

Two-meson cloud contribution to the baryon antidecuplet binding

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We study the two-meson virtual cloud contribution to the self-energy of the SU(3) antidecuplet, to which the Θ^+ pentaquark is assumed to belong. This is motivated by the large branching ratio of the $N(1710)$ decay into two pions and one nucleon. We derive effective Lagrangians that describe the $N(1710)$ decay into $N\pi\pi$ with two pions in s or p wave. We obtain increased binding for all members of the antidecuplet and a contribution to the mass splitting between states with different strangeness which is at least 20% of the empirical one. We also provide predictions for three-body decays of the pentaquark antidecuplet.

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I. INTRODUCTION

The observation of the signal of the Θ^+ exotic baryon [1], broadly known as the pentaquark for its minimal five-quark Fock space assignment in quantum chromodynamics, was stimulated by the prediction [2, 3] of a $1/2^+$ baryon antidecuplet. Many experimental and theoretical studies have been devoted to this resonance [4, 5]. The original states proposed to form this antidecuplet [2] were:

$$\Theta(1540), N(1710), \Sigma(1890), \Xi(2070),$$

where the first and last, explicitly exotic states, had not been observed at that time. Isospin SU(2) is expected to hold to very good accuracy and we do not list the I_3 quantum number.

This assignment is now, however, challenged for several reasons. First, the NA49 collaboration [6] reported evidence for an exotic cascade Ξ^{--} , probably in the same antidecuplet, with a much lighter mass, 1860 MeV. This is somewhat problematic as doubts have arisen [7], and it has not been seen in other experiments [8, 9] (See, however, K. Kadija's presentation at the PENTAQUARK04 Workshop [10] with new reanalyses still supporting the findings of Ref. [7]). However, should the state be reconfirmed at 1860 MeV, using the standard Gell-Mann-Okubo rule (GMO) of equal mass splittings for the SU(3) antidecuplet, the mass of $N_{\overline{10}}$ would have to be near 1647 MeV, which is about 60 MeV below the nominal one $N(1710)$. Furthermore, the mass of $\Sigma_{\overline{10}}$ would have to be about 1753 MeV. Since a Σ resonance is listed at 1770 MeV with the same spin and parity, we will refer to the Σ member of the antidecuplet as $\Sigma(1770)$. The association of this state to the $\Sigma(1890)$ would not fit in that

scenario [11].

Second, quark model calculations that have appeared after the report of the evidence of Θ^+ tend to predict an $N_{\overline{10}}$ at around 1650 MeV [12, 13]. These predicted the $\Xi_{\overline{10}}$ at 1900 MeV [13], which is more in line with the experimental outcome than the original calculation of the chiral soliton model, although the latter can be readjusted (then underestimating the N^*).

Another difficulty arises because of the potential mixing of the nonexotic members of the multiplet, the $N_{\overline{10}}$ and $\Sigma_{\overline{10}}$ with members of pentaquark or ordinary three-quark octets [11, 14, 15]. This would make the mass splitting between the physical states dependent on two mixing angles. A current conjecture is a mixing with the Roper resonance [14] that would, by level repulsion, push the $N(1710)$ further above the Θ^+ than predicted by the GMO rule. Also with ideal mixing, the hidden strangeness $s\bar{s}$ wave function dominates the $N(1710)$, thus raising its mass. However, such a strong mixing is not preferred by other authors [11, 16, 17]. In summary, a new N^* state would have to be searched for at a smaller mass if we were to impose perfect GMO rule.

The models we work with in this paper are rather phenomenological. However, our method, based on symmetry principles, is suited to at least estimating meson cloud effects, which are important for the understanding of pentaquark properties. The main conclusion of this work is that the virtual "two-meson cloud" yields an attractive self-energy that provides about 20% of the pentaquark mass splittings. We believe that our study here will become useful when more data are available.

The study presented here is complementary and looks for another source of mass splitting not contemplated by the GMO rule. It would come from the two-meson cloud. The possibility of constructing the Θ^+ as a $K\pi N$ bound state [18–21] has been examined in some detail [22] employing meson-meson and meson-baryon interactions from chiral Lagrangians, where attraction was found but not strong enough to bind the system. Yet, this result

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leaves one wondering as to what role the two-meson cloud could play in the stability of the state. Coupling to multi-meson components is also implicit in the chiral soliton picture, which leads to small masses of the Θ^+ [2, 23].

In the present paper, we do not face the possible contribution of the one-meson cloud to the antidecuplet binding, which can be easily addressed as a minor correction to our results. The small width of the Θ^+ to KN , in spite of the appreciable phase space available, qualitatively demands that this contribution should be reasonably small; in fact, it has been checked quantitatively in Refs. [24–26]. The self-energy of Θ^+ with a two-meson cloud has been studied in parallel [26] in the context of the medium modification of Θ^+ and possible formation of Θ^+ hypernuclei [27]. We here report in full on vacuum results for not only the Θ^+ but also other members of the antidecuplet.

An important experimental input relevant to the present study is the relatively large branching ratio of $N(1710)$ into $N\pi\pi$, about 40 – 90% [28]. The branching ratio into $N\pi\pi$ with the two pions in an s wave is 10 – 40% and into ρN , 5 – 25%. This $N(1710)$ resonance and its baryon-meson-meson decay mode has been used in Ref. [29] to produce a good shape of the $\Sigma\pi$ distribution in the $\pi^-p \rightarrow K^0\pi\Sigma$ reaction leading to the $\Lambda(1405)$ [46].

In the present work, we assume that the $N(1710)$ has a large antidecuplet component [11], and we will perform a study of the $N\pi\pi$ s wave and ρN decay channels of this resonance and their influence on the masses of various members of the antidecuplet. Certainly one has to accept a mixing with an octet component for realistic resonances in order, for instance, to explain the $N(1710)$ decay into $\Delta\pi$, which is forbidden for its antidecuplet component [15, 30]. But we do not expect the mixing angle to be close to ideal, as this would imply a stronger ΛK branching ratio than 5 – 25%, as observed experimentally. The decay pattern of $N(1710)$ and $N(1440)$ also supports the small mixing angle [16, 17].

The present study also provides information on the antidecuplet baryon-baryon-meson-meson ($PBMM$) contact interaction, which could be applied to the study of Θ^+ production with the $\pi^-p \rightarrow K^-\Theta^+$ and $K^+p \rightarrow \pi^+\Theta^+$ reactions. These reactions are studied in Refs. [31–34] and experimental information is becoming available [35, 36].

The paper is organized as follows. In Sec. II, we construct various $PBMM$ interactions with the two octet mesons and one baryon belonging to octets and with the other baryon to an antidecuplet. In Sec. III, we compute the contributions of two-meson and one-baryon loops to the mass splittings among the members of antidecuplet baryons. In Sec. IV, we present numerical results and discuss the importance of two-meson contributions to the mass splittings and partial decay widths. As we will see, the contributions from the two-meson loops provide sizable contributions to supplement the mass splittings naively expected from strange quark counting. We will

then discuss the range of interaction strengths of various coupling terms. Section V is devoted to a summary. We also add appendices, where complete tables for the $PBMM$ interactions are presented.

II. CONSTRUCTION OF EFFECTIVE INTERACTION LAGRANGIANS

A. Definition of fields

Following a common convention [37–39], we write the physical meson and baryon fields as follows

$$\phi = \begin{pmatrix} \frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta & \pi^+ & K^+ \\ \pi^- & -\frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta & K^0 \\ K^- & \bar{K}^0 & -\frac{2}{\sqrt{6}}\eta \end{pmatrix}, \quad (1)$$

$$B = \begin{pmatrix} \frac{1}{\sqrt{2}}\Sigma^0 + \frac{1}{\sqrt{6}}\Lambda & \Sigma^+ & p \\ \Sigma^- & -\frac{1}{\sqrt{2}}\Sigma^0 + \frac{1}{\sqrt{6}}\Lambda & n \\ \Xi^- & \Xi^0 & -\frac{2}{\sqrt{6}}\Lambda \end{pmatrix}. \quad (2)$$

The antidecuplet containing the exotic pentaquark states is a tensor P^{ijk} totally symmetric in its three SU(3) indices. The components of P^{ijk} are related to the physical fields by

$$\begin{aligned} P^{333} &= \sqrt{6}\Theta_{10}^+, & P^{133} &= \sqrt{2}N_{10}^0, \\ P^{233} &= -\sqrt{2}N_{10}^+, & P^{113} &= \sqrt{2}\Sigma_{10}^-, \\ P^{123} &= -\Sigma_{10}^0, & P^{223} &= -\sqrt{2}\Sigma_{10}^+, \\ P^{111} &= \sqrt{6}\Xi_{10}^{--}, & P^{112} &= -\sqrt{2}\Xi_{10}^-, \\ P^{122} &= \sqrt{2}\Xi_{10}^0, & P^{222} &= -\sqrt{6}\Xi_{10}^+, \end{aligned} \quad (3)$$

where we have adopted the normalization in Ref. [40], which is different from those used in Refs. [25, 41, 42] by a sign and/or a factor.

Now we consider the possible interaction Lagrangians, constrained to be SU(3) symmetric. We intend to address the process

$$\mathbf{8}_M + \mathbf{8}_M + \mathbf{8}_B \rightarrow \bar{\mathbf{10}}_P, \quad (4)$$

where an octet baryon $\mathbf{8}_B$ and two octet mesons $\mathbf{8}_M$ couple to an antidecuplet baryon $\bar{\mathbf{10}}_P$. To have an SU(3) invariant Lagrangian, we couple first the two $\mathbf{8}_M$ and then combine the resulting irreducible representations with the baryon $\mathbf{8}_B$ to produce a $\bar{\mathbf{10}}_{BMM}$ representation.

The group theoretical irreducible decomposition gives

$$\begin{aligned}
& \mathbf{8}_M \otimes \mathbf{8}_M \otimes \mathbf{8}_B \\
&= (\mathbf{1} \oplus \mathbf{8}^s \oplus \mathbf{8}^a \oplus \mathbf{10} \oplus \overline{\mathbf{10}} \oplus \mathbf{27})_{MM} \otimes \mathbf{8}_B \\
&= \mathbf{8} \quad \leftarrow \text{from } \mathbf{1}_{MM} \otimes \mathbf{8}_B \\
&\quad \oplus (\mathbf{1} \oplus \mathbf{8} \oplus \mathbf{8} \oplus \mathbf{10} \oplus \overline{\mathbf{10}} \oplus \mathbf{27}) \quad \leftarrow \text{from } \mathbf{8}_{MM}^s \otimes \mathbf{8}_B \\
&\quad \oplus (\mathbf{1} \oplus \mathbf{8} \oplus \mathbf{8} \oplus \mathbf{10} \oplus \overline{\mathbf{10}} \oplus \mathbf{27}) \quad \leftarrow \text{from } \mathbf{8}_{MM}^a \otimes \mathbf{8}_B \\
&\quad \oplus (\mathbf{8} \oplus \mathbf{10} \oplus \mathbf{27} \oplus \mathbf{35}) \quad \leftarrow \text{from } \mathbf{10}_{MM} \otimes \mathbf{8}_B \\
&\quad \oplus (\mathbf{8} \oplus \overline{\mathbf{10}} \oplus \mathbf{27} \oplus \mathbf{35}') \quad \leftarrow \text{from } \overline{\mathbf{10}}_{MM} \otimes \mathbf{8}_B \\
&\quad \oplus (\mathbf{8} \oplus \mathbf{10} \oplus \overline{\mathbf{10}} \oplus \mathbf{27} \oplus \mathbf{27} \oplus \mathbf{35} \oplus \mathbf{35}'' \oplus \mathbf{64}) \\
&\quad \leftarrow \text{from } \mathbf{27}_{MM} \otimes \mathbf{8}_B. \tag{5}
\end{aligned}$$

Here $\mathbf{8}^s$ and $\mathbf{8}^a$ denote symmetric and antisymmetric combinations of the two-meson fields. Hence we obtain four $\overline{\mathbf{10}}_{BMM}$ representations after recoupling $\mathbf{8}_{MM}^s$, $\mathbf{8}_{MM}^a$, $\mathbf{10}_{MM}$ and $\mathbf{27}_{MM}$ with $\mathbf{8}_B$.

B. Two-meson $\mathbf{8}^s$ representation

In constructing effective Lagrangians, we follow the principle of using the minimum numbers of derivatives in the fields. This will be released later when we discuss possible structures involving derivatives. To construct $\mathbf{8}^s$ from two $\mathbf{8}_M$, we have in tensor notation

$$\begin{aligned}
D_i^j[\mathbf{8}_{MM}^s] &= \phi_i^a \phi_a^j + \phi_i^a \phi_a^j - \frac{2}{3} \delta_i^j \phi_a^b \phi_b^a \\
&= 2\phi_i^a \phi_a^j - \frac{2}{3} \delta_i^j \phi_a^b \phi_b^a. \tag{6}
\end{aligned}$$

We combine this now with an $\mathbf{8}_B$ to give an antidecuplet

$$\begin{aligned}
T^{ijk}[\overline{\mathbf{10}}_{BMM(8s)}] &= 2\phi_l^a \phi_a^i B_m^j \epsilon^{lmk} \\
&\quad + (i, j, k \text{ symmetrized}). \tag{7}
\end{aligned}$$

Hence, the interaction Lagrangian becomes

$$\mathcal{L}^{8s} = \frac{g^{8s}}{2f} \bar{P}_{ijk} \epsilon^{lmk} \phi_l^a \phi_a^i B_m^j + \text{h.c.}, \tag{8}$$

where h.c. denotes the Hermitian conjugate terms, in order to take into account the processes in which the antidecuplet is in the initial state. Note also that two ϕ fields have appeared, and we have included a factor $1/2f$ in order to make g^{8s} dimensionless (f is the pion decay constant $f = 93$ MeV).

C. Two-meson $\mathbf{8}^a$ representation

Next we take the antisymmetric combination of the $\mathbf{8}_M$ and $\mathbf{8}_M$, which for identical meson octets leads to

$$A_i^j[\mathbf{8}_{MM}^a] = \phi_i^a \phi_a^j - \phi_i^a \phi_a^j = 0. \tag{9}$$

So given the identity of the meson octets, this combination is zero. The simplest way to construct the Lagrangian of this structure is to introduce a derivative in

one of the fields, which leads automatically to the vector current consisting of two meson fields. Proceeding as before, we combine this structure with the $\mathbf{8}_B$ to give $\overline{\mathbf{10}}$ then finally

$$\mathcal{L}^{8a} = i \frac{g^{8a}}{4f^2} \bar{P}_{ijk} \epsilon^{lmk} \gamma^\mu (\partial_\mu \phi_l^a \phi_a^i - \phi_l^a \partial_\mu \phi_a^i) B_m^j + \text{h.c.}, \tag{10}$$

where g^{8a} is dimensionless. This interaction Lagrangian contains the coupling of the $N(1710)$ with $N\pi\pi$, the two pions in a ρ -meson type correlation. From the experimental branching ratio, we can determine the coupling constant g^{8a} .

D. Two-meson $\overline{\mathbf{10}}$ representation

To construct the $\overline{\mathbf{10}}$ combination from two mesons, we have now

$$\begin{aligned}
T_{MM}^{ijk}[\overline{\mathbf{10}}_{MM}] &= \epsilon^{lmk} \phi_l^i \phi_m^j + (i, j, k \text{ symmetrized}) \\
&= \epsilon^{lmk} \phi_l^i \phi_m^j + \epsilon^{lmk} \phi_l^j \phi_m^i + \epsilon^{lmi} \phi_l^j \phi_m^k \\
&\quad + \epsilon^{lmi} \phi_l^k \phi_m^j + \epsilon^{lmj} \phi_l^k \phi_m^i + \epsilon^{lmj} \phi_l^i \phi_m^k \\
&= 0, \tag{11}
\end{aligned}$$

which is identically zero for equal meson octets.

E. Two-meson $\mathbf{27}$ representation

The expansion for the $\mathbf{27}$ representation leads to

$$\begin{aligned}
H_{ik}^{jl}[\mathbf{27}_{MM}] &= \phi_i^j \phi_k^l + \phi_i^l \phi_k^j + \phi_k^j \phi_i^l + \phi_k^l \phi_i^j \\
&\quad - \frac{1}{5} (\delta_i^j D_k^l + \delta_i^l D_k^j + \delta_k^j D_i^l + \delta_k^l D_i^j) \\
&\quad - \frac{1}{6} (\delta_i^j \delta_k^l \phi_a^b \phi_b^a + \delta_i^l \delta_k^j \phi_a^b \phi_b^a), \tag{12}
\end{aligned}$$

where D_i^j is defined in Eq. (6). Now the combination of $\mathbf{27}_{MM}$ to $\mathbf{8}_B$ to give the $\overline{\mathbf{10}}$ representation leads to

$$\begin{aligned}
\mathcal{L}^{27} &= \frac{g^{27}}{2f} \left[4\bar{P}_{ijk} \epsilon^{lbk} \phi_l^i \phi_a^j B_b^a \right. \\
&\quad \left. - \frac{4}{5} \bar{P}_{ijk} \epsilon^{lbk} \phi_l^a \phi_a^j B_b^i \right] + \text{h.c.}, \tag{13}
\end{aligned}$$

where the first term gives us a new SU(3) structure, but the second one is equal to \mathcal{L}^{8s} given in Eq. (8).

To summarize briefly, for the possible SU(3) symmetric couplings of $PBMM$, there are two independent terms with no derivatives, namely Eqs. (8) and (13). With one derivative, there are four more terms available, but we will consider only Eq. (10), which has the structure for the decay of $N(1710) \rightarrow N\pi\pi$ (p -wave) as observed experimentally.

F. Chiral symmetric Lagrangians

In the perturbative chiral Lagrangian approach, one would like to implement chiral symmetry as a derivative expansion. In addition, one of the advantages of chiral Lagrangians is that they relate coupling constants of different processes and, in particular, with increasing number of mesons. However, in the present case we cannot take advantage of any of these relations, since the couplings for the present Lagrangians are *a priori* completely arbitrary, and we are only interested in the two-meson problem. Still, in this section we build the lowest-order chiral Lagrangian, with two derivatives. Let us remark that the chiral expansion with baryons is known to converge much more slowly than chiral perturbation theory with mesons, and this lowest-order Lagrangian can only be expected to give a mere qualitative description of the physics. For that reason, to build the Lagrangians of the previous Secs. II B and II E we just relied on flavor SU(3). Still, we will check here that the lack of chiral symmetry in those Lagrangians does not have much relevance to the mass splittings and decays we are interested in, since already with the leading-order Lagrangian we get qualitatively the same results. In other words, the relevant symmetry here is SU(3), not chiral symmetry.

To show this, we write a chiral invariant Lagrangian by making the substitution $\phi \cdot \phi \rightarrow A_\mu \cdot A^\mu$ in Eq. (8) such that

$$\mathcal{L}^\chi = \frac{g^\chi}{2f} \bar{P}_{ijk} \epsilon^{lmk} (A_\mu)_l^a (A^\mu)_a^i B_m^j + \text{h.c.}, \quad (14)$$

where A_μ is the axial current written in terms of the chiral field ξ :

$$A_\mu = \frac{i}{2} (\xi^\dagger \partial_\mu \xi - \xi \partial_\mu \xi^\dagger), \quad (15)$$

with $\xi = e^{i\phi/\sqrt{2}f}$. To the leading order in meson field, $A_\mu \sim -\partial_\mu \phi/\sqrt{2}f$, we find the interaction Lagrangian induced from Eq. (14) by making the replacement

$$(A_\mu)_l^a (A^\mu)_a^i \rightarrow \frac{1}{2f^2} \partial_\mu \phi_l^a \partial^\mu \phi_a^i. \quad (16)$$

Obviously, the SU(3) structure is not affected by this procedure, although the use of Lagrangians involving derivatives will introduce some degree of SU(3) breaking due to the momenta of mesons. Hence, it is useful to verify that this chiral invariant Lagrangian will lead eventually to the same results as those obtained from the Lagrangians without derivatives in the fields. We also perform self-energy calculations using this $\mathbf{8}^s$ chirally symmetric Lagrangian, Eq. (14).

G. Explicit SU(3) breaking term

In this section, we consider the SU(3) breaking interaction term within the context of chiral Lagrangians. Without using derivatives in the fields, the only possible term

is a mass term that violates both SU(3) and chiral symmetry, but in the way demanded by the underlying QCD Lagrangian [37–39]. The mass term appears through the combination

$$S = \xi M \xi + \xi^\dagger M \xi^\dagger, \quad (17)$$

with the mass matrix, written in terms of the meson masses,

$$M = \begin{pmatrix} m_\pi^2 & & \\ & m_\pi^2 & \\ & & 2m_K^2 - m_\pi^2 \end{pmatrix}. \quad (18)$$

Then it leads to the Lagrangian

$$\mathcal{L}^M = \frac{g^M}{2f} \bar{P}_{ijk} \epsilon^{lmk} S_l^i B_m^j + \text{h.c.}, \quad (19)$$

In the expansion of S , we have two meson fields with the structure

$$S^{(2)} = -\frac{1}{2f^2} (2\phi M \phi + \phi \phi M + M \phi \phi). \quad (20)$$

Substituting $S^{(2)}$ for S in Eq. (19), we obtain the desired mass Lagrangian.

III. SELF-ENERGIES

A. Two-meson loops

The antidecuplet self-energies deduced from one of the interaction Lagrangians can be obtained by

$$\begin{aligned} \Sigma_P^{(j)}(p^0) &= \sum_{B, m_1, m_2} \left(F^{(j)} C_{P, B, m_1, m_2}^{(j)} \right) \\ &\times I^{(j)}(p^0; B, m_1, m_2) \left(F^{(j)} C_{P, B, m_1, m_2}^{(j)} \right), \end{aligned} \quad (21)$$

where the index j stands for $8s$, $8a$, 27 , χ and M for corresponding Lagrangians (8), (10), (13), (14) and (19); P denotes the antidecuplet states $P = \Theta_{\overline{10}}, N_{\overline{10}}, \Sigma_{\overline{10}}$ and $\Xi_{\overline{10}}$; the argument p^0 is the energy of the antidecuplet baryon; and the factors $F^{(j)}$ are

$$\begin{aligned} F^{8s} &= \frac{g^{8s}}{2f}, & F^{8a} &= \frac{g^{8a}}{4f^2}, \\ F^{27} &= \frac{g^{27}}{2f}, & F^\chi &= \frac{g^\chi}{2f}, & F^M &= \frac{g^M}{2f}. \end{aligned} \quad (22)$$

In Eq. (21), $C_{P, B, m_1, m_2}^{(j)}$ are SU(3) coefficients that come directly from the Lagrangians when evaluating the different matrix elements. We compile the results in Appendix A.

The function $I^{(j)}(p^0; B, m_1, m_2)$ of argument p^0 (the energy of the assumed state of the antidecuplet at rest)

is the two-loop integral with two mesons and one baryon as shown in Fig. 1.

$$\begin{aligned}
I^{(j)}(p^0; B, m_1, m_2) &= - \int \frac{d^4 k}{(2\pi)^4} \int \frac{d^4 q}{(2\pi)^4} \\
&\times |t^{(j)}|^2 \frac{1}{k^2 - m_1^2 + i\epsilon} \frac{1}{q^2 - m_2^2 + i\epsilon} \\
&\times \frac{M}{E} \frac{1}{p^0 - k^0 - q^0 - E + i\epsilon}, \quad (23)
\end{aligned}$$

where

$$|t^{(j)}|^2 = 1 \quad \text{for } j = 8s, 27, M, \quad (24)$$

$$|t^\chi|^2 = \frac{(\omega_1 \omega_2 - \mathbf{k} \cdot \mathbf{q})^2}{4f^4}, \quad (25)$$

$$\begin{aligned}
|t^{8a}|^2 &= \frac{1}{2M} \left\{ (E + M)(\omega_1 - \omega_2)^2 + 2(|\mathbf{k}|^2 - |\mathbf{q}|^2)(\omega_1 - \omega_2) \right. \\
&\quad \left. + (E - M)(\mathbf{k} - \mathbf{q})^2 \right\}, \quad (26)
\end{aligned}$$

$$E = \sqrt{M^2 + (\mathbf{k} + \mathbf{q})^2},$$

$$\omega_1 = \sqrt{m_1^2 + \mathbf{k}^2}, \quad \omega_2 = \sqrt{m_2^2 + \mathbf{q}^2}.$$

In these expressions, M and m_i are the masses of a baryon and mesons. The more complicated integrand in $|t^{(8a)}|^2$ arises because of the $\bar{u}\gamma^\mu(k - q)_\mu u$ factor when one derivative is included as in Eq. (10). We neglect the negative-energy intermediate baryon propagator as this is suppressed by a further power of q/M , leading only to a small relativistic correction. The k^0 and q^0 integrations of Eq. (23) are easily carried out, and we obtain

$$\begin{aligned}
I^{(j)}(p^0; B, m_1, m_2) &= \int \frac{d^3 k}{(2\pi)^3} \int \frac{d^3 q}{(2\pi)^3} |t^{(j)}|^2 \frac{1}{2\omega_1} \frac{1}{2\omega_2} \\
&\times \frac{M}{E} \frac{1}{p^0 - \omega_1 - \omega_2 - E + i\epsilon}, \quad (27)
\end{aligned}$$

The real part of this integral is divergent. We regularize it with a cutoff Λ in the three momentum on \mathbf{k} and \mathbf{q} , which is a parameter of the calculation and its value must be somewhat larger than the scale of the typical pion momenta. On the other hand, we use low-energy Lagrangians with one or two derivatives at most, and thus the cutoff should not be too large; otherwise, terms with more derivatives could become relevant. In this work we will take Λ in the range 700 – 800 MeV, roughly the order of magnitude of the cutoff used to regularize the meson-baryon loops in the study of the $\bar{K}N$ interaction [43]. With the \mathcal{L}^χ of Sec. IIF, the cutoff is smaller in order to reproduce analogous results to those with the $8s$ Lagrangian.

The imaginary part of the diagram represents the decay width, in accordance with the optical theorem. The total decay width of a member of the antidecuplet to any BMM states is given by

$$\Gamma_P^{(j)}(p^0) = -2\text{Im}\Sigma_P^{(j)}(p^0), \quad (28)$$

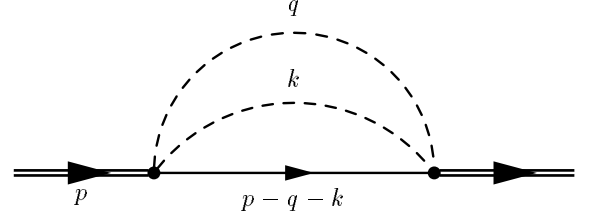


FIG. 1: Self-energy of baryon antidecuplet caused by two-meson cloud.

while the partial decay width to a particular channel is given by

$$\begin{aligned}
\Gamma_P^{(j)}(p^0; B, m_1, m_2) &= -2\text{Im} \left(F^{(j)} C_{P,B,m_1,m_2}^{(j)} \right) \\
&\times I^{(j)}(p^0; B, m_1, m_2) \left(F^{(j)} C_{P,B,m_1,m_2}^{(j)} \right), \quad (29)
\end{aligned}$$

As an example, let us give in detail the contribution from \mathcal{L}^{8a} to the Θ_{10} self-energy

$$\begin{aligned}
\Sigma_{\Theta}^{8a}(p^0) &= (F^{8a})^2 [18I^{8a}(p^0; N, K, \pi) \\
&\quad + 18I^{8a}(p^0; N, K, \eta)], \quad (30)
\end{aligned}$$

and the contribution from \mathcal{L}^{8s} to the Ξ_{10} self-energy

$$\begin{aligned}
\Sigma_{\Xi}^{8s}(p^0) &= (F^{8s})^2 [9I^{8s}(p^0; \Sigma, \bar{K}, \pi) + I^{8s}(p^0; \Sigma, \bar{K}, \eta) \\
&\quad + 6I^{8s}(p^0; \Xi, \bar{K}, K) + 4I^{8s}(p^0; \Xi, \pi, \eta)]. \quad (31)
\end{aligned}$$

The expression for all cases can be derived from Tables IX–XII in Appendix B.

In Eq. (21), we gave a contribution to the self-energy from one interaction Lagrangian $\mathcal{L}^{(j)}$. For the total self-energy, the sum should be taken over the five interactions ($j = 8s, 8a, 27, \chi$ and M) at each vertex. This means that at each vertex function, we should make the replacement as $(F^{(j)} C_{P,B,m_1,m_2}^{(j)} |t^{(j)}|) \rightarrow (|\sum_j F^{(j)} C_{P,B,m_1,m_2}^{(j)} t^{(j)}|)$. We shall, however, not take into account interference between the $8a$ term and the others because of the p -wave nature of the term.

B. Inclusion of the ρ meson

It is known that $N(1710) \rightarrow N\pi\pi$ (p wave) occurs through the $N\rho$ decay. In order to keep close to the experimental information, we shall also assume that the pair of mesons in the $8a$ case reconstruct a vector meson. Hence, we replace the contact interaction of the \mathcal{L}^{8a} to account for the vector meson propagator (Fig. 2) and include the factor

$$\frac{m_v^2}{(q+k)^2 - m_v^2}, \quad (32)$$

in each $P \rightarrow BMM$ vertex. The consideration of these contributions needs extra work on the loop integrals since

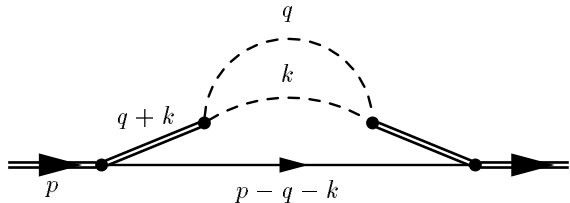


FIG. 2: Self-energy of baryon antidecuplet caused by two-meson cloud with vector meson propagators.

we introduce new poles. The imaginary part of the integrals (associated to placing on-shell the BMM intermediate states) can be easily accounted for by multiplying the integrand of Eq. (23) by

$$\left| \frac{m_v^2}{(q+k)^2 - m_v^2 + im_v \Gamma(q+k)} \right|^2, \quad (33)$$

where $\Gamma(q+k)$ accounts for the width of the vector meson (ρ or K^* depending on the MM) incorporating the energy dependence through the factor $(P(q+k)/P_{on})^3$ multiplied to the nominal width, with $P(q+k)$ the relative three momentum of the mesons in the decay of the vector meson in the rest frame and $P_{on} = P((M_v, \mathbf{0}))$.

For the real part, one must sort out the poles of the vector meson and the intermediate BMM state, which is technically implemented by means of the integral

$$\begin{aligned} & \text{Re} \{ I^{8a}(p^0; B, m_1, m_2) \} \\ &= -m_v^4 \frac{\partial}{\partial(m_v^2)} \text{P.V.} \int \frac{d^4 q}{(2\pi)^4} \int \frac{d^4 k}{(2\pi)^4} |t^{8a}|^2 \\ & \quad \times \frac{1}{k^2 - m_1^2 + i\epsilon} \frac{1}{q^2 - m_2^2 + i\epsilon} \\ & \quad \times \frac{1}{(k+q)^2 - m_v^2 + i\epsilon} \\ & \quad \times \frac{M}{E} \frac{1}{p^0 - k^0 - q^0 - E + i\epsilon}, \end{aligned} \quad (34)$$

where P.V. stands for the principal value. Here, we neglected the width of the vector meson, which does not play much of a role in the off-shell regions of integrations. The k^0 and q^0 integrations can be performed analytically, and one obtains the simple expression

$$\begin{aligned} & \text{Re} \{ I^{8a}(p^0; B, m_1, m_2) \} \\ &= m_v^4 \frac{\partial}{\partial(m_v^2)} \text{P.V.} \int \frac{d^3 k}{(2\pi)^3} \int \frac{d^3 q}{(2\pi)^3} |t^{8a}|^2 \\ & \quad \times \frac{1}{2\omega_1} \frac{1}{2\omega_2} \frac{1}{\omega_v} \frac{1}{\omega_v + \omega_1 + \omega_2} \\ & \quad \times \frac{1}{p_0 - \omega_v - E + i\epsilon} \\ & \quad \times \frac{1}{p_0 - \omega_1 - \omega_2 - E + i\epsilon} \frac{M}{E} \\ & \quad \times (\omega_1 + \omega_2 + \omega_v - p_0 + E), \end{aligned} \quad (35)$$

where ω_v is the on-shell energy of the vector meson.

IV. NUMERICAL EXAMPLES

Next we present some numerical results that illustrate the antidecuplet mass shifts and decay widths to three-body channels. One of the most exciting aspects in the antidecuplet is that the Θ^+ is located about 30 MeV below the $NK\pi$ threshold. Hence, it cannot decay into this or any other BMM channels to which it couples. For the interaction Lagrangians, we obtain the $g^{(j)}$ coefficients from the experimentally allowed decay amplitudes of the $N(1710)$. We give several examples that illustrate the general behavior of the two-meson cloud, common to the Lagrangians described in previous sections.

Before studying each of the Lagrangians, let us recall that the mass splitting of the antidecuplet has a contribution which follows the GMO rule, and it would be originated by the difference of the masses of the constituent quarks and their correlations. To this, we add the splitting coming from the real part of the self-energy due to the meson cloud that we are studying. Thus, the masses of the antidecuplet are approximately given by

$$\begin{aligned} M_{\Theta_{\overline{10}}} &= M_0 + \text{Re}\Sigma_{\Theta_{\overline{10}}}, \\ M_{N_{\overline{10}}} &= M_0 + \text{Re}\Sigma_{N_{\overline{10}}} + \Delta, \\ M_{\Sigma_{\overline{10}}} &= M_0 + \text{Re}\Sigma_{\Sigma_{\overline{10}}} + 2\Delta, \\ M_{\Xi_{\overline{10}}} &= M_0 + \text{Re}\Sigma_{\Xi_{\overline{10}}} + 3\Delta, \end{aligned} \quad (36)$$

where M_0 is the bare mass of the antidecuplet and Δ is the GMO mass splitting, part of which simply comes from the difference of the constituent quark masses. In the constituent quark model, Δ is related to the difference between the constituent masses of u , d and s quarks, $3\Delta = \langle m_s - m_{u,d} \rangle_{\text{baryon}}$. Certainly, quark correlations can also contribute to the experimental value of Δ .

The difference between the light and strange quark masses has been obtained, for example from hyperfine splittings, in Ref. [44],

$$\begin{aligned} \langle m_s - m_u \rangle_{\text{meson}} &= \frac{3(M_{K^*} - M_\rho) + (M_K - M_\pi)}{4} \\ &\simeq 180 \text{ MeV}, \end{aligned} \quad (37)$$

whereas for baryons

$$\begin{aligned} \langle m_s - m_u \rangle_{\text{baryon}} &= M_\Lambda - M_N \simeq 177 \text{ MeV}, \\ \langle m_s - m_u \rangle_{\text{baryon}} &= \frac{M_N + M_\Delta}{6} \left(\frac{M_\Delta - M_N}{M_{\Sigma^*} - M_\Sigma} - 1 \right) \\ &\simeq 190 \text{ MeV}. \end{aligned} \quad (38)$$

But other differences like $M_{K^*} - M_\rho$, $M_\Xi - M_N$ or $M_\Sigma - M_N$ suggest a wider range, from 122 to 190 and 250 MeV, respectively. As we will see, the values of 3Δ needed within this work are of this order of magnitude but somewhat larger, leaving room for extra quark correlations effects.

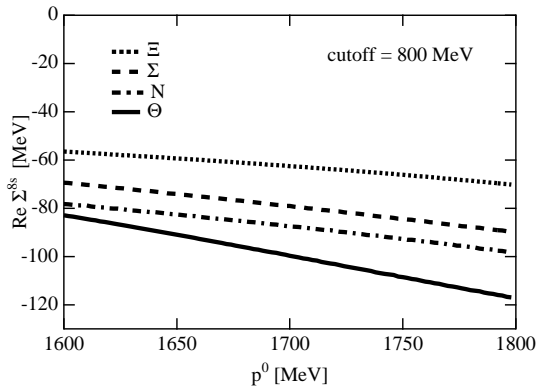


FIG. 3: Mass shifts of baryon antidecuplet ($\text{Re}\Sigma_P$) due to two-meson cloud from \mathcal{L}^{8s} with cutoff = 800 MeV; p^0 dependence.

A. Antidecuplet mass shift with \mathcal{L}^{8s} and \mathcal{L}^{8a}

To fix the couplings of the Lagrangians, we start by taking \mathcal{L}^{8s} and \mathcal{L}^{8a} defined above and adjusting the coupling constants to obtain the partial decay widths of the $N(1710)$ to $N\pi\pi$ (s wave, isoscalar) and $N\rho \rightarrow N\pi\pi$ (p wave, isovector) respectively. These are controlled by the imaginary part of the self-energies (29), which are finite and independent of the cutoff. The central values in the Particle Data Group (PDG) [28] are

$$\begin{aligned} \Gamma(N\pi\pi, s \text{ wave}) &= 25 \text{ MeV}, \\ \Gamma(N\pi\pi, p \text{ wave}) &= 15 \text{ MeV}, \end{aligned} \quad (39)$$

and the uncertainties (counting those of the branching ratio and the total width) can be a large fraction of these numbers.

A fit to these central values gives us

$$g^{8s} = 1.9, \quad g^{8a} = 0.32. \quad (40)$$

With these couplings, we calculate the real part of the self-energies for all the antidecuplet. For the bare antidecuplet mass p^0 as input, we take an average value of $p^0 = 1700$ MeV. We also performed a calculation with different values of p^0 and found that the results have the same qualitative trend, but the depth of the binding varies. To estimate the binding, we show the mass shift from the \mathcal{L}^{8s} with respect to p^0 in Fig. 3. We see that, independently of the values of p^0 , all the self-energies are attractive, and that the interaction is more attractive the larger the strangeness; hence, the $\Theta_{\overline{10}}$ is always more bound.

In Fig. 4 we show the results for the contributions from \mathcal{L}^{8s} and total contributions of \mathcal{L}^{8a} and \mathcal{L}^{8s} , with $p^0 = 1700$ MeV and cutoffs 700 and 800 MeV. The numerical values of the mass shifts are displayed in Table I. We see that \mathcal{L}^{8s} provides more binding than \mathcal{L}^{8a} for the same cutoff. The total binding for $\Theta_{\overline{10}}$ ranges from 90 to about 130 MeV, depending on the cutoff. The splitting between

TABLE I: Mass shifts of baryon antidecuplet ($\text{Re}\Sigma_P$) due to two-meson cloud with $p^0 = 1700$ MeV and cutoffs 700 and 800 MeV. All values are shown in units of MeV.

	cutoff 700 MeV			cutoff 800 MeV		
	\mathcal{L}^{8s}	\mathcal{L}^{8a}	total	\mathcal{L}^{8s}	\mathcal{L}^{8a}	total
$\Theta_{\overline{10}}$	-71	-20	-91	-100	-32	-132
$N_{\overline{10}}$	-60	-7	-67	-87	-17	-104
$\Sigma_{\overline{10}}$	-54	-9	-63	-79	-15	-94
$\Xi_{\overline{10}}$	-40	-5	-45	-63	-9	-72

the $\Theta_{\overline{10}}$ and $\Xi_{\overline{10}}$ states is about 45 MeV for a cutoff of 700 MeV and 60 MeV for a cutoff of 800 MeV. Since the experimental splitting is 320 MeV for the $\Theta(1540)$ and $\Xi(1860)$, the splitting provided by the two-meson cloud is on the order of 20% of the experimental one.

We believe these magnitudes to be realistic (and hence one of the reasons to settle for a cutoff) based on the findings of Ref. [22] that the meson-baryon interaction is insufficient to bind the $K\pi N$ system and that one has to increase the interaction by about a factor of 5 to have the three-particle system bound. Indeed, had the nature of the $\Theta(1540)$ been that of the $K\pi N$ system, we would have obtained all the splitting from the two-meson cloud. There is, hence, a qualitative correlation between the moderate amount of the two-meson cloud contribution claimed here and the difficulty to make the stable $K\pi N$ system based alone on the $K\pi N$ dynamics.

Next we present the antidecuplet spectrum generated with the splitting obtained here. We take the cutoff 800 MeV for reference. Inserting $M_{\Theta_{\overline{10}}} = 1540$ MeV and $M_{\Xi_{\overline{10}}} = 1860$ MeV in Eq. (36), together with our calculated self-energies, we obtain $M_0 = 1670$ MeV and $\Delta = 87.5$ MeV, then

$$\begin{aligned} M_{\Theta_{\overline{10}}} &= 1540 \text{ MeV} \quad (\text{input}), \\ M_{N_{\overline{10}}} &= 1652 \text{ MeV}, \\ M_{\Sigma_{\overline{10}}} &= 1749 \text{ MeV}, \\ M_{\Xi_{\overline{10}}} &= 1860 \text{ MeV} \quad (\text{input}). \end{aligned} \quad (41)$$

The value $3\Delta \sim 260$ MeV is fairly reasonable for our estimate purposes. It would indicate, however, that about 30 MeV of Δ , above the 60 MeV coming from the constituent quark consideration, would come from quark correlations. The large $\Theta_{\overline{10}}$ binding with respect to that of the $N_{\overline{10}}$ state is responsible for the new value $M_{N_{\overline{10}}} = 1652$ MeV, slightly higher than the value we would obtain from an exact GMO rule splitting (1646 MeV), but still far from the 1710 MeV resonance we have assumed for the antidecuplet. As discussed in the introduction, a necessary mixture of an octet representation with the antidecuplet could bring the mass close to that of the $N(1710)$, although the possibility of having a new N^* resonance belonging to the antidecuplet cannot be ruled out [45].

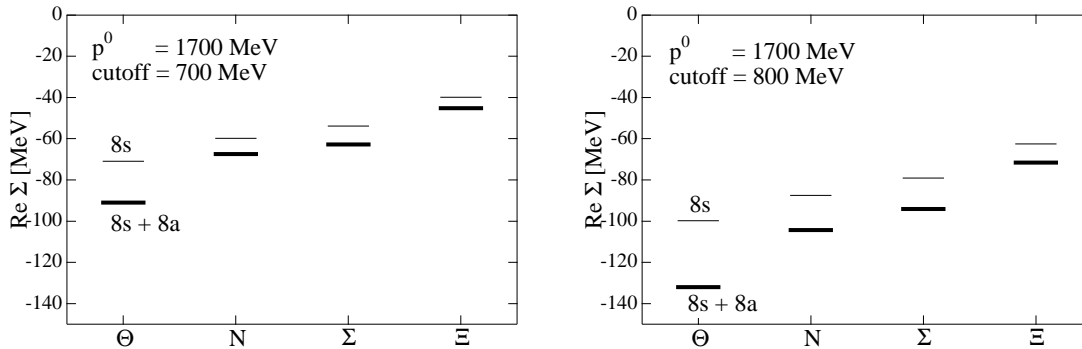


FIG. 4: Mass shifts of baryon antidecuplet ($\text{Re}\Sigma_P$) due to two-meson cloud with $p^0 = 1700$ MeV at two cutoff values. Thin lines represent the results from contributions from \mathcal{L}^{8s} , and thick lines denote the total contribution with \mathcal{L}^{8s} and \mathcal{L}^{8a} .

B. Antidecuplet decay widths from \mathcal{L}^{8s} and \mathcal{L}^{8a}

Now we show the partial decay width obtained according to Eq. (29). As already mentioned, $\Theta(1540)$ has no BMM channel to decay. Among all decay channels, the $N(1710)$ decays broadly into $N\pi\pi$, and it can also decay into $N\pi\eta$. The $\Sigma(1770)$ can decay into $N\bar{K}\pi$, $\Lambda\pi\pi$, and $\Sigma\pi\pi$, and the $\Xi(1860)$ into $\Sigma\bar{K}\pi$ and $\Xi\pi\pi$, because of the threshold energies of BMM channels.

To calculate the decay, since the phase space is essential for the imaginary part, we take the observed masses,

$$M_{N_{\overline{10}}} = 1710, \quad M_{\Sigma_{\overline{10}}} = 1770, \quad M_{\Xi_{\overline{10}}} = 1860. \quad (42)$$

The results appear in Table II. We can see that the widths are not very large for all channels. Among them, we obtain the partial decay widths of the $\Sigma(1770)$ into $\Sigma\pi\pi$ and $N\bar{K}\pi$. When compared with the experimental data, indeed, the $\Sigma(1770)$ would have a total width into two-meson and baryon of about 24 MeV, which is well within the total width of the $\Sigma(1770)$ of about 70 MeV [28]. As to the $\Xi(1860)$ resonance, we obtain a total width of about 2 MeV, which is certainly compatible with the total width less smaller than 18 MeV claimed by the NA49 collaboration [6]. Detailed information of the partial decay widths of these resonances to three-body channels will give us more understanding of the $PBMM$ interaction.

C. Mass shifts and decay widths from \mathcal{L}^X

Here we show the results for the interaction Lagrangian given in Sec. II F, namely the two-meson coupling derived from the chiral symmetric Lagrangian \mathcal{L}^X . We fix the coupling constant g^X from the $N(1710)$ decay to $N\pi\pi$ (s wave, isoscalar), and we find $g^X = 0.218$. Then the antidecuplet mass shifts and decay widths are calculated. However, for the mass shifts, we obtain binding energies that are too large—on the order of several hundreds MeV

TABLE II: Partial decay widths for the allowed channels and total width for any BMM channel, at the masses of the antidecuplet members. All values are in MeV.

Decay widths (MeV)	$\Gamma^{(8s)}$	$\Gamma^{(8a)}$	Γ_{BMM}^{tot}
$N(1710) \rightarrow N\pi\pi$ (inputs)	25	15	40
$N(1710) \rightarrow N\eta\pi$	0.58	-	
$\Sigma(1770) \rightarrow N\bar{K}\pi$	4.7	6.0	24
$\Sigma(1770) \rightarrow \Sigma\pi\pi$	10	0.62	
$\Sigma(1770) \rightarrow \Lambda\pi\pi$	-	2.9	
$\Xi(1860) \rightarrow \Sigma\bar{K}\pi$	0.57	0.46	2.1
$\Xi(1860) \rightarrow \Xi\pi\pi$	-	1.1	

with cutoffs around 700-800 MeV—because the loop integral is more divergent than the previous \mathcal{L}^{8s} case. To reach some reasonable results, we decrease the cutoff, and find that $\Lambda = 525$ MeV would give mass shifts similar to those of \mathcal{L}^{8s} without derivatives.

We compare the mass shifts of \mathcal{L}^X with cutoff 525 MeV and \mathcal{L}^{8s} with 800 MeV in Table III. The decay widths obtained from these Lagrangians are given in Table IV. As expected from the fact that the $C^{(j)}$ coefficients of two Lagrangians are identical, we obtain almost the same mass shifts for \mathcal{L}^X and \mathcal{L}^{8s} by properly adjusting the cutoffs. The decay widths are considered to be in fair agreement qualitatively, when considering that the values span two orders of magnitude. Some quantitative differences would come from the $SU(3)$ breaking in the meson momenta appearing in the \mathcal{L}^X loop, and they are regarded as the uncertainty in our analysis.

D. Effects of \mathcal{L}^{27} and \mathcal{L}^M

Next we draw our attention to the \mathcal{L}^{27} and \mathcal{L}^M Lagrangians, that we have not yet used. First note that it is unrealistic to make these Lagrangians solely responsible for the $N(1710)$ decay width into $N\pi\pi$ (s wave) channel. This would lead to some unphysical results such

TABLE III: Mass shifts of baryon antidecuplet ($\text{Re}\Sigma_P$) due to two-meson cloud with 800 MeV cutoff for \mathcal{L}^{8s} and 525 MeV for \mathcal{L}^χ . All values are in MeV.

Mass shifts (MeV)	\mathcal{L}^{8s}	\mathcal{L}^χ
$\Theta_{\overline{10}}$	-100	-99
$N_{\overline{10}}$	-87	-83
$\Sigma_{\overline{10}}$	-79	-70
$\Xi_{\overline{10}}$	-63	-57

TABLE IV: Partial decay widths for the allowed channels with \mathcal{L}^{8s} and \mathcal{L}^χ , at the masses of the antidecuplet members. All values are in MeV.

Decay widths [MeV]	$\Gamma^{(8s)}$	$\Gamma^{(\chi)}$
$N(1710) \rightarrow N\pi\pi$ (input)	25	25
$N(1710) \rightarrow N\eta\pi$	0.58	0.32
$\Sigma(1770) \rightarrow N\bar{K}\pi$	4.7	4.5
$\Sigma(1770) \rightarrow \Sigma\pi\pi$	10	3.6
$\Xi(1860) \rightarrow \Sigma\bar{K}\pi$	0.57	0.40

as very large decay widths of the $\Xi_{\overline{10}}$ into BMM channels, or a large binding energy of several hundred MeV. Hence, combined with the analyses in the previous section, this fact would justify the approach followed in Ref. [26], where only the \mathcal{L}^{8s} and \mathcal{L}^{8a} terms are taken to study the Θ^+ self-energies in a nuclear medium. Thus, assuming that one cannot have a large fraction of these Lagrangians, we will determine to what extent we can allow the contributions from \mathcal{L}^{27} and \mathcal{L}^M .

We first pursue a model that mixes \mathcal{L}^{8s} and \mathcal{L}^{27} . The coupling constants should be determined such that the decay width of $N_{\overline{10}} \rightarrow N\pi\pi$ (s -wave) is unchanged. According to Table VI, the $C_{B,m_1,m_2}^{(j)}$ coefficients for $N_{\overline{10}} \rightarrow N\pi\pi$ channels are

$$C_{p\pi^0\pi^0}^{8s} = \frac{1}{\sqrt{2}}, \quad C_{p\pi^0\pi^0}^{27} = -\frac{2\sqrt{2}}{5},$$

$$C_{p\pi^+\pi^-}^{8s} = \sqrt{2}, \quad C_{p\pi^+\pi^-}^{27} = -\frac{4\sqrt{2}}{5}.$$

To see the contribution from each Lagrangian clearly, we set $g^{8s} = g^{27} = 1.88$, and take the combination

$$a\mathcal{L}^{8s} + b\mathcal{L}^{27}, \quad b = -\frac{5}{4}(1-a) \quad (43)$$

In this case,

$$C_{p\pi^0\pi^0}^{8s+27} = \frac{1}{\sqrt{2}}a - \frac{2\sqrt{2}}{5} \times \left(-\frac{5}{4}(1-a)\right) = \frac{1}{\sqrt{2}},$$

$$C_{p\pi^+\pi^-}^{8s+27} = \sqrt{2}a - \frac{4\sqrt{2}}{5} \times \left(-\frac{5}{4}(1-a)\right) = \sqrt{2},$$

and, therefore, we have the same $N(1710) \rightarrow N\pi\pi$ (s wave) decay independent of a , but different decays into other channels. With this parametrization, $a = 1$ corresponds to the limit where \mathcal{L}^{27} is switched off, while $a = 0$

relates to the \mathcal{L}^{27} contribution only. We vary a around 1 and find that for $0.90 < a < 1.06$, the self-energy results are acceptable on physical grounds. If we exceed this range, the splitting of the different strangeness states of the antidecuplet spoils agreement with the GMO rule. Taking this range of acceptable values of a into account, we find the results for the binding energies shown in Fig. 5. As we see in the figure, \mathcal{L}^{27} tends to contribute to make the binding energy deeper. A possible contribution from \mathcal{L}^{27} would be considered as a theoretical uncertainty in our analysis.

Next we address the \mathcal{L}^M term. Once again, as in the \mathcal{L}^{27} case, we set $g^{8s} = g^M = 1.88$ and take the combination

$$a\mathcal{L}^{8s} + b\mathcal{L}^M, \quad b = \frac{f^2}{m_\pi^2}(1-a), \quad (44)$$

in order to have the same $N(1710) \rightarrow N\pi\pi$ (s wave). In this case, we also see that the values of $0.76 < a < 1.06$ are acceptable on physical grounds, but larger deviations of a again lead to undesired signs of the splitting between members of the antidecuplet, as well as to unacceptably large results of the binding energies. Within this interval of coupling constant, the results obtained for the binding energies of the antidecuplet members are given in Fig. 6. We observe that \mathcal{L}^M also contributes to attractive binding energy, and the splitting of $\Theta_{\overline{10}}$ and $N_{\overline{10}}$ becomes large compared with the other splittings.

V. DISCUSSION AND CONCLUSION

The assumptions made throughout the paper and the uncertainties in the experimental input make the nature of our analysis qualitative. We assume that the Θ^+ is a $1/2^+$ state with $I = 0$ and that it belongs to an antidecuplet. In addition to these minimal assumptions, we consider that the $N(1710)$ also belongs to this same antidecuplet. The meson cloud mechanism proposed in this work leads, in all different cases studied, to the following conclusions:

1. The two-meson cloud yields an attractive self-energy for all members of the antidecuplet. The observation of attraction is consistent with the previous attempts to describe the Θ^+ as a $K\pi N$ state [18–20, 22].
2. It also contributes to the splitting between antidecuplet members, which is only moderately cutoff dependent and provides about 20% of the total splitting to a stronger effect for reasonable values of the cutoff. The role played by the two-meson cloud is therefore of relevance for a precise understanding of the nature of the Θ^+ and the antidecuplet.
3. The magnitude of 20% is also in agreement quantitatively with the strength of attraction found in the previous study of BMM three-body system [22].

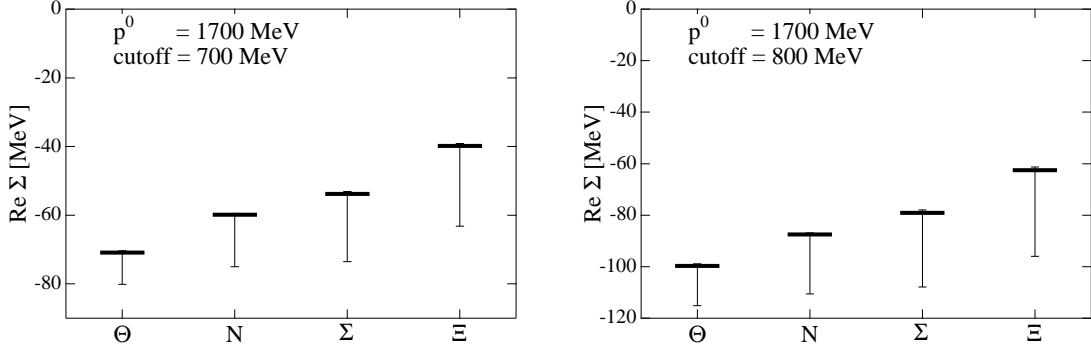


FIG. 5: Mass shifts of baryon antidecuplet due to two-meson cloud from \mathcal{L}^{8s} and possible \mathcal{L}^{27} contributions with two cutoff values. Horizontal bar: results with \mathcal{L}^{8s} only. Vertical bar: band of values including \mathcal{L}^{27} in the range of the text.

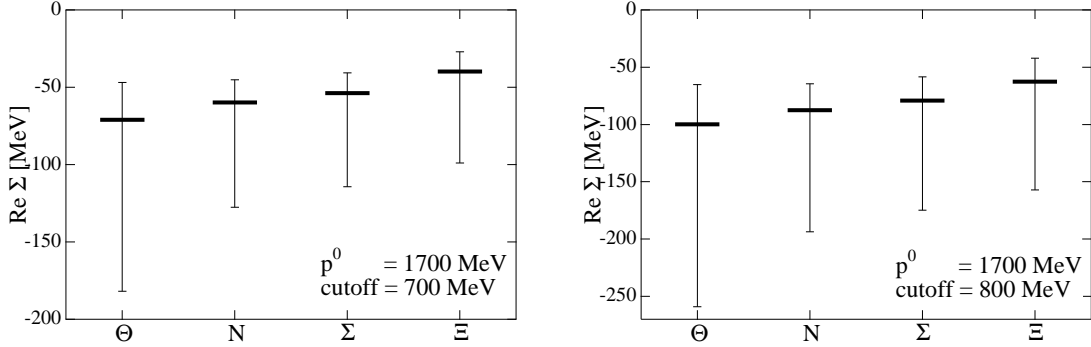


FIG. 6: Mass shifts of baryon antidecuplet due to two-meson cloud from \mathcal{L}^{8s} and possible \mathcal{L}^M contributions with two cutoff values. Horizontal bar: results with \mathcal{L}^{8s} only. Vertical bar: band of values including \mathcal{L}^M in the range of the text.

The values of the mass splitting are such that they still leave some room for quark correlation effects after the GMO mass splitting coming from the mass difference between u , d and s constituent quarks is considered. The contribution to the splitting from the meson cloud is of the same order of magnitude as the one provided by these quark correlations.

4. From the experimental point of view, it is clear that the investigation of the decay channels into two mesons and a baryon of the resonances $N(1710)$, $\Sigma(1770)$, and $\Xi(1860)$ deserves renewed interest.

Acknowledgments

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APPENDIX A: FLAVOR COEFFICIENTS FOR $PBMM$ VERTICES

This appendix contains the flavor coefficients for the tree-level vertices in the three Lagrangians considered. The coefficients for $\Theta_{\overline{10}}$, $N_{\overline{10}}$, $\Sigma_{\overline{10}}$, and $\Xi_{\overline{10}}$ are shown in Tables V, VI, VII, and VIII, respectively.

APPENDIX B: SELF-ENERGY FORMULAE

Below are the formulae for calculating the self-energies as described in Eq. (21). In the isospin symmetric limit,

$$\Sigma_P^{(j)} = \left(F^{(j)}\right)^2 \sum_{\alpha} I^{(j)}(\alpha) D_{P,\alpha}^{(j)}, \quad (\text{B1})$$

with α being the BMM channel in the isospin basis, such as $NK\pi$, $NK\eta$, etc., and $D^{(j)}$ are expressed as the sum of the $(C^{(j)})^2$. In Table IX–XII, we show the $D^{(j)}$ coefficients. For the 27 and M cases, following the procedure in Sec. IV D, we set $g^{8s} = g^{27} = g^M = 1.88$ and take

$$a\mathcal{L}^{8s} + b\mathcal{L}^{27}, \quad b = -\frac{5}{4}(1-a) \quad (\text{B2})$$

TABLE V: The $C_{B,m_1,m_2}^{(j)}$ flavor coefficients for the vertex with Θ_{10}^+ , octet baryons, and two octet mesons.

P	BMM	$8s$	$8a$	27	M
Θ_{10}^+	$pK^+\pi^-$	$-\sqrt{6}$	$-\sqrt{6}$	$\frac{4\sqrt{6}}{5}$	$-\sqrt{6}\frac{m_K^2+m_\pi^2}{2f^2}$
	$pK^0\pi^0$	$\sqrt{3}$	$\sqrt{3}$	$-\frac{4\sqrt{3}}{5}$	$\sqrt{3}\frac{m_K^2+m_\pi^2}{2f^2}$
	$pK^0\eta$	1	-3	$\frac{36}{5}$	$\frac{5m_K^2-3m_\pi^2}{2f^2}$
	$nK^+\pi^0$	$\sqrt{3}$	$\sqrt{3}$	$-\frac{4\sqrt{3}}{5}$	$\sqrt{3}\frac{m_K^2+m_\pi^2}{2f^2}$
	$nK^+\eta$	-1	3	$-\frac{36}{5}$	$-\frac{5m_K^2-3m_\pi^2}{2f^2}$
	$nK^0\pi^+$	$\sqrt{6}$	$\sqrt{6}$	$-\frac{4\sqrt{6}}{5}$	$\sqrt{6}\frac{m_K^2+m_\pi^2}{2f^2}$
	$\Sigma^+K^0K^0$	$-$	$-$	$-4\sqrt{6}$	$-$
	$\Sigma^0K^0K^+$	$-$	$-$	$-8\sqrt{3}$	$-$
	$\Sigma^-K^+K^+$	$-$	$-$	$4\sqrt{6}$	$-$

TABLE VI: The $C_{B,m_1,m_2}^{(j)}$ flavor coefficients for the vertex with N_{10}^+ , octet baryons, and two octet mesons. Coefficients for N_{10}^0 are obtained by using isospin symmetry.

P	BMM	$8s$	$8a$	27	M
N_{10}^+	pK^+K^-	$-\sqrt{2}$	$-\sqrt{2}$	$\frac{4\sqrt{2}}{5}$	$-\sqrt{2}\frac{m_K^2}{f^2}$
	$pK^0\bar{K}^0$	$-$	$-2\sqrt{2}$	$4\sqrt{2}$	$-$
	$p\pi^0\pi^0$	$\frac{1}{\sqrt{2}}$	$-$	$-\frac{2\sqrt{2}}{5}$	$\frac{1}{\sqrt{2}}\frac{m_\pi^2}{f^2}$
	$p\pi^+\pi^-$	$\sqrt{2}$	$\sqrt{2}$	$-\frac{4\sqrt{2}}{5}$	$\sqrt{2}\frac{m_\pi^2}{f^2}$
	$p\eta\eta$	$-\frac{1}{\sqrt{2}}$	$-$	$-\frac{18\sqrt{2}}{5}$	$-\frac{1}{\sqrt{2}}\frac{8m_K^2-5m_\pi^2}{3f^2}$
	$p\eta\pi^0$	$-\sqrt{\frac{2}{3}}$	$-$	$\frac{8\sqrt{6}}{5}$	$-\sqrt{\frac{2}{3}}\frac{m_\pi^2}{f^2}$
	$n\bar{K}^0K^+$	$-\sqrt{2}$	$-\sqrt{2}$	$-\frac{16\sqrt{2}}{5}$	$-\sqrt{2}\frac{m_K^2}{f^2}$
	$n\pi^+\eta$	$-\frac{2}{\sqrt{3}}$	$-$	$\frac{16\sqrt{3}}{5}$	$-\frac{2}{\sqrt{3}}\frac{m_\pi^2}{f^2}$
	$n\pi^+\pi^0$	$-$	-2	$-$	$-$
	$\Lambda K^+\pi^0$	$-\sqrt{\frac{3}{2}}$	$-\sqrt{\frac{3}{2}}$	$\frac{2\sqrt{6}}{5}$	$-\sqrt{\frac{3}{2}}\frac{m_K^2+m_\pi^2}{2f^2}$
	$\Lambda K^+\eta$	$\frac{1}{\sqrt{2}}$	$-\frac{3}{\sqrt{2}}$	$\frac{18\sqrt{2}}{5}$	$\frac{1}{\sqrt{2}}\frac{5m_K^2-3m_\pi^2}{2f^2}$
	$\Lambda K^0\pi^+$	$-\sqrt{3}$	$-\sqrt{3}$	$\frac{4\sqrt{3}}{5}$	$-\sqrt{3}\frac{m_K^2+m_\pi^2}{2f^2}$
	$\Sigma^+K^+\pi^-$	$\sqrt{2}$	$\sqrt{2}$	$-\frac{4\sqrt{2}}{5}$	$\sqrt{2}\frac{m_K^2+m_\pi^2}{2f^2}$
	$\Sigma^+K^0\eta$	$-\frac{1}{\sqrt{3}}$	$\sqrt{3}$	$\frac{28\sqrt{3}}{5}$	$-\frac{1}{\sqrt{3}}\frac{5m_K^2-3m_\pi^2}{2f^2}$
	$\Sigma^+K^0\pi^0$	-1	-1	$-\frac{36}{5}$	$-\frac{m_K^2+m_\pi^2}{2f^2}$
	$\Sigma^0K^+\pi^0$	$\frac{1}{\sqrt{2}}$	$\frac{1}{\sqrt{2}}$	$-\frac{22\sqrt{2}}{5}$	$\frac{1}{\sqrt{2}}\frac{m_K^2+m_\pi^2}{2f^2}$
	$\Sigma^0K^0\pi^+$	1	1	$\frac{36}{5}$	$\frac{m_K^2+m_\pi^2}{2f^2}$
	$\Sigma^0K^+\eta$	$-\frac{1}{\sqrt{6}}$	$\sqrt{\frac{3}{2}}$	$\frac{14\sqrt{6}}{5}$	$-\frac{1}{\sqrt{6}}\frac{5m_K^2-3m_\pi^2}{2f^2}$
	$\Sigma^-K^+\pi^+$	$-$	$-$	$-8\sqrt{2}$	$-$
	$\Xi^-K^+K^+$	$-$	$-$	$4\sqrt{2}$	$-$
	$\Xi^0K^+K^0$	$-$	$-$	$4\sqrt{2}$	$-$

and

$$a\mathcal{L}^{8s} + b\mathcal{L}^M, \quad b = \frac{f^2}{m_\pi^2}(1-a), \quad (\text{B3})$$

TABLE VII: The $C_{B,m_1,m_2}^{(j)}$ flavor coefficients for the vertex with Σ_{10}^+ , octet baryons, and two octet mesons. Coefficients for Σ_{10}^0 and Σ_{10}^- are obtained by using isospin symmetry.

P	BMM	$8s$	$8a$	27	M
Σ_{10}^+	$p\pi^+K^-$	$-\sqrt{2}$	$-\sqrt{2}$	$\frac{4\sqrt{2}}{5}$	$-\sqrt{2}\frac{m_K^2+m_\pi^2}{2f^2}$
	$p\pi^0\bar{K}^0$	1	1	$-\frac{24}{5}$	$\frac{m_K^2+m_\pi^2}{2f^2}$
	$p\bar{K}^0\eta$	$\frac{1}{\sqrt{3}}$	$\sqrt{3}$	$\frac{32\sqrt{3}}{5}$	$\frac{1}{\sqrt{3}}\frac{5m_K^2-3m_\pi^2}{2f^2}$
	$n\bar{K}^0\pi^+$	$-$	$-$	$-4\sqrt{2}$	$-$
	$\Lambda\bar{K}^0K^+$	$-\sqrt{3}$	$-\sqrt{3}$	$-\frac{16\sqrt{3}}{5}$	$-\sqrt{3}\frac{m_K^2}{f^2}$
	$\Lambda\pi^+\eta$	$-\sqrt{2}$	$-$	$\frac{24\sqrt{2}}{5}$	$-\sqrt{2}\frac{m_\pi^2}{f^2}$
	$\Lambda\pi^+\pi^0$	$-$	$-\sqrt{6}$	$-$	$-$
	$\Sigma^+K^+K^-$	$-\sqrt{2}$	$-\sqrt{2}$	$\frac{4\sqrt{2}}{5}$	$-\sqrt{2}\frac{m_K^2}{f^2}$
	$\Sigma^+\pi^+\pi^-$	$\sqrt{2}$	$\sqrt{2}$	$-\frac{4\sqrt{2}}{5}$	$\sqrt{2}\frac{m_\pi^2}{f^2}$
	$\Sigma^+\eta\eta$	$-\frac{1}{\sqrt{2}}$	$-$	$\frac{12\sqrt{2}}{5}$	$-\frac{1}{\sqrt{2}}\frac{8m_K^2-5m_\pi^2}{3f^2}$
	$\Sigma^+\eta\pi^0$	$-\sqrt{\frac{2}{3}}$	$-$	$-\frac{12\sqrt{6}}{5}$	$-\sqrt{\frac{2}{3}}\frac{m_\pi^2}{f^2}$
	$\Sigma^+\pi^0\pi^0$	$\frac{1}{\sqrt{2}}$	$-$	$\frac{8\sqrt{2}}{5}$	$\frac{1}{\sqrt{2}}\frac{m_\pi^2}{f^2}$
	$\Sigma^+K^0\bar{K}^0$	$-$	$-2\sqrt{2}$	$-4\sqrt{2}$	$-$
	$\Sigma^0\bar{K}^0K^+$	1	1	$-\frac{24}{5}$	$\frac{m_K^2}{f^2}$
	$\Sigma^0\eta\pi^+$	$\sqrt{\frac{2}{3}}$	$-$	$\frac{12\sqrt{6}}{5}$	$\sqrt{\frac{2}{3}}\frac{m_\pi^2}{f^2}$
	$\Sigma^0\pi^+\pi^0$	$-$	$\sqrt{2}$	$-4\sqrt{2}$	$-$
	$\Sigma^-\pi^+\pi^+$	$-$	$-$	$-4\sqrt{2}$	$-$
	$\Xi^0K^+\pi^0$	1	1	$-\frac{24}{5}$	$\frac{m_K^2+m_\pi^2}{2f^2}$
	$\Xi^0K^0\pi^+$	$\sqrt{2}$	$\sqrt{2}$	$\frac{16\sqrt{2}}{5}$	$\sqrt{2}\frac{m_K^2+m_\pi^2}{2f^2}$
	$\Xi^0K^+\eta$	$-\frac{1}{\sqrt{3}}$	$-\sqrt{3}$	$\frac{8\sqrt{3}}{5}$	$-\frac{1}{\sqrt{3}}\frac{5m_K^2-3m_\pi^2}{2f^2}$
	$\Xi^-K^+\pi^+$	$-$	$-$	$8\sqrt{2}$	$-$

In these cases, D^j are defined as

$$\Sigma_P^{(j)} = \left(F^{(8s)}\right)^2 \sum_\alpha I^{(j)}(\alpha) D_{P,\alpha}^{(j)}, \quad (\text{B4})$$

for $(j) = 8s+27, 8s+M$. One can easily check that when $a = 1, b = 0, D_{P,\alpha}^{(j)}$ for $(j) = 8s+27, 8s+M$ becomes $D_{P,\alpha}^{(8s)}$.

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TABLE VIII: The $C_{B,m_1,m_2}^{(j)}$ flavor coefficients for the vertex with Ξ_{10}^+ , octet baryons, and two octet mesons. Coefficients for Ξ_{10}^0 , Ξ_{10}^- and Ξ_{10}^{--} are obtained by using isospin symmetry.

P	BMM	$8s$	$8a$	27	M
Ξ_{10}^+	$\Sigma^+\pi^+K^-$	$-\sqrt{6}$	$-\sqrt{6}$	$\frac{4\sqrt{6}}{5}$	$-\sqrt{6}\frac{m_K^2+m_\pi^2}{2f^2}$
	$\Sigma^+\pi^0\bar{K}^0$	$\sqrt{3}$	$\sqrt{3}$	$\frac{16\sqrt{3}}{5}$	$\sqrt{3}\frac{m_K^2+m_\pi^2}{2f^2}$
	$\Sigma^+\bar{K}^0\eta$	1	3	$-\frac{24}{5}$	$\frac{5m_K^2-3m_\pi^2}{2f^2}$
	$\Sigma^0\bar{K}^0\pi^+$	-	-	$-4\sqrt{3}$	-
	$\Lambda\bar{K}^0\pi^+$	-	-	-12	-
	$p\bar{K}^0\bar{K}^0$	-	-	$-4\sqrt{6}$	-
	$\Xi^0\bar{K}^0K^+$	$\sqrt{6}$	$\sqrt{6}$	$-\frac{4\sqrt{6}}{5}$	$\sqrt{6}\frac{m_K^2}{f^2}$
	$\Xi^0\eta\pi^+$	2	-	$\frac{12}{5}$	$2\frac{m_\pi^2}{f^2}$
	$\Xi^0\pi^+\pi^0$	-	$2\sqrt{3}$	$-4\sqrt{3}$	-
	$\Xi^-\pi^+\pi^+$	-	-	$4\sqrt{6}$	-

TABLE IX: The $D_\alpha^{(j)}$ coefficients for the Θ_{10} self-energies.

P	α	$8s$	$8a$	$8s+27$	$8s+M$
Θ_{10}	$NK\pi$	18	18	18	$18(a + \frac{m_K^2+m_\pi^2}{2f^2}b)^2$
	$NK\eta$	2	18	$2(a + \frac{36}{5}b)^2$	$2(a + \frac{5m_K^2-3m_\pi^2}{2f^2}b)^2$
	$\Sigma K\pi$	-	-	$576b^2$	-

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TABLE X: The $D_\alpha^{(j)}$ coefficients for the N_{10} self-energies.

P	α	$8s$	$8a$	$8s+27$	$8s+M$
N_{10}	$NK\bar{K}$	4	12	$2+2(a+\frac{16}{5}b)^2-32b^2$	$4(a+\frac{m_K^2}{f^2}b)^2$
	$N\pi\pi$	3	6	3	$3(a+\frac{m_\pi^2}{f^2}b)^2$
	$N\pi\eta$	2	-	$2(-a+\frac{24}{5}b)^2$	$2(a+\frac{m_\pi^2}{f^2}b)^2$
	$N\eta\eta$	1	-	$(a+\frac{36}{5})^2$	$(a+\frac{8m_K^2-5m_\pi^2}{3f^2}b)^2$
	$\Lambda K\pi$	$\frac{9}{2}$	$\frac{9}{2}$	$\frac{9}{2}$	$\frac{9}{2}(a+\frac{m_K^2+m_\pi^2}{2f^2}b)^2$
	$\Lambda K\eta$	$\frac{1}{2}$	$\frac{9}{2}$	$\frac{1}{2}(a+\frac{36}{5})^2$	$\frac{1}{2}(a+\frac{5m_K^2-3m_\pi^2}{2f^2}b)^2$
	$\Sigma K\pi$	$\frac{9}{2}$	$\frac{9}{2}$	$2+2(a+\frac{36}{5}b)^2+\frac{1}{2}(a-\frac{44}{5})^2+128b^2$	$(a+\frac{m_K^2+m_\pi^2}{2f^2}b)^2$
	$\Sigma K\eta$	$\frac{1}{2}$	$\frac{9}{2}$	$\frac{1}{2}(-a+\frac{84}{5})^2$	$\frac{1}{2}(a+\frac{5m_K^2-3m_\pi^2}{2f^2}b)^2$
	ΞKK	-	-	$96b^2$	-

TABLE XI: The $D_\alpha^{(j)}$ coefficients for the Σ_{10} self-energies.

P	α	$8s$	$8a$	$8s+27$	$8s+M$
Σ_{10}	$N\bar{K}\pi$	3	3	$2+(a-\frac{24}{5}b)^2+32b^2$	$3(a+\frac{m_K^2+m_\pi^2}{2f^2}b)^2$
	$N\bar{K}\eta$	$\frac{1}{3}$	3	$\frac{1}{3}(a+\frac{96}{5}b)^2$	$\frac{1}{3}(a+\frac{5m_K^2-3m_\pi^2}{2f^2}b)^2$
	$\Lambda K\bar{K}$	3	3	$3(a+\frac{16}{5}b)^2$	$3(a+\frac{m_K^2}{f^2}b)^2$
	$\Lambda\pi\eta$	2	-	$2(a-\frac{24}{5}b)^2$	$2(a+\frac{m_\pi^2}{f^2}b)^2$
	$\Lambda\pi\pi$	-	6	-	-
	$\Sigma K\bar{K}$	3	11	$2+(a-\frac{24}{5}b)^2+32b^2$	$3(a+\frac{m_K^2}{f^2}b)^2$
	$\Sigma\pi\pi$	3	4	$2+(a+\frac{16}{5}b)^2+96b^2$	$(a+\frac{m_\pi^2}{f^2}b)^2$
	$\Sigma\pi\eta$	$\frac{4}{3}$	-	$\frac{4}{3}(a+\frac{36}{5}b)^2$	$\frac{4}{3}(a+\frac{m_\pi^2}{f^2}b)^2$
	$\Sigma\eta\eta$	1	-	$(a-\frac{24}{5}b)^2$	$(a+\frac{8m_K^2-5m_\pi^2}{3f^2}b)^2$
	$\Xi K\pi$	3	3	$2(a+\frac{16}{5}b)^2+(a-\frac{24}{5}b)^2+128b^2$	$3(a+\frac{m_K^2+m_\pi^2}{2f^2}b)^2$
	$\Xi K\eta$	$\frac{1}{3}$	3	$\frac{1}{3}(a-\frac{24}{5}b)^2$	$\frac{1}{3}(a+\frac{5m_K^2-3m_\pi^2}{2f^2}b)^2$

TABLE XII: The $D_\alpha^{(j)}$ coefficients for the Ξ_{10} self-energies.

P	α	$8s$	$8a$	$8s+27$	$8s+M$
Ξ_{10}	$\Sigma\bar{K}\pi$	9	9	$6+3(a+\frac{16}{5}b)^2+48b^2$	$9(a+\frac{m_K^2+m_\pi^2}{2f^2}b)^2$
	$\Sigma\bar{K}\eta$	1	9	$(a-\frac{24}{5}b)^2$	$(a+\frac{5m_K^2-3m_\pi^2}{2f^2}b)^2$
	$\Xi K\bar{K}$	6	6	6	$6(a+\frac{m_K^2}{f^2}b)^2$
	$\Xi\pi\eta$	4	-	$4(a+\frac{6}{5}b)^2$	$4(a+\frac{m_\pi^2}{f^2}b)^2$
	$\Xi\pi\pi$	-	12	$240b^2$	-
	$\Lambda\bar{K}\pi$	-	-	$144b^2$	-
	$N\bar{K}\bar{K}$	-	-	$192b^2$	-

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