881	1891	0.32	4600	1888	0.41

Table 14. Comparison of Monthly Heat Pump Energy Use and Air Infiltration Energy Loss/Gain for Standard and Upgraded Manufactured Homes - 1995-1996 Data

### 3.3.6 Total Energy Use for Heating and Cooling

Table 15 contains the cumulative power use for the two full-size manufactured home units. The electric power used for the heat pump and air circulation was submetered and reported under the "Heat Pump". The heading "Resistance" refers to power consumed by the resistive heating section in the heat pump. These cumulative power readings have a zero time effect of 86 kWh since the watt-hour meters were not zeroed. This difference loses significance as the number of months of operation increases. The power bill for maintaining the two units with the same interior conditions is proportional to the number under "Total". It is clear that the upgraded unit is using less electrical power than the standard unit. The difference, however, is not due totally to the upgraded insulation package. Slight differences in air exchange rates, for example, were measured, and the exact response of the control equipment was not determined. Since these units represent two units built at the same time a direct comparison of monthly power usages has some value.

Table 16 contains monthly electric power use for heating and cooling for the two units and the ratio of standard unit use divided by upgraded unit use. The value for the ratio fluctuates about 1.30, the overall value for the ratio for 40 months of operation.

The two manufactured home units were heated with only resistive heating during February 1996. The ratio of standard/upgraded power use for this month is 1.27, a ratio that is very close to the overall ratio. The absolute power use for February 1996 is substantially greater than the earlier or later months. This can readily be seen in Table 16.

The power use ratio of 1.30 is too large to be explained by the difference in roof cavity insulation. The upgraded unit, however, did show better thermal performance than the standard. Some of the difference is no doubt manufacturing variability.

		Upgraded Unit	(R-28)	Standard Unit (R-14)		(R-14)
Date	Heat Pump	Resistance	Total	Heat Pump	Resistance	Total
01/95	0657	0112	769	0608	0075	683
02/95	1218	0225	1443	1173	0182	1355
03/95	1711	0333	2044	1772	0245	2017
04/95	1938	0367	2305	2068	0271	2339
05/95	2083	0374	2457	2224	0276	2500
06/95	2328	0375	2703	2484	0276	2760
07/95	2583	0375	2958	2813	0276	3089
08/95	3176	0375	3551	2847	0276	3123
09/95	3723	0375	4098	3367	0276	3643
10/95	3981	0375	4356	3603	0276	3879
11/95	4148	0376	4524	3751	0281	4032
12/95	4448	0424	4872	4223	0362	4585
		Resist	tive heating			-
01/96	4896	0498	5394	4913	0468	5381
02/96	5367	0625	5992	5642	0645	6287
03/96	5404	1376	6780	5668	1623	7291
04/96	5713	1426	7139	6182	1696	7828
		Resist	tive heating			-
05/96	5884	1439	7323	6418	1722	8140
06/96	6143	1440	7583	6702	1722	8424
07/96	6492	1440	7932	7127	1722	8849
08/96	6866	1440	8306	7583	1722	9305
		Reflecti	ve roof coat	ing applied		
09/96	7241	1440	8681	7973	1722	9695
10/96	7386	1440	8826	8108	1722	9830

Table 15. Electric Power Use (kWh) in the Manufactured Home Units

		Upgraded Unit	(R-28)	Standard Unit (R-14)		
Date	Heat Pump	Resistance	Total	Heat Pump	Resistance	Total
11/96	7524	1442	8966	8253	1725	9978
12/96	7861	1483	9344	8806	1795	10601
01/97	8248	1532	9780	9418	1874	11292
02/97	8825	1606	10431	10166	2057	12223
03/97	9233	1663	10896	10732	2137	12869
04/97	9443	1677	11120	11082	2161	13243
06/97	9698	1686	11384	11493	2173	13666
07/97	9758	1686	11444	11547	2173	13720
08/97	10003	1686	11689	11857	2173	14030
09/97	10236	1686	11922	12043	2173	14216
11/97	10603	1692	12295	12402	2183	14585
12/97	11007	1723	12730	13008	2250	15258
01/98	11442	1797	13239	13723	2357	16080
02/98	11891	1876	13767	14476	2472	16948
03/98	12232	1938	14170	14994	2553	17547
04/98	12516	1977	14493	15562	2623	18185
06/98	12797	1982	14779	15954	2633	18587
07/98	13235	1982	15217	16206	2633	18839
08/98	13413	1982	15395	16356	2633	18989
09/98	13633	1982	15615	16574	2633	19207
10/98	13895	1982	15877	16809	2633	19442
11/98	13943	1983	15926	16987	2634	19621
12/98	14156	1983	16139	17335	2657	19992
01/99	14423	2042	16465	18212	2784	20996
02/99	14996	2117	17113	18630	2835	21465

Month	Upgradad	Standard	Standard/
wionui	Unit	Unit	Ungradad
			Opgraded
	(KWN)	(KWN)	
01/95	674	672	1.00
02/95	601	662	1.10
03/95	261	322	1.23
04/95	152	161	1.06
05/95	246	260	1.06
06/95	255	329	1.29
08/95	547	520	0.95
09/95	258	236	0.91
10/95	168	153	0.91
11/95	348	553	1.59
12/95	522	796	1.52
01/96	598	906	1.52
02/96 (a)	788	1004	1.27
03/96	359	587	1.63
04/96	184	262	1.42
05/96	260	284	1.09
06/96	349	425	1.22
07/96	374	456	1.22
08/96	375	390	1.04
09/96	145	135	0.93
10/96	107	148	1.38
11/96	378	623	1.67
12/96	436	691	1.58
01/97	651	931	1.43
02/97	465	646	1.39

Month	Upgraded	Standard	Standard/
	Unit	Unit	Upgraded
	(kWh)	(kWh)	
03/97	224	374	1.67
07/97	245	310	1.27
08/97 (b)	233	186	0.80
11/97	435	673	1.55
12/97	509	822	1.61
01/98	528	868	1.64
02/98	403	599	1.49
03/98	323	638	1.98
06/98	438	252	0.58
07/98	178	150	0.84
08/98	220	218	0.99
09/98	262	235	0.90
11/98	213	371	1.74
12/98	326	469	1.44
01/99	648	1001	1.55
Total	14868	19321	1.30

Table 16. Monthly Power Use for Two Unoccupied Full-Size Single-Wide Manufactured Homes

<sup>(a)</sup> Units were conditioned with resistive heat only. <sup>(b)</sup> Radiation Control coating applied.

### 3.3.7 Effect of Radiation Control Coating Applied to Roof

The exterior surfaces of the roofs of both single-wide manufactured homes were painted with radiation control coating on August 9, 1996. The radiation control coating was manufactured by  $Solex^{TM}$ , a coating with a solar reflectance of 0.86 and an infrared emittance of approximately 0.9. The coating was applied in accordance with manufacturer's instructions. A clear protective coating was applied after the relatively thick white coating had cured. The radiation control coating reflects a large fraction of the incoming solar flux thus reducing the roof surface temperature and heat gain across the roof assembly.<sup>7</sup>

Data from the manufactured homes were merged with separately recorded local weather data. Although the weather data were not synchronous with the heat flux/temperature data, they were matched within the nearest hour. Two approaches were used in this particular examination of the data. First, a multiple regression analysis was done using summer-time data before and after the roof coatings were applied. This analysis assumed quasi-steady-state conditions and produced estimates for indoor temperature, overall attic assembly U-value, and roof surface emittance. The second approach examined changes due to the application of a roof coating by selecting "similar" summer days from the before and after summer seasons. This approach allowed us to examine the attic temperature variations throughout the day, as well as daily average values.

The Multi variate regression model is based on the sol-air temperature, defined as "the temperature of the outdoor air that, in the absence of all radiation changes, gives the same rate of heat entry into the surface as would the combination of incident solar radiation, radiant energy exchange with the sky and other outdoor surroundings, and convective heat exchange with the outdoor air" as shown in Eqs. 20, 21, and 22.<sup>2</sup>

$$\frac{q}{A} = \alpha I_t + h_o (T_o - T_s) - \varepsilon \Delta R$$
<sup>(20)</sup>

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$$\frac{q}{A} = h_o(T_e - T_s) \tag{21}$$

$$T_e = T_o + \frac{\alpha I_t}{h_o} - \frac{\varepsilon \Delta R}{h_o}$$
(22)

Where:

q/A	=	heat flux into the surface
α	=	absorptance of surface for solar radiation
I <sub>t</sub>	=	total solar radiation incident on surface, Btu/h-ft <sup>2</sup>
h <sub>o</sub>	=	coefficient of heat transfer by long-wave radiation and convection
		at outer surface, Btu/h-ft <sup>2</sup> -°F
To	=	outdoor air temperature, °F
T <sub>s</sub>	=	surface temperature, °F
3	=	hemispherical emittance of surface
ΔR	=	difference between long-wave radiation incident on surface from
		sky and surroundings and radiation emitted by black body at
		outdoor air temperature, Btu/h-ft <sup>2</sup> , and
T <sub>e</sub>	=	sol-air temperature, °F.

ASHRAE gives typical values of  $\Delta R$  and  $h_o$  for horizontal surfaces that receive long-wave radiation from the sky only.<sup>2</sup> Given the shallow slope of the manufactured home roofs and their elevation above the ground, these were considered applicable. For the units given above,  $\Delta R$  is about 20 Btu/h-ft<sup>2</sup> and  $h_o$  is about 3 Btu/h-ft<sup>2</sup>-°F. A reasonable value for the long-wave hemispherical emittance,  $\varepsilon$ , is 0.9. Considering the roof and attic as an assembly, and defining the overall thermal conductance, U, of that assembly, produces Eq. 23. These equations can be rearranged to give Eq. 24.

$$\frac{q}{A} = U\left(T_e - T_i\right) \tag{23}$$

$$\frac{q}{A} = -U\left(T_{in} + \frac{\varepsilon \Delta R}{h_o}\right) + UT_o + \frac{U\alpha}{h_o}I_t$$
(24)

where  $T_{in}$  is the indoor temperature, and U is the overall conductance of the roof/attic assembly.

When Eq. 24 is used with the measured values of heat flux, outdoor air temperature, incident solar radiation, and the assumed values for  $\Delta R$ ,  $\varepsilon$ , and  $h_o$ , multivariate regression produces the values for indoor temperature, overall conductance, and emissivity shown in Table 17. The regression results show that the overall thermal resistance has been significantly increased and that the solar absorptivity,  $\alpha$ , of the roof has been reduced by approximately 50%. The relatively low regression coefficients show that this simple model is not adequate to explain all the complex interactions between the environment and the attic assembly. These efforts also revealed that the indoor temperature was somewhat hotter during the second summer, a finding that was confirmed by examination of the recorded gypsum temperatures. The cause of this temperature rise is unknown, given that the thermostat controls were unchanged.

Regression model: $(q/A)_{avg} = C_1 + C_2T_0 + C_3I_t$ (SD= standard deviation)								
House	Roof Coating	R <sup>2</sup>	C <sub>1</sub> (SD)	T <sub>in</sub> (°F)	C <sub>2</sub> (SD)	R = 1/U (h-ft <sup>2</sup> -°F /Btu)	C <sub>3</sub> (SD)	α
Upgraded	no	.59	-3.92 (0.26)	70	.052 (0.0036)	19	.0050 (0.00025)	.29
	yes	.52	-2.25 (0.095)	74	.030 (0.0014)	33	.000936 (0.00013)	.10
Standard	no	.65	-3.73 (0.37)	74	.047 (0.0052)	21	.0109 (.00037)	.70
	yes	.78	-2.63 (0.083)	85	.029 (0.0012)	34	.0290 (0.0012)	.35

Table 17. Multi Variate Regression Results for Eq. 24 for Data Taken During Daytime Hours of June, July, and August of 1996 and 1997.

The second analysis approach was to examine the weather data from the 1996 and 1997 summer periods. These data were examined by comparing the maximum and average values of both the air temperature and the incident solar radiation. Six pairs of days were selected and the hourly profiles for the air temperature and solar radiation were examined. The best two pairs of days were then selected, sets 2 and 4. The weather variables for these two pairs of days are shown in Table 18 and Figs. 22 and 23.

Examining data from these two pairs of similar days shows that the difference between the attic ridge temperature and the outdoor air temperature was significantly modified by the roof coating (see Figs. 24 and 25). This temperature *difference*, which ranged from noontime highs of 40 to  $80^{\circ}$ F (22 to  $44^{\circ}$ C) was cut down to about  $10^{\circ}$ F (5.6°C) by the application of the radiation-control coating.

Table 18. Comparison of Weather Variables for Selected Days from the Summers of 1996 and 1997.

Set	Date	Average air temperature (°F)	Maximum air temperature (°F)	Average solar radiation (Btu/hr·ft <sup>2</sup> )	Maximum solar radiation (Btu/hr·ft <sup>2</sup> )
2	Jul 24, 1996	76.0	85.9	95.1	295.4
2	Jun 19, 1997	75.1	83.9	96.4	294.2
4	Jul 19, 1996	81.5	90.6	89.4	288.8
4	Aug 16, 1997	82.1	90.1	86.2	286.5

The major thermal benefit of a radiation-control coating is reduced air conditioning load during the summer. Because of variations in the indoor air temperature between the two seasons, the measured attic heat fluxes were not used to quantify this effect. However, the significant decreases in both overall thermal conductance and the solar absorptance shown in Table 17 indicate that summer time heat transfer through the roof should be significantly decreased. An effort was therefore made to estimate these savings for a variety of climates.

Eleven roof-assembly DOE 2.1E simulations were completed using typical meteorological year weather files for nine U.S. cities. The simulations were carried out



Figure 22. Comparison of outdoor air temperatures for similar summer days.



Figure 23. Comparison of incident solar radiation for similar summer days.



**Figure 24**. Comparison of temperature differences between the attic ridge and the outdoor air for similar summer days (set 2) before and after application of reflective roof coating.



**Figure 25**. Comparison of temperature differences between the attic ridge and the outdoor air for similar summer days (set 4) before and after application of reflective roof coating.

for a single-wide manufactured home roof assembly like that studied in the project. The simulation parameters were the slope of the roof, equal to 15.2°, and area of the roof, equal to 345.8 ft<sup>2</sup> (32.2 m<sup>2</sup>). The roof assembly was specified to contain fiberglass batts with a specified thermal resistance. The roof assembly was covered with a roof material with specific solar absorptance and infrared emittance. The simulated unit's heating and cooling equipment was set to operate with a coefficient of performance equal to 1.0. Therefore, energy output into the simulated building will equal the energy input from the heating/cooling device. Each simulation run resulted in an annual energy consumption for both heating and cooling. A complete set of numerical outputs have been assembled by Andrews.<sup>8</sup> Table 19 contains a complete set of simulation results for Nashville, Tennessee.

Roof Cavity	Reflectance	Emmitance	Electrical Power Use (kWh/Yr)		
Insulation R-Value			Total	Cooling	Heating
14	0.90	0.8	1928	1285	643
14	0.85	0.8	2043	1421	622
14	0.70	0.8	2305	1733	572
14	0.10	0.8	3170	2710	460
14	0.05	0.8	3219	2768	451
10	0.85	0.8	2313	1502	811
20	0.85	0.8	1775	1314	461
30	0.85	0.8	1485	1168	317
50	0.85	0.8	1156	975	181
30	0.85	0.5	1622	1334	288
30	0.85	0.1	1928	1698	230

 Table 19. DOE 2.1E Roof Coating Simulations for Computational Model Tests Run with

 Weather Data from Nashville, Tennessee

An estimate of the savings resulting from the application of a radiation control coating to an absorbing roof can be obtained for a roof cavity insulation of R-14 ( $R_{SI}$ -2.4) by subtracting the total electrical use in line 2 of Table 19 from the total electrical use in line 4. R-14 ( $R_{SI}$ -2.4) is the insulation level in the standard unit that was studied in this project. The result is 1127 kWh/yr or 3.3 kWh/(yr•ft<sup>2</sup> of roof) [or 0.31 kWh/(yr•m<sup>2</sup> of roof)]. The results in Table 19 show the strong dependence of electrical energy savings on roof cavity insulation R-value. The results also show the modest dependence of electrical use on the surface infrared emittance of the roof.

Table 20 shows the electrical energy use reductions for buildings in nine cities based on the parameters described above. In all of the cities considered there was a reduction in cooling load and an increase in heating load.

	Electrical Power (kWh/yr) Reduction						
City	Cooling	Heating	Total				
Denver	1571	-297	1274				
Los Angeles	2281	-162	2119				
Nashville	1289	-162	1127				
New Orleans	1508	-95	1413				
Miami	1495	-17	1478				
Phoenix	1858	-124	1734				
Rapid City	1139	-245	894				
San Antonio	1454	-100	1354				
Washington, D.C.	1239	-197	1042				

Table 20. Annual Electrical Energy Savings for Nine Cities Based on a Roof Cavity Insulation of R-14 ( $R_{st}$ -2.4)

### 3.4. Roof Cavity Heat Flow with Vacuum Insulation Panels

### 3.4.1 Laboratory Measurements

Thermal resistance data were obtained for the loose-fill rock wool that was installed in the roof test facility using a heat-flow-meter apparatus built and operated in accordance with ASTM C 518<sup>1</sup>. The rock wool thermal resistance was measured at mean temperatures 50, 75, and 100°F (10, 24, and 39°C) using the same procedure described for the fiberglass batts. The loose-fill insulation test specimens were 24x24 in. (0.61x0.61 m). The laboratory measured apparent thermal conductivities,  $k_a$ , for the rock wool insulation are given in Table 21. Equations (25), (26), and (27) provide correlations for  $k_a$  of the rock wool insulation used in this project at 50, 75, and 100°F (10, 24, and 39°C), respectively.

$$\overline{T} = 50^{\circ}F$$
  $k_a = 0.013935 + 0.53986 \times 10^{-3}\rho + 0.18217 \times 10^{-1}/\rho$  (25)

$$\overline{T} = 75^{\circ}F \qquad k_a = 0.011753 + 0.98300 \text{ x } 10^{-4}\rho + 0.26248 \text{ x} 10^{-1}/\rho \quad (26)$$

$$\overline{T} = 100^{\circ}F$$
  $k_a = 0.025641 + 0.12535 \times 10^{-2}\rho + 0.11527 \times 10^{-1}/\rho$  (27)

where T is the Temperature, °F,  $k_a$  is the apparent thermal conductivity, Btu/ft·h·°F, and  $\rho$  is the density, lb/ft<sup>3</sup>.

Measurement of the thermal resistances of the vacuum insulation panels was accomplished with the same apparatus used for the loose-fill rock wool insulations. A relatively large number of panels were measured. Table 22 contains the measured R-values at  $\overline{T} = 75^{\circ}F$  (24°C) for the six panels that were actually installed in the roof test facility. It also shows laboratory results for seven panels that were aged for three years,

Table 21. Apparent Thermal Conductivity Data for Roof Test Facility Rock Wool as a Function of Temperature and Density (Specimen Dimensions 24x24 In. At Several Thicknesses.)

Thickness (ft)	$\overline{\mathrm{T}}$ (°F)	$k_a$ (Btu/ft•h•°F)	$\rho$ (lb/ft <sup>3</sup> )
0.4922	50.0	0.02216	3.028
	75.0	0.02444	
	100.0	0.02889	
0.3500	50.0	0.02064	4.257
	75.0	0.02218	
	100.0	0.02348	
0.4659	50.0	0.02330	2.645
	75.0	0.02465	
	100.0	(Discarded)	
0.4035	50.0	0.02083	3.054
	75.0	0.02258	
	100.0	0.02444	
0.3451	50.0	0.02147	3.570
	75.0	0.02321	
	100.0	0.02376	
0.5414	50.0	0.0229	2.308
	75.0	0.02538	
	100.0	0.02780	
0.5249	50.0	0.02273	2.380
	75.0	0.02506	
	100.0	0.02738	
0.4921	50.0	0.02224	2.539
	75.0	0.02439	
	100.0	0.02660	
0.4101	50.0	0.02110	3.047
	75.0	0.02290	
	100.0	0.02479	
0.3416	50.0	0.02035	3.657
	75.0	0.02190	
	100.0	0.02353	

from 1994 to 1997, in an unconditioned warehouse. Some of these panels showed signs of aging as their thermal resistance decreased by 0 to 8%.

Panel ID	$k_a$ (Btu•in/ft <sup>2</sup> •h•°F)		R-Value ( $ft^2 \cdot h \cdot F/Btu$ )				
	Oct 1994	Mar 1997	June 1999	Oct 1994	Mar 1997	June 1999	Change (%)
11440008	0.0509	0.0554		15.3	14.6		-4.4
11440009	0.0529	0.0599		14.6	13.4		-8.2
11440011	0.0527	0.0551		14.8	14.6		-1.3
11440021	0.0552	0.0569		14.0	14.1		0.2
11440006	0.0547	0.0587		14.2	13.7		-3.6
1144023	0.0535	0.0597		14.5	13.5		-6.9
18240145	0.0535	0.0558		14.4	14.5		0.4
18240217*		0.0524	0.0530		15.1	14.9	-1.1
18240212*		0.0518	0.1915		15.3	4.14	-73.
18240210*		0.0525	0.0540		15.2	14.8	-2.6
18240223*		0.0617	0.0624		13.0	12.8	-1.5
18240218*		0.0517	0.0515		15.4	15.5	0.6
18240221*		0.0518	0.1937		15.3	4.15	-73.

Table 22. Vacuum Insulation Panels' Laboratory Measurements of Thermal Conductivity and Resistance at a Mean Temperature of 75°f (Note That the R-values Reflect the Actual Measured Panel Thicknesses)

\*used in the Roof Test Facility

# 3.4.2 Field Data Analysis

The vacuum insulation panels listed in Table 22 were installed in the roof test facility in August, 1998. First, the six heat flux transducers were affixed to the plywood separating the conditioned space from the attic space. Then the entire roof cavity of the test facility was insulated with blown-in rock wool insulation, installed by an insulation

contractor to provide a nominal R-19 ( $R_{sI}$ -3.3). In six locations, panels were installed atop the rock wool, directly above the heat-flux transducers, in such a way that the space between trusses was covered with a layer of superinsulation. The heat flux data obtained from the transducers and the attic-air to interior-air temperature difference were used with a linear regression technique to calculate the thermal conductance and resistance using Eq. (4). These linear regression R-values will be referred to as the "Field" values. For two of the panels, the data showed a wide spread instead of the expected linear distribution, leading to very low regression coefficients, and these values were therefore not reported.

A "laboratory" R-value for the vacuum insulation panel/ rock wool combination was obtained from the data in Table 22 and Eq. (26) which is a correlation for the  $k_a$  of the rock wool density at a mean temperature of 75°F (24°C). The density of the loose-fill rock wool insulation was determined from insulation thickness and weight measurements using a circular "cookie-cutter" device 12.45 in. (0.32 m) in diameter to define a volume of insulation. The average density of the loose-fill rock wool was determined to be 1.47 lb/ft<sup>3</sup>(23.5 kg/m<sup>3</sup>). The average depth of loose-fill insulation above the vacuum insulation panels was determined to be 7.0 in. (0.18 m) for the region near the edge of the roof cavity (locations 1,3,5 in Fig. 5) and 8.1 in. (0.21 m) away from the edge of the roof cavity (locations 2,4,6 in Fig. 5). These data provide for a calculation of R-18.8 (Rm-3.2) for the edge region and R-21.7 (Rm-3.8) for the central region. Table 23 summarizes the results for the vacuum insulation panels.

The Lab-R values are based on 75°F (24°C) measurements while the Field-R values may have been a few degrees warmer. Since thermal resistance decreases with increasing temperature, the Lab-R are overestimates. Two of the test panels, 1 and 5, deviated significantly from the Lab-R or predicted value. This suggested a failure on the part of vacuum insulation panels 1 and 5. Panel Number 5 is "soft" to the touch indicating a loss of internal vacuum and significant loss of R-value. The panels were retested in the laboratory after they were removed from the roof test facility and those two panels had indeed failed (see Table 22). The other two panels, for which the field data was not available, tested very near their pre-installation values.

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Location	Field R (ft <sup>2</sup> •h• °F/Btu)	Lab R (ft <sup>2</sup> •h• °F/Btu)	Field/Lab
1 - Edge	12.5	34.1	0.37
3 - Edge 28.3		31.8	0.89
5 - Edge	8.5	33.1	0.26
2 - Central	Not reported	36.8	
4 - Central	Not reported	36.9	
6 - Central 32.4		37.1	0.87

Table 23. Effective R-Values for a Combination of Vacuum Insulation Panels and Loose-Fill Rock Wool Insulation

# 4. INVENTIONS

No inventions were made as part of this CRADA.

# 5. COMMERCIALIZATION POSSIBILITIES

Clayton Homes now uses ceiling insulation methods recommended by this project to reduce energy loss through ceiling joists.

# 6. PLANS FOR FUTURE COLLABORATIONS

There are no definite plans for future collaborations.

### 7. CONCLUSIONS

Two single-wide manufactured home units have been studied over a period of four years. The units were instrumented to obtain heat flow data, temperatures, and electric power use. One of the single-wide homes contained the standard insulation package provided by the manufacturer while the second single-wide unit contained an upgraded insulation package. The roof test facility was constructed to test specialized roof cavity insulation like evacuated panel insulation. The field-site data collection was supplemented by careful laboratory characterization of the insulations used in the roof cavities. Important results from the project are summarized below.

- The installed roof cavity insulation performed at, or better than, the expected level of R-value. Time-average R-values were R-17 ( $R_{SI}$ -3.0) for the unit with nominal R-14 ( $R_{SI}$ -2.4) and R-23.5 ( $R_{SI}$ -4.1) for the unit with nominal R-21 ( $R_{SI}$ -3.6). These R-values are for the floor of the roof cavity.
- A significant energy savings would result from increasing the thermal resistance in the region occupied by trusses. These energy savings vary according to the climate and can be accomplished by covering the trusses with insulation.
- The total amount of air infiltration energy losses was nearly equal for both units. This heat loss or gain due to air infiltration accounted for 32% of the heat pump power use in the case of the standard unit and 41% in the case of the upgraded unit.
- The standard unit used 30% more electric power for heating and cooling than the upgraded unit. This difference is too large to be accounted for solely by differences in roof cavity insulation. Differences between construction details and heating/cooling equipment are other factors.
- The application of a radiation control coating with a solar reflectance of 0.86 resulted in significant decreases in the summer-time attic temperatures.
- Intact vacuum insulation panels delivered predicted (laboratory measured) Rvalues when installed in the roof cavity. However, two out of six panels were damaged either during transport or installation, emphasizing the importance of careful handling of this type of insulation.
- Computer simulations showed an average savings of 1382 kWh/year attributable to a radiation control roof coating for single-wide units with roof cavity insulation at the R-14 ( $R_{st}$ -2.4) level for the nine cities considered. As expected, the electric power savings were greatest in the South. There was a wintertime electric power penalty predicted in every city included in the analysis.

# 8. ACKNOWLEDGMENTS

Funding for this CRADA was provided by Clayton Homes Inc, Tennessee Technological University, and the US Department of Energy, Office of Building Technology, State and Community Programs, under contract number DE-AC05-96OR22464 with the Oak Ridge National Laboratory, managed by Lockheed Martin Energy Research Corportation. A large number of people have contributed to the progress and completion of this manufactured home project. The authors acknowledge DOE managers Bill Stewart (now retired), Fred Singleton, and Robert Brown for their help with funding and management of the program. Tom Kollie at the Oak Ridge
National Laboratory (now retired) was instrumental in initiating the project. Ron Graves of the Oak Ridge National Laboratory (now retired) supervised the instrumentation of the full-size units. Fred Weaver (ORNL) made numerous heat flow measurements and Ken Childs and Mark Wendel(ORNL) provided valuable computational fluid dynamics analysis. J. R. Booth, Don Williams, and Perry Melton at Tennessee Tech contributed time and expertise in designing, building, and gathering data. Sharon Robinson of the Department of Chemical Engineering at Tennessee Tech helped with report preparation and Suzanne Henry of the Center for Manufacturing Research at Tennessee Tech managed the financial aspects of the project. The authors are grateful to all of these individuals.

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