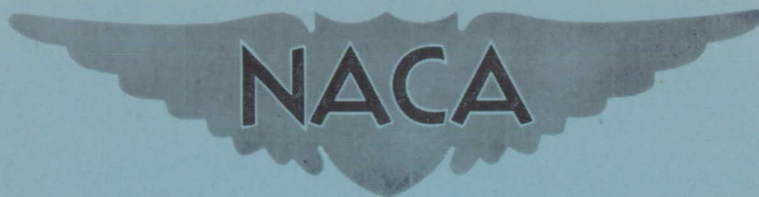


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# RESEARCH MEMORANDUM

PREDICTION OF FLAME VELOCITIES OF HYDROCARBON FLAMES

By Gordon L. Dugger and Dorothy M. Simon

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## PREDICTION OF FLAME VELOCITIES OF HYDROCARBON FLAMES

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## SUMMARY

The laminar-flame-velocity data previously reported by the Lewis laboratory are surveyed with respect to the correspondence between experimental flame velocities and values predicted by semitheoretical and empirical methods. The combustible mixture variables covered are hydrocarbon structure (56 hydrocarbons), equivalence ratio of fuel-air mixture, mole fraction of oxygen in the primary oxygen-nitrogen mixture (0.17 to 0.50), and initial mixture temperature (200° to 615° K). The semitheoretical methods of prediction considered are based on three approximate theoretical equations for flame velocity: the Semenov equation (bimolecular), which is primarily based on conductive heat transfer between the flame and the reactants; the Tanford-Pease equation, which is based on the diffusion of chain carriers of the oxidation reaction into the reactants; and the Manson equation, which is a modification of the momentum-pressure-drop equation that does not include chemical kinetics. In each equation a semiempirical factor is used to bring the predicted values for a given variable and fuel into the best average agreement with the data, so that the variation in the relative prediction of the individual datum points may be considered. For the resulting semitheoretical equations, it is assumed that thermal equilibrium is attained at the end of the flame zone, and values for the transport properties are estimated by extrapolation and simple additive relations. The empirical relations between combustible mixture variables and flame velocity are based on the usual methods of correlation.

Within these limitations, the results may be generalized as follows:

1. The three semitheoretical equations predict relative flame velocities reasonably well, generally with mean deviations of 2 to 15 percent.
2. Considering only the bimolecular fuel-oxygen reaction and with low-temperature activation energies, the Semenov equation may be used to give good relative predictions when a "steric factor" is determined semiempirically.
3. The average "specific rate constants" ( $\bar{k}_a$ ) obtained with the Tanford-Pease equation for molecular fuel - active particle reactions behave as Arrhenius rate constants only with the data on the effect of initial temperature, not with the equivalence-ratio or oxygen-concentration data. The relative predictions obtained by this equation

are not very sensitive either to the temperature dependence assigned to the diffusion coefficients or to the recombination factor computed for hydrogen atoms. Regarding active particles considered, better results are generally obtained for hydrocarbon flames when the hydroxyl radical and the hydrogen and oxygen atoms (OH, H, and O) are considered rather than H alone; this is particularly true for studies of the effect of equivalence ratio.

4. For the equivalence-ratio and oxygen-concentration data, considerably better relative predictions are obtained from the Manson equation when the pressure drop across the flame front is considered to be due to H, OH, and O than when only H atoms are taken into account.

5. The example presented by the ethylene data shows that an empirically determined rate constant or proportionality factor from equivalence-ratio data at atmospheric pressure and room temperature may predict the effect of initial temperature or oxygen concentration within approximately 20 percent by the Semenov or Tanford-Pease equation and within approximately 30 percent by the Manson equation.

6. For engineering applications, the effects of the parameters studied could be estimated just as satisfactorily, and more easily, by one or another of the empirical correlations indicated, as compared with the three semitheoretical equations considered. However, the use of the semitheoretical equations in some cases reduces the number of constants required.

## INTRODUCTION

The ability to predict flame velocities of fuels is of growing importance in the field of aircraft propulsion, since a correlation has been found between combustion efficiency of a ram-jet burner and the laminar flame velocity of the fuel (reference 1). The prediction of flame velocities is difficult for three reasons. (1) There is no complete, rigorous theory which can be readily applied. There are, however, a number of approximate equations in the literature which approach the problem of flame propagation from various viewpoints. (2) There are no data on the kinetics of the oxidation process under flame conditions and very few data on transport properties at high temperatures. (3) Different methods of flame-velocity measurement give different values, so that it is difficult to compare data from different sources. The uncertainty in measurements made by a given method is of the order of 5 percent.

In this report flame-velocity measurements made at the NACA (references 2 to 7) for different hydrocarbons, initial temperatures, and compositions are used with semitheoretical and empirical methods of

flame-velocity prediction to show the correspondence between the measured velocities and the predicted velocities. The semitheoretical methods are based on the Semenov equation (reference 8), the Tanford-Pease square-root law (reference 9), and the Manson equation (reference 11). These three equations were derived from different models of the flame-propagation process. The Semenov model is essentially a thermal model which includes chemical reaction kinetics; the Tanford-Pease model is based on the diffusion of chain carriers of the oxidation reaction; and Manson used a modification of the momentum-pressure-drop equation which does not include chemical kinetics. The empirical relations for the effect on maximum flame speed of hydrocarbon structure, of initial mixture temperature, and of oxygen concentration were based on the usual methods of correlation.

It is recognized that there are other approximate theoretical equations which may give as good or better predictions of the NACA experimental results. These particular equations were chosen because they exemplify three different approaches to the problem and because the Semenov and Tanford-Pease equations were used in previous NACA papers and many of the calculations had already been made individually. It is also recognized that there are many flame-speed data in the literature which could be used in such studies; the present paper is confined to NACA data because many of the calculations had been made, and because it was desirable to avoid the complications arising from comparing data obtained by many different methods and techniques.

#### NOMENCLATURE

The following nomenclature is used in this paper:

- a fuel concentration, molecules of fuel per  $\text{cm}^3$  of mixture
- b oxygen concentration, molecules of oxygen per  $\text{cm}^3$  of mixture
- $B_i$  term near unity arising from radical recombination
- $C_p$  molar heat capacity at constant pressure,  $\text{cal/mole-}^\circ\text{K}$
- $c_p$  specific heat,  $\text{cal/g-}^\circ\text{K}$
- $\bar{c}_p$  mean specific heat,  $T_0$  to  $T_f$ ,  $\text{cal/g-}^\circ\text{K}$
- D diffusion coefficient,  $\text{cm}^2/\text{sec}$
- $D_i$  diffusion coefficient of  $i^{\text{th}}$  active species into unburned gas at initial mixture temperature,  $\text{cm}^2/\text{sec}$

- E activation energy, kcal/g-mole
- $\bar{E}_a$  fitted activation energy for a group of data points, kcal/g-mole
- K empirical proportionality constant between experimental flame velocity and value predicted by the Manson equation
- $K_H$  empirical K from Manson equation when  $\Delta p = 1/2 P_H \frac{T_O}{T_F}$
- $K_\Sigma$  empirical K from Manson equation when  

$$\Delta p = 1/2 \left( P_H + P_{OH} \frac{D_{OH}}{D_H} + P_O \frac{D_O}{D_H} \right) \frac{T_O}{T_F}$$
- $\bar{K}_H, \bar{K}_\Sigma$  average  $K_H$  or  $K_\Sigma$  for a group of data points
- k specific rate constant,  $\text{cm}^3/\text{molecule-sec}$
- $k_a$  weighted mean  $k_i$  for the three active particles H, OH, and O, each reacting with fuel molecules,  $\text{cm}^3/\text{molecule-sec}$
- $\bar{k}_a$  average  $k_a$  for a group of data points,  $\text{cm}^3/\text{molecule-sec}$
- $k_i$  specific rate constant for reaction between fuel molecule and  $i^{\text{th}}$  active particle,  $\text{cm}^3/\text{molecule-sec}$
- $L_m$  total concentration of gas at mean combustion-zone temperature,  $\text{molecule}/\text{cm}^3$
- M molecular weight
- m molecularity of flame reaction
- $N_i$  mole fraction of  $i^{\text{th}}$  component
- n total number of molecules of  $\text{H}_2\text{O}$  and  $\text{CO}_2$  in products per molecule of fuel by stoichiometric relation
- $n_1/n_2$  moles of reactants per mole of products from stoichiometric equation
- P steric factor, or probability factor, from the expression  

$$k = PZe^{-E/RT}$$
- $\bar{P}$  average P for a group of data points
- p total pressure of mixture

- $p_i$  mole fraction of the  $i^{\text{th}}$  active particle in burned gas
- $Q$  mole fraction of potential combustion product in unburned gas
- $Q'$  mole fraction of fuel in unburned gas
- $R$  universal gas constant, kcal/(g-mole)( $^{\circ}\text{K}$ ) or ergs/(g-mole)( $^{\circ}\text{K}$ )
- $T$  absolute temperature,  $^{\circ}\text{K}$
- $T_f$  computed equilibrium flame temperature,  $^{\circ}\text{K}$
- $U$  flame velocity, cm/sec; implies maximum flame velocity with respect to equivalence ratio, except in discussion of the variation of equivalence ratio
- $w$  reaction rate, molecules reacting per  $\text{cm}^3/\text{sec}$
- $Z$  collision number; the number of molecular collisions per second when the concentration is one molecule of each type per  $\text{cm}^3$
- $\alpha$  mole fraction of oxygen in oxygen-nitrogen portion of mixture,  $\text{O}_2/(\text{O}_2+\text{N}_2)$
- $\delta$  percentage mean deviation in the ratio of predicted flame velocity to the experimental value for a given group of data
- $\eta$  viscosity of mixture, poise
- $\eta_i$  viscosity of  $i^{\text{th}}$  component, poise
- $\theta_m$  ratio of mean reaction-zone temperature to initial temperature
- $\lambda$  thermal conductivity,  $\text{cal}/(\text{cm}^2)(\text{sec})(^{\circ}\text{K}/\text{cm})$
- $\rho$  density of mixture,  $\text{g}/\text{cm}^3$
- $\sigma$  collision diameter, cm
- $\varphi$  equivalence ratio, fraction of stoichiometric fuel-oxygen ratio

## Subscripts:

- eff effective value at mean reaction temperature
- f at flame temperature

m at mean reaction-zone temperature

0 initial conditions

### APPROXIMATE THEORETICAL EQUATIONS USED

#### The Semenov Bimolecular Equation

Zeldovich and Frank-Kamenetsky obtained an approximate solution for the rate of flame propagation from the differential equations for heat conduction and fuel concentration change across the flame front. This approximate solution was presented in detail by Semenov (reference 8). The general approximate solution may be written (see reference 8, pp. 31, 48, and 49):

$$U = \sqrt{\frac{2\lambda \int_0^{T_f} w \, dT}{a_0 \rho_0 c_p (T_f - T_0)} \left(\frac{n_1}{n_2}\right)^m \left(\frac{\lambda}{Dc_p \rho}\right)_f^m} \quad (1)$$

where, for a bimolecular reaction between unlike molecules

$$\begin{aligned} \int_0^{T_f} w \, dT &= \int_0^{T_f} k(a)(b) \, dT \\ &= a_{\text{eff}} b_{\text{eff}} PZ \cdot \frac{RT_f^2}{E} \cdot e^{-E/RT_f} \end{aligned} \quad (2)$$

For lean mixtures,  $\varphi < 1$ ,  $a_{\text{eff}}$  and  $b_{\text{eff}}$  are computed by (following the assumptions of reference 8, p. 45):

$$\begin{aligned} a_{\text{eff}} &= a_0 \frac{T_0}{T_f} \frac{RT_f^2}{E(T_f - T_0)} \\ b_{\text{eff}} &= b_0 \frac{T_0}{T_f} \left[ 1 - \varphi \left( 1 - \frac{RT_f^2}{E(T_f - T_0)} \right) \right] \end{aligned} \quad (3)$$

For rich mixtures,  $\varphi > 1$ :

$$a_{\text{eff}} = a_0 \frac{T_0}{T_f} \left[ 1 - \frac{1}{\varphi} \left( 1 - \frac{RT_f^2}{E(T_f - T_0)} \right) \right]$$

$$b_{\text{eff}} = b_0 \frac{T_0}{T_f} \frac{RT_f^2}{E(T_f - T_0)} \quad (4)$$

For stoichiometric mixtures, equations (3) and (4) are identical. All of the factors in equations (1) through (4) can, with the exceptions of  $P$  and  $E$ , be estimated by the extrapolation of thermodynamic tables (references 12 and 13) or calculated by the relations

$$\eta = \sum_i \eta_i N_i$$

(Values calculated for combustion-product mixtures by this simple, additive method were within 1 percent of values calculated by the method of reference 14.)

$$\left. \begin{aligned} C_p &= \sum_i C_{p,i} N_i \\ \lambda &= (C_p + \frac{5}{4} R) \eta / M \text{ (reference 13)} \\ D &= 1.336 \eta / \rho \text{ (reference 15)} \\ \rho &= p / MRT \\ Z &= \left( \frac{\sigma_1 + \sigma_2}{2} \right)^2 \left[ 8\pi RT \frac{(M_1 + M_2)}{M_1 M_2} \right]^{1/2} \end{aligned} \right\} \quad (5)$$

Flame-velocity predictions by the Semenov equation are evaluated herein as follows. Activation energies from low-temperature reactions and measured flame velocities are substituted in equation (1) and a steric factor  $P$  is calculated for each experimental flame velocity. These  $P$ 's are then averaged to give  $\bar{P}$  for the group of data points. The ratio of the predicted flame velocity to the experimental velocity is calculated as  $(\bar{P}/P)^{1/2}$ . The average deviation of the ratios from 1 is considered to be a measure of the accuracy of the predicted flame velocities. (The word accuracy is used to denote the degree of correspondence between flame velocities calculated by the methods described and measured flame velocities.)

The data for various hydrocarbons consisted of maximum flame velocities (maximum with respect to equivalence ratio) of 56 pure hydrocarbons at 298° K and atmospheric pressure (references 2 and 3). These data were obtained by the NACA tube method. The hydrocarbons included straight and branched chain members of the alkane, alkene, alkadiene, alkyne, and cycloalkane series and benzene. No calculations are made by



the Semenov equation for these data, because the work required by this treatment would not be warranted in view of the slight differences in flame velocities observed for most of the hydrocarbons studied. However, it has been shown by more approximate calculations (reference 16) that relative predictions would be satisfactory.

The initial-mixture-temperature data included maximum flame velocities of methane-air, propane-air, and ethylene-air mixtures obtained by a Bunsen burner method (total area method, outside edge of shadow cast by flame cone, reference 5) at seven initial mixture temperatures ranging from 200° to 617° K. The following activation energies, in kilocalories per gram-mole, are reported in references 17, 18, and 19, respectively: methane, 51; propane, 38; ethylene, 40. These values are used in the Semenov equation to evaluate the flame-velocity predictions. The accuracy of the predicted flame velocities is 2 to 3 percent. Specific values are tabulated in table I under "Semenov Equation".

Two kinds of mixture-composition variables are studied. The first is the change of hydrocarbon concentration in air over an equivalence-ratio range of 0.7 to 1.3. Flame-velocity values by the tube method for ethylene-air and pentane-air at 298° K (reference 4), and Bunsen burner values (total area method, outer edge of cone shadow) for methane-air at 307° K and propane-air at 302° K (reference 5) are used. When the effect of changes in equivalence ratio on the flame velocity is computed by the Semenov equation, it is found that the approximations used in equations (3) and (4) are not very consistent for the region near stoichiometric, particularly for equivalence ratios between 0.95 and 1.05. This fact is shown by the difference between the Semenov curves in figure 1(a), where points in the range 0.95 to 1.05 are included in plotting the curve, and figure 1(b), where these points are omitted. If this critical region is omitted, the accuracy of the predicted flame velocities over the equivalence range is 3 to 7 percent. Specific deviations are listed in table I.

The second composition variable studied is the ratio of oxygen to oxygen plus nitrogen  $\alpha = O_2/(O_2+N_2)$ . Maximum flame velocities for several  $\alpha$  ratios were available for the following fuels and ranges of  $\alpha$ : propane, 0.17 to 0.50; ethylene, 0.17 to 0.35; and 2,2,4-trimethylpentane, 0.21 to 0.50. The accuracy of prediction of these data is 3 to 17 percent (table I).

It may be noted in table I that flame-velocity predictions by the Semenov equation for ethylene flames are accurate to 4 percent for variations in both composition and initial temperature. For these predictions (as discussed previously), each type of data was considered separately, and steric factors were calculated from the data. Now usually, when it is desired to predict flame velocities, only one type

of data is available - for example, fuel-air ratio data at atmospheric pressure and room temperature. It is therefore important to know how well the effects of initial temperature and oxygen concentration can be predicted from such data. The ethylene data are used as an example.

The steric factor  $\bar{P}$  calculated from the equivalence-ratio data and the low-temperature activation energy of 40 kilocalories per gram-mole are used in the Semenov equation to predict flame velocities over the ranges of initial temperature and oxygen concentration covered by the experimental data. In both cases the predicted flame velocities deviated from the normalized measured flame velocities by an average of +14 percent, the maximum deviation being +24 percent for the oxygen-concentration data. (Because different methods of measuring flame velocity were used, differences in values for mixtures of the same composition and temperature were found. For these calculations all flame velocities were normalized by a simple ratio factor to the values for the initial-temperature data.)

#### Tanford-Pease Equation

Tanford and Pease (references 9 and 20) equated the amount of product formed in the combustion zone by a second-order reaction between fuel molecules and hydrogen atoms (or other active particles such as hydroxyl radicals or oxygen atoms) to the amount of product formed at the flame front by conversion of the fresh gas expressed in terms of initial conditions and flame velocity. An approximate solution for flame velocity from this equation was given:

$$U = \left( \frac{L_m Q' n}{Q \theta_m^2} \sum_i \frac{k_i p_i D_m}{B_i} \right)^{1/2} \quad (6)$$

Three methods of evaluating the predictions of the Tanford and Pease equation are used herein. For all three, the following calculations are the same: (a) flame temperature  $T_f$  and active particle concentrations  $p_i$  are calculated assuming adiabatic thermal equilibrium by a matrix method (reference 21); (b) the mean combustion-zone temperature is assumed to be  $0.7 T_f$  (reference 9); (c) diffusion coefficients  $D_m$  are calculated from  $D_m = D_i (0.7 T_f / T_0)^{1.67}$ , where  $D_i$  is the diffusion coefficient at initial temperature calculated by the Stefan-Maxwell equation (reference 22); (d) the recombination factor  $B_i$  is calculated by the method of Tanford (reference 10) for the hydrogen atoms and is assumed to be one for OH and O; (e) the ratio  $L_m Q' n / Q$  is calculated from a knowledge of the over-all oxidation process and the initial concentrations of reactants.

The three methods of evaluation differ in the calculation of  $k_i$ . For the first method only one chain carrier, the hydrogen atom, is considered. For this case  $k_H$  values are calculated from single-point flame-velocity determinations by equation (6). For the second method, H, O, and OH are considered to be the chain carriers and

$$\sum_i \frac{k_i p_i D_m}{B_i} \approx k_a \left( \frac{p_H D_H}{B_H} + p_{OH} D_{OH} + p_O D_O \right) \left( \frac{0.7 T_f}{T_0} \right)^{1.67} \quad (7)$$

Single-point  $k_a$  values are calculated. For these two methods, the ratio of the predicted flame velocity to the experimental flame velocity is calculated as  $(\bar{K}_i/k_i)^{1/2}$  and the average deviation of the ratio from 1 is used as a measure of the accuracy of the predictions.

For the third method, an Arrhenius type temperature dependence of the rate constant is used:

$$k_a = P_a Z_a \exp(-E_a/R(0.7 T_f)) \quad (8)$$

The following method is used to calculate an activation energy  $\bar{E}_a$  for best fit from the initial-temperature data. Several values of  $E_a$  are substituted in the equation and for each a value of  $(\bar{P}/P)^{1/2}$  is calculated. Then  $\delta$ , the percentage mean deviation in  $(\bar{P}/P)^{1/2}$  for the group, is plotted against the  $E_a$  used. The "fitted" value of  $\bar{E}_a$  is the one which gives the minimum  $\delta$ . All other calculations by the third method are made by equations (7) and (8), measured flame velocities, and  $\bar{E}_a$  from initial-temperature data. The accuracy is calculated as the mean deviation of  $(\bar{P}/P)^{1/2}$  from 1.

The predictions of the Tanford-Pease equation are evaluated by methods 1 and 2 for the maximum flame velocities of a series of hydrocarbons (reference 23). Table I shows that the accuracy of prediction of flame velocity is 3.3 percent considering hydrogen atoms ( $\bar{k}_H$ ) only and 3.5 percent considering all three active particles ( $\bar{k}_a$ ). These mean deviations are small enough to indicate either that the "rate constants" are not temperature-dependent, in which case the steric factors are of the order of  $10^{-3}$ , or that  $\left[ \exp\left(\frac{\bar{E}_a}{R(0.7 T_f)}\right) \right] \sqrt{T_f}$  is nearly constant for the hydrocarbons studied, which is probable. If the activation energy is of the order of 10 kilocalories per gram-mole, the steric factor is of the order of  $10^{-2}$ .

All three methods of evaluation are used with the initial-temperature data. The accuracy of the flame velocity predictions is

9 to 12 percent (table I) for the first method ( $\bar{k}_H$ ) and 6 to 8 percent for the second method. The use of method 3, which includes the temperature dependence of the rate constant, improves the prediction so that the accuracy is about 2 percent. The calculated activation energies and steric factors are: for methane, 17 and 0.19; and for ethylene, 18 and 0.21. The calculated activation energy for ethylene is high when compared with the experimental activation energy for the reaction  $H + C_2H_4 \rightarrow C_2H_5$ , which is 2.6 kilocalories (calculated from data in reference 24). The relative predictions are not appreciably changed by assuming  $B_H = 1$  or by assuming  $D_m \propto T_m^2$  which was used in reference 7 instead of  $D_m \propto \eta/\rho$ .

If the entire equivalence-ratio ranges which were covered experimentally by the flame-velocity data are used for the prediction of velocities by the Tanford-Pease method, the accuracy of prediction is very poor as illustrated in figure 1(a) for ethylene. If the equivalence range is limited to one near the maximum flame velocity (for example,  $\varphi = \varphi_{max} \pm 0.15$ ), the accuracy of the predictions is 1 to 6 percent (table I) when all active particles are considered. However, if only hydrogen atoms are used the accuracy is very poor - 17 to 65 percent.

The variations of flame velocity with oxygen concentration were calculated for all active particles. The accuracy of prediction is 4 to 6 percent.

The ethylene data are again used as an example to show how well an average "rate constant" ( $\bar{k}_a$  from method 2) from the fuel-air ratio data predicts the effects of temperature and oxygen concentration on the maximum flame velocity. Predicted flame velocities for various temperatures differ from the normalized experimental values by -9 to +13 percent with an average deviation of 6 percent. Predicted flame velocities for various oxygen concentrations differ from experimental values by +8 to +22 percent with an average deviation of 12 percent.

#### The Manson Equation

The momentum relationship between the flame (or combustion wave) velocity and the pressure drop across a plane, steady-state flame front may be expressed in the form (reference 25, pp. 241):

$$U = \left( \frac{\rho_f}{\rho_0} \frac{\Delta p}{\rho_0 - \rho_f} \right)^{1/2} \quad (9)$$

Manson (reference 11) suggested that the small pressure drop could be caused by the projection of hydrogen atoms into the unburned gas. Because the H atoms would recombine to  $H_2$  at the unburned gas temperature,  $\Delta p$  was assumed to be one-half the equilibrium H atom pressure reduced to unburned gas temperature. In the present paper,  $\Delta p$  is calculated as both  $\frac{1}{2} P_H \frac{T_0}{T_F}$  and  $\frac{1}{2} \left( P_H + P_{OH} \frac{D_{OH}}{D_H} + P_O \frac{D_O}{D_H} \right) \frac{T_0}{T_F}$ . The second method of calculating  $\Delta p$  takes into account three of the lightest and most abundant species which might be considered active particles and assumes that all of these would recombine in pairs. The average proportionality factor for a group of data is calculated by dividing the experimental flame velocity by the right-hand side of equation (9) for each point and averaging the quotients. These average empirical proportionality factors are designated  $\bar{K}_H$  for the first method and  $\bar{K}_\Sigma$  for the second. The accuracy of the predicted flame velocities is considered to be the average deviation of  $\bar{K}_H/K_H$  or  $\bar{K}_\Sigma/K_\Sigma$  from 1. For the maximum flame velocities of the different hydrocarbons, the accuracy of prediction by the Manson equation for either method of evaluation is about 4 percent (table I). For the first method ( $\bar{K}_H$ ), the proportionality factor is 0.5; that is, the predicted value is twice the experimental value.

For the initial-temperature data the predicted flame velocities differ from the experimental velocities by 10 to 14 percent. When the total range of the equivalence-ratio data is considered, the accuracy of prediction of flame velocities by the Manson equation and either of the methods of evaluating  $\Delta p$  is poor. If the equivalence range is limited as for the Tanford-Pease method and with all active particles, predictions accurate to 2 to 4 percent are obtained (table I). The accuracy of prediction of flame velocities for mixtures containing different concentrations of oxygen varies from hydrocarbon to hydrocarbon. For 2,2,4-trimethylpentane, the accuracy is about 1 percent; for ethylene, 5 percent; and for propane, 15 percent.

The ethylene data are again considered in order to determine the accuracy with which the  $\bar{K}_\Sigma$  from the equivalence-ratio data predicts the effects of temperature and oxygen concentration on flame velocity. The deviations for the initial-temperature data varied from -8 to +45 percent with a mean deviation of 27 percent. For the oxygen data the deviations varied from +1 to +19 percent with a mean value of +10 percent.

#### Empirical Correlations

A correlation was obtained (reference 26) by which maximum flame velocities of various hydrocarbons in air could be predicted with an average deviation of 2 percent. The predicted flame velocity is calculated from the sum of the contributions of various H-C bonds in the fuel molecule according to the following relationship:

$$U = N_A K_A + N_B K_B + N_C K_C + \dots$$

where  $N_A$ ,  $N_B$ ,  $N_C$ ,  $N_D$ ,  $N_E$ ,  $N_F$ ,  $N_G$ , and  $N_H$  are the numbers of methane, primary, secondary, tertiary, alkene, alkyne, cyclohexyl and aromatic C-H bonds, respectively, per unit volume of hydrocarbon-air mixture, and  $K_A$ ,  $K_B$ ,  $K_C$ , . . . are the flame-speed coefficients of these bonds. For the special cases of C-H bonds on carbon atoms placed alpha to the alkyne  $C \equiv C$  bond, a factor  $M = 0.96$  was introduced into terms representing these alpha bonds. Correlation coefficients (table II) established from 34 hydrocarbons excluding ethylene then gave an average deviation of 1.9 percent in the ratio of predicted to measured flame velocity.

A correlation was also observed between the equivalence ratio for maximum flame velocity and the total bond dissociation energy of the fuel. As shown in table III, the total bond dissociation energy per unit volume of the hydrocarbon-air mixture corresponding to the maximum flame velocity is nearly constant, with an average deviation of only 0.9 percent from the average value. This deviation is less than one-third of that obtained by simply assuming that the maximum will occur at an average equivalence ratio of 1.15. Bond energy calculations for 37 hydrocarbons similar to those presented in table III had an average deviation of 1.6 percent.

For the equivalence-ratio data, linear relationships were found between flame velocity and the logarithm of the equivalence ratio  $\Phi$ , where  $\Phi < \Phi_{\max}$ . An interesting variation is the plot of flame velocity against the total bond dissociation energy of the fuel per unit volume of mixture in figure 2 for pentane, ethylene, and propyne mixtures with air. It may be seen that the correlation is linear for the lean mixtures and that the line extrapolates to the lean limit for flame propagation (where  $U = 0$ ) as determined in the 1-inch flame tube. For these data, determined by the tube method for three hydrocarbons, good estimates of the maximum flame velocities are obtained by reading from the curves at a total bond dissociation energy of 1.75 kilocalories per liter. This constant bond-energy value of 1.75 kilocalories per liter for this correlation does not equal the bond energy of the hydrocarbon concentration corresponding to the maximum flame velocity which was previously calculated to be 1.96 kilocalories per liter. Work with other flame-velocity data shows that both the position of the horizontal line and the slopes of the lines for specific hydrocarbons depend somewhat on the method of measurement of flame velocity.

Empirical equations predicting the effect of initial mixture temperature on flame velocity with mean deviations of approximately 2 percent for the range from  $200^\circ$  to  $615^\circ$  K are (reference 5):

for methane

$$U = 10 + 7.40 \times 10^{-5} T_0^{2.23}$$

for propane

$$U = 10 + 3.42 \times 10^{-4} T_0^{2.00}$$

for ethylene

$$U = 10 + 2.59 \times 10^{-3} T_0^{1.74}$$

Empirical relationships were found which predict the effect of oxygen concentration (for the experimental range covered) and limited temperature ( $311^{\circ}$ - $422^{\circ}$  K) on the flame velocity for the three hydrocarbons studied (reference 6):

for 2,2,4-trimethylpentane

$$U = 0.133 T_0^{1.40} (\alpha - 0.120)$$

for propane

$$U = 0.766 T_0^{1.16} (\alpha - 0.133)$$

for ethylene

$$U = 0.998 T_0^{1.18} (\alpha - 0.133)$$

The accuracy of prediction was about 3 percent for ethylene and 2,2,4-trimethylpentane and 6 percent for propane.

#### CONCLUDING REMARKS

The semitheoretical calculations of this paper are dependent on the assumption that thermal equilibrium is attained at the end of the combustion zone. Actual flame temperatures and product concentrations would differ from equilibrium values if (a) equilibrium is not attained, (b) any appreciable reaction takes place at the initial temperature, or (c) there is a large chain branching term affecting the radical distribution in and ahead of the flame zone. These calculations are also dependent on the inherent assumptions of the approximate theoretical equations and the methods used to calculate transport properties. Within these limitations, the results of the calculations may be generalized as follows:

1. The Semenov bimolecular equation (thermal mechanism), the Tanford-Pease square-root law (active-particle diffusion mechanism), and the Manson modification of the momentum-pressure-drop equation (including diffusion of active particles, but not chemical kinetics) will all predict relative changes in flame velocity caused by changes in hydrocarbon structure, initial temperature, equivalence ratio (limited range), or oxygen concentration. The accuracies of the predictions are summarized in table I.

2. Low-temperature activation energies may be used in the Semenov equation to give good relative predictions of flame velocities for variations in initial temperature, equivalence ratio, and oxygen concentration. Only the bimolecular fuel-oxygen reaction is considered in this paper; other combinations such as fuel and hydrogen atoms should be investigated to determine whether the kinetics indicated for such other reactions are not more probable than for the fuel-oxygen case.

3. The average "specific rate constants" ( $\bar{k}_a$ ) obtained with the Tanford-Pease equation for molecular fuel - active particle reactions behave as Arrhenius rate constants only with the data on the effect of initial temperature, not with the equivalence-ratio or oxygen-concentration data. The relative predictions obtained by this equation are not very sensitive either to the temperature dependence assigned to the diffusion coefficients or to the recombination factor computed for hydrogen atoms; these factors do appreciably affect absolute predictions of flame velocity or, conversely, determinations of steric factors from experimental flame velocities. Regarding active particles considered, better results are generally obtained for hydrocarbon flames when H, OH, and O are considered rather than H alone; this is particularly true for studies of the effect of equivalence ratio.

4. For the equivalence-ratio and oxygen-concentration data, considerably better relative predictions are obtained from the Manson equation when the pressure drop across the flame front is considered to be due to H, OH, and O than when only H atoms are taken into account. Further thought should be given as to how this pressure drop should be computed, taking into account any net diffusional flow of any component between the flame front and the unburned gas.

5. The example presented by the ethylene data shows that an empirically determined rate constant or proportionality factor from equivalence-ratio data at atmospheric pressure and room temperature may predict the effect of initial temperature or oxygen concentration within approximately 20 percent by the Semenov or Tanford-Pease equation and within approximately 30 percent by the Manson equation.

6. For engineering applications, the effects of the parameters studied could be estimated just as satisfactorily, and more easily, by



one or another of the empirical correlations indicated, as compared with the three semitheoretical equations considered. However, the use of the semitheoretical equations in some cases reduces the number of constants required.

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TABLE I - PERCENTAGE MEAN DEVIATIONS IN RATIO OF PREDICTED TO MEASURED FLAME VELOCITY

NACA RM E52J13

Type of data	Empirical correlation		Semenov bimolecular equation	Tanford-Pease equation			Manson equation	
	Form of correlation	Deviation (percent)		Using $\bar{k}_H$	Using $\bar{k}_a$	Using $\bar{E}$ from $T_0$ data	Using $\bar{K}_H$	Using $\bar{K}_\Sigma$
Hydrocarbon structure <sup>a</sup>	$U = N_A K_A + N_B K_B + \dots$	1.9		3.3	3.5		3.6	3.8
Initial temperature <sup>b</sup> (200° to 615° K)	$U = a + bT_0^n$							
Methane		2.1	2.7	11.8	7.8	0.8	10.3	10.1
Propane		1.6	2.0	12.5	6.1		10.0	13.0
Ethylene		1.4	1.8	9.4	5.8	1.8	12.0	13.8
Equivalence ratio (range limited, see text)	$U = a (\log B) + b$							
Methane, 307° K <sup>b</sup>			7.4	25.8	5.7	7.0	23.6	1.8
Pentane <sup>a</sup>		4.9	3.0	64.8	3.8		39.9	3.6
Propane, 302° K <sup>b</sup>			4.0		0.6		15.1	1.2
Ethylene <sup>a</sup>		2.2	5.0	16.6	3.7	3.3	10.0	1.8
Oxygen concentration <sup>c</sup>								
Propane, 311° K	} $U = aT_0^n (\alpha-b)$	} 5.5	17.3		6.4		16.5	15.2
422° K			12.4		5.2		12.7	13.0
Ethylene, 311° K	} $U = aT_0^n (\alpha-b)$	} 3.2	4.0		4.9		7.5	5.2
422° K			3.0		4.6		6.8	5.3
2,2,4-trimethyl- pentane	} $U = a (\alpha-b)$	} 2.0	6.4		4.5		7.3	1.1
			422° K	2.7	7.3		4.0	8.2
	$U = aT_0^n (\alpha-b)$	2.6						

<sup>a</sup>Data determined by tube method at room temperature (reference 2).

<sup>b</sup>Data determined by Bunsen burner method, shadow cone (reference 5).

<sup>c</sup>Data determined by Bunsen burner method, schlieren cone (references 6 and 7).



TABLE II - EMPIRICAL COEFFICIENTS FOR CALCULATING MAXIMUM FLAME  
VELOCITY FROM HYDROCARBON STRUCTURE (REFERENCE 26)

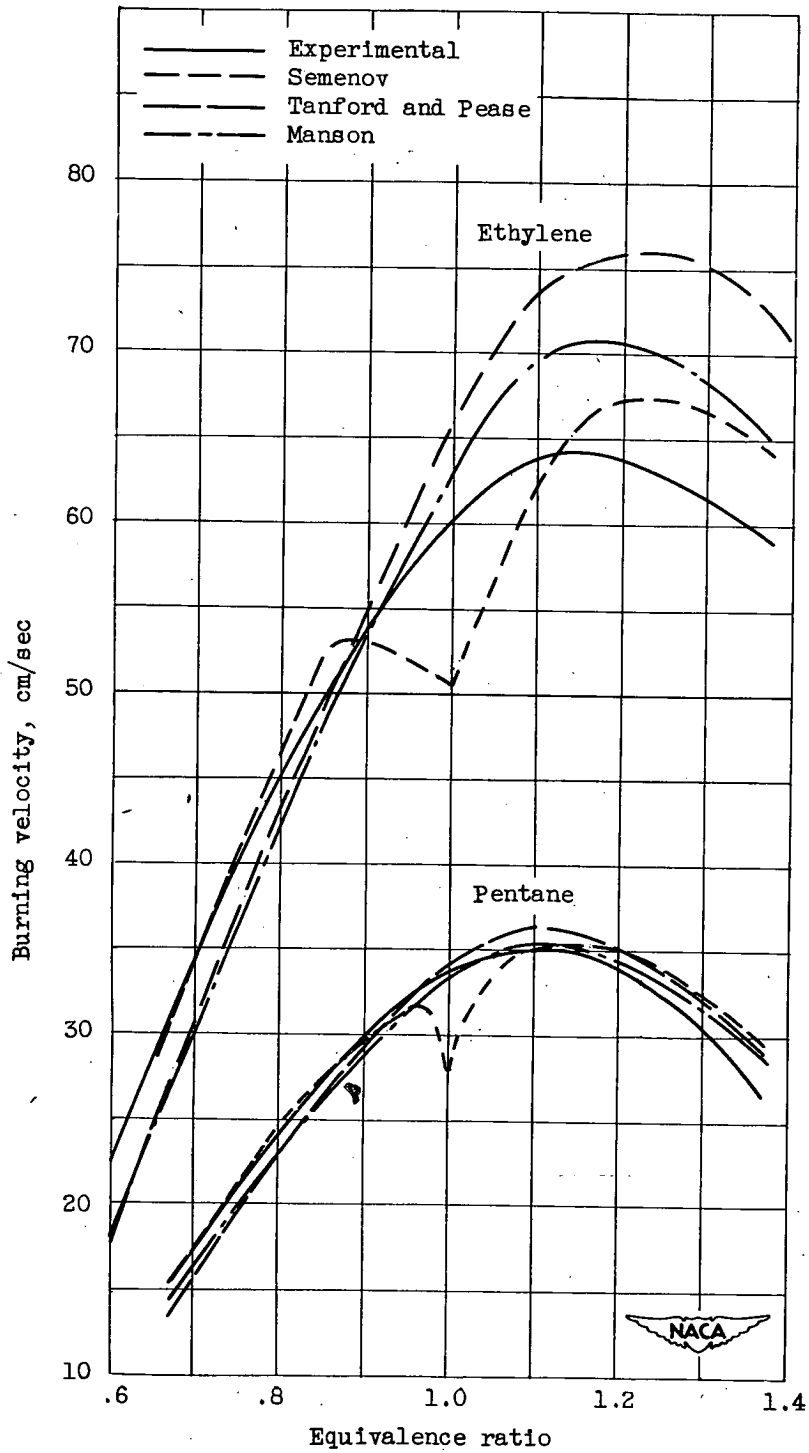


Type C-H bond		Coefficient
Methane	$K_A$	$35.2 \times 10^{-19}$
Primary	$K_B$	42.5
Secondary	$K_C$	47.5
Tertiary	$K_D$	45.4
Cyclohexyl	$K_G$	50.5
Alkene	$K_E$	80.7
Aromatic	$K_H$	84.3
Alkyne	$K_F$	223.9

TABLE III - BOND DISSOCIATION ENERGIES FOR  $C_4$  AND  $C_6$  HYDROCARBONS  
AT CONCENTRATION FOR MAXIMUM FLAME VELOCITY

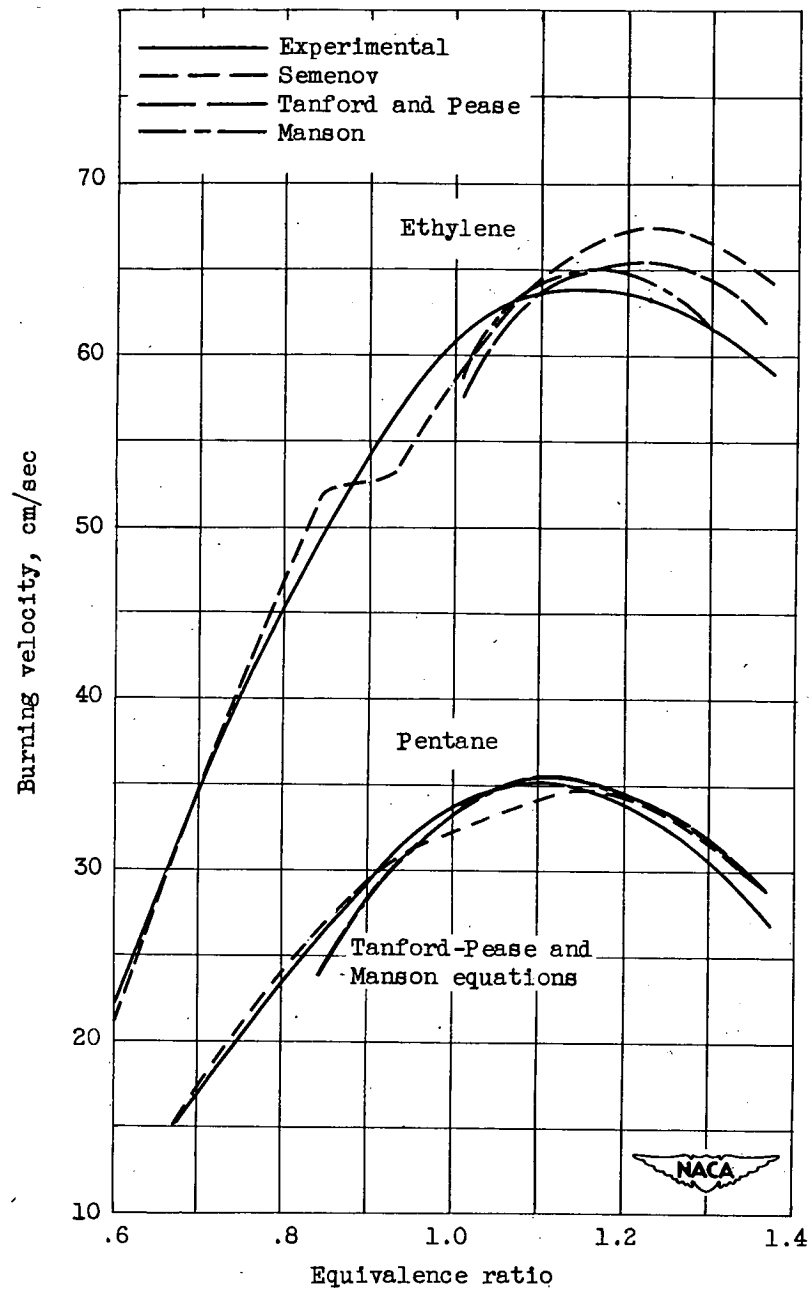
Hydrocarbon	Equiva- lence ratio for max- imum $U$ , $\varphi_{max}$	Deviation of $\varphi_{max}$ from average $\varphi_{max}$ (percent)	Dissocia- tion energy of hydro- carbon $\left(\frac{\text{kcal}}{\text{g-mole}}\right)$ (a)	Dissocia- tion energy of mixture at $\varphi_{max}$ $\left(\frac{\text{kcal}}{\text{liter}}\right)$	Devia- tion from average (percent)
Butane	1.09	5.5	1250	1.93	2.0
Hexane	1.16	0.9	1791	2.00	1.5
2-Methylpropane	1.11	3.6	1257	1.94	1.5
2,2-Dimethyl- butane	1.12	2.5	1821	1.97	0.0
Butene-1	1.17	1.7	1133	1.98	0.5
Hexene-1	1.16	0.9	1680	2.02	2.5
Isobutene	1.14	0.9	1147	1.97	0.0
2-Methylpentene-1	1.19	3.4	1603	1.99	1.0
Butyne-1	1.17	1.7	1016	1.95	1.0
Hexyne-1	1.21	5.0	1564	1.97	0.0
4-Methylpentyne	1.18	2.5	1574	1.95	1.0
Benzene	1.34	14.2	1305	1.96	0.5
Average	1.15	3.29	----	1.96	0.9

<sup>a</sup>Single-bond energies from reference 27. Multiple-bond energies from reference 28: 151.2 kcal/g-mole for C=C in olefins and cyclic compounds; 198.5 kcal/g-mole for C≡C bond.



(a) Complete experimental range.

Figure 1. - Predictions of the effect of equivalence ratio on flame velocity.



(b) Limited range.

Figure 1. - Concluded. Predictions of the effect of equivalence ratio on flame velocity.

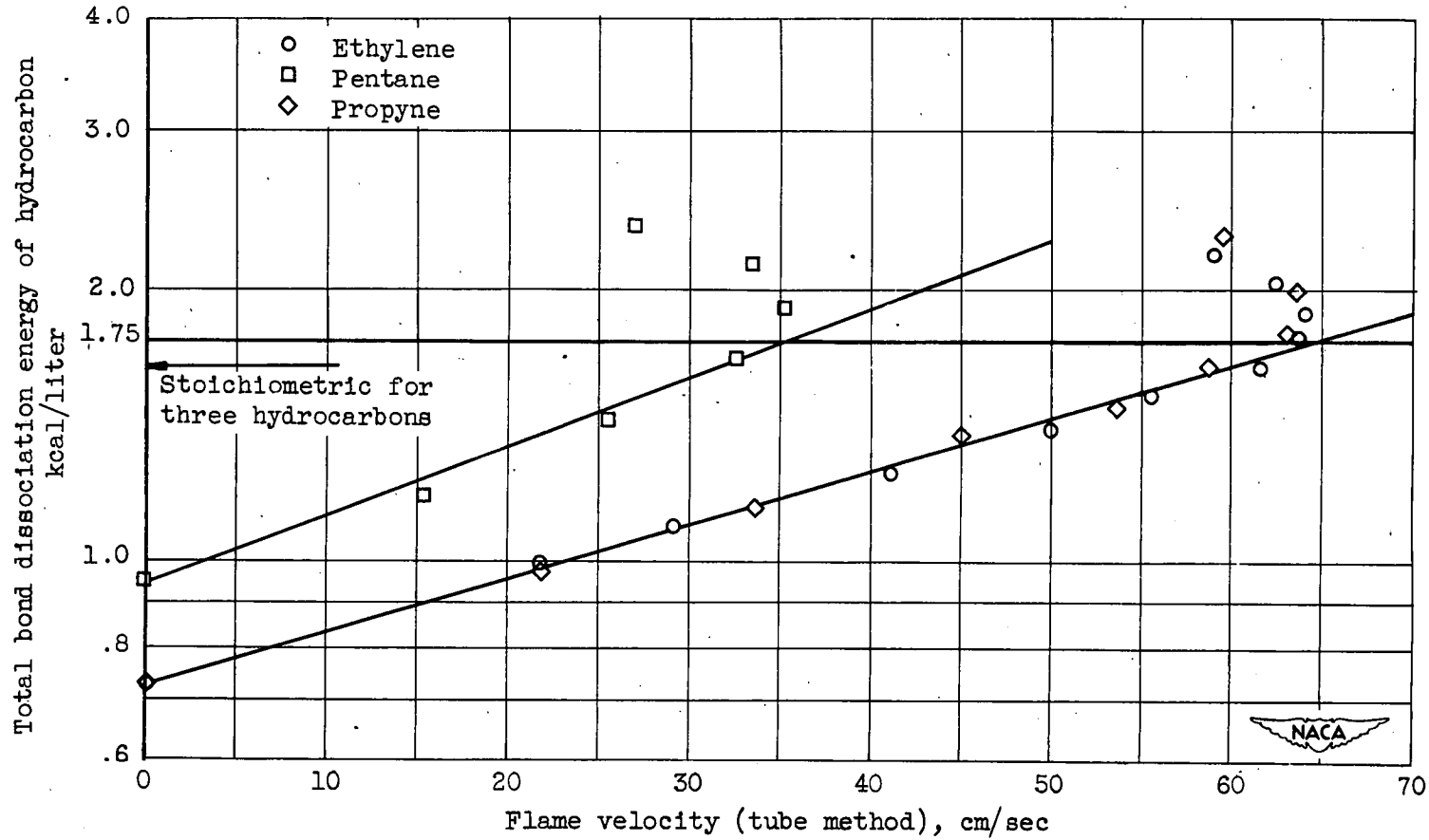


Figure 2. - Empirical correlation for equivalence ratio data.