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> K.E. Gray, D.G. Steel, J.D. Hettinger,^{*} D.J. Miller, B.R. Washburn, M. Ware, J.T. Parkman, M.E. Yoder, C. Moreau

Materials Science Division and the Science and Technology Center for Superconductivity Argonne National Laboratory, Argonne, IL 60439

M.M. Eddy

Superconducting Technologies, Inc., Santa Barbara, CA 93111

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*Present address: Dept. of Chemistry and Physics, Rowan College of New Jersey, Glassobro, NJ 08028.

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Effects of Vortex-Vortex Interactions on Ion-Track Pinning in High-T_c Superconductors

K.E. Gray, D.G. Steel, J.D. Hettinger*, D.J. Miller, B.R. Washburn, M. Ware, J.T. Parkman, M.E. Yoder, C. Moreau

Materials Science Division and Science and Technology Center for Superconductivity

Argonne National Laboratory, Argonne, IL 60439

M.M. Eddy,

Superconducting Technologies, Inc., Santa Barbara, CA 93111

Abstract---Many superconductor applications rely on the ability to pin vortex lattices. This ability depends on structural defects to pin individual vortices, but vortex-vortex interactions often play an important role in pinning the other vortices. Experimental progress on this complex problem can be made by introducing random arrays of welldefined pinning centers and studying the flux dynamics for a range of vortex densities (i.e., fields). The results of such studies in épitaxial Tl2Ba2CaCu2Ov films containing ion tracks show the importance of vortex-vortex interactions. As an example, the effective pinning field of the defects rises to many times the ion-dose field for temperatures well below T_c.

I. INTRODUCTION

The principal effect of linear ion-damage tracks is well established. It provides extremely strong pinning centers for magnetic vortices, and because the tracks can be made continuous, their effectiveness is not diminished in regions of field and temperature where the vortices behave two dimensionally [1], e.g., Bi₂Sr₂CaCu₂O_x at 77 K. However, because thermal energy scales are not so different from pinning and vortex-vortex interaction energies, the detailed picture is richer, and the defects may provide additional benefits to applications. It is the purpose of this paper to further explore such ideas by connecting incisive experimental results with simple models.

In particular, we show that the randomness of the defect positions washes out any sharp distinction between fields less than or greater than the dose field, $B_{\phi}=\Phi_0/d_0^2$ where d_0 is the average defect spacing and Φ_0 is the flux quantum. Although the fundamental field scale is still related to the defect density, a temperature-dependent effective dose field B_{ϕ} is found: its value is small just above T_c , but because of vortex-vortex interactions it rises to many times B_{ϕ} for T<<T_c. Comparing data with a simple model of randomness, one concludes that the vortex lattice will distort by a reasonable fraction (~0.25-0.33) of the intervortex spacing, a_0 , to find favorable ion-core pinning sites.

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*Present address: Rowan College, Glassboro, NJ.

Another important issue addresses the dimensionality of the vortices: Are they three-dimensional (3D) vortex lines, or 2D pancake vortices residing independently in every bilayer of closely-spaced Cu-O planes? It is generally agreed that in the most isotropic HTS cuprate, fully-oxygenated YBa₂Cu₃O₇, the vortices are 3D over much of the superconducting phase. However, experiments and theory for the highly-anisotropic HTS, like $Bi_2Sr_2CaCu_2O_x$ and $Tl_2Ba_2CaCu_2O_x$, predict crossovers [1] or phase transitions [2,3], from 3D vortex lines at low fields and temperatures to 2D independent pancakes at higher fields. Linear ion tracks have been used extensively to study the 3D or 2D nature of vortices [4-8]. The high-energy ions amorphize the superconductor in fine (~10 nm diameter) columns along their linear trajectory which provide very strong columnar flux pinning centers. As such, a strong dependence of pinning on the angle between the tracks and the magnetic field is expected for 3D vortices, but not for independent, strictly 2D pancakes. Thus, ion-irradiated samples of YBa2Cu3O7 have demonstrated [4] the 3D nature of its vortices, while initial measurements on $Bi_2Sr_2CaCu_2O_x$ were interpreted [5] to imply 2D pancakes. More recent work [6,7] has concluded that the vortices in Bi₂Sr₂CaCu₂O_x show a finite interbilayer coupling (or line tension) and thus behave 3D. We report measurements showing such 3D behavior at fields and temperatures where thermal activation [1] and scaling [9] measurements imply that the vortices exhibit strongly 2D behavior. We address this contradiction directly and show how the apparent 3D behavior may be consistent with a 2D thermal-activation limit and that the scaling behavior [9] may be the result of very strong intrinsic pinning by the Cu-O layers, rather than strictly uncoupled 2D vortices.

II. SAMPLE FABRICATION AND IRRADIATION

Films of phase pure $Tl_2Ba_2CaCu_2O_x$ were made at Superconductor Technologies, Inc., using laser ablation with a post-deposition anneal: they showed rocking curves with a full-width at half maximum of $<0.4^{\circ}$. Such films display very reproducible superconducting properties, particularly in high magnetic fields where their irreversibility behavior is very nearly identical from sample to sample. Before irradiation, the 8000 Å-thick films were patterned into a series of four microbridges, each 50 mm x 1 mm. Two of the microbridges were shielded from the ion beam using a Ta shield, so that samples with exactly the same process history could be compared with and without irradiation. Transport data on *all* unirradiated (and on all similarly irradiated) sections were virtually identical.

The ion irradiation was performed at the Argonne Tandem Linac Accelerator System (ATLAS) facility at Argonne National Laboratory using 650 MeV Xe or Sn ions. Based on TRIM calculations, the energy deposited by such ions falls below the threshold for continuous tracks only after a distance of about 20 µm, which is much greater than the film thickness (0.8 µm). A uniform lateral distribution of ion tracks was ensured by scattering the ion beam through a Au foil at a distance of ~1 m from the sample (a simple Rutherford scattering algorithm was used to determine the Au thickness needed to achieve a specific ion distribution at the target position). Scattering the beam using the Au foil did not introduce any spaying of the columnar defects, but it had the additional advantage that part of the beam could be scattered into a Si detector for an in-situ measure of the ion flux. The Si detector was calibrated versus a Faraday cup and the resulting distribution of the ion beam was confirmed using a Faraday cup behind various sized apertures.

The defects were confirmed to be amorphous and columnar using transmission electron microscopy on a companion sample irradiated at the same time. Samples were compared before and after irradiation in a magnetic field using standard four-probe dc transport measurements. Both linear response (limit of ohmic resistance at small current density, J) and the very non-ohmic, high-current regime were probed as a function of temperature, T, magnetic field, B, and ion dose.

III. VORTEX DIMENSIONALITY

Upon ion irradiation, thin films generally show a larger reduction in the transition temperature, T_c , in comparison to bulk, e.g., single crystals. This may be caused [10] by the creation of substrate defects which can create stress at the film interface, thereby suppressing T_c . This reduction in T_c becomes quite significant at higher doses, B_{ϕ} . Using the resistive midpoint, T_c is suppressed by ~0.7 K for $B_{\phi}=1$ T, while for $B_{\phi}=2$ T, the difference is ~2 K. For the lowest measurable resistances, these were 1.5 and 4.8 K.

Typical resistance data are shown in Fig. 1 for a $Tl_2Ba_2CaCu_2O_y$ (Tl-2212) epitaxial film as a function of angle between the applied field and the c-axis. These were taken at various magnetic fields (1-7 T), at a temperature of 80 K and in the small-current limit (i.e., the linear current-voltage, I(V), response regime in which the Magnus (Lorentz) force plays a negligible role in depinning vortices). These data are for that part of the film which has been irradiated with ions approximately parallel to the c-axis ($T_c=102.2$ K) at an average density of $B_{\phi}=2$ T. Comparable data on the unirradiated section ($T_c=104.2$ K) are shown in Fig. 2.

Qualitatively similar data are found at other temperatures, and virtually identical data are found on other films. Data are normalized by R_n , the high-temperature, normal-state value extrapolated to T_c , which changes slightly after irradiation.

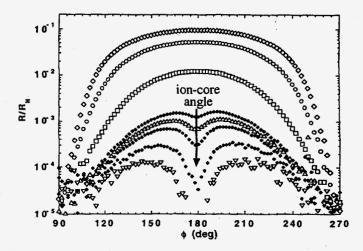


Fig 1. Normalized resistance vs. angle between c-axis and applied field for B=1.5, 1.7, 1.9, 2, 2.1, 3, 5 and 7 (top) T.

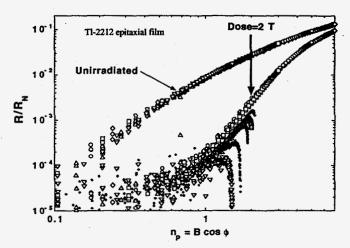


Fig. 2. Data of Fig. 1 with similar data on an unirradiated portion of film plotted against pancake vortex density. The dip of Fig. 1 appears as a downward spike here.

In the irradiated section, dip features are found with the field, c-axis and ion tracks all colinear (i.e., at 0° and 180°), but only at the lowest fields. All the data of Fig. 1, plus the same full set of field values for the unirradiated section, are plotted in Fig. 2 as a function of B|cos ϕ |, which is the areal density of pancake vortices, n ϕ , in the Cu-O bilayers. In the unirradiated section (upper data sets), one observes essentially perfect scaling. Based on Ref. 9, such scaling behavior is often taken to be a sign of 2D pancake vortices. The dissipation measured in the companion irradiated section (see Fig. 2) also scales at the highest fields (3-7 T), but a dip in dissipation is seen for fields aligned with the columnar ion tracks ($|cos\phi|=1$) at lower fields (1.5-2.1 T). These fields are well within both the scaling regime of the *unirradiated* films and the 2D regime of the thermal-activation model [1].

The strong dependence of pinning on the angle between the tracks and the field represented by the dip feature in Fig. 1 is expected for 3D line vortices, but not for independent 2D pancake vortices. Thus these results seemingly contradict both the thermally-activated 2D limit of [1] and the 2D limit implied by [9] from the scaling. We therefore discuss both cases in greater detail.

Thermally-Activated 2D Limit. Dissipation in linear response requires thermal activation, and in [1] this is only significant in the '2D limit', i.e., where kBT exceeds the coupling energy to adjacent bilayers. For the interbilayer coupling, a Josephson coupling energy, $E_j=e_j\Phi_0/B$, where e_j is the intrinsic value per unit area is used and the area is determined by the magnetic length, $\sqrt{\Phi_0/B}$, where Φ_0 is the flux quantum. The need to overcome the interbilayer coupling energy is based on the likely assumption that there is at least one very strong pinning center somewhere along the length of any vortex line. Experimental justification is presented in [1,11]. It should be emphasized that this model predicts strictly 2D behavior only for kBT>>E_j. We thus consider the possibility that even in the dissipative mode with kBT>E_j, that the dip in Fig. 1 can occur upon ion irradiation.

We specifically consider the lowest-energy configuration of pancake vortices in an irradiated sample (modeled by ignoring thermal fluctuations). Such a configuration exhibits stacks of pancake vortices within columnar tracks separated by 'unpinned' chains of pancake vortices, and is described in detail in [12]. It reproduces a dip for alignment, because then there are fewer 'unpinned' chains. If the above model [12] is applied to the lowest-field data of Fig. 1, the fits to the angular dependence are qualitatively reasonable, but the coupling strength compared to pinning is significantly larger than expected from other experiments or the enormous anisotropy of the material. The conclusion of [12] is that of vortexvortex interactions may be needed. Nonetheless, the qualitative results and discussion indicates that the apparent contradiction of the dip with [1] may be a semantical one: the line tension, or E_i, is never strictly zero (i.e., the system is never strictly 2D), and although its effect on thermal activation in linear response is small when kBT>E;, it still affects the number of pancake vortices that, on average, reside outside the columnar defects at a given field angle. A more complete model, which includes finite field effects and vortexvortex interactions, is clearly needed.

Two-Dimensional (2D) Scaling. In spite of the near perfect '2D' scaling shown in Fig. 2 for the unirradiated section, it is clearly seen that the dissipation is not directly proportional to the pancake vortex density, $n_{\varphi}=B|\cos\varphi|$, although such behavior is approached at the highest fields. This is consistent with, and expected for, samples with a distribution of pinning energies. The shift in this distribution from the naturally occurring pinning sites to include the strong ion-defect pinning sites is also clearly visible in the scaled data for the irradiated films of Fig. 2 when compared with the unirradiated data: to achieve the same resistance in irradiated samples takes additional pancake vortices which are rigidly pinned in ion-defect pinning sites.

However, the apparent inconsistency between: the implication of 2D vortices because of such scaling; and the 3D-like dip feature of the irradiated films is still to be addressed. It should be pointed out that the scaling seen in Fig. 2 can also result from the very strong intrinsic pinning which prevents Josephson vortex segments (parallel to the ab-

planes) from moving across such ab-planes. Then only the ab-plane component of the Lorentz force [13] can induce a time-average velocity, v_{ff} , for the thermally-excited vortices. Note that v_{ff} should be unaffected by the presence or absence of Josephson vortex segments because of the negligible dissipation (drag) associated with the small pair density between the bilayers. Finally, the Lorentz transformation to the laboratory frame gives an electric field component in the ab planes to be $v_{ff}B|cos\phi|$. Thus the scaling seen in Fig. 2 may not be a sign of strictly independent 2D pancake vortices, but just weakly-coupled Cu-O bilayers. Note that this conclusion is not in conflict with the idea of a 2D-3D crossover in [9].

Implications of the Dip. Having addressed the apparent inconsistencies of the occurrence of the dip in the 2D regime, we now consider the implications of our measurements. Clearly the simple model described above and in [1] does not satisfactorily explain the dip and it seems likely that the effects of vortex-vortex interactions are its most serious deficiency. As a result, these data may be a useful probe of vortex-vortex interactions in systems with well-defined pinning centers.

IV. EFFECTS OF RANDOMNESS

Our goal here is to consider whether the differences between irradiated and unirradiated samples (e.g., Fig. 2) other than the dip can be quantitatively understood based on the randomness of ion-core defect locations. However, since flux flow dissipation by unpinned vortices is a thermally activated process, data at one temperature alone are not adequate. We therefore have analyzed data similar to Fig. 2 but taken at four temperatures (75, 80, 85 and 90 K), where $T_c=102.2$ and 104.2 K for the irradiated and unirradiated sections of the epitaxial film sample. Such data for rotations in a 6 T field for the irradiated section only are shown in Fig. 3. The Arrenhius plots at all fields are strictly linear, indicating the activation energies are ~1-T/T_c. This is consistent with

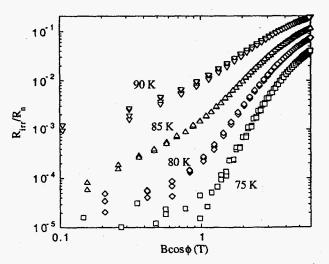


Fig. 3. Effect of temperature on the dissipation as a function of pancake vortex density for a 2 T irradiation dose.

vortex-vortex interactions, as well as depinning from the ion cores of radius $r_{core} >> \xi$, the vortex core diameter. For $B|\cos\phi|=0.4 \text{ T}<< B_{\phi}=2 \text{ T}$, the activation energy is more than four times larger than at 6 T, and we assume this is due to activation *out of* the ion core pinning sites. We make a simple power-law extrapolation of this low-field behavior to higher fields, subtract it from the total and obtain the dissipation from the 'unpinned' vortices, R_{un}. At the highest fields this extrapolation can be questioned, but then the total dissipation is so large that the error would be small.

We proceed by analyzing the 'unpinned' vortex dissipation according to its Arrenhius behavior:

$$\frac{R_{un}}{R_n} \sim n_{un} \nu \exp(E(0)(1-T/T_c)/kT)$$
(1)

where n_{un} is the number of unpinned vortices, v the attempt frequency and E(0) the activation energy. Extrapolating the Arrenhius plot to $T=T_c$, we obtain values of R_{un} as a function of $B|\cos\phi|$, which should be proportional to n_{un} , if we assume a constant v. These are shown as (+) symbols in Fig. 4 as the *fraction* 'unpinned', $F_{un} \sim n_{un}/B|\cos\phi|$. With the temperature dependence thus accounted for, we can compare to simple models which address the random defect positions.

We have numerically determined coincidences between random distributions of defects (both 576 and 900 defects are shown) and rigid Abrikosov lattices of various spacings, a_0 , (defined by $B=2\Phi_0/\sqrt{3} a_0^2$), or equivalently, B/B_{ϕ} . Using the measured ion-core diameter $d_0=10$ nm [12], only a very small fraction of the vortices are pinned by cores except for $B/B_{\phi}<<1$, in contrast to the experiment. Therefore, we modeled a non-rigid vortex lattice by simply increasing the effective core radius. Good agreement was not possible using a larger, but field-independent, effective core radius, r_{eff} . However, the interaction energy between two vortices separated by r_{VV} is $\sim \ln(\lambda/r_{VV})$. As a result, for unperturbed separations of a_0 , the differences in interaction energies, for equal fractional deviations, are independent of a_0 .

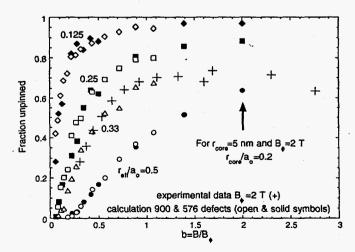


Fig. 4. Comparison of experimental 'unpinned' vortex dissipation with calculations for random ion-core defects.

We can model this by choosing r_{eff} to be proportional to a₀, and such calculations are shown in Fig. 4 for various r_{eff}/a_0 . Note that the experimental data, F_{un} , has been scaled arbitrarily, since the scale factors in Eq. 1 are unknown. The 'best' fit is for $r_{eff}/a_0=0.33$, but since the experimental data at lowest fields depends most sensitively on background subtraction (see Fig. 3), values of r_{eff}/a_0 as low as 0.2-0.25 cannot be ruled out. Such large deviations in vortex positions have been observed [14] by scanning tunneling microscopy in ion-irradiated Bi₂Sr₂CaCu₂O_x and NbSe₂, and ultrasound absorption [15] also indicates a softer lattice at smaller fields.

The drop in the experimental data at highest fields can be explained by the finite physical core radius, $r_{core}=d_0/2$ which should be added to r_{eff} , but which is negligible at low fields.

For B/B $_{\phi}$ >>1, all ion cores pin a vortex so the unpinned fraction becomes F_{un}=1-B $_{\phi}$ /B. Note that placing two vortices in a defect is energetically unfavorable due the very small ratio of physical core radius, r_{core}, to penetration length, λ .

V. INTERACTIONS WITH PINNED VORTICES

In order to account for the interactions of unpinned vortices with those in ion-core defects, an effective dose field is introduced. To see this, the data in Fig. 2 are plotted using linear scales in Fig. 5 to emphasize the high field regime, $B>B_{\phi}$. These give the appearance that the primary effect of irradiation is to shift the resistance curves to higher values of the pancake density, n_{ϕ} . In such an interpretation, the shift in n_{ϕ} at constant resistance can be regarded as the number of pancakes firmly pinned by the defects: this can be thought of as the *effective* dose field, B_{ϕ} , of the columnar defects to be compared with the actual dose field, $B_{\phi}=2$ T. Figure 6 shows the temperature dependence of B_{ϕ}/B_{ϕ} , interpreted in this way. These determinations of B_{ϕ} are complemented by measurements of J_c at lower temperatures where the linear response regime is inaccessable at available field strengths.

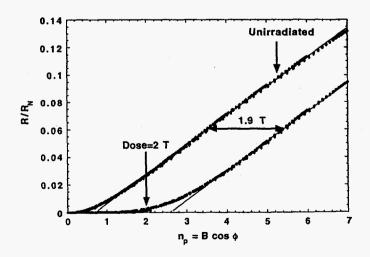


Fig. 5. Data of Fig. 1 plotted on linear scales to show B_{Φ} .

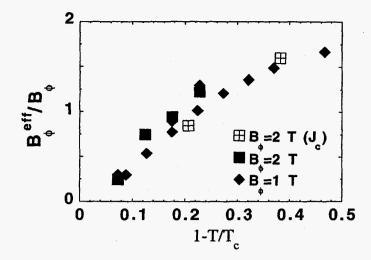


Fig. 6. The effective dose field vs. temperature.

Enhancements of J_c are found up to at least 3 T at 60 K (and 6-7 T at 40 K). There is a fair amount of subjectiveness to the B_{φ} data: the irradiated and unirradiated data of Fig. 5 are not perfectly parallel (as B approaches $B_{c2}(T)$, they must converge); and the low-temperature data (J_c) could not be taken over a sufficiently wide range of currents to define a systematic criterion. Nonetheless, from Fig. 6, we see that B_{φ} is temperature dependent: it vanishes near T_c and rises above B_{φ} at low temperatures. The absence of any apparent feature corresponding to $B=B_{\varphi}$ is consistent with our TEM observations of the ion tracks, which is indistinguishable by eye from a simulated random distribution, but which indicates a significant degree of contact (or overlap) of tracks, together with large areas which contain no ion tracks.

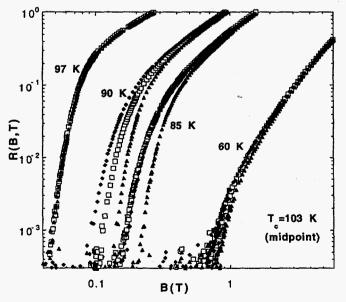


Fig. 7. For $B_{\phi}=0.05$ T: irradiated (triangles); unirradiated (open squares); irradiated data shifted by B_{ϕ} (diamonds).

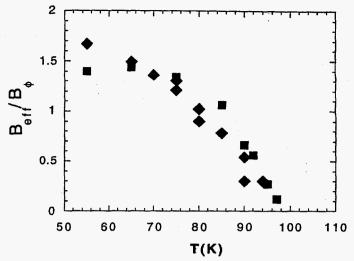


Fig. 8. Comparison of effective dose field for $B_{\phi}=0.05$ T (squares) and $B_{\phi}=2$ T (diamonds).

It seems clear that a treatment of vortex-vortex interactions will be necessary to fully understand how the effective dose can be larger than the actual dose of defects. A more rigorous confirmation and a further exploration of this effect requires samples with lower B_{φ} , to obtain larger B_{ϕ}/B_{ϕ} ratios. Data on similar epitaxial Tl₂Ba₂CaCu₂O_v films irradiated to a dose of 0.05 T are shown in Fig. 7. At 85 K, there is no difference if the irradiated curve is shifted by 0.05 T, which is consistent with all defects being occupied by vortices. However, at 90 K such a shift overestimates the differences indicating a smaller effective field and at 97 K there is virtually no difference after irradiation, i.e., $B_{\phi}=0$. Finally, at 60 K a greater shift than 0.05 T is required to match the data. Qualitatively this is the same result found for the film with a 2 T dose, and Fig. 8 demonstrates the nearly equivalent behavior, indicating that this general trend may be universal.

VI. SUMMARY

We have made careful measurements in a magnetic field of the resistive dissipation in high-quality epitaxial films of $Tl_2Ba_2CaCu_2O_x$, both in the pristine state and after ion irradiation to various doses. These data were collected as a function of the field angle with respect to the crystallographic c-axis (which coincided in most samples with the ion-track direction) over a wide range of fields and temperatures. The appearance of a dip in dissipation for fields aligned with the columnar defects of the irradiated sample was surprising since such a dip has been taken as evidence for 3D vortices yet our data is collected at fields and temperatures where the thermal activation [1] model and scaling [9] measurements imply that the vortices exhibit strongly 2D behavior. We have presented a qualitative model to address the apparent contradiction with thermal activation, but recognize that important effects, such as vortex interactions, are missing and may be the key to a

quantitative reconciliation. We also suggest that the scaling behavior may be connected with weak interlayer coupling and not necessarily with the occurrence of strictly 2D vortices.

We have shown that the randomness of the defect positions washes out any sharp distinction between fields less than or greater than the dose field. Comparing data with a simple model of randomness, one concludes that to maximize the occupation of favorable ion-core pinning sites, the vortex lattice will distort by a reasonable fraction (~0.25-0.33) of its intervortex spacing, ao.

A second result of vortex-vortex interactions, is the appearance of an effective dose field, B_{ϕ} , which is temperature dependent. Because of interactions between the 'unpinned' vortices and those in ion-core defects, Bo rises to many times B_{ϕ} for T<<T_c.

In total, these experiments indicate that including vortexvortex interactions in important to a full understanding of flux dynamics in high-temperature superconductors. The picture is summarized by Fig. 4, in which there is presumably one universal curve for the reff/ao value corresponding to the appropriate effect of vortex interactions on the rigidity of the vortex lattice. In principle, the vortex interactions with pinned vortices and thermal effects represented in Fig. 6 and 8 should rescale the dose field used in Fig. 4, but the experimental evaluation of the 'unpinned' fraction is non trivial since the data for Fig. 4 was determined from activation analyses over a range of temperatures.

Further work should be done on other high-temperature superconducting materials and other doses to understand the connection between these results. Among other things, it would be useful to verify the universality of the value of reff/ao and of the temperature dependence of the effective dose field. In principle, the ideas here can be extended to other

types of defects, e.g., point defects in materials with 3D vortices, like YBa2Cu3O7.

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