1

# Quark model description of the $NN^*(1440)$ potential

B. Juliá<sup>a</sup>, F. Fernández<sup>a</sup>, A. Valcarce<sup>a</sup>, and P. González<sup>b</sup>

<sup>a</sup>Grupo de Física Nuclear, Universidad de Salamanca, E-37008 Salamanca, Spain

<sup>b</sup>Dpto. de Física Teórica-IFIC, Universidad de Valencia-CSIC, E-46100 Burjassot, Valencia, Spain

We derive a  $NN^*(1440)$  potential from a non-relativistic quark-quark interaction and a chiral quark cluster model for the baryons. By making use of the Born-Oppenheimer approximation we examine the most important features of this interaction in comparison to those obtained from meson-exchange models.

### 1. INTRODUCTION

Baryonic resonances play a major role in the understanding of reactions that take place in nucleons and nuclei in the so-called intermediate energy regime [1]. In particular, the low-lying nucleonic resonances  $\Delta(1232)$  and  $N^*(1440)$ , can be now analyzed in more detail due to the development of specific experimental programs in TJNAF, Uppsala...

In this context the transition,  $NN \to NR$  (R: resonance), and direct  $NR \to NR$ and  $RR \to RR$  interactions should be understood. Usually these interactions have been written as straightforward extensions of some pieces of the  $NN \to NN$  potential with the modification of the values of the coupling constants, extracted from their decay widths. Though this procedure can be appropriate for the very long-range part of the interaction, it is under suspicion at least for the short-range part for which the detailed structure of the baryons may determine to some extent the form of the interaction. This turns out to be the case for the  $NN \to N\Delta$  and  $N\Delta \to N\Delta$  potentials previously analyzed elsewhere [2]. It seems therefore convenient to proceed to a derivation of these potentials based on the more elementary quark-quark interaction.

This is the purpose of this talk: starting from a quark-quark non-relativistic interaction, we implement the baryon structure through technically simple gaussian wave functions and we calculate the potential at the baryonic level in the static Born-Oppenheimer approach. The  $N^*(1440)$ , the Roper resonance, considered as a radial excitation of the nucleon, is taken as a stable particle. For dynamical applications its width should be implemented through the coupling to the continuum.

We center our attention in the  $NN^* \rightarrow NN^*$  potential where a complete parallelism with the  $NN \rightarrow NN$  case can be easily established. Notice that the quark-quark interaction parameters are fixed (from the  $NN \rightarrow NN$  case) and are kept independent of the baryons involved in the interaction. This eliminates the bias introduced in models at the baryonic level by a different choice of effective parameters according to the baryon-baryon interaction considered (this effectiveness of the parameters may hide distinct physical effects).

## 2. THE NN\*(1440) WAVE FUNCTION

The wave function of a two-baryon system,  $B_1$  and  $B_2$ , with a definite symmetry under the exchange of the baryon quantum numbers is written as [3]:

$$\Psi_{B_{1}B_{2}}^{ST}(\vec{R}) = \frac{\mathcal{A}}{\sqrt{1+\delta_{B_{1}B_{2}}}} \sqrt{\frac{1}{2}} \left\{ \left[ B_{1}\left(123; -\frac{\vec{R}}{2}\right) B_{2}\left(456; \frac{\vec{R}}{2}\right) \right]_{ST} + (-1)^{f} \left\{ \left[ B_{2}\left(123; -\frac{\vec{R}}{2}\right) B_{1}\left(456; \frac{\vec{R}}{2}\right) \right]_{ST} \right\},$$
(1)

being  $\mathcal{A}$  the six-quark antisymmetrizer given by:

$$\mathcal{A} = (1 - \sum_{i=1}^{3} \sum_{j=4}^{6} P_{ij})(1 - \mathcal{P}), \qquad (2)$$

where  $\mathcal{P}$  exchanges the three quarks between the two clusters and  $P_{ij}$  exchanges quarks i and j.

If one projects on a state of definite orbital angular momentum L, due to the  $(1 - \mathcal{P})$  operator in the antisymmetrizer the wave function  $\Psi_{B_1B_2}^{ST}(\vec{R})$  vanishes unless:

$$L + S_1 + S_2 - S + T_1 + T_2 - T + f = \text{odd}.$$
(3)

Since  $S_1 = \frac{1}{2} = S_2$ ,  $T_1 = \frac{1}{2} = T_2$ , this fixes the relative phase between the two components of the wave function at Eq. (1) to be:

$$f = S + T - L + \text{odd} \,. \tag{4}$$

It is important to realize that for the NN system f is necessarily even in order to prevent the vanishing of the wave function. No such restriction exists for  $NN^*$ . Therefore, there are  $NN^*$  channels (f odd) with no counterpart in the NN case.

We will assume the three-quark wave function for the quark clusters at a position  $\vec{R}$  to be given by

$$|N\rangle = |[3](0s)^3\rangle, \qquad (5)$$

$$|N^*\rangle = \sqrt{\frac{2}{3}} |[3](0s)^2(1s)\rangle - \sqrt{\frac{1}{3}} |[3](0s)(op)^2\rangle, \qquad (6)$$

explicitly,

$$N(\vec{r}_1, \vec{r}_2, \vec{r}_3; \vec{R}) = \prod_{n=1}^3 \left(\frac{1}{\pi b^2}\right)^{3/4} e^{-\frac{(\vec{r}_n - \vec{R})^2}{2b^2}} \otimes [3]_{ST} \otimes [1^3]_c \,, \tag{7}$$

and

$$N^*(\vec{r_1}, \vec{r_2}, \vec{r_3}; \vec{R}) = (\sqrt{\frac{2}{3}}\phi_1 - \sqrt{\frac{1}{3}}\phi_2) \otimes [3]_{ST} \otimes [1^3]_C, \qquad (8)$$

being

$$\phi_1 = \frac{\sqrt{2}}{3} \left(\frac{1}{\pi b^2}\right)^{9/4} \sum_{k=1}^3 \left[\frac{3}{2} - \frac{(\vec{r_k} - \vec{R})^2}{b^2}\right] \prod_{i=1}^3 e^{-\frac{(\vec{r_i} - \vec{R})^2}{2b^2}},\tag{9}$$

and

$$\phi_2 = -\frac{2}{3} \left( \frac{1}{\pi^{\frac{9}{4}} b^{\frac{13}{2}}} \right) \sum_{j < k=1}^3 (\vec{r}_j - \vec{R}) \cdot (\vec{r}_k - \vec{R}) \prod_{i=1}^3 e^{-\frac{(\vec{r}_i - \vec{R})^2}{2b^2}},\tag{10}$$

where  $[3]_{ST}$  and  $[1^3]_c$  stand for the spin-isospin and color part, respectively. The validity of the harmonic oscillator wave functions to calculate the two-baryon interaction has been discussed in ref. [4].

The quark-quark potential we use can be written in terms of the interquark distance  $\vec{r}_{ij}$  as:

$$V_{qq}(\vec{r}_{ij}) = V_{CON}(\vec{r}_{ij}) + V_{OGE}(\vec{r}_{ij}) + V_{OPE}(\vec{r}_{ij}) + V_{OSE}(\vec{r}_{ij}), 3$$
(11)

where  $V_{CON}$  stands for the confining potential, and  $V_{OGE}$ ,  $V_{OPE}$ , and  $V_{OSE}$  for onegluon, one-pion and one-sigma exchange potentials, respectively. The expression of these potentials has been very much detailed elsewhere [5].

The baryon-baryon potential is obtained as the expectation value of the energy of the six-quark system minus the self-energy of the two clusters. The presence of the antisymmetrization in the two-baryon wave function has also an important dynamical effect, the baryon-baryon potential contains quark-exchange contributions where the interaction takes place between two baryons that exchange a quark.

## 3. RESULTS

In Figure 1 we show the results for the  $NN^*$  potential in terms of the interbaryon distance R for two channels:  ${}^{1}S_0(T = 0)$ , which is forbidden in the NN system, and the  ${}^{1}S_0(T = 1)$ , which is allowed in the NN system. In this last case, the result is quite close to the corresponding channel in the NN system, a consequence of the near to identity similarity of N and  $N^*$ . As can be seen, the behavior in the two previous channels is completely different such that it could not be obtained by a simple rescaling of the vertex coupling constants from one case to the other. In order to emphasize the effects of quark antisymmetrization, we have compared to a direct potential without quarkexchange contributions. We have also separated the contribution of the different terms of the quark-quark potential in Eq.

As general features of the results we may remark that the OPE interaction determines the very long range behavior (R>4 fm), the OPE altogether with the OSE are responsible for the long-range par (1.5 fm < R < 4 fm), and OPE, OSE and OGE added to quark-exchange determine the attractive or repulsive character of the interaction at the intermediate- and short-range.

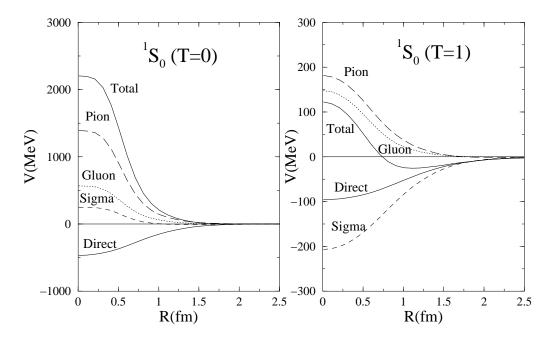


Figure 1.  ${}^{1}S_{0}(T=0)$  and  ${}^{1}S_{0}(T=1)$  NN<sup>\*</sup> potentials.

Certainly data on  $NN^* \rightarrow NN^*$  phase shifts can be only obtained indirectly and no direct experimental test of our results can actually be performed. Nonetheless, our results should help to a better understanding of baryonic processes at a microscopic level and serve as a guide when dealing with reactions where some indicative predictions are needed in theoretical as well as in experimental studies. The elastic  $\pi d$  scattering above the Roper threshold as well as the breakup of the deuteron into  $NN^*$  channels, although not available for the moment, should serve as a test of the results we have derived.

A transition potential  $NN \to NN^*$  can also be derived within the same framework. Althought this transition does not show forbidden channels, the quantum numbers are fixed by the NN system, the quark model provides a parameter-free prediction. This potential can be tested in several reactions [6]. We have determined the  $NN^*(1440)$  probability on the deuteron by means of a multichannel calculation including:  ${}^{3}S_{1}^{NN}$ ,  ${}^{3}D_{1}^{NA}$ ,  ${}^{3}D_{1}^{\Delta\Delta}$ ,  ${}^{7}D_{1}^{\Delta\Delta}$ ,  ${}^{7}G_{1}^{\Delta\Delta}$ ,  ${}^{3}S_{1}^{NN^*(1440)}$ , and  ${}^{3}D_{1}^{NN^*(1440)}$ , finding for the Roper components 0.003% and 0.024%, respectively, much lower than the  $\Delta\Delta$  ones ( $\approx 0.25\%$ ).

#### 4. ACKNOWLEDGMENTS

We thank to D. R. Entem for the calculations on the deuteron.

#### REFERENCES

- 1. E. Oset, H. Toki, and W. Weise, Phys. Rep. 82, 282 (1982).
- 2. A Valcarce, F. Fernández, P. González, and V. Vento, Phys. Rev. C52, 38 (1995).
- 3. A Valcarce, F. Fernández, and P. González, Phys. Rev. C56, 3026 (1997).
- 4. A Valcarce, F. Fernández, P. González, and V. Vento, Phys. Lett. B367, 35 (1996).
- 5. F. Fernández, A. Valcarce, U. Straub, and, A. Faessler, J. Phys. **G19**, 2013 (1993).
- 6. H. P. Morsch and P. Zupranski, Phys. Rev. C61, 024002 (1999).