

Heavy Quark Spin Symmetry and SU(3)-Flavour Partners of the X(3872)

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Abstract

In this work, an Effective Field Theory (EFT) incorporating light SU(3)-flavour and heavy quark spin symmetry is used to describe charmed meson-antimeson bound states. At Lowest Order (LO), this means that only contact range interactions among the heavy meson and antimeson fields are involved. Besides, the isospin violating decays of the X(3872) will be used to constrain the interaction between the D and a \bar{D}^* mesons in the isovector channel. Finally, assuming that the X(3915) and Y(4140) resonances are $D^*\bar{D}^*$ and $D_s^*\bar{D}_s^*$ molecular states, we can determine the four Low Energy Constants (LECs) of the EFT that appear at LO and, therefore, the full spectrum of molecular states with isospin $I = 0, \frac{1}{2}$ and 1.

Keywords: Heavy Quark Spin and Flavour Symmetries, Hidden charm molecules, XYZ states.

1. Introduction

Since the discovery of the X(3872) resonance [1], many theoretical approaches have been used trying to describe it. Even though it contains a $c\bar{c}$ pair, it does not seem to fit in the charmonium spectrum. Because of that disagreement, other more exotic proposals have been made. Among these, the interpretation of the X(3872) as a hadronic molecule is the most likely so far. Within this assumption, the X(3872) would be a bound state of both a charm meson and antimeson. However, this hypothesis strongly depends on the J^{PC} quantum numbers of the resonance, which have not been experimentally established. They are either 1^{++} or 2^{-+} (analysis done in Ref. [2]), of which only 1^{++} is compatible with a low-lying S-wave hadronic molecule.

Apart from the X(3872), many other experimental hidden charm resonances have been observed: the XYZ states. Many of these states can be new candidates for heavy meson-antimeson molecules.

These resonances are near their threshold. This means that the meson and the antimeson are not so close to be sensitive to find the details of the interaction at short distances. So, both of them are preserving their individuality and will not probe the specific details of the short range interaction responsible of their binding. Hence, a scale separation exists and the interaction between these two mesons can be described by different EFT's [3, 4]. Besides, the presence of a heavy quark in the heavy mesons imposes that our EFT should be consistent with Heavy Quark Spin Symmetry (HQSS), which implies certain constraints to the heavy meson-antimeson interaction [5]. On the other hand, the light quark content of the heavy mesons ($q = u, d, s$ in this work) imposes SU(3) flavour symmetry and, because of that, molecular states should be classified into SU(3) multiplets.

As a consequence of the symmetries discussed (HQSS and SU(3)) flavour symmetry) only four parameters are enough to describe the molecular states at leading order in the EFT we use. That is, we need four data points to predict the full molecular spectrum. For this purpose we will assume the molecular nature of certain XYZ states such as the X(3872), X(3915) and Y(4140) and the fourth assumption will be derived from the analysis of the isospin violating branching ratio of the X(3872) decays into $J/\psi\omega$ and $J/\psi\rho$.

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2. The EFT Description at Lowest Order

In this section, the EFT used in this work to describe the heavy meson molecules is briefly presented. The EFT description must involve pions

and heavy meson/antimeson fields and local interactions among these degrees of freedom that are compatible with the known low energy symmetries, most notably HQSS and chiral symmetry. Nevertheless, according to [6]: pion exchanges are weaker than naively expected and only enter as a perturbation at subleading orders. Similarly, coupled channel effects turn out to be also sufficiently small to be ignored at LO. Hence, at LO, the EFT consists of heavy mesons and antimesons interacting through a contact range potential, similar to the one in [5]. Then, once we have determined our potential, the wave functions and observables will be calculated in the standard quantum mechanical fashion. For example, we can generate bound states by iterating the EFT potential in the Schrödinger / Lippmann-Schwinger equation, as previously done in [6]. See details in [7].

3. Isospin Symmetry Violation in the $X(3872)$

The first step is to solve the bound state equation for the $X(3872)$. We consider that the $X(3872)$ is a $D\bar{D}^*$ molecule with quantum numbers $J^{PC} = 1^{++}$, where we distinguish between the neutral ($D^0\bar{D}^{*0}$) and charged (D^+D^{*-}) components of the wave function. That is, there are two channels in the bound state equation. And we will regularize the LO potential (here, and in the following cases when not specified) with a Gaussian regulator function with a cut-off Λ varying in the 0.5 – 1.0 GeV range.

Moreover, the Belle collaboration reported the decays of the $X(3872)$ into the (isoscalar) $J/\Psi\pi^+\pi^-\pi^0$ and the (isovector) $J/\Psi\pi^+\pi^-$ channels. The latest measurements yield to the isospin violating ratio [8]:

$$\mathcal{B}_X = \frac{\Gamma(X(3872) \rightarrow J/\Psi \pi^+\pi^-\pi^0)}{\Gamma(X(3872) \rightarrow J/\Psi \pi^+\pi^-)} = 0.8 \pm 0.3$$

which is difficult to accommodate from the theoretical point of view.

In this work, we will assume that this isospin violation is caused by the isospin breaking generated by the mass difference of the neutral ($D^0\bar{D}^{*0}$) and charged (D^+D^{*-}) channels in the $X(3872)$, which would not have a definite isospin. In this picture, at short $D\bar{D}^*$ distances, the $X(3872)$ would be a linear combination of $I = 0$ and $I = 1$ components whilst the $J/\Psi 3\pi$ and $J/\Psi 2\pi$ decays would be described

by an isospin invariant coupling via an intermediate ρ and ω meson (as suggested in [9]).

The analysis performed by Hanhart et al. in [2], leads to the following branching ratio

$$R_X = \frac{\mathcal{M}(X \rightarrow J/\Psi \rho)}{\mathcal{M}(X \rightarrow J/\Psi \omega)} = 0.26_{-0.05}^{+0.08}, \quad (2)$$

where \mathcal{B}_X is translated into a ratio of the decay amplitudes of the $X(3872)$ instead of its corresponding decay widths. In our model, this ratio R_X can be rewritten as (details in [7])

$$R_X = \frac{g_\rho}{g_\omega} \frac{\hat{\Psi}_{X0} - \hat{\Psi}_{X1}}{\hat{\Psi}_{X0} + \hat{\Psi}_{X1}}, \quad (3)$$

being $g_V = \mathcal{M}_V[D\bar{D}^*(I = 0, 1) \rightarrow J/\Psi V]$ with $V = \rho/\omega$ and $\hat{\Psi}_{X0}$ y $\hat{\Psi}_{X1}$ an average of the neutral and charged $D^*\bar{D}$ wave function components in the vicinities of the origin.

So, with the experimental determination of R_X and the binding energy of the $X(3872)$ we could determine the contact range potential that binds the $X(3872)$ if we knew the g_ρ/g_ω ratio,. But the g_ρ/g_ω ratio can be determined from the SU(3) relation $g_\rho - g_\omega = -\sqrt{2}g_\phi$, and, as the OZI (the strange quark pair creation is suppressed) rule implies $g_\rho, g_\omega \gg g_\phi$, that is, we are ignoring the $X(3872)$ decay into $J/\psi\phi$. Thus, we can approximately consider $g_\rho/g_\omega \simeq 1$, so the R_X ratio in our model is

$$R_X = \frac{\hat{\Psi}_{X0} - \hat{\Psi}_{X1}}{\hat{\Psi}_{X0} + \hat{\Psi}_{X1}}, \quad (4)$$

which only depends on the wave function components in the vicinities of the origin.

4. The SU(3) and HQSS Partners of the $X(3872)$

If we determine the value of the counterterms of the LO EFT, we will be able to calculate the location of the molecular partners of the $X(3872)$.

There are four unknown LEC's. We fix two of them from the location of the $X(3872)$ resonance and its isospin breaking branching ratio, as explained in the previous section. The remaining two require the identification of two partners of the $X(3872)$: the $X(3915)$ as a $0^{++} D^*\bar{D}^*$ molecule and the $Y(4140)$ as a $0^{++} D_s^*\bar{D}_s^*$ molecule, guided by its apparently dominant decay into $J/\Psi\phi$.

Apart from the R_X errors, there is an extra error source which has to be taken into account: the approximate nature of HQSS. In this EFT, we expand

J^{PC}	$\text{H}\bar{\text{H}}$	E ($\Lambda = 0.5$ GeV)	E ($\Lambda = 1$ GeV)
0^{++}	$D\bar{D}$	3709 ± 10	3715^{+12}_{-15}
1^{++}	$D^*\bar{D}$	Input	Input
1^{+-}	$D^*\bar{D}$	3815 ± 17	3821^{+23}_{-26}
0^{++}	$D^*\bar{D}^*$	Input	Input
1^{+-}	$D^*\bar{D}^*$	3955 ± 17	3958^{+24}_{-27}
2^{++}	$D^*\bar{D}^*$	$4013^{+\dagger}_{-9}$	$4013^{+\dagger}_{-12}$

Table 1: Predicted masses (in MeV) of the SU(2) isoscalar HQSS partners of the $X(3872)$ resonance for two different values of the Gaussian cutoff. Errors in the predicted masses are obtained by adding in quadratures the uncertainties stemming from the two sources of systematic errors discussed at the end in Subsect. 4. $\dagger\dagger$: see discussion in [7]

J^{PC}	$\text{H}\bar{\text{H}}$	E ($\Lambda = 0.5$ GeV)	E ($\Lambda = 1$ GeV)
0^+	$D_s^+\bar{D}^-$	$3835.8^{+2.3}_{-3.9}$	$3837.7^{+0.4}_{-4.3}$
1^+	$D_s\bar{D}^*$	3949 ± 13	3957^{+14}_{-19}
0^+	$D_s^*\bar{D}^*$	4056 ± 22	4061^{+29}_{-33}
1^+	$D_s^*\bar{D}^*$	4091^{+13}_{-14}	4097^{+15}_{-20}
2^+	$D_s^*\bar{D}^*$	—	—

Table 2: Predicted masses (in MeV) of the isospinor ($I = \frac{1}{2}$) HQSS partners of the $X(3872)$ resonance, for two different values of the Gaussian cutoff. The meaning of the quoted errors in the table is the same as in Table 1.

the QCD lagrangian into powers of (Λ_{QCD}/m_Q) so that

$$V_{(m_Q=m_c)}^{\text{LO}} = V_{(m_Q \rightarrow \infty)}^{\text{LO}} \left(1 \pm \frac{\Lambda_{QCD}}{m_c}\right), \quad (5)$$

Taking an approximate value of $m_c \simeq 1.5$ GeV for the charm quark mass and $\Lambda_{QCD} \sim 200$ MeV, we should expect a 15% violation of HQSS for the LO contact range potentials. Since the two error sources are independent, the total error will be computed by adding in quadratures the partial errors.

4.1. The SU(2) Isoscalar ($I = 0$) Partners

In this sector the hidden strange components are ignored. We do not take into account particle coupled channel effects as they are subleading unless the mass gap between the neutral and charged channels is similar in size to the binding energy in the isospin symmetric limit. Thus, in the 1^{++} and 2^{++} channels, we are using a coupled channel potential. The analysis of this sector was previously done in Ref. [6] without including strangeness into the analysis (SU(2) light quark flavour symmetry) and, as there is almost no difference in the resonances predicted, we conclude that the effect of the isospin violation and the inclusion of the quark s must be small. The spectrum of molecular states is presented in Table 1.

4.2. The Isospinor ($I = \frac{1}{2}$) Partners

In this sector, the C-parity of the molecules is not well defined, as they are not bound states of a heavy meson and its antimeson. However, the formalism is identical to the one in the previous case,

except for the $1^+ D_s\bar{D}^*$ and DD_s^* molecules. The $D_s\bar{D}^*$ and DD_s^* thresholds are separated by only 2 MeV and require a coupled channel treatment. In this case, we obtain just one single bound state. This resonance and its other isospinor partners are shown in Table 2, where we have considered only the strangeness one states (it would be the same for strangeness $S = -1$).

4.3. The Isovector ($I = 1$) Partners

The potential in the isovector and isospinor sector is the same (except in the 1^{++} and 2^{++} molecules owing to the isospin violation). For this reason, the spectrum in the isovector sector would be similar to the isospinor one. The four molecular states obtained are listed in Table 3. The other two possible states correspond to the isovector partners of the $X(3872)$ and $X(4012)$ resonances where a single bound state is obtained.

4.4. The Hidden Strange Partners

In this sector, the resonances must also contain a $s\bar{s}$ quark-antiquark pair. The potential derived for this latter case is the arithmetic mean of the isoscalar and isovector one. So if there was a bound state in the isoscalar and isovector sector, there would probably exist its hidden strange partner. On the other hand, considering that the $X(3872)$ and $X(4012)$ molecules have no isovector partners, it is very likely that there will not be hidden strange partners either with those quantum numbers. Therefore, the four states obtained are listed in Table 4.

J^{PC}	H \bar{H}	E ($\Lambda = 0.5$ GeV)	E ($\Lambda = 1$ GeV)
0^{++}	$D^+ \bar{D}^0$	$3732.5^{+2.0}_{-3.9}$	$3734.3^{+0.1}_{-3.6}$
1^{++}	$D^* \bar{D}$	—	—
1^{+-}	$D^* \bar{D}$	3848^{+12}_{-11}	3857^{+13}_{-18}
0^{++}	$D^* \bar{D}^*$	3953 ± 22	3960^{+28}_{-32}
1^{+-}	$D^* \bar{D}^*$	3988 ± 13	3995^{+14}_{-19}
2^{++}	$D^* \bar{D}^*$	—	—

Table 3: Predicted masses (in MeV) of the SU(2) isovector HQSS partners of the $X(3872)$ resonance for two different values of the Gaussian cutoff. The meaning of the quoted errors in the table is the same as in Table 1.

J^{PC}	H \bar{H}	E ($\Lambda = 0.5$ GeV)	E ($\Lambda = 1$ GeV)
0^{++}	$D_s \bar{D}_s$	3924^{+6}_{-7}	3928^{+7}_{-11}
1^{++}	$D_s^* \bar{D}_s$	—	—
1^{+-}	$D_s^* \bar{D}_s$	4035 ± 15	4040^{+20}_{-24}
0^{++}	$D_s^* \bar{D}_s^*$	Input	Input
1^{+-}	$D_s^* \bar{D}_s^*$	4177 ± 16	4180^{+21}_{-24}
2^{++}	$D_s^* \bar{D}_s^*$	—	—

Table 4: Predicted masses (in MeV) of the hidden strange isoscalar HQSS partners of the $X(3872)$ resonance for two different values of the Gaussian cutoff. The meaning of the quoted errors is the same as in Table 1.

5. Conclusions

As a summary, we have established the location of 15 molecular partners of the $X(3915)$, $Y(4140)$ and $X(3872)$ states using HQSS and SU(3) flavour symmetry, see Tables 1-4. These predictions have a series of uncertainties, being the most important the approximate nature of HQSS. According to the estimations of these uncertainties, the spectrum of these states should be stable but their location can vary up to a few tens of MeV in certain cases.

However, the family of $D^{(*)} \bar{D}^{(*)}$ states we theorize depends on the assumptions we made: the molecular description of the $X(3872)$, $X(3915)$ and $Y(4140)$ resonances. Whilst there is a consensus on the molecular nature of the $X(3872)$ resonance, and its existence is well established, the situation for the $X(3915)$ and $Y(4140)$ are more dubious. Thus not all the predictions are probable alike. Predictions derived from the $X(3872)$ are supposed to be more solid than those depending on the $X(3915)$, which in turn are less hypothetical than the ones obtained from the $Y(4140)$. In this sense, as mentioned in Ref. [6] too, the $2^{++} D^* \bar{D}^*$ isoscalar partner of the $X(3872)$ is still the most reliable prediction of the present work. So, if any new analysis of the XYZ resonances provides us with a better molecular candidate than one of our assumptions, it can easily be included in this scheme. Thus, we will be able to replace one of the doubtful molecular states we have assumed with this new resonance so the new predictions are more robust. On the other way, if eventually any of the predictions we have established is detected, it could be a proof to the molecular nature of these resonances.

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