Dynamical Generation of Hyperon Resonances

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 In this talk we report on how, using a chiral unitary approach for the meson–baryon interactions, two octets of how, using a chiral a chiral unitary approach for the meson–baryon interactions, two octets of how, using a chiral a chiral unitary approach for the sentence of the sentence of how evidence. We suggest experiments which could show evidence for the existence of these states.

1. Introduction

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The discussion below will clarify this issue and the structure of these resonances.

2. Description of the meson baryon interactions

Starting from the chiral Lagrangians for meson–baryon interactions [9] and using the N/D method to obtain a scattering matrix for meson–baryon interactions [9] and using [9] and using the chiral ch

$$T = [1 - VG]^{-1}V. (1)$$

$$V_{ij} = -C_{ij} \frac{1}{4f^2} (2\sqrt{s} - M_i - M_j) \left(\frac{M_i + E}{2M_i}\right)^{1/2} \left(\frac{M_j + E'}{2M_j}\right)^{1/2} , \qquad (2)$$

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where the C_{ij} coefficients are given in Ref. [3], and an averaged meson decay constant to the term of the term of the term of the term of term of the term of terms of term of terms of term of terms of ter

 a matrix G stands for the loop function of a meson and a baryon and is defined by a subtracted dispersion relation in terms of phase space with a cut starting at the corresponding threshold [4]. It corresponds to the loop function of a meson and a baryon once the logarithmic divergent constant is removed.

 the divergent constant piece leads to

$$\begin{aligned} G_l &= i \, 2M_l \int \frac{d^4q}{(2\pi)^4} \frac{1}{(P-q)^2 - M_l^2 + i\epsilon} \frac{1}{q^2 - m_l^2 + i\epsilon} \\ &= \frac{2M_l}{16\pi^2} \left\{ a_l(\mu) + \ln \frac{M_l^2}{\mu^2} + \frac{m_l^2 - M_l^2 + s}{2s} \ln \frac{m_l^2}{M_l^2} + \frac{q_l}{\sqrt{s}} \left[\ln(s - (M_l^2 - m_l^2) + 2q_l\sqrt{s}) + \ln(s + (M_l^2 - m_l^2) + 2q_l\sqrt{s}) - \ln(-s + (M_l^2 - m_l^2) + 2q_l\sqrt{s}) - \ln(-s - (M_l^2 - m_l^2) + 2q_l\sqrt{s}) \right] \right\} , (3) \end{aligned}$$

This meson baryon loop function was calculated in Ref. [3] with a cut-off regularization, similarly as previously done in meson–meson scattering [14]. The values of tregularization, similarly as previously done in meson–meson scattering [14]. The values of the acut-off acut-of

$$a_{\bar{K}N} = -1.84 , \quad a_{\pi\Sigma} = -2.00 , \quad a_{\pi\Lambda} = -1.83 , \\ a_{\eta\Lambda} = -2.25 , \quad a_{\eta\Sigma} = -2.38 , \quad a_{K\Xi} = -2.67 ,$$
(4)

one reproduces the results for the G functions obtained in Ref. [3] with a cut–off of 630

3. Poles of the T-matrix

The appearance of a multiplet of dynamically generated mesons and baryons seems most natural once a state of the multiplet of dynamically generated mesons and baryons seems most natural once a state of the multiplet of dynamically generated mesons and baryons eets the multiplet on the multiplet of the multiplet on the multiplet of dynamically generated mesons and baryons eets the multiplet of the multiplet of the multiplet on the multiplet on

$$8 \otimes 8 = 1 \oplus 8_s \oplus 8_a \oplus 10 \oplus \overline{10} \oplus 27 .$$
⁽⁵⁾

Thus, on pure SU(3) grounds, should we have a SU(3) symmetric Lagrangian, one can expect e.g. one singlet and two octets of we have a SU(3) symmetric Lagrangian, one can expect e.g. one singlet and two octets of resonances, the symmetric can expect e.g. one singlet and two octets of the meson-metric construction expected by the symmetric constructions where the building blocks could appear and there is no reason why they should be degenerate in principle.

The lowest order meson–baryon chiral Lagrangian is exactly SU(3) invariant if all the masses of the mesons are set equal. As stated above [see Eq. (2)], in Ref. [10] the baryon masses of the mesons are set equal. As stated above [see Eq. (2)], in Ref. [10] the baryon masses are equals as stated above [see Eq. (2)], in Ref. [10] the baryon masses are equals as the equal as the equal as the equal of the equal to the eq

<b <p>If we do such an SU(3) symmetry approximation and look for poles of the scattering matrix, we find poles corresponding to the octets and singlet. The surprising result is that the two octet poles are degenerate as a consequence of the dynamics contained in the chiral Lagrangians. Indeed, if we evaluate the matrix elements of the transition potential V in a basis of SU(3) states,

$$V_{\alpha\beta} = \sum_{i,j} \langle i, \alpha \rangle C_{ij} \langle j, \beta \rangle, \tag{6}$$

$$V_{\alpha\beta} = \text{diag}(6, 3, 3, 0, 0, -2) , \qquad (7)$$

taking the following order for the irreducible representations: 1, 8_s , 8_a , 10, $\overline{10}$ and 27.

 th t the states belonging to different irreducible representations do not mix and the two octets appear degenerate. The coefficients in Eq. (7) clearly illustrate why there are no bound states in the 10, 10 and 27 representations. Indeed, considering the minus sign in Eq. (2), a negative sign in Eq. (7) means repulsion.

i g sind che approach of Ref. [10] and using the physical masses of the baryons and the mesons, the position of the poles change and the two occets split apart in four



show the trajectories of the poles as a function of a parameter x that breaks gradually the show the trajectories of the physical values. The dependence of masses and subtraction constants on the parameter x is given by

$$M_i(x) = M_0 + x(M_i - M_0), \quad m_i^2(x) = m_0^2 + x(m_i^2 - m_0^2), \quad a_i(x) = a_0 + x(a_i - a_0), \quad (8)$$

where 0 ≤ x ≤ 1. For the baryon masses, M_i(x), the breaking of the SU(3) symmetry follows linearly, while for the meson masses, M_i(x), the breaking of the SU(3) symmetry follows linearly, while for the meson masses, M_i(x), the breaking of the meson masses, m_i(x), the law is quadratic in the meson masses, m_i(x), the law is quadratic in the meson masses depend on the quark masses linearly. In the calculation of Fig. 1, the values M₀ = 1151 MeV, m₀ = 368 MeV and a₀ = -2.148 are used.

her complex poles, z_R, appear in unphysical sheets. In the present search we follow the strategy of changing the sign of the momentum q_l in the G_l(z) loop function of Eq. (3) for the channels which are open at an energy equal to Re(z).

The splitting of the two I = 0 octet states is very interesting. One moves to higher energies giving rise to the A(1670) resonance and the other one moves to not energies energies energies giving rise to the A(1670) resonance and the other one moves to not energies to the A(1670) resonance and the other one moves to not energies giving rise to the A(1670) resonance and the other one moves to not energies energies with the energies energies with the energies energies with the energies with a norm width.
On the other hand, the singlet also evolves to produce a pole at low energies with a quite large width.

We note that the singlet and the I = 0 octet states appear nearby in energy and one

of the purposes of this paper is, precisely, to point out the fact that what experiments actually see is a combination of the effect of these two resonances.

Similarly as for the I = 0 octet states, we can see that one branch of the I = 1 states moves to higher energies while another moves to lower energies. The branch moving to higher energies finishes at what would correspond to the $\Sigma(1620)$ resonance when the physical masses are reached. The branch moving to lower energies fades away after a while when getting close to the $\bar{K}N$ threshold.

ਂ hoddel of Ref. [4] reproduces qualitatively the same results. However, this model of the model of Ref. [4] reproduces qualitatively the same results. However, this model also produces in the formation of the second constant of the same results. In the model of the second constant of the second the second constant of the second constant of the second second the second constant of the second constant of the second second the second constant of the second constant of the second second the second constant of the second constant of the second constant of the second the second constant of the second constant of the second constant of the second the second constant of the second constan

$$T_{ij} = \frac{g_i g_j}{z - z_R} \,. \tag{9}$$

z_R	1390 + 66	i	1426 + 16	i	1680 + 20i	
(I=0)	g_i	$ g_i $	g_i	$ g_i $	g_i	$ g_i $
$\pi\Sigma$	-2.5 - 1.5i	2.9	0.42 - 1.4i	1.5	-0.003 - 0.27i	0.27
$\bar{K}N$	1.2 + 1.7i	2.1	-2.5 + 0.94i	2.7	0.30 + 0.71i	0.77

Table 1 Pole positions and couplings to I = 0 physical states from the model of Ref. [10]

0.77

0.61

0.010 + 0.77i

-0.45 - 0.41i

 $\eta \Lambda$

 $K\Xi$

We now consider the results obtained from the model of Ref. [4]. Making use of their set I of parameters, which correspond to a baryon mass M₀ = 1286 MeV and a meson

-1.4 + 0.21i

0.11 - 0.33i

1.4

0.35

-1.1 - 0.12i

3.4 + 0.14i

1.1

3.5

z_R	1401 + 40	i	1488 + 114i		
(I=1)	g_i	$ g_i $	g_i	$ g_i $	
$\pi\Lambda$	0.60 + 0.47i	0.76	0.98 + 0.84i	1.3	
$\pi\Sigma$	1.27 + 0.71i	1.5	-1.32 - 1.00i	1.7	
$\bar{K}N$	-1.24 - 0.73i	1.4	-0.89 - 0.57i	1.1	
$\eta\Sigma$	0.56 + 0.41i	0.69	0.58 + 0.29i	0.65	
$K\Xi$	0.12 + 0.05i	0.13	-1.63 - 0.91i	1.9	

Table 2 Pole positions and couplings to I = 1 physical states from the model of Ref. [4]

We observe that the second resonance with I = 0 couples strongly to KN channel, while the second resonance couples monce with I = 0 couples strongly to T = 0 shown in Table 1 resonance couples monce couples monce strongly to T = 0 shown in Table 1 resonance couples monce obtained in Ref. [6] and Ref. [8] where two resonances are also found to the second and the second monce obtained in Ref. [6] and Ref. [8] where two resonances are also found to the second monce obtained in Ref. [6] and Ref. [8] where two resonances are also found to the second monce obtained in Ref. [6] and Ref. [8] where two resonances are also found to the second monce obtained in Ref. [6] and Ref. [8] where two resonances are also found to the second monce obtained in Ref. [6] and Ref. [8] where two resonances are also found to the second monce obtained in Ref. [6] and Ref. [8] where two resonances are also found to the second monce obtained in Ref. [6] and Ref. [8] where two resonances are also found to the second monce obtained in Ref. [6] and Ref. [8] where two resonances are also found to the second monce obtained monce obtained in Ref. [8] where the second monce obtained monce obta

We can also project the states found over the pure SU(3) states and we find the results

Table 3

z_R	1390 + 66i		1426 + 16i		1680 + 20i	
	(evolved singlet)		(evolved octet 8_s)		(evolved octet 8_a)	
	g_γ	$ g_{\gamma} $	g_γ	$ g_{\gamma} $	g_γ	$ g_{\gamma} $
1	2.3 + 2.3i	3.3	-2.1 + 1.6i	2.6	-1.9 + 0.42i	2.0
8_s	-1.4 - 0.14i	1.4	-1.1 - 0.62i	1.3	-1.5 - 0.066i	1.5
8_a	0.53 + 0.94i	1.1	-1.7 + 0.43i	1.8	2.6 + 0.59i	2.7
27	0.25 - 0.031i	0.25	0.18 + 0.092i	0.21	-0.36 + 0.28i	0.4

Couplings of the I = 0 bound states to the meson–baryon SU(3) basis states, obtained with the model of Ref. [10]

We observe that the physical singlet couples mostly to the singlet SU(3) state. This means that the physical state has retained couples mostly to the singlet state. This means that this physical state has retained largely the singlet state it has been metric octet retained that, due to its proximiter and antisymmetric octets.

4. Influence of the poles on the physical observables

$$\frac{d\sigma}{dM_i} = \left|\sum_i C_i T_{i \to \pi\Sigma}\right|^2 q_{\rm c.m.} , \qquad (10)$$

$$\frac{d\sigma}{dM_i} = C |T_{\pi\Sigma \to \pi\Sigma}|^2 q_{\rm c.m.} , \qquad (11)$$

where C is a constant, which has no justification. Indeed, if the sum in eq. (11) were dominated by the $\bar{K}N \to \pi\Sigma$ amplitude, then the second resonance R_2 would be weighted ೧ more, since it has a stronger coupling to the *KN* state, resulting into an apparent narrower resonance peaking at higher energies. This can be seen in Fig. 2. In ref. [4] the C_i coefficients foor KN and $\pi\Sigma$ were fitted to the data. The fact is that if there were **u** only one resonance eqs. (10) and (11) would lead to the same shape of the distribution **s** ince all the amplitudes would have the same resonance shape. But the existence of two poles makes the sum in eq. (10) dependent on the weights C_i and then dependent on the particular reaction. Hence, from now on, a theoretical claim about understanding the $\Lambda(1405)$ properties has to be substanciated by a simultaneous theoretical analysis of the ೧ particular reaction where this resonance has been seen. In this sense, there is a recent work [21] in which the dynamics of the $\pi^- p \to K^0 \pi \Sigma$, from where the nominal $\Lambda(1405)$ resonance comes, has been studied and the particular shape of the resonance found in this reaction is traced back to a nontrivial combination of chiral mechanisms involving the meson pole and contact term in the $MB \rightarrow MMB$ amplitudes together with the contribution of the s-wave $N^*(1710)$ resonance which has a strong coupling to the MMBsystem, as proved by the large decay width into $\pi\pi N$.



5. Conclusions

In both approaches a set of resonances is generated dynamically from the interaction of the octet of pseudoscalar mesons with the octet is generated dynamically from the interaction of the totaches a set of resonances a set of resonances is generated dynamically from the interaction of the totaches a set of resonances are set of the totaches as the totaches and totaches a set of the between the set of the totaches degenerated between to the totaches degenerated between totaches degenerated between totaches and totaches a set of the between the between

Another interesting finding is the suggestion that it is possible to find out the existence of the two resonances by performing different experiments, since in different experiments the weights by which the two resonances are excited are different. In this respect we call the attention to one reaction, $K^-p \to \Lambda(1405)\gamma$, which gives much weight to the two resonances.

resonance which couples strongly to the KN states and, hence, leads to a peak structure in the invariant mass distributions which is narrower and appears at higher energies than the experimental A(1405) peaks observed in hadronic experiments performed so far.

Acknowledgments

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