

Metallic Stripes in High-Temperature Superconductors

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A phenomenological approach is applied to explore signatures of disordered charge stripes and antiphase spin domains in single-particle properties of the high-temperature superconductors. Stripe phases are shown to explain many experimentally observed unusual features measured in angle-resolved photoemission and optical spectroscopy. It is argued that disordered and fluctuating stripe phases are a common feature of high-temperature superconductors, supported by the additional evidence from neutron scattering and NMR.

I. INTRODUCTION

One of the emerging new paradigms of high-temperature superconductors is that their normal-state properties are inherently connected to disordered or fluctuating stripe phases [1]. In this paper, we show that single-particle properties of a disordered stripe phase can account for exotic features of the spectral density measured by angle-resolved photoemission spectroscopy (ARPES) in $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+x}$ (for which the best data is available). In particular, we compute the spectral density in a background of disordered stripes and show that it reproduces the experimentally-observed shape of the Fermi surface, the existence of nearly dispersionless states at the Fermi energy ("flat bands"), and the appearance of weak additional states ("shadow bands") [2-5], features which have no natural explanation within conventional band theory. Finally, we comment briefly on the implications of partially ordered spin domains for NMR experiments.

Recent elastic neutron-scattering experiments [6] in $\text{La}_{1.6-x}\text{Nd}_{0.4}\text{Sr}_x\text{CuO}_4$ show that the suppression of superconductivity in the neighborhood of $x = \frac{1}{8}$ is associated with the formation of an ordered array of charged stripes which form antiphase domain walls between antiferromagnetically ordered spins in the CuO_2 planes. This observation provides the long-sought explanation of the behavior [7] of the $\text{La}_2\text{CuO}_{4-\delta}$ family of compounds near to $\frac{1}{8}$ doping, and strongly supports the idea of stripe phases.

Antiphase spin domains in $\text{La}_{1.6-x}\text{Nd}_{0.4}\text{Sr}_x\text{CuO}_4$ are indicated by a set of resolution-limited peaks in the magnetic structure factor at wave vectors $(\frac{1}{2} \pm \epsilon, \frac{1}{2})$ and $(\frac{1}{2}, \frac{1}{2} \pm \epsilon)$ [6]. The associated charge stripes give rise to peaks in the nuclear structure factor at wave vectors $(\pm 2\epsilon, 0)$ and $(0, \pm 2\epsilon)$ [8]. As mentioned by Tranquada *et al.* [6], it is natural to interpret the *inelastic* peaks in the magnetic structure factor which occur [9] at similar locations in reciprocal space in *superconducting* samples of $\text{La}_{2-x}\text{Sr}_x\text{CuO}_{4-\delta}$ as evidence of "extended domains"

[10] of stripe fluctuations, in which the stripes are oriented along vertical or horizontal Cu-O bond directions respectively.

In the early days of high-temperature superconductivity, it was shown that holes added to an antiferromagnet form an *insulating* stripe phase via a Fermi-surface instability [11], which leads to a reduced density of states, or a gap, at the Fermi energy. An alternative mechanism for stripe phases is the competition between phase separation [12] (*i.e.*, the tendency of an antiferromagnetic insulator to expel doped holes) and the long-range part of the Coulomb interaction. In this case, the stripes may be either ordered, quantum melted, or disordered by quenched randomness [13]. The charge forms an array of *metallic* stripes, with a period that is determined by the energetics of phase separation and is unrelated to nesting vectors of the Fermi surface. The charge structures, in turn, drive the modulation of the antiferromagnetic order. The experiments [6] on $\text{La}_{1.6-x}\text{Nd}_{0.4}\text{Sr}_x\text{CuO}_4$ clearly favor the latter point of view. The ordering wave vectors do not nest the Fermi surface, and the ordered system has partially-filled hole bands associated with the stripes. Moreover the magnetic peaks first develop below the charge-ordering temperature [6,14]. Our interpretation of the ARPES experiments on $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+x}$ lends further support to this conclusion: we find an increased density of states corresponding to the flat bands seen in the experiments.

II. STRIPE PHENOMENOLOGY

Our objective is to determine a phenomenological band structure for electrons moving in an effective potential generated by charge stripes and antiphase spin domains. The phenomenological one-body Hamiltonian is given by:

$$H = -t \sum_{\langle l'l' \rangle \sigma} (c_{l'\sigma}^\dagger c_{l\sigma} + H.c.) + \sum_{l\sigma} V_\sigma(\mathbf{R}_l) n_{l\sigma}, \quad (1)$$

where the first term is the nearest-neighbor hopping on a square lattice and the second one describes the interaction with the effective stripe potential. Here, $c_{l\sigma}$ annihilates an electron of spin $\sigma = \pm$ at site \mathbf{R}_l and $n_{l\sigma} = c_{l\sigma}^\dagger c_{l\sigma}$. The effective potential is given by:

$$V_\sigma(\mathbf{R}) = \rho(\mathbf{R}) + \sigma S(\mathbf{R})e^{i\mathbf{Q}\cdot\mathbf{R}}, \quad (2)$$

where $\mathbf{Q} = (\frac{\pi}{a}, \frac{\pi}{a})$ and a is the lattice spacing. Specifically, for vertical stripes, we use the forms $\rho(x, y) = \rho_0 \sum_n \text{sech}[(x - x_n)/\xi_c]$ and $S(x, y) = S_0 \prod_n \tanh[(x - x_n)/\xi_s]$, where $\mathbf{R} = (x, y)$, x_n are fixed centers of the stripes, and the parameters ρ_0 , S_0 , ξ_c , and ξ_s determine the amplitude of the charge and spin modulation and whether the stripes are narrow or broad.

III. ARPES AND STRIPE PHASES

According to the usual interpretation [15], the measured photo-current in a photoemission experiment is the product of the electronic spectral density $A_-(\mathbf{k}, \epsilon)$ for the removal of one electron from the system and a slowly varying matrix element which reflects the photon polarization selection rules. This spectral density can be written as $A_-(\mathbf{k}, \epsilon) = f(\epsilon)A(\mathbf{k}, \epsilon)$, where $f(\epsilon) = 1/[e^{(\epsilon - \epsilon_F)/k_B T} + 1]$ is the Fermi function, ϵ_F is the Fermi energy, and $A(\mathbf{k}, \epsilon) = -(1/\pi)\text{Im}G(\mathbf{k}, \epsilon + i0^+)$ is the spectral density of the one-electron Green's function $G(\mathbf{k}, t) = -i\langle T c_{\mathbf{k}\sigma}(t) c_{\mathbf{k}\sigma}^\dagger(0) \rangle$.

A. An ordered stripe phase

First, consider vertical stripes condensed into a regular array: $\rho(x+\ell) = \rho(x)$ and $s(x+2\ell) = s(x)$, where ℓ is the separation between stripes. Results will be presented for bond-centered stripes, $x_n = n\ell + a/2$ with ℓ/a integer, but they are largely insensitive to this assumption. For even ℓ/a , the unit cell size is $(2\ell/a) \times 2$ so the band-structure is computed by diagonalizing a $(4\ell/a) \times (4\ell/a)$ matrix for each \mathbf{k} -vector.

Figure 1 shows the spectral density A_- (integrated over an energy window $\Delta\epsilon = t/30$ about ϵ_F) as a function of \mathbf{k} . For illustration, we have used the parameters $\rho_0 = -t/2$, $S_0 = 2t$, $\xi_c = a$, and $\xi_s = 2a$, for which the Hamiltonian in Eq. (1) solves Hartree-Fock theory for the Hubbard model with $U/t = 4 - 5$. However, to describe $\text{La}_{1.6-x}\text{Nd}_{0.4}\text{Sr}_x\text{CuO}_4$ [6] at $x = \frac{1}{8}$ doping, we choose $\ell/a = 4$, which does not minimize the Hartree-Fock energy.

The fine features of the Fermi surface reflect the energy gaps at points spanned by the wave vectors $(\frac{1}{2} \pm \epsilon, \frac{1}{2})$ of the spin order and $(\pm 2\epsilon, 0)$ of the charge order, where $\epsilon = a/2\ell$: they are generated by the multiple foldings of

the energy band in the first Brillouin zone by the effective stripe potential $V_\sigma(\mathbf{R})$. Figure 1 also shows shadow bands — weak features of the Fermi surface created by the local doubling of the unit cell in the regions between the stripes.

In Fig. 2, the spectral density A_- is shown for $\ell/a = 10$ at $x = \frac{1}{20}$ doping to demonstrate the diminishing effect of the energy gaps when the periods of the stripe order and the underlying lattice are commensurate of a high rational fraction. Here, $\xi_c = 4a$ and $\xi_s = 8a$ in order to have a smooth spin wave. Interestingly, the shadow band circling the Γ point is very clear.

The condition of half-filled stripes, $x/2\epsilon = \frac{1}{2}$, yields an enhanced density of states at Fermi energy. This feature is clearly seen in Figs. 1(b) and 2(b).

B. A disordered stripe phase

In order to describe superconducting materials, we now consider a quenched random distribution of stripes [16], which should give essentially the correct band structure [17] for slow collective charge dynamics. With $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+x}$ in mind, we chose 15% doping and a mean stripe separation $\ell/a = 4$. The ensemble of stripe locations was constructed by taking $x_{n+1} - x_n = \ell + \delta$, where the random variable δ is uniformly distributed between $-3a$ and $3a$, which destroys long-range charge and spin order. The spectral density was averaged over five realizations, and we assumed a non-zero temperature, $k_B T = t/10$, which further diminishes finite size effects. We have found that the results do not depend markedly on the choice of ensemble, or the parameters in the effective potential and that the large lattices used in the calculation (linear dimension 184 sites) are essentially self-averaging. In other words, our results are robust consequences of a disordered stripe array, and are largely independent of other details. (We have not investigated the effects of orientational disorder.)

Figure 3 summarizes shows the \mathbf{k} -dependence of the spectral density at the Fermi energy, and the quasi-electron dispersion along the line $\Gamma\text{-}\bar{M}_1\text{-X/Y}$ for a single, extended domain, with disordered vertical stripes (running in the $\Gamma\text{-}\bar{M}_2$ direction). Stripe disorder has removed the fine details from the Fermi surface [Fig. 3(a)] which now closely resembles experiments. [2,4]. In particular, near \bar{M}_1 , there is a high density of states and a truly flat “band” at the Fermi energy, extending towards the Γ and X/Y points; see Fig. 3(b) and (c). The flatness along the $\Gamma\text{-}\bar{M}_1$ line is a consequence of both the smearing of the energy gap structure of the ordered system, and the localization of the electronic wave functions in the direction perpendicular to the stripes. The spectral density of the shadow band is reduced so much that it no longer shows up although, on a logarithmic scale, A_- looks qualitatively like that of Ref. [3]. The effect of

vertical stripes at \bar{M}_2 is completely different: band narrowing in a direction parallel to the stripes leads to an open Fermi surface.

It is clear from the energy dependence of the spectral density that there are no well-defined quasiparticle features near the \bar{M}_1 point, which is consistent with a widely held view of the normal-state properties of the high-temperature superconductors [18]. This has profound implications for d.c. transport and other low-energy two-particle properties.

The van Hove singularities of the ordered stripe phase are broadened by disorder. As a result, the density of states $\mathcal{N}(\epsilon_F)$ at the Fermi energy remains enhanced even for $x/2\epsilon = \frac{3}{5}$, because it is less sensitive to small variations in doping concentration; see Fig. 3(d).

IV. OPTICAL CONDUCTIVITY

Finally, consider the real part of the optical conductivity at non-zero energy,

$$\sigma'_{\alpha\alpha}(\omega) = \frac{1 - e^{-\hbar\omega/k_B T}}{2\omega} \int_{-\infty}^{\infty} dt e^{i\omega t} \langle j_{\alpha}(t) j_{\alpha}(0) \rangle, \quad (3)$$

where $j_{\alpha}(t)$ ($\alpha = x, y$) is the current operator of wave vector $\mathbf{q} = 0$ in the Heisenberg presentation [19]. Figure 4 illustrates the optical conductivity for an ordered array of vertical stripes. Transitions from and to the stripe-induced mid-gap states contribute to the pronounced peak at $\hbar\omega \gtrsim t$, while the other transitions yield only a weak feature at $\hbar\omega \sim .3t$.

Disordering the stripes destroys the momentum conservation in the perpendicular direction to the stripes. One consequence of this that the spectral features in the optical conductivity, shown in Fig. 5, are broadened; there is a rather small weight in the Drude component, so most of the oscillator strength appears as a broad continuum, extending to zero energy and centered in the neighborhood of $\hbar\omega \sim t$. This property is related to the absence of well-defined quasiparticle features near the \bar{M}_1 point, as indicated already by the behavior of the spectral density $A_{-}(\mathbf{k}, \epsilon)$ near the Fermi energy ϵ_F .

V. DISCUSSION

In summary, ordered stripe phases have been observed by neutron scattering in non-superconducting $\text{La}_{1.6-x}\text{Nd}_{0.4}\text{Sr}_x\text{CuO}_4$, and there is strong evidence for disordered and/or fluctuating stripes in $\text{La}_{2-x}\text{Sr}_x\text{CuO}_{4-\delta}$. Here we have shown that disordered, or slowly fluctuating stripes in $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+x}$ provide a natural explanation for the unusual features of the ARPES data, including the shape of the Fermi surface and the regions of flat bands. It is reasonable to

re-examine other experiments on the high-temperature superconductors to see whether they can be better understood in terms of the properties of extended domains with short-ranged stripe order.

Charged stripes are easily pinned by disorder and, at moderate temperatures, they form an essentially quenched-disordered array, which divides the Cu-O plane into long thin regions, with weak antiphase coupling between the intervening hole-deficient regions. This provides natural interpretation of NMR experiments [20] which see two distinct species of Cu nuclei; in our picture, one is in a pinned stripe, the other between the stripes. The fact that the coupling between spin domains is potentially frustrating provides a microscopic justification for the "cluster-spin-glass" phase in samples with $x < 15\%$ [21]. Moreover the creation of dilute metallic stripes can account for the rapid suppression of the Néel temperature for $x < 2\%$ [22].

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- [16] In principle, a superconducting material could have an ordered array of stripes. However, there is no long-range magnetic order in $\text{La}_{2-x}\text{Sr}_x\text{CuO}_{4-\delta}$ and no evidence of charge order in $\text{La}_{2-x}\text{Sr}_x\text{CuO}_{4-\delta}$ or $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+x}$. Consequently it is appropriate to assume disordered stripes in calculating the band structure. The agreement with experiment indicates that this is a realistic assumption.
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FIG.1 (a) The spectral density A_- in the first Brillouin zone integrated over an energy window $\Delta\epsilon = t/30$ about ϵ_F and (b) the density of states $\mathcal{N}(\epsilon)$ as a function of energy ϵ for an ordered array of vertical stripes of period $\ell = 4a$ with $\frac{1}{8}$ doping. The size of a circle, denoting a Fermi-surface crossing at a given value of k , shows the relative magnitude of $A(k, \epsilon_F)$. The parameters specifying the effective potential are $\rho_0 = -t/2$, $S_0 = 2t$, $\xi_c = a$, and $\xi_s = 2a$.

FIG.2 (a) The spectral density A_- in the first Brillouin zone integrated over an energy window $\Delta\epsilon = t/30$ about ϵ_F and (b) the density of states $\mathcal{N}(\epsilon)$ as a function of energy ϵ for an ordered array of vertical stripes of period $\ell = 10a$ with $\frac{1}{20}$ doping. The size of a circle, denoting a Fermi-surface crossing at a given k , shows the relative magnitude of $A(k, \epsilon_F)$. The parameters specifying the effective potential are $\rho_0 = -t/2$, $S_0 = 2t$, $\xi_c = 4a$, and $\xi_s = 8a$.

FIG.3 (a) The spectral density A_- in the first Brillouin zone integrated over an energy window $\Delta\epsilon = t/30$ about ϵ_F , (b) the dispersion relation, (c) the corresponding spectral density of the highest-energy occupied “band” as a function of k along the $\Gamma\text{-}\bar{M}_1\text{-X/Y}$ line, and (d) the density of states $\mathcal{N}(\epsilon)$ as a function of energy ϵ . The band is determined by broadening the energy δ -functions by a Lorentzian of the full width of $t/4$ at half maximum and finding the highest-energy maximum of A_- . The results are for a disordered array of vertical stripes with the mean separation of $\ell = 4a$ with 15 % doping at the temperature $k_B T = t/10$. The rest of the parameters are $\rho_0 = -t/2$, $S_0 = 2t$, $\xi_c = a$, and $\xi_s = 2a$.

FIG.4 The real (absorptive) part of the optical conductivity $\sigma'_{\parallel,\perp}(\omega)$ perpendicular (solid line) and parallel (dashed line) to an ordered array of vertical stripes with the separation of $\ell = 4a$ at $\frac{1}{8}$ doping at zero temperature. The stripe configuration and the parameters are the same as in Fig. 1.

FIG.5 The real (absorptive) part of the optical conductivity $\sigma'_{\parallel,\perp}(\omega)$ perpendicular (solid line) and parallel (dashed line) to a disordered array of vertical stripes with the mean separation of $\ell = 4a$ at 15 % doping at zero temperature. The stripe ensemble and the parameters are the same as in Fig. 3.

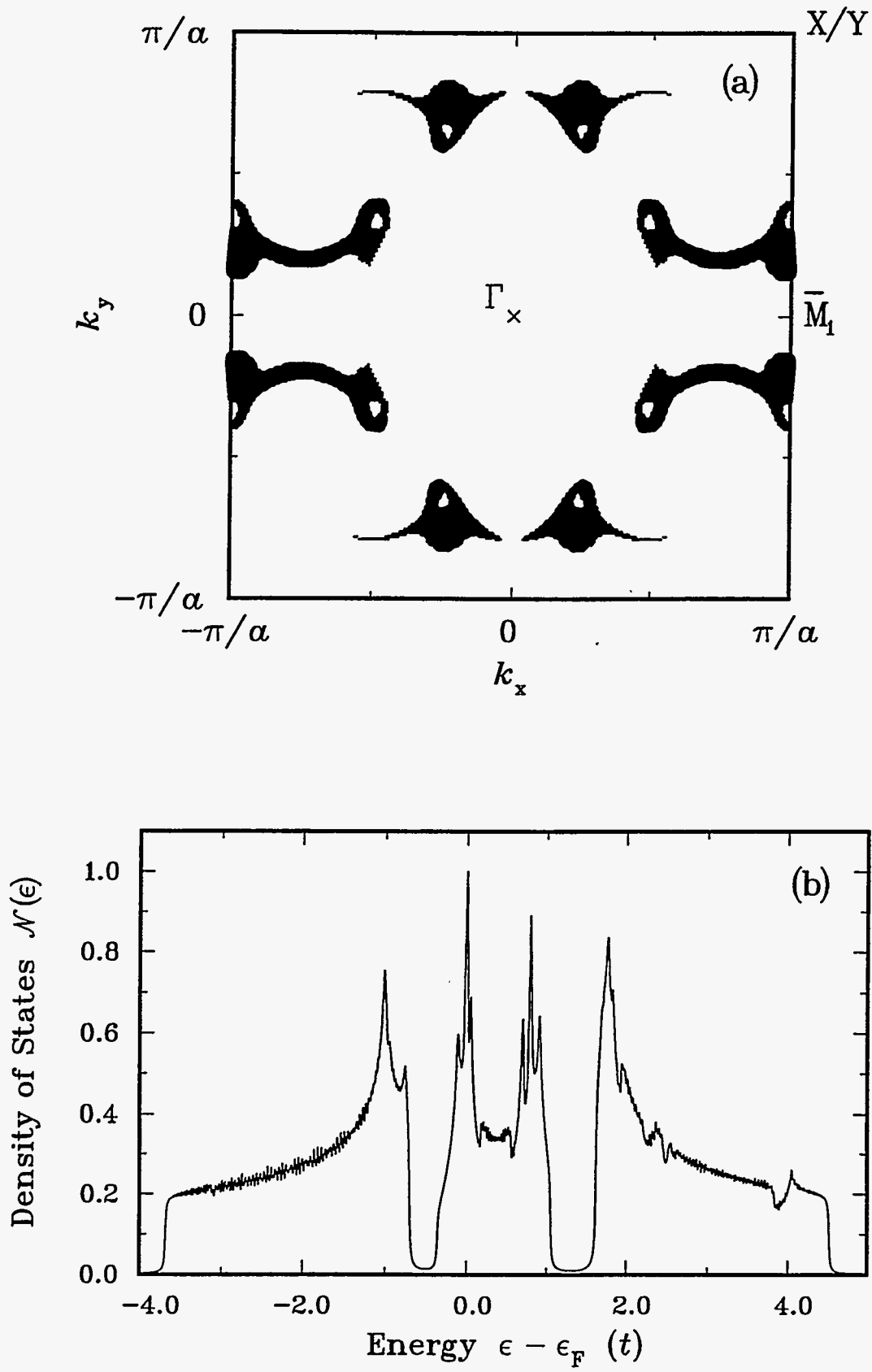


Fig. 1

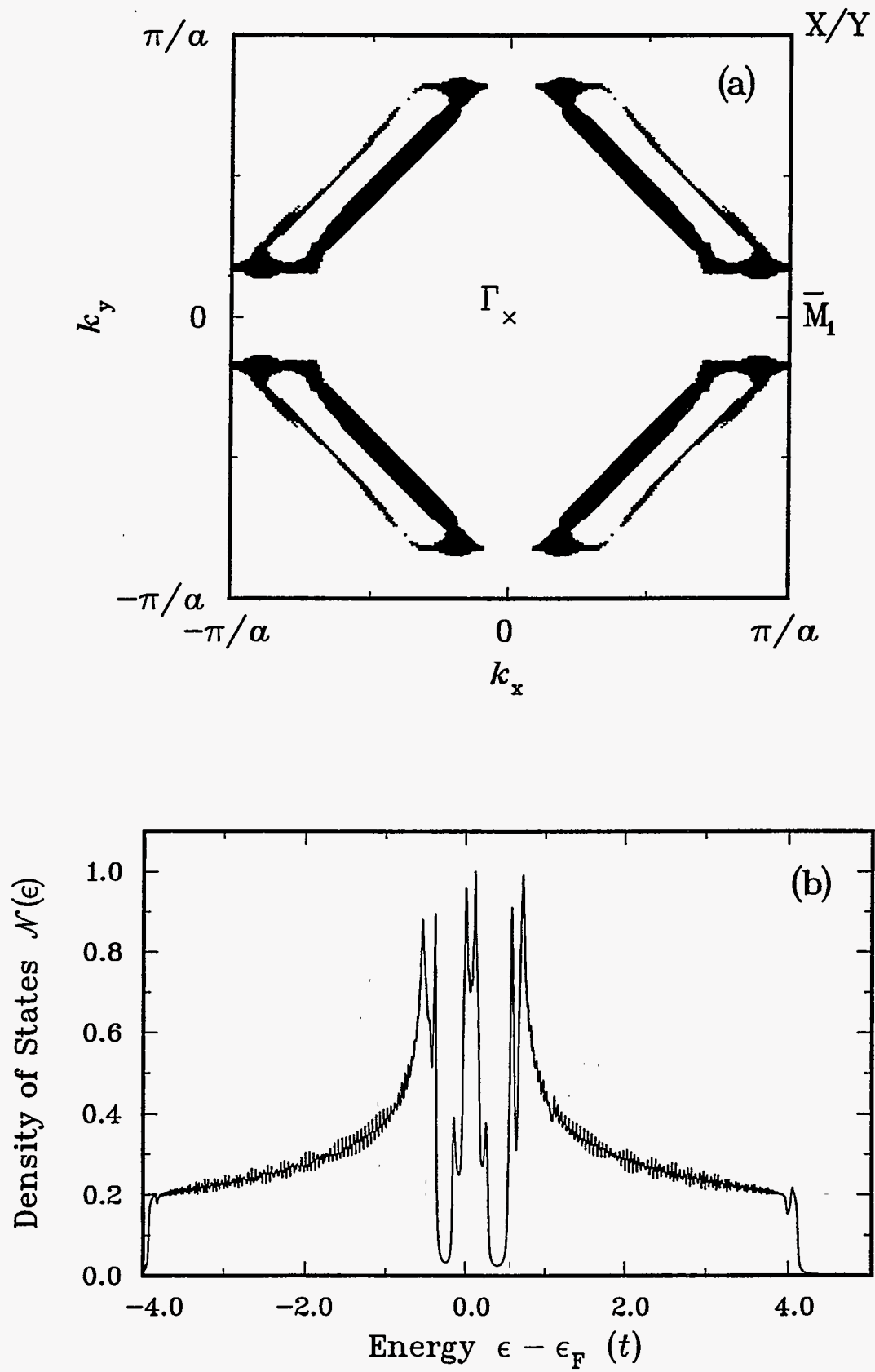


Fig. 2

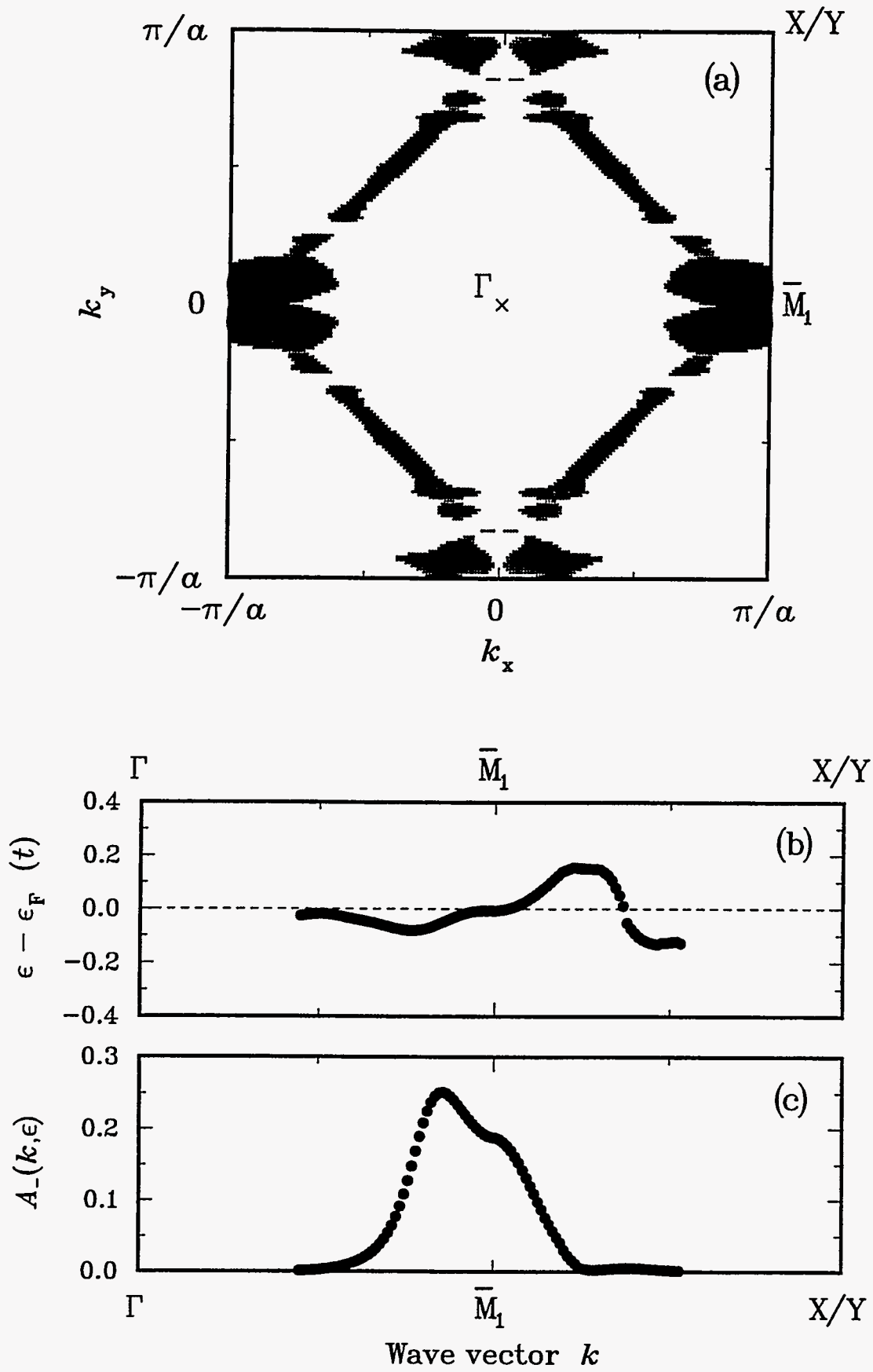


Fig. 3

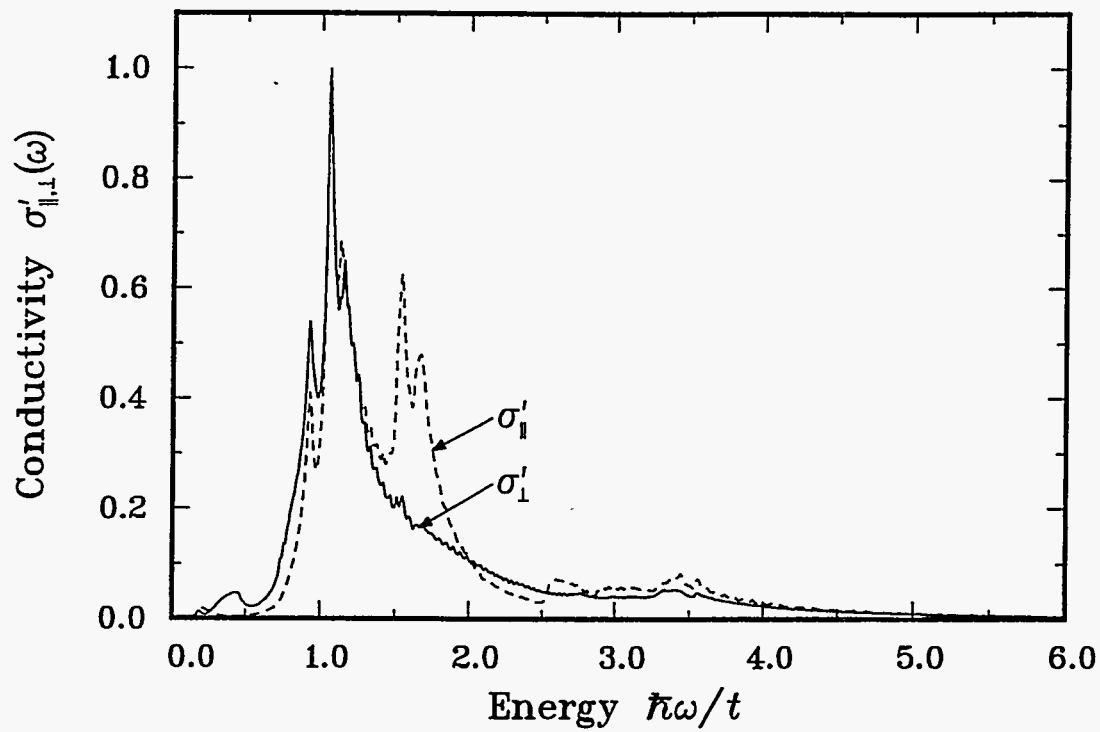


Fig. 4

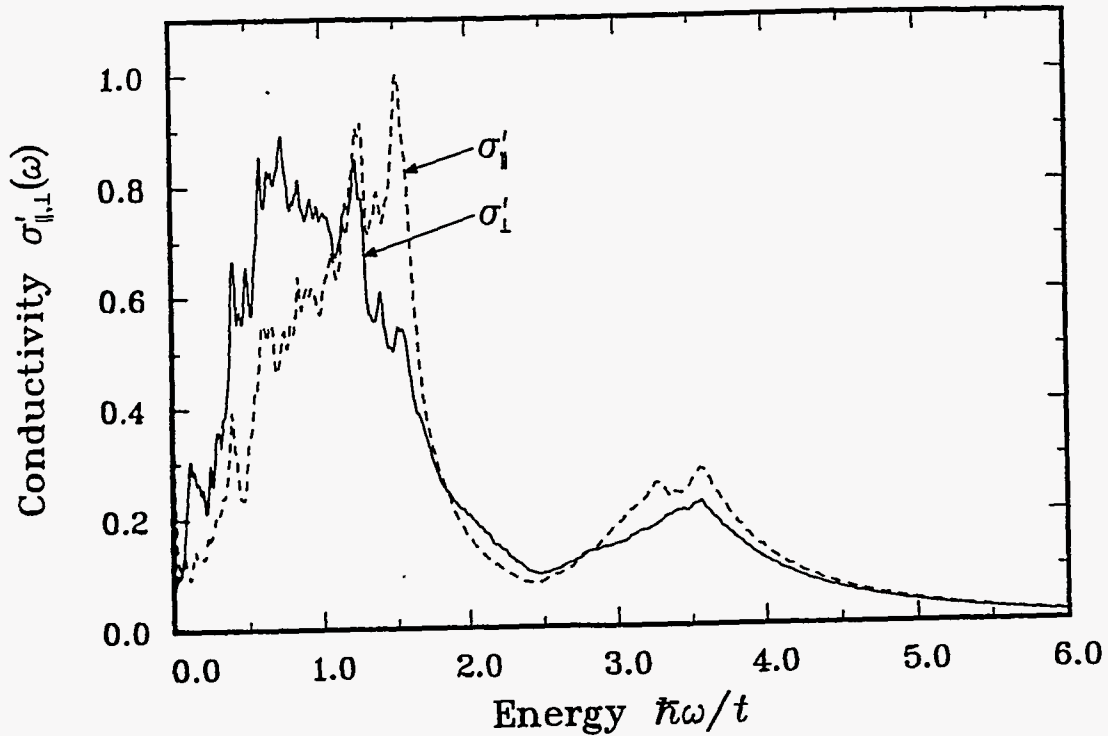


Fig. 5

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