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NUMERICAL MODELING OF THE THERMAL AND HYDROLOGICAL ENVIRONMENT AROUND A NUCLEAR WASTE PACKAGE USING THE EQUIVALENT CONTINUUM APPROXIMATION: HORIZONTAL EMPLACEMENT

John J. Nitao

MAY 1988



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Numerical Modeling of the Thermal and Hydrological Environment around a Nuclear Waste Package using the Equivalent Continuum Approximation: Horizontal Emplacement

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ABSTRACT

In support of the investigations for an underground high-level nuclear waste repository at Yucca Mountain, Nevada, we have performed computer simulations of the immediate thermal and hydrological environment around a nuclear waste package. Calculations of this type will be needed for waste package design, performance assessment, and radionuclide transport analyses. Two dimensional computer simulations using a modified version of the TOUGH code were run for an idealized configuration derived from the COVE3 benchmarking effort consisting of a single spent fuel waste package with laterally periodic boundary conditions. The model domain extended downward to the water table and upward to the ground level. Fluid behavior in the rock was modeled using the the equivalent continuum approximation. Runs were made with surface water influx rates at the surface set to 0.1, 0.5, and 1.0 mm/yr. A significant amount of code modification and development was needed in order to develop the capability to run these types of problems out to the long time spans required.

Since any significant transport of non-gaseous radionuclides will involve liquid water as a main vehicle of movement, and since liquid water, if present, will also contribute to to waste package entrosion, its presence is of vital concern. Initial heating from the radioactive decay will vaporize the liquid pore water around the waste package. Of major interest to waste container design

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is the time at which possible wetting of the package occurs during the subscquent cooldown period. Our simulations showed that vapor transport and capillary condensation are the the major mechanisms of water movement early in the cool-down period. However, the amount of liquid water in the rock next the waste package during this time is very small and will have very low mobility, although the diffusive transport properties of this water are not exactly known. In our simulations the main front of water returns to the borehole wall at approximately 1000 years from emplacement as it is drawn in by capillary imbibition. At no time during the 2600 year time span of our simulation does the water saturation of the rock next to the borehole wall increase above initial native saturation. The values of these two time periods as well as the other predictions reported in this paper are highly preliminary due to the current uncertainty in the model input parameters and the sub-models used in our simulations. However, it is seen that the effect of the hydrological fluid flow on the thermal history may be significant. Considerable work needs to be done to develop better models of fluid behavior in partially fractured rock and more experimental data is needed to accurately model the waste package environment.

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Nomenclature

Greek Symbols

- μ_l viscosity of liquid phase
- μ, viscosity of gas phase
- o fractional porosity of the porous media
- ϕ_b bulk porosity of the porous media, equal to total void space in a unit elemental volume of equivalent porous media
- ϕ_f fracture porosity, equal to void volume of fractures in a unit elemental volume
- ϕ_{g} connected matrix porosity, equal to void volume of connected pores in a unit elemental volume
- ρ_{a} , density of air in gas phase
- ρ_{o_1} density of air in liquid phase
- ρ_t density of liquid phase
- ρ, density of gas phase
- ρ_{w_a} density of water in gas phase
- ρ_{w_i} density of water in liquid phase
- τ reciprocal of the pore space tortuosity

Roman Symbols

- C_p unsaturated specific heat of the bulk porous media
- g gravitational acceleration
- $h_{a_{\perp}}$ specific enthalpy of air in gas phase
- $h_{a,}$ specific enthalpy of air in liquid phase
- $h_{\rm g}$ specific enthalpy of gas phase
- h_l specific enthalpy of liquid phase
- h_{w_a} specific enthalpy of water in gas phase
- h_{ω_i} specific enthalpy of water in liquid phase

- K absolute permeability of the porous media
- K_{b} thermal conductivity of the bulk porous media, a function of fluid saturation
- $\dot{\kappa}_{rd}$ relative permeability of liquid phase
- k_{re} relative permeability of gas phase
- M_1 molecular weight of the liquid phase
- p_c capillary pressure
- p_i liquid phase pressure
- $p_{\mathbf{z}}$ gas phase pressure
- $p_{sat.}$ saturation pressure of water, function of temperature, obtained from steam tables
- p, vapor pressure
- R gas constant
- Q_a source term for air component
- Q_h source term for non-convective heat
- Q_w source term for water component
- q_{cond} heat flow rate due to conduction
- $q_{a \text{ diff}}$ flow rate of air in gas phase due to binary diffusion
- q_g flow rate of gas phase due to Darcy flow
- q_l flow rate of liquid phase due to Darcy flow
- $q_{w diff}$ flow rate of water vapor in gas phase due to binary diffusion
- s₁ liquid saturation
- s_g gas saturation
- T absolute temperature of the fluid and porous media
- t time
- u_{a_e} specific internal energy of air in gas phase
- u_{a_i} specific internal energy of air in liquid phase
- u_{e} specific internal energy of gas phase
- u_i specific internal energy of liquid phase
- $u_{w_{a}}$ specific internal energy of water in gas phase
- u_{w_i} specific internal energy of water in liquid phase
- x_a mass fraction of air in liquid phase
- x_w mass fraction of water in liquid phase

- y_a mass fraction of air in gas phase
- y_w mass fraction of water in gas phase
- 2 unit vector in downward direction

Subscripts

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: .

- a air component
- b bulk
- f fracture
- 1 liquid phase
- g gas phase
- m matrix
- w water component

Introduction

The Topopah Spring unit at Yucca Meuntain, Nevada, is being evaluated by the Nevada Nuclear Waste Storage Investigations project (NNWSI) as a possible location for an underground high level nuclear waste repository. Future license approval of such a site demands that scientific investigations and analyses be conducted to determine if the containment of the waste can meet the necessary environmental protection requirements. Lawrence Livermore National Laboratory has been given the responsibility for the design of the waste package at Yucca Mountain and for predicting the performance of the package with respect to the near-field environment. Near-field hydrology plays an important factor in both of these tasks. Liquid water can act as a transport mechanism for radionuclides and chemical components found in soluble minerals in the host rock. Its presence is known to strongly influence the corrosion rates of the waste container.

The purpose of this report is to review numerical simulations of the hydrologic and thermal waste package environment as well as to describe the capabilities that we have developed that will aid us in future studies. Our results should only be viewed as preliminary at this time because many of the physical input parameters to the model as well as the exact conditions in Yucca Mountain are either not known or have a high degree of uncertainty and many idealizations and approximations of complicated physical and chemical behavior have been made. Chemical effects, such as possible increased concentration and redistribution of silica by dissolution in hot water moving toward the waste package via "heat pipes" and deposition where water evaporates, are not taken into account. Better knowledge of the site and the physical processes involved and their mathematical representation will lead to more accurate predictions in the future.

The Topopah Springs formation consists of welded tuff that is believed to be highly fractured. Due to the low surface recharge rate, the rock is only partially saturated. Multiphase flow of air and liquid water in both matrix and fracture is therefore possible. Heat from the radioactive waste can lead to vaporization of the water and vapor flow in the fractures and matrix around the waste package. Some specific items of interest to package design and performance are the temperature history, time to rewetting of the container, radionuclide transport, and mechanisms, if any, for directing water to any opening in the container. In this report we will restrict ourselves to the first two of these items.

Significant progress has been made in the numerical modelling of the near-waste package environment in partially-saturated media [Pruess and Wang, 1984; Pruess, et. al., 1986; Travis et. al., 1984; Bixler, 1985]. Our goal was to perform simulations out to the extended time spans needed by container design and performance assessment applications using current knowledge and conceptual models of the proposed site. Numerical modelling was based upon LLNL's modified version of the TOUGH code. The original version of this code was developed by Karsten Pruess at the Lawrence Berkeley Laboratory [Pruess, 1985]. The governing equations appear in the appendix. The problem that was run has its origins in the COVE3 benchmarking exercise [Langkopf, 1985].

1. Equivalent Continuum Approximation

The conceptual model for flow that we have used is based upon the equivalent continuum approximation which lumps the fracture and matrix into a single porous medium equivalent. The equivalent continuum approach assumes that the matrix and fracture system is in thermo-dynamic equilibrium, i.e. phase pressures and temperatures between the matrix and fractures are continuous and equilibrate instantaneously. This assumption is valid as long as the source terms that drive the model change sufficiently slowly in time so as to allow the matrix and fracture to come to equilibrium. In reality, as the waste package gives off heat, a pressure buildup occurs in the matrix relative to the pressure in the fractures that is caused by the expansion of liquid water to steam. If the rock is highly fractured this pressure difference is low because the steam has only a short distance to escape to a fracture and equilibrium is attained relatively quickly. For our simulations to be valid it is essential that the rock be sufficiently fractured and that the matrix permeability be sufficiently high. High liquid fluxes in the fracture would be another case where the equilibrium assumption is violated.

The work in [Pruess and Tsang, 1986] describes simulations to investigate the validity of the assumption under non-isothermal conditions. Using discrete fracture modelling they simulated partially saturated flow in a fracture orthogonal to the longitudinal axis of a waste package container with periodic boundary conditions representative of an infinite array of fractures with an equal spacing of 0.22 meters. The effects of gravity and surface fluxes were ignored. The simulations showed that the equivalent continuum model is adequate for matrix permeabilities greater than $32.6 \times 10^{-18} m^2$. However, simulations out to 0.1 years using a smaller permeability of $1.9 \times 10^{-18} m^2$ showed significant differences in the saturation and gas pore pressures between the discrete fracture model and the equivalent continuum model. Agreement with the temperatures and air humidity were good. The smaller permeability is the one used in our simulations because it is close in magnitude to those expected at Yucca Mountain. Hence, we would expect to see some differences from the discrete fracture model in the saturations and gas phase pressures. However, since they only ran their cases for a relatively short time span, it is not clear how important these differences are at later times since much of the discquilibrium can be expected to occur at early times where temporal temperature changes are the greatest. Further comparisons with discrete fracture models at larger times are needed. Also, higher fracture densities may lead to near equilibrium conditions. Additional work by Wang and Narasimhan [1986] and Klavetter and Peters [1986] indicated the validity of the equivalent continuum approach in isothermal infiltration problems with low surface recharge rates.

Within the equivalent porous medium approach, it is useful to consider how the bulk hydraulic quantities and parameters are defined. We wish to identify a representative elementary volume of the rock-fracture system large enough so that a meaningful continuum fracture porosity ϕ_f can be defined. This porosity is just the ratio of the fracture volume to the total bulk rock volume. The term "matrix" will be used to signify that portion of the elementary volume occupied by the bulk rock excluding the fracture void space. The matrix porosity ϕ_m is defined as the ratio of the volume of the voids in the matrix to the volume of the matrix. A bulk, equivalent porosity ϕ_b can then be defined as the total void space fraction within the volume.

$$\phi_b = \phi_f + (1 - \phi_f) \phi_m$$

Given the fracture and matrix saturations s_f and s_m , the equivalent bulk saturation is given by

$$s_b = \frac{s_f \phi_f + s_m (1 - \phi_f) \phi_m}{\phi_f + (1 - \phi_f) \phi_m}$$

It is important to recognize that the balance equations used in our TOUGH simulations (see appendix) involve hydraulic quantities and parameters representative of bulk behavior that occurs within the fracture matrix elementary volume. A pore velocity predicted by TOUGH will not necessarily represent a velocity observed in either the matrix or fractures; it is a bulk average. By partitioning the flow areas within elementary volumes, an equivalent bulk conductivity of the equivalent medium has been used by Klavetter and Peters [1986], Pruess [1986], and Wang and Narasimban, [1986] as

$$K = K_m (1 - \phi_f) + K_f \phi_f$$

This expression assumes that there are enough fractures of varied orientation to ensure isotropic behavior. Since we are assuming equilibrium between the matrix and the fracture, the liquid and gas phase pressures in the matrix and fracture are assumed to be equal such that the capillary pressures are also equal:

$p_{cap f}(s_b) = p_{cap m}(s_b)$

Since TOUGH requires a capillary pressure as a function of bulk saturation, we need to solve this equation for the bulk saturation s_{σ} . In our code we generate a table of capillary pressure versus saturation and perform inverse linear interpolation to obtain the capillary pressure as a function of saturation. At the same time a table of relative permeability based on the van Genuchten [1980] relationships are also generated.

Figures 1 is a plot of the equivalent continuum capillary pressure versus bulk liquid saturation while figure 2 shows the relative permeability curves as a function of bulk gas saturation. These curves are based on the characteristic curves for the matrix and the fractures that were used in our simulations (see section 2 for description of the characteristic curves that were used). Figure 3 is a liquid relative permeability curve in linearly scaled axes. Note that the value of the liquid relative permeability becomes nearly zero at about 0.984 bulk liquid saturation. This value is the point at which the fracture nearly desaturates and the net liquid permeability, which is the product of the bulk absolute permeability times the relative permeability, becomes close to that of the matrix. At each value of bulk liquid saturation there corresponds a bulk suction pressure based on equilibrium of the matrix and fractures, and at each such suction pressure there will be a liquid saturation value for the matrix and a separate value for the fractures.

In figure 4 we have plotted the relationship between the saturations in the fracture and matrix as a function of bulk saturation. Note that below the critical bulk saturation of about 0.534 the fracture saturation is zero or nearly zero. Above this value the fracture begins to have a significant liquid saturation. The behavior of these curves rely entirely on the characteristic curves that are used. The fracture suction curves that we have used have low values relative to the matrix suction over most of the saturation range (figure 1). Suction equilibrium of the matrix and fracture can only occur at higher matrix saturations where the matrix suction curve is lower. If the fractures had , suction curve that was higher, the critical bulk saturation crossover point where the matrix begins to saturate would be lower,

2. Description of the Problem and Model Input Parameters

The current problem considers a two-dimensional domain transverse to a single horizontally emplaced cylindrical waste package (see figure 6). The two vertical edges are treated as no-flow boundaries to simulate an infinite periodic array of containers with 37.8 meters spacing. The waste package is represented by a cross-sectional half-circular element. The input parameters used in our simulations are primarily those that were collected during the COVE3 code benchmarking exercise [Langkopf, 1985]. The original COVE3 problem is no longer part of the benchmarking effort and has been replaced by a simpler heat pipe problem exercise which is called COVE3a. The original COVE3 problem domain was limited to a region 20 m above and below the waste package. The domain has been extended to include the 348 m above the waste package to the ground level and 225 m below the package to the water table for this problem. The matrix-rock fluid model is based upon the equivalent continuum approximation as described in the previous section. The heat loading of the container was based on that of 8.6 year old PWR spent fuel. The boundary conditions at the top and bottom of the model were constant temperature and phase pressures with no fluid influx at the water table and a constant non-zero surface recharge rate of water at the surface. Runs were made out to 2600 years for three different surface water influxes of 0.1 mm/year, 0.5 mm/year, and 1.0 mm/year.

The input parameters to our problem are given in the following. Those items marked with an asterisk are in variance to the original COVE3 exercise input parameters.

Rock Properties

- fracture permeability 1.x 10⁻¹¹ m²
- matrix permeability 1.9 x 10⁻¹⁸ m²
- fracture porosity 1.8 x 10⁻³
- matrix porosity 0.11
- · thermal conductivity in formation within 20 m below and above waste package:

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(linear in saturation between wet and dry values)

wet thermal conductivity: 2.30 W / m-K dry thermal conductivity: 1.74 W / m-K

- 2580 kg/m³
- specific heat of rock: 840 J/kg-K
- thermal conductivity 20 m. above waste package: 1.82 W/m-K
- thermal conductivity 20 m. below waste package: 1.56 W/m-K

Binary Diffusion

• density of rock:

• The binary diffusion coefficient is given in units of $\frac{m^2}{sec}$ by the correlation

$$D = \frac{4.40 \, x \, 10^{-6} \, T^{2.334}}{p}$$

where T is in degrees Kelvin and p is in Pascals.

Liquid Relative Permeability and Capillary Pressure Curves

. In the van Genuchten correlation [Peters et al., 1984] the capillary head h is related to the saturation by

$$s_{e} = \left[1 + (\alpha h)^{\beta}\right]^{-\lambda}$$

where

$$S_{s} = \frac{(s_{l} - s_{r})}{(1 - s_{r})}$$

 $s_r = residual saturation$

$$\lambda = 1 - 1/\beta$$

- α , β = two correlating parameters found by curve fitting with experimental data
- The liquid relative perneability is given by

$$k_{rl} = \frac{\left\{1 - (\alpha h)^{\beta-1} \left[1 + (\alpha h)^{\hat{\mu}}\right]^{-\lambda}\right\}^2}{\left[1 + (\alpha h)^{\beta}\right]^{\lambda/2}}$$

- for the fractures, $\alpha = 1.2851 \text{ m}^{-1}$, $\beta = 4.23$,
- for the matrix, $\alpha = 5.67 \times 10^{-3} m^{-1}$, $\beta = 1.798$,
- matrix residual liquid saturation* s_r = 0.0 (the original COVE3 value was 0.0801, personal communication with R. Peters [1987] indicates that a value of 0.0 is closer to experimental data)
- fracture residual liquid saturation* s_r = 0.0 (the original value was 0.0395; results for the equivalent continuum model used in this report are not sensitive to this parameter; they would be if there were a high suction gradient in the fractures near the residual value)

However, note that due to the functional form of the curves used, the relative permeability (arve for the fractures (figure 5) becomes essentially non-conductive at a fracture saturation of 0.3, and, similarly, at a matrix saturation of 0.1 for the matrix curve (figure 5)

In figure 1 we show the plots of the capillary curves for the fracture, the matrix, and for the bulk continuum. Note that due to the low suction of the fracture curve over most of its range, equilibrium between the fracture and matrix can only occur when the matrix is nearly saturated with liquid.

Equivalent Continuum Relative Permeability

$$k_{rl} = \left[K_f k_{rl_f} \phi_f + K_m k_{rl_m} (1 - \phi_f)\right] / K_b$$

where

 K_f , K_m = fracture and matrix saturated permeabilities and the saturated bulk liquid permeability is given by

$$K_b = K_f \phi_f + K_m (1 - \phi_f)$$

A plot of the bulk relative permeabilities is given in figure 2.

Gas relative permeability

 $k_{rg} = 1 - k_{rl}$

Capillary pressure cutoff*

The original van Genuchten correlation for the capillary pressure goes to infinity at

the liquid residual saturation and is undefined below this value. In order to use the correlation below residual saturation a capillary cutoff at a liquid saturation of 0.12 was specified in COVE3, i.e. the capillary pressure evaluated at points below 0.12 was set to the value computed by the van Genuchten formula at 0.12 saturation. The resulting derivative discontinuity at this cutoff point was found to cause numerical problems during the cool-down phase. We therefore replaced the cutoff by a more gradual linear one that intersects the y axis at a capillary head equal to the largest measured in [Peters et al.,1984]. Furthermore, a matrix residual saturation of 0.0 instead of the previous value of 0.0801 appears to be closer to the experimental data [R. Peters, personal communication]. Therefore, the actual portion of the curve that needs to be smoothed is very small in extent. The actual capillary curve modification used in terms of head is

 $h = h_0 + (h_1 - h_0)/s_1$

for $0.0 \le s < s_1$

where

 $s_1 = 0.0432$

 $h_1 = 1.89 \times 10^4 \text{ m}$

 $h_0 = 9.1 \times 10^3 \text{ m}$

A plot of the capillary curve is given in figure 1.

Waste Package Configuration

348 m below surface

225 m above water table

Spacing between containers: 37.8 m based on 57 kW/acre initial average heat load based on 8.555 year old PWR spent fuel container [Langkopf, 1985]

Boundary Conditions*

ground surface 348 m above container:

286° K constant temperature and 1.0×10^5 Pa gas phase pressure with zero capillary pressure and zero water saturation at the topmost element representing the surface; constant water influx rate of 0.1 mm/year, 0.5 mm/year, or 1.0 mm/year into first

element below ground surface element

water table

225 m below container: fixed temperature of 304 K, constant gas phase pressure of 1.0422×10^5 Pa with saturation fixed at 1.0

lateral boundaries

18.9 m from container: no lateral flow

Waste Package Heat Source Term

5.05 m long container of 8,555 PWR spent fuel

$$H(t) = \sum_{i=1}^{6} b_i \exp(-a_i t) \quad (Watts)$$

t = years emplacement

$$b_1 = 31.7$$
 $a_1 = 2.82 \times 10^{-5} \text{ year}^{-1}$

 $b_2 = 48.6$ $a_2 = 1.29 \times 10^{-4} \text{ year}^{-1}$

 $b_3 = 443.3$ $a_3 = 1.76 \times 10^{-3} \text{ year}^{-1}$

$$b_4 = 2123.$$
 $a_4 = 2.0 \times 10^{-2} \text{ year}^{-1}$

$$b_5 = 431.5$$
 $a_5 = 6.35 \times 10^{-2} \text{ year}^{-1}$

- $b_6 = 321.9$ $a_6 = 4.4 \times 10^{-1} \text{ year}^{-1}$
- container average heat capacity: 325 J/kg-K
- container average density: 2535 kg/m³
- container radius (set to borehole radius): 0.36 m

Mesh Geometry of Numerical Model

Originally a rectangular mesh was used to perform our simulations, but 1-D and 2-D grid sensitivity runs showed the need for finer radial resolution with respect to distance from the waste package. This could not be achieved using a rectangular mesh due to the large bandwidths that result in the system of linear equations that are solved in TOUGH. We therefore implemented a curvilinear mesh (figure 7) allowing for a fine radial resolution to be achieved with minimal matrix bandwidths.

Since the space discretization method in TOUGH requires an orthogonal mesh, we wrote a program that uses streamlines and level curves of the harmonic potentials

resulting from an array of line sources in order to generate our grid lines. Further grid sensitivities need to be made in the future to see whether the fine resolution we used near borehole is really necessary for predicting parameters pertinent to the waste package design and performance. In any case, the use of a curvilinear mesh is much more efficient than a rectangular mesh.

The mesh generation software was checked by running TOUGH on a thermal conduction problem and comparing the results with an analytic solution.

The particular mesh used for our runs has a total of 1473 elements with 119 divisions in the radial direction and 12 divisions in the angular direction (figure 7). At distances farther than 22 meters above and below the waste package the two dimensional mesh becomes a one-dimensional column of elements stacked on top of each other, extending to the ground surface and the water table.

Table 2.1 gives the thickness of the radial divisions in the radial direction with respect to the points where the grid lines intersect the z axis.

Table 2.1		
no.of divisions	size	
1	0.3588 m (borehole)	
10	0.07	
40	0.1	
1	0.11	
1	0.12	
1	0.13	
1	0.14	
1	0.15	
1	0.16	
1	0.18	
50	0.20	
1	0.22	
1	0.24	
1	0.26	
1	0.28	
1	0.30	
4	0.4	
1	0.8	
1	1.6	

The original COVE3 problem was limited to only 20 m above and below the waste package. In our simulations we have extended the domain to include the region of rock

up to the surface and down to the water table to provide what we think are more realistic boundary conditions. Although in reality the thermal and hydrologic properties vary significantly over this extended domain, we have, except for the thermal conductivities which are spatially averaged values, used the same property values as those that are expected to occur at the repository level. For the effects of this approximation see below under "Initial Conditions".

Initial Conditions

TOUGH uses gas phase pressure, temperature, and mass fraction or gas saturation as state variables (see appendix). The initial conditions for these variables were obtained by making runs with no container heat flux until steady state fluid and thermal conditions were attained. This was done for each of the surface recharge rates: 0.1 mm/year, 0.5 mm/year, and 1.0 mm/year. These initialization runs were non-isothermal.

It is possible that the variabilities in the rock properties which are not considered in our model, but which are known to occur at the different horizons above and below the repository formation, could lead to saturation conditions being in significant error from currently predicted repository conditions. However, it turns out that our calculated steady values at the repository level were close to those obtained by Wang and Narasimhan [1986] who did take the spatial variability of the rock properties into account. Because of this fact and since the perturbations due to the waste package will be localized around the waste package the use of uniform properties is justified when modeling conditions near the waste package.

Table 2.2.

The initial values that occur in the rock immediate to the waste package are given in

Table 2.2			
surface influx	gas phase pressure	liquid saturation	temperature
0.1 mm/ут	1.026 x 10 ⁵ Pa	0.854	23.18° C.
0.5 mm/yr	1.026 x 10 ⁵ Pa	0.980	23.14° C.
1.0 mm/yr	1.026x 10 ⁵ Pa	0.985	23.09° C.

Note that the 1.0 mm/yr case in Table 2.2 is above the critical bulk saturation of

$$\frac{(1-\phi_f)\phi_m}{\phi_f+(1-\phi_f)\phi_m}=0.98387$$

which was discussed at the end of section 1 and is the point at which the matrix becomes nearly saturated and significant amounts of fracture water begins to exist. The value of 0.985 bulk liquid saturation converts to a saturation of 0.085 in the fractures. A look at the fracture relative permeability curve (figure 5) indicates that the water is essentially immobile in the fracture at this saturation. The bulk saturation for the 0.5 mm/yr case is just below the critical value. Also note that the slight differences in initial temperature are due to the cooling effects of the surface recharge water that has a temperature of 12.85° Celsius, the same as the constant ground surface temperature used in our boundary conditions.

3. Discussion of the Physical Assumptions

It is important to keep in mind the many assumptions, estimations, and approximations present in our model. These are reviewed below.

- The equivalent continuum model for fracture flow in a partially saturated porous medium is based upon the assumption that thermodynamic equilibrium between matrix and fractures is attained over sufficiently small times relative to the time constants of the physical phenomena of interest. The degree of accuracy of this approximation is, as mentioned previously, not completely known. The continuum approximation is also based in some sense upon the existence of a sufficient fracture density. If fracture spacings are too large in comparison with the scale of the problem, the effective bulk hydraulic behavior will be predicted on too large a scale. In other words, the behavior will likely be inconsistent with that which is measured in the near-field environment. Thus, the model results used in this report may not be accurate if the rock at the repository level is fractured less than is believed or if the fracture density is highly variable over space. Our continuum model also assumes that the individual fractures are sufficiently oriented such that their bulk hydraulic behavior can be described as isotropic. One other factor that has not been addressed is the extent to which fractures act as capiliary barriers or conduits for cross-frecture flow [Wang and Narasimhan, 1986].
- The boundary conditions chosen represent, by symmetry, an infinite array of waste packages. Comparison of this approximation with that of a finite array has been done by Montan [1987] using pure thermal conduction models. His work indicates that for times greater than 600 years the infinite array assumption can lead to the prediction of higher temperatures due to the contribution of the "image" sources located beyond the finite extent of the array.
- The repository configuration is currently planned to have different kinds of waste in alternating rows [Schelling, 1987]. We have assumed that our waste package contains typical PWR spent fuel that is 8.55 years old. We have adjusted the spacing in order for

the heat load per acre to be representative. The spacing of the various rows of waste packages will likely have a strong effect on the hydrological and thermal behavior as will the emplacement scheduling of the containers on the amount of heat given off by the various kinds of waste.

- In our simulations we have assumed constant rock properties around the waste package; i.e., variations in matrix as well as fracture properties have been neglected. Future simulations may have to consider inhomogeneities such as highly rubblized shear zones found in the G-tunnel complex at the Nevada Test Site which has formations similar in origin to those at Yucca Mountain.
- Our model ignores any thermal effects due to the large scale convection cells that may exist over the repository [Pruess, 1986].
- The model does not address the effects of the gap between the waste package container and the bore hole wall. In particular if this gap is empty, preliminary runs that we have done show that a significant amount of steam can escape through this pathway assuming that the borehole is not completely scaled from the drifts. The extensive drift ventilation that will be present before repository closure [Hopkins,1987] will also reduce the moisture coment in the rock. Thus, our simulations are conservative in this regards in overpredicting the amount of water in the rock around the package.
- The thermal effect of a borehole air gap, which we have neglected, is to insulate the container to some degree. The temperature of the container we predict will be lower than if this effect is incorporated, especially at early times, but the rest of the system should not be affected significantly.
- Capillary pressure is one of the main mechanisms that affect the time for the wetting front to recede and reach the bore hole wall. Our model does not have capillary hysteresis. The curves that we used are from Peters et al. [1984] who varied saturations in their core by drying in a microwave oven thus resulting in measurements that are under

mixed drainage and imbibitory conditions. Use of pure imbibition curves would be more appropriate for our modeling during the cooldown rewetting phase and could significantly increase the predicted time required to rewet the borehole. The proportional increase in time is approximately given by a factor which is equal to the average ratio of the drainage to imbibition suction pressure over the saturation range of interest [Buscheck and Nitao, 1988].

- Vapor pressure lowering, as given by the Kelvin law or its variants, is due to the surface energy present at the liquid-gas interface. Its effects are significant at the strong matric potential that exists in tuff at low liquid saturations. Because the mean pore radii in Topopah tuff are on the order of 40 nanometers [Klavetter, 1986], there is reason to believe that the high potentials are caused by surface adsorbed water. Experimental evidence indicates that the amount of adsorbed water decreases as temperature increases [Derjaguin, 1981]. This leads one to believe that the amount of water that is adsorbing onto the rock due to vapor pressure lowering is being overpredicted since the curves being used are measured at room temperature. Capillary curves need to be measured at different temperatures and different saturation histories.
- It is important to realize that the characteristic curves for the fractures are estimates [Wang and Narasimhan, 1986]; no experimental curves are available. Pruess has shown that different characteristic curves in the fractures can lead to highly different hydro-thermal behavior --- film flow in the fractures under high suction gradients could lead to a heat pipe that has a strong cooling effect on the container which would then allow liquid water to remain close to the borehole. It is clear that more experimental work needs to be performed in this area. The matrix relative permeabilities that have been used are not from direct experimental data. They were derived from the capillary curves of Peters et.al. [1984] using the theoretical method of Mualem [1976].

4. Code Modifications and Enhancements

Several modifications to the TOUGH code were necessary in order to be able to run the problems described in this report. The modifications to the physical process models included the incorporation of vapor pressure lowering and the characteristic curves for the the equivalent continuum approximation. (Some versions of the code at Lawrence Berkeley Laboratories have vapor pressure lowering but the release version does not since for most applications vapor pressure lowering is negligible and would increase computational time.)

The TOUGH code is written in FORTRAN and encompasses about 7,000 lines of source code. The original code that we obtained had a limitation of 500 elements and had to be converted to variably dimensioned format. It was converted to run on the CIVIC compiler at the NMFE Center in order to allow us to make our runs on the CRAY-2 which is able to handle larger problems because of its large memory. Other code changes were necessary in order to increase the speed of execution. A block banded matrix solver was coded to replace the general-purpose sparse matrix solver in TOUGH. The PVT functions were replaced by a table lookup algorithm. An improved automatic time stepping algorithm was developed to allow long problems to be run more efficiently without user intervention. Together with various other code optimizations, these changes accelerated the code by a factor of five. These changes were verified by running test problems numbers 1 and 6 in the TOUGH manual. Further verification occurred in the COVE3a code benchmarking exercise which is currently in progress.

Use of preconditioned conjugate gradient linear equation solvers [Behie, 1980], adaptive moving meshes, and more extensive vectorization are other changes that could further increase the code's efficiency. The implementation of these changes has been resisted, however, as it would probably require a major rewrite of the code and destroy its modularity. A more general porous media flow model is currently being developed that will have these enhanced features.

The original COVE problem specified a capillary curve that had a sharp cutoff at residual liquid saturation. If this curve is smoothed near the residual saturation level (section 2) the number of iterations required for convergence is reduced. This procedure improves the computational efficiency by another factor of two, giving an overall improvement factor of 10 for the COVE problem. A COVE run out to 2600 years now requires 4 cpu hours of CRAY-2 time as compared with 40 hours without these modifications.

In order to reduce the bandwidth of our solution matrix we have implemented a curvilinear mesh generator based on potentials. The TOUGH code is based on the integrated finite difference method and therefore requires orthogonal grid lines if a 5-spot computational molecule in two dimensions is used. It is a common procedure to generate such a grid using level curves and streamlines from harmonic potentials [Robertson and Woo, 1978]. The potentials we used were a superposition of logarithmic potentials with singularities at the periodic locations of the waste packages up to 15 on each side of the package being modeled. A preprocessor was written that creates the curvilinear mesh and generates TOUGH input parameters. In order to interpret the results we need to have graphical output of the physical variables. A postprocessing system was therefore developed on the Sun Workstation that extracts data from TOUGH output, performs any necessary interpolations, and converts it into a form suitable for plotting. The graphs used in this report were performed using the SAC graphics software [Tull, 1987].

Most of the above enhancements have found use in other NNWSI hydrological modeling studies as in Buscheck and Nitao [1988].

5. Model Calculations

The calculations were carried out using the TOUGH code which uses the integrated finite difference method [Preuss, 1985]. The governing equations are given in the appendix.

As mentioned earlier, model simulations were made with surface recharge fluxes of 0.1 mm/yr, 0.5 mm/yr, and 1.0 mm/yr. Typical cases took 4 CPU hours on the CRAY-2 with 350 time steps. In order to ascertain the effect of the pore water on the thermal history, a case which considered only thermal conduction was also carried out by initializing the model with no water in the pores and setting hydraulic conductivities to zero. A rock thermal conductivity of 2.08 W/mC was used for this case which is an average value of dry and wet thermal conductivities, and the specific heat of the rock was set to equal to the dry rock value as given in section 2.

We now discuss the results of all of these cases. Times reported will always be with respect to the time at which the waste package is emplaced into the repository. Vertical distances are with respect to the waste package center, positive being above and negative below.

Table 5.1				
recharge rate	initial liq. sat. at waste pkg.	time to first presence of water at bore hole wall	time to reach initial liq. sat.	max. temperature of waste pkg.
0.1 mm/yr	0.854	1400 yr	> 2600 yr	202 deg. C.
0.5	0.980	1000		199
1.0	0.985	1000	11	199

Table 5.1 summarizes the three cases that have fluid flow.

Temperature Field

Figures 8-9 are a comparison of the temperature history of the container. The effect of the surface recharge rate is relatively small. The temperatures for the cases that included fluid flow in the pores, as opposed to the case where only thermal conduction was considered, is significantly lower after the first 20 years. This is due to the increased heat transfer of the

"heat-pipes" that occur. Their effect is to flatten the temperature gradient at approximately 100 degrees C. as can be seen in figures 10-11. Later, in order to demonstrate the existence of the heat-pipe effect we will show plots of the counterflow of vapor and liquid phases. The temperature profiles along the vertical line through the waste package are shown at different times in figure 12 where negative and positive values on the x axis correspond to distance below and above the waste package center, respectively.

Figures 13-18 are temperature contours at 50 and 400 years for different recharge fluxes. They show that increasing recharge flux results in the contours lying closer to the container. This difference is particularly pronounced between the 0.1 mm/yr and 0.5 mm/yr cases. However, there is only a slight difference between the 0.5 and 1.0 mm/yr cases.

Our use of periodic boundary conditions, which in effect model an infinite array of containers, result in slightly higher temperatures than in the case where a finite array is modeled. As demonstrated by Montan [1987] using models that consider only thermal conduction the temperature difference starts to become significant at 600 years from the time of container emplacement.

Fluid Saturation Field

In figure 19 we have the time history of the liquid saturation in the rock next to the borehole face. Water first returns at about 200 years. This water is due to vapor condensation. Figures 20-21 shows that water mass transfer near the waste package is due to the steam in the gas phase moving towards the container and condensing at temperatures higher than the nominal boiling point due to capillary condensation (vapor pressure lowering). Significant capillary condensation occurs only at liquid saturations below about 0.1 where the capillary tension is sufficiently high. Note that significant condensation will, at this stage, occur in the rock where the capillarity is high and not significantly on the container itself since the container walls are relatively smooth. The high capillary pressures at low saturations that have been measured for Topopah tuff could be due to surface adsorption phenomenon [Marshall, 1979]. Thus, at low saturations the "capillary condensation" may actually be condensation due to surface adsorption. It is important to note that the capillary curves used in our model were measured only at room temperature. To correct for higher temperatures only a simple adjustment factor based on the dependency of the interfluid surface tension on temperature was used. The curves also

do not include the dependence of surface adsorption on temperature. Some experiments (Derjaguin, 1981) indicate that surface adsorption effects may have a decreasing dependence with temperature. If this is so, our simulations would overpredict the condensation due to surface adsorption.

In the vicinity of the waste package our plots show the liquid saturation in the rock during portions of thermal loading to be exactly zero. In actuality there will always be at least a small amount of water adsorbed on the pore walls of the rock. The cause for this difference between theory and simulation is due to our modification described in section 2 of the capillary curve which prevents the capillary pressure from going to the theoretical limit of infinity as the saturation tends to zero. This puts a lower limit on the vapor pressure lowering as given by the Kelvin type equation [Marshall, 1979]

$$p_{\star} = p_{sat.}(T) \exp(\frac{-p_c M_I}{\rho_I T R})$$

As this equation shows, the vapor pressure would go to zero if the capillary curve went to infinity, and therefore the saturation in our simulations would then go to zero. The effect of the capillary pressure at low saturations has been confirmed by previous runs that we have made which were initialized for a slightly different geometry but all other input parameters were the same as the present runs. They show that by increasing the capillary curve at small saturations one can produce simulations that have wa're at the borehole walls at all times.

The amount of water we are underpredicting by our modification of the capillary curve is however very small, and depending on the pore size of tuff may consist of only a few molecular layers in thickness that is very tightly bound to the matrix pore walls. Investigations by Klavetter and Peters [1986] indicate that Topopah tuff may have very small pore sizes. It is known that the few layers of water mext to a pore wall are tightly bound [Derjaguin, 1981] and would not be free to advect although transfer by surface diffusion may be possible [Barrer, 1941].

The water due to capillary imbibition (for our purposes, a liquid saturation greater than 0.1) reaches the borehole wall at about 1000 years for the 0.5 mm/yr and 1.0 mm/yr cases and

1400 years for the 0.1 mm/yr case. There are at least two factors that may actually increase these rewetting times. The first is the fact that the equivalent continuum model ignores the fact that fractures can retard the liquid flow movement as the liquid tries to cross a fracture. The second is that the capillary curves were measured under conditions closer to drainage conditions rather than the imbibition conditions of rewetting. Suction under imbibition is typically an order of magnitude or so lower than under drainage.

At no time within the 2600 year time span of our runs is the water able to enter the borehole space. This conclusion holds for even the 1.0 mm/yr case which has a small amount of liquid water in the fractures. The liquid phase pressure is always less than atmospheric pressure due to the tensions in the matrix and fractures, and the liquid saturation remains below the initial saturation level during the entire 2600 year period. This conclusion is valid, of course, only under our modeling assumptions. For example, the effect of severe hetero-geneities such as rubblized shear zones is unknown.

Figures 22-27 are saturation profiles along the vertical at different times. Note that during the heating period the vaporization of liquid water in the rock near the container and its subsequent condensation results in a transfer of water away from the container. At early times the condensed water increases the liquid saturation in the rock in the region ahead of the boiling zone causing a "hump" to occur in the saturation curve in figure 22 for the 0.1 mm/yr case. This hump is hardly noticeable in higher recharge cases occause the matrix is initially nearly saturated. The vaporization front is rather sharp during the heatup period as the front recedes from the waste package. Preliminary simulations with discrete fractures have shown that in actuality the bulk liquid saturation front would be significantly smeared because of the higher boiling point inside the matrix due to the higher gas pressures in the matrix than in the fractures; the boiling front propagates away from a fracture into the matrix. Such effects are, of course, not considered in our equivalent continuum model. The extent of the vaporized zone is greater in the 0.1 mm/yr case than in the other two cases by about 2 m. This is accounted for by the fact that the initial amount of the water in the rock as given by the initial saturation in the 0.1 mm/yr case is 0.854 which is about 15 percent lower than for the other two cases. The 0.5 mm/yr and 1.0 mm/yr cases have nearly identical initial saturations of 0.980 and

0.985, respectively, and have nearly identical profiles even though the latter case is above the critical saturation at which fracture flow occurs. The main effect of recharge rate may be its effect on raising steady state initial saturation levels near the waste container before heating begins than in its transport properties.

Figures 28-33 show the regions where the fractures contain water at various times for the 0.1 mm/yr and 1.0 mm/yr cases. With our input parameters the significant liquid water saturation in the fractures occurs at a bulk liquid saturation of about 0.984. The fracture water in the 0.1 mm/yr case occurs as a halo about the waste package, wider below the waste package than above it due to gravity driven flow. The 1.0 mm/yr case has, as expected, water in the fractures at all points behind the vaporization front since the initial saturation of 0.985 is above the critical value. The 0.5 mm/yr case which has initial saturation of 0.980 is close enough to the critical value so that it behaves like the 1.0 mm/yr case. The thermal effects of the water in the fractures is small due to the small gradients in the fracture capillary gradient as would occur for surface films, a highly efficient heat pipe in the fracture would keep the rock around the waste package at 100° C. and would result in the water remaining close to the waste package [Pruess, Nov. 1984]. Clearly, more experimental work needs to be done to determine the possible existence of film flow in fractures.

In figures 34-36 we have calculated the liquid saturation in the fractures based on the bulk saturation along a vertical line through the waste package center for the 0.1 mm/yr case. Note that the saturations stay below a value of 0.2.

Figures 37-42 are contours of the liquid saturation at 50 and 400 years.

Water Vapor

Figure 43 is the water vapor mass fraction history at the borchole wall. The atmosphere around the waste package quickly becomes 100 percent steam and stays at this level until 600 years. After this point the water vapor continues to remain higher than the value before

heating started of 2 percent. Figures 44-45 shows the profiles at different times.

Gas Phase Pressure

Figures 46-48 show profiles of the gas phase pressure. They show very little rise from the initial pressure. For the tight matrix permeabilities used in these cases the equivalent continuum model is known to severely underpredict the gas pressures in the matrix. In actuality, simulations with discrete fracture models have shown that several atmospheres of pressure can build up in the matrix.

Darcy Velocities and Flow Rates

Figures 49-51 gives the vertical profile of the vertical component of the gas phase bulk Darcy velocities above the waste package. Gas velocities are generally upward except for a small downward flux near the container. In figure 49 a relatively high blip in the gas velocities is seen at the vaporization front where steam is carried outward and then is condensed. Figures 52-55 give the vertical profile of the vertical component of bulk continuum liquid phase Darcy velocities above the waste package. Liquid Darcy velocities are oriented downward primarily in response to capillary suction. The pronounced blip seen in Figures 52 and 53 is due to the capillary imbibition from the sharp saturation gradient at the saturation halo, as predicted by the equivalent continuum model, into the vaporized zone. A discrete representation of fractures would likely result in a more diffuse transition at the imbibition front,

In order to confirm that the heat pipe effect is the cause of the flat temperature profiles in figures 10 and 11, we have plotted the profile of the vapor mass flow rate to liquid mass flow rate ratio along a vertical line passing through the waste package (figures 56-57). This plot covers only the part of the heat pipe above the waste package. A ratio value of negative one indicates a balanced counter-current of liquid to vapor flow. The region where the heat pipe occurs coincides with the region where the temperature is flat. Note that this part of the heat pipe starts about 12 m above the container center and extends to about 19 m, and evidently lasts for several hundred years. Below the waste package the heat pipe is located lower due to the effect of gravity and starts from about 15 m below the package and ends at about 23 m.

Because of the low permeability of the matrix, liquid counter-current velocities are very low. Therefore, thermal fluxes from the waste package will be greater than the amount that a heat pipe can handle unless the flux area is large. At small distances from the waste package the flux area for a heat pipe across a cylindrical control volume are too low for a heat pipe to be sustained. But from the geometry of the system, the effective flux area will increase, up to a point, as the drying front proceeds outward. At a sufficiently large flux area the convective flux of the counter-current liquid will be balanced, and heat pipe is sustained. Note that at radii farther than 19 m, which is the distance to the no-flow boundary, the flux area across the drying front can no longer increase radially but stays fixed.

The regions of counter current flow of the gas and liquid phases in the heat-pipes can be seen in figures 58-59 which show the vector fields of the phase velocities. The lengths of the vectors are normalized with respect to the maximum velocity in each separate plot.
6. Conclusions

Within the approximations and assumptions utilized in the models our simulations showed the following:

- At the surface recharge rates studied and during the 2600 year time span of our simulations the liquid saturation at the borehole wall next to the container did not return to the initial native saturation after drying from the waste package waste heat began. Liquid pore pressures remain below the borehole pressure so that no liquid flow into the borehole is predicted.
- 2. Small amounts of water due to capillary condensation first reaches the borehole wall at about 200 years. This time is very sensitive to the capillary curves used at the low saturation range. Based upon the conservative surface recharge rate estimate of 0.5 mm./yr. [Montazer and Wilson, 1984], bulk water (saturation > 0.10) first reaches the borehole wall at about 1000 years from emplacement due primarily to capillary imbibition. Future incorporation of hysteretic capillary curves and improved models that take into account the reduced permeability of the flow crossing fractures would further delay the arrival of liquid water.
- Predictions of temperatures near the waste package are significantly lower when flow is included as compared to the case where only thermal conduction and constant specific heat are considered.
- 4. Significant amounts of fracture water are predicted to occur due to the movement and condensation of water vapor in the fractures during the heating period. However, there is no water in the fractures in the vicinity of the waste package due to the drying effects of the waste package heat. For the fracture capillary curves used in this study the effect of fracture water on the thermal response of the system is not significant. It must be kept in mind, however, that these curves are approximations and there is a need for experimental data before any firm conclusions can be made.

Some of the important research areas that we believe should be pursued include:

1. The accuracy and applicability of the equivalent continuum model needs to be reexamined in light of work done in Pruess [1986].

- 2. With regard to analyzing techniques for thermal predictions, comparisons need to be made with heat conduction models that use variable specific heats to model latent heat, such as those used in Montan [1986], and, perhaps, recalibrating such models as necessary. The issue of the effect of using periodic boundary conditions needs to be considered.
- The effect of container spacings and the placement of containers with different heat outputs needs to be studied.
- Experimental data for the matrix and fracture characteristic curves is needed, including measurements at different temperatures, and under both drainage and imbibition conditions.
- Discrete fracture modelling is needed to study the effect of gravity driven flow in fractures, fracture orientation, fracture cross-flow, and highly permeable rubblized shear zones.
- The effect of thermally stressed fracture closures on the near field hydrology is not known.
- 7. The possible effect of film flow in fractures should be investigated since its presence could possibly contribute to water movement toward the container.
- 8. Depending on the suction potential curves, there may be significant amounts of surface adsorbed water in the matrix rock near the container even during the period when the matrix has been almost dehydrated by the waste package heat. The diffusive transport properties of this water may have to be determined experimentally.

Acknowledgments

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Appendix: Description of Governing Equations in TOUGH

The code we have used in our simulations was a version of the TOUGH simulator which we have modified. TOUGH was developed by K. Pruess at LBL [Pruess,1985] and treats two-phase two-component flow in porous media including thermal flow and water-steam interphase mass transfer. Both liquid and gas phases are considered. The liquid phase contains a mixture of water and dissolved air and the gas phase a mixture of water vapor and air. The solid phase of the host porous medium is included in the energy balance but is otherwise passive and immobile. Binary diffusion of the air and water vapor is included. The conservation equations that are solved per are those for total water, air, and energy. Hydrodynamic dispersive fluxes of the individual components in each phase are neglected as is the dispersion of thermal energy in each of the advecting phases. The partial differential equations solved by the TOUGH code have been discussed in Pruess [1985]; for completeness they are given by

<u>Water</u>

$$\frac{\partial}{\partial t} \phi \left(\rho_l s_l x_w + \rho_g s_g y_w \right) + \nabla \cdot \left(x_w q_l + y_w q_g + q_w diff \right) = Q_w$$

<u>Air</u>

$$\frac{\partial}{\partial t} \phi \left(\rho_l s_l x_a + \rho_g s_g y_a \right) + \nabla \cdot \left(x_a q_l + y_a q_g + q_{a, diff} \right) = Q_a$$

Thermal Energy

$$\frac{\partial}{\partial t} (1 - \phi) \left(C_p T \right) + \frac{\partial}{\partial t} \phi \left(\rho_l s_l u_l + \rho_g s_g u_g \right) + \nabla \cdot \left[q_{cond} + h_l q_l + h_g q_g + h_{w_g} q_{wdiff} + h_{a_g} q_{adiff} \right] = Q_h + h_w Q_w + h_a Q_a$$

These equations are spatially discretized using a finite volume, or integrated finite difference, approach and discretized in time by the fully implicit backward Euler method. The resulting set of discretized algebraic equations are non-linear and are solved iteratively using the Newton-Raphson method. The set of primary variables that are solved depend on which phases are present in a grid block:

state	primary variable set
no liquid $s_l = 0.0$	$p_{\mathbf{g}}$, T, y_{a}
no gas $s_l = 1.0$	$p_{\mathbf{f}}, \mathbf{T}, \mathbf{x}_{a}$
liquid and gas $0.0 < s_l < 1.0$	p_{e} , T, s_{e}

We note again several of the main assumptions made in the above conservation equations and in their implementation in TOUGH:

- 1. Thermal equilibrium between the pore fluid and the rock
- 2. Hydrodynamic dispersion is neglected
- 3. Equilibrium thermodynamics is assumed

We now give the constitutive equations that are necessary to close the partial differential equations.

Heat and Mass Transfer Relations

$q_i = \rho_i K \frac{k_{ri}}{\mu_i} (\nabla p_i + g \rho_i \hat{z})$	Darcy's Law
$q_{t} = \rho_{t} K \frac{k_{r_{t}}}{\mu_{t}} (\nabla p_{t} + g \rho_{s} \hat{z})$	
$q_{cond} = K_h \nabla T$	Fourier's Law of Heat Conduction
$q_{wdiff} = \tau \phi s_g D \rho_g \nabla y_w$	Fickian Law for Binary Diffusion
$q_{adiff} = \tau \phi s_g D \rho_g \nabla y_o$	
$D = \frac{D^{0} (T + 273.15)^{\theta}}{p}$	

Characteristic Curves

The characteristic curves that we used are described in section 2. They are of the general form:

$\boldsymbol{k}_{rl} = \boldsymbol{k}_{rl} \left(\boldsymbol{s}_{l} \right)$	$k_{rg} = k_{rg} \left(s_g \right)$	Relative Permeabilities
$p_{\mathbf{g}} - p_{t} = p_{c} \left(s_{\mathbf{g}} \right)$, T)	Capillary Pressure

In COVE3 the capillary curves are multiplied by a temperature dependent water surface tension factor.

Mixing Relations

The properties of the phases are obtained from those of the component PVT values by

$\rho_g = y_w \ \rho_{w_g} + y_a \ \rho_{a_g}$	$\rho_i = \mathbf{x}_w \ \rho_{w_i} + \mathbf{y}_a \ \rho_{a_i}$
$h_g = y_w h_{w_g} + y_a h_{a_g}$	$h_i = \mathbf{x}_{\boldsymbol{w}} \ h_{\boldsymbol{w}_i} + \mathbf{x}_a \ h_{\boldsymbol{a}_i}$
$u_g = y_w \ u_{w_g} + y_a \ u_{a_g}$	$u_l = x_w \ u_{w_l} + x_a \ u_{a_l}$
$\mu_{l} = \mu_{l} \left(\mu_{w_{l}}, \mu_{a_{l}}, x_{w} \right)$	$\mu_g = \mu_g \left(\mu_{w_g}, \mu_{a_g}, y_w \right)$

Tables of component properties are available as functions of temperature and pressure. Interphase Mass Transfer

The mass fraction of air dissolved in the liquid phase is given by

$$\frac{x_a}{y_a} = constant$$
 Henry's Law

The mass fraction of water vapor in the gas phase when the two phases are present is a function of pressure and temperature based on Dalton's Partial Pressure Law, steam table saturation pressure, and vapor pressure lowering

$$y_{w} = f(\rho, T, s_{l})$$

The equation in TOUGH incorporates a more rigorous relationship than the more common approximation

$$y_{w} = \frac{p_{v}}{p_{g}}$$

The vapor pressure lowering due to the suction potential is given by

$$p_r = p_{sol}(T) \exp(\frac{-p_c M_l}{\rho_l T R})$$
 vapor pressure lowering based on Kelvin type law







Figure 2. Bulk Relative Permeability Curves (Log-Log)



Equivalent Continuum Relative Permeability vs. Bulk Liquid Saturation

Figure 4. Matrix and Fracture Liquid Saturation vs. Bulk Liquid Saturation



Figure 5. Matrix and Fracture Relative Permeability

Matrix (solid line) and Fracture (dashed line)

Ground Surface

constant water flux and fluid properties



Water Table

constant fluid properties

Figure 6. COVE3 Problem Geometry (not to scale)



Figure 7. Computational Mesh around Waste Package



Figure 8. Comparison of Temperature at Waste Package, 0-200 years



Comparison of Temperature at Waste Package 0.1 mm/yr, 1.0 mm/yr, and no pore fluid

Figure 9. Comparison of Temperature at Waste Package, 0-2000 years

TEMPERATURE ALONG VERTICAL THROUGH WASTE PACKAGE CENTERLINE AT 100 YRS. 0.1 mm/yr (solid lin.) and 1.0 mm/yr (dotted line) recharge,



Figure 10. Temperature Profile along Vertical through Waste Package at 100 years



Figure 11. Temperature Profile along Vertical through Waste Package at 400 years

TEMPERATURE ALONG VERTICAL THROUGH WASTE PACKAGE CENTERLINE 0.1 mm/yr recharge



Figure 12. Temperature Profiles along Vertical through Waste Package at Various Times, 0.1 mm/yr recharge



Figure 13. Temperature Contours at 50 years, 0.1 mm/yr



Figure 14. Temperature Contours at 400 years, 0.1 mm/yr



Figure 15. Temperature Contours at 50 years, 0.5 mm/yr



Figure 16. Temperature Contours at 400 years, 0.5 mm/yr



Figure 17. Temperature Contours at 50 years, 1.0 mm/yr



Figure 18. Temperature Contours at 400 years, 1.0 mm/yr



Comparison of Liquid Saturation At Borehole Wall 0.1 mm/yr, 0.5 mm/yr, and 1.0 mm/yr

Figure 20. Ratio of Water Vapor Mass Flow Rate to Liquid Flow Rate, Profile above Waste Package at 400 years, 0.1 mm/yr



Gas Phase Darcy Velocities at 400 years 0.1 mm / yr recharge



LIQUID SATURATION PROFILES ALONG VERTICAL LINE THROUGH WASTE PACKAGE CENTER 0.1 mm/yr recharge



Figure 22. Liquid Saturation Profiles along Vertical through Waste Package, 0.1 mm/yr



Figure 23. Liquid Saturation Profiles along Vertical through Waste Package, 0.1 mm/yr

LIQUID SATURATION PROFILES ALONG VERTICAL LINE THROUGH WASTE PACKAGE CENTER 0.5 mm/yr recharge



Figure 24. Liquid Saturation Profiles along Vertical through Waste Package, 0.5 mm/yr



LIQUID SATURATION PROFILES ALONG VERTICAL LINE THROUGH WASTE PACKAGE CENTER 0.5 mm/yr recharge

Figure 25. Liquid Saturation Profiles along Vertical through Waste Package, 0.5 mm/yr

LIQUID SATURATION PROFILES ALONG VERTICAL LINE THROUGH WASTE PACKAGE CENTER 1.0 mm/yr recharge



Figure 26. Liquid Saturation Profiles along Vertical through Waste Package, 1.0 mm/yr



Figure 27. Liquid Saturation Profiles along Vertical through Waste Package, 1.0 mm/yr



Figure 28. Water in Fracture at 29 years, 0.1 mm/yr



Figure 29. Water in Fracture at 39 years, 0.1 mm/yr



Figure 30. Water in Fracture at 50 years, 0.1 mm/yr



Figure 31. Water in Fracture at 100 years, 0.1 mm/yr



Figure 32. Water in Fracture at 29 years, 1.0 mm/yr







Figure 34. Fracture Liquid Saturation along Vertical Line through Waste Package Center, 29 years



Figure 36. Fracture Liquid Saturation along Vertical Line through Waste Package Center, 100 years



Figure 37. Liquid Saturation Contours at 50 years, 0.1 mm/yr



Figure 38. Liquid Saturation Contours at 400 years, 0.1 mm/yr



Figure 39. Liquid Saturation Contours at 50 years, 0.5 mm/yr



Figure 40. Liquid Saturation Contours at 400 years, 0.5 mm/yr



Figure 41. Liquid Saturation Contours at 50 years, 1.0 mm/yr



Figure 42. Liquid Saturation Contours at 400 years, 1.0 mm/yr



Comparison of Water Vapor Mass Fractions At Borehole Wall 0.1 mm/yr, 0.5 mm/yr, and 1.0 mm/yr

Verficel Distance Relative to Wosfe Package Center (m.) Figure 44. Water Vapor Mass Fraction Profiles along Vertical through Waste Package Center, 0.1 mm/yr

- 20

_____ -30

0.01-30

-20



Figure 45. Water Vapor Mass Fraction Profiles along Vertical through Waste Package Center, 0.1 mm/yr



Figure 46. Gas Phase Pressure Profile at 1 year





1.10

Figure 48. Gas Phase Pressure Profile at 400 years

30



Figure 50. Gas Phase Darcy Velocities at 1500 years, 0.1 mm/yr



Figure 51. Gas Phase Darcy Velocities at 2000 years, 0.1 mm/yr

Liquid Darcy Velocities at 400 years 0.1 mm / yr recharge



Figure 52. Liquid Phase Darcy Velocities at 400 years, 0.1 mm/yr
-69-Liquid Darcy Velocities at 400 years 0.1 mm / yr rocharge







Figure 54. Liquid Phase Darcy Velocities at 1500 years, 0.1 mm/yr



Figure 56. Ratio of Water Vapor Mass Flow Rate to Liquid Mass Flow Rate at 100 years, 0.1 mm/yr



Figure 57. Ratio of Water Vapor Mass Flow Rate to Liquid Mass Flow Rate at 400 years, 0.1 mm/yr



Figure 58. Liquid Phase Velocity Vectors at 400 years, 0.1 mm/yr



Figure 59. Gas Phase Velocity Vectors at 400 years, 0.1 mm/yr