

Bose-Einstein Correlations in charged current muon-neutrino interactions in the NOMAD experiment at CERN

NOMAD Collaboration

P. Astierⁿ D. Autiero^h A. Baldisseri^r M. Baldo-Ceolin^m
M. Bannerⁿ G. Bassompierre^a K. Benslamaⁱ N. Besson^r
I. Bird^{h,i} B. Blumenfeld^b F. Bobisut^m J. Bouchez^r S. Boyd^t
A. Bueno^{c,x} S. Bunyatov^f L. Camilleri^h A. Cardini^j
P.W. Cattaneo^o V. Cavasinni^p A. Cervera-Villanueva^{h,v}
R.C. Challis^k A. Chukanov^f G. Collazuol^m G. Conforto^{h,u,1},
C. Conta^o M. Contalbrigo^m R. Cousins^j D. Daniels^c
H. Degaudenziⁱ T. Del Prete^p A. De Santo^{h,p} T. Dignan^c
L. Di Lella^{h,z} E. do Couto e Silva^h J. Dumarchezⁿ M. Ellis^t
G.J. Feldman^c R. Ferrari^o D. Ferrère^h V. Flaminio^p
M. Fraternali^o J.-M. Gaillard^a E. Gangler^{h,n} A. Geiser^{e,h}
D. Geppert^e D. Gibin^m S. Gninenko^{h,l} A. Godley^s
J.-J. Gomez-Cadenas^{h,v} J. Gosset^r C. Gößling^e M. Gouanère^a
A. Grant^h G. Graziani^g A. Guglielmi^m C. Hagner^r
J. Hernando^v D. Hubbard^c P. Hurst^c N. Hyett^k E. Iacopini^g
C. Josephⁱ F. Jugetⁱ N. Kent^k M. Kirsanov^l O. Klimov^f
J. Kokkonen^h A. Kovzelev^{l,o} A. Krasnoperov^{a,f} S. Lacaprara^m
C. Lachaudⁿ B. Lakić^w A. Lanza^o L. La Rotonda^d
M. Laveder^m A. Letessier-Selvonⁿ J.-M. Levyⁿ L. Linssen^h
A. Ljubičić^w J. Long^b A. Lupi^g V. Lyubushkin^f
A. Marchionni^g F. Martelli^u X. Méchain^r J.-P. Mendiburu^a
J.-P. Meyer^r M. Mezzetto^m S.R. Mishra^{c,s} G.F. Moorhead^k
D. Naumov^f P. Nédélec^a Yu. Nefedov^f C. Nguyen-Mauⁱ
D. Orestano^q F. Pastore^q L.S. Peak^t E. Pennacchio^u
H. Pessard^a R. Petti^{h,o} A. Placci^h G. Polesello^o D. Pollmann^e
A. Polyarush^l B. Popov^{f,n} C. Poulsen^k L. Rebuffi^m J. Rico^x
P. Riemann^e C. Roda^{h,p} A. Rubbia^{h,x} F. Salvatore^o

arXiv:hep-ex/0404011v1 8 Apr 2004

K. Schahmanecheⁿ B. Schmidt^{e,h} T. Schmidt^e A. Sconza^m
 M. Sevier^k D. Sillou^a F.J.P. Soler^{h,t} G. Sozziⁱ D. Steele^{b,i}
 U. Stiegler^h M. Stipčević^w Th. Stolarczyk^r M. Tareb-Reyesⁱ
 G.N. Taylor^k V. Tereshchenko^f A. Toropin^ℓ A.-M. Touchardⁿ
 S.N. Tovey^{h,k} M.-T. Tranⁱ E. Tsesmelis^h J. Ulrichs^t
 L. Vacavantⁱ M. Valdata-Nappi^{d,y} V. Valuev^{f,j} F. Vannucciⁿ
 K.E. Varvell^t M. Veltri^u V. Vercesi^o G. Vidal-Sitjes^h
 J.-M. Vieiraⁱ T. Vinogradova^j F.V. Weber^{c,h} T. Weisse^e
 F.F. Wilson^h L.J. Winton^k B.D. Yabsley^t H. Zaccone^r R. Zei^p
 K. Zuber^e P. Zuccon^m

^a*LAPP, Annecy, France*

^b*Johns Hopkins Univ., Baltimore, MD, USA*

^c*Harvard Univ., Cambridge, MA, USA*

^d*Univ. of Calabria and INFN, Cosenza, Italy*

^e*Dortmund Univ., Dortmund, Germany*

^f*JINR, Dubna, Russia*

^g*Univ. of Florence and INFN, Florence, Italy*

^h*CERN, Geneva, Switzerland*

ⁱ*University of Lausanne, Lausanne, Switzerland*

^j*UCLA, Los Angeles, CA, USA*

^k*University of Melbourne, Melbourne, Australia*

^ℓ*Inst. Nucl. Research, INR Moscow, Russia*

^m*Univ. of Padova and INFN, Padova, Italy*

ⁿ*LPNHE, Univ. of Paris VI and VII, Paris, France*

^o*Univ. of Pavia and INFN, Pavia, Italy*

^p*Univ. of Pisa and INFN, Pisa, Italy*

^q*Roma Tre University and INFN, Rome, Italy*

^r*DAPNIA, CEA Saclay, France*

^s*Univ. of South Carolina, Columbia, SC, USA*

^t*Univ. of Sydney, Sydney, Australia*

^u*Univ. of Urbino, Urbino, and INFN Florence, Italy*

^v*IFIC, Valencia, Spain*

^w*Rudjer Bošković Institute, Zagreb, Croatia*

^x*ETH Zürich, Zürich, Switzerland*

^y*Now at Univ. of Perugia and INFN, Italy*

^z*Now at Scuola Normale Superiore, Pisa, Italy*

Abstract

Bose-Einstein Correlations in one and two dimensions have been studied, with high statistics, in charged current muon-neutrino interaction events collected with the NOMAD detector at CERN. In one dimension the Bose-Einstein effect has been analyzed with the Goldhaber and the Kopylov-Podgoretskii phenomenological parametrizations. The Goldhaber parametrization gives the radius of the pion emission region $R_G = 1.01 \pm 0.05(\text{stat})_{-0.06}^{+0.09}(\text{sys})$ fm and for the chaoticity parameter the value $\lambda = 0.40 \pm 0.03(\text{stat})_{-0.06}^{+0.01}(\text{sys})$. Using the Kopylov-Podgoretskii parametrization yields $R_{KP} = 2.07 \pm 0.04(\text{stat})_{-0.14}^{+0.01}(\text{sys})$ fm and $\lambda_{KP} = 0.29 \pm 0.06(\text{stat})_{-0.04}^{+0.01}(\text{sys})$. Different parametrizations of the long-range correlations have been also studied. The two-dimensional shape of the source has been investigated in the longitudinal co-moving frame. A significant difference between the transverse and the longitudinal dimensions is observed. The high statistics of the collected sample allowed the study of the Bose-Einstein correlations as a function of rapidity, charged particle multiplicity and hadronic energy. A weak dependence of both radius and chaoticity on multiplicity and hadronic energy is found.

¹ Deceased

1 Introduction

The quantum mechanical wave function of two identical bosons has to be symmetric under particle exchange. The symmetrization gives rise to an observable interference pattern which enhances the number of identical bosons emitted close to one another in phase space. Such Bose-Einstein Correlations (BEC) were observed for the first time in astronomical measurements of photon pairs emitted by stars [1] and soon after for like-sign hadrons produced in $p\bar{p}$ annihilations [2]. Since then BEC, were also measured in several other types of particle interactions (for a review see [3]). The shape of the BEC depends on the spatial and temporal distributions of the boson source and on its degree of coherence. The theoretical aspects of the BEC were developed in the papers of Kopylov and Podgoretskii [4] and Cocconi [5]. From these studies it appears that the measurements of BEC may be important to gain an understanding on the dynamics of the particle interactions yielding like-sign bosons in the final state.

Previous measurements of the BEC effects in neutrino interactions have been performed by the Big European Bubble Chamber Collaboration (BEBC) [6] including data collected on a variety of targets by both BEBC at CERN and the 15-foot Bubble Chamber at Fermilab. Nevertheless, the number of events globally collected by these experiments is still about one order of magnitude smaller than the data set collected by NOMAD and used in this paper.

2 The phenomenology of BEC

The BEC effect can be parametrized in terms of the two particle correlation function R defined as:

$$R(p_1, p_2) = D(p_1, p_2)/D_0(p_1, p_2) \quad (1)$$

where $p_{1,2}$ are the particle four-momenta, $D(p_1, p_2)$ is the measured two-particle density and $D_0(p_1, p_2)$, the particle density in the absence of BEC. $D_0(p_1, p_2)$ should include any other two-particle correlations such as those coming from phase space, long-range correlations, charge effects, etc. which in the ratio should be divided out leaving only the BEC effects. According to the Goldhaber parametrization [2], which assumes that the emitting sources of identical bosons are described by a spherical Gaussian density function, BEC are usually parametrized as:

$$R(Q) = 1 + \lambda \exp\left(-R_G^2 Q^2\right) \quad (2)$$

where $Q^2 = -(p_1 - p_2)^2 = M_{\pi\pi}^2 - 4m_\pi^2$, with $M_{\pi\pi}$ the invariant mass of the pion pair, R_G the width of the Gaussian distributed emitting source and m_π the pion mass. The chaoticity (or incoherence) parameter λ measures the degree of coherence in pion production, i.e. the fraction of pairs of identical particles that undergo interference ($0 \leq \lambda \leq 1$).

The Kopylov-Podgoretskii (KP) parametrization [4] corresponds to a radiating spherical surface of radius R_{KP} with pointlike oscillators of lifetime τ :

$$R(Q_t, Q_0) = 1 + \lambda \left[4J_1^2(Q_t R_{KP}) / (Q_t R_{KP})^2 \right] / \left[1 + (Q_0 \tau)^2 \right] \quad (3)$$

where J_1 is the first-order Bessel function, $\vec{p} = \vec{p}_1 + \vec{p}_2$, $\vec{Q} = \vec{p}_1 - \vec{p}_2$, $Q_0 = |E_1 - E_2|$, $Q_t = |\vec{Q} \times \vec{p}| / |\vec{p}|$. This parametrization is not Lorentz invariant and the variables are calculated in the centre of mass of the hadronic final state. It can be shown that at small values of Q_t and Q_0 the relation $R_{KP} \approx 2R_G$ is expected [6].

The shape of the hadronic source can be measured by studying BEC as a function of the components of the vector \vec{Q} . It is convenient to perform this study in the so-called longitudinal centre of mass system (LCMS). This reference system is defined for every particle pair as that where $\vec{p} = \vec{p}_1 + \vec{p}_2$ is perpendicular to the axis defined by the hadronic jet direction (see fig. 1). With this choice, possible effects caused by the Lorentz boost are avoided. In the LCMS, \vec{Q} is decomposed into the following components: Q_{long} , parallel to the hadronic jet axis; $Q_{t,out}$, collinear with \vec{p} and the complementary $Q_{t,side}$, perpendicular to both Q_{long} and $Q_{t,out}$. In this analysis we use the longitudinal component $Q_{\parallel} = Q_{long}$ and the perpendicular component $Q_{\perp} = \sqrt{Q_{t,out}^2 + Q_{t,side}^2}$ (see fig.1). The parametrization of the correlation is then performed separately for the longitudinal Q_{\parallel} and transverse Q_{\perp} components as suggested in ref [2]:

$$R(Q_{\parallel}, Q_{\perp}) = 1 + \lambda \exp \left(- Q_{\parallel}^2 R_{\parallel}^2 - Q_{\perp}^2 R_{\perp}^2 \right) \quad (4)$$

the longitudinal and transverse dimensions of the hadron source being represented by R_{\parallel} and R_{\perp} , respectively.

3 Experimental procedure

3.1 The NOMAD experiment

The main goal of the NOMAD experiment [7] was the search for $\nu_{\mu} \rightarrow \nu_{\tau}$ oscillations in a wide-band neutrino beam from the CERN SPS. The full data sample, corresponding to about 1.3 million ν_{μ} charged-current (CC) interactions collected in four years of data taking (1995–1998) in the detector fiducial volume, is used in the present analysis. The data are compared to the results of a Monte Carlo simulation based on modified versions of the LEPTO 6.1 [8] and the JETSET 7.4 [9] generators for neutrino interactions and on a GEANT 3.21 [10] based program for the detector response. BEC effects are not included in the Monte Carlo. For the analysis reported below we have used a Monte Carlo sample of size comparable to the data.

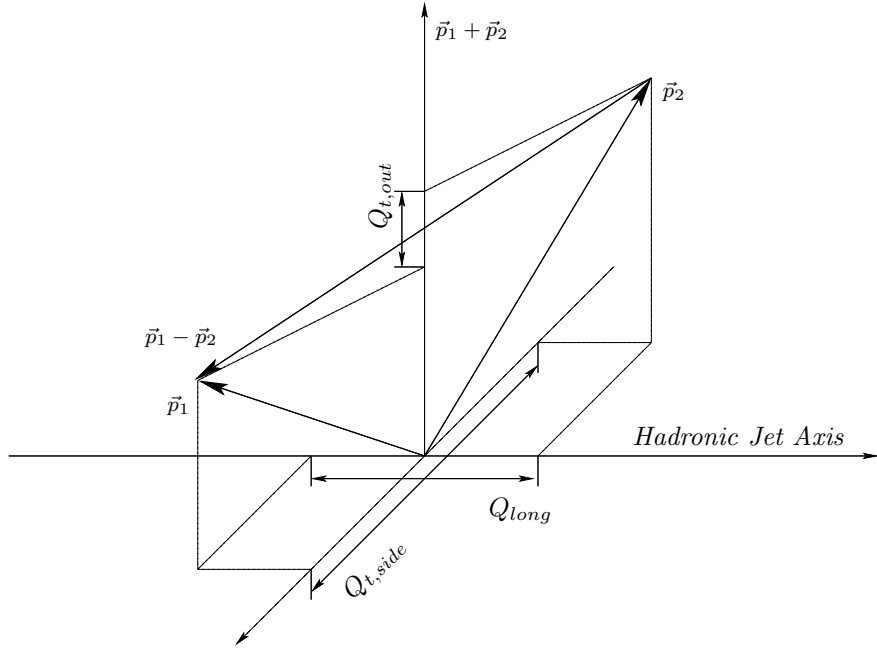


Fig. 1. *The definition of the LCMS system.*

3.2 *The NOMAD detector*

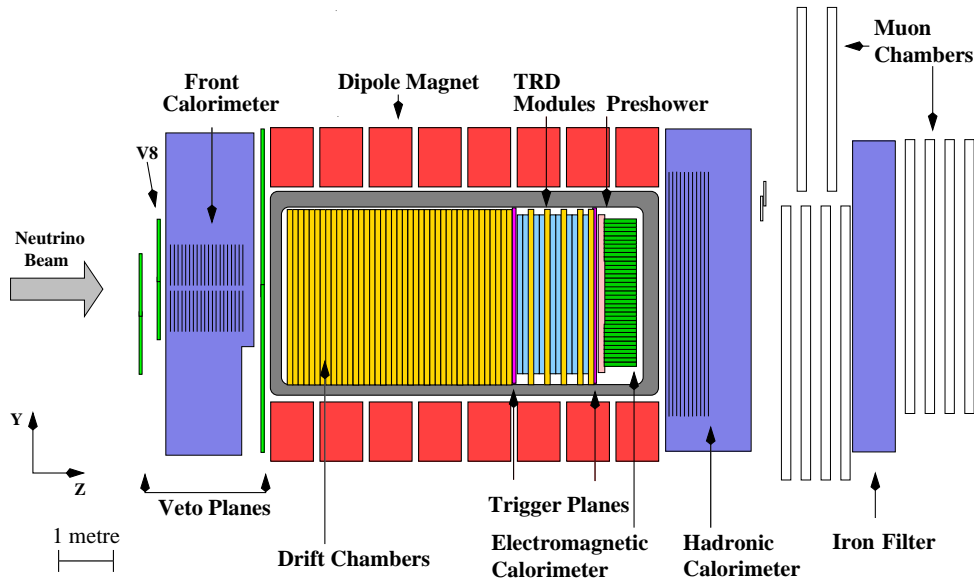


Fig. 2. *NOMAD Apparatus.*

The tracking capabilities of the detector are essential for the study of BEC. The NOMAD detector shown in fig. 2 is especially well suited for this. It consists of an active target of 44 drift chambers, with a total fiducial mass of 2.7 tons located in a 0.4 T dipole magnetic field. The drift chambers (DC) [11], made of low Z material (mainly carbon), serve the dual role of a nearly isoscalar target for neutrino interactions and of a tracking

medium. These drift chambers provide an overall efficiency for charged particle reconstruction greater than 95% and a momentum resolution which can be parametrized as $\frac{\sigma_{|\vec{p}|}}{|\vec{p}|} = \frac{0.05}{\sqrt{L}} \oplus \frac{0.008|\vec{p}|}{\sqrt{L^5}}$ where the track length L is in metres and the track momentum $|\vec{p}|$ in GeV/c. This amounts to a resolution $\leq 3.5\%$ for $|\vec{p}| \leq 10$ GeV/c. Reconstructed tracks are used to determine the event topology (the assignment of tracks to vertices) and to reconstruct the vertex position and the track parameters at each vertex (primary, secondary, V0, etc. . .). A transition radiation detector (TRD) [12] is used for electron identification. The pion rejection achieved for isolated tracks is 10^3 with a 90% electron identification efficiency. A lead-glass electromagnetic calorimeter (ECAL) [13] located downstream of the tracking region provides an energy resolution of $3.2\%/\sqrt{E[\text{GeV}]} \oplus 1\%$ for electromagnetic showers and is essential to measure the total energy flow in neutrino interactions. In addition an iron absorber and a set of drift chambers located after the electromagnetic calorimeter are used for muon identification, providing a muon detection efficiency of 97% for momenta greater than 5 GeV/c.

3.3 Event selection

The identification of ν_μ CC events requires the presence of a primary negative muon in the final state, i.e. a track segment in the muon detector matched to a track reconstructed in the drift chambers. The muon momentum and its transverse component (relative to the neutrino beam) are required to be greater than 5 GeV/c and 0.5 GeV/c, respectively. Preliminary cuts are applied to ensure good quality event reconstruction²:

- Number of primary charged tracks (excluding the muon) $N_{ch} \geq 2$;
- Muon energy $E_\mu \geq 5$ GeV and hadronic energy $E_{hadrons} \geq 5$ GeV;
- Hadronic invariant mass $W \geq 2$ GeV (to reject quasi-elastic events and baryon resonance production);
- Event vertex within the fiducial region of the DC target.

Tracks to be used for BEC are then selected using the following criteria:

- Only primary tracks are selected, i.e. either belonging or pointing to the primary vertex; in the latter case, to avoid potential dangerous contamination from photon conversions, the track first hit must occur no further than 15 cm downstream of the vertex along the detector axis (the z axis);
- A minimum momentum of the track is required: $|\vec{p}_{track}| \geq 100$ MeV/c;
- A minimum number of hits is used to build the track: $N_{hits} \geq 12$;
- A good momentum resolution is required: $\frac{\Delta|\vec{p}|}{|\vec{p}|} \leq 6\%$, where $\Delta|\vec{p}|$ is the the uncertainty on the momentum of that track calculated by the reconstruction program;
- The track should not be identified as an electron by the TRD and the ECAL;
- The track should not be identified as a proton by the range-momentum correlation method (see ref. [15] for details).

² additional details on the analysis can be found in [14].

The total number of events selected by these cuts is 398K. These events contain 544K ($++$), 143K ($--$), and 852K ($+ -$) pairs.

After the event and track quality cuts, we have performed a preliminary analysis of the simulated events to assess the purity of the track identification. The tracks investigated are those obtained from the full Monte Carlo simulation. An appropriate algorithm allowed an association between the reconstructed tracks and those generated at the primary vertex. We have found that the positive and negative samples of particles used for BEC studies contain respectively $\approx 61\%$ of π^+ and $\approx 77\%$ of π^- . The relative contributions of various positive and negative particles in NOMAD entering the correlation plots are listed in table 1. The tracks labeled “not recognized” are those for which no association with a

Particle	Percentage
π^+	61.2%
p	18.4%
K^+	5.6%
μ^+	0.1%
e^+	0.2%
Not recognized	14.5%
π^-	77.2%
\bar{p}	2.4%
K^-	7.8%
e^-	0.3%
Not recognized	12.3%

Table 1

Composition of the charged particle sample used in the analysis.

generated primary track was found. These tracks are produced by secondary interactions or photon-conversions. As we can see from table 1 the negative tracks exhibit a better pion purity than the positive ones. Contaminations from electrons and positrons which are mainly present in the “not recognized” samples could be dangerous since these particles come from photon conversions and therefore they can populate the low Q region where BEC effects are expected. This problem, together with the effects caused by the proton and kaon contaminations, will be discussed in section 4.

The Monte Carlo simulation was also used to verify the experimental resolution in the determination of the BEC parameters. BEC effects are expected to occur in any of the kinematical variables Q , Q_t , Q_0 , Q_{\parallel} , Q_{\perp} at small values of these parameters (≤ 0.2 GeV) and we have verified that the resolution in any of these variables is ≤ 0.02 GeV. The BEC parameters are obtained by fits to the experimental distributions in the interval 0.0-1.5 GeV. This interval is large enough to study possible long-range correlations as well.

4 The reference samples

We have studied several alternatives for the choice of the reference sample $D_0(p_1, p_2)$ used in eq. 1. In principle the Monte Carlo events, which do not contain BEC, would be good candidates. However the capability of the Monte Carlo to accurately reproduce the data (except for BEC) especially in the tiny phase-space region where BEC are present is limited and other methods based on the data themselves must be found. Several methods have been used in previous experiments to build the reference sample from the data (see for example [6]). They are:

- The reference sample is formed of all unlike-sign pairs;
- The reference sample is formed by building a so called “mixed event”: a hadron from one event is combined with a hadron of the same charge, chosen at random from another event that has approximately the same kinematical characteristics: total hadron momentum, hadron energy, charged multiplicity...
- The reference sample is formed by pairing unlike-charge hadrons from the same event after the transverse momenta \vec{p}_t (with respect to the current direction) have been interchanged at random in the hadronic centre-of-mass system (c.m.s).

We have carefully tested the three methods with a full Monte Carlo simulation (discussed in more detail later in this section) which includes also the response of the detector. The Monte Carlo results reproduce correctly the inclusive particle distribution in neutrino interactions, but not the correlations among particles. This Monte Carlo is therefore adequate to study the bias introduced by the reference sample. In fact, in the absence of BEC, the distributions in R should be flat or, in any case, have no structure at small Q (≤ 0.2 GeV) which would distort the study of R . We have found that none of the three reference samples completely fulfills this requirement, however the unlike-sign one was eventually found to be the most adequate in the BEC region. Moreover this reference sample has been used by the great majority of previous BEC studies.

BEC effects are then investigated by looking in the data at the following ratio:

$$R(Q) = \frac{\text{“like-sign” pion-pairs}}{\text{“unlike-sign” pion-pairs}} = \frac{N_{++}(Q) + N_{--}(Q)}{N_{+-}(Q)} \quad (5)$$

The Monte Carlo samples are used to estimate possible spurious BEC effects from non-pion contaminations present in the sample as discussed in the following section.

4.1 Systematic effects

In the analysis, all secondary charged particles have been assumed to be pions, unless identified as muons, electrons or protons. However, as seen in section 3 for simulated events, there is a fraction of 39% and 23%, respectively of these positive and negative

particles, which are not pions. Here we want to study how the BEC could be changed by these misidentified tracks and by the use of the unlike-sign sample as a reference. These effects could manifest themselves in three distinct ways:

- BEC for like-sign kaons and correlations for like-sign fermions (electrons, protons). The BEC for kaons were measured at LEP and showed characteristics very similar to those of pions. Fermion pairs, instead, could exhibit an anticorrelation effect. However, the number of like-sign kaon and fermion pairs is very small and their contribution is negligible.
- Pairs of like-sign, but not identical particles in the numerator of eq. 5, for example $K^+\pi^+$ pairs, have no BEC. This contribution could bias the value of λ .
- Unlike-sign pairs in the denominator of eq. 5 include contributions from K^0 and resonances such as ρ , ω , as well as from electron-positron pairs from photon conversions. The latter could severely affect the distributions of R at small Q .

Fig. 3 (a) shows the simulated Q distributions for reconstructed particles associated to generated primary pion pairs for like and unlike-charge distributions. One can notice that the unlike-sign pair distribution exhibits strong enhancements around $Q \approx 0.35$ GeV and $Q \approx 0.7$ GeV due to K^0 and ρ decays, respectively. For this reason the Q intervals $0.3 \leq Q \leq 0.45$ and $0.6 \leq Q \leq 0.825$ GeV have been excluded from the analysis. The ratio like/unlike pairs, eq. 5, is also shown in fig. 3: as expected, no structure is observed at low Q . Adding kaons and protons we obtain the Q distribution shown in fig. 4 (a).

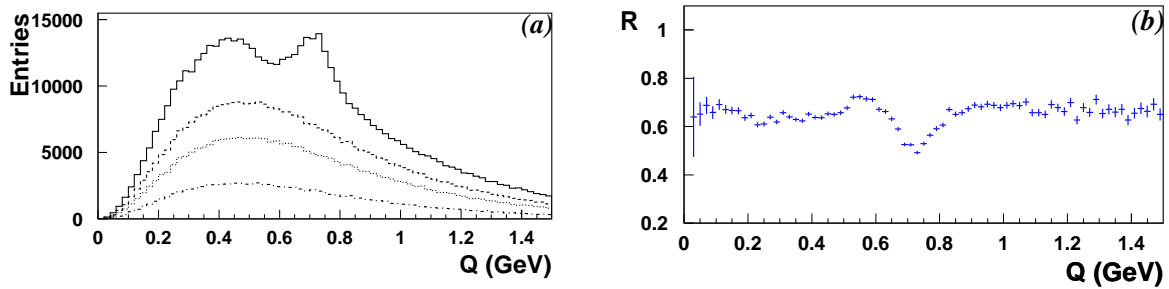


Fig. 3. (a), Q -distributions for Monte Carlo generated pion pairs; top to bottom: unlike, like, (+), (−) pairs. (b), the ratio like/unlike pairs, $R(Q)$ of eq. 5, for a pure pion MC sample.

The Q variable was calculated assigning the pion mass to all particles. No structure is visible, only a global shift towards higher values. Fig. 4 (b), shows the effect of adding all other particles including the “not recognized” ones in the sample: the first bin is now low, demonstrating that the denominator of eq. 5 contains a sizeable contribution at very low values of Q due to e^+e^- pairs from photon conversions. For this reason the data at $Q \leq 0.04$ GeV have been excluded from the fit used to extract the BEC parameters.

We observe that the unlike-sign pair distribution as reference sample has the essential property of reproducing faithfully the non-BEC distribution of like-sign pairs (the ratio is flat). However, it is dangerously affected by meson resonances and by electron-positron pairs from photon conversions. In particular the conversions give a major contribution to our systematic errors which will be estimated in section 6.

From this study we conclude that contaminations from particles other than electrons produce only a variation of the overall normalization of the distributions and no distortion of its shape. Therefore they do not affect the measurement of the radius of the emitting source while some effects could be induced on the chaoticity parameter. The observation, described in section 5, that the results obtained for the $(--)$ sample are very similar to those obtained for the $(++)$ pairs, although the two samples are affected by different contaminations, demonstrates that these latter are not a critical issue.

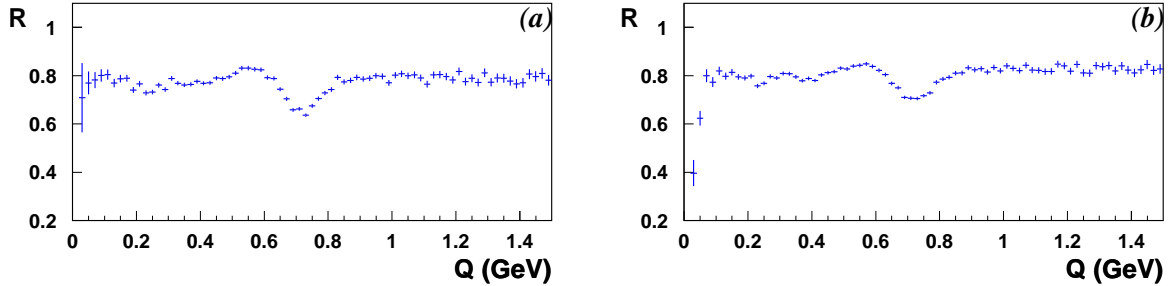


Fig. 4. (a), $R(Q)$ for a Monte Carlo sample of pions, kaons and protons. (b), $R(Q)$ for a Monte Carlo sample of all particle types.

5 Results

This section presents the results on the chaoticity parameter λ and the source radius R obtained following the Goldhaber, KP and $(Q_{\parallel}, Q_{\perp})$ parametrizations.

5.1 The Goldhaber parametrization

The inclusive experimental correlation $R(Q)$ as a function of Q is shown in fig. 5. The empty regions in the distribution fit correspond to the excluded intervals described above. Superimposed to the data is a fit of the form:

$$R(Q) = N \left[1 + \lambda \exp(-R_G^2 Q^2) \right] (1 + aQ + bQ^2) \quad (6)$$

where N is a normalization constant and the second degree polynomial is a parametrization of the shape of the long-range correlations outside the BEC region. The choice of the parametrization used to describe the long-range correlations inevitably affects the results of the BEC analysis and contributes to the systematic errors on λ and R_G . The second degree polynomial gives the best $\chi^2/d.o.f.$ (compared to a quadratic or linear long-range form) of the fit and it has been often used in other experiments. Therefore, we shall use it in this paper and we shall discuss the use of other parametrizations in the section on systematic uncertainties.

Fig. 6 shows the BEC for $(+ +)$ pairs (a) and $(--)$ pairs (b) again with a fit of the form of eq. 6 superimposed. The long-range correlations are very different between positive and negative pairs: for positive pairs there is a steady increase of the correlation function for $Q \geq 0.4$ GeV, while for negative pairs the correlation function is almost flat at large Q . The long-range correlations for positive pairs also determine the behaviour of the like-sign pair sample. However, as opposed to the long-range correlations, the BEC are similar for the $(++)$ and $(--)$ samples. Table 2 summarizes the results on λ and R_G for the like, $(++)$ and $(--)$ samples. The values of λ and R_G of the three samples are in good agreement, in spite of the different shape of the long-range correlation region. This demonstrates that our parametrization (6) is robust and capable of describing correctly all three sets of data. The BEC parameter λ is about 0.4 and R_G is about 1 fm, independent of the particle charge. We notice the following:

- The measured R distribution, in the region $Q \geq 0.5$ GeV (the region of the long-range correlation) differs from the Monte Carlo simulation, which produces a flat distribution (see fig. 4).
- The best fit χ^2 value is inconsistent with statistical errors alone. Most of the contribution to the χ^2 comes from the region of long-range correlations ($Q \geq 0.8$ GeV) which is not fully accounted for by our empirical parametrization. Results from the NOMAD experiment on the production of the $f_0(980)$ and $f_2(1270)$ resonances in ν_μ^{CC} interactions have been published [19]. These resonances contaminate the region at $Q > 0.8$ GeV and contribute to the large χ^2 of the fit. We verified that the exclusion of the region $0.9 < Q < 1.3$ GeV improves the $\chi^2/d.o.f.$ from 1.75 to 1.5 and does not affect significantly the results. Moreover in the BEC region ($Q < 0.2$ GeV) the quality of the fit is always good.

Pairs	λ	R_G (fm)	$\chi^2/d.o.f.$
like	0.40 ± 0.03	1.01 ± 0.05	90/52
$(+ +)$	0.38 ± 0.04	1.03 ± 0.07	80/52
$(--)$	0.43 ± 0.04	0.96 ± 0.06	75/52

Table 2

Chaoticity λ and Goldhaber radius R_G . Errors are statistical only.

5.2 The Kopylov-Podgoretskii parametrization

The dependence of R on Q_t and Q_0 is shown in fig. 7 (a) for $(--)$ pairs. A peak at Q_t and $Q_0 \approx 0$ is visible with a width of ≈ 0.2 GeV in both variables.

To fit the two dimensional structure of BEC it is convenient to use a one dimensional Q_t parametrization derived from eq. 3 (see [6], [17]) by restricting the allowed energy difference to $Q_0 \leq Q_{max}$. Then, under the hypothesis that $(Q_{max}\tau)^2 \ll 1$:

$$C(Q_t) = N_{KP} \left[1 + \lambda_{KP} [2J_1(R_{KP}Q_t)/(R_{KP}Q_t)]^2 \right] (1 + aQ_t + bQ_t^2) \quad (7)$$

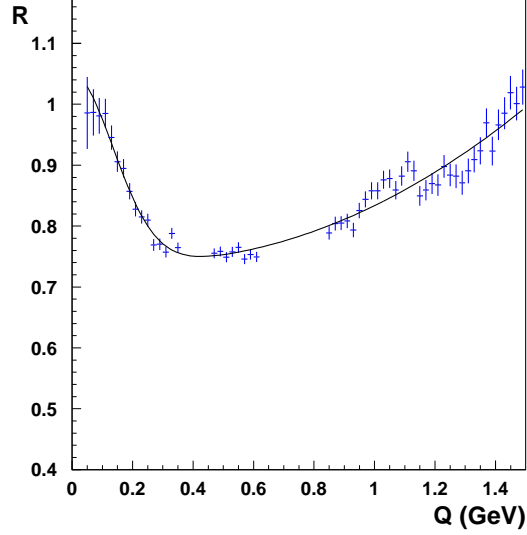


Fig. 5. R as a function of Q in the like-sign pair sample. Superimposed is a fit obtained using the Goldhaber parametrization (eq. 6).

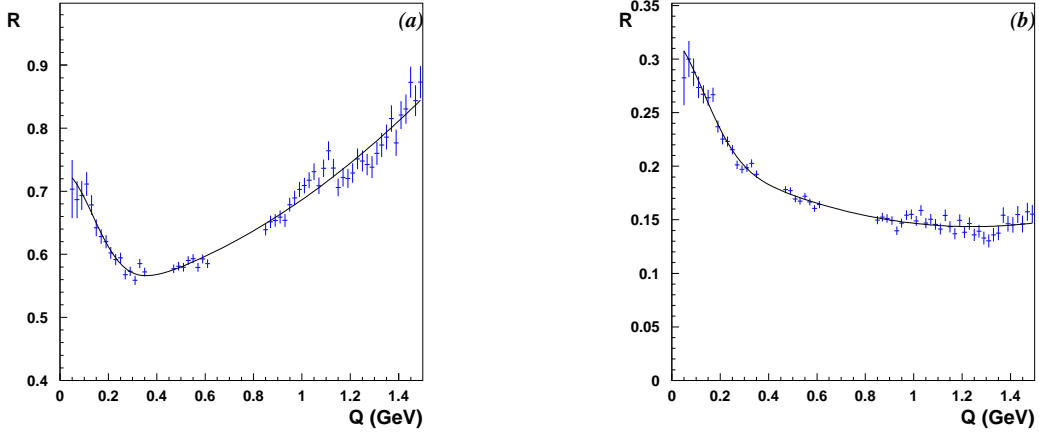


Fig. 6. R as a function of Q in the $(++)$ (a) and $(--)$ (b) pair sample. Superimposed is a fit following the Goldhaber parametrization (eq. 6).

Here too a polynomial form is used to parametrize the long-range correlation. The Q_t distribution for $Q_0 \leq 0.2$ GeV is shown in fig. 7 (b). Notice that also in this case we remove from the fit the two regions where the presence of K^0 and resonance contributions affects the Q_t variable.

The result of a fit using the parametrization given in eq. 7 yields $\lambda_{KP} = 0.29 \pm 0.06$ and $R_{KP} = 2.07 \pm 0.04$ fm, in agreement with the expected relation $R_{KP} \approx 2R_G$. Again the results obtained using the $(++)$ and $(--)$ samples are consistent with each other.

Pairs	λ_{KP}	R_{KP} (fm)	$\chi^2/d.o.f.$
like	0.29 ± 0.06	2.07 ± 0.04	51/52
(+ +)	0.28 ± 0.04	2.13 ± 0.04	56/52
(- -)	0.32 ± 0.06	2.01 ± 0.04	38/52

Table 3

Chaoticity parameter λ_{KP} and radius R_{KP} . Errors are statistical only.

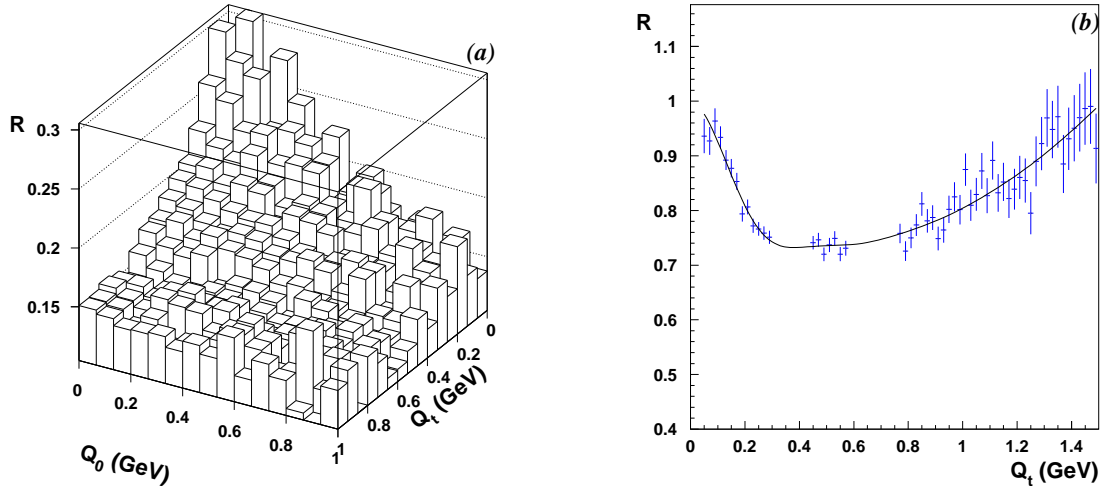


Fig. 7. (a), R as a function of the KP variables Q_t and Q_0 for $(--)$ pairs. (b), R as a function of Q_t for $Q_0 \leq 0.2$ GeV. Superimposed is a fit using eq. 7.

5.3 Longitudinal and transverse shapes

A possible deviation of the pion emitting source from a spherical shape in its rest frame can be investigated in the LCMS system using the variables Q_\perp and Q_\parallel . The BEC behaviour is studied separately for the two variables by requiring $Q_\parallel \leq 0.2$ GeV for the Q_\perp distribution and, conversely, $Q_\perp \leq 0.2$ GeV for the Q_\parallel distribution. These distributions are shown in Fig. 8. Again the regions where the presence of K^0 's and resonances affects Q_\parallel and Q_\perp have been removed from the fit. The fit is performed with a parametrization as in eq. 4, multiplied by a second degree polynomial to reproduce the long-range correlations. The fitted values for the BEC parameters are shown in tables 4 and 5 together with the results obtained from $(++)$ and $(--)$ pairs separately. Our measurements confirm the LEP results [22] that in the LCMS reference frame the longitudinal size of the pion source is 30-40% larger than the transverse one.

Pairs	R_{\perp} (fm)	$\chi^2/d.o.f.$
like	0.98 ± 0.10	71/52
(+ +)	1.04 ± 0.12	63/52
(--)	0.81 ± 0.15	50/52

Table 4

The LCMS variable R_{\perp} for $Q_{\parallel} \leq 0.2$ GeV. Errors are statistical only.

Pairs	R_{\parallel} (fm)	$\chi^2/d.o.f.$
like	1.32 ± 0.14	54/52
(+ +)	1.39 ± 0.24	50/52
(--)	1.15 ± 0.12	64/52

Table 5

The LCMS variable R_{\parallel} for $Q_{\perp} \leq 0.2$ GeV. Errors are statistical only.

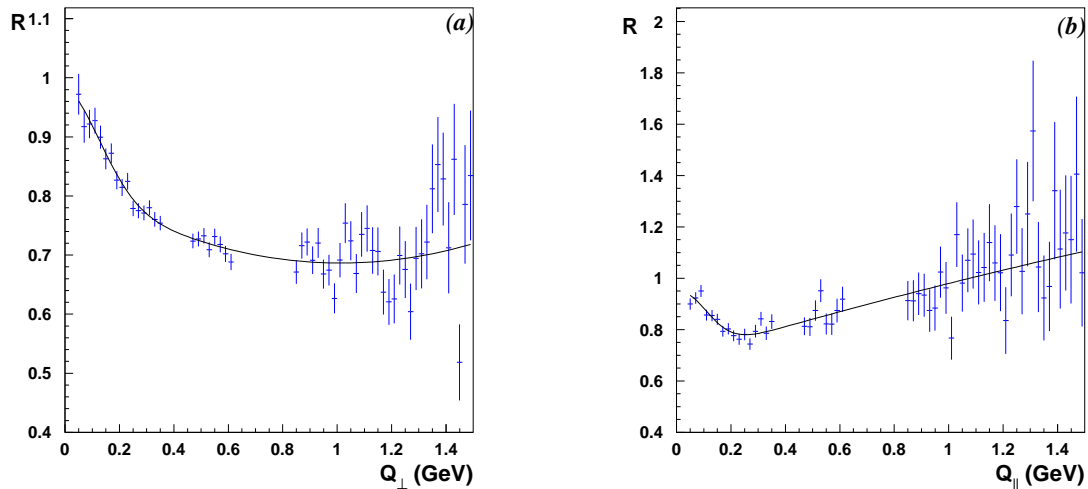


Fig. 8. (a), R vs Q_{\perp} for $Q_{\parallel} \leq 0.2$ GeV. (b), R vs Q_{\parallel} for $Q_{\perp} \leq 0.2$ GeV. Superimposed is a fit using eq. 4 multiplied by a second degree polynomial.

5.4 BEC dependence on the rapidity of the pair

Deep inelastic CC neutrino interactions involve a d quark in the target nucleon leaving as spectators the remaining quarks. We naively expect, therefore, two distinct sources of secondary hadrons: the single struck d quark and the spectators. At high energy the two contributions should be fairly well separated in the c.m. frame of the hadronic jet as the particles coming from the fragmentation of the struck quark should have positive rapidities while those produced by the spectator quarks should have negative rapidities. To investigate possible differences between the two pion sources we studied the BEC distributions, using the Goldhaber parameter Q , for pairs of particles of equal rapidity

sign and also for pairs of particles of opposite rapidity sign in the rest frame of the hadronic jet. The data are shown in fig. 9 and 10. Table 6 summarizes the results obtained on λ

Rapidity	λ	R_G (fm)	$\chi^2/d.o.f.$
Inclusive	0.40 ± 0.03	1.01 ± 0.05	90/52
Positive	0.47 ± 0.04	0.98 ± 0.07	84/52
Negative	0.42 ± 0.09	1.03 ± 0.17	53/52
Opposite	0.37 ± 0.06	0.98 ± 0.08	52/52

Table 6

Rapidity dependence of the chaoticity λ and the Goldhaber radius R_G . Errors are statistical only.

and R_G for the various rapidity configurations. The source radius R_G shows no differences for particles emitted at different rapidities, demonstrating that the typical hadronization scale is much longer than the interaction radius, resulting in a unique hadron source, independent of the detail of the quark interactions.

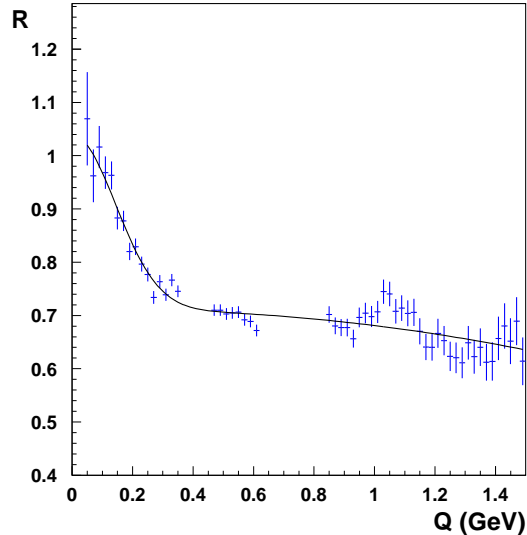


Fig. 9. R vs Q for positive rapidity sign pairs. Superimposed is a fit using eq. 6.

5.5 BEC dependence on event charged multiplicity and hadronic energy W

The large number of events collected by NOMAD allows the study of BEC effects in different final state configurations. In particular it is interesting to verify the observations in hadronic [26] and e^+e^- interactions [20] that the Goldhaber radius increases with the event charged multiplicity N_{ch} . Fig. 11 (a) shows the Goldhaber radius R_G and the chaoticity parameter λ for seven different N_{ch} values. We see that there is here an indication for a

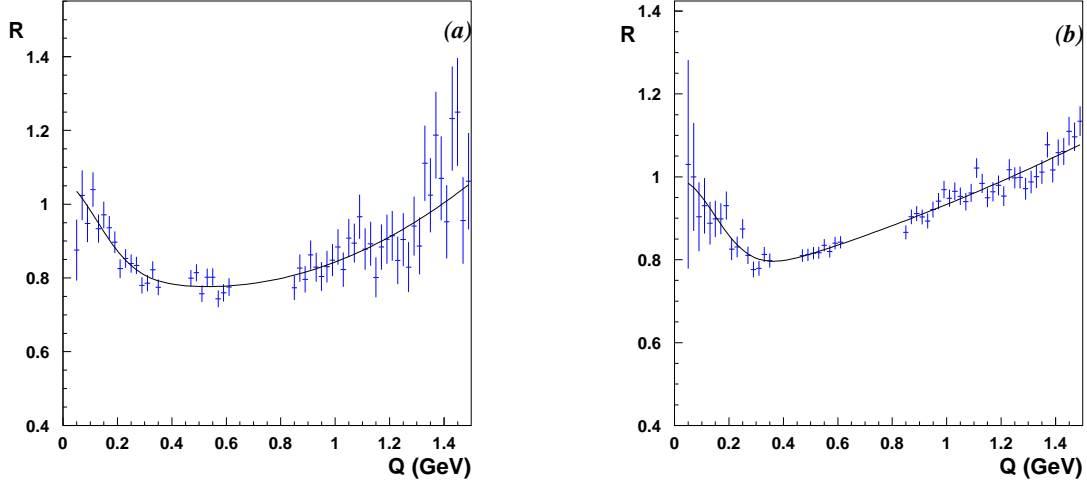


Fig. 10. R vs Q for negative (a) and opposite (b) rapidity sign pairs. Superimposed are fits using eq. 6.

decrease of R_G with N_{ch} . One should notice that the rise of the emission radius R_G with N_{ch} at LEP is only visible at very high multiplicities ($N_{ch} > 10$) which are not accessible to this experiment. The chaoticity parameter λ appears to increase with N_{ch} .

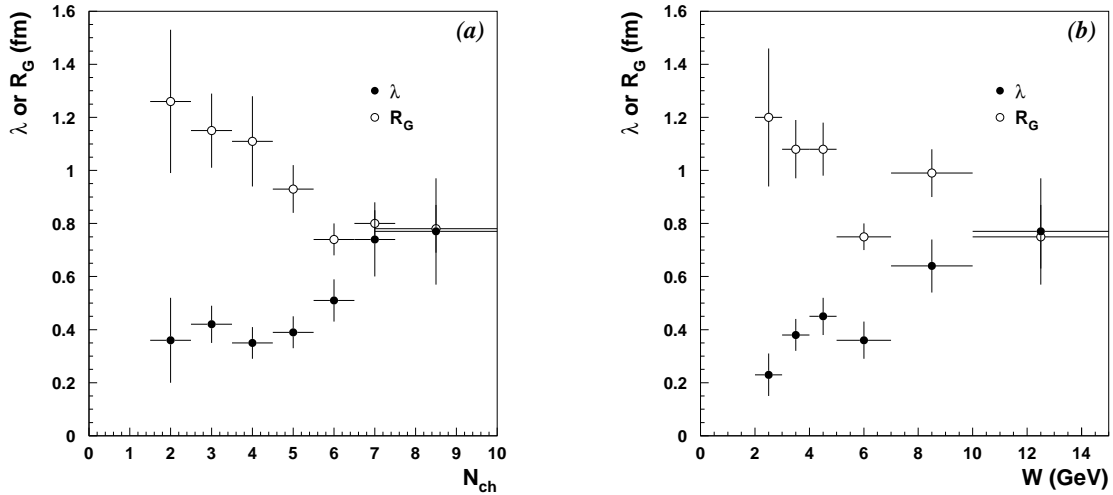


Fig. 11. Dependence of the chaoticity parameter λ and Goldhaber radius R_G on the event charged multiplicity N_{ch} (a) and on the hadronic energy W (b).

A similar conclusion can be drawn when studying the BEC effects as a function of the hadronic energy W : fig. 11 (b) presents R_G and λ for six W intervals. R_G decreases with W whereas λ increases.

6 Systematic errors

We focus the discussion of systematic errors to the inclusive BEC study using the Goldhaber parametrization.

Coulomb interactions between particles which affect like-sign and unlike-sign pairs in opposite ways, can alter the correlations. This effect changes the two pion cross section by the Gamow factor [16], a significant correction only at very small values of Q . We checked that the effect enhances both λ and R_G by only a few percent therefore we decided not to apply it.

We identify three sources of systematic errors in our results:

- The uncertainty in the background contribution underneath the BEC peak at $Q \leq 0.2$ GeV. In the NOMAD experiment BEC effects could be affected by an insufficient rejection of e^+e^- pairs from photon conversions contaminating the reference sample.
- The cuts applied.
- The track reconstruction efficiency. We verified that this effect does not produce sizeable effects on the Goldhaber parameters, decreasing the track reconstruction efficiency by 10%. This was done by removing tracks at random from the sample before calculating the BEC.

6.1 Systematic errors from the e^+e^- background

As already noted in section 4.1, BEC could be altered by the presence of background of e^+e^- pairs from photon conversions in the unlike-sign sample used as a reference. Most of this background is at low Q and could seriously affect the results. To reduce this effect the data at $Q \leq 0.04$ GeV in all the previous correlation distributions have been excluded from the fit used to extract the BEC parameters. The systematic uncertainty from this cut is then estimated by enlarging the data excluded from the fit to $Q \leq 0.06$ GeV (i.e. the first bin of fig. 5). The results obtained for λ and R_G are shown in table 7. By comparing table 7 to table 2 we see that our results are insensitive to a variation of the lowest accepted Q bin. A larger sensitivity of λ and R_G is found when varying the track quality cuts (see next paragraph).

Pairs	λ	R_G (fm)	$\chi^2/d.o.f.$
like	0.40 ± 0.03	1.02 ± 0.05	89/51
(+ +)	0.39 ± 0.03	1.04 ± 0.06	80/51
(--)	0.44 ± 0.05	0.98 ± 0.08	84/51

Table 7

Chaoticity parameter λ and Goldhaber radius R_G obtained from a fit to the R distribution where the data at $Q \leq 0.06$ GeV have been removed.

6.2 Systematic errors due to the selection cuts

We checked the stability of our results by varying the following track selection parameters:

- The difference Δz between the first point of the reconstructed track and the primary vertex position along z : $\Delta z \leq 15$ cm;
- the minimum track momentum: $|\vec{p}| \geq 100$ MeV/c;
- the maximum acceptable momentum uncertainty $\frac{\Delta|\vec{p}|}{|\vec{p}|} \leq 6\%$.

We note that these selection parameters affect differently pions and electrons and, therefore, they could change the fraction of conversions included in the data.

To estimate the effect of varying these cuts on the fitted parameters λ and R_G each cut was modified and the relevant BEC distribution was again fitted. The results are shown in table 8. The interval chosen for Δz corresponds to the thickness of one DC chamber. The variations of the momentum and $\frac{\Delta|\vec{p}|}{|\vec{p}|}$ cut positions in table 8 reflect the uncertainty in their choice for an optimum separation of the electron and the pion populations. A similar procedure was adopted also for $(--)$ and $(++)$ pairs separately. The largest

cut	λ	R_G (fm)
all cuts	0.40 ± 0.03	1.01 ± 0.05
$\Delta z \leq 10$ cm	0.40 ± 0.04	1.10 ± 0.09
$\Delta z \leq 20$ cm	0.37 ± 0.03	0.95 ± 0.04
$\frac{\Delta \vec{p} }{ \vec{p} } \leq 8\%$	0.35 ± 0.03	0.99 ± 0.04
$ \vec{p} \geq 150$ MeV/c	0.40 ± 0.03	1.01 ± 0.05

Table 8

Chaoticity parameter λ and Goldhaber radius R_G obtained for like pairs and for different cut configurations.

effect is the one induced on R_G by changes in the Δz cut and on λ by changes in the $\frac{\Delta|\vec{p}|}{|\vec{p}|}$ cut. The systematic uncertainty due to the Δz cut can be also estimated by extrapolating the parameters to $\Delta z = 0$. The variations for R_G and λ amount to 15% and to 12% respectively.

6.3 Effect of the long-range correlation parametrization

The numerical values of R_G and λ depend on the parametrization used to describe the long-range correlations. In the literature linear, quadratic and polynomial forms have been used. This ambiguity must be taken into account when comparing results from different experiments. Throughout this paper the long range correlations, necessary to describe effects other than BEC, have been described by a second degree polynomial form $(1 + aQ + bQ^2)$. Different parametrizations are possible and have been used in other

experiments: i.e. a linear form: $(1 + aQ)$ or a quadratic form: $(1 + bQ^2)$. Table 9 shows the results of the three different choices for the long range parametrizations when the like distribution is analyzed. We see that the fit worsens when using the linear parametrization and there are also significant differences in the fit values for λ and R_G , while the quadratic parametrization reproduces almost exactly the results of the polynomial. We conclude that the linear approximation is inadequate to be used in the analysis of these data. For completeness in section 8 our results obtained with different parametrizations of the long range effects will be compared with the data of other experiments using similar parametrizations.

Long range parametrization	λ	R_G (fm)	$\chi^2/d.o.f.$
Polynomial	0.40 ± 0.03	1.01 ± 0.05	90/52
Linear	0.54 ± 0.02	0.86 ± 0.03	123/52
Quadratic	0.43 ± 0.02	0.95 ± 0.03	93/52

Table 9

Chaoticity parameter λ and Goldhaber radius R_G for three choices of the long range correlation parametrization in the NOMAD analysis. Errors are only statistical.

7 Final results

Table 10 summarizes our final results on λ and R_G including also the systematic errors from variations of the cuts discussed in the previous section (added in quadrature).

Pairs	λ	R_G (fm)
like	$0.40 \pm 0.03^{+0.01}_{-0.06}$	$1.01 \pm 0.05^{+0.09}_{-0.06}$
(+ +)	$0.38 \pm 0.04^{+0.01}_{-0.05}$	$1.03 \pm 0.07^{+0.09}_{-0.07}$
(--)	$0.43 \pm 0.04^{+0.01}_{-0.04}$	$0.96 \pm 0.06^{+0.09}_{-0.06}$

Table 10

Chaoticity λ and Goldhaber radius R_G . The first error is statistical, the second one is systematic.

8 Comparison with the results of other experiments

Fig. 12 and table 11 display a compilation of some measurements of λ and R_G in the $\pi\pi$ channel in high statistics lepton-induced reactions: neutrino interactions [6], muon DIS [18], electron-proton DIS [21], [27], e^+e^- collisions [23], [24], [20], [25]. These experiments were performed at different energies; they have different selection criteria and biases and also different parametrizations for the long-range correlation (see table 11).

Our results agree within errors with those of the combined analysis the BEBC and of the Fermilab neutrino data [6].

The results on λ (fig. 12 (a)) shows that there are two groups of experiments which are consistent within each group, but not between them. The first group clusters around $\lambda \approx 0.5$ and the other around $\lambda \approx 1$. The parametrization of long-range correlations does not seem to be the origin of this discrepancy. Since λ is sensitive to the purity of the pion sample the origin of this difference could be the different pion identification criteria of the experiments.

The results on R_G are shown in fig. 12 (b): it appears that the value of R_G computed with a linear model is systematically lower than the one computed with a quadratic or polynomial form. The two groups of data are rather well consistent within each other: the “linear” group cluster at $R_G \approx 0.6$ fm and the “quadratic-polynomial” group at $R_G \approx 0.9$ fm.

Experiment	Fit type	$\langle\sqrt{s}\rangle$ (GeV)	$\langle Q^2 \rangle$ (GeV ²)	λ	R_G (fm)
BEBC-Fermilab	quadratic	10	10	$0.61 \pm 0.04 \pm 0.15$	$0.80 \pm 0.04 \pm 0.16$
EMC	quadratic	23	50	1.08 ± 0.1	0.84 ± 0.03
DELPHI	linear	91		$1.06 \pm 0.05 \pm 0.16$	$0.49 \pm 0.01 \pm 0.05$
ALEPH	linear	91		$0.51 \pm 0.04 \pm 0.11$	$0.65 \pm 0.04 \pm 0.16$
ZEUS (DIS)	linear	300	400	$0.431 \pm 0.012^{+0.042}_{-0.130}$	$0.671 \pm 0.016^{+0.030}_{-0.032}$
H1 (DIS)	linear	300	40	$0.52 \pm 0.03^{+0.19}_{-0.21}$	$0.68 \pm 0.04^{+0.02}_{-0.05}$
L3	linear	189		$0.48 \pm 0.05 \pm 0.07$	$0.71 \pm 0.04 \pm 0.05$
OPAL	polynomial	91		$0.672 \pm 0.013 \pm 0.024$	$0.955 \pm 0.012 \pm 0.015$
NOMAD	polynomial	8	10	$0.40 \pm 0.03^{+0.01}_{-0.06}$	$1.01 \pm 0.05^{+0.09}_{-0.06}$
NOMAD	quadratic	8	10	0.43 ± 0.02	0.95 ± 0.03
NOMAD	linear	8	10	0.54 ± 0.02	0.86 ± 0.03

Table 11

Summary of results published in previous experiments.

9 Conclusions

The NOMAD experiment has measured BEC in charged-current neutrino interactions using different parametrizations for this effect. The general picture emerging from the data is that the size and the chaoticity of the pion source are about 1 fm and about 0.4 respectively, quite independent of the final state rapidity sign of the emitted pions. A difference of about 40% is found between the longitudinal and transverse size of the source.

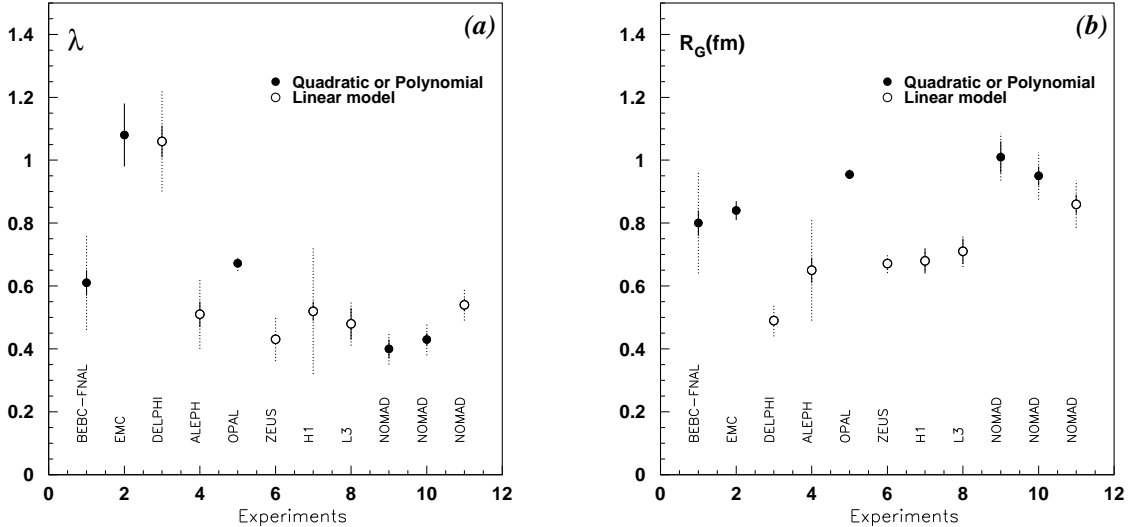


Fig. 12. *Compilation of results obtained by various experiments for the chaoticity parameter λ (a) and the Goldhaber radius R_G (b).*

We observe a decrease of the Goldhaber radius as a function on the charged multiplicity and of the hadronic energy of the event. A comparison of our results with those of other experiments studying other processes than neutrino interactions shows a fair agreement, demonstrating that the final state hadronization processes have universal features with little dependence on the type or energy of the interacting particles.

Acknowledgements

We thank the management and staff of CERN and of all participating institutes for their vigorous support of the experiment. Particular thanks are due to the CERN accelerator and beam-line staff for the magnificent performance of the neutrino beam. The following funding agencies have contributed to this experiment: Australian Research Council (ARC) and Department of Education, Science, and Training (DEST), Australia; Institut National de Physique Nucléaire et Physique des Particules (IN2P3), Commissariat à l’Energie Atomique (CEA), Ministère de l’Education Nationale, de l’Enseignement Supérieur et de la Recherche, France; Bundesministerium für Bildung und Forschung (BMBF, contract 05 6DO52), Germany; Istituto Nazionale di Fisica Nucleare (INFN), Italy; Russian Foundation for Basic Research, Institute for Nuclear Research of the Russian Academy of Sciences, Russia; Fonds National Suisse de la Recherche Scientifique, Switzerland; Department of Energy, National Science Foundation (grant PHY-9526278), the Sloan and the Cottrell Foundations, USA.

We also thank our secretarial staff, Jane Barney, Katherine Cross, Joanne Hebb, Marie-

Anne Huber, Jennifer Morton, Rachel Phillips and Mabel Richtering, and the following people who have worked with the collaboration on the preparation and the data collection stages of NOMAD: M. Anfreville, M. Authier, G. Barichello, A. Beer, V. Bonaiti, A. Castera, O. Cloué, C. Détraz, L. Dumps, C. Engster, G. Gallay, W. Huta, E. Lessmann, J. Mulon, J.P. Passérieux, P. Petitpas, J. Poinsignon, C. Sobczynski, S. Soulié, L. Visentin, P. Wicht.

References

- [1] R. Hanbury-Brown and R. Q. Twiss, *Phil. Mag.* **45** (1954) 663.
- [2] G. Goldhaber *et al.*, *Phys. Rev. Lett* **3** (1959) 181;
G. Goldhaber *et al.*, *Phys. Rev. Lett* **120** (1960) 300.
- [3] R. M. Weiner, *Bose-Einstein Correlations in particle and nuclear physics*, John Wiley & sons pub. (1997);
R. M. Weiner, *Introduction to Bose-Einstein Correlations and subatomic interferometry*, Chichester: Wiley, (2000).
- [4] G. I. Kopylov and M. I. Podgoretskii, *Sov. J. Nucl. Phys.* **19** (1974) 215.
- [5] G. Cocconi, *Phys. Lett.* **49** (1974) 459.
- [6] Big Bubble Chamber Neutrino Collaboration, V. A. Korotkov *et al.*, *Z. Phys.* **C60**(1993) 37;
see also WA 25 Collaboration, D. Allasia *et al.*, *Z. Phys.* **C37** (1988) 527.
- [7] J. Altogether *et al.*, *Nucl. Instrumen. Meth.* **A428** (1999) 299.
- [8] G. Ingelman, *LEPTO version 6.1*, TSL-ISV-92-0065 (1992);
G. Ingelman *et al.*, *LEPTO version 6.5*, *Comp. Phys. Comm.* (1997) 101.
- [9] T. Sjostrand, LU-TP-95-20 (1995);
T. Sjostrand, *Comp. Phys. Comm.* (1086) 39, (1987) 43.
- [10] GEANT: Detector description and simulation tool, CERN programming Library Long Writeups W5013, Geant version 3.21, (1994).
- [11] M. Anfreville *et al.*, *Nucl. Instrumen. Meth.* **A481** (2002) 339.
- [12] G. Bassompierre *et al.*, *Nucl. Instrumen. Meth.* **A403** (1998) 363;
G. Bassompierre *et al.*, *Nucl. Instrumen. Meth.* **A411** (1998) 63.
- [13] D. Autiero *et al.*, *Nucl. Instrumen. Meth.* **A373** (1996) 358;
D. Autiero *et al.*, *Nucl. Instrumen. Meth.* **A387** (1997) 352;
D. Autiero *et al.*, *Nucl. Instrumen. Meth.* **411** (1998) 285.
- [14] R. Zei, *Tesi di Laurea Specialistica*, Università di Pisa (2003),
http://www.pi.infn.it/atlas/documenti/note/tesi_zei.ps;
R. C. Challis, *PhD thesis*, University of Melbourne (2002),
http://epp.ph.unimelb.edu.au/epp/epp/epp_current_projects.html#past_theses.

- [15] NOMAD Collaboration, P. Astier *et al.*, Nucl. Phys. **B609** (2001) 255.
- [16] M. Gyulassy *et al.*, Phys. Rev. **C20** (1979) 2267.
- [17] AFS Collaboration, T. Akesson *et al.*, Phys. Lett. **B129** (1983) 269;
AFS Collaboration, T. Akesson *et al.*, Phys. Lett. **B187** (1987) 420;
EHS/Na22 Collaboration, N. M. Agababian *et al.*, Z. Phys. **C59** (1993) 195.
- [18] EMC Collaboration, M. Arneodo *et al.*, Z. Phys. **C32** (1986) 1.
- [19] NOMAD Collaboration, P. Astier *et al.*, Nucl. Phys. **B601** (2001) 3.
- [20] OPAL Collaboration, G. Alexander *et al.*, Z. Phys. **C72** (1996) 389.
- [21] M. Derrick, for the ZEUS Collaboration, Acta Physica Pol. **B33** (2002) 3281.
- [22] DELPHI Collaboration, P. Abreu *et al.*, Phys. Lett. **B471** (2000) 460.
- [23] DELPHI Collaboration, P. Abreu *et al.*, Z. Phys. **C63** (1994) 17.
- [24] ALEPH Collaboration, D. Decamp *et al.*, Z. Phys. **C54** (1992) 75.
- [25] L3 Collaboration, M. Acciarri *et al.*, Phys. Lett. **B493** (2000) 233.
- [26] A. Breakstone *et al.*, Z. Phys. **C33** (1987) 333.
- [27] H1 Collaboration, C. Adloff *et al.*, Z. Phys. **C75** (1997) 437.