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THE CRYSTAL AND MOLECULAR STRUCTURE  
OF 2,2'BIPYRIDYLGLYCINATOCHLORO  
COPPER(II) DIHYDRATE

THESIS

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By

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The three-dimensional x-ray structure of 2,2'-bipyridyl-glycinatochloro copper(II) dihydrate has been fully refined to a final R factor of 0.081. The bipyridyl and glycine ligands are arranged about the central copper atom in a square planar configuration while the chlorine atom is 2.635 angstroms above this plane directly over the copper atom. This unusually long distance is explained by the positioning of a glycine group on the opposite side of the square plane, resulting in a distorted octahedral arrangement. Also, the chlorine atom is linked to three oxygen atoms via hydrogen bonding, thus stabilizing the distorted octahedral complex.

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## CHAPTER I

### INTRODUCTION

It has been known for some time (8) that  $3d^9$  copper(II) octahedral and square planar complexes undergo considerable Jahn-Teller (9) distortions. These distortions produce respectively distorted octahedral and distorted tetrahedral structures (1). Dutta and associates observed that the magnetic moments of several  $3d^9$  copper(II) heterochelates in aqueous solution are approximately 1.90 Bohr Magnetons (5), indicating the presence of an unpaired electron (4, p. 537).

2,2'-Bipyridylglycinatochloro copper(II) dihydrate (BPGC) absorbs at  $16,940(5)^*$  to  $15,880(5)$   $\text{cm}^{-1}$  in the ultra-violet region (5, p. 354). For a system with one free electron in its d orbitals, transitions in the ultraviolet region are expected to peak out at a wave-number of approximately 10,000 (4, p. 572). This is true also of the  $d^9$  system. The absorption band of copper(II) in aqueous media is complex and the bands tend to consist of many peaks over a rather scattered range, which is indicative of Jahn-Teller distorted systems (2; 4, p. 572). Most copper(II) compounds

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\*Here and elsewhere in this manuscript, the standard error or estimated deviation will be specified in parenthesis following the parameter value. The digits of this number correspond to the least-significant digits of the parameter.

exhibit such extreme distortions that they are best described as distorted square planar. The distortions most frequently occur along the  $dz^2$  axis (6, p. 322).

A comparison of some copper(II) pyridine bonded systems is shown in Table I. It should be noted that the square planar and octahedral complexes are distorted. Huheey has compiled a table of bond distances for Jahn-Teller distorted copper(II) complexes, part of which is shown in Table II (7, p. 325). From the table, it can be seen that, for octahedral distorted structures, certain bond lengths differ dramatically. These deviations could be, in some cases, explained by arguments consistent with the Jahn-Teller theorem.

Using this information, it is possible to say tentatively that BPGC will be distorted from an octahedral or tetrahedral structure. Merritt found that short hydrogen-hydrogen contacts produced steric interaction, thereby resulting in distortions (11). The bonding sights for dipyridine in all cases observed have been at the nitrogen positions. The glycine molecule can bond at either oxygen or nitrogen positions, or both.

From this information, it is possible to obtain several chemically acceptable structures of BPGC. The crystal structure of this compound was attempted in order to observe



TABLE I  
 BOND LENGTHS (Å) AND COORDINATION STRUCTURE OF SOME  
 COPPER(II) COMPLEXES CONTAINING PYRIDINE

| Copper(II)<br>Coordination<br>Structure | Cu - N                   | Cu - O                   | Cu - Halide |
|---|--------------------------|--------------------------|-------------|
| Trigonal<br>Bipyramid (13)              | 2.04, 2.01<br>2.07, 1.99 | 2.30                     | -----       |
| Trigonal<br>bipyramid (17)              | 1.98, 2.11<br>2.07, 1.96 | 2.05                     | -----       |
| Trigonal<br>bipyramid ( 2)              | 2.03, 2.10<br>1.96, 2.00 | ----                     | 2.70        |
| Square<br>planar<br>distorted (15)      | 1.98, 1.98               | ----                     | 2.25        |
| Square<br>planar<br>distorted (15)      | 1.98, 1.98               | ----                     | 2.39        |
| Square<br>planar<br>distorted (16)      | 1.98, 1.98               | 1.99, 1.99               | -----       |
| Octahedral<br>distorted (12)            | 1.98, 2.02<br>1.97, 1.99 | 2.45, 2.73               | -----       |
| Octahedral<br>distorted ( 6)            | 1.98, 2.02               | 1.98, 1.95<br>2.40, 2.40 | -----       |
| Octahedral<br>distorted (10)            | 2.00, 2.00               | 1.92, 1.92<br>2.38       | -----       |
| Octahedral<br>distorted ( 3)            | 1.98, 1.98<br>2.03, 2.03 | 2.72, 2.72               | -----       |

TABLE II  
METAL-LIGAND DISTANCES OF SOME  
COPPER(II) COMPLEXES\*

| Compound   | Short Distances (Å) |      |      | Long Distances (Å) |
|--|---------------------|------|------|--------------------|
|  | Cu-Cl               | Cu-O | Cu-N | Cu-Cl              |
| CuCl <sub>2</sub>                                    | 2.30                |      |      | 2.95               |
|  | 2.30                |      |      | 2.95               |
|  | 2.30                |      |      |                    |
|  | 2.30                |      |      |                    |
| CsCuCl <sub>3</sub>                                  | 2.30                |      |      | 2.65               |
|  | 2.30                |      |      | 2.65               |
|  | 2.30                |      |      |                    |
|  | 2.30                |      |      |                    |
| CuCl <sub>2</sub> · 2H <sub>2</sub> O                | 2.28                | 1.93 |      | 2.95               |
|  | 2.28                | 1.93 |      | 2.95               |
| CuCl <sub>2</sub> · 2C <sub>5</sub> H <sub>5</sub> N | 2.28                |      | 2.02 | 3.05               |
|  | 2.28                |      | 2.02 | 3.05               |
| Cu(NH <sub>3</sub> ) <sub>2</sub> Cl <sub>2</sub>    |                     |      | 1.95 | 2.78               |
|  |                     |      | 1.95 | 2.78               |
|  |                     |      |      | 2.78               |
|  |                     |      |      | 2.78               |

\*Table from Huheey (7)

effects of Jahn-Teller distortions on the copper coordination as well as the types, if any, of hydrogen bonding.

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## CHAPTER II

### EXPERIMENTAL

Deep blue, long prismatic crystals of BPGC (1) were obtained from A. Syamal of the Department of Chemistry, North Texas State University, Denton, Texas. The crystals were recrystallized in a slightly basic aqueous solution in order to reduce the crystalline size to a suitably small size for the General Electric manual diffractometer. Flo-tation methods indicated a crystal density of approximately  $1.55 \text{ g cm}^{-3}$ . Using four molecules per unit cell, the actual calculated density is  $1.665 \text{ g cm}^{-3}$ . These crystals were examined with the aid of a polarizing microscope, and several optically suitable crystals were selected. Single oscillation photographs revealed, after several tried, a non-twinned crystal. The crystal chosen was approximately  $0.30 \times 0.42 \times 0.25 \text{ mm}$  in size. The crystal was mounted along the long axis, later designated as the b axis, in an effort to minimize absorption problems. From the oscillation and Weissenberg photographs, the cell geometry was determined to be monoclinic. It was determined from the systematic absences of reflections,

Ok0 absent when k is odd,

h0l absent when l is odd,

that the unit cell is of the centric space group  $P2_1/c$  (3). Easy alignment on the General Electric XRD manual diffractometer was possible due to the fact that the crystal was mounted along the b axis giving a plane of reflection at a chi ( $\chi$ ) of  $90^\circ$  and any setting of phi ( $\phi$ ).

Using cell constants calculated from Weissenberg photographs, preliminary settings of two-theta ( $2\theta$ ),  $\chi$ , and  $\phi$  were calculated for twelve reflections in the  $2\theta$  range of between  $0.00^\circ$  and  $23.00^\circ$ . The intensities were maximized for these reflections, none of which were in the zero layer, and the settings of  $\chi$ ,  $\phi$ , and  $2\theta$  were recorded. Subsequently, these settings were used to refine the unit cell constants through a least squares fit of the original settings to the settings calculated from the indices. These results are shown in Table III.

Using the unit cell constants thus obtained, a new set of reflection settings was generated to a  $2\theta$  of  $60^\circ$ . Intensity data were collected, using the peak height method. Molybdenum  $K\alpha_1$  radiation ( $\lambda = 0.70926 \text{ \AA}$ ) was used with a zirconium filter. The x-ray tube was operated at 40,000 volts and twenty milliamps. The takeoff angle on the x-ray tube was  $2.00^\circ$ . Originally, data were taken using a forty second peak top count and two background counts of twenty seconds each. This procedure was modified to a twenty second peak top count and ten second background counts after approximately twenty percent of the data had been

TABLE III  
THE EXPERIMENTAL AND CALCULATED CELL CONSTANTS  
FOR THE MONOCLINIC UNIT CELL OF BPGC

| Cell Constants | Film Data | Least Squares Fit Data |
|----------------|-----------|------------------------|
| A              | 10.473 Å  | 10.474(3) Å            |
| B              | 18.525    | 18.507(13)             |
| C              | 7.723     | 7.724(6)               |
| $\beta$        | 103.87°   | 103.918(59)°           |

taken. This modification was made due to the excessive time being consumed in data collection. Initially, the (800) reflection was used as a standard. When counting time was reduced, it was decided to add a thicker zirconium filter. This modification reduced the (800) standard to below 1000 counts per twenty second timing period; therefore, a new standard, the (830) reflection was chosen. The standard was measured at the end of each fifteen intensity collections. When the standard reflection intensity began to fluctuate over ten percent, data collection was stopped for that day under the assumption that the diffractometer power supply stability was beginning to vary with increasing temperature. All data were collected using the same crystal.

The raw data were interpolated between standards and then corrected for peak spreading as  $2\theta$  increased. The

constants used to account for peak spreading were empirically determined by graphing as the abscissa,

$$\frac{\text{SCANNED INTENSITY} - 6(\text{FIXED BACKGROUND})}{\text{FIXED INTENSITY} - \text{FIXED BACKGROUND}}$$

and  $2\theta$  as the ordinate for numerous reflections along the entire  $2\theta$  range. A least squares best line was drawn through these points and the constant values taken from this line. This graph is shown in Figure 1. There were initially 3649 reflections, ranging through a  $2\theta$  of  $55^\circ$ .

The data thus obtained were multiplied by 0.9 to minimize computation errors. The resultant intensities,  $I_{\text{obs}}$ , were corrected for Lorentz and polarization effects (6, p. 196), which led to the observed structure factor,  $F_{\text{obs}}$ , for each hkl reflection. The structure factors were put on an absolute basis by the equation,

$$|F_{\text{abs}}| = K |F_{\text{obs}}|$$

where  $K$  is the scale factor calculated by the statistical methods of Wilson (5) and  $|F_{\text{abs}}|$  is the observed structure factor scaled to an absolute basis. In the Wilson method, a value for  $K$  is obtained from the equation,

$$\ln \frac{I_{\text{obs}}}{\sum f_{o_i}} = \ln \frac{1}{K^2} - \frac{2B \sin^2 \theta}{\lambda^2}$$

where  $B$  is the overall isotropic temperature factor and  $f_{o_i}$  is the atomic scattering factor for the  $i$ th atom. This latter quantity is summed over all  $N$  atoms in the unit cell.  $B$  and  $K$  are determined from the slope and intercept,



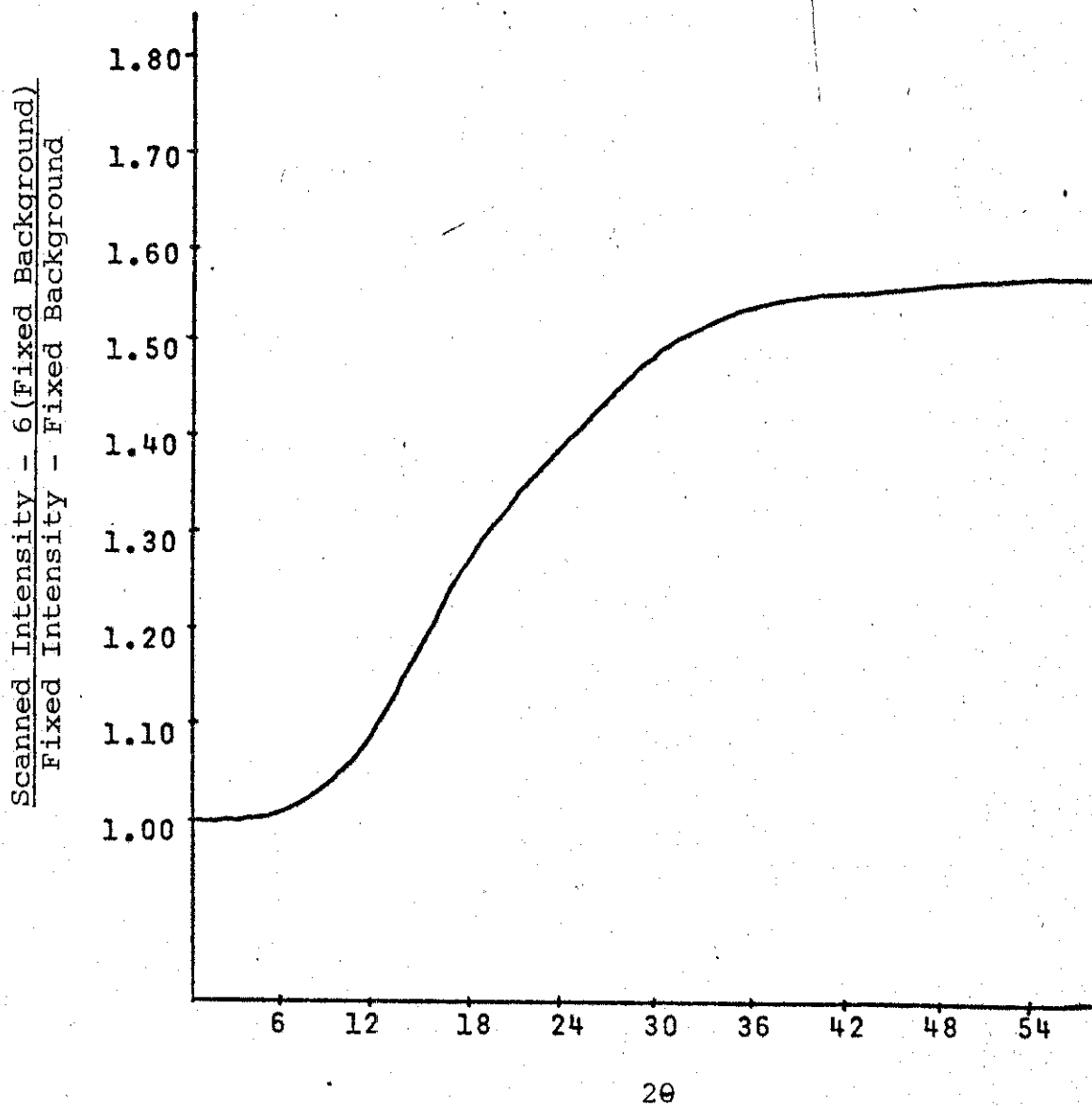


Fig. 1--Graph of correction constants for BPGC used to correct for peak spreading as  $2\theta$  increases.

respectively, of the Wilson plot. The values of B and K were found to be  $3.20 \text{ \AA}^2$  and 0.7645, respectively.

Normalized structure factors, E's, were computed according to the equation (5),

$$E = \frac{KF_{\text{obs}} \exp [B(\sin\theta/\lambda)^2]}{\epsilon \sum_{i=1}^N f_{\alpha_i}^2}$$

The factor  $\epsilon$  is a statistical factor determined by symmetry which allows for the fact that reflections which are systematically absent have average intensities which are integral multiples of the average of the general reflections (6). For the space group  $P2_1/c$ ,  $\epsilon$  is equal to two for  $h0l$  and  $0k0$  reflections, and equal to one for all other reflections. The experimental values for the E distribution are found in Table IV. This again confirms the centric space group.

TABLE IV

THE EXPERIMENTAL DISTRIBUTION OF E VALUES FROM  
DIFFRACTOMETER INTENSITY DATA FOR BPGC  
COMPARED WITH THE THEORETICAL CENTRIC  
AND ACENTRIC DISTRIBUTIONS

| E Value<br>Distribution                     | Experimental | Theoretical<br>(Centric) | Theoretical<br>(Acentric) |
|---|--------------|--------------------------|---------------------------|
| Average magnitude of E                      | 0.814        | 0.798                    | 0.886                     |
| Average magnitude of $E^2$                  | 1.003        | 1.000                    | 1.000                     |
| Average magnitude of<br>( $E^2-1$ )         | 0.931        | 0.968                    | 0.736                     |
| Percentage of E values<br>greater than 1.00 | 32.86        | 32.00                    | 37.00                     |
| Percentage of E values<br>greater than 2.00 | 4.59         | 5.00                     | 1.80                      |
| Percentage of E values<br>greater than 3.00 | 0.26         | 0.30                     | 0.01                      |

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## CHAPTER III

### STRUCTURE DETERMINATION AND REFINEMENT

It has been shown that when a molecule possesses an atom which comprises approximately thirty percent of the total molecular weight of the molecule, heavy atom methods are preferred over a direct method solution. Heavy atom methods were used to determine the structure of BPGC due to the fact that the copper composition is approximately twenty-one percent.

At this point, in the absence of knowledge of the signs of the structure factors, it was not possible to deduce directly the actual positions of atoms contained within the unit cell. However, it is theoretically possible to deduce the interatomic vectors between the atoms. It has been shown by Patterson (1) that a Fourier synthesis, using the values of the observed structure factors squared, as Fourier coefficients, will produce a density map which yields the coordinates of the ends of these vectors according to the equation (1),

$$\rho(u, v, w) = \frac{1}{V} \sum_{h=-\infty}^{\infty} \sum_{k=-\infty}^{\infty} \sum_{l=-\infty}^{\infty} |F_{obs}(h, k, l)|^2 \cos 2\pi(hu + kv + lw).$$

Here,  $\rho(u, v, w)$  represents the magnitude of an interatomic vector peak at the point  $(u, v, w)$ . If one considers the

fact that groups of atoms are spherically symmetric (9), implying complete scattering, then the calculated structure factor has the equation

$$F_{\text{calc}} = \sum_{j=1}^N f_j \exp(2\pi i S \cdot r_j).$$

Here,  $r$  is the position vector of atom  $j$  and is mathematically defined as  $hx_j + ky_j + lz_j$ .  $S$  is the reciprocal lattice point at which the function is evaluated. One can derive the square for the structure factor by simply multiplying the factors together for the peak involved. For two atoms,  $j$  and  $k$ , the vectors  $r_j$  and  $r_k$  enter into the relation

$$|F_h|^2_{i,n} = \sum_{j=1}^N \sum_{k=1}^N f_j f_k \exp(2\pi i S \cdot (r_k - r_j)),$$

where  $|F_h|^2_{i,n}$  represents a structure in which "atoms" of scattering factors  $f_j f_k$  are located at  $r_k - r_j$  (10, p. 228).

In 1936, Harker showed that for three-dimensional Patterson maps certain symmetry related conveniences were present (4). These conveniences were restricted to structures possessing certain symmetry operators (10, p. 232). For the BPGC monoclinic system, the Harker sections correspond to the  $P2/m$  point group (7). The  $P2/m$  symmetry lacks the glide plane and screw axis required for  $P2_1/c$ .

Using Harker symmetry points, it was possible to find the copper coordinates, from which a set of structure

factors was calculated according to the equation (7)

$$F_{\text{calc}} = \sum_{j=1}^N f_j^0 \cos 2\pi (hx_j + ky_j + lz_j) \exp(-B \sin^2\theta/\lambda^2).$$

In the above equation,  $f_j^0$  is the atomic scattering factor at zero degrees kelvin for the  $j$ 'th atom and the exponential term is the temperature correction for isotropic vibration. The scattering power curves were obtained from the averaged set of scattering curves in the International Tables for X-ray Crystallography (7, pp. 216-227).

Having obtained the calculated structure factors ( $F_{\text{calc}}$ ) and the previously defined observed structure factors ( $F_{\text{obs}}$ ), it was possible to calculate the residual index (R). This index,

$$R = \frac{\sum_{i=1}^N \left| |F_{\text{obs}}| - |F_{\text{calc}}| \right|}{\sum_{i=1}^N |F_{\text{obs}}|}$$

where  $i$  represents an individual reflection and  $N$  represents the total number of reflections, is a measure of the reliability of a proposed structure solution. It has been shown (11, p. 372) that the theoretical statistical residual index should have the following values for centric and acentric random structures:

$$R_{\text{random,centric}} = 0.83$$

$$R_{\text{random,acentric}} = 0.59.$$

Using only the copper atom found from the Patterson

synthesis, the residual index was 0.568. This index value was below the theoretical random centric value.

This copper position was refined isotropically through a block diagonal least squares, minimizing the quantity

$$\sum_{h,k,l} w(h,k,l) ( |F_{\text{obs}}(h,k,l)|^2 - |k F_{\text{calc}}(h,k,l)|^2 )^2$$

where  $k$  is a factor scaling the  $F_{\text{calc}}$  to the  $F_{\text{obs}}$ . This method of refinement (4) allows the inclusion of "accidentally absent" reflections which are too weak for observation. Usually, the minimum observed structure factor can be estimated in the part of the spectrum where the reflection resides. Thus, in a centrosymmetric space group, such a  $P2_1/c$ , the expected observed structure factor for the reflection can be estimated as (1)  $0.5 F_{\text{obs min}}$  and its variance estimated as  $\alpha^2 = 0.08 F_{\text{obs min}}$ , where  $F_{\text{obs min}}$  is the minimum observable structure factor. In the above equation,  $w$  is represented as  $w = \alpha^{-2} = 12 / (F_{\text{obs min}})^2$ .

One cycle of least squares isotropic refinement produced calculated structure factors which were used to produce an electron density map, using the equation (6, p.

$$329) \quad \rho(x,y,z) = \frac{4}{V} \left( \sum_{h,k,l}^{k+1=2N} [A - B] + \sum_{h,k,l}^{k+1=2n+1} [D - C] \right)$$

where  $\rho(x,y,z)$  is the electron density at the point  $(x,y,z)$

and  $A = [F(h,k,l) + F(h,k,\bar{l})] \cos 2\pi hx \cos 2\pi ky \cos 2\pi lz$ ,

$B = [F(h,k,l) - F(h,k,\bar{l})] \sin 2\pi hx \cos 2\pi ky \sin 2\pi lz$ ,



$C = [F(h, k, l) - F(h, k, \bar{l})] \sin 2\pi hx \sin 2\pi ky \sin 2\pi lz$ , and

$D = [F(h, k, l) - F(h, k, \bar{l})] \cos 2\pi hx \sin 2\pi ky \sin 2\pi lz$ .

From the electron density map produced, two nitrogen and one oxygen atom were located. Subsequent isotropic least squares refinement produced more precise coordinates for these atoms which led to a residual index of 0.413. The electron density map produced from these coordinates revealed the positions of one oxygen atom and twelve carbon atoms. Once again, an isotropic least squares refinement was carried out and resulted in a new residual index of 0.28.

At this point, a difference Fourier map was calculated using the equation (12, p. 356)

$$\Delta \rho(x, y, z) = \frac{1}{V} \sum_h \sum_k \sum_l (F_{\text{obs}} - F_{\text{calc}}) \cos 2\pi (hx + ky + lz),$$

where  $\Delta \rho(x, y, z)$  represents the difference between the density calculated with the observed magnitudes and the trial structure (3, p. 198). This method revealed one more oxygen atom which, when included in an isotropic least squares cycle, lowered the residual index to 0.26.

At this point, six cycles of anisotropic block diagonal least squares calculations were performed on the structure resulting in a lowering of the residual index to 0.154. The calculated structure factor expression for anisotropic temperature factors is given in the expression

$$F_{\text{calc}_r} = \sum_r f_r^{\circ} \cos [2\pi (hx_r + ky_r + lz_r)] \exp(-C_r)$$

(12, p. 450), where  $C_r$  is defined as

$$C_r = B_{11}h^2 + B_{22}k^2 + B_{33}l^2 + 2B_{23}kl + 2B_{13}hl + 2B_{12}hk$$

for the  $r^{\text{th}}$  atom. In the above equation,  $f_r^0$  is the atomic scattering factor at zero degrees kelvin and the exponential term is a correction for the anisotropic thermal vibration.

Using the calculated and observed structure factors, a graph was constructed of  $\sin^2\theta$  verses relative index for all data collected. From the graph, it was possible to determine that the data were inconsistent above forty-five degrees in  $2\theta$ . The computer program used as an aid in generating Figure 2 is contained in the appendix.

Using the forty-five-degree cutoff point reduced the number of usable reflections to 1896. Seven cycles of anisotropic refinement reduced the residual index to 0.101. At this point, theoretical atomic positions for the hydrogen atoms were calculated for the rings, as well as the tetrahedral positions (3). The hydrogen atoms coordinated to the two free water oxygen atoms were not determined. The temperature factors for the hydrogen atoms were the same as those for the atoms to which they were coordinated; however, they remained fixed during refinement. The hydrogen atomic positions were included in the refinement, but were not allowed to vary. An additional three anisotropic refinements reduced the residual index to 0.091. With the change in the atomic positions of the non-hydrogen atoms,

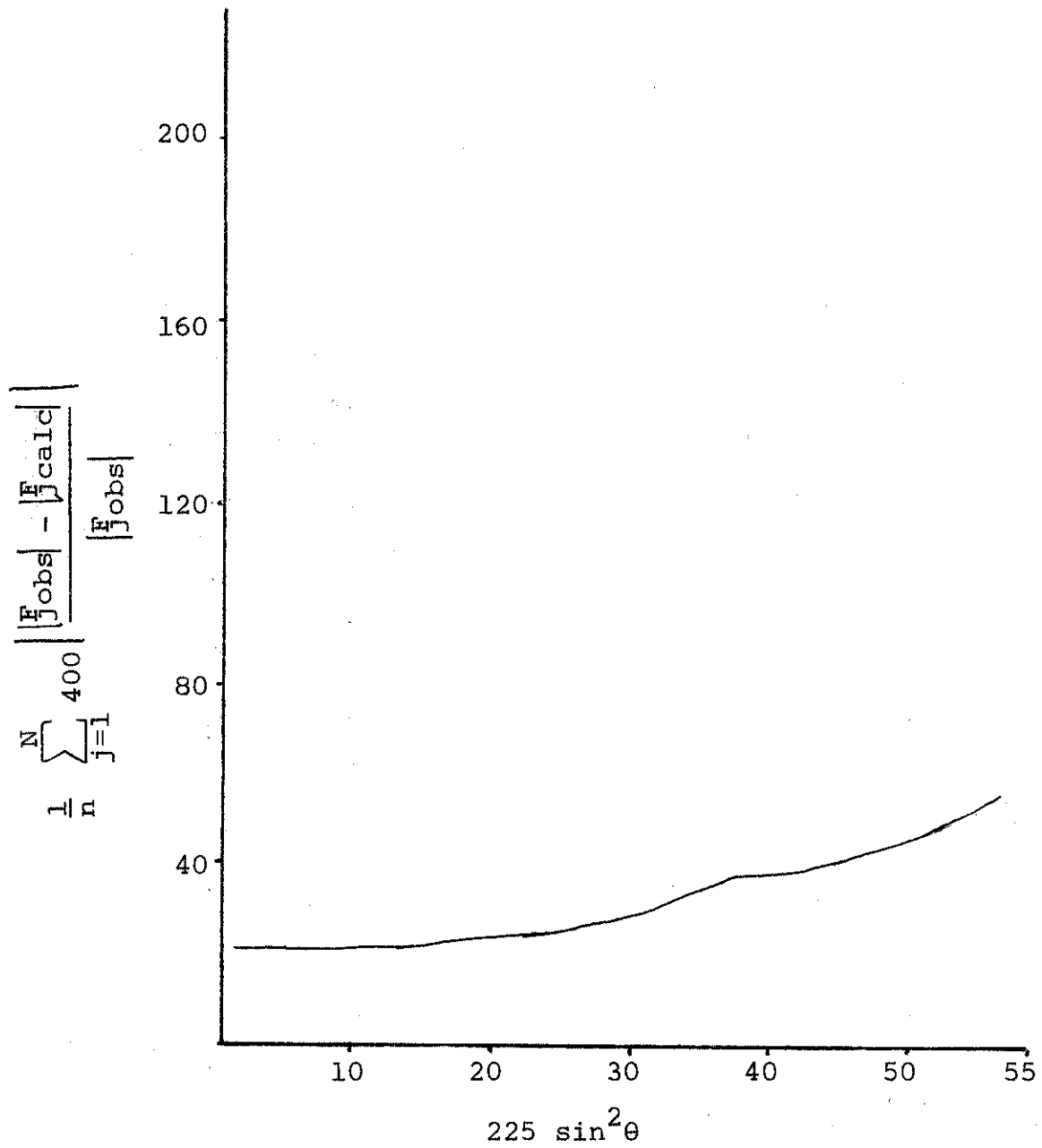


Fig. 2--The graph of relative index verses  $\sin^2 \theta$  required to choose a data cutoff point.

it was necessary to recalculate the hydrogen positions. Using these new hydrogen positions, one last structure factor calculation resulted in a final residual index of 0.081.

The final atomic and thermal parameters for BPGC are listed in Table V. A listing of the final observed and calculated structure factors for the 1896 reflections used is given in Table VI.

TABLE V

FINAL ATOMIC AND THERMAL PARAMETERS OF THE CRYSTAL STRUCTURE OF BPGC

| Atom   | Fractional Coordinates X 10 <sup>5</sup> |            |             |
|--------|--|------------|-------------|
|        | x  | y          | z           |
| Cu     | 13724 (14)                               | 8656 (8)   | 32998 (21)  |
| Cl     | 5819 (32)                                | 17508 (18) | 5809 (47)   |
| O (1)  | -1780 (69)                               | 2380 (69)  | 28201 (110) |
| O (2)  | 78371 (75)                               | 1034 (49)  | 33829 (118) |
| O (3)  | 26719 (90)                               | 38262 (50) | 35056 (127) |
| O (4)  | 85258 (113)                              | 25980 (64) | 22973 (154) |
| N (1)  | 24339 (81)                               | 1606 (47)  | 22446 (119) |
| N (2)  | 31456 (86)                               | 13577 (51) | 40760 (126) |
| N (3)  | 4982 (86)                                | 13920 (51) | 50080 (134) |
| C (1)  | 19540 (108)                              | -4250 (67) | 12910 (166) |
| C (2)  | 27740 (117)                              | -9400 (68) | 7340 (165)  |
| C (3)  | 41180 (121)                              | -7980 (71) | 11970 (177) |
| C (4)  | 46100 (106)                              | -0164 (68) | 21640 (169) |
| C (5)  | 37389 (104)                              | 2950 (62)  | 26473 (147) |
| C (6)  | 41289 (105)                              | 9932 (59)  | 36345 (148) |
| C (7)  | 54146 (105)                              | 12548 (67) | 40872 (169) |
| C (8)  | 56440 (112)                              | 19076 (70) | 48709 (181) |
| C (9)  | 46412 (127)                              | 22790 (69) | 52700 (187) |
| C (10) | 33925 (123)                              | 19946 (69) | 48396 (184) |
| C (11) | -8910 (115)                              | 11340 (67) | 46526 (194) |
| C (12) | -11260 (113)                             | 4446 (68)  | 35219 (164) |
| H (1)  | 90355                                    | 44903      | 40610       |
| H (2)  | 76044                                    | 35829      | 50127       |
| H (3)  | 84710                                    | 15540      | 39493       |
| H (4)  | 44128                                    | 49570      | 25017       |

TABLE V--Continued

| Atom  | Fractional Coordinates X 10 <sup>5</sup> |          |            | Z          |            |            |
|---|--|----------|------------|------------|------------|------------|
|   | X  | Y        | Z          |            |            |            |
| H (7)   | 61852                                    | 9295     |            | 38016      |            |            |
| H (8)   | 65667                                    | 21304    |            | 51808      |            |            |
| H (9)   | 48167                                    | 22052    |            | 9235       |            |            |
| H (10)  | 26414                                    | 23034    |            | 51348      |            |            |
| H (11)  | 88667                                    | 10271    |            | 59083      |            |            |
| H (11)  | 53499                                    | 38230    |            | 41857      |            |            |
| H (N)   | 9831                                     | 37206    |            | 13169      |            |            |
| H (N)   | 5177                                     | 30546    |            | -2040      |            |            |
| Anisotropic Temperature Factors X 10 <sup>5</sup> |  |          |            |            |            |            |
|   | B (1,1)                                  | B (2,2)  | B (3,3)    | B (1,2)    | B (1,3)    | B (2,3)    |
| Cu  | 387 (15)                                 | 172 (5)  | 1797 (35)  | 32 (16)    | 795 (36)   | -193 (25)  |
| Cl  | 905 (41)                                 | 198 (12) | 2166 (87)  | 19 (37)    | 961 (96)   | 156 (53)   |
| O (1)   | 353 (86)                                 | 226 (32) | 2410 (225) | -238 (86)  | 803 (222)  | -406 (138) |
| O (2)   | 487 (95)                                 | 376 (40) | 2723 (251) | -257 (102) | 1107 (250) | -366 (163) |
| O (3)   | 1368 (138)                               | 327 (40) | 2914 (272) | -35 (122)  | 2215 (317) | 77 (169)   |
| O (4)   | 2095 (195)                               | 568 (57) | 3770 (353) | 582 (180)  | 1114 (423) | 64 (237)   |
| N (1)   | 473 (106)                                | 149 (34) | 1451 (222) | 1 (99)     | 908 (250)  | -278 (142) |
| N (2)   | 505 (113)                                | 221 (39) | 1711 (242) | -108 (107) | 746 (265)  | -122 (157) |
| N (3)   | 507 (112)                                | 198 (38) | 2255 (267) | 11 (107)   | 999 (285)  | 527 (164)  |
| C (1)   | 452 (136)                                | 263 (51) | 2026 (328) | 110 (136)  | 682 (339)  | -47 (209)  |
| C (2)   | 905 (162)                                | 231 (50) | 1968 (324) | 47 (150)   | 1447 (372) | 168 (213)  |
| C (3)   | 934 (165)                                | 273 (53) | 2452 (359) | -197 (161) | 1883 (397) | 115 (233)  |
| C (4)   | 401 (134)                                | 259 (52) | 2162 (333) | -3 (135)   | 757 (341)  | -128 (211) |
| C (5)   | 485 (131)                                | 214 (46) | 1220 (265) | -11 (127)  | 722 (300)  | -13 (180)  |
| C (6)   | 647 (140)                                | 129 (41) | 1320 (267) | 66 (124)   | 446 (309)  | 310 (170)  |
| C (7)   | 257 (126)                                | 252 (49) | 2295 (327) | -114 (128) | 165 (322)  | 89 (207)   |

TABLE V--Continued

| Atom  | Anisotropic Temperature Factors X 10 <sup>5</sup> |          |            |            |            |             |
|-------|---|----------|------------|------------|------------|-------------|
|       | B(1,1)  | B(2,2)   | B(3,3)     | B(1,2)     | B(1,3)     | B(2,3)      |
| C(8)  | 475 (142)   | 279 (55) | 2634 (373) | -274 (145) | 288 (368)  | -282 (232)  |
| C(9)  | 1012 (181)  | 204 (52) | 2742 (388) | 402 (157)  | 1034 (424) | 457 (228)   |
| C(10) | 910 (171)   | 242 (53) | 2796 (387) | -292 (152) | 1447 (417) | -1148 (234) |
| C(11) | 607 (146)   | 275 (53) | 1691 (310) | 194 (144)  | 313 (336)  | 115 (208)   |
| C(12) | 611 (153)   | 193 (48) | 3731 (444) | -12 (138)  | 2001 (427) | -397 (235)  |
| H(1)  | 726   | 219      | 1334       | .          | 473        | .           |
| H(2)  | 726   | 219      | 1334       | .          | 473        | .           |
| H(3)  | 726   | 219      | 1334       | .          | 473        | .           |
| H(4)  | 726   | 219      | 1334       | .          | 473        | .           |
| H(7)  | 726   | 219      | 1334       | .          | 473        | .           |
| H(8)  | 726   | 219      | 1334       | .          | 473        | .           |
| H(9)  | 726   | 219      | 1334       | .          | 473        | .           |
| H(10) | 726   | 219      | 1334       | .          | 473        | .           |
| H(11) | 726   | 219      | 1334       | .          | 473        | .           |
| H(11) | 726   | 219      | 1334       | .          | 473        | .           |
| H(N)  | 726   | 219      | 1334       | .          | 473        | .           |
| H(N)  | 726   | 219      | 1334       | .          | 473        | .           |

TABLE VI

FINAL OBSERVED AND CALCULATED STRUCTURE FACTORS FOR BPGC

| L  | FO    | FC    | L  | FO    | FC   | L  | FO    | FC   | L  | FO    | FC   | L  | FO    | FC   | L  | FO    | FC   |
|----|-------|-------|----|-------|------|----|-------|------|----|-------|------|----|-------|------|----|-------|------|
| M= | J, K= | 0     | M= | 0, K= | 7    | 1  | 520   | -527 | M= | 1, K= | 2    | -6 | 116   | -131 | M= | 1, K= | 10   |
|    |       |       |    |       |      | 2  | 21    | -44  |    |       |      | -7 | 102   | -117 |    |       |      |
| 2  | 153   | -113  | 1  | 168   | 145  | 3  | 187   | 172  | 0  | 325   | 266  |    |       |      | 0  | 74    | 32   |
| -4 | 219   | -135  | 2  | 775   | -718 | -4 | 64    | -60  | 1  | 224   | -158 | M= | 1, K= | 6    | M= | 1, K= | 10   |
| -6 | 278   | 251   | 3  | 367   | -371 | -5 | 222   | -228 | 2  | 190   | -176 |    |       |      |    |       |      |
| -8 | 60    | -56   | -4 | 200   | 118  |    |       |      | 3  | 531   | -433 |    |       |      | 0  | 117   | -62  |
| M= | 0, K= | L     | -5 | 380   | 342  | M= | 0, K= | 15   | 4  | 62    | -73  |    |       |      | 1  | 342   | -122 |
|    |       |       | -6 | 34    | 57   |    |       |      | 5  | 99    | 139  |    |       |      | 2  | 31    | -67  |
| 1  | 740   | -755  | -7 | 69    | 80   | 1  | 200   | -208 | 6  | 211   | 247  |    |       |      | 3  | 55    | -36  |
| 2  | 882   | 856   | M= | 0, K= | 8    | 2  | 404   | 393  | 7  | 127   | -144 |    |       |      | 4  | 568   | 533  |
| 3  | 682   | 630   |    |       |      | 3  | 250   | -257 | -1 | 1056  | 1113 |    |       |      | 5  | 24    | -39  |
| -4 | 455   | 412   | 0  | 268   | 261  | -4 | 196   | 181  | -2 | 357   | 364  |    |       |      | 6  | 255   | -278 |
| -5 | 403   | -356  | 1  | 95    | 35   | -5 | 107   | 112  | -3 | 337   | -305 |    |       |      | 7  | 71    | 66   |
| -6 | 191   | 164   | 2  | 383   | -345 | M= | 0, K= | 10   | -4 | 152   | -130 |    |       |      | -1 | 134   | 231  |
| -7 | 167   | -181  | 3  | 84    | -63  |    |       |      | -5 | 85    | 43   |    |       |      | -2 | 1446  | 1374 |
| -8 | 61    | -46   | -4 | 132   | 121  | 0  | 245   | -275 | -6 | 243   | 239  |    |       |      | -3 | 257   | 241  |
| M= | 0, K= | 2     | -5 | 336   | 501  | 1  | 271   | -291 | -7 | 308   | 238  |    |       |      | -4 | 593   | -533 |
|    |       |       | -6 | 112   | -112 | 2  | 309   | 299  | -8 | 61    | -60  |    |       |      | -5 | 20    | -5   |
| 0  | 1000  | 1096  | -7 | 176   | -177 | 3  | 136   | 143  | M= | 1, K= | 3    |    |       |      | -6 | 133   | -135 |
| 1  | 1037  | -1148 |    |       |      | -4 | 37    | 37   |    |       |      |    |       |      | -7 | 20    | 33   |
| 2  | 1383  | -1560 | M= | 0, K= | 9    |    |       |      | 0  | 713   | -647 | M= | 1, K= | 7    |    |       |      |
| 3  | 294   | -280  |    |       |      |    |       |      | 1  | 758   | -738 |    |       |      | 0  | 359   | 306  |
| -4 | 421   | -380  | 1  | 705   | -635 | M= | 0, K= | 17   | 2  | 984   | 1087 |    |       |      | 1  | 570   | 543  |
| -5 | 131   | -92   | 2  | 267   | -280 |    |       |      | 3  | 376   | 221  |    |       |      | 2  | 379   | -357 |
| -6 | 137   | 142   | 3  | 94    | -73  | 1  | 280   | 289  | 4  | 309   | -305 |    |       |      | 3  | 354   | -341 |
| -7 | 231   | 216   | -4 | 449   | -414 | 2  | 59    | 64   | 5  | 33    | -12  |    |       |      | 4  | 520   | -431 |
| -8 | 26    | 26    | -5 | 9     | 1    | 3  | 230   | -249 | 6  | 115   | -131 |    |       |      | 5  | 406   | -376 |
| M= | 0, K= | 3     | -6 | 0     | -4   | -4 | 26    | -15  | 7  | 159   | 138  |    |       |      | 6  | 59    | 64   |
|    |       |       | -7 | 21    | 31   | M= | 0, K= | 13   | -1 | 743   | -733 |    |       |      | -1 | 581   | -570 |
| 1  | 359   | 378   |    |       |      |    |       |      | -2 | 637   | 646  |    |       |      | -2 | 173   | -167 |
| 2  | 1651  | 2057  | M= | 0, K= | 10   | 0  | 372   | -354 | -3 | 330   | -332 |    |       |      | -3 | 710   | -610 |
| 3  | 358   | 322   |    |       |      | 1  | 37    | 49   | -4 | 599   | 555  |    |       |      | -4 | 318   | -340 |
| -4 | 551   | 510   | 0  | 818   | 743  | 2  | 214   | 228  | -5 | 62    | 64   |    |       |      | -5 | 231   | 226  |
| -5 | 109   | 89    | 1  | 212   | 255  | 3  | 137   | -124 | -6 | 400   | -376 |    |       |      | -6 | 541   | 538  |
| -6 | 19    | 21    | 2  | 180   | -192 |    |       |      | -7 | 44    | 34   |    |       |      | -7 | 137   | -159 |
| -7 | 99    | 74    | 3  | 197   | 196  | M= | 0, K= | 19   | -8 | 37    | -53  |    |       |      |    |       |      |
| M= | 0, K= | 4     | -4 | 53    | -101 |    |       |      |    |       |      |    |       |      |    |       |      |
|    |       |       | -5 | 155   | 169  | 1  | 52    | 67   |    |       |      |    |       |      |    |       |      |
| 0  | 635   | -580  | -6 | 148   | 178  | 2  | 253   | -291 |    |       |      |    |       |      |    |       |      |
| 1  | 763   | -723  | M= | 0, K= | 11   |    |       |      |    |       |      |    |       |      |    |       |      |
| 2  | 954   | -934  |    |       |      |    |       |      |    |       |      |    |       |      |    |       |      |
| 3  | 771   | 759   | 1  | 187   | 155  | M= | 1, K= | 0    |    |       |      |    |       |      |    |       |      |
| -4 | 633   | 581   | 2  | 232   | 205  |    |       |      |    |       |      |    |       |      |    |       |      |
| -5 | 492   | -478  | 3  | 651   | 648  | 0  | 812   | 870  |    |       |      |    |       |      |    |       |      |
| -6 | 167   | -171  | -4 | 89    | -107 | 2  | 64    | -114 |    |       |      |    |       |      |    |       |      |
| -7 | 129   | 127   | -5 | 242   | -245 | 4  | 510   | -487 |    |       |      |    |       |      |    |       |      |
| M= | 0, K= | 5     | -6 | 116   | -106 | 6  | 169   | 182  |    |       |      |    |       |      |    |       |      |
|    |       |       |    |       |      | -2 | 433   | -361 |    |       |      |    |       |      |    |       |      |
| 1  | 370   | 348   | M= | 0, K= | 12   | -4 | 572   | 513  |    |       |      |    |       |      |    |       |      |
| 2  | 603   | 554   |    |       |      | -6 | 270   | 277  |    |       |      |    |       |      |    |       |      |
| 3  | 612   | -543  | 0  | 546   | 524  | -8 | 258   | -263 |    |       |      |    |       |      |    |       |      |
| -4 | 287   | 226   | 1  | 492   | -437 |    |       |      |    |       |      |    |       |      |    |       |      |
| -5 | 89    | 92    | 2  | 321   | -294 |    |       |      |    |       |      |    |       |      |    |       |      |
| -6 | 14    | -46   | 3  | 55    | 93   |    |       |      |    |       |      |    |       |      |    |       |      |
| -7 | 20    | -26   | -4 | 114   | -125 |    |       |      |    |       |      |    |       |      |    |       |      |
| M= | 0, K= | 6     | -5 | 102   | 85   |    |       |      |    |       |      |    |       |      |    |       |      |
|    |       |       | -6 | 151   | 166  |    |       |      |    |       |      |    |       |      |    |       |      |
| 0  | 359   | -285  | M= | 0, K= | 13   |    |       |      |    |       |      |    |       |      |    |       |      |
| 1  | 243   | -234  |    |       |      |    |       |      |    |       |      |    |       |      |    |       |      |
| 2  | 471   | 445   | 1  | 120   | -142 |    |       |      |    |       |      |    |       |      |    |       |      |
| 3  | 309   | 240   | 2  | 170   | 172  |    |       |      |    |       |      |    |       |      |    |       |      |
| -4 | 618   | 521   | 3  | 358   | 373  |    |       |      |    |       |      |    |       |      |    |       |      |
| -5 | 90    | 79    | -4 | 444   | 472  |    |       |      |    |       |      |    |       |      |    |       |      |
| -6 | 361   | -358  | -5 | 55    | -61  |    |       |      |    |       |      |    |       |      |    |       |      |
| -7 | 25    | 29    | -6 | 19    | 23   |    |       |      |    |       |      |    |       |      |    |       |      |
|    |       |       | M= | 0, K= | 14   |    |       |      |    |       |      |    |       |      |    |       |      |
|    |       |       |    |       |      |    |       |      |    |       |      |    |       |      |    |       |      |
|    |       |       | 0  | 228   | -214 |    |       |      |    |       |      |    |       |      |    |       |      |



TABLE VI--Continued

| L  | FO       | FC   | L  | FO      | FC   | L  | FO      | FC   | L  | FO       | FC   | L  | FO       | FC   | L  | FO      | FC   |
|----|----------|------|----|---------|------|----|---------|------|----|----------|------|----|----------|------|----|---------|------|
| 3  | 287      | -325 | M= | 2, K= 1 |      | M= | 2, K= 5 |      | 1  | 388      | -382 | M= | 2, K= 14 |      | L  | FO      | FC   |
| 4  | 56       | 63   |    |         |      |    |         |      | 2  | 319      | -306 |    |          |      | -9 | 11      | 55   |
| 5  | 84       | 75   | 0  | 359     | -319 | 0  | 373     | 309  | 3  | 91       | 137  | 0  | 197      | -159 | M= | 3, K= 1 |      |
| -1 | 544      | 560  | 1  | 413     | -393 | 1  | 1080    | 1041 | 4  | 264      | -244 | 1  | 271      | 261  |    |         |      |
| -2 | 260      | -263 | 2  | 506     | -517 | 2  | 261     | 245  | 5  | 123      | 142  | 2  | 195      | 175  | 0  | 351     | -366 |
| -3 | 252      | -246 | 3  | 47      | -70  | 3  | 356     | -317 | 6  | 255      | 264  | 3  | 317      | -333 | 1  | 201     | -178 |
| -4 | 94       | -115 | 4  | 78      | -58  | 4  | 229     | 237  | -1 | 332      | -324 | 4  | 18       | -12  | 2  | 408     | -420 |
| -5 | 14       | 38   | 5  | 172     | 162  | 5  | 443     | -443 | -2 | 608      | -568 | 5  | 47       | 53   | 3  | 433     | -455 |
| M= | 1, K= 15 |      | 6  | 152     | -185 | 6  | 10      | -19  | -3 | 406      | -388 | -1 | 85       | -76  | 4  | 132     | 140  |
| 0  | 311      | -329 | 7  | 176     | -197 | 7  | 115     | 135  | -4 | 235      | -219 | -2 | 325      | -309 | 5  | 220     | 255  |
| 1  | 72       | 77   | -1 | 160     | -128 | -1 | 136     | -130 | -5 | 92       | -108 | -3 | 259      | -256 | 6  | 29      | -56  |
| 2  | 466      | 461  | -2 | 364     | 303  | -2 | 23      | -71  | -6 | 31       | -15  | -4 | 76       | -5   | 7  | 26      | -10  |
| 3  | 151      | -121 | -3 | 30      | -5   | -3 | 508     | 452  | -7 | 66       | 42   | -5 | 199      | 229  | -1 | 917     | 902  |
| 4  | 26       | -15  | -4 | 396     | 359  | -4 | 309     | 292  | M= | 2, K= 10 |      | M= | 2, K= 15 |      | -2 | 40      | 16   |
| 5  | 0        | 16   | -5 | 359     | -347 | -5 | 276     | 274  | 0  | 140      | -134 | 0  | 405      | -473 | -3 | 492     | -479 |
| -1 | 265      | -293 | -6 | 70      | -87  | -6 | 242     | -45  | 1  | 93       | -119 | 1  | 66       | 85   | -4 | 243     | -277 |
| -2 | 52       | -64  | -7 | 260     | 262  | -7 | 203     | -199 | 2  | 360      | 365  | 2  | 265      | 263  | -5 | 281     | -240 |
| -3 | 98       | -114 | -8 | 122     | 161  | -8 | 89      | 97   | 3  | 536      | 531  | 3  | 14       | -19  | -6 | 57      | 32   |
| -4 | 70       | 89   | M= | 2, K= 2 |      | M= | 2, K= 7 |      | 4  | 265      | -262 | 4  | 130      | 118  | -7 | 279     | -270 |
| -5 | 42       | 67   | 0  | 639     | -596 | 0  | 465     | 437  | 5  | 34       | -7   | -1 | 115      | -121 | -8 | 174     | 180  |
| M= | 1, K= 18 |      | 1  | 497     | -464 | 1  | 9       | -14  | 6  | 35       | -19  | -2 | 195      | 194  | M= | 3, K= 2 |      |
| 0  | 117      | -142 | 2  | 209     | -186 | 2  | 793     | -750 | -1 | 117      | -98  | -3 | 193      | -179 | 0  | 495     | -452 |
| 1  | 36       | 60   | 3  | 846     | -836 | 3  | 89      | 105  | -2 | 405      | -387 | -4 | 160      | 175  | 1  | 272     | 243  |
| 2  | 29       | -21  | 4  | 88      | 76   | 4  | 401     | 398  | -3 | 387      | 353  | -5 | 64       | -58  | 2  | 289     | 232  |
| 3  | 93       | 95   | 5  | 168     | 193  | 5  | 137     | -181 | -4 | 225      | 214  | 0  | 0        | 47   | 3  | 615     | -635 |
| 4  | 162      | 141  | 6  | 7       | 15   | 6  | 120     | -125 | -5 | 518      | -493 | M= | 2, K= 16 |      | 4  | 277     | 263  |
| -1 | 389      | 414  | 7  | 90      | 98   | 7  | 42      | 36   | -6 | 43       | -69  | 0  | 423      | 477  | 5  | 125     | -124 |
| -2 | 248      | 269  | -1 | 160     | 95   | -1 | 319     | -279 | -7 | 76       | -109 | 1  | 109      | -111 | 6  | 74      | -75  |
| -3 | 232      | -261 | -2 | 569     | -593 | -2 | 1198    | 1166 | M= | 2, K= 11 |      | 2  | 13       | -1   | 7  | 216     | 236  |
| -4 | 102      | -120 | -3 | 179     | -229 | -3 | 115     | 141  | 0  | 486      | 460  | 3  | 61       | 80   | -1 | 657     | -641 |
| M= | 1, K= 17 |      | -4 | 139     | 78   | -4 | 263     | -249 | 1  | 187      | -186 | 4  | 13       | 0    | -2 | 609     | -624 |
| 0  | 125      | -138 | -5 | 545     | 504  | -5 | 170     | -137 | 2  | 100      | 78   | -1 | 23       | 7    | -3 | 702     | -676 |
| 1  | 545      | 591  | -6 | 78      | -97  | -6 | 95      | 84   | 3  | 26       | -57  | -2 | 301      | 320  | -4 | 392     | 374  |
| 2  | 29       | -14  | -7 | 177     | 162  | -7 | 21      | 6    | 4  | 72       | -64  | -3 | 202      | -223 | -5 | 747     | 711  |
| 3  | 91       | -84  | -8 | 24      | -27  | M= | 2, K= 7 |      | 5  | 158      | 138  | -4 | 112      | -141 | -6 | 354     | -368 |
| -1 | 45       | -42  | 0  | 834     | -873 | 0  | 273     | 249  | 6  | 143      | 146  | M= | 2, K= 17 |      | -7 | 29      | 13   |
| -2 | 0        | 14   | 1  | 490     | 491  | 1  | 650     | 630  | 7  | 158      | 138  | -5 | 34       | 30   | -8 | 34      | 30   |
| -3 | 119      | -124 | 2  | 296     | 311  | 2  | 567     | -516 | -1 | 856      | 824  | 0  | 159      | -178 | M= | 3, K= 3 |      |
| -4 | 73       | 65   | 3  | 51      | -64  | 3  | 88      | -57  | -2 | 18       | -14  | 1  | 186      | 206  | 0  | 135     | -154 |
| M= | 1, K= 18 |      | 4  | 203     | 176  | 4  | 423     | -406 | -3 | 22       | 36   | 2  | 38       | 56   | 1  | 119     | 115  |
| 0  | 45       | -90  | 5  | 166     | 167  | 5  | 285     | -273 | -4 | 87       | -72  | 3  | 0        | -7   | 2  | 353     | -337 |
| 1  | 165      | -193 | 6  | 195     | -214 | 6  | 206     | 215  | -5 | 64       | -48  | -1 | 69       | -95  | 3  | 217     | 194  |
| 2  | 39       | -32  | 7  | 149     | 169  | 7  | 95      | 98   | -6 | 48       | -39  | -2 | 26       | -38  | 4  | 447     | 425  |
| 3  | 28       | 27   | -1 | 450     | -459 | -1 | 689     | -667 | M= | 2, K= 12 |      | -3 | 153      | 167  | 5  | 31      | 16   |
| -1 | 94       | -127 | -2 | 587     | -522 | -2 | 587     | -522 | 0  | 46       | -6   | -4 | 93       | 94   | 6  | 172     | -167 |
| -2 | 332      | 363  | -3 | 155     | 166  | -3 | 155     | 166  | 1  | 124      | -151 | M= | 2, K= 18 |      | 7  | 112     | 124  |
| -3 | 161      | 197  | -4 | 82      | 72   | -4 | 82      | 72   | 2  | 637      | 599  | 0  | 71       | 81   | -1 | 329     | -336 |
| M= | 1, K= 19 |      | -5 | 129     | 124  | -5 | 129     | 124  | 3  | 314      | -321 | 1  | 23       | -42  | -2 | 1001    | 977  |
| 0  | 74       | 89   | -6 | 181     | 174  | -6 | 181     | 174  | 4  | 262      | -377 | 2  | 186      | -207 | -3 | 82      | 69   |
| 1  | 161      | 156  | -7 | 166     | -164 | -7 | 166     | -164 | 5  | 74       | -33  | -1 | 141      | -138 | -4 | 547     | -499 |
| 2  | 212      | -222 | -8 | 124     | 166  | M= | 2, K= 8 |      | -1 | 85       | -62  | -2 | 316      | 371  | -5 | 182     | -158 |
| -1 | 169      | -177 | 0  | 336     | -299 | 0  | 336     | -299 | -2 | 436      | -415 | -3 | 104      | 124  | -6 | 194     | -165 |
| -2 | 74       | 56   | 1  | 236     | -249 | 1  | 236     | -249 | -3 | 138      | 121  | -7 | 81       | 91   | -8 | 81      | 91   |
| M= | 2, K= 0  |      | 2  | 157     | -160 | 2  | 157     | -160 | -4 | 385      | 350  | M= | 2, K= 19 |      | -8 | 201     | 217  |
| 0  | 331      | 361  | 3  | 524     | 506  | 3  | 524     | 506  | -5 | 86       | 92   | M= | 3, K= 4  |      | 0  | 185     | -178 |
| 1  | 738      | 727  | 4  | 229     | 230  | 4  | 229     | 230  | -6 | 17       | -7   | 0  | 67       | 93   | 1  | 998     | 986  |
| 2  | 254      | -254 | 5  | 224     | -242 | 5  | 224     | -242 | M= | 2, K= 13 |      | 1  | 62       | 102  | 2  | 138     | -123 |
| 3  | 74       | -36  | 6  | 133     | 109  | 6  | 133     | 109  | 0  | 467      | -469 | -1 | 132      | -186 | 3  | 20      | -31  |
| -1 | 594      | 613  | -1 | 298     | -257 | -1 | 298     | -257 | 1  | 218      | -215 | -2 | 102      | -112 | 4  | 101     | 104  |
| -2 | 1164     | 1129 | -2 | 185     | 225  | -2 | 185     | 225  | 2  | 49       | -34  | M= | 3, K= 0  |      | 5  | 53      | -65  |
| -3 | 126      | -123 | -3 | 775     | 711  | -3 | 775     | 711  | 3  | 82       | -95  | 0  | 655      | -664 | 6  | 100     | 108  |
| -4 | 104      | -107 | -4 | 130     | -118 | -4 | 130     | -118 | 4  | 41       | -38  | 2  | 577      | 586  | 7  | 119     | 120  |
|    |          |      | -5 | 235     | -219 | -5 | 235     | -219 | 5  | 85       | 81   | 4  | 221      | -217 | -1 | 127     | 100  |
|    |          |      | -6 | 40      | -17  | -6 | 40      | -17  | -1 | 447      | 472  | 6  | 322      | -341 | -2 | 601     | -549 |
|    |          |      | -7 | 98      | 102  | -7 | 98      | 102  | -2 | 88       | 94   | -3 | 953      | 940  | -3 | 677     | -610 |
|    |          |      | M= | 2, K= 9 |      | M= | 2, K= 9 |      | -3 | 335      | -325 | -4 | 1198     | 1151 | -4 | 216     | -199 |
|    |          |      | 0  | 1233    | 1170 | 0  | 1233    | 1170 | -4 | 313      | 306  | -5 | 389      | -383 | -5 | 318     | 308  |
|    |          |      |    |         |      |    |         |      | -5 | 120      | -140 | -6 |          |      | -6 | 114     | 117  |

TABLE VI--Continued

| L  | FO    | FC    | L  | FO    | FC   | L  | FO    | FC   | L  | FO    | FC   | L  | FO    | FC   | L  | FO    | FC   |
|----|-------|-------|----|-------|------|----|-------|------|----|-------|------|----|-------|------|----|-------|------|
| -7 | 261   | -288  | M= | J, K= | 9    | -3 | 202   | -188 | -4 | 387   | 386  | -7 | 399   | -195 | 0  | 309   | -292 |
| -8 | 16    | -10   | 0  | 600   | 555  | -4 | 138   | 132  | -6 | 157   | -179 | -8 | 160   | -169 | 1  | 84    | 112  |
| M= | J, K= | 5     | 1  | 88    | -89  | -5 | 0     | 7    | M= | 4, K= | 1    | M= | 4, K= | 9    | 2  | 721   | 672  |
| 0  | 71    | 98    | 2  | 169   | 147  | -6 | 42    | 56   | 0  | 776   | -758 | 0  | 660   | 615  | 3  | 54    | -33  |
| 1  | 91    | 83    | 3  | 27    | 41   | M= | J, K= | 14   | 1  | 867   | 841  | 1  | 760   | -734 | 4  | 170   | -162 |
| 2  | 185   | -124  | 4  | 442   | -430 | 0  | 131   | -143 | 2  | 661   | -663 | 2  | 38    | 22   | 5  | 136   | 124  |
| 3  | 303   | 316   | 5  | 261   | 290  | 1  | 388   | 381  | 3  | 738   | -745 | 3  | 321   | 318  | -1 | 13    | -7   |
| 4  | 297   | 324   | 6  | 57    | 93   | 2  | 169   | 162  | 4  | 52    | 67   | 4  | 156   | 178  | -2 | 420   | -408 |
| 5  | 484   | -499  | -1 | 159   | 186  | 3  | 190   | -218 | 5  | 6     | -11  | 5  | 72    | -73  | -3 | 162   | -193 |
| 6  | 79    | 61    | -2 | 816   | -782 | 4  | 47    | 52   | 6  | 62    | 64   | 6  | 27    | 21   | -4 | 672   | 648  |
| 7  | 24    | 25    | -3 | 365   | -364 | -1 | 0     | -24  | -1 | 249   | 227  | -1 | 199   | -174 | -5 | 116   | -87  |
| -1 | 748   | -687  | -4 | 190   | 191  | -2 | 76    | -56  | -2 | 211   | -170 | -2 | 854   | 824  | -6 | 105   | -81  |
| -2 | 471   | 453   | -5 | 319   | -348 | -3 | 375   | -357 | -3 | 448   | -424 | -3 | 1078  | 1048 | -7 | 97    | -104 |
| -3 | 980   | 918   | -6 | 86    | -64  | -4 | 61    | -67  | -4 | 255   | -284 | -4 | 111   | -141 | M= | 4, K= | 10   |
| -4 | 28    | -50   | -7 | 27    | 35   | -5 | 325   | 353  | -5 | 553   | 541  | -5 | 275   | -280 | 0  | 222   | -223 |
| -5 | 130   | 136   | M= | J, K= | 10   | M= | J, K= | 15   | -6 | 157   | 176  | -6 | 81    | -96  | 1  | 95    | -95  |
| -6 | 276   | -264  | 0  | 266   | -287 | 0  | 187   | -190 | -7 | 38    | 42   | -7 | 47    | 45   | 2  | 152   | -135 |
| -7 | 102   | -90   | 1  | 363   | -350 | 1  | 61    | -56  | M= | 4, K= | 6    | 0  | 1198  | 1132 | 3  | 0     | 49   |
| -8 | 65    | 63    | 2  | 435   | 433  | 2  | 93    | -85  | 0  | 56    | -12  | 1  | 462   | -442 | 4  | 47    | 61   |
| M= | J, K= | 8     | 3  | 432   | 358  | 3  | 21    | 7    | 1  | 635   | 580  | 2  | 399   | -383 | 5  | 59    | 73   |
| 0  | 1092  | 1041  | 4  | 144   | -105 | 4  | 286   | 319  | 2  | 46    | -28  | 3  | 114   | 88   | -1 | 785   | 752  |
| 1  | 567   | -537  | 5  | 129   | 139  | -1 | 279   | -324 | 3  | 335   | 327  | 4  | 419   | -418 | -2 | 156   | 148  |
| 2  | 615   | -609  | 6  | 95    | -103 | -2 | 188   | 186  | 4  | 222   | 210  | 5  | 107   | 109  | -3 | 212   | -219 |
| 3  | 150   | 169   | -1 | 704   | 694  | -3 | 69    | -95  | 5  | 268   | -244 | 6  | 140   | 140  | -4 | 90    | 93   |
| 4  | 19    | -33   | -2 | 96    | -101 | -4 | 204   | -231 | 6  | 101   | -109 | -1 | 25    | 34   | -5 | 308   | -309 |
| 5  | 82    | -102  | -3 | 117   | 82   | -5 | 91    | -121 | -1 | 1023  | -987 | -2 | 909   | -863 | -6 | 249   | -280 |
| 6  | 95    | 86    | -4 | 230   | 233  | M= | J, K= | 16   | 5  | 47    | -87  | -3 | 47    | -87  | -7 | 77    | 68   |
| -1 | 276   | 253   | -5 | 102   | -94  | 0  | 175   | 192  | -1 | 465   | -439 | -4 | 226   | 213  | M= | 4, K= | 11   |
| -2 | 235   | 194   | -6 | 110   | -122 | 1  | 375   | 403  | -2 | 337   | 316  | -5 | 110   | 91   | 0  | 5     | 14   |
| -3 | 37    | 16    | -7 | 51    | -59  | 2  | 215   | -244 | -3 | 310   | 275  | -6 | 352   | 397  | 1  | 372   | 362  |
| -4 | 45    | -4    | M= | J, K= | 11   | 3  | 25    | -20  | -4 | 401   | 383  | -7 | 100   | 125  | 2  | 244   | 232  |
| -5 | 69    | 90    | 0  | 372   | 371  | -1 | 115   | 125  | -5 | 154   | -198 | 3  | 302   | -293 | 3  | 302   | -293 |
| -6 | 356   | 363   | 1  | 47    | -40  | -2 | 227   | 235  | -6 | 241   | -266 | 4  | 41    | -65  | 4  | 41    | -65  |
| -7 | 90    | -104  | 2  | 191   | 193  | -3 | 158   | -142 | -7 | 69    | 65   | 5  | 29    | 29   | -1 | 288   | 264  |
| M= | J, K= | 7     | 3  | 543   | -545 | -4 | 102   | -121 | M= | 4, K= | 3    | 0  | 689   | -622 | -2 | 200   | -172 |
| 0  | 69    | -53   | 4  | 38    | 31   | M= | J, K= | 17   | 0  | 195   | 203  | 1  | 626   | -566 | -3 | 166   | -160 |
| 1  | 24    | -30   | 5  | 185   | 188  | 0  | 100   | 125  | 1  | 165   | 147  | 2  | 105   | -92  | -4 | 202   | 193  |
| 2  | 325   | -278  | -1 | 915   | 884  | 1  | 104   | 126  | 2  | 681   | -633 | 3  | 236   | 241  | -5 | 350   | 377  |
| 3  | 302   | 293   | -2 | 76    | -109 | 2  | 32    | -37  | 3  | 316   | 323  | 4  | 205   | -223 | -6 | 9     | -12  |
| 4  | 277   | -295  | -3 | 124   | -99  | 3  | 113   | 130  | 4  | 480   | 464  | 5  | 35    | 25   | M= | 4, K= | 12   |
| 5  | 253   | -249  | -4 | 156   | 156  | -1 | 83    | -76  | 5  | 177   | 193  | 6  | 34    | -32  | 0  | 423   | -420 |
| 6  | 167   | 192   | -5 | 81    | -81  | -2 | 36    | -1   | 6  | 68    | 79   | -1 | 22    | -33  | 1  | 54    | -63  |
| -1 | 711   | -656  | -6 | 22    | -2   | -3 | 323   | 368  | -1 | 594   | -545 | -2 | 610   | -602 | 2  | 92    | -86  |
| -2 | 378   | -356  | M= | J, K= | 12   | -4 | 0     | 8    | -2 | 477   | 447  | -3 | 723   | 677  | 3  | 56    | 72   |
| -3 | 486   | 455   | 0  | 471   | -463 | M= | J, K= | 18   | -3 | 329   | -233 | -4 | 271   | 267  | 4  | 70    | 72   |
| -4 | 397   | 373   | 1  | 134   | -125 | 0  | 82    | 122  | -4 | 552   | -528 | -5 | 392   | -382 | 5  | 0     | -9   |
| -5 | 59    | -95   | 2  | 577   | 567  | 1  | 162   | -185 | -5 | 331   | -332 | -6 | 109   | -122 | -1 | 226   | -246 |
| -6 | 142   | 129   | 3  | 224   | -252 | 2  | 209   | -244 | -6 | 112   | 110  | -7 | 105   | -122 | -2 | 566   | 566  |
| -7 | 28    | -21   | 4  | 203   | -196 | 3  | 17    | 23   | -7 | 41    | -53  | M= | 4, K= | 8    | -3 | 0     | 11   |
| M= | J, K= | 8     | 5  | 14    | -24  | -1 | 31    | 41   | 0  | 58    | 63   | 0  | 646   | 537  | -4 | 298   | 334  |
| 0  | 3     | 28    | -1 | 191   | -196 | -2 | 60    | -61  | 1  | 165   | 147  | 1  | 546   | -528 | -5 | 53    | 00   |
| 1  | 1059  | -1016 | -2 | 52    | 48   | M= | J, K= | 19   | 2  | 681   | -633 | 2  | 158   | 137  | -6 | 171   | -189 |
| 2  | 100   | -90   | -3 | 457   | -481 | 0  | 82    | 122  | 3  | 316   | 323  | 3  | 171   | -166 | M= | 4, K= | 13   |
| 3  | 383   | 350   | -4 | 306   | 310  | 1  | 162   | -185 | 4  | 480   | 464  | 4  | 0     | -2   | 0  | 67    | 92   |
| 4  | 59    | -40   | -5 | 149   | 144  | 2  | 209   | -244 | 5  | 177   | 193  | 5  | 182   | 156  | 1  | 51    | 20   |
| 5  | 117   | 132   | -6 | 100   | -183 | -1 | 17    | 23   | 6  | 183   | 192  | 6  | 119   | 134  | 2  | 227   | -236 |
| 6  | 143   | 132   | M= | J, K= | 13   | -2 | 31    | 41   | 6  | 114   | -114 | -1 | 755   | 731  | 3  | 138   | -194 |
| -1 | 498   | 437   | 0  | 400   | -396 | -3 | 60    | -61  | 5  | 325   | -319 | -2 | 578   | -551 | 4  | 67    | 101  |
| -2 | 141   | -113  | 1  | 0     | -8   | M= | J, K= | 20   | 6  | 183   | 192  | -3 | 152   | -164 | 5  | 25    | -42  |
| -3 | 383   | 350   | 2  | 286   | -306 | 0  | 448   | -462 | -1 | 925   | -866 | -4 | 254   | -212 | -1 | 152   | 161  |
| -4 | 355   | -347  | 3  | 238   | -245 | 2  | 282   | 277  | -2 | 620   | -581 | -5 | 176   | -137 | -3 | 254   | -226 |
| -5 | 182   | -130  | 4  | 200   | 227  | 3  | 314   | 283  | -3 | 314   | 283  | -6 | 110   | 110  | -4 | 268   | -308 |
| -6 | 86    | 64    | 5  | 195   | 205  | 4  | 237   | 285  | -4 | 47    | 21   | -7 | 350   | 394  | -5 | 98    | 98   |
| -7 | 17    | -6    | -1 | 391   | 384  | 6  | 330   | -380 | -5 | 174   | 179  | M= | 4, K= | 9    | -6 | 82    | 95   |
|    |       |       | -2 | 207   | 227  | -2 | 291   | 285  | -6 | 98    | 96   |    |       |      |    |       |      |

TABLE VI--Continued

| L  | FO       | FC   | L  | FO       | FC   | L  | FO       | FC   | L  | FO       | FC   | L  | FO       | FC   | L  | FO       | FC   |
|----|----------|------|----|----------|------|----|----------|------|----|----------|------|----|----------|------|----|----------|------|
| M= | 4, K= 14 |      | -5 | 277      | -268 | -1 | 131      | -154 | 1  | 215      | 234  | -4 | 171      | 204  | -1 | 195      | 209  |
| 0  | 0        | 0    | -6 | 123      | -148 | -2 | 548      | 574  | 2  | 191      | -193 | -5 | 83       | -78  | -2 | 228      | 319  |
| 1  | 24       | -35  | -7 | 133      | 124  | -3 | 57       | -34  | 3  | 76       | 54   | -6 | 140      | 140  | -3 | 133      | -138 |
| 2  | 160      | 196  | M= | 5, K= 8  |      | -4 | 282      | -325 | 4  | 101      | -118 | -7 | 282      | 317  | -4 | 256      | -283 |
| 3  | 21       | 29   | 0  | 55       | 32   | -5 | 205      | -232 | 5  | 230      | -226 | M= | 6, K= 6  |      | -5 | 167      | 188  |
| 4  | 195      | 218  | 1  | 134      | -119 | -6 | 27       | 14   | -1 | 744      | -679 | 0  | 279      | -282 | -6 | 134      | 150  |
| -1 | 416      | -444 | 2  | 47       | 12   | M= | 5, K= 13 |      | -2 | 501      | -507 | 1  | 18       | 46   | M= | 6, K= 11 |      |
| -2 | 174      | -183 | 3  | 117      | -93  | 0  | 137      | 144  | -3 | 516      | 518  | 2  | 271      | 257  | 0  | 88       | -109 |
| -3 | 25       | -30  | 4  | 46       | 13   | 1  | 175      | 176  | -4 | 291      | -288 | 3  | 42       | -37  | 1  | 228      | 234  |
| -4 | 56       | -90  | 5  | 131      | 136  | 2  | 160      | -157 | -5 | 199      | 206  | 4  | 371      | -384 | 2  | 22       | -16  |
| -5 | 59       | 81   | -1 | 331      | 321  | -3 | 43       | -27  | -6 | 152      | 141  | 5  | 26       | -19  | 3  | 46       | 61   |
| M= | 4, K= 15 |      | -2 | 359      | -374 | 4  | 70       | 42   | M= | 6, K= 2  |      | -1 | 248      | -244 | 4  | 22       | -21  |
| 0  | 244      | 230  | -3 | 704      | -714 | -1 | 141      | -131 | 0  | 25       | 20   | -2 | 91       | -95  | -1 | 597      | -574 |
| 1  | 187      | -202 | -4 | 34       | -14  | -2 | 318      | -318 | 1  | 272      | -429 | -1 | 203      | -201 | -2 | 152      | 173  |
| 2  | 191      | -218 | -5 | 227      | 209  | -3 | 89       | -117 | 2  | 130      | -178 | -4 | 477      | 493  | -3 | 197      | 211  |
| 3  | 128      | 159  | -6 | 77       | 90   | -4 | 97       | -106 | 3  | 337      | 349  | -5 | 11       | 10   | -4 | 57       | 61   |
| -1 | 0        | -21  | -7 | 241      | 267  | -5 | 204      | 220  | 4  | 141      | 155  | -6 | 64       | -55  | -5 | 236      | 261  |
| -2 | 299      | 319  | M= | 5, K= 9  |      | M= | 5, K= 14 |      | 5  | 34       | 12   | -7 | 44       | 21   | -6 | 55       | -67  |
| -3 | 664      | 647  | 0  | 566      | -550 | 0  | 48       | -51  | -1 | 25       | 38   | M= | 6, K= 7  |      | M= | 6, K= 12 |      |
| -4 | 193      | -165 | 1  | 182      | 204  | 1  | 100      | -93  | -2 | 372      | 708  | 0  | 542      | -514 | 0  | 0        | 19   |
| -5 | 23       | -39  | 2  | 171      | 160  | 2  | 18       | 1    | -3 | 414      | 427  | 1  | 148      | -142 | 1  | 56       | -53  |
| -6 | 75       | 54   | 3  | 368      | 383  | 3  | 212      | 261  | -4 | 344      | -347 | 2  | 142      | 148  | 2  | 450      | -470 |
| -7 | 197      | -202 | 4  | 120      | -130 | -1 | 19       | -10  | -5 | 370      | -380 | 3  | 73       | -46  | 3  | 177      | 191  |
| M= | 5, K= 5  |      | 5  | 84       | 94   | -2 | 103      | 126  | -6 | 10       | -6   | 4  | 67       | 68   | -1 | 153      | -151 |
| 0  | 488      | 447  | -1 | 212      | -217 | -3 | 354      | 380  | -7 | 102      | 121  | 5  | 111      | 125  | -2 | 215      | 232  |
| 1  | 815      | -799 | -2 | 47       | 58   | -4 | 157      | -158 | M= | 6, K= 3  |      | -1 | 391      | 393  | -3 | 5        | 9    |
| 2  | 69       | 27   | -3 | 12       | -22  | -5 | 78       | -75  | 0  | 555      | 536  | -2 | 97       | -92  | -4 | 233      | -256 |
| 3  | 100      | 130  | -4 | 287      | 307  | M= | 5, K= 13 |      | -3 | 175      | -163 | -5 | 97       | -95  | -5 | 131      | -153 |
| 4  | 10       | 34   | -5 | 11       | 12   | 0  | 408      | 417  | -4 | 175      | -163 | M= | 6, K= 13 |      |    |          |      |
| 5  | 40       | 12   | -6 | 447      | -506 | 1  | 9        | -11  | -5 | 83       | -98  | 0  | 0        | -36  |    |          |      |
| 6  | 45       | 48   | -7 | 194      | -231 | -1 | 123      | 119  | -6 | 218      | -217 | 1  | 391      | 403  |    |          |      |
| -1 | 426      | 394  | M= | 5, K= 10 |      | -2 | 155      | -151 | -7 | 193      | 220  | 2  | 211      | 221  |    |          |      |
| -2 | 198      | -167 | 0  | 77       | -71  | -3 | 168      | -206 | 3  | 219      | -217 | 3  | 219      | -217 |    |          |      |
| -3 | 337      | 324  | 1  | 64       | 32   | -4 | 195      | -220 | 4  | 38       | 45   | 4  | 38       | 45   |    |          |      |
| -4 | 76       | -106 | 2  | 241      | -245 | M= | 5, K= 16 |      | -1 | 18       | -36  | -1 | 18       | -36  |    |          |      |
| -5 | 369      | -368 | 3  | 62       | 73   | 0  | 0        | 17   | -2 | 86       | -81  | -2 | 86       | -81  |    |          |      |
| -6 | 168      | 167  | 4  | 77       | 89   | 1  | 7        | -15  | -3 | 410      | -433 | -3 | 410      | -433 |    |          |      |
| -7 | 229      | 242  | 5  | 119      | 118  | 2  | 80       | 105  | -4 | 94       | -83  | -4 | 94       | -83  |    |          |      |
| M= | 5, K= 6  |      | -1 | 693      | 689  | 3  | 109      | -128 | -5 | 265      | 272  | -5 | 265      | 272  |    |          |      |
| 0  | 426      | 389  | -2 | 323      | 321  | -3 | 208      | 219  | -6 | 191      | -210 | -6 | 191      | -210 |    |          |      |
| 1  | 197      | -168 | -3 | 194      | -173 | -4 | 189      | 239  | -7 | 59       | 22   | -7 | 59       | 22   |    |          |      |
| 2  | 00       | 47   | -4 | 255      | -288 | M= | 5, K= 17 |      | 4  | 59       | -83  | M= | 6, K= 9  |      |    |          |      |
| 3  | 51       | -37  | -5 | 137      | 115  | 0  | 135      | 161  | 5  | 165      | -191 | 0  | 391      | -368 |    |          |      |
| 4  | 292      | -272 | -6 | 63       | 78   | -1 | 261      | -315 | -1 | 189      | 169  | 1  | 278      | 281  |    |          |      |
| 5  | 175      | -184 | M= | 5, K= 11 |      | -2 | 171      | 187  | -2 | 65       | -58  | 2  | 251      | 237  |    |          |      |
| -1 | 28       | 23   | 0  | 149      | 136  | -3 | 49       | 80   | -3 | 533      | 527  | 3  | 101      | 119  |    |          |      |
| -2 | 535      | -522 | 1  | 31       | -28  | -4 | 94       | 128  | -4 | 243      | 247  | 4  | 101      | 127  |    |          |      |
| -3 | 433      | -427 | 2  | 149      | 176  | M= | 6, K= 8  |      | -5 | 319      | -323 | -1 | 193      | -181 |    |          |      |
| -4 | 535      | 503  | 3  | 189      | -209 | 0  | 119      | -104 | -6 | 86       | -99  | -2 | 450      | 441  |    |          |      |
| -5 | 106      | 97   | 4  | 45       | 62   | 2  | 790      | -813 | -7 | 0        | 6    | -3 | 68       | 75   |    |          |      |
| -6 | 233      | 262  | -1 | 344      | -343 | 4  | 249      | 224  | M= | 6, K= 5  |      | -4 | 64       | -63  |    |          |      |
| -7 | 0        | 29   | -2 | 114      | 136  | -2 | 416      | 407  | 0  | 490      | 449  | -5 | 69       | -104 |    |          |      |
| M= | 5, K= 7  |      | -3 | 147      | 126  | -3 | 491      | -483 | 1  | 356      | -320 | -6 | 190      | -224 |    |          |      |
| 0  | 354      | -345 | -4 | 351      | 378  | -6 | 163      | 150  | 2  | 141      | 155  | M= | 6, K= 10 |      |    |          |      |
| 1  | 505      | -496 | -5 | 531      | 594  | M= | 5, K= 12 |      | 3  | 275      | -283 | 0  | 43       | -42  |    |          |      |
| 2  | 165      | 150  | -6 | 82       | -95  | 0  | 44       | -74  | 4  | 150      | -157 | 1  | 391      | 394  |    |          |      |
| 3  | 301      | 318  | M= | 5, K= 12 |      | 1  | 434      | -453 | 5  | 42       | 55   | 2  | 189      | -218 |    |          |      |
| 4  | 159      | 156  | 0  | 44       | -74  | 2  | 274      | -262 | -1 | 383      | 359  | 3  | 204      | -220 |    |          |      |
| 5  | 42       | -33  | 1  | 434      | -453 | 3  | 0        | -78  | -2 | 305      | 247  | 4  | 176      | 209  |    |          |      |
| -1 | 279      | 251  | 2  | 274      | -262 | M= | 6, K= 1  |      | -3 | 186      | -197 | M= | 6, K= 16 |      |    |          |      |
| -2 | 420      | -399 | 3  | 0        | -78  | 0  | 34       | -24  | M= | 6, K= 10 |      | 0  | 98       | -134 |    |          |      |
| -3 | 167      | 169  | 4  | 134      | 166  | M= | 6, K= 1  |      | 1  | 391      | 394  | 1  | 139      | -134 |    |          |      |
| -4 | 282      | 276  | M= | 5, K= 12 |      | 0  | 34       | -24  | 2  | 189      | -218 | -1 | 113      | 143  |    |          |      |

TABLE VI--Continued

| L          | FO  | FC   | L           | FO          | FC   | L           | FO          | FC   | L           | FO          | FC   | L           | FO         | FC         | L          | FO         | FC         |      |      |     |
|------------|-----|------|-------------|-------------|------|-------------|-------------|------|-------------|-------------|------|-------------|------------|------------|------------|------------|------------|------|------|-----|
| M= 7, K= 0 | 0   | 314  | 231         | 3           | 138  | -147        | -3          | 704  | 719         | -6          | 164  | -190        | M= 8, K= 7 | 0          | 163        | 180        | M= 9, K= 0 | 0    | 99   | 135 |
| 0          | 540 | 488  | 1           | 27          | -34  | -1          | 238         | 249  | -4          | 238         | 249  | 0           | 404        | 402        | 0          | 140        | 141        | 0    | 99   | 135 |
| 2          | 520 | -557 | 2           | 22          | -13  | -2          | 392         | -397 | -5          | 392         | -397 | 1           | 87         | -102       | 2          | 571        | -531       | 2    | 140  | 141 |
| 4          | 120 | -127 | 3           | 477         | -511 | -3          | 135         | 141  | -6          | 213         | -237 | 2           | 276        | -745       | -2         | 571        | -531       | -2   | 256  | 306 |
| -2         | 314 | -297 | 4           | 51          | -67  | -4          | 211         | -229 | -7          | 96          | 107  | 3           | 276        | -745       | -4         | 256        | 306        | -4   | 256  | 306 |
| -4         | 495 | -487 | -1          | 145         | 143  | -5          | 279         | 331  | M= 8, K= 2  | 0           | 503  | 435         | -6         | 128        | 162        | M= 9, K= 1 | 0          | 238  | -233 |     |
| -6         | 395 | 404  | -2          | 111         | -96  | -6          | 103         | 120  | 0           | 42          | -20  | -1          | 46         | -29        | -1         | 437        | -445       |      |      |     |
| M= 7, K= 1 | 0   | 130  | -128        | M= 7, K= 11 | 0    | 190         | 215         | 2    | 107         | 106         | -2   | 0           | 6          | 0          | 238        | -233       |            |      |      |     |
| 1          | 67  | -81  | 1           | 79          | -103 | 2           | 107         | 106  | 3           | 24          | 12   | -3          | 285        | -276       | 1          | 437        | -445       |      |      |     |
| 2          | 85  | 116  | 2           | 159         | -171 | 3           | 24          | 12   | 4           | 47          | -37  | -4          | 297        | -331       | 2          | 133        | 134        |      |      |     |
| 3          | 175 | 185  | 3           | 147         | 166  | -1          | 584         | -552 | -1          | 584         | -552 | -5          | 182        | 195        | 3          | 161        | 197        |      |      |     |
| 4          | 78  | -99  | -1          | 393         | -406 | -2          | 375         | -346 | -2          | 375         | -346 | -6          | 52         | 89         | -2         | 87         | -85        |      |      |     |
| 5          | 87  | -57  | -2          | 17          | -10  | -3          | 570         | -563 | -3          | 570         | -563 | M= 8, K= 8  | 0          | 32         | 2          | -3         | 89         | -37  |      |     |
| -1         | 433 | -396 | -3          | 217         | 214  | -4          | 273         | 300  | -4          | 273         | 300  | 0           | 32         | 2          | -4         | 52         | -127       |      |      |     |
| -2         | 873 | -859 | -4          | 44          | 46   | -5          | 300         | -298 | -5          | 300         | -298 | 1           | 33         | -45        | -5         | 46         | -45        |      |      |     |
| -3         | 694 | 688  | -5          | 0           | -26  | -6          | 79          | 46   | -6          | 79          | 46   | 2           | 119        | 98         | -6         | 289        | -327       |      |      |     |
| -4         | 51  | -52  | M= 7, K= 12 | 0           | 337  | 335         | M= 8, K= 3  | 0    | 538         | -472        | -1   | 300         | -290       | M= 9, K= 2 | 0          | 221        | 193        |      |      |     |
| -5         | 201 | -204 | 1           | 118         | -155 | 0           | 538         | -472 | -2          | 24          | -27  | -2          | 24         | -27        | 1          | 63         | 45         |      |      |     |
| -6         | 49  | 11   | 2           | 223         | -233 | 1           | 67          | 39   | -3          | 110         | 134  | -3          | 110        | 134        | 2          | 54         | 55         |      |      |     |
| -7         | 0   | -6   | -1          | 96          | -89  | 2           | 279         | 230  | -4          | 33          | 27   | -4          | 33         | 27         | 3          | 124        | -188       |      |      |     |
| M= 7, K= 2 | 0   | 280  | 265         | -2          | 111  | -136        | 3           | 18   | 16          | -5          | 93   | 117         | -5         | 93         | 117        | -2         | 229        | 224  |      |     |
| 1          | 365 | -358 | -3          | 128         | -147 | 4           | 142         | -134 | -6          | 148         | -150 | -6          | 148        | -150       | -2         | 356        | -320       |      |      |     |
| 2          | 51  | -21  | -4          | 108         | -116 | -1          | 155         | -170 | M= 8, K= 9  | 0           | 94   | 116         | -3         | 179        | -151       |            |            |      |      |     |
| 3          | 179 | 165  | -5          | 71          | -82  | -2          | 192         | -209 | 0           | 94          | 116  | -4          | 58         | 35         |            |            |            |      |      |     |
| 4          | 34  | 28   | M= 7, K= 7  | 0           | 88   | -33         | -3          | 99   | 96          | 1           | 100  | 118         | -5         | 186        | 231        |            |            |      |      |     |
| 5          | 215 | 233  | 1           | 98          | 106  | -4          | 532         | 523  | 2           | 427         | -440 | -6          | 94         | 121        |            |            |            |      |      |     |
| -1         | 389 | 384  | 2           | 268         | -286 | -5          | 206         | -202 | -1          | 233         | 258  | M= 9, K= 3  | 0          | 455        | -433       |            |            |      |      |     |
| -2         | 68  | 43   | 3           | 337         | -321 | -6          | 317         | -365 | -2          | 124         | 124  | 1           | 75         | 77         |            |            |            |      |      |     |
| -3         | 50  | -44  | 4           | 285         | 325  | M= 8, K= 4  | 0           | 45   | 50          | -3          | 57   | 117         | 2          | 222        | 232        |            |            |      |      |     |
| -4         | 313 | -276 | -1          | 187         | 195  | 0           | 45          | 50   | -4          | 173         | -176 | 3           | 74         | 71         |            |            |            |      |      |     |
| -5         | 404 | -405 | -2          | 187         | 195  | 1           | 206         | -226 | -5          | 99          | -141 | -1          | 255        | 272        |            |            |            |      |      |     |
| -6         | 119 | 97   | -3          | 313         | -336 | 2           | 0           | -2   | M= 8, K= 10 | 0           | 211  | 239         | -2         | 252        | 268        |            |            |      |      |     |
| -7         | 195 | 220  | -4          | 180         | -174 | 3           | 191         | -193 | 1           | 53          | 6    | -3          | 136        | 131        |            |            |            |      |      |     |
| M= 7, K= 3 | 0   | 247  | 248         | -5          | 153  | 154         | 4           | 105  | 120         | 2           | 100  | -104        | -4         | 220        | 252        |            |            |      |      |     |
| 1          | 273 | 251  | -6          | 242         | -234 | -4          | 130         | 167  | 3           | 191         | -193 | -5          | 0          | 5          |            |            |            |      |      |     |
| 2          | 338 | 315  | M= 7, K= 8  | 0           | 61   | -61         | M= 8, K= 5  | 0    | 117         | 114         | -4   | 173         | -176       | -6         | 257        | -295       |            |      |      |     |
| 3          | 7   | -11  | 1           | 410         | 420  | -1          | 152         | -152 | 1           | 206         | -226 | -5          | 99         | -141       | M= 9, K= 4 | 0          | 198        | 204  |      |     |
| 4          | 259 | -262 | 2           | 101         | 97   | -2          | 456         | -506 | 2           | 0           | -2   | 0           | 0          | -7         | 1          | 47         | -44        |      |      |     |
| -1         | 44  | 38   | 3           | 192         | -196 | -3          | 106         | 107  | 3           | 191         | -193 | 1           | 367        | -415       | 2          | 58         | -86        |      |      |     |
| -2         | 862 | -854 | 4           | 65          | 59   | -4          | 130         | 167  | 4           | 105         | 120  | 2           | 57         | -115       | -1         | 184        | 180        |      |      |     |
| -3         | 35  | -30  | -1          | 326         | -314 | -5          | 152         | -152 | -1          | 882         | 853  | -1          | 24         | -27        | -2         | 164        | 190        |      |      |     |
| -4         | 480 | 461  | -2          | 87          | 80   | -2          | 456         | -506 | -2          | 244         | 247  | -2          | 104        | 92         | -3         | 163        | -162       |      |      |     |
| -5         | 261 | -265 | -3          | 206         | -210 | -3          | 106         | 107  | -3          | 131         | -106 | -3          | 217        | 227        | -4         | 203        | -237       |      |      |     |
| -6         | 87  | 85   | -4          | 0           | -35  | -4          | 130         | 167  | -4          | 121         | 127  | -4          | 90         | 114        | -5         | 197        | 221        |      |      |     |
| -7         | 50  | -69  | -5          | 208         | 222  | M= 7, K= 14 | 0           | 117  | 114         | -5          | 38   | 4           | -5         | 217        | 255        | -6         | 233        | 243  |      |     |
| M= 7, K= 4 | 0   | 214  | -394        | -6          | 217  | -252        | M= 7, K= 15 | 0    | 63          | 125         | -6   | 233         | -263       | M= 8, K= 6 | 0          | 189        | 210        |      |      |     |
| 1          | 394 | -393 | M= 7, K= 9  | 0           | 50   | 71          | 0           | 63   | 125         | M= 8, K= 7  | 0    | 49          | 43         | 0          | 0          | -7         |            |      |      |     |
| 2          | 232 | 260  | 1           | 264         | 272  | -1          | 152         | 207  | 1           | 335         | 309  | 0           | 0          | -7         | 1          | 367        | -415       |      |      |     |
| 3          | 13  | -31  | 2           | 464         | -465 | -2          | 296         | -333 | 2           | 176         | 185  | 1           | 367        | -415       | 2          | 57         | -115       |      |      |     |
| 4          | 115 | 140  | 3           | 154         | 167  | M= 8, K= 0  | 0           | 197  | 177         | 3           | 168  | -167        | -1         | 24         | -27        | -2         | 164        | 190  |      |     |
| -1         | 473 | 473  | -1          | 41          | 72   | 0           | 197         | 177  | -1          | 370         | -335 | -2          | 104        | 92         | -3         | 163        | -162       |      |      |     |
| -2         | 211 | 193  | -2          | 406         | 384  | 1           | 258         | -275 | -2          | 16          | 28   | -3          | 184        | 224        | -4         | 203        | -237       |      |      |     |
| -3         | 180 | 143  | -3          | 23          | 37   | -1          | 75          | 117  | -3          | 339         | -378 | -4          | 74         | 79         | -5         | 197        | 221        |      |      |     |
| -4         | 466 | 469  | -4          | 139         | -147 | -2          | 48          | -72  | -4          | 325         | 331  | -5          | 217        | 255        | -6         | 233        | 243        |      |      |     |
| -5         | 280 | -276 | -5          | 83          | -109 | -3          | 20          | 9    | -5          | 276         | 292  | M= 8, K= 11 | 0          | 189        | 210        |            |            |      |      |     |
| -6         | 127 | -149 | -6          | 140         | -146 | M= 8, K= 1  | 0           | 215  | -204        | -6          | 91   | -79         | 0          | 0          | -7         |            |            |      |      |     |
| -7         | 189 | 199  | M= 7, K= 10 | 0           | 297  | 320         | 0           | 215  | -204        | M= 8, K= 12 | 0    | 189         | 210        | 1          | 103        | -105       |            |      |      |     |
| M= 7, K= 5 | 0   | 214  | -394        | 1           | 399  | -359        | 1           | 258  | -275        | 1           | 103  | -105        | 1          | 103        | -105       |            |            |      |      |     |
| 1          | 394 | -393 | 2           | 199         | 174  | -1          | 75          | 117  | 2           | 190         | -184 | -1          | 166        | 198        | 2          | 42         | 11         |      |      |     |
| 2          | 232 | 260  | 3           | 97          | 131  | -2          | 48          | -72  | 3           | 28          | -39  | -2          | 201        | -218       | -1         | 307        | -312       |      |      |     |
| 3          | 13  | -31  | 4           | 44          | 17   | -3          | 20          | 9    | -1          | 32          | 10   | -3          | 226        | -253       | -2         | 75         | 79         |      |      |     |
| 4          | 115 | 140  | -1          | 72          | 72   | M= 8, K= 2  | 0           | 215  | -204        | -2          | 191  | 153         | -4         | 106        | 122        | -3         | 122        | -121 |      |     |
| -1         | 473 | 473  | -2          | 201         | -179 | 0           | 215         | -204 | -3          | 187         | -114 | M= 8, K= 13 | 0          | 84         | -97        | -4         | 388        | 400  |      |     |
| -2         | 211 | 193  | M= 7, K= 6  | 0           | 893  | -925        | 1           | 399  | -359        | -4          | 22   | -11         | 0          | 84         | -97        | -5         | 95         | 133  |      |     |
| -3         | 180 | 143  | 1           | 58          | 66   | 2           | 199         | 174  | -5          | 22          | -11  | -1          | 113        | 88         | -6         | 20         | 35         |      |      |     |
| -4         | 466 | 469  | 2           | 94          | 86   | 3           | 97          | 131  | -6          | 101         | -104 | -2          | 177        | -210       | M= 9, K= 6 | 0          | 274        | -256 |      |     |
| -5         | 280 | -276 | 3           | 103         | -108 | 4           | 44          | 17   | M= 8, K= 14 | 0           | 535  | -514        | 0          | 274        | -256       |            |            |      |      |     |
| -6         | 127 | -149 | 4           | 49          | 49   | -1          | 72          | 72   | 0           | 535         | -514 | 1           | 62         | 74         |            |            |            |      |      |     |
| -7         | 189 | 199  | -5          | 178         | -198 | -2          | 201         | -179 | 1           | 318         | -338 | 2           | 42         | 11         |            |            |            |      |      |     |

TABLE VI--Continued

| L          | PO  | PC   | L           | PO  | PC   | L           | PO          | PC          | L           | PO          | PC   | L           | PO  | PC   | L   | PO  | PC   |
|------------|-----|------|-------------|-----|------|-------------|-------------|-------------|-------------|-------------|------|-------------|-----|------|-----|-----|------|
| 0          | 27  | -11  | M= 9, K= 8  | 0   | 84   | 98          | M= 10, K= 1 | M= 10, K= 3 | 0           | 24          | -4   | 0           | 24  | -4   |     |     |      |
| 1          | 45  | 59   |             | 1   | 181  | -235        | 0           | 117         | -101        | 1           | 161  | 201         | 1   | 161  | 201 |     |      |
| 2          | 352 | -367 | 0           | 91  | 122  | -1          | 54          | -68         | 0           | 301         | -313 | -1          | 512 | -560 | -1  | 512 | -560 |
| -1         | 10  | -22  | 1           | 120 | -145 | -2          | 149         | -177        | 1           | 145         | 164  | -2          | 52  | 43   | -2  | 52  | 43   |
| -2         | 229 | 240  | -1          | 214 | -248 | -3          | 384         | 485         | -1          | 168         | -214 | -3          | 277 | 312  | -3  | 277 | 312  |
| -3         | 47  | -44  | -2          | 219 | 226  | -4          | 219         | 276         | -2          | 176         | 183  | -4          | 65  | 69   | -4  | 65  | 69   |
| -4         | 396 | -428 | -3          | 209 | 232  |             |             |             | -3          | 126         | 127  |             |     |      |     |     |      |
| -5         | 147 | -173 | -4          | 112 | -118 | M= 9, K= 11 |             |             | -4          | 96          | -114 | M= 10, K= 6 |     |      |     |     |      |
|            |     |      | -5          | 263 | -325 | 0           | 86          | 89          | -5          | 107         | -122 | 0           | 55  | 58   | 0   | 55  | 58   |
|            |     |      |             |     |      | -1          | 146         | 177         |             | 157         | -196 | -1          | 112 | -148 | -1  | 112 | -148 |
| M= 9, K= 7 |     |      | M= 9, K= 9  |     |      | -2          | 54          | -94         | M= 10, K= 2 | M= 10, K= 4 |      | -2          | 30  | 18   | -2  | 30  | 18   |
| 0          | 147 | 190  | 0           | 360 | 393  | -3          | 76          | -83         | 0           | 94          | 64   | -3          | 52  | 61   | -3  | 52  | 61   |
| 1          | 208 | 219  | 1           | 56  | -81  |             |             |             | 1           | 339         | 373  | -4          | 393 | -458 | -4  | 393 | -458 |
| 2          | 51  | 11   | -1          | 134 | 120  | M= 10, K= 8 |             |             | -1          | 21          | -13  | M= 10, K= 7 |     |      |     |     |      |
| -1         | 162 | -175 | -2          | 212 | -223 | 0           | 367         | -399        | -2          | 207         | 222  | 0           | 342 | 367  | 0   | 342 | 367  |
| -2         | 257 | -280 | -3          | 4   | 29   | -2          | 250         | -270        | -3          | 305         | -336 | -1          | 363 | -381 | -1  | 363 | -381 |
| -3         | 61  | 69   | -4          | 101 | -141 | -4          | 181         | -180        | -4          | 51          | 55   | -2          | 272 | -276 | -2  | 272 | -276 |
| -4         | 103 | -118 |             |     |      |             |             |             | -5          | 126         | 135  | -3          | 791 | 340  | -3  | 791 | 340  |
| -5         | 258 | 302  | M= 9, K= 10 |     |      |             |             |             |             |             |      | M= 10, K= 5 |     |      | -4  | 58  | 82   |

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## CHAPTER IV

### DISCUSSION AND CONCLUSION

#### Thermal Motion

All atoms in a molecule undergo a certain amount of vibration. This vibration increases with increasing temperatures; thus, it is called thermal motion. The thermal motion of an atom results from the superposition of all the normal modes of vibration in the crystal and yields a very complicated result (1). The net effect of vibration is to spread out the electron density of the atom over a finite volume. The spreading of electron density over an atom's equilibrium position results in a volume element consistent with the bonding for the complex involved. Since a vibrating atom possesses a scattering power less than that of a stationary atom, it is necessary to determine the vibrational contributions to the scattering factor through x-ray methods. A first approximation would be to assume that each sphere of vibration possesses a constant radius and is, therefore, isotropic. This would produce an individual temperature parameter for each atom,  $B = 8\pi^2 \bar{u}^2$ , where  $\bar{u}^2$  represents the root-mean-square amplitude of atomic vibration. As mentioned in the previous chapter, this produces an approximate model for a tentative structure,



but it represents each atom as a centroid. A more accurate description of the temperature factor is given by considering the thermal motion as anisotropic. The anisotropic model contains all of the information normally obtained on thermal motion. The anisotropic temperature factor is expressed as,

$$\exp[-(B_{11}h^2 + B_{22}k^2 + B_{33}l^2 + 2B_{12}hk + 2B_{13}hl + 2B_{23}kl)],$$

where  $h$ ,  $k$ , and  $l$  are the indices of a reflection and the  $B$  terms are components of a symmetry second-order tensor, representing the vibrational modes for each atom of the molecule (3; 8, p. 44). The six  $B$  terms are convenient to use in least squares refinement.

One can compute the directions of each principal axis and the root-mean-square displacement along each axis of the thermal ellipsoid from a principal axis transformation done on the exponential forms containing the  $B$  terms. Table VII gives these root-mean-square displacements for BPGC. Figure 3 shows a CalComp plot of the molecule with fifty percent probability ellipsoids (4, p. 220; 5). From the figure, one can see that the principal axes with the longest root-mean-square amplitude for some atoms are not perpendicular to the plane of the bipyridyl ring. This would indicate that some poor data exist in the reflection list, which resulted in some difficulty in the least squares convergence. These slight abnormalities are not

TABLE VII

ROOT-MEAN-SQUARE AMPLITUDES ( $\text{\AA}$ ) OF VIBRATION IN THE  
PRINCIPAL AXES DIRECTIONS FOR THE ATOMS IN BPGC

| Atom  | Axis 1 | Axis 2 | Axis 3 |
|-------|--------|--------|--------|
| Cu    | 0.1283 | 0.1672 | 0.2310 |
| Cl    | 0.1821 | 0.2097 | 0.2520 |
| O(1)  | 0.1121 | 0.1917 | 0.2735 |
| O(2)  | 0.1388 | 0.2411 | 0.2937 |
| O(3)  | 0.2155 | 0.2403 | 0.3095 |
| O(4)  | 0.2750 | 0.3289 | 0.3660 |
| N(1)  | 0.1190 | 0.1590 | 0.2174 |
| N(2)  | 0.1504 | 0.1929 | 0.2270 |
| N(3)  | 0.1352 | 0.1735 | 0.2702 |
| C(1)  | 0.1437 | 0.2159 | 0.2417 |
| C(2)  | 0.1747 | 0.1968 | 0.2569 |
| C(3)  | 0.1472 | 0.2318 | 0.2807 |
| C(4)  | 0.1372 | 0.2090 | 0.2511 |
| C(5)  | 0.1406 | 0.1902 | 0.1941 |
| C(6)  | 0.1312 | 0.1806 | 0.2102 |
| C(7)  | 0.1128 | 0.2109 | 0.2638 |
| C(8)  | 0.1352 | 0.2291 | 0.2860 |
| C(9)  | 0.1507 | 0.2389 | 0.2921 |
| C(10) | 0.1305 | 0.1969 | 0.3288 |
| C(11) | 0.1308 | 0.1820 | 0.3324 |
| C(12) | 0.1667 | 0.2238 | 0.2268 |

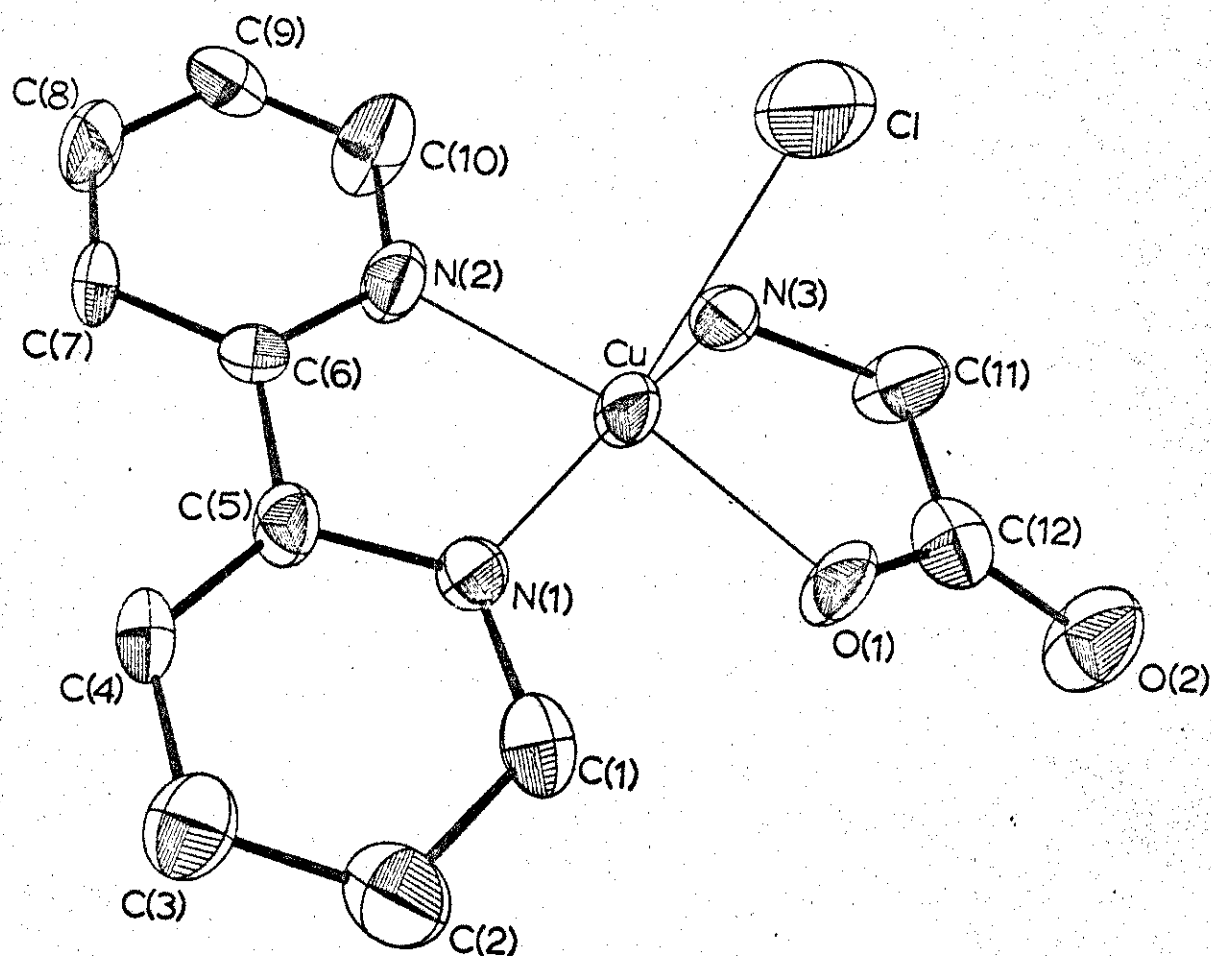


Fig. 3--The fifty percent probability thermal ellipsoids from the thermal parameters of BPGC. View is twisted ten degrees along the Cu-N(1) axis and also the Cu-N(2) axis with copper as the origin.

reflected to any major extent in the bond distances, however.

### Molecular and Crystal Structures

Figure 4 shows the entire unit cell and atoms located in the region twenty percent beyond the cell in each direction. The viewing direction is rotated twenty degrees along the c axis and twelve degrees along the a axis. The calculated hydrogen positions are not shown. Bond distances are given in Table VIII. Valance angles for BPGC are given in Table IX.

TABLE VIII  
BOND LENGTHS ( $\text{\AA}$ ) IN BPGC

| Atom 1 | Atom 2 | Distance Apart ( $\text{\AA}$ ) |
|--------|--------|---------------------------------|
| Cu     | O (1)  | 1.957 (8)                       |
| Cu     | N (3)  | 2.025 (10)                      |
| Cu     | N (1)  | 2.010 (9)                       |
| Cu     | N (2)  | 2.027 (10)                      |
| Cu     | Cl     | 2.635 (4)                       |
| O (1)  | C (12) | 1.298 (15)                      |
| N (1)  | C (1)  | 1.339 (16)                      |
| N (1)  | C (5)  | 1.350 (14)                      |
| N (2)  | C (6)  | 1.342 (15)                      |
| C (1)  | C (2)  | 1.417 (18)                      |
| C (2)  | C (3)  | 1.392 (18)                      |
| C (3)  | C (4)  | 1.426 (18)                      |
| C (4)  | C (5)  | 1.358 (17)                      |
| C (5)  | C (6)  | 1.506 (16)                      |
| C (6)  | C (7)  | 1.394 (16)                      |
| C (7)  | C (8)  | 1.347 (18)                      |
| C (8)  | C (9)  | 1.351 (18)                      |
| C (9)  | C (10) | 1.374 (19)                      |
| C (10) | N (2)  | 1.316 (16)                      |
| C (11) | N (3)  | 1.492 (16)                      |
| C (12) | C (11) | 1.533 (18)                      |
| C (12) | O (2)  | 1.244 (18)                      |

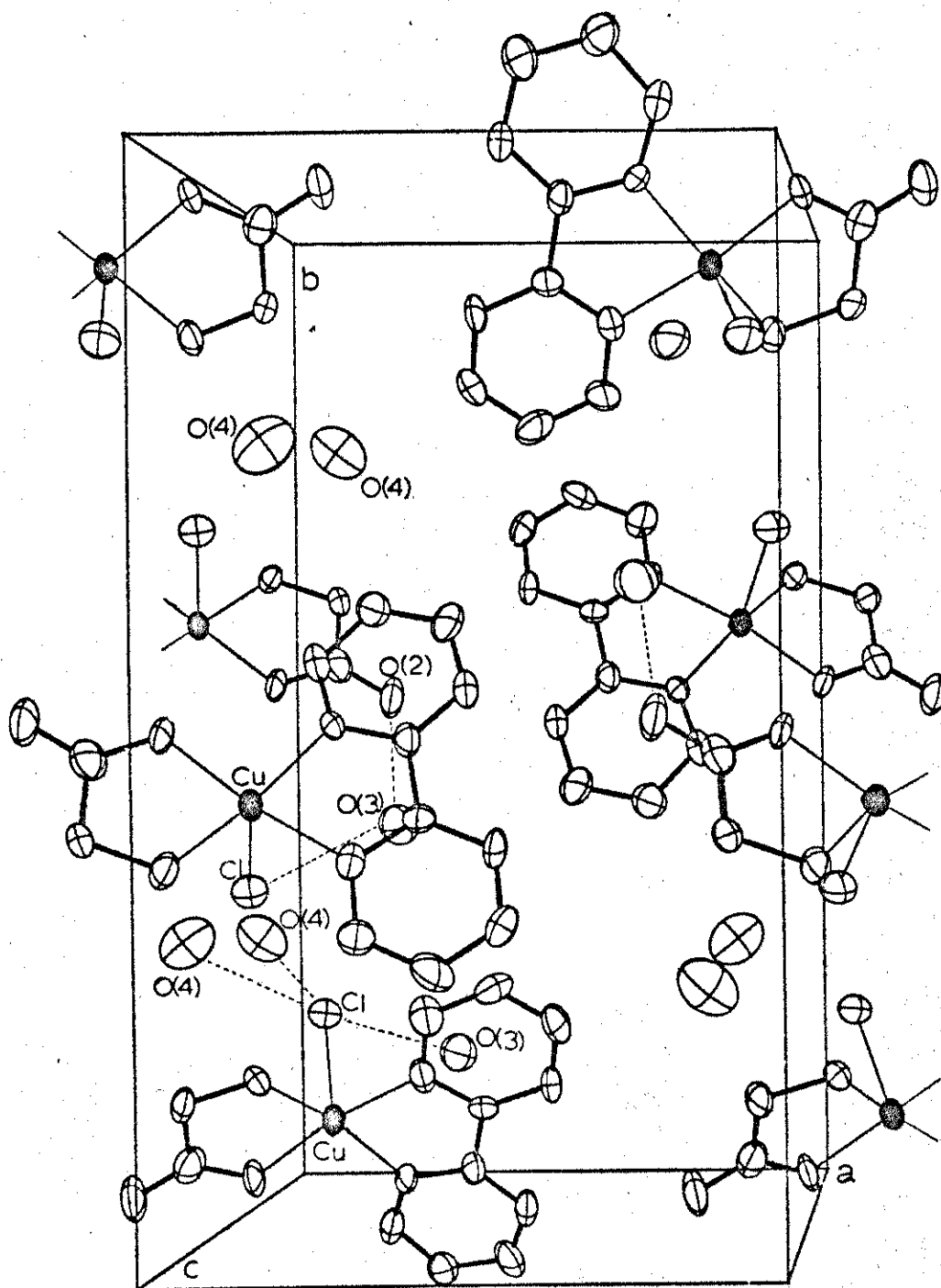


Fig. 4--The unit cell structure of BPGC (See text for further planation.)

TABLE IX  
VALENCE ANGLES (DEGREES) IN THE BPGC MOLECULE

| Atoms Forming Angle  | Angle     |
|----------------------|-----------|
| Cu - O(1) - C(12)    | 115.5(7)  |
| Cu - N(1) - C(1)     | 125.3(7)  |
| Cu - N(1) - C(5)     | 114.5(7)  |
| Cu - N(2) - C(6)     | 113.8(7)  |
| Cu - N(2) - C(10)    | 127.1(8)  |
| Cu - N(3) - C(11)    | 107.5(7)  |
| Cl - Cu - O(1)       | 97.5(6)   |
| Cl - Cu - N(1)       | 100.3(6)  |
| Cl - Cu - N(2)       | 92.7(6)   |
| Cl - Cu - N(3)       | 96.6(6)   |
| O(1) - Cu - N(1)     | 93.0(3)   |
| O(1) - Cu - N(3)     | 86.7(3)   |
| O(1) - C(12) - O(2)  | 123.9(12) |
| O(1) - C(12) - C(11) | 116.7(10) |
| O(2) - C(12) - C(11) | 119.4(11) |
| N(1) - Cu - N(2)     | 81.6(3)   |
| N(1) - C(1) - C(2)   | 122.5(10) |
| N(1) - C(5) - C(4)   | 122.2(10) |
| N(1) - C(5) - C(6)   | 114.3(9)  |
| N(2) - Cu - N(3)     | 96.7(3)   |
| N(2) - C(6) - C(5)   | 115.4(9)  |
| N(2) - C(6) - C(7)   | 121.1(10) |
| N(2) - C(10) - C(9)  | 121.6(12) |
| N(3) - C(11) - C(12) | 112.7(10) |
| C(1) - N(1) - C(5)   | 120.1(9)  |
| C(1) - C(2) - C(3)   | 116.4(11) |
| C(2) - C(3) - C(4)   | 120.5(11) |
| C(3) - C(4) - C(5)   | 118.4(11) |
| C(4) - C(5) - C(6)   | 123.6(10) |
| C(5) - C(6) - C(7)   | 123.6(10) |
| C(6) - N(2) - C(10)  | 119.0(10) |
| C(6) - C(7) - C(8)   | 118.8(11) |
| C(7) - C(8) - C(9)   | 119.6(12) |
| C(8) - C(9) - C(10)  | 119.8(12) |

One can easily see that the coordination about the copper atom is distorted from octahedral. One would predict from Table I that the most probable structure would be distorted octahedral.

From the least squares mean plane calculation, Table X, one can see that the copper atom is slightly above the plane of the four atoms coordinated to it. This could be due to steric interaction of the glycine group and the chlorine atom with the central copper atom.

It has been postulated by Hamilton (2, p. 13) that the O - H...Cl bonding distance is 3.10 Å to 3.20 Å. In the same article, he also postulates the O-H...O bonding distance to be from 2.70 Å to 2.80 Å.

The chlorine atom of BPGC is surrounded by three oxygen atoms which are approximately equidistant to it. From the bond distances found, it is apparent that these bonds are most probably hydrogen bonds. The proposed hydrogen bonded distances are 3.15, 3.20 and 3.19 Å for the two O(4) - H...Cl and O(3) - H...Cl bonds, and are shown in Figure 5. The O(2) and O(3) atoms also indicate, by their distance apart, that they could possess some hydrogen bonding between them. The proposed hydrogen bonded distance for O(2)...H - O(3) is approximately 2.76 Å, and can be seen in Figure 4.

TABLE X

EQUATIONS OF THE LEAST SQUARES BEST PLANES THROUGH THE  
TWO RING SYSTEMS OF BIPYRIDYL IN THE MOLECULE OF  
BPGC AND THE DEVIATION OF ATOMS FROM THE  
BEST PLANES

| Ring                    | Equations of Best Planes                |
|-------------------------|---|
| Ring 1* . . . . .       | $0.0397X + 0.4478Y - 0.8933Z = -1.3879$ |
| Ring 2* . . . . .       | $0.1186X + 0.5054Y - 0.8547Z = -1.0212$ |
| Ring 1 + Ring 2 . . . . | $0.0789X + 0.4835Y - 0.8717Z = -1.1533$ |

Distances of Atoms from Best Planes (Å)

| Atoms | Ring 1         | Ring 2         | Ring 1 + Ring 2 |
|-------|----------------|----------------|-----------------|
| N(1)  | 0.2022(89)     | -0.0143(89)**  | 0.0003(89)**    |
| N(2)  | -0.0162(94)**  | -0.0199(94)    | -0.0929(94)**   |
| C(1)  | 0.3433(125)    | 0.0112(125)**  | 0.0742(125)**   |
| C(2)  | 0.3278(125)    | 0.0002(125)**  | 0.0541(125)**   |
| C(3)  | 0.1865(132)    | -0.0082(132)** | -0.0171(132)**  |
| C(4)  | 0.0781(127)    | 0.0053(126)**  | -0.0545(126)**  |
| C(5)  | 0.0945(111)    | 0.0058(111)**  | -0.0404(111)**  |
| C(6)  | 0.0208(117)**  | 0.0531(111)    | -0.0425(111)**  |
| C(7)  | -0.0147(124)** | 0.1578(124)    | -0.0028(124)**  |
| C(8)  | 0.0040(135)**  | 0.2762(134)    | -0.0755(135)**  |
| C(9)  | 0.0009(139)**  | 0.2359(137)    | 0.0584(137)**   |
| C(10) | 0.0051(137)**  | 0.1006(136)    | -0.0929(94)**   |

\*Rings are defined in figure 3.

\*\*Atom used to define the least squares plane.



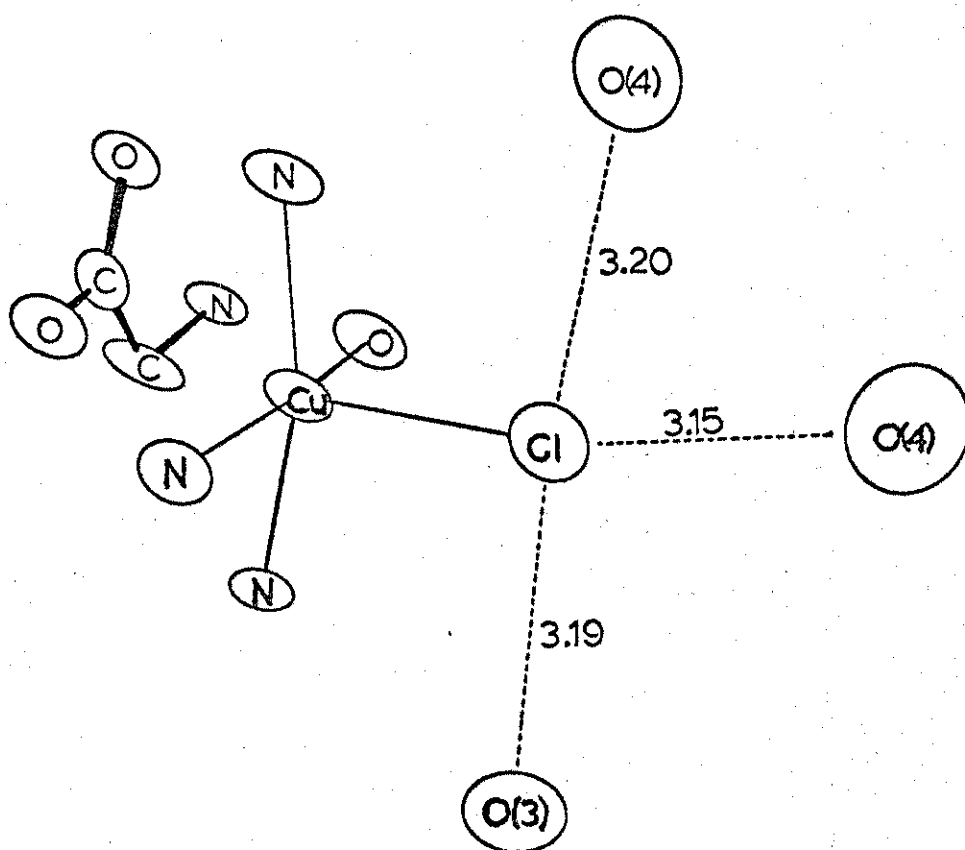


Fig. 5--The hydrogen bonded environment surrounding the chlorine atom, with symmetry related glycine group opposite to the chlorine. (See text for further explanation.)

TABLE XI

EQUATIONS OF THE LEAST SQUARES BEST PLANES THROUGH THE FIVE  
 ATOM CENTRAL COORDINATION AND GLYCINE LIGAND OF BPGC  
 AND THE DEVIATION OF ATOMS FROM THE BEST PLANES

| Equations of Best Planes                |  |              |
|---|--|--------------|
| Plane 1. . . . .                        | $-0.1372X + 0.5794Y - 0.8034Z = -1.4082$ |              |
| Plane 2. . . . .                        | $-0.1365X + 0.5792Y - 0.0837Z = -1.3615$ |              |
| Distances of Atoms from Best Planes (Å) |  |              |
| Atoms                                   | Plane 1                                  | Plane 2      |
| Cu                                      | 0.2358(15)                               | 0.1886(15)*  |
| N(1)                                    | -0.0641(89)*                             | -0.1099(89)* |
| N(2)                                    | 0.0610(94)*                              | 0.0146(94)*  |
| N(3)                                    | -0.0594(99)*                             | -0.1079(99)* |
| O(1)                                    | -0.0625(81)*                             | 0.0146(81)*  |
| O(2)                                    | -0.1216(89)                              | -0.1710(89)  |
| C(11)                                   | 0.0683(138)                              | 0.0190(138)  |
| C(12)                                   | -0.0146(124)                             | -0.0343(124) |

\*Atom used to define the least-squares plane.

From Table XI one can see that the least squares best planes through the bipyridyl system indicate that the two bipyridyl rings are not coplanar. The dihedral angle between the planes is approximately six degrees. It is possible to see this puckering of the two rings in Figure 4. This is unusual since other copper structures coordinated to 2,2'-bipyridyl show the pyridine ring as planar (6, 9).

The distance between the C(5) and C(6) atoms indicates a small amount of  $\pi$  bonding, if any, between them, as compared with the other bond distances of other atoms composing the rings. Merritt (7) has shown that the free bipyridyl system is in the least sterically hindered position, with the two nitrogen atoms opposing each other by approximately 180 degrees relative to the center of the molecule. The N(1) - Cu - (N(2)) bond angle is only eighty-one degrees. These facts could cause a weakening of the C(5)-C(6) bond by causing a bending stress on the bond.

The glycine ligand could be a stabilizing factor in the tetrahedral distortion due to the  $sp^3$  nature of the C(11) and N(3) atoms. These  $sp^3$  bonds cause a slight misalignment of the  $sp^2$  bonded O(2), C(12), and O(1) atoms. The steric configuration of the molecule is best seen in Figure 6.

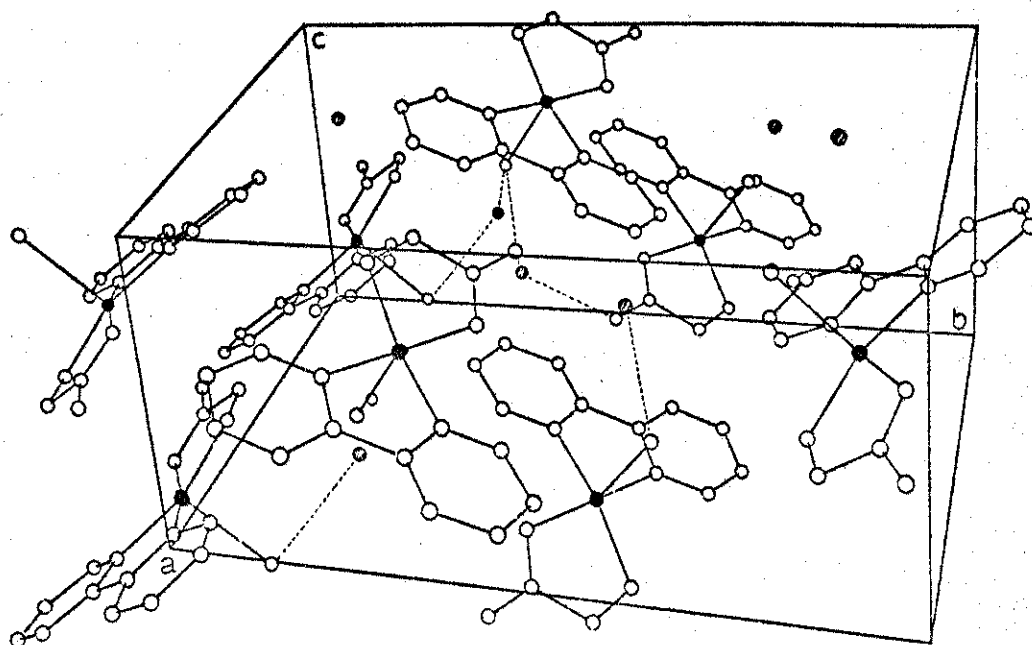


Fig. 6--The unit cell of BPGC. Viewing direction is rotated twenty degrees along the a axis and twelve degrees along the c axis.

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## APPENDIX

An IBM 360 computer program was used in the determination of diffractometer linearity. This program produces a series of printer plotted graphs of R index verses  $\sin^2\theta$ , containing a data point for each reflection. From these graphs, it is possible to observe the contribution of individual reflections as well as small groups of reflections to the overall R index. The input to this program consists of  $\sin^2\theta$  and individual R index for each reflection observed.

```

C *****
C * THIS PROGRAM READS THE SINE SQUARED THETA AND THE *
C * INDIVIDUAL RESIDUAL INDEXES FOR A SET OF REFLECTIONS *
C * STORED ON TAPE AND GENERATES A GRAPH OF SINE SQUARED *
C * THETA VERSES THE INDIVIDUAL R VALUES. THE COLUMNS *
C * ARE THEN INDEPENDANTLY AVERAGED AND THE AVERAGE *
C * SUPERIMPOSED ON THE GRAPH. THE GRAPH IS INTERPRETED *
C * AS: *
C * A) EACH LETTER CORRESPONDS TO BETWEEN ONE AND *
C * TWENTY SEVEN REFLECTIONS REPRESENTED BY THE *
C * LETTERS FROM A THROUGH Z PLUS *. *
C * B) EACH OF THE DOTS REPRESENT THE AVERAGE OF ALL *
C * DATA POINTS IN THE COLUMN. *
C * EACH GRAPH GENERATED IS AN AMPLIFICATION OF THE *
C * PREVIOUS GRAPH. FROM THESE GRAPHS IT IS POSSIBLE *
C * TO VISUALLY DETERMINE THE CUTOFF POINT FOR THE HIGH *
C * AND LOW TWO THETA RANGE. THIS IS ACCOMPLISHED BY *
C * DRAWING TWO LINES, ONE ON EITHER SIDE OF THE DIS- *
C * CONTINUOUS LINE OF AVERAGES. WHEN THE TWO LINES *
C * BEGAN TO DIVERGE OR THE AVERAGE OF THE LINES BEGINS *
C * TO FALL THE DATA AT THAT POINT IS CONSIDERED BAD. *
C *****
REAL A(28),BAR,BLIN,GRAPH(60,45),B(28),DOT,N,VERT(45)
READ(5,105)VERT
REWIND 1
N = 450
DATA A / ' ','A','B','C','D','E','F','G','H','I','J',
2 'K','L','M','N','O','P','Q','R','S','T','U','V','W',
3 'X','Y','Z','*' /
DATA BAR,BLIN/' ','_ '/
DATA DOT/'.'/
DO 112 I =1,28
112 B(I) = I - 1
1000 DO 1 J=1,45
DO 1 I=1,60
1 GRAPH(I,J) = A(1)
DO 2 I=1,45
GRAPH(1,I) = BAR
2 GRAPH(60,I) = BAR
DO 3 I=1,60
GRAPH(I,1) = BLIN
3 GRAPH(I,45) = BLIN
4 READ(1,20,END=100)SINSQ,RINDX
I = N * (SINSQ*.5) + 1.
J = RINDX / 4. + 1.
IF((I.GT.60).OR.(J.GT.45))GO TO 4
IF(GRAPH(I,J).EQ.A(28))GO TO 4
DO 5 INDX = 1,28

```

```

IF(BAR.EQ.GRAPH(I,J))GO TO 6
IF(BLIN.EQ.GRAPH(I,J))GO TO 6
IF(A(INDX).EQ.GRAPH(I,J))GC TO 6
5 CCNTINUE
GO TO 4
6 GRAPH(I,J) = A(INDX + 1)
GC TO 4
100 WRITE(6,103)
DO 110 I=1,60
XNUM = 0.0
XDEN = 0.0
DC 111 J=1,45
DC 111 L=1,28
IF(GRAPH(I,J).EQ.A(L))XNUM = XNUM+B(L)*J
111 IF(GRAPH(I,J).EQ.A(L)) XDEN = XDEN + B(L)
IF(XDEN.EQ.0.)GO TO 110
NAVG = XNUM / XDEN + 1.
GRAPH(I,NAVG) = DOT
110 CONTINUE
DO 101 J=1,45
JJ = (J-1) * 4
101 WRITE(6,102)(GRAPH(I,J),I=1,60),JJ,VERT(J)
DC 7 I=1,61
XC = I
SINSQ = XC/N
SI = SQRT(SINSQ)
SII = ARSIN(SI)* 229.183
7 WRITE(6,104)I,SINSQ,SII
N = N + 200.
REWIND 1
IF(N.GT.2200.)STOP
GC TO 1000
20 FCFMAT(21X,F10.4,30X,F10.4)
102 FCFMAT(30X,60A1,1X,I3,2X,1A1)
103 FCFMAT(1H1,/////////,25X,'SINE **2 THETA',/)
104 FORMAT(I4,2F10.4)
105 FCFMAT(4A1)
END

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