# Nuclear structure of ${ }^{231}$ Ac 

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#### Abstract

The low-energy structure of ${ }^{231} \mathrm{Ac}$ has been investigated by means of $\gamma$ ray spectroscopy following the $\beta^{-}$decay of ${ }^{231}$ Ra. Multipolarities of 28 transitions have been established by measuring conversion electrons with a mini-ORANGE electron spectrometer. The decay scheme of ${ }^{231} \mathrm{Ra} \rightarrow{ }^{231} \mathrm{Ac}$ has been constructed for the first time. The Advanced Time Delayed $\beta \gamma \gamma(t)$ method has been used to measure the half-lives of five levels. The moderately fast $\mathrm{B}(\mathrm{E} 1)$ transition rates derived suggest that the octupole effects, albeit weak, are still present in this exotic nucleus.


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Key words: RADIOACTIVITY, ${ }_{87}^{231} \mathrm{Fr}$ and ${ }_{88}^{231} \mathrm{Ra}$ [from ${ }_{92}^{238} \mathrm{U}(\mathrm{p}, \mathrm{xpyn})$ mass separation]; Measured $E_{\gamma}, I_{\gamma}, \mathrm{I}(\mathrm{CE}), \gamma-\gamma$ and $\gamma$-e ${ }^{-}$coincidences, $\mathrm{T}_{1 / 2}$; Deduced ${ }_{89}^{231}$ Ac levels, ICC multipolarities, spin-parities, B(X $\lambda$ ); Advanced Time Delayed $\beta \gamma \gamma(\mathrm{t})$ method; $\mathrm{Ge}, \mathrm{Si}(\mathrm{Li})$, Plastic $\mathrm{BaF}_{2}$ detectors; mini-OrANGE spectrometer.

## 1 Introduction

Since the observation of low-lying $\mathrm{K}^{\pi}=0^{-}$bands in doubly even radium nuclei [1] the possibility that some nuclei can be described by a mean field approach with broken reflection symmetry has been considered [2]. Numerous experimental and theoretical discoveries were done in the 80's providing extra evidence of reflection asymmetric octupole deformation around $A=225$ [3]. Many of these nuclei have been studied at ISOLDE in beta decay experiments [4]. In odd-A nuclei an important feature of static octupole deformation is the observation of parity doublets, i.e. rotational bands lying close in excitation energy with the same intrinsic parameters and spins, but opposite parity.

A survey of the available data for odd-A nuclei reveals that the largest amount of octupole correlations is present in the Ac and Pa nuclei. In particular for the odd actinium isotopes near $\mathrm{A}=225$ spectroscopy studies have been done in $\alpha$ decay ( ${ }^{219-225} \mathrm{Ac}$ ), $\beta$ decay $\left({ }^{225-231} \mathrm{Ac}\right.$ ) and reactions (see 5] and references therein). The high spin states of ${ }^{219} \mathrm{Ac}$ observed in heavy-ion fusion reactions [6] have been described using small quadrupole and octupole deformation components $\beta_{2}=\beta_{3}=0.05$. The nucleus ${ }^{221} \mathrm{Ac}$ was predicted as a good example of octupole instability with the $\mathrm{K}=5 / 2$ and $\mathrm{K}=3 / 2$ band heads calculated to be very close in energy. Experimentally two bands were found [7] with the same angular momentum, opposite parity and an average difference of 44 keV between equivalent members of the doublets. This fact suggested parity doublets but the differences in intrinsic dipole moment $\left(\mathrm{D}_{0}\right)$ values indicated that the two bands originate from different orbitals. The low-energy spectra of ${ }^{223,225} \mathrm{Ac}$ display the $\mathrm{K}=3 / 2$ and $\mathrm{K}=5 / 2$ parity doublets [38]. In ${ }^{227} \mathrm{Ac}$ only the $\mathrm{K}=5 / 2$ parity doublet band, observed at 300 keV excitation energy, can be described in terms of static octupole deformation. In the case of ${ }^{229} \mathrm{Ac}$ the four $\mathrm{K}=1 / 2^{ \pm}$and $\mathrm{K}=3 / 2^{ \pm}$bands observed in ( $\mathrm{t}, \alpha$ ) reactions [9] are interpreted either as normal Nilsson levels or by assuming a weak octupole coupling, $\beta_{3}=0.07$ [10]. In summary, the low energy properties of the ${ }^{223,225,227} \mathrm{Ac}$ isotopes have been accounted for using the reflection asymmetric rotor-plus-quasiparticle model [10] and, in this context, the ${ }^{219,229} \mathrm{Ac}$ isotopes have been described as shape transitional nuclei.

The study of transitional nuclei in the upper border of this octupole deformed region is of relevance to understand the interplay of octupole and quadrupole collectivities. In transitional nuclei the mechanism of grouping rotational bands differs from that of parity-doublets in nuclei with stable octupole deformation. Two intrinsic states (or rotational bands) with a given K and opposite parity have strong octupole correlations, if the dominant one-

[^0]quasiparticle component of the first partner coupled to the octupole phonon of the core forms the largest collective component in the structure of the second partner and vice versa. Experimentally one observes an enhancement of the E1 strength for the parity pair partner bands.

With this aim the IS322 collaboration at ISOLDE-CERN has carried out a systematic investigation of the heavy transitional Fr - Th nuclei, for which scarce spectroscopic information was available. These experiments have provided the first information on the absolute values of $\mathrm{B}(\mathrm{E} 1)$ in this octupole transitional region. Relatively large $\mathrm{B}(\mathrm{E} 1)$ rates have been measured indicating the presence of octupole correlations in ${ }^{227} \mathrm{Fr}$ [11, ${ }^{229} \mathrm{Ra}$ [12] and ${ }^{229} \mathrm{Th}$ [13] 14]. Much weaker but still noticeable are the correlations in the heavier ${ }^{231} \mathrm{Ra}$ [15] and ${ }^{231} \mathrm{Th}$ [16] isotopes. We report here on the structure of their isobar, ${ }^{231} \mathrm{Ac}$.

Actinium-231 was first produced by bombarding ${ }^{232} \mathrm{Th}$ with $14-\mathrm{MeV}$ neutrons [17]. Its half-life was then measured to be $7.5 \pm 0.1 \mathrm{~min}$ and the strongest $\gamma$ rays into ${ }^{231} \mathrm{Th}$ were identified. The proton pickup ( $\mathrm{t}, \alpha$ ) reaction was used to investigate the structure of ${ }^{233} \mathrm{~Pa}$ and its isotone ${ }^{231} \mathrm{Ac}$ [9. In the case of ${ }^{231} \mathrm{Ac}$ the lack of information from beta decay caused that the band assignments from the experimental cross sections were only based on a comparison to those assigned to the isotone ${ }^{233} \mathrm{~Pa}$. A later study, and the only previous investigation where the $\beta^{-}$decay of ${ }^{231} \mathrm{Ra}$ has been reported [18], assigned six gamma lines to ${ }^{231}$ Ac. From their time behaviour a half-life of $103(3)$ s was obtained for ${ }^{231}$ Ra, but no attempt to build a level scheme was made.

In this paper the low-energy structure of ${ }^{231} \mathrm{Ac}$ fed in the $\beta^{-}$decay of ${ }^{231} \mathrm{Ra}$ has been investigated by $\gamma-\gamma$ and $\gamma-\mathrm{e}^{-}$spectroscopy. Multipolarities of 28 transitions have been established by measuring conversion electrons with a miniORANGE electron spectrometer. The decay scheme of ${ }^{231} \mathrm{Ra} \rightarrow{ }^{231} \mathrm{Ac}$ has been constructed for the first time. The Advanced Time Delayed $\beta \gamma \gamma(t)$ method [19] has been used to measure the half-lives of several levels. The deduced B(E1) rates are used to infer the possible presence of octupole correlations in the ${ }^{231} \mathrm{Ac}$ nucleus.

## 2 Experimental Setup

The study on the ${ }^{231} \mathrm{Ac}$ structure is based on two sets of measurements performed at the PSB-ISOLDE on-line mass separator [20]. In both experiments, a 1 GeV proton beam from the CERN PS-Booster bombarded a $\mathrm{UC}_{2}$ - C target, producing via spallation reactions the $\mathrm{A}=231$ isobars. In the first experiment the excited structure of ${ }^{231} \mathrm{Ac}$ was populated directly from the $\beta$ decay of ${ }^{231} \mathrm{Ra}$ with an estimated production of $4 \times 10^{3}$ atoms per $\mu \mathrm{C}$. In the second experiment a $\mathrm{Ta}(\mathrm{Re})$ surface ionizer was employed, favouring the ionization
of Fr, and ${ }^{231} \mathrm{Ac}$ was populated through the decay chain of ${ }^{231} \mathrm{Fr} \rightarrow{ }^{231} \mathrm{Ra} \rightarrow$ ${ }^{231} \mathrm{Ac}$ [15], with an estimated yield of $7 \times 10^{4}{ }^{231} \mathrm{Fr}$ ions per $\mu \mathrm{C}$. The produced ions were accelerated to 60 kV and mass-separated before being collected onto a magnetic tape transport system which connected two independent but simultaneously operated measurement stations.

The radioactive beam was deposited in the centre of the fast timing station specially designed to measure the half-life of excited states in the nanoand pico-second range by the Advanced Time Delayed (ATD) $\beta \gamma \gamma(\mathrm{t})$ method [19|21|22]. The setup of this station consisted of a 3 mm thick NE111A plastic scintillator positioned behind the tape at the collection point and used as fast-timing $\beta$-detector. The thickness was chosen to have an almost uniform response to the different $\beta$ energies. A 2.5 cm thick $\mathrm{BaF}_{2}$ scintillator was used as fast-timing gamma detector. In addition, there were two HPGe detectors with relative efficiencies of $70 \%$ and $40 \%$, respectively, and energy ranges from 30 to 1500 keV . They were used to provide a unique selection of the $\gamma$ decay branch in the $\beta \gamma \gamma(\mathrm{t})$ method and to study $\gamma \gamma$ coincidences in order to determine the level scheme. A detailed description of the setup is given elsewhere [15]. Up to seven parameters were recorded simultaneously for each event, namely the $\beta$ energy and up to three $\gamma$ energies plus the time differences between the $\beta$ signal and a given coincident $\gamma$ event. The energy and efficiency calibrations of the gamma detectors were determined using a ${ }^{140} \mathrm{Ba}$ source and an absolutely calibrated mixed source of ${ }^{57} \mathrm{Co},{ }^{88} \mathrm{Y},{ }^{109} \mathrm{Cd},{ }^{139} \mathrm{Ce},{ }^{113} \mathrm{Sn},{ }^{137} \mathrm{Cs}$ and ${ }^{241} \mathrm{Am}$.

The $\mathrm{A}=231$ sample was transported one meter away by the tape to the conversion electron station specially designed for gamma identification and electron conversion measurements. It consisted of an electron spectrometer, a gamma telescope and a $\beta$ detector.

The electron spectrometer incorporated a mini-ORANGE filter [2324] and a 2 mm thick $\mathrm{Si}(\mathrm{Li})$ detector with an active area of $300 \mathrm{~mm}^{2}$ and 1.9 keV energy resolution at $\sim 100 \mathrm{keV}$. The detector was cooled to liquid nitrogen temperature by means of a copper cold finger. For the mini-orange filter a first set of permanent magnets was carefully shaped according to the design of van Klinken and Wisshak. A relatively high transmission of $1.8 \%$ of $4 \pi$ was achieved, but over a small energy range. Thus the set of magnets finally chosen had a lower $(\simeq 0.5 \%)$ but more uniform transmission over a broad range of energies $(\sim 25-800 \mathrm{keV})$. This set consisted of three equally spaced rectangular magnetic plates of $50 \times 20 \times 5 \mathrm{~mm}^{3}$, with the largest dimension oriented radially. Measurements with different mini-ORANGe and detector positions showed that the transmission maximum was achieved with de $\mathrm{Si}(\mathrm{Li})$ detector at 150 mm from the source and the MINI-ORANGE approximately midway between the source and the detector. A central lead absorber was used to shield the detector from direct X-rays and $\gamma$ rays.

The gamma telescope consisted of a $19.5 \mathrm{~cm}^{3}$ planar HPGe followed by a $20 \%$ coaxial HPGe, both in a single cryostat behind a $300 \mu \mathrm{~m}$ beryllium window. The FWHM energy resolution varied from 0.4 keV at very low energies up to 1.4 keV at $\mathrm{E}_{\gamma}=560 \mathrm{keV}$ for the planar detector, and between 1.3 keV at $\mathrm{E}_{\gamma}=137 \mathrm{keV}$ and 2.5 keV at $\mathrm{E}_{\gamma}=1836 \mathrm{keV}$ for the coaxial detector. Special care was given to detect low energy $\gamma$ rays with the limit of sensitivity in the planar detector being 4 keV in single events and about 12 keV in coincidence events. The Ge-escape peaks of the main L X-ray components of Ra, Ac and Th from 4.9 to 6.7 keV are clearly identified. This blurs unfortunately the possible contribution of any low energy gamma lines. The L X-rays from ${ }^{241} \mathrm{Am}$ have allowed to extend the efficiency calibration down to 13.4 keV . Moreover, $\beta$-gated $\gamma$ ray singles spectra were also recorded with the coaxial Ge detector. For beta-gating, a NE102 plastic scintillator was placed outside the chamber in front of the gamma telescope. Simultaneously to the gamma spectra, conversion electron singles spectra were measured with the electron spectrometer. By dividing the acquisition time into 8 consecutive subgroups, $\gamma$ multispectra from the planar Ge detector, the $\beta$-gated coaxial Ge detector and the electron detectors were also recorded allowing time evolution studies. The $\mathrm{e}^{-}$and $\gamma$ signals were also recorded in list-mode allowing for an identification of $\gamma$ lines in coincidences down to 12 keV . The energy and efficiency calibrations for these detectors were obtained using sources of ${ }^{133} \mathrm{Ba}$ and ${ }^{152} \mathrm{Eu}$, and the practically summing-free mixed source previously described. Singles spectra from the planar detector as well as electron and $\beta$-gated $\gamma$ singles spectra for the coaxial HPGe were collected in the conversion electron station.

Data were collected in three different modes of operation. In the first two, measurements were conducted simultaneously at the two stations, i.e. while a sample was measured in the conversion electron station a new one was collected at the fast timing one. The time cycle was chosen to enhance the nucleus activity of interest in the isobaric chain. The time interval had to be slightly shorter than a multiple of the proton supercycle from the CERN PS-Booster. In the first experiment the cycles were chosen as 17 s and 190 s , and in the second one as 26 s and 200 s , respectively, to enhance the decay of ${ }^{231} \mathrm{Fr}\left(\mathrm{T}_{1 / 2}=17.5(8) \mathrm{s}\right)$ and ${ }^{231} \mathrm{Ra}\left(\mathrm{T}_{1 / 2}=103(3) \mathrm{s}\right)$. In the third mode of operation the tape was stopped, and the beam was continuously deposited at the collection point in order to enhance the decay of ${ }^{231} \mathrm{Ac}$ to ${ }^{231} \mathrm{Th}\left(\mathrm{T}_{1 / 2}=450\right.$ s). The data acquisition was divided in 8 subgroups of equal time intervals for gamma assignment and half-life determination. In the first experiment about $7000{ }^{231} \mathrm{Ra}$ ions/s were transmitted to the setup at the fast timing station. The average count rate in the beta detector was about 100 counts/s in the short cycle and 1350 counts/s in the long cycle. Both cycles were used for the present analysis, with a total of 425 Mb of list mode data over 33 hours. In the second experiment up to $110000{ }^{231} \mathrm{Fr}$ ions/s reached the fast timing station. The average count rate in the beta detector was $\sim 8000$ counts $/ \mathrm{s}$ in the short cycle. In the long cycle the beam intensity was reduced to limit the
count rate in the beta detector to 10000 counts/s. Only data from the long cycle has been used for the present analysis, with 5 hours of data taking. The results on ${ }^{231} \mathrm{Ra}$ and ${ }^{231} \mathrm{Th}$ have been reported in [15] and [16], respectively.

## 3 Experimental results

In the present study, the results on the decay of ${ }^{231} \mathrm{Ra}$ to ${ }^{231} \mathrm{Ac}$ are based on the data collected with the long cycles. The intensity ratio of the gamma lines between the short and long cycles has helped to identify the low intensity gamma transitions. The most intense $\gamma$ transitions have been assigned to the decay of ${ }^{231} \mathrm{Ra}$ by comparing their temporal behaviour to that of the ${ }^{231} \mathrm{Ac}$ X-rays. The fifteen most intense $\gamma$ transitions have been used to deduce the half-life value. The weighted mean value of the half-life is 104.1(8) s in good agreement but more precise than the previous value [18]. For more details of the analysis see [25].

## $3.1 \gamma$ ray singles and $\gamma-\gamma$ measurements

Fig. 1 shows the low energy gamma spectrum recorded in the planar detector at the conversion electron station. Notice that the sensitivity of the detector reached below 5 keV of energy. The aim was to identify the expected low energy transitions as proposed to exist in the $2 \mathrm{p}-2 \mathrm{n}$ neighbour ${ }^{227} \mathrm{Fr}$ [11]. The peaks observed between 4.8 and 6.4 keV have been identified as the $\mathrm{K}_{\alpha}$ and $\mathrm{K}_{\beta}$ escape peaks in germanium of the most intense L X-ray components of Ac and Th. These low energy peaks are about 10-12 \% of the L X-ray assuming that the relative variation of efficiency in this energy range is the same, and that the efficiencies at these very low energies followed the curves given in [26]. The lines marked with an asterisk belong to the decay chain of the $A=231$ molecule ${ }^{212} \mathrm{RaF}$ observed mainly in the data of the second experiment.

The gamma transitions belonging to the $\beta$ decay of ${ }^{231} \mathrm{Ac}$ are listed in Table $\mathbb{1}$, the energies of the $\gamma$ transitions are the average of the values obtained in the two experiments. The uncertainties in the intensity values were calculated as a weighted mean of the statistical errors and the error in the efficiency curve. The latter one was estimated to be $10 \%$ for the planar detector up to energies of 40 keV and $6 \%$ for higher energies. The uncertainties of the efficiency curve of the coaxial detector are estimated to be $5 \%$ up to 205 keV and $3 \%$ for higher energies. Profiting from the good resolution of the planar detector (0.4 keV at 6 keV and 0.5 keV at 54 keV ) some transitions could be only separated in this detector, in these cases the intensity was taken from the planar detector only. Summing of the K X-rays with the most intense $\gamma$ lines was observed in
the planar detector. The summing contribution was estimated to be 1.2(2) \% from the intensity of the peaks observed at $145.05(10)$ and $168.72(8) \mathrm{keV}$ in comparison with the individual intensities of the K X-ray and the 54.29 and $77.97 \mathrm{keV} \gamma$ rays. These low intensity peaks were not observed in the coaxial 20 \% HPGe detector placed behind the planar detector. Therefore we consider the relative intensity given in Table 1 for the $409.9 \mathrm{keV} \gamma$ transition as the one obtained in the coaxial detector in order to avoid the possible contribution of summing of the 204.79(10) and 205.00(10) $\mathrm{keV} \gamma$ lines. Most of the transitions have been observed in singles, only some very low energy transitions have emerged in $\mathrm{e}^{-}-\gamma$ coincidences, see subsection 3.2. The relative intensities of $\gamma$ transitions are listed in Table 1. The 54.29 keV transition has been chosen for the normalization, since the most intense one at 205 keV is a doublet as clearly observed in the coincidence study.

Some $\gamma$ lines could only be observed or separated in coincidences and therefore their relative intensity was obtained from coincidences and marked with a footnote in Table 1. The values obtained were compatible with the expected values in singles. When the peaks are doublets with $\gamma$ lines belonging to the decay of an isobar or a contaminant, the extra contribution has been subtracted and specifically indicated with a footnote. In Table 1, the $\gamma$ transitions, their energies, intensities, the criteria used for the identification, $\gamma$ transitions seen in coincidences and placement in the level scheme are given. A careful study of the shape of the 205 keV peak has been done in the planar detector, where the FWHM at this energy is of 0.7 keV . The least square fit to two peaks indicates that their energies are at maximum 0.2 keV apart with intensities of $40 \%$ and $60 \%$ for peaks with centroids at 204.79 and 205.00 keV , respectively. In the projection of the $\gamma-\gamma$ coincidence matrix a comparison of intensity of the 205.00 and the $198.18 \mathrm{keV} \gamma$ lines both de-exciting the 266.76 keV state has given a relative intensity for this component of $60 \%$ of the total gamma intensity in good agreement with the value deduced from singles.

The $\beta$ gated $\gamma-\gamma$ coincidences were collected at the first station and sorted offline. There are intense low energy transitions in ${ }^{231} \mathrm{Ac}$ coincident with many strong $\gamma$ lines, see, for instance, the $\gamma$ spectrum coincident with the 54.29 keV transition displayed in the upper part of Fig. 2. The spectrum shown is a sum of the reciprocal projection placed in both HPGe detectors of the first station. As the threshold is different for these two detectors, the summed projection is only reliable at energies higher than 30 keV . For comparison the bottom part of Fig. 22 shows the electron coincidence spectrum gated on the $54.29 \mathrm{keV} \gamma$ line seen in the planar detector (for $\gamma-\mathrm{e}^{-}$coincidences see section 3.2). Column 7 of Table 1 lists the strong $\gamma-\gamma$ coincidences observed in the present measurements; weaker but still convincing coincidences are given within parenthesis.

The gate on the $198.18 \mathrm{keV} \gamma$ line shows in coincidence the Ac K X-rays and
the component of the 205 -doublet at 204.79 keV . Therefore the $\alpha_{K}$ internal conversion coefficient for this component is extracted from the ratio of intensities of the $\mathrm{K}_{\alpha}+\mathrm{K}_{\beta}$ and the $204.79 \mathrm{keV} \gamma$ line corrected by the fluorescence yield $\omega_{K}$ for Ac equal to 0.969 (value taken from appendix F of [5]), following the formula $\alpha_{K}=\frac{I_{K_{\alpha}}+I_{K_{\beta}}}{I_{\gamma}} \frac{1}{\omega_{K}}$. The resulting $\alpha_{K}$ value is $1.77(24)$ for the $204.79 \mathrm{keV} \gamma$ transition.

### 3.2 Internal conversion coefficients and $\gamma-e^{-}$coincidences

The conversion coefficients were obtained from the simultaneous measurement of gammas and conversion electrons at the second station. The analysis was done using the data from the long cycle, where the conversion electrons of the 66.2 keV transition in ${ }^{231} \mathrm{Ra}$ that clearly dominate the electron spectrum in the short cycle (see Fig. 4 of ref. [15]) are not visible. The electron spectrum obtained using the long cycle measurement time is shown in Fig. 3. The main electron lines correspond to the K components of the 221 keV M1 transition in ${ }^{231} \mathrm{Th}$ and the 204.79 keV M1 transition in ${ }^{231} \mathrm{Ac}$.

The conversion coefficient values were obtained using the transmission function curve of the MINI-ORANGE spectrometer, determined by internal calibration with the conversion coefficients of the transitions in ${ }^{231} \mathrm{Th}$ [27. When an electron peak corresponds partially to conversion electrons of ${ }^{231} \mathrm{Ac}$ that overlap with the ones of a line in ${ }^{231} \mathrm{Th}$, the latter contribution has been corrected for by using the known conversion coefficients for transitions in ${ }^{231} \mathrm{Th}$ [27]. The internal conversion coefficients obtained in this work, the theoretical values from [28] and the multipolarities established for the transitions in ${ }^{231} \mathrm{Ac}$ are presented in Table 2. The total conversion coefficient, $\alpha_{T}$, needed to calculate the intensity balance has been deduced from the experimental conversion coefficient values in the following way. If only one or two of the partial conversion coefficients are extracted from the data and they are sufficient to determine the multipolarity $(\mathrm{X} \lambda)$ of the transition, we deduce $\alpha_{T}(\exp )=$ $\alpha_{i}(\exp ) \alpha_{T}^{t h}(X \lambda) / \alpha_{i}^{t h}(X \lambda)$ with $\mathrm{i}=\mathrm{K}, \mathrm{L} 1+\mathrm{L} 2, \Sigma \mathrm{M}$ or $\Sigma \mathrm{N}$. The total intensities obtained from the determined $\alpha_{T}$ values are given in the second column of Table 2,

The conversion coefficient for the doublet at 205 keV has been obtained in the following way. As previously explained we obtained an $\alpha_{K}$ value of 1.77(24) for the 204.79 keV transition from $\gamma-\gamma$-coincidences corresponding to an M1 multipolarity. This value almost exhausts the full electron peak observed for the K component. Knowing the M1 character of the 204.79 keV transition, we have used the theoretical conversion coefficient to extract its contribution to the electron spectrum and from that we estimate the contribution of the 205.00 keV transition to the electron spectrum. The extracted conversion coefficients
given in Table 2have large error bars, but clearly exclude the M1 multipolarity for the 205.00 keV transition.

The coincident events involving $\gamma$ rays in the planar Ge detector and conversion electrons in the MINI-ORANGE spectrometer have allowed us to identify low energy transitions. The $\mathrm{e}^{-}-\gamma$ coincidences have also been used to identify to which nucleus the converted gamma line belonged by studying the coincident X-rays in the planar detector.

### 3.3 Level lifetime measurements

The Advanced Time Delayed (ATD) $\beta \gamma \gamma(\mathrm{t})$ technique detailed in [19, 21, 22 ] has been used to measure level lifetimes in ${ }^{231} \mathrm{Ac}$. This method involves triple coincidences of $\beta-\mathrm{BaF}_{2}-\mathrm{Ge}$ events. The timing information is provided by the coincidences between the fast-timing $\beta$ and $\gamma\left(\mathrm{BaF}_{2}\right)$ detectors, while a coincidence with one of the two Ge detectors permits to univocally select the desired decay branch. Two different analysis methods are applicable, depending on the lifetime range of the level of interest. Long lifetimes, observed as slopes on the time-delayed tail of the time spectra, are measured by the shape deconvolution method [19]. For lifetimes in the sub-nanosecond regime the centroid shift technique is used. Both methods can be applicable in some cases. Three calibration curves are essential for the centroid shift measurements. The prompt curve describes the timing response of the $\mathrm{BaF}_{2}$ detector as a function of the energy of the full-energy peak from an incident $\gamma$ ray. The time response curve provides the time response for the complete energy spectrum generated by a monoenergetic transition; and, finally, the Compton correction curve corresponds to the time shift between Compton events of the same energy but originated by prompt primary $\gamma$ rays of higher energies. The first two curves were obtained off-line at ISOLDE using a pre-calibrated source of ${ }^{140} \mathrm{Ba} \rightarrow$ ${ }^{140} \mathrm{La} \rightarrow{ }^{140}$ Ce prepared at the OSIRIS fission product separator at Studsvik in Sweden [29,30]. The measurement of the Compton correction curve and a more exhaustive calibration of the prompt curve were performed on-line at OSIRIS using a variety of beams while preserving, as much as possible, the experimental geometry used at ISOLDE. Preliminary results of the lifetime values are given in [31].

- Lifetime of the 116.02 keV level

The slope-fitting method has been used to determine the lifetime of the 116.02 keV level. A clear asymmetry is observed in the time spectrum obtained as a projection onto the $\mathrm{BaF}_{2}-\mathrm{Ge}$ fast time difference signal of the 54.3 keV transition selected in the $\mathrm{BaF}_{2}$ detector and the 299.10 keV selected in the Ge detectors. Due to the low statistics of this time spectrum, it has been successively compressed in order to increase the statistics and
make use of a more convenient $\chi^{2}$ fit. An average value of $\mathrm{T}_{1 / 2}=14.3(11)$ ns has been obtained. The error bar takes into account the systematic error due to the use of a $\chi^{2}$ fit for a Poisson distribution and any possible deviation of the prompt time response from a Gaussian shape. As an example we show in the panel (a) of Fig. 4 the $\mathrm{BaF}_{2}$ energy spectrum projected from the $\beta$-Ge- $\mathrm{BaF}_{2}$ data (the gate in the Ge spectrum on the 299.10 keV line) and in the panel (b) of Fig. 4 the slope fitting of the fast-timing spectrum gated on the peak at 54.29 keV in the $\mathrm{BaF}_{2}$ and compressed by a factor of 30 .

- Lifetime of the 160.73 keV level

When gating on the 254.57 keV transition in the Ge detector spectrum and on the $54.29-77.97 \mathrm{keV}$ group in the $\mathrm{BaF}_{2}$ spectrum, the centroid shift of the time spectrum is equal to $\tau_{0}+\tau_{415}+\tau_{161}+\tau_{116}$ where $\tau_{0}$ is the prompt position, and $\tau_{415}, \tau_{161}$ and $\tau_{116}$ are the mean lifetimes $\left(\tau=\mathrm{T}_{1 / 2} / \ln 2\right)$ of the 415.31, 160.73 and 116.02 keV levels, respectively. A reference time spectrum obtained by gating on the 299.10 keV transition in the Ge spectrum and on the 54.29-77.97 keV region in the $\mathrm{BaF}_{2}$ spectrum has a centroid shift equal to $\tau_{0}+\tau_{415}+\tau_{116}$. The difference between these two centroid shifts has been measured to be $\tau_{161}<1298 \mathrm{ps}$, which yields $\mathrm{T}_{1 / 2}<900 \mathrm{ps}$ for the half-life of the 160.73 keV level.

- Lifetime of the 238.01 keV level

The double $\gamma$ ray cascade $247.65-232.71 \mathrm{keV}$ was used for the determination of the half-life of the intermediate level at 238.01 keV . We observe a centroid shift between the projected $\beta-\mathrm{BaF}_{2}(\mathrm{t})$ time spectrum obtained by selecting one transition in the $\mathrm{BaF}_{2}$ detector and the other in the Ge detectors and the one obtained by inverting the gates. This centroid shift directly provides the value of the lifetime of the 238.01 keV level. In this special case, there is no need to know the prompt position as it cancels out when calculating the difference between both centroid positions. The measurement gives a value of $\mathrm{T}_{1 / 2}=57(11) \mathrm{ps}$ for the 238.01 keV level.

- Lifetime of the 266.76 keV level

The two analysis methods, the deconvolution of the slope and the centroid shift have been employed to measure the half-life of the 266.76 keV level.
In the hereinafter discussion of the centroid shift analysis method, we adopt the following notation. If we consider a cascade of two gamma lines $\gamma_{1}$ and $\gamma_{2}$, where the Ge detectors are gated on the first transition $\gamma_{1}$, while a second gate on $\gamma_{2}$ is applied to the $\mathrm{BaF}_{2}$ detector, the time spectrum obtained by the projection onto the fast TAC will be labelled by $S=\left[\gamma_{1}(\mathrm{Ge})-\gamma_{2}\left(\mathrm{BaF}_{2}\right)\right]$. For the application of the centroid shift method to the 266.76 keV level we consider on the one hand the [198.18-204.8] cascade. The fitting of the centroid position in the time spectrum yields $\tau_{0}+\tau_{472}$, where $\tau_{0}$ is the prompt response position and $\tau_{472}$ is the mean lifetime of the 471.60 keV level, $S_{1}=[198.18-204.8]=\tau_{0}+\tau_{472}$. On the other hand, we take the [205.00-
204.8] cascade. As we cannot resolve the two components of the 205 keV doublet in the Ge detectors, the obtained time spectrum $S_{2}$ is actually the sum of two theoretical time spectra $\mathrm{S}_{21}=[205.00-204.8]$ and $\mathrm{S}_{22}=[204.79-$ 205.0] in the ideal case where both components could be completely resolved in the detector. If $A$ and $B$ are the fractions by which the $\mathrm{S}_{21}$ and $\mathrm{S}_{22}$ spectra contribute to the $\mathrm{S}_{2}$ spectrum, we will have:

$$
\begin{array}{r}
S_{2}=A \cdot S_{21}+B \cdot S_{22} \\
S_{2}=A\left(\tau_{0}+\tau_{472}\right)+B\left(\tau_{0}+\tau_{267}+\tau_{472}\right) \\
S_{2}=\tau_{0}+\tau_{472}+B \cdot \tau_{267}
\end{array}
$$

where $\tau_{267}$ is the mean lifetime of the 266.76 keV level. The difference of the two centroid shifts is then $S_{2}-S_{1}=B \cdot \tau_{267}$.
The value of $B$ is estimated from the analysis of the sum of the 205.0 keV gate projections onto the Ge detectors. $B$ is given by the ratio of the area of the 205.00 keV singlet and the sum of the areas of the $192.00,198.18 \mathrm{keV}$ peaks and the 205.0 keV doublet. This is so because the corresponding peak in the $\mathrm{BaF}_{2}$ detector includes all these contributions. We deduce a value of $69(7) \%$ for B . This gives a value of $\mathrm{T}_{1 / 2}=89(11) \mathrm{ps}$ for the half-life of the 266.76 keV level.

For the slope fitting analysis method, we had to generate a time-delayed spectrum "free" from the influence of the 471.60 keV level lifetime. In the same manner as for the centroid shift, this has been achieved by subtracting the projected time spectra from the [205-205] and [198-205] cascades, where the latter was corrected to account only for the contribution of the 266.76 keV level lifetime. From the deconvolution and fitting of this time spectrum, we obtain a value of $\mathrm{T}_{1 / 2}=85(29) \mathrm{ps}$ as the average of the half-lives from the last and more compressed spectra. This value is consistent with 89(11) ps obtained from the centroid shift method. We adopt a value of $\mathrm{T}_{1 / 2}=$ $90(20)$ ps for the half-life of the 266.76 keV level.

- Lifetime of the 471.60 keV level

The slope fitting of the time spectrum obtained when selecting the 198.18 keV line in the Ge detector and the 204.79 keV transition in the $\mathrm{BaF}_{2}$ deexciting in cascade the 471.60 keV level, allowed to obtain an upper limit for the lifetime of this level. By averaging over various values obtained from the fitting of time spectra with different compression factors, we obtain a value of 54 ps as a conservative upper limit for the half-life of the 471.60 keV level.

## 4 Decay scheme

The level scheme of ${ }^{231} \mathrm{Ac}$ adopted in this work is shown in Figs. 5-a, 5-b and 5-c. The level scheme includes 38 excited states covering about half of the $\mathrm{Q}_{\beta}$ energy window, see Table 3, A certain $\gamma$ transition is assigned to the decay if it fulfills at least one of the following criteria: i) the time behaviour of the intensity follows the value of the $\beta$ decay half-life, ii) for the very low intensity lines, the $\gamma$ line is assigned if the ratio of intensities for the short and long cycle is the same as the one obtained for the intense transitions already assigned, iii) it is seen in $\gamma-\gamma$ coincidences or iv) it is seen in $\mathrm{e}^{-}-\gamma$ coincidences with a transition already assigned. In this way more than one hundred transitions have been placed in the level scheme, with less than $2 \%$ of total intensity not being included in the level scheme. For the majority of the transitions in the decay scheme the measured energy is within 0.35 keV of the energy differences of the initial and final state. Total intensities were calculated using the determined total conversion coefficient as explained in the subsection 3.2. For the less intense transitions, whose conversion coefficients could not be experimentally determined, the lowest conversion coefficient value compatible with the parity of the two connecting states was adopted in most of the cases. The levels assured by coincidences are shown in Figs. 5-a, 5-b] and 5-c by continuous lines. The states determined by an energy fit are considered if at least two transitions connect the state to lower known states. The levels determined by energetics are shown in Figs. 5-a, 5-b, 5-0 with dashed lines.

The information available on the ${ }^{231} \mathrm{Ac}$ levels prior to the present work comes from the ${ }^{232} \mathrm{Th}(\mathrm{t}, \alpha){ }^{231} \mathrm{Ac}$ reaction study [9], where 17 levels were identified. The ground state of ${ }^{231} \mathrm{Ac}$ was assigned as the $\mathrm{I}=1 / 2$ member of the $1 / 2^{+}[400]$ band in agreement with the predictions of the Nilsson model. The level assignment was based on the comparison of the differential cross section estimates and experimental values. The calculation of the differential cross section used Nilsson wave functions with pairing and Coriolis effects included. The deformation parameters $\varepsilon_{2}$ and $\varepsilon_{4}$ were treated as free parameters to reproduce the observed levels resulting in $\varepsilon_{2}=0.24$ and $\varepsilon_{4}=-0.02$. The two main conclusions of the ( $\mathrm{t}, \alpha$ ) work [9] relevant for our study are the assignments of the ground state as the $1 / 2^{+}[400]$ band head and the $235(4) \mathrm{keV}$ state as the $3 / 2^{+}[402]$ band head. Both states are observed in our work and used to deduce the parity of the other levels established in this $\beta$ decay work up to 600 keV in excitation energy.

Recently deep inelastic one-proton transfer studies on ${ }^{137} \mathrm{Cs}$ produced by the ${ }^{232} \mathrm{Th}+{ }^{136} \mathrm{Xe}$ reaction [32] gave two extra bands tentatively assigned to ${ }^{231} \mathrm{Ac}$, since ${ }^{231} \mathrm{Ac}$ is expected to be produced in this type of proton transfer reaction as the main reaction partner of ${ }^{137} \mathrm{Cs}$. In this work Ac X-rays and several $\gamma$ lines, grouped in two bands with energies between 100 and 500 keV , were
observed. These bands were proposed to be the two-signature branches of a $\mathrm{K}=1 / 2$ rotational band, as observed in ${ }^{239} \mathrm{Pu}$. One of the bands was firmly proposed to be part of the ground state band of ${ }^{231} \mathrm{Ac}$ with the 163.3 keV transition assumed to connect to the ground state and as such it has passed to the literature [32],33]. In our work we observe a weak $\gamma$ line of 163.02 keV , but its relative intensity with respect to the main $\gamma$ transitions in ${ }^{231} \mathrm{Ac}$ changes by a factor of two when the time of the cycle is changed. So it was not assigned to the decay scheme. As none of the $\gamma$ lines of band A of ref. [32] is observed in our work we conclude that they probably connect high spin states not fed by $\beta$ decay.

We identify most of the low energy levels seen in the ( $\mathrm{t}, \alpha$ ) study although our scheme is richer. The starting point for parity assignment are the positive parity ground state and the $3 / 2^{+}$state at 238.01 keV characterized in the reaction work [9]. We assume that the $\beta$ feeding to the ground state is negligible, since this is a $\Delta \mathrm{I}=2$ and $\Delta \mathrm{K}=2$ transition from the $\mathrm{I}^{\pi}=5 / 2^{+}[522]{ }^{231}$ Ra ground state [15]. For the $\log f t$-value calculation [34] a $\mathrm{Q}_{\beta}$ value of 2306(102) keV is used together with the half-life value of $104.1(8)$ s obtained in this work. The $\mathrm{Q}_{\beta}$ value is derived from the ${ }^{231} \mathrm{Ra}$ mass measurement $(\Delta \mathrm{M}=38226(19)$ keV ) [35] and the value given in [36] for the ${ }^{231} \mathrm{Ac}$ mass $(\Delta \mathrm{M}=35920$ (100) keV ). A summary of the beta feeding and logft values for the different states is given in Table 3. The $\beta$ feedings compatible with zero are not given.

The low energy part of the level scheme is based in the $\gamma-\gamma$ coincidence observed between the 37.8 keV and the 77.17 and $77.97 \mathrm{keV} \gamma$ doublet and the 54.29 keV and the $56.50 \mathrm{keV} \gamma$ transitions. The latter has also been observed in $\mathrm{e}^{-}-\gamma$ coincidences.

The levels observed in this $\beta$ decay study are compared with the quasiparticle states and energies obtained from a self-consistent deformed Hartree-Fock calculation [37] with the Skyrme force SLy4 [38] and pairing correlations. The BCS approximation was used with constant pairing gaps for protons and neutrons of $\Delta_{p}=\Delta_{n}=0.8 \mathrm{MeV}$. The self-consistent deformation in ${ }^{231} \mathrm{Ac}$ is found at $\beta_{2}=0.22$ with $K^{\pi}=1 / 2^{+}$as the ground state. The deduced single particle energies place the band heads $K^{\pi}=1 / 2^{-}$at $192 \mathrm{keV}\left(1 / 2^{-}[530]\right) ; K^{\pi}=3 / 2^{+}$ at $253 \mathrm{keV}\left(3 / 2^{+}[651]\right) ; K^{\pi}=3 / 2^{-}$at $618 \mathrm{keV}\left(3 / 2^{-}[532]\right) ; K^{\pi}=5 / 2^{-}$at $644 \mathrm{keV}\left(5 / 2^{-}[523]\right)$. This calculation does not include any Coriolis mixing between orbitals coming from the same shell, needed to explain the low energy structure observed in ${ }^{231} \mathrm{Ac}$ and other nuclei of the same region, but it gives an idea of the ordering of the bands. The excitation energy systematics of some of these bands in the neighbourhood of ${ }^{231} \mathrm{Ac}$ are shown in Fig. 6. The band assignments for ${ }^{231} \mathrm{Ac}$ obtained in the reaction work [9] are also displayed. Although the knowledge on the excited structure of the isotones of Ac and Pa in this region is reduced with little overlap, the comparison indicates that the systematics of excitation energy for the $1 / 2^{+}[400]$ band observed in [39]
can be extended to the $3 / 2^{+}$[402] band. Furthermore, a parallel behaviour of the excitation energy of the $5 / 2^{+}[642]$ and $5 / 2^{-}[523]$ bands is observed for the isotopes of Ac and their isotones in Pa .

In the following the states established up to 550 keV excitation energy are discussed. The more speculative level assignments are described at the end of the section.

The ground state level. The lowest level observed in the experiment is assumed to be the ground state. It is fed by low energy transitions such as the observed $\gamma$ lines of 18.44 and 37.8 keV and several transitions of high energy and intensity that have not been observed in coincidences, such as the 372.30, 498.20 and $513.00 \mathrm{keV} \gamma$ lines. As discussed above, both theoretical predictions and experimental findings agree in the assignment of $\mathrm{I}^{\pi}=1 / 2^{+}$for the ground state. In the $(\mathrm{t}, \alpha)$ reaction the most populated level is the $1 / 2$ member of the $1 / 2[400]$ band which appears at zero energy [9]. But as indicated by the authors, the high density of levels in this mass region leads to a situation, where some peaks in the ( $\mathrm{t}, \alpha$ ) spectra are unresolved multiplets, making the interpretation more difficult. In fact the energy resolution in the ( $\mathrm{t}, \alpha$ ) work [ 9 was around 18 keV and in our study several excited states have been identified within this energy interval. Although the high density of low-lying states in ${ }^{231} \mathrm{Ac}$ does not allow to be conclusive about the assignment of the $1 / 2[400]$ band head as ground state, there is extra supporting evidence from the value of $\log f t=5.6$, of the $\beta$ transition from the ${ }^{231} \mathrm{Ac}$ ground state to the 555 keV level in ${ }^{231} \mathrm{Th}$. This low $\log f t$ value can be explained, if we assume that the ${ }^{231} \mathrm{Ac}$ ground state is the $1 / 2^{+} 1 / 2[400]$ level decaying to the $1 / 2^{-} 1 / 2[501]$ state as argued in [40] for the case of ${ }^{227}$ Fr decay. The $1 / 2$ [400] Nilsson configuration originates from the $\mathrm{s}_{1 / 2}$ proton orbit and the $1 / 2[501]$ comes from the $\mathrm{p}_{1 / 2}$ neutron orbit. This very favorable $\beta$ transition has been observed in several $\beta$ decays beyond ${ }^{208} \mathrm{~Pb}$. The excitation energy systematics of the $1 / 2[400]$ band is discussed in 39 for isotopes of $\mathrm{Fr}, \mathrm{Ac}, \mathrm{Pa}$ and Np . These independent facts give us confidence in the assignment of the $1 / 2^{+}[400]$ band head as the ground state of ${ }^{231} \mathrm{Ac}$.

The level at 5.6(4) keV is established by coincidences. The parity is determined to be positive by the $232.71 \mathrm{keV} \mathrm{E} 2(+\mathrm{M} 1)$ transition that de-excites the $3 / 2^{+}$ 238.01 keV state and corroborated by the rest of the transitions feeding the level.

The level at 18.35(15) keV is established by coincidences. The parity is assigned to be negative due to the tentative E1 character of the 219.69 keV transition connecting the level to the $3 / 2^{+} 238.01 \mathrm{keV}$ state. We have identified the $18.44 \mathrm{keV} \gamma$ transition connecting this level to the ground state. Its multipolarity should be of E1 type, otherwise an unexpected extremely high $\beta$ feeding to this level needs to be considered. Thus this state is a candidate
for the band head of the $1 / 2[530]$ band. The $3 / 2^{-}$state of this band is the ground state of the isotone, ${ }^{233} \mathrm{~Pa}$.

The level at $37.95(15) \mathrm{keV}$ is fed by several $\gamma$ transitions and de-excited by the 19.64 and 37.8 keV transitions. The latter has only been observed in coincidence with the $77.17+77.97 \mathrm{keV}$ doublet, connected through the 44.6 keV M1 transition. In fact the intensity of the 37.8 keV transition given in Table 1 has been extracted from the comparison with the intensity of the 44.6 keV transition observed simultaneously in the coincidence spectrum. The 38 keV level was identified by Thompson et al. [9] as a doublet due to the width of the observed peak (energy resolution $\simeq 18 \mathrm{keV}$ ) and the comparison of the experimental and the calculated ${ }^{232} \mathrm{Th}(\mathrm{t}, \alpha){ }^{231} \mathrm{Ac}$ differential cross section for the different excited states. To explain the high value of the experimental differential cross section the contribution of the $I=3 / 2$ member of the $1 / 2[530]$ band was assumed to be very close in energy. In this work we have no indications of the double character of the 38 keV state, as the 37.8 keV transition has only been observed in coincidences with the $77.17+77.97 \mathrm{keV}$ doublet. Furthermore we have not succeeded to place another level nearby without great rearrangement of the level scheme. The mixing of M1/E2 character of the 37.8 $\mathrm{keV} \gamma$ line can balance the in-out $\gamma$ intensity $\left(\alpha_{T}=900(80)\right.$ ).

The 61.73(20) keV level is fed by very intense $\gamma$ transitions such as the 54.29, $205.00,394.90,409.89$ and 469.23 keV transitions, and de-excited by the highly converted 56.50 keV transition to the 5.6 keV state. Notice that the 56.50 keV line has been observed in coincidence with the 54.29 keV line both in $\gamma-\gamma$ and $\gamma-\mathrm{e}^{-}$coincidences, see Fig. 2, allowing to deduce the conversion coefficient for the 56.50 keV transition given in Table 2. The parity of this level is defined by the 54.29 E 1 transition connecting it to the negative parity state at 116.02 keV excitation energy. As we will discuss later, we favour for this level a spinparity assignment of $\mathrm{I}^{\pi}=3 / 2^{+}$. One should notice that the band head of the $3 / 2[651]$ band is assumed to be the ground state of the two-neutronless Ac isotope, ${ }^{229} \mathrm{Ac}$ [9.39], and is located at 86.48 keV in the isotone ${ }^{233} \mathrm{~Pa}$ (see Fig. (6).

The 68.57(20) keV level is fed by more than ten transitions of E1 and M1 multipolarity. The de-excitation occurs via the $63.23 \mathrm{keV} \gamma$ line to the 5.6 keV state. A positive parity for this level is proposed based on the 198.18 keV E1 transition de-exciting the negative parity state at $266.76(10) \mathrm{keV}$. The $5 / 2^{+}$ state of the $3 / 2^{+}[651]$ is located 5 keV above the band head in the ${ }^{229} \mathrm{Ac}$ isotope and 8.2 keV in the isotone ${ }^{233} \mathrm{~Pa}$. This leads to tentatively assign this level as the $5 / 2^{+}$member of the $3 / 2^{+}[651]$ band in ${ }^{231} \mathrm{Ac}$.

The 74.75 (20) keV level is fed by several transitions of 41.27, 192.00, (381.76), 456.19 and 1040.2 keV and de-excites by the 36.74 keV transition to the $3 / 2^{+}$ 37.95 keV state. To fulfill the intensity balance a M1 multipolarity is needed
for this transition fixing a positive parity for the level. Thompson and coworkers [9] identified a level at 76(5) keV as the $9 / 2$ member of the $3 / 2[651$ ] band. Due to the M1 transition to the $3 / 2^{+} 37.95 \mathrm{keV}$ state and the M1 character of the one coming from the $5 / 2^{+} 531.00 \mathrm{keV}$ state $3 / 2$ or $5 / 2$ spin values for this state are more plausible.

The 116.02 (20) keV level. This is a well established level populated by many transitions. Its position is fixed by the coincidence between the 77.97 and 37.8 keV lines. Taking into account the E1 character of the 77.97 keV transition feeding the $38 \mathrm{keV} \mathrm{3/2+}$ state, the 116.02 keV state is given a negative parity. There are two strong E1 transitions connecting this level to the $3 / 2^{+}$at 38 keV level and the tentatively assigned $3 / 2^{+}$state at 61.73 keV , so we assume this level to be $1 / 2^{-}, 3 / 2^{-}$or $5 / 2^{-}$. The intensity of the eleven transitions feeding the state is balanced nicely by the four lines de-exciting it, so no beta feeding is obtained, consistent with the spin-parity assignment of the level. No equivalent level could be identified in the previous reaction work 9]. A long half-life of $14.3(11) \mathrm{ns}$ has been determined for this level by the slope method, see section 3.3. Similar half-life values for an excited state have been measured in this region for the $3 / 2^{+} 27.37 \mathrm{keV}$ state $(38.3(3) \mathrm{ns})$ in the isotope ${ }^{227} \mathrm{Ac}$ [41], $5 / 2^{+} 84.21 \mathrm{keV}$ state (45.1(13) ns) in the isobar ${ }^{231} \mathrm{~Pa}$ [41] and 36.5(4) ns [33] for the $5 / 2^{+} 86.47 \mathrm{keV}$ state in the isotone ${ }^{233} \mathrm{~Pa}$. The $\mathrm{B}(\mathrm{E} 1)$ value for the 27.37 keV transition in ${ }^{227} \mathrm{Ac}$ connecting the $3 / 2^{+} 3 / 2[651] \rightarrow 3 / 2^{-} 3 / 2[532]$ states is similar [41] to the one obtained for the $54.29 \mathrm{keV} \gamma$ transition in this study, supporting the assignment of this state as the $3 / 2^{-} 3 / 2[532]$ band head. This band was not observed in the work of Thompson et al. 9].

The 160.73 (15) keV level is populated by the 77.17, (106.48), 254.57, 288.94, $295.74,325.12$ and $434.50 \mathrm{keV} \gamma$ transitions and de-excited by the 44.6 M 1 transition to the 116.02 keV state. Due to the M1 character of the 44.6 keV transition we assign this level as the 5/2- member of the $3 / 2[532]$ band based on the 116.02 keV state. The half-life of the state, see section 3.3 , has been determined to be less than 900 ps.

The 238.01(15) keV level. The position of the level is fixed by the coincidence between the 121.96 keV and the 77.97 and 54.29 keV E1 transitions. The most intense transitions de-exciting the state have been observed in coincidence with the 177.39 and $247.65 \mathrm{keV} \gamma$ lines placed above. We assume that the level observed with high cross section in the ( $\mathrm{t}, \alpha$ ) reaction work 9 at 235(4) keV corresponds to this level observed in the $\beta$ decay of ${ }^{231} \mathrm{Ra}$. The measured half-life of the 238.01 keV state is of $57(11) \mathrm{ps}$. No half-life of this order has been measured in other actinium isotopes. Equivalent values of half-lives have been measured in the two-proton two-neutron neighbour ${ }^{227} \mathrm{Fr}$ for the 147 and 166 keV states identified as the $3 / 2^{+}$and $5 / 2^{+}$members of the $3 / 2[402]$ band [11]. Therefore we identify the 238.01 keV level as the $3 / 2^{+}$member of the $3 / 2$ [402] band (see Fig. 6). This level has been observed in ${ }^{233} \mathrm{~Pa}$ at 454.4 keV
and at 336 keV in ${ }^{229} \mathrm{Ac}$. This is the lowest state for which an appreciable beta feeding is found from the in-out intensity balance.

The 266.76(10) keV level. The negative parity of this level is defined by the E1 character of the 205.00 and 198.18 keV transitions to the $61.73(20)$ and $68.57(20) \mathrm{keV}$ states of positive parity. The decay pattern is very similar to the one of the 116.02 keV state. The half-life of the level is $90(20) \mathrm{ps}$, see Fig. 4 and section 3.3. Possible spin values for the level are $3 / 2^{-}$and $5 / 2^{-}$. Due to the identification of a $\gamma$ transition to the ground state a spin value of $3 / 2^{-}$is more favourable. The beta feeding to this level is smaller than the error bar, so no value is given in Table 3.

The 415.31(15) keV level. The position and parity of the level are assured by the coincidence between the 177.39 and the 232.71 keV transitions, the 254.57 M 1 transition with the 44.6 and 54.29 keV transitions, and the 299.10 M1 transition with the 77.97 and 54.29 keV E1 transitions. The 116.02 and 160.73 keV states are of negative parity and are connected by M1 transitions of 299.10 and 254.57 keV to the 415.31 keV level. Therefore the latter should also be of negative parity and spin value of either $3 / 2$ or $5 / 2$. This level has a beta feeding of $5(2) \%$, giving a logft of 6.7 (see Table 3). There is a level identified in the reaction work [9] at $420(6) \mathrm{keV}$, but no band assignment was given to this state.

The $471.60(15) \mathrm{keV}$ level. This level is determined by the coincidence of the 204.79 keV M1 transition with the $205.00 \mathrm{keV} \gamma$ line and other transitions deexciting the negative parity 266.76 keV state. The negative parity assignment is compatible with the non-observation of conversion electrons of the relatively intense 403.03 keV transition that connects this level to the 68.73 keV level of positive parity. The very intense $\mathrm{E} 1 \gamma$ line of 409.89 keV has been assigned by an energy match to connect this state with the 61.73 keV state. The half-life of this level has been measured to be less than 54 ps . A strong $\beta$ feeding of $27(10) \%$ with $\log f t=5.9$ is obtained for this level. This strong $\beta$ transition should most probably connect the ${ }^{231}$ Ra ground state $\left(5 / 2^{+}[622]\right)$ with a state of the same K. Strong beta feeding up to $90 \%$ to levels of opposite parity but with the same K is rather common in this region, see [15] for a systematics of $\beta$ transitions between the $1 / 2^{+}[400] \longrightarrow 1 / 2^{-}[501]$ band heads. The compilation of $\log f t$ values 42 in the actinide region $(Z>82)$ lists two first-forbidden transitions with $\Delta \mathrm{I}=0$ and $\Delta \pi=$ yes of the type $5 / 2^{+} \rightarrow 5 / 2^{-}$with $\log f t$ value $\leq 6$. Thus we favour an assignment of $5 / 2^{-}$for this state. This level could be the band head of the $5 / 2[523]$ band observed in other isotopes of Ac, at 120.80 keV in ${ }^{225} \mathrm{Ac}$ and at 273.14 keV in ${ }^{227} \mathrm{Ac}$, see Fig. 6. In our case the state is placed much higher in excitation energy, but in our HF+Skyrme calculations the single particle state corresponding to the $5 / 2^{-}$[523] configuration moves from 219 keV for $\beta_{2}=0.17$ (with this deformation the ground state is $1 / 2^{-}$) to 597 keV for the case of $\beta_{2}=0.22$ and $1 / 2^{+}[400]$ as ground state. In the
reaction work [9] there is a level identified at $469(10) \mathrm{keV}$ with no tentative band assignment given. Furthermore in our case we have identified three levels close to this excitation energy at $471.60,473.40$ and 478.30 keV .

The $485.70(15) \mathrm{keV}$ level de-excites mainly by the following transitions: the 369.52 keV transition in coincidence with the 54.29 and the 77.97 keV E1 transitions that de-excite the negative parity $116.02(20) \mathrm{keV}$ state, the 247.65 keV M1 transition in strong coincidence with the transitions de-exciting the $238.01 \mathrm{keV} \mathrm{3/2+}$ state and the 467.39 keV transition connecting the state to the $3 / 2^{+} 37.95 \mathrm{keV}$ state of positive parity. Thus we assign the parity of the 485.70 keV state as positive. Due to the M1 multipolarity of the transition to the 238.01 keV state possible spin-parity for this level are: $1 / 2^{+}, 3 / 2^{+}$or $5 / 2^{+}$. The $\log f t$ value of 6.7 excludes the possibility of a spin value of $1 / 2^{+}$.

The 513.10(15) keV level is determined by an energy match by the link of the 513.00 keV M1 transition to the ground state and of the 494.57 keV transition to the 18.35 keV state. A considerable $\beta$ feeding is found for this level, see Table 3, suggesting $\Delta \mathrm{K}=0, \pm 1$. The M1 transition to the ground state suggests $\mathrm{I}^{\pi}=1 / 2^{+}$or $3 / 2^{+}$. The relative strong beta feeding excludes the possibility of a spin value of $1 / 2^{+}$favouring $3 / 2^{+}$for this state.

The 531.00(15) keV level is determined by an energy match by the connection of three of the most intense M1 transitions at $469.23,462.38$ and 456.19 keV to the low energy levels at $61.73,68.57$ and 74.75 keV , respectively. The parity of the level is defined positive and the most probable values for the spin are $3 / 2$ or $5 / 2$. Considering the assignment of the parent ${ }^{231}$ Ra ground state as the $5 / 2^{+}[622]$ and the strong beta feeding observed to this level (see Table 3) we assume the 531.00 keV level to be the $5 / 2$ member of the $5 / 2[642$ ] band.

## Other levels

A level at 94(3) keV was identified in the reaction work [9]. It was assumed to be the $7 / 2$ member of the $1 / 2[530]$ band. In our work we had identified a transition at 96.01 keV . If this transition is the one de-exciting the proposed level, the spin of the state cannot be so high. There is a weak $\gamma$ line of 141.88 keV that could feed this state from the 238.01 keV level and explain the coincidences between the 96.01 and 247.65 keV transitions. Energetically a transition from the 266.76 keV state could be also identified. We tentatively include this state in the level scheme but not in the band assignment shown in Fig 7, as no M1 nor E2 transitions connecting the 96 keV level to the 18.35 keV state $\left(\mathrm{E}_{\gamma}=77.65 \mathrm{keV}\right)$ have been identified. One should note that there is an intense transition of 77.97 keV but of E 1 character.
The 245.78(20) keV level is established by coincidences. Two transitions in cascade of 21.0 and 129.76 keV connect the 116.02 and 266.76 keV levels of negative parity. From the coincidence studies we could not decide the ordering, so the level could be placed either at 137.00 or at 245.78 keV excitation
energy. The M1+E2 character of the 129.76 keV transition gives negative parity to this new level. The reaction studies [9] propose a level at $135(3) \mathrm{keV}$ as the $13 / 2$ member of the $3 / 2[651$ ] band. To avoid strong $\beta$ feeding to a level originally assigned as a high spin state, we chose the placement of this state at 245.78 keV . This placement is more consistent with the absence of $\gamma$ transitions to lower positive parity states. It is difficult to understand how a $13 / 2$ state could be populated from a $5 / 2^{+}$state in $\beta$ decay as some $\beta$ feeding is assigned to this intermediate level.
The 372.30(10) keV level has been tentatively placed in the level scheme connecting the 372.27 keV E1 transition to the ground state and the 256.79 keV weak transition to the 116.02 state. Therefore this level would be of negative parity. No level at this energy has been observed in the ${ }^{232} \mathrm{Th}(\mathrm{t}, \alpha)$ reaction work [9]. Plausible spin assignments for this state are $1 / 2^{-}$or $3 / 2^{-}$and due to the measured $\beta$ feeding we favour $3 / 2^{-}$.
Other levels placed at $449.53,478.30$ and 498.20 keV excitation energies have been established to account for strong $\gamma$ transitions for which no coincidences have been found. In all cases several other weaker transitions could be placed to strengthen the assignment. For higher excited states the parity could not be determined.

A summary of the properties of the levels in ${ }^{231} \mathrm{Ac}$ is given in Table 3. For each level tentative spin and parity assignments as well as beta feeding, $\log f t$ values and half-lives are listed. Due to the density of low lying states and the absence of multipolarity determination for the low energy transitions, the beta feeding and $\log f t$ values in Table 3 should be taken with caution.

## 5 Discussion

Möller et al. [43] have tabulated the atomic mass excesses and nuclear ground state deformation for most of the known nuclei. The calculated $\mathrm{Q}_{\beta}$ for ${ }^{231} \mathrm{Ra}$ is 2.56 MeV in reasonable agreement with the experimental value, $2.30(10)$ MeV . They predicted for the parent ${ }^{231} \mathrm{Ra}$ and the daughter ${ }^{231} \mathrm{Ac}$ the same quadrupole deformation, $\beta_{2}=0.207$, and no octupole deformation for any of them. Nevertheless moderately fast $\mathrm{B}(\mathrm{E} 1)$ rates connecting the lowest-lying $\mathrm{K}^{\pi}=5 / 2^{ \pm}$and $\mathrm{K}^{\pi}=1 / 2^{ \pm}$bands were found in ${ }^{231}$ Ra revealing the persistence of octupole collective effects [15]. Therefore it is interesting to investigate if some octupole collectivity is present in ${ }^{231} \mathrm{Ac}$.

### 5.1 Rotational bands

The spin of the parent, ${ }^{231} \mathrm{Ra}$, is assigned to be $5 / 2^{+}$in ref. [15] and identified as the $5 / 2^{+}[622]$ Nilsson level, with quadrupole and hexadecapole parameters $\beta_{2}=0.17$ and $\beta_{4}=0.06$. The characterization of the ${ }_{89}^{231} \mathrm{Ac}_{142}$ ground state as the $1 / 2^{+}$member of the $1 / 2[400]$ band was done in $(\mathrm{t}, \alpha)$ reaction studies [9] and corroborated by the low $\log f t$ value of the $\beta$ transition to the $1 / 2[501]$ band head in the daughter, ${ }^{231} \mathrm{Th}$ [41]. In the $(\mathrm{t}, \alpha)$ reaction work the structure of the heavy Pa and Ac isotopes were studied by the $\mathrm{U}(\mathrm{t}, \alpha)^{233,235,237} \mathrm{~Pa}$ and $\operatorname{Th}(\mathrm{t}, \alpha)^{229,231} \mathrm{Ac}$ reactions. The comparison of Figs. 1 and 2 of their work indicates that the level structure and mainly the ground states of the closest isotone, ${ }_{91}^{233} \mathrm{~Pa}_{142}$, and isotope ${ }_{89}^{229} \mathrm{Ac}_{140}$ are different from the one of ${ }_{89}^{231} \mathrm{Ac}_{142}$. We could have more similarities with the two-protonless isotone ${ }^{229} \mathrm{Fr}$, but no information is available for this nucleus. The two-proton-two-neutronless neighbour, the ${ }_{87}^{227} \mathrm{Fr}_{140}$ nucleus, has been studied by $\beta$ decay [11] and the spins and parities of the parent and the daughter are the same as in the case under study.

The band structure of ${ }^{229} \mathrm{Ac}$ has been described fairly well both considering quadrupole deformation plus Coriolis coupling as done in the reaction work [9] or small octupole deformation [10]. The agreement was better when the octupole deformation term was included. The lowest states were assumed to be part of the $\mathrm{K}=3 / 2^{ \pm}$and the $\mathrm{K}=1 / 2^{ \pm}$parity doublet bands. A second $\mathrm{K}=$ $3 / 2^{ \pm}$parity partners band is identified between the $\mathrm{K}=3 / 2^{+}$at 336 keV and a second $\mathrm{K}=3 / 2^{-}$which $3 / 2^{-}$band head was calculated to lie at 366 keV [45]. The band structure of the isotone, ${ }^{233} \mathrm{~Pa}$, is explained considering quadrupole and Coriolis coupling exclusively.

The ground state and the observed 38 keV state are assigned as the $1 / 2^{+}$ and $3 / 2^{+}$members of the $1 / 2^{+}[400]$ band based in the findings of the reaction work [9]. Assuming that the moment of inertia parameter $\hbar^{2} / 2 \Im$ has a value around $4-6 \mathrm{keV}$ typical of this region, we expect the $5 / 2^{+}$member to be below the $3 / 2^{+}$, between $15-34 \mathrm{keV}$ excitation energy according to the relationship 44]

$$
\begin{equation*}
E_{I, \text { rot }}=\varepsilon_{0}+\left(\frac{\hbar^{2}}{2 \Im}\right)\left[I(I+1)+\delta_{K, \frac{1}{2}}(-1)^{I+\frac{1}{2}}\left(I+\frac{1}{2}\right) a\right] \tag{1}
\end{equation*}
$$

This is the case for the distribution of the excited states of the $1 / 2^{+}[400]$ band in the neighbours $\mathrm{N}=140{ }^{227} \mathrm{Fr}$ and ${ }^{231} \mathrm{~Pa}$. We have a level at 5.6 keV that could fulfill the requirements, but a E2 transition connecting this state to the ground state will exhaust the beta strength. We are more tented to consider this level as belonging to the $1 / 2[660]$ band, due to the strong Coriolis coupling of this band with the $3 / 2[651]$ band that could push the former down. In fact
the intrinsic ground state of ${ }^{231} \mathrm{Ac}$ is considered in [45] as a mixture of $1 / 2[400]$ and $1 / 2[660]$ bands.

The next candidates are the $74.75(68.57) \mathrm{keV}$ states, where the zeroth-order position of the band head $\left(\varepsilon_{0}\right)$, the moment of inertia parameter $\hbar^{2} / 2 \Im$ and the decoupling parameter $a$ are calculated to be $4.84(3.76) \mathrm{keV}$, 10.01(9.39) keV and $0.2667(0.3502)$ respectively. The excitation energy for the $\frac{7}{2}^{+}$state is then calculated to be at $173.2(164.87) \mathrm{keV}$. The deep inelastic 1 p-transfer ${ }^{232} \mathrm{Th}+{ }^{136} \mathrm{Xe}$ reaction work mentioned in the previous section 32 provides two extra bands tentatively assigned to ${ }^{231} \mathrm{Ac}$. The first transition of 163.3 keV was assumed in the compilation [41] to connect a state at this energy to the $1 / 2^{+}$ ground state and therefore $\mathrm{J}^{\pi}=5 / 2^{+}$was inferred for this level. In our work none of the proposed gamma rays have been observed, but from this simple calculation it sounds plausible to place the observed $163 \mathrm{keV} \gamma$ transition on top of the 38 keV state, placing the $7 / 2^{+}$member of the $1 / 2[400]$ band at 201 keV excitation energy. This is compatible with the results in [32] as their setup was not sensitive to low-energy gamma rays such as the 38 keV transition.

The 61.73 keV state is assigned as the band head of the $3 / 2[651]$ band based on systematics. The $3 / 2^{+}$state of this band is found at 40.09 keV in ${ }^{225} \mathrm{Ac}$, at 27.37 keV in ${ }^{227} \mathrm{Ac}$, is the ground state of ${ }^{229} \mathrm{Ac}$ [9]39], and is located at 94.66 keV in the isotone ${ }^{233} \mathrm{~Pa}$. The first excited member of this band is located 5 keV above the band head in ${ }^{229} \mathrm{Ac}$ and 8 keV above in the isotone ${ }^{233} \mathrm{~Pa}$. So we favour the assignment of the 68.57 keV state as the first excited state of the band although the 74.75 keV state cannot be completely excluded. The $9 / 2$ and $13 / 2$ members of this band were assigned in [9] as the states at $76(5)$ and $135(3) \mathrm{keV}$ excitation energy, respectively. As already discussed, if the 76(5) keV state corresponds to the 74.75 keV state determined in this work, it is very unlikely that the spin of the state is so high. Assuming that the 61.73 and the 68.57 keV states are the $3 / 2^{+}$and $5 / 2^{+}$members of the band the $13 / 2$ member is expected at 125 keV consistent with the findings of the reaction work [9].

We assume that the level placed at $238.01(15) \mathrm{keV}$ is the $235(4) \mathrm{keV}$ state identified in the $(\mathrm{t}, \alpha)$ reaction work [9] and assigned as the band head of the $3 / 2[402]$ band. The excitation energy of this band has a behaviour with respect to the neutron number similar to the one of the $1 / 2[400]$ band that becomes the ground state in ${ }^{231} \mathrm{Ac}$ (see Fig. (6).

The assignment of the 266.76 keV state is rather complicated. It is connected by very intense E1 transitions to the 61.73 and 68.67 keV states assumed to be the band head and the $5 / 2^{+}$members of the $3 / 2[651]$ band and with reasonable intensity to the 74.75 and the 37.95 keV states of the $1 / 2[400]$ band. The $\mathrm{B}(\mathrm{E} 1)$ values of the first two transitions are a factor of 5 faster. So we favour the assignment of this state as a member of a $K=3 / 2^{-}$band, see

Fig. 7. Similarly a $\mathrm{K}^{\pi}=3 / 2^{-}$band was assigned in the two-protonless two neutronless ${ }^{227} \mathrm{Fr}$ at 224.23 keV .

The 471.60 keV state is of negative parity due to the M1 transition to the 266.8 keV state. The strong $\beta$ feeding with $\log f t=5.9$ favours a first forbidden transition of the type $5 / 2^{+} \rightarrow 5 / 2^{-}$. For more details see discussion in the previous section. Tentatively we assign this state as the band head of the $5 / 2[523]$ band. This band constituted the ground state of ${ }^{223} \mathrm{Ac}$ and it has been identified in ${ }^{225} \mathrm{Ac}$ at 120.8 keV and at 273.14 keV in ${ }^{227} \mathrm{Ac}$. The systematics shows a strong increase of the excitation energy with the neutron number in both Ac and Pa compatible with our placement at 471.60 keV for ${ }^{231} \mathrm{Ac}$, see Fig. 6,

Similarly strong $\beta$ feeding is found for the 531.00 keV state assigned as the band head of the $5 / 2[642]$ band. This band is located at 64 keV in ${ }^{223} \mathrm{Ac}$ as the parity doublet of the ground state band and it is also observed in ${ }^{225} \mathrm{Ac}$ and ${ }^{227} \mathrm{Ac}$. It is found in all Ac isotopes at $30-60 \mathrm{keV}$ higher excitation energy than the $5 / 2[523]$ band, in good agreement with the findings for ${ }^{231} \mathrm{Ac}$.

A summary of the tentative band assignments as discussed above is given in Fig. 7 ,

### 5.2 Reduced transition probabilities

The decay scheme shown in Figs. 5-a, 5-b and 5-c has the striking feature that several states at $116.02,266.76$ and 471.60 keV of negative parity are connected through the most intense E1 $\gamma$ lines to the positive parity states at 61.73, 68.57 and 74.75 keV . In this work we have directly measured the lifetimes of these levels and deduced the $\mathrm{B}(\mathrm{E} 1)$ values for the de-exciting transitions. The experimental $B(E 1)$ values together with their values in Weisskopf units are listed in Table 4. The $\mathrm{B}(\mathrm{E} 1)$ transition rates range from $5 \times 10^{-6}$ to $2 \times 10^{-3}$ $e^{2} \mathrm{fm}^{2}$.

The presence of octupole phonon components enhances the E1 rates between members of parity partner bands. Typical B(E1) values for enhanced E1 transition between $K=3 / 2^{ \pm}$member are, in this region, around $10^{-4} \mathrm{e}^{2} \mathrm{fm}^{2}$, whereas $B(E 1)$ values for nuclei from a region without octupole collectivity are much slower below $10^{-5} \mathrm{e}^{2} \mathrm{fm}^{2}$, see [14]16]. Strong mixing between bands is indicated by the fact that no clear differences appear between $B(E 1)$ values for transitions connecting the parity partner bands (intraband transitions) with those connecting opposite parity bands with different K (interband transitions). This effect has already been observed in ${ }^{229} \mathrm{Th}$ [14].

In this work enhanced $\mathrm{B}(\mathrm{E} 1)$ rates in ${ }^{231} \mathrm{Ac}$ are found for the 77.17 and the
121.96 keV transitions de-exciting the 238.01 keV state, with $\mathrm{B}(\mathrm{E} 1)$ values of $4.4(12) \times 10^{-4}$ and $2.1(5) \times 10^{-4} \mathrm{e}^{2} \mathrm{fm}^{2}$, respectively. These transitions connect the $3 / 2^{+}[402]$ band with the band head and the $5 / 2^{+}$member of the $3 / 2[532]$ band. The ratio of $B(E 1)$ values, 2.1(8), is in good agreement with the theoretical intensity ratio given by Alaga's rule [46] of 2.1(5), giving support to these assignments. Similarly, the E1 transitions connecting the $266.76(10) \mathrm{keV}$ $3 / 2^{-}$state with the $61.73 \mathrm{keV} \mathrm{3/2+}$ state and $68.57 \mathrm{keV} 5 / 2^{+}$are moderately fast with $B(E 1)$-values of $1.4(4) \times 10^{-4}$ and $1.4(3) \times 10^{-4} \mathrm{e}^{2} \mathrm{fm}^{2}$, respectively, almost one order of magnitude faster than the 228.73 keV E1 transition to the $3 / 2^{+}$state of the $1 / 2[400]$ band, confirming the presence of octupole phonon components.

To ease the comparison of E1 strength over a wide range of nuclei, we use the definition of the intrinsic dipole moment $D_{0}$, which removes the spin dependence of the $B(E 1)$ rates. Assuming a strong coupling limit and an axial shape of the nucleus, $D_{0}$ is defined for K different from $1 / 2$ via the rotational formula,

$$
\begin{equation*}
\left.B\left(E 1 ; I_{i} \longrightarrow I_{f}\right)=\frac{3}{4 \pi} D_{0}^{2}<I_{i} K_{i} 10 \right\rvert\, I_{f} K_{f}>^{2} \tag{2}
\end{equation*}
$$

One should stress that the $\left|D_{0}\right|$ moment is used in this case as a convenient parameter for inter-comparison, although this rotational formula may not be strictly applicable for an octupole transitional nucleus.

The $\left|D_{0}\right|$ values have been calculated for the $\mathrm{K}^{\pi}=3 / 2^{ \pm}$bands in ${ }^{231} \mathrm{Ac}$, for which experimental information exists. The values are compiled in Table 5 and compared to those obtained for the nearby nuclei ${ }^{227} \mathrm{Fr}$ and ${ }^{227} \mathrm{Ac}$. As stated before, the enhancement of the $B(E 1)$ transition for $K^{\pi}=3 / 2^{ \pm}$partner bands is larger in the region than for other partner bands. An average value of $\left|D_{0}\right|=0.044(4) \mathrm{e} \cdot \mathrm{fm}$ is obtained for the $3 / 2^{ \pm}$with band heads at 116 and 238 keV , and for the $3 / 2^{ \pm}$bands at 266.8 and 61.7 keV we get $\left|D_{0}\right|=0.035(3)$ $\mathrm{e} \cdot \mathrm{fm}$. These values are higher than those obtained for the lighter ${ }^{227} \mathrm{Ac}$ isotope and slightly lower than the value for the 2.0 and 267.0 keV partner bands in ${ }^{227} \mathrm{Fr}$. Note that $\left|D_{0}\right|$ values of $0.077(3) \mathrm{e} \cdot \mathrm{fm}$ (on average) were obtained in [14] for the E1 transitions connecting the $\mathrm{K}^{\pi}=3 / 2^{ \pm}$parity partner bands in ${ }^{229} \mathrm{Th}$ with band heads at 0.0035 and 164.5 keV .

The effect of the enhancement of the E1 transition rates in ${ }^{231} \mathrm{Ac}$ seems to be still perceptible and this may reveal the presence of weak octupole correlations in this transitional nucleus.

## 6 Summary

Our study has been focused on the properties of the low energy states in ${ }^{231} \mathrm{Ac}$ in a search for octupole correlations in this nucleus. The level scheme of ${ }^{231} \mathrm{Ac}$ has been determined from $\gamma$ and $\mathrm{e}^{-}$singles as well as $\gamma-\gamma$ and $\mathrm{e}^{-}-\gamma$ coincidences. More than $100 \gamma$ lines have been assigned to the decay scheme. The multipolarity of 28 transitions has been experimentally established. This has allowed to determine the parity of many levels. This study represents the first decay scheme obtained for ${ }^{231} \mathrm{Ra}$ and enriches the known levels in ${ }^{231} \mathrm{Ac}$. We have identified up to a total of 30 new levels and assigned possible spin and parities for 21 of them. The Advanced Time-Delayed $\beta \gamma \gamma(t)$ method was applied to measure lifetimes of several states in ${ }^{231} \mathrm{Ac}$. Some particularly fast E1 transitions have been observed indicating that the octupole effects although weak still persist in this nucleus.

## 7 Acknowledgements

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Table 1
Gamma transitions belonging to ${ }^{231}$ Ac. Tentative assignments are given in parenthesis. A tick in the $\mathrm{S} / \mathrm{L}$ column indicates that the intensity ratio between the short cycle ( 17 or 26 s ) and the corresponding long cycle ( 190 or 200 s ) for a given transition is consistent with the ${ }^{231}$ Ac half-life.


Table 1, cont.


Table 1, cont.

| $\mathrm{E}_{\gamma}(\mathrm{keV})$ | $\mathrm{T}_{1 / 2} \gamma-\gamma \mathrm{e}$ | $\mathrm{e}^{-}-\gamma$ S/L | $\mathrm{I}_{\gamma}$ |  | Coincidences | $\mathrm{E}_{i}(\mathrm{keV})$ | $\mathrm{E}_{f}(\mathrm{keV})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 254.57(10) | $\checkmark$ | $\sqrt{ } \sqrt{ }$ | 165(16) | 18.4(er) | ) 41.344 .547 .554 .3 | 415.31 | 160.73 |
|  |  |  |  |  | 78.096 .0 |  |  |
| 256.79(15) | $\sqrt{ } \sqrt{ }$ | $\checkmark$ | 22(3) |  |  |  |  |
| 260.82(10) | $\checkmark \sqrt{ }$ | $\sqrt{ } \sqrt{ }$ | 158(15) |  | 204.8 | 266.76 | 5.6 |
| 275.38(10) |  | $\checkmark$ | 16(6) |  |  | 1100.20 | 824.82 |
| 288.94(10) | $\sqrt{ }(\sqrt{ })$ | $\sqrt{ } \sqrt{ }$ | 30(4) |  |  | 449.53 | 160.73 |
| 295.74(15) | $\checkmark$ | $\checkmark$ | 19(5) |  |  | 456.56 | 160.73 |
| 299.10(15) | $\sqrt{ } \sqrt{ }$ | $\checkmark$ | 66(7) |  | 54.378 .0 | 415.31 | 116.02 |
| 313.50(10) |  | $\checkmark$ | 16(3) |  |  |  |  |
| 325.12(15) | $\sqrt{ } \sqrt{ }$ | $\checkmark$ | 25(3) |  |  | 485.70 | 160.73 |
| 355.66(20) | $\sqrt{ } \sqrt{ }$ | $\checkmark$ | 40(7) $\}$ |  | 54.378 .0 | 471.60 | 116.02 |
| 357.26(10) | $\sqrt{ } \sqrt{ }$ |  | 193(18) |  |  | 473.40 | 116.02 |
| 369.52(30) | $\checkmark$ | $\checkmark$ | $148(26){ }^{d}$ |  | 54.378 .0 | 485.70 | 116.02 |
| 372.27 (10) | $\sqrt{ } \sqrt{ }$ |  | $455(43)^{d}$ |  |  | 372.30 | 0.0 |
| (375.72(10) |  | $\checkmark$ | 68(9) |  |  | 849.00 | 473.40) |
| (381.16(30) |  | $\checkmark$ | 11(1) |  |  | 912.10 | 531.00) |
| (381.76(15) |  |  | 30(5) |  |  | 456.56 | 74.75) |
| (387.99(15) | $\checkmark$ |  | $45(12)^{f}$ |  |  | 456.56 | 68.57) |
| 394.90(15) | $\checkmark$ | $\checkmark$ | 127(13) |  |  | 456.56 | 61.73 |
| 396.92(15) | $\checkmark$ |  | $57(18)^{g}$ |  |  | 415.31 | 18.35 |
| 403.03(15) | $\checkmark$ | $\checkmark$ | 301(29) |  |  | 471.60 | 68.57 |
| 409.89(10) | $\checkmark \sqrt{ }$ | $\sqrt{ } \sqrt{ }$ | 1080(103) |  |  | 471.60 | 61.73 |
| (417.55(10) |  | $\checkmark$ | 14(2) |  |  | 485.70 | 68.57) |
| 425.02(10) | $\checkmark$ | $\checkmark$ | 23(5) |  |  | 670.80 | 245.78 |
| 429.62(15) | $\checkmark$ | $\checkmark$ | 110(14) |  |  | 498.20 | 68.57 |
| (432.00(30) |  | $\checkmark$ | 36(5) |  |  | 847.40 | 415.31) |
| 434.50(15) | $\checkmark$ | $\sqrt{ }$ | 143(13) |  |  | 595.15 | 160.73 |

Table 1, cont.

| $\mathrm{E}_{\gamma}(\mathrm{keV})$ | $\mathrm{T}_{1 / 2}$ | $\gamma-\gamma \mathrm{e}^{-}-\gamma$ | S/L | $\mathrm{L}_{\gamma}$ | Coincidences | $\mathrm{E}_{i}(\mathrm{keV})$ | $\mathrm{E}_{f}(\mathrm{keV})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 442.90(10) | $\checkmark$ |  |  | 43(6) |  | 680.80 | 238.01 |
| (444.32(10) | $(\sqrt{ })$ |  |  | 32(6) |  | 513.10 | 68.57) |
| 445.74(10) | $\checkmark$ |  |  | 48(6) |  | 931.57 | 485.70 |
| 456.19(15) | $\checkmark$ | $\sqrt{ }$ |  | 676(61) |  | 531.00 | 74.75 |
| 462.38(15) |  | $\sqrt{ }$ |  | 534(48) |  | 531.00 | 68.57 |
| 467.39(15) | $\sqrt{ }$ | $\sqrt{ }$ |  | 136(20) |  | 485.70 | 18.35 |
| 469.23(15) | $\checkmark$ | $\checkmark$ |  | 909(85) |  | 531.00 | 61.73 |
| (473.40(30) |  |  |  | 28(6) |  | 473.40 | 0.0) |
| 475.29(15) | $\sqrt{ }$ | $\sqrt{ }$ |  | 23(31) |  | 513.10 | 37.95 |
| 478.15(15) | $\checkmark$ |  |  | $148(21)^{f}$ |  | 478.30 | 0.0 |
| (481.74(30) |  |  |  | 25(5) |  | 931.57 | 449.53) |
| 494.57(30) | $(\sqrt{ })$ |  |  | 28(6) |  | 513.10 | 18.35 |
| 498.20(15) | $\checkmark$ |  |  | 227(21) |  | 498.20 | 0.0 |
| 513.00(15) | $\checkmark$ | $\sqrt{ }$ |  | 659(86) ${ }^{\text {d }}$ |  | 513.10 | 0.0 |
| 569.4(5) |  |  |  | 51(7) |  | 1100.20 | 531.00 |
| (577.7(3) |  |  |  | 19(6) |  | 1248.40 | 670.80) |
| 586.8(6) | $\checkmark$ |  |  | 30(6) |  | 824.82 | 238.01 |
| 595.3(5) |  |  |  | $51(7)$ |  | 595.15 | 0.0 |
| 607.6(5) |  |  |  | 10(1) |  |  |  |
| (609.3(5) |  |  |  | 28(3) |  | 670.80 | 61.73) |
| (612.5(5) |  |  |  | 10(1) |  | 680.80 | 68.57) |
| (614.6(3) |  |  |  | 15(2) |  | 1100.20 | 485.70) |
| 662.0(3) |  |  |  | 52(5) |  | 680.80 | 18.35 |
| (666.3(4) |  |  |  | 17(3) |  | 1137.92 | 471.60) |

Table 1, cont.

| $\mathrm{E}_{\gamma}(\mathrm{keV})$ | $\mathrm{T}_{1 / 2}$ | $\gamma-\gamma \mathrm{e}^{-}-\gamma$ | S/L $\mathrm{I}_{\gamma}$ | Coincidences | $\mathrm{E}_{i}(\mathrm{keV})$ | $\mathrm{E}_{f}(\mathrm{keV})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 732.6(5) | $\sqrt{ }$ | $\checkmark$ | $\sqrt{ } 80(24)$ |  | 849.00 | 116.02 |
| 754.1(5) |  | $\checkmark$ | $\sqrt{ } 31(5)$ |  | 870.16 | 116.02 |
| 763.1(3) | $(\sqrt{ })$ |  | $\sqrt{ } 45(12)$ |  | 824.82 | 61.73 |
| 842.0(5) |  |  | $\checkmark \sqrt{18(6)}$ |  | 847.40 | 5.6 |
| 844.2(5) |  |  | $\sqrt{ } 18(3)$ |  |  |  |
| 849.1(5) |  |  | $\sqrt{ } 13(5)$ |  | 849.00 | 0.0 |
| 857.8(6) |  |  | $\sqrt{ }$ 35(6) |  |  |  |
| 868.4(6) |  |  | $\sqrt{ } 69(11)$ |  | 1354.20 | 485.70 |
| 871.1(6) |  | $\sqrt{ }$ | $\sqrt{ }$ 60(6) | (205.0) | 1137.92 | 266.76 |
| 912.1(6) | $\checkmark$ | $\sqrt{ }$ | $\sqrt{ } 150(26)$ |  | 912.10 | 0.0 |
| 937.7(5) |  |  | $\sqrt{ }$ 32(9) |  |  |  |
| 986.9(4) |  |  | $\sqrt{ }$ 31(9) |  |  |  |
| 1040.2(5) |  |  | $\sqrt{ }$ 72(7) |  | 1114.90 | 74.75 |
| (1046.2(5) |  |  | $\sqrt{ }$ 27(3) |  | 1114.90 | 68.57) |
| (1086.3(6) |  |  | $\sqrt{ }$ 24(3) |  | 1155.30 | 68.57) |
| (1150.1(4) |  |  | $\sqrt{ }$ 31(4) |  | 1155.30 | 5.6) |
| 1155.6(6) |  |  | $\sqrt{ } 40(12)$ |  | 1155.30 | 0.0 |
| (1248.3(5) |  |  | $\sqrt{ } \quad 7(2)$ |  | 1248.40 | 0.0) |
| (1354.4(9) |  |  | $\sqrt{ } 10(2)$ |  | 1354.20 | 0.0) |

$\dagger$ The absolute $\gamma$ intensity is obtained by multiplying by $7.58(19) \times 10^{-5}$ per decay $\left(\mathrm{I}_{\gamma}(54.29)=0.0758(19)\right.$ per decay $)$.
${ }^{a}$ Intensity seen in singles 22(5), but there is a tabulated 26.0 keV Th line of relative intensity $<0.006$ of the 282 keV Th $\gamma$ line [16] which has been subtracted.
${ }^{b}$ Seen only in a coincidence spectrum (namely with 78.0 keV ).
${ }^{c}$ Contribution from At X-ray subtracted.
${ }^{d}$ Contribution from Th subtracted.
${ }^{e}$ Contribution from Ac X-ray subtracted.
${ }^{f}$ Doublet. Contribution from Ra subtracted.
${ }^{g}$ Triplet with contribution of $\mathrm{Ra}(397.3 \mathrm{keV})$ and $\mathrm{Th}(396.9 \mathrm{keV})$. The intensity corresponding to these components is subtracted.
${ }^{h}$ The intensity of this $\gamma$ line is shared between the two assignments.
${ }^{i}$ It could be due to summing of the $54.29 \mathrm{keV} \gamma$ ray and the $87.66 \mathrm{keV} \mathrm{Ac} \mathrm{K}_{\alpha 2}$ X-ray.

Table 2
Experimental internal conversion coefficients for transitions in ${ }^{231} \mathrm{Ac}$. Theoretical values are taken from [28].

| $\begin{gathered} E_{\gamma} \\ (\mathrm{keV}) \end{gathered}$ | $\mathrm{I}_{\text {total }}$ | Initial <br> level <br> (keV) | Conversion <br> shell | Internal conversion coefficients |  |  |  | Adopted multipolarity |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | $\alpha_{\text {exp }}$ | $\alpha_{\text {theo }}$ |  |  |  |
|  |  |  |  |  | E1 | E2 | M1 |  |
| 44.6(1) | 1100(300) | 160.73 | $\mathrm{L} 1+\mathrm{L} 2$ | 24(6) | 0.467 | 192.2 | 27.30 | M1 |
| 54.29(5) | 1580(180) | 116.02 | L1+L2 | $\leq 0.11$ | 0.291 | 76.69 | 15.32 | E1 |
| 56.50(5) | 1200(200) | 61.73 | L1+L2 | $58(17)^{a}$ | 0.264 | 62.72 | 13.63 | E2(+M1) |
|  |  |  | $\Sigma \mathrm{M}$ | $31(9)^{a}$ | 0.096 | 31.38 | 3.292 |  |
|  |  |  | $\Sigma \mathrm{N}$ | $12(4)^{a}$ | 0.025 | 8.339 | 0.874 |  |
| 77.17(7) | 18(3) | 238.01 | $\mathrm{L} 1+\mathrm{L} 2$ | $\leq 0.15$ | 0.120 | 14.00 | 5.319 | E1 |
| 77.97(6) | 460(50) | 116.02 | $\mathrm{L} 1+\mathrm{L} 2$ | $\leq 0.15$ | 0.120 | 14.00 | 5.319 | E1 |
| 129.76(7) | 445(128) | 245.78 | $\mathrm{L} 1+\mathrm{L} 2$ | 1.31(40) ${ }^{\text {a }}$ | 0.034 | 1.426 | 1.218 | $\mathrm{M} 1+\mathrm{E} 2$ |
| 198.18(8) | 670(70) | 266.76 | K | 0.06(2) | 0.075 | 0.163 | 1.964 | E1 |
|  |  |  | $\mathrm{L} 1+\mathrm{L} 2$ | 0.07(5) | 0.012 | 0.242 | 0.366 |  |
| 204.79(10) | 1560(570) | 471.60 | K | $1.77(24)^{b}$ | 0.069 | 0.153 | 1.785 | M1 |
| 205.00(10) | 790(170) | 266.76 | K | $\leq 0.23{ }^{\text {c }}$ | 0.070 | 0.155 | 1.880 | E1 |
|  |  |  | $\mathrm{L} 1+\mathrm{L} 2$ | $\leq 0.12^{\text {c }}$ | 0.012 | 0.215 | 0.352 |  |
| 232.71(9) | 330(50) | 238.01 | K | 0.12(6) | 0.052 | 0.120 | 1.254 | E2(+M1) |
| 247.65(15) | 290(40) | 485.70 | K | 0.87(22) | 0.045 | 0.106 | 1.054 | M 1 (+E2) |
|  |  |  | $\mathrm{L} 1+\mathrm{L} 2$ | 0.31(14) | 0.007 | 0.101 | 0.196 |  |
| 254.57(10) | 365(60) | 415.31 | K | $1.07(26)$ | 0.042 | 0.100 | 0.977 | M1 |
|  |  |  | L1+L2 | 0.34(14) | 0.007 | 0.091 | 0.181 |  |
| 288.94(10) | 60(13) | 449.53 | K | $0.87(26)^{a}$ | 0.032 | 0.078 | 0.688 | M1 |
| 299.10(15) | 130(30) | 415.31 | K | 1.01(35) | 0.029 | 0.072 | 0.626 | M1 |
| 355.66(20) | 64(14) | 471.60 | K | 0.60 (20) | 0.020 | 0.051 | 0.385 | M1 |
| 357.26(10) | 310(50) | 473.40 | K | 0.60(20) | 0.020 | 0.051 | 0.385 | M1 |
| 372.27 (10) | 465(45) | 372.30 | K | 0.021(12) | 0.018 | 0.047 | 0.344 | E1 |
| 394.90(15) | 170(30) | 456.56 | K | $0.25(15)$ | 0.016 | 0.041 | 0.293 | M1 |
| 396.92(15) | $77(25)$ | 415.31 | K | 0.25(15) | 0.016 | 0.041 | 0.293 | M1 |

Table 2, cont.

| $\begin{gathered} E_{\gamma} \\ (\mathrm{keV}) \end{gathered}$ | $\mathrm{I}_{\text {total }}$ | Initial <br> level <br> (keV) | Conversion <br> shell | Internal conversion coefficients |  |  |  | Adopted multipolarity |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | $\alpha_{\text {exp }}$ | $\alpha_{\text {theo }}$ |  |  |  |
|  |  |  |  |  | E1 | E2 | M1 |  |
| 409.89(10) | 1100(100) | 471.60 | K | $<0.035$ | 0.015 | 0.038 | 0.265 | E1 |
| 434.50(15) | 180(25) | 595.15 | K | 0.28(9) | 0.013 | 0.034 | 0.227 | M1 |
| 456.19(15) | 840(90) | 531.00 | K | 0.28(6) | 0.012 | 0.031 | 0.199 | M1 |
|  |  |  | $\mathrm{L} 1+\mathrm{L} 2$ | 0.04(2) | 0.002 | 0.012 | 0.036 |  |
| 462.38(15) | 660(70) | 531.00 | K | 0.21(5) | 0.012 | 0.030 | 0.192 | M1 |
|  |  |  | L1+L2 | 0.06(3) | 0.002 | 0.012 | 0.035 |  |
| 469.23(15) | 1120(105) | 531.00 | K | 0.21(5) | 0.011 | 0.029 | 0.184 | M1 |
|  |  |  | L1+L2 | 0.04(2) | 0.002 | 0.011 | 0.034 |  |
| 475.29(15) | 395(40) | 513.10 | K | 0.21(6) | 0.011 | 0.029 | 0.178 | M1 |
| 478.15(15) | 180(25) | 478.30 | K | $0.15(6)$ | 0.011 | 0.028 | 0.175 | M1 |
| 498.20(15) | 275(33) | 498.20 | K | 0.17(7) | 0.010 | 0.026 | 0.157 | M1 |
| 513.00(15) | 780(100) | 513.10 | K | 0.14(4) | 0.009 | 0.025 | 0.145 | M1 |

${ }^{a}$ Conversion coefficient deduced from $\gamma-\mathrm{e}^{-}$and $\gamma-\gamma$ coincidences with $54.29 \mathrm{keV} \gamma$ line.
${ }^{b}$ Conversion coefficient deduced from $\gamma-\gamma$ coincidences.
${ }^{c}$ Values extracted subtracting the contribution of the calculated K and (L1+L2) electron conversion coefficients of the $204.79 \mathrm{keV} \gamma$ line of multipolarity M1.

Table 3
Beta feeding (normalized to 100 decays of ${ }^{231} \mathrm{Ra}$ ) and properties of the low spin levels in ${ }^{231} \mathrm{Ac}$

| Energy (keV) | $\mathrm{J}^{\pi}$ | $\mathrm{I}_{\beta}(\%)^{a}$ | $\log f t$ | $\mathrm{~T}_{1 / 2}$ |
| :---: | :---: | :---: | :---: | :---: |
| 0.0 | $\frac{1}{2}^{+}$ |  |  |  |
| $5.6(4)$ | $\frac{1}{2}^{+} ; \frac{3}{2}^{+} ; \frac{5}{2}^{+}$ |  |  |  |
| $18.35(15)$ | $\frac{3}{2}^{-}$ |  |  |  |
| $37.95(15)$ | $\frac{3}{2}^{+}$ |  |  |  |
| $61.73(20)$ | $\frac{3}{2}^{+}$ |  |  |  |
| $68.57(20)$ | $\frac{5}{2}^{+}$ |  |  |  |
| $74.75(20)$ | $\frac{3}{2}^{+} ; \frac{5}{2}^{+}$ |  |  |  |
| $96.10(20)$ | $\left.\frac{1}{2}^{-} ; \frac{3}{2}^{-}\right)$ |  |  |  |
| $116.02(20)$ | $\frac{3}{2}^{-}$ |  |  | $14.3(11) \mathrm{ns}$ |
| $160.73(15)$ | $\frac{5}{2}^{-}$ |  |  | $<900 \mathrm{ps}$ |
| $238.01(15)$ | $\frac{3}{2}^{+}$ | $1.2(7)$ | 7.5 | $57(11) \mathrm{ps}$ |
| $245.78(20)$ | ${\left(\frac{1}{2}^{-} ; \frac{3}{2}^{-} ; \frac{3}{2}^{-}\right.}^{-}$ |  |  |  |
| $266.76(10)$ | $\frac{3}{2}^{-}$ |  |  | $90(20) \mathrm{ps}$ |
| $372.30(10)$ | $\left.\frac{1}{2}^{-}\right) ; \frac{3}{2}^{-}$ | $4.2(14)$ |  |  |
| $415.31(15)$ | $\frac{3}{2}^{-} ; \frac{5}{2}^{-}$ | $5(2)$ | 6.7 |  |
| $449.53(30)$ | $\frac{3}{2}^{-} ;\left(\frac{5}{2}^{-}\right)$ |  |  |  |
| $456.56(15)$ | $\frac{3}{2}^{+} ; \frac{5}{2}^{+}$ | $2.5(8)$ | 6.9 |  |
| $471.60(15)$ | $\frac{5}{2}^{-}$ | $27(10)$ | 5.9 | $<54 \mathrm{ps}$ |
| $473.40(15)$ | $\frac{1}{2}^{-} ; \frac{3}{2}^{-}$ | $2.2(8)$ | 7.0 |  |
| $478.30(10)$ | $\frac{1}{2}^{+} ; \frac{3}{2}^{+}$ | $1.7(6)$ | 7.1 |  |
| $485.70(15)$ | $\frac{3}{2}^{+} ; \frac{5}{2}^{+}$ | $4.5(15)$ | 6.7 |  |
| $498.20(20)$ | $\frac{3}{2}^{+}$ | $3.9(13)$ | 6.7 |  |
| $513.10(15)$ | $\frac{3}{2}^{+}$ | $11(4)$ |  |  |
| $531.00(15)$ | $\frac{5}{2}^{+}$ | $24(8)$ | 5.9 |  |
| $595.15(20)$ | $\frac{3}{2}^{-}$ | $2.1(7)$ | 6.9 |  |
| $670.80(20)$ |  | $0.30(12)$ | 7.7 |  |
| $680.80(30)$ |  | $1.8(6)$ | 6.9 |  |

Table 3, cont.

| Energy (keV) | $\mathrm{J}^{\pi}$ | $\mathrm{I}_{\beta}(\%)^{a}$ | $\log f t$ | $\mathrm{~T}_{1 / 2}$ |
| :---: | :---: | :---: | :---: | :---: |
| $824.82(30)$ | $0.5(2)$ | 7.3 |  |  |
| $847.40(30)$ |  | $0.5(2)$ | 7.3 |  |
| $849.00(20)$ | $1.5(5)$ | 6.8 |  |  |
| $870.16(40)$ | $0.3(1)$ | 7.5 |  |  |
| $912.10(20)$ | $1.5(5)$ | 6.7 |  |  |
| $931.57(20)$ | $0.7(2)$ | 7.1 |  |  |
| $1100.20(30)$ | $0.8(3)$ | 6.8 |  |  |
| $1114.90(40)$ | $0.8(3)$ | 6.8 |  |  |
| $1137.92(40)$ | $0.7(2)$ | 6.8 |  |  |
| $1155.30(30)$ | $1.0(3)$ | 6.6 |  |  |
| $1248.40(50)$ | $0.24(9)$ | 7.1 |  |  |
| $1354.20(50)$ | $0.7(2)$ | 6.5 |  |  |

${ }^{a}$ The $\beta$ feeding is considered only when it is larger than the error bar.

Table 4
Experimental reduced transition probabilities in ${ }^{231} \mathrm{Ac}$.

| Level(keV) | $\mathrm{T}_{1 / 2}$ | $\mathrm{E}_{\gamma}(\mathrm{keV})$ | $\mathrm{X} \lambda$ | $\mathrm{B}(\mathrm{X} \lambda)$ | $\mathrm{B}(\mathrm{X} \lambda)$ (W.u.) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 116.02(20) | $14.3(11) \mathrm{ns}$ | 41.27 | $E 1^{a}$ | $1.8(4) \times 10^{-5} \mathrm{e}^{2} \mathrm{fm}^{2}$ | $7.4(16) \times 10^{-6}$ |
|  |  | 47.45 | $E 1^{a}$ | $4.6(8) \times 10^{-6} \mathrm{e}^{2} \mathrm{fm}^{2}$ | $1.9(3) \times 10^{-6}$ |
|  |  | 54.29 | E1 | $8.2(7) \times 10^{-5} \mathrm{e}^{2} \mathrm{fm}^{2}$ | $3.4(3) \times 10^{-5}$ |
|  |  | 77.97 | E1 | $1.05(15) \times 10^{-5} \mathrm{e}^{2} \mathrm{fm}^{2}$ | $4.3(6) \times 10^{-6}$ |
| 160.73(15) | <900 ps | 44.6 | M1 | $>1.5(5) \times 10^{-2} \mu_{N}^{2}$ | $>8(3) \times 10^{-3}$ |
| 238.01(15) | 57(11)ps | 77.17 | E1 | $4.4(12) \times 10^{-4} \mathrm{e}^{2} \mathrm{fm}^{2}$ | $1.8(5) \times 10^{-4}$ |
|  |  | 121.96 | E1 ${ }^{a}$ | $2.1(5) \times 10^{-4} \mathrm{e}^{2} \mathrm{fm}^{2}$ | $9(2) \times 10^{-5}$ |
|  |  | 141.88 | E1 ${ }^{a}$ | $\leq 7.6(19) \times 10^{-5} \mathrm{e}^{2} \mathrm{fm}^{2}$ | $\leq 3.1(8) \times 10^{-5}$ |
|  |  | 219.69 | E1 ${ }^{a}$ | $1.2(3) \times 10^{-4} \mathrm{e}^{2} \mathrm{fm}^{2}$ | $4.8(12) \times 10^{-5}$ |
|  |  | 237.86 | M1 ${ }^{a}$ | $2.5(4) \times 10^{-3} \mu_{N}^{2}$ | $1.4(2) \times 10^{-3}$ |
| 266.76(10) | $90(20) \mathrm{ps}$ | 106.48 | M1 ${ }^{a}$ | $6.4(18) \times 10^{-4} \mu_{N}^{2}$ | $3.6(10) \times 10^{-4}$ |
|  |  | 150.75 | M1 ${ }^{a}$ | $3.6(10) \times 10^{-5} \mu_{N}^{2}$ | $2.0(6) \times 10^{-5}$ |
|  |  | 170.41 | M1 ${ }^{a}$ | $4.4(12) \times 10^{-5} \mu_{N}^{2}$ | $2.4(7) \times 10^{-5}$ |
|  |  | 192.00 | E1 ${ }^{a}$ | $3.7(9) \times 10^{-5} \mathrm{e}^{2} \mathrm{fm}^{2}$ | $1.5(4) \times 10^{-5}$ |
|  |  | 198.18 | E1 | $1.4(3) \times 10^{-4} \mathrm{e}^{2} \mathrm{fm}^{2}$ | $5.6(14) \times 10^{-5}$ |
|  |  | 205.00 | E1 | $1.4(4) \times 10^{-4} \mathrm{e}^{2} \mathrm{fm}^{2}$ | $5.9(16) \times 10^{-5}$ |
|  |  | 228.73 | E1 ${ }^{a}$ | $2.5(6) \times 10^{-5} \mathrm{e}^{2} \mathrm{fm}^{2}$ | $1.0(3) \times 10^{-5}$ |
|  |  | 260.82 | E1 ${ }^{a}$ | $1.5(4) \times 10^{-5} \mathrm{e}^{2} \mathrm{fm}^{2}$ | $6.2(16) \times 10^{-6}$ |
| 471.60(12) | $<54 \mathrm{ps}$ | 204.79 | M1 | $>1.3(2) \times 10^{-2} \mu_{N}^{2}$ | $>7.4(13) \times 10^{-3}$ |
|  |  | 355.66 | M1 | $>2.1(5) \times 10^{-4} \mu_{N}^{2}$ | $>1.2(3) \times 10^{-4}$ |
|  |  | 396.92 | E1 ${ }^{a}$ | $>2.4(9) \times 10^{-6} \mathrm{e}^{2} \mathrm{fm}^{2}$ | $>1.0(4) \times 10^{-6}$ |
|  |  | 403.03 | E1 ${ }^{a}$ | $>1.2(2) \times 10^{-5} \mathrm{e}^{2} \mathrm{fm}^{2}$ | $>5.0(10) \times 10^{-6}$ |
|  |  | 409.89 | E1 | $>4.1(8) \times 10^{-5} \mathrm{e}^{2} \mathrm{fm}^{2}$ | $>1.7(3) \times 10^{-5}$ |

$\overline{\bar{a} \text { The multipolarity is taken from the decay scheme. For the case of possible E2 or }}$ M1 character the latter is chosen if compatible with the level scheme.

Table 5
Intrinsic dipole moments, $\left|D_{0}\right|$, for E1 transitions in nuclei near ${ }^{231} \mathrm{Ac}$.

| Nucleus | $\mathrm{E}_{i}$ <br> $(\mathrm{keV})$ | $\mathrm{I}_{i}^{\pi} \mathrm{K}_{i}$ | $\mathrm{E}_{\gamma}$ <br> $(\mathrm{keV})$ | $\mathrm{I}_{f}^{\pi} \mathrm{K}_{f}$ | $\left\|D_{0}\right\|$ <br> $(\mathrm{e} \mathrm{fm})$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| ${ }^{227} \mathrm{Fr}$ | 144.32 | $3 / 2^{-} 3 / 2$ | 141.54 | $3 / 2^{+} 3 / 2$ | $0.034(5)^{a}$ |
|  | 164.95 | $5 / 2^{+} 3 / 2$ | 162.17 | $3 / 2^{-} 3 / 2$ | $0.089(7)^{a}$ |
| ${ }^{227} \mathrm{Ac}$ | 27.37 | $3 / 2^{+} 3 / 2$ | 27.37 | $3 / 2^{-} 3 / 2$ | $0.0265(16)^{b}$ |
| ${ }^{231} \mathrm{Ac}$ | 116.02 | $3 / 2^{-} 3 / 2$ | 54.29 | $3 / 2^{+} 3 / 2$ | $0.0239(11)$ |
|  |  |  | 47.45 | $5 / 2^{+} 3 / 2$ | $0.0070(6)$ |
| ${ }^{231} \mathrm{Ac}$ | 238.01 | $3 / 2^{+} 3 / 2$ | 121.96 | $3 / 2^{-} 3 / 2$ | $0.039(5)$ |
|  |  |  | 77.17 | $5 / 2^{-} 3 / 2$ | $0.068(9)$ |
| ${ }^{231} \mathrm{Ac}$ | 266.76 | $3 / 2^{-} 3 / 2$ | 205.00 | $3 / 2^{+} 3 / 2$ | $0.032(4)$ |
|  |  |  | 198.18 | $5 / 2^{+} 3 / 2$ | $0.038(5)$ |

[^1]


Fig. 1. Low-energy part of the gamma spectrum recorded in the planar Ge detector at the conversion electron station. The spectrum was taken during 4 hours and 52 minutes in the second experiment with a collection and measuring time of 200 s. The lines marked with an asterisk belong to the decay chain of the ${ }^{212} \mathrm{Ra}^{19} \mathrm{~F}$ contaminant.


Fig. 2. Compton-subtracted projection spectra gated on the $54.29 \mathrm{keV} \gamma$ line. In the upper part, the summed gamma coincidence spectrum gated on the HPGe detectors from the fast timing station is shown. In the bottom part, the electron- $\gamma$ coincidence spectrum gated on the planar detector from the conversion electron station is displayed. The electron peaks are labelled with the energy values of their corresponding $\gamma$ transitions. The $\mathrm{K}, \mathrm{L}_{I, H} \mathcal{H}_{0} \Sigma \mathrm{M}$ and $\Sigma \mathrm{N}$ electron binding energies in Ac are 106.76, 19.57, 4.47 and 1.07 keV , respectively.


Fig. 3. Conversion electron spectrum taken with the long cycle of 200 s . The electron peaks are labelled with the energy values of their corresponding $\gamma$ transitions. The $\mathrm{K}, \mathrm{L}_{I, I I}, \Sigma \mathrm{M}$ and $\Sigma \mathrm{N}$ electron binding energies in Ac are 106.76, 19.57, 4.47 and 1.07 keV , respectively.


Fig. 4. (a) and (c) $\mathrm{BaF}_{2}$ energy spectra sorted from the triple coincidence $\beta$ - $\mathrm{Ge}^{-}-\mathrm{BaF}_{2}$ events. The Ge-energy gates were set on (a) the 299.10 keV and (c) the 205.0 keV transitions.
(b) and (d) Decay time curves due to the lifetimes of the 116.02 and 266.76 keV levels, respectively. These spectra were obtained by selecting in the $\mathrm{BaF}_{2}$ detector the $54.29 \mathrm{keV} \gamma$ transition (marked by a black rectangle in panel (a)) and the 200 keV region (marked in panel (c)). Panel (d) shows the experimental points, the prompt curve and the slope curve fitted in the deconvolution method.



 $(7 /)^{\text {ZtI }} \mathbf{O V}^{68}$



Fig. 6. Excitation energy systematics for the $1 / 2[400], 1 / 2[530], 3 / 2[651], 3 / 2[402]$, $5 / 2[523], 5 / 2[642]$ bands in the neutron rich Ac and Pa isotopes around $\mathrm{N}=142$. The lowest state of the $3 / 2[651]$ band in ${ }^{231} \mathrm{~Pa}$ is the $5 / 2^{+}$level at $86.48 \mathrm{keV}, 8.18$ keV below the $3 / 2^{+}$. Data are taken from [39|47].
$\frac{5 / 2^{+} \quad 531.0}{5 / 2[642]}$

$$
\frac{5 / 2^{-} \quad 471.6}{5 / 2[532]}
$$



Fig. 7. Tentative assignment of the low energy experimental levels in ${ }^{231} \mathrm{Ac}$ into rotational bands, see text. The levels in green were originally established in reference [9].


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[^1]:    ${ }^{\bar{a}} \mathrm{D}_{0}$ moment values taken from [11].
    ${ }^{b} \mathrm{~B}(\mathrm{E} 1)$ value taken from [41].

