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Amplitude-Probability Distributions for Atmospheric Radio Noise



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Amplitude-Probability Distributions for Atmospheric Radio Noise

W. Q. Crichlow, A. D. Spaulding, C. J. Roubique, and R. T. Disney



National Bureau of Standards Monograph 23

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Contents

		Page
1.	Introduction.	. 1
2.	References	_ 2
3.	Appendix	. 15
	1. Introduction	. 15
	2. Measurements of the amplitude-probability distribution	. 15
	3. Definition of parameters and statistical moments	. 16
	4. Determination of the parameters as functions of the measured moments	
	5. Errors in noise measurements and their influence on the calculated distribution	
	6. Bandwidth considerations	. 20
	7. References	. 22

Amplitude-Probability Distributions for Atmospheric Radio Noise

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Families of amplitude-probability distribution curves are presented in a form such that by using three statistical parameters of atmospheric radio noise, of the type published by the National Bureau of Standards, the corresponding amplitude-probability distribution may be readily chosen. Typical values of these parameters are given.

1. Introduction

A knowledge of the detailed characteristics of atmospheric radio noise is essential to the design of radio communication systems operating at frequencies up to about 30 Mc/s. These characteristics can conveniently be expressed in terms of an amplitudeprobability distribution which has been found to be an extremely useful tool in the analysis of the expected interference to a communication system [1].¹ However, since the measurement of the complete amplitude-probability distribution on a continuous basis for many frequencies and locations is prohibitive in both manpower and equipment needs, a method of obtaining this distribution from three easily measured statistical moments has been developed at the National Bureau of Standards [2]. The three moments are the average power, the average envelope voltage, and the average logarithm of the envelope voltage, and are expressed, respectively, as:

 F_a —the effective antenna noise figure,

= the external noise power available from an equivalent, short, lossless, vertical antenna in decibels above ktb (the thermal noise power in a passive resistance at room temperature, t, in a bandwidth, b),

 V_a —the voltage deviation in decibels below F_a , L_a —the log deviation in decibels below F_a .

 F_a can be expressed in terms of the root mean square field strength by means of the nomogram in figure 1. It should be noted that although F_a is independent of bandwidth, the root mean square field strength is proportional to the square root of the bandwidth used

The shape of the distribution curve is dependent only on V_a and L_a , and since they have been normalized to F_a , it is possible to construct [2] distribution curves for various combinations of these parameters, independently of the value of F_a . Such curves are given in figures 2 through 21 for the range of values of V_a and L_a for which the distribution is valid. These curves give the percentage of time

the ordinate is exceeded. In order to minimize the number of graphs required, several curves have been drawn on each graph at arbitrary levels. The circle on each curve corresponds to the value of F_a (the root mean square voltage for the distribution) and by shifting the ordinate scale so that zero decibel corresponds to the circle on the proper curve, the ordinate can be determined in decibels above F_a .

Values of F_a , V_a , and L_a are recorded continuously at ten of the stations in the worldwide network established by NBS [3]. These recordings are made at eight fixed frequencies between 13 kc/s and 20 Mc/s, using a bandwidth of about 200 c/s, and the data are published [4, 5] in tabular form. Values of F_a only are recorded at six additional stations in the network and are included in the publications. In addition, predictions of worldwide values of F_a have been published by C.C.I.R. [6].

Typical values of the three parameters are shown in figures 22 and 23. Figure 22 gives F_a versus frequency for summer nighttime and winter daytime, which are the periods of highest and lowest atmospheric noise levels, respectively. Curves are shown for the estimated values of F_a for each type of noise (atmospheric, galactic, and manmade) by taking into account propagation conditions as well as the recorded values.

Figure 23 gives V_d and L_d versus frequency for summer nighttime and winter daytime. The curves were not drawn through all of the measured points, since some signal contamination has been encountered and the smoothed curves are considered more representative of true conditions. The portions of the V_d and L_d curves that result from each of the three noise sources will be the same as shown for

 F_a in figure 22.

Although the distribution curves given in figures 2 through 21 are considered valid for a wide range of bandwidths, the values of V_d and L_d used in determining the distribution must correspond to the bandwidth to be used. The values given in figure 23 are for a 200 c/s bandwidth and must be adjusted for any other bandwidth. Methods of converting these statistical moments from one bandwidth to another are under development at NBS and will be published in the near future.

 $^{^1}$ Figures in brackets indicate the literature references on page 2.

2. References

- A. D. Watt, R. M. Coon, E. L. Maxwell, and R. W. Plush, Performance of some radio systems in the presence of thermal and atmospheric noise, Proc. IRE 46, 12, 1914 (1958).
- (1958).
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- [4] W. Q. Crichlow, C. A. Samson, R. T. Disney, and M. A. Jenkins, Radio Noise Data for the Season March, April, May 1959, NBS Tech. Note 18-2 (PB 151377-2) (March 14, 1960).
- [5] W. Q. Crichlow, Noise investigation at VLF by the National Bureau of Standards, Proc. IRE 45, 6, 778 (1957).
- [6] Report on Revision of Atmospheric Radio Noise Data, C.C.I.R. Rept. No. 65, VIIIth Plenary Assembly, Warsaw (Intern. Radio Consultative Comm., Secretariat, Geneva, Switzerland) (1956).

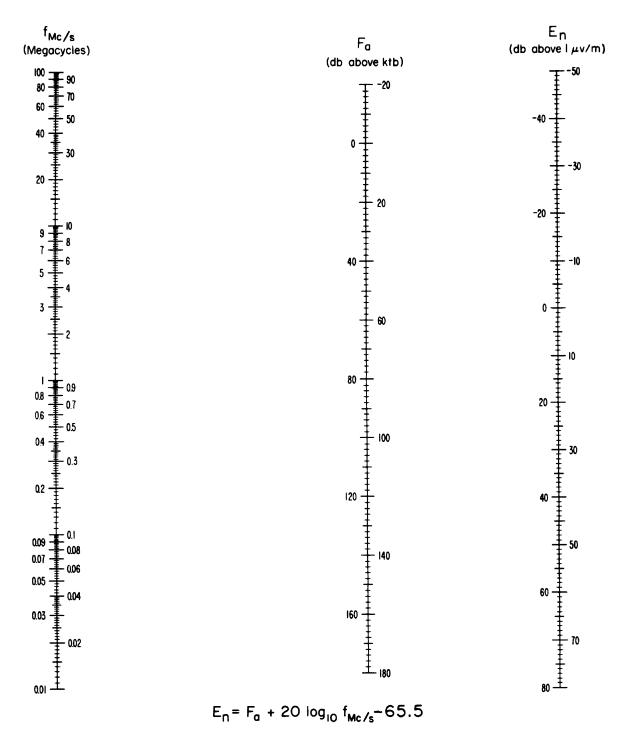
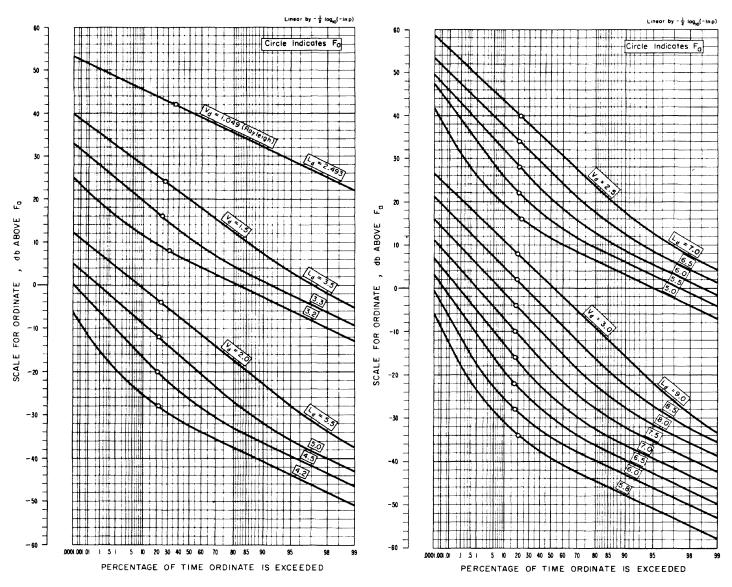


Figure 1. Nomogram for transforming effective antenna noise figure to noise field strength as a function of frequency.

 F_a =effective antenna noise figure=external noise power available from an equivalent short, lossless, vertical antenna in decibels above ktb. E_n =equivalent vertically polarized ground-wave root mean square noise field strength in decibels above 1 μ V/m for a 1-kc/s bandwidth. $f_{Me/e}$ =frequency in megacycles.



 ${\bf Figure} \,\, 2. \quad Amplitude\mbox{-}probability \,\, distributions.$

 ${\tt Figure~3.} \quad {\it Amplitude-probability~distributions}.$

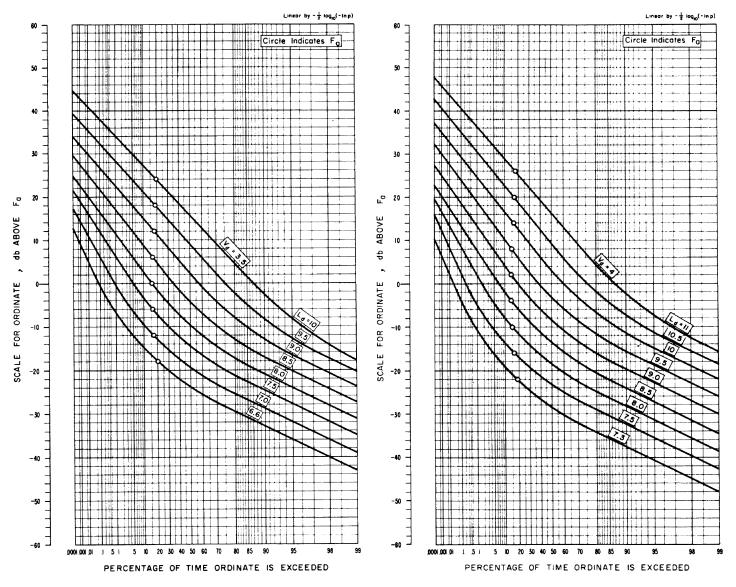


FIGURE 4. Amplitude-probability distributions.

FIGURE 5. Amplitude-probability distributions.

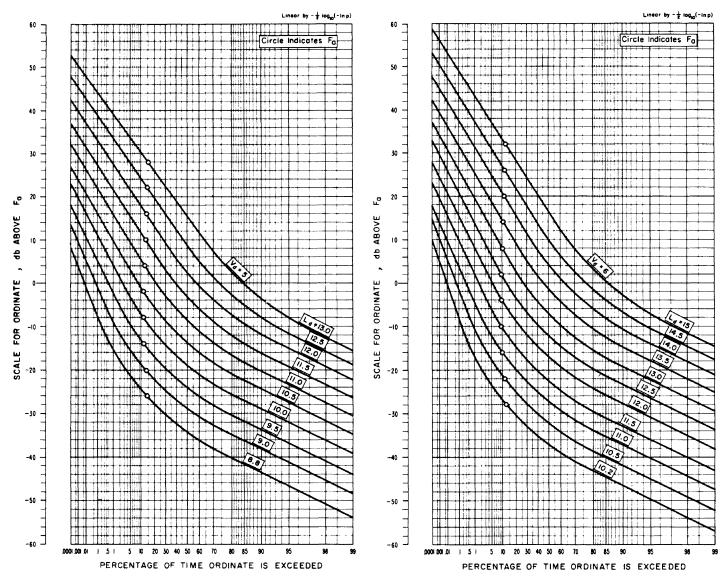


FIGURE 6. Amplitude-probability distributions.

FIGURE 7. Amplitude-probability distributions.

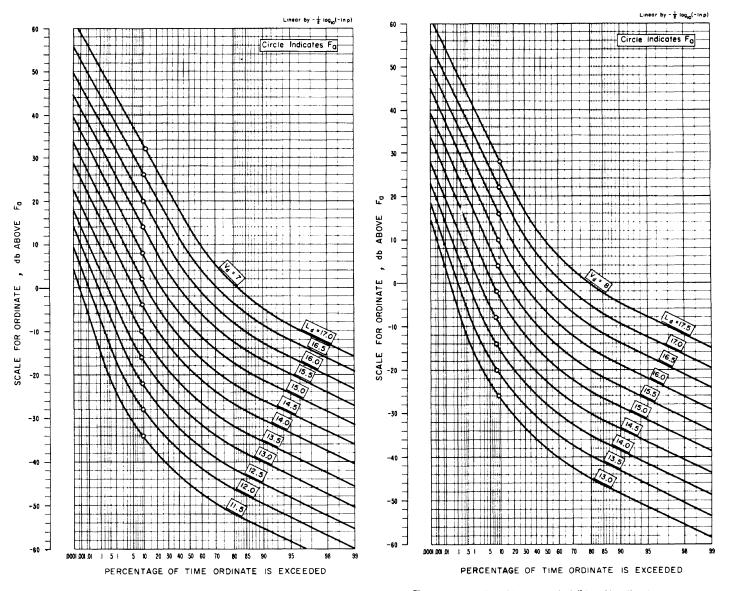


Figure 8. Amplitude-probability distributions.

FIGURE 9. Amplitude-probability distributions.

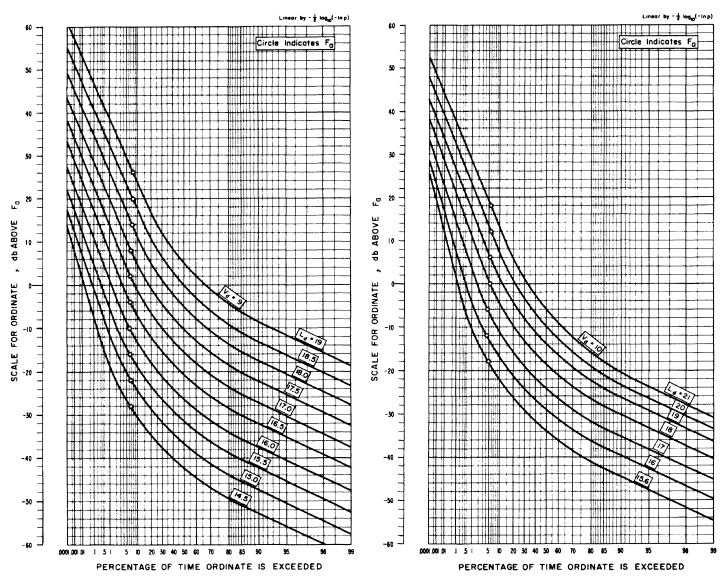


FIGURE 10. Amplitude-probability distributions.

FIGURE 11. Amplitude-probability distributions.

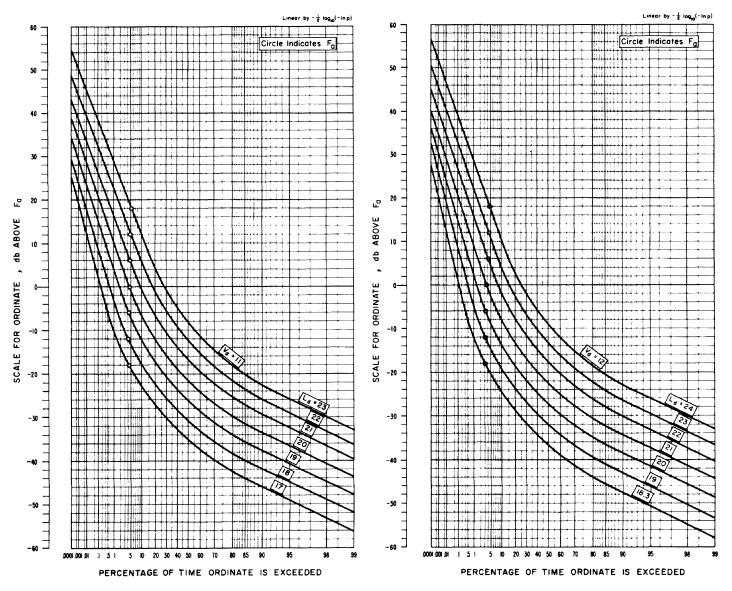
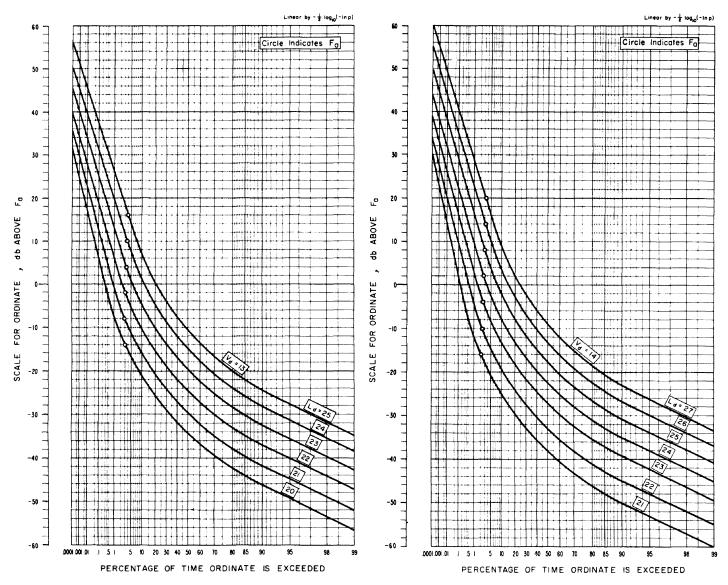


FIGURE 12. Amplitude-probability distributions.

FIGURE 13. Amplitude-probability distributions.



 ${\bf Figure\ 14.} \ \ Amplitude\mbox{-} probability\ distributions.$

Figure 15. Amplitude-probability distributions.

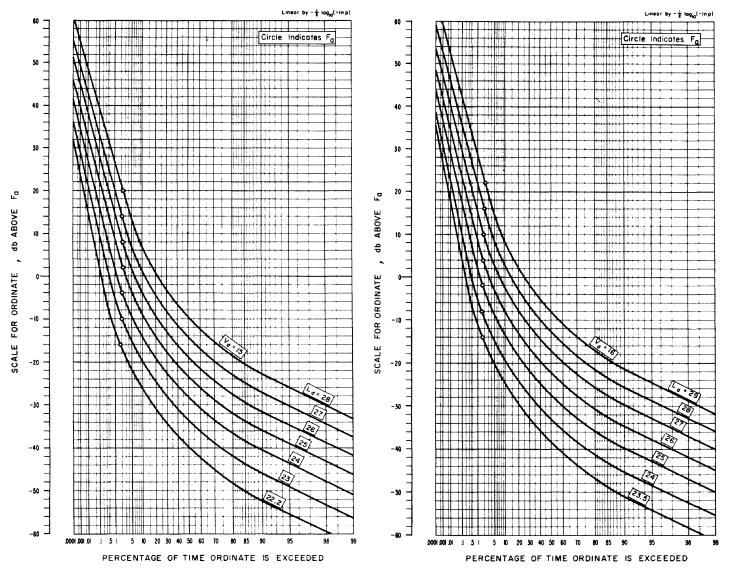


FIGURE 16. Amplitude-probability distributions.

Figure 17. Amplitude-probability distributions.

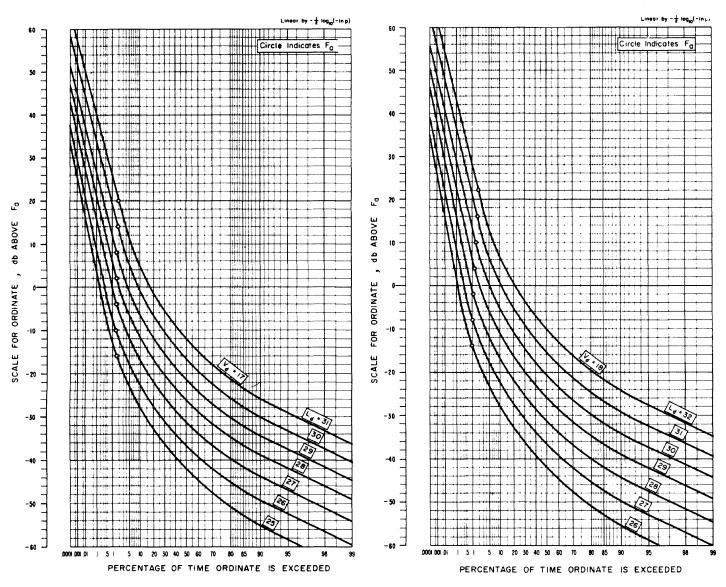


Figure 18. Amplitude-probability distributions.

FIGURE 19. Amplitude-probability distributions.

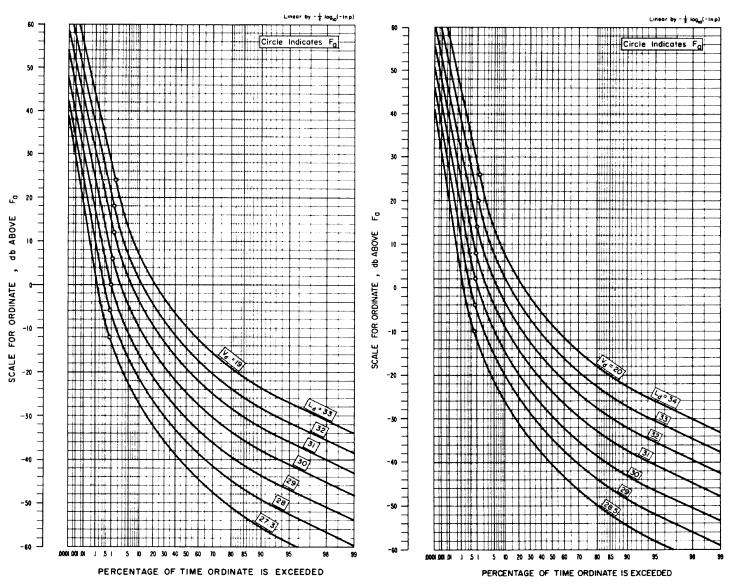


FIGURE 20. Amplitude-probability distributions.

FIGURE 21. Amplitude-probability distributions.

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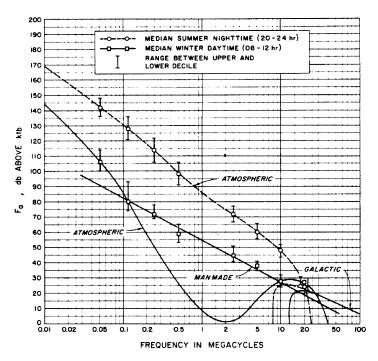


Figure 22. Radio noise levels measured during IGY, Gunbarrel Hill, Boulder, Colo.

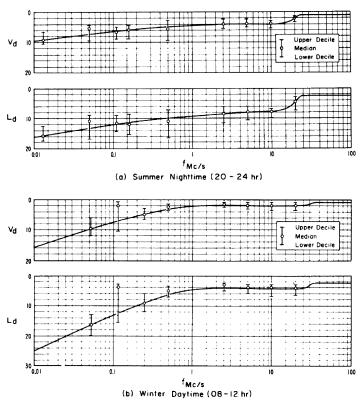


Figure 23. Radio noise statistical parameters.

Measured during summer 1959 and winter 1958-1959, Gunbarrel Hill, Boulder, Colo.

Determination of the Amplitude-Probability Distribution of Atmospheric Radio Noise From Statistical Moments*

W. Q. Crichlow, C. J. Roubique, A. D. Spaulding, and W. M. Beery

(July 23, 1959)

During the International Geophysical Year, the National Bureau of Standards established a network of atmospheric noise recording stations throughout the world. The ARN-2 noise recorder at these stations measures three statistical moments of the noise: average power, average voltage, and average logarithm of the voltage. An empirically-derived graphical method of obtaining an amplitude-probability distribution from these three moments, and its development, is presented. Possible errors, and their magnitudes, are

1. Introduction

The interference to reception of radio signals caused by atmospheric noise depends not only on its average level but also on its detailed characteristics. A complete description of the noise received at a particular location would require an exact determination of the variation of its instantaneous amplitude as a function of time. Because of the complexity of the noise structure and the fact that no two samples of noise have identical amplitudetime functions, it is necessary to resort to simpler types of description of a statistical nature.

Various methods of measurement have been investigated by experimenters throughout the world for many years, and the relationship between the measured values and the interference caused to various types of service has been studied.

In order to determine the most significant characteristics to be measured, an international subcommittee was formed within Commission IV of URSI 1 to study the problem. A recommendation [1], based on the subcommittee's report [2], was endorsed by Commission IV at the XIIth General Assembly of the URSI in 1957. In the Annex to this recommendation, it is stated that "it would be highly desirable to obtain detailed statistical information on the amplitude-probability distribution of the instantaneous envelope voltage, the various time functions, and the direction of arrival of the noise at many locations throughout the world. However, since continuous detailed measurements of this type at all frequencies and a large number of stations become prohibitive because of the complexity of the equipment involved and the large number of personnel necessary to carry out the observations, it is recommended that these complete studies of the detailed noise characteristics be confined to a few selected locations with continuous measurements of one or more simple parameters at a large number of stations."

During the International Geophysical Year, the National Bureau of Standards established a network of 16 noise recording stations distributed throughout the world [3]. Measurements are made with the ARN-2 recorder which was designed at NBS to record the average noise power in a bandwidth of about 200 cps on eight fixed frequencies between 13 kc and 20 Mc. In order to obtain additional information on the character of the noise, two other statistical moments, the average envelope voltage, and the average logarithm of the envelope voltage are recorded at ten of the stations. These data are available from IGY World Data Center A, NBS, Boulder, Colo., at a nominal fee. The results of data analysis will also be published in an NBS Technical Note for public sale.

The amplitude-probability distribution is very useful in assessing the interference potential of noise and has been measured at several locations [4, 5, 6, 7]. Since data on the moments measured by the ARN-2 can be recorded continuously over the full frequency range with much less equipment and fewer personnel than would be required for a comparable amount of data on the complete amplitude-probability distribution, an investigation was made at the NBS of methods of deriving the complete distribution from these three moments.

It is the opinion of the authors that mathematical models for the distribution [1,5,7,8] have proved to be extremely cumbersome and of doubtful value in deriving the distribution from measured moments: therefore, an empirically derived graphical method has been developed.

2. Measurements of the Amplitude-**Probability Distribution**

Simultaneous measurements of the amplitudeprobability distribution and the three moments measured by the ARN-2 were needed over a wide frequency range with a variety of types of noise. There were two specific purposes in making these measurements:

^{*}Reprinted from J. Research NBS, Vol. 64D, No. 1, Jan.-Feb. 1960.

International Scientific Radio Union.
 Figures in brackets indicate the literature references at the end of this paper.

- a. The distribution measurements, alone, were needed to establish typical shapes that could be expressed by numerical parameters, easily related to the measured statistical moments.
- b. The simultaneous measurements of the distributions and the moments were needed to check the accuracy of the ARN-2 noise recorder in measuring the moments.

Accordingly, a distribution meter was constructed to be used in conjunction with the ARN-2 recorder.

The operation of the distribution meter is based on counting techniques. The total number of IF cycles in the ARN-2 which exceed a specified amplitude in a given time interval are counted. By proper choice of the time interval, the percentage of time a level is exceeded can be read directly from the counter. Three counters are used to provide simultaneous measurement at three levels, separated in amplitude by 6 db. By use of a calibrated, manually-operated attenuator, the total possible range of 100 db can be covered in levels separated by multiples of 2 db. The time duration of each sample can be preset to provide an automatically timed sample having an interval ranging from 1 sec to 1 hr, in 1 sec increments.

The actual intervals were chosen of sufficient duration to provide a statistically significant sample of a slowly varying phenomenon such as thunderstorm activity. Longer intervals were required for the high-level, low-probability noise pulses than for the low-level, high-probability noise. The time necessary to obtain a complete curve ranged from about 15 min to 30 min. The longer period was necessary for measuring noise with a large dynamic range.

A check for accuracy of operation was made by obtaining a distribution of thermal noise. The Rayleigh distribution thus obtained confirmed the accuracy of measurement. Figure 1 is a typical amplitude-probability distribution of atmospheric radio noise at 13.3 kc. This was plotted on Rayleigh graph paper, whose coordinates were chosen so that a Rayleigh distribution will plot as a straight line with a slope of $-\frac{1}{2}$. The coordinates are shown as noise level in decibels above the root mean square voltage versus the percentage of the time that each level is exceeded. This measurement was made with the distribution meter at the Boulder Laboratories. The dynamic range between the 0.0001 percent and 99 percent intercepts is approximately 84 db.

It was found that these amplitude-probability distributions for atmospheric radio noise can be adequately represented by a three-section curve which has been drawn through the data points in figure 1. This curve has a characteristic shape that can be described by means of four numerical parameters to be defined later. The accuracy of fit using this particular kind of curve composed of three sections is typical of more than 100 distributions experimentally measured at Boulder. In the particular case of thermal noise, this curve becomes a straight line.

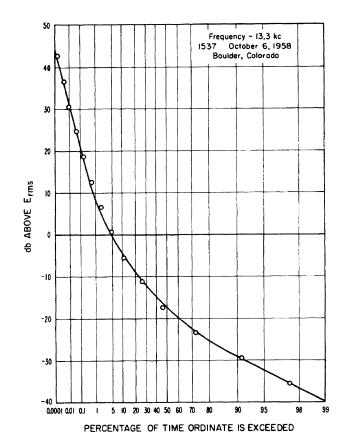


FIGURE 1. Measured amplitude-probability distribution of atmospheric radio noise.

Data obtained by other experimenters [2] in Alaska, Panama, England, and Florida when plotted on Rayleigh paper also fit curves of this form.

The lower portion of the curve, representing low voltages and high probabilities, is composed of many random overlapping events, each containing only a small portion of the total energy. Therefore, this portion of the curve must approach a Rayleigh distribution.

The section representing very high voltages exceeded with low probabilities is, in general, composed of nonoverlapping large pulses occurring infrequently. From experimental measurements of atmospheric noise distributions, this section has been found to be well represented by a straight line on Rayleigh graph paper. On this graph paper, the remaining section of the distribution has been found to correspond quite closely to an arc of a circle tangent to the above two straight lines. Based on experimental evidence, it is assumed that no pulses of amplitude greater than those for which the probability of being exceeded is 10^{-6} are present in the distribution.

3. Definition of Parameters and Statistical Moments

Since on the coordinate paper used for the plotting of amplitude distributions for atmospheric radio noise a Rayleigh distribution will always have a slope of —½, and since the center of the circular arc men-

 $^{^{1}}$ These coordinates are log of voltage versus $-\frac{1}{2}\log_{10}$ (-ln of probability).

tioned above will lie on the bisector of the angle formed by the Rayleigh and high-voltage, lowprobability lines, four parameters are needed to define the distribution. A point through which the Rayleigh line passes, a point and a slope for the high-voltage, low-probability line, and a parameter of some kind to determine the radius of the circular arc are needed.

These four parameters are defined as follows:

a=point at which the Rayleigh line intersects the

0.5 probability coordinate.

b=point on that tangent to the circular arc which is perpendicular to the bisector of the angle formed by the Rayleigh and high-voltage, low-probability lines and on the probability coordinate through the vertex of this angle.

c=point where the high-voltage, low-probability line intersects the 0.01 probability coordinate.

s = slope of the high-voltage, low-probability line. The three statistical moments experimentally determined are defined as follows:

rms voltage:
$$e_{\rm rms} = \sqrt{\int_0^1 e^2 dp}$$

average voltage:
$$e_{ave} = \int_0^1 e dp$$

antilog of the mean log of voltage:

$$e_{\log} = \operatorname{antilog} \int_0^1 \log e \, dp.$$

where e is $1/\sqrt{2}$ times the instantaneous envelope voltage, and p is the probability of e being exceeded.

Since the ARN-2 noise recorder measures the db difference between the $e_{\rm rms}$ and $e_{\rm ave}$ and between the $e_{\rm rms}$ and $e_{\rm log}$, and in order to minimize the necessary graphical calculations, the above parameters are altered to relate them to the Rayleigh section of the distribution as follows (see fig. 2):

 $A=20 \log \frac{a}{e_{\rm rms}}$ =db difference between Rayleigh at 0.5 probability and the $e_{\rm rms}$ value. $B={\rm db}$ difference between the point of intersection

of the Rayleigh and high-voltage, low-probability lines and the tangent to the circular arc. (The tangent is drawn perpendicular to the bisector of the angle formed by the Rayleigh and high-voltage, low-probability lines.)

C=db difference between c and value of Rayleigh

at the 0.01 probability coordinate.

X=absolute value of slope of high-voltage, lowprobability line relative to Rayleigh. X=-2s

The moments actually measured are labeled as follows:

$$V_d = 20 \log \frac{e_{\rm rms}}{e_{\rm ave}}$$

$$L_d = 20 \log \frac{e_{\rm rms}}{e_{\rm log}}$$

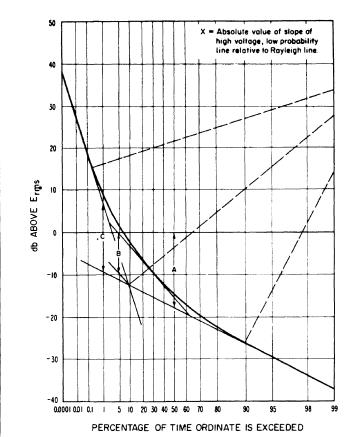


Figure 2. Definition of parameters for amplitude-probability distribution atmospheric radio noise.

The $e_{\rm rms}$ is also measured.

The following relation will always hold true for the distribution:

$$e_{\log} < e_{\text{ave}} < e_{\text{rms}}$$

therefore, V_d and L_d are always positive.

4. Determination of the Parameters as Functions of the Measured Moments

Since four parameters are needed and only three statistical moments are measured, a dependency between two of the parameters must be determined in order to be able to obtain the remaining three independent parameters as functions of the measured moments. From experimentally measured distributions at eight frequencies and various bandwidths, the following linear relation between X and B is found to hold in general (fig. 3).

$$B = 1.5(X-1)$$

Distributions were employed in which C was allowed to vary from 0 to 40 db and X from 1 to 12. These distributions were numerically integrated in order to determine their three moments. From these integrations, V_d and L_d were obtained as functions of X and C. A was also obtained as a function of X and C (fig. 4). These functional relations were solved simultaneously by graphical means to obtain X and C as functions of V_d and L_d (figs. 5 and 6).

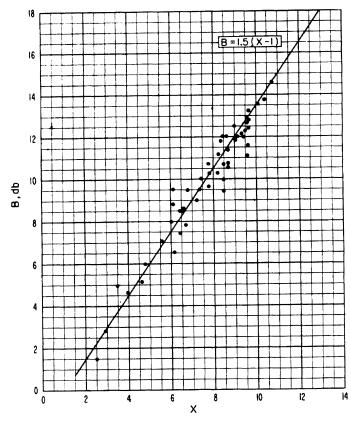


FIGURE 3. Experimental correlation of B and X.

Figure 7 shows the distribution obtained by the above procedure for the following measurements:

 $V_d = 4.5 \text{ db below } e_{rms}$

 $L_d = 9.2$ db below $e_{\rm rms}$.

On the X versus V_a and L_a curves, the above measurements are seen to give an X of 3.7, and on the Cversus V_a and L_a curves the above measurements give a C of 15.8 db. Using the A versus X and Ccurves, this pair of values for X and C gives an A of 12.3 db. Point a is located on the 50 percent coordinate 12.3 db below the $E_{\rm rms}$ and the Rayleigh line with slope $-\frac{1}{2}$ is drawn. Point c is located 16 db above the point where the Rayleigh line intersects the 1 percent coordinate, and through point c the high-voltage, low-probability line with slope s = -X/2 = -1.8 is drawn. The angle formed by the Rayleigh line and the high-voltage, low-probability line is now bisected and B is calculated from the relationship B=1.5(X-1). B is found to be 3.6 db. Point b is located 3.6 db above the intersection of the Rayleigh and high-voltage, low-probability lines and through this point the tangent line is drawn perpendicular to the angle bisector. Distance 2 to 3 is made equal to distance 1 to 2, and at point 3 on the Rayleigh line a perpendicular to the Rayleigh line is constructed. This perpendicular intersects the angle bisector at the center of the circular-arc portion of the distribution. The complete distribution is now determined with the construction of this arc.

It should be noted from the curves (figs. 5 and 6) that for a given V_d only a certain range of values of L_d will result in a distribution of the above form. These ranges are enclosed approximately within the dashed lines. Also, the combination of the above given V_d and the minimum allowable L_d results in a nonunique solution, i.e., there is, essentially (within the range of accuracy of measurements), an infinite number of distributions, all with the same V_d and L_d of the above special combination. Fortunately these special combinations almost never occur.

The above facts allow us to determine to some extent the validity of data received from recording stations, and whether a measured sample is true atmospheric noise or contaminated noise.

5. Errors in Noise Measurements and Their Influence on the Calculated Distribution

The accuracy with which a distribution can be determined from measured moments depends upon (1) the validity of the form factor which has been taken to represent the distribution, and (2) the accuracy of the measured statistical moments.

The validity of the form factor is very difficult to check because of the fact that 15 to 30 min are required to measure the distribution, and the statistics of the noise do not always remain constant for this period of time. As a check for changing noise characteristics, each series of distribution measurements was immediately repeated and any changes noted. Further, the moments recorded by the ARN-2 provided information on the stability of the noise statistics. Figure 1 represents an example of the fit in the case where the noise moments were measured precisely and the noise characteristics appeared to be constant during the interval required for the measurement of the entire distribution. Methods of recording noise samples on magnetic tape are under development and these samples will enable a more critical study of the form factor as well as other detailed characteristics.

Errors in the ARN-2 could be detected by comparing the recorded three parameters with the same three parameters as numerically integrated from the curve recorded by the distribution meter. The most likely source of error in the ARN-2 was the possible saturation of the square law detector with a resultant lowered value for $E_{\rm rms}$. Since the average voltage and average logarithm of the voltage are measured in decibels relative to $E_{\rm rms}$, their values would be in error by the same amount.

Approximately sixty sets of distribution measurements were analyzed for the error made by the ARN-2 recorder in measuring the moments. These ARN-2 errors were divided into class-intervals and plotted as error-probability curves on arithmetic probability graph paper in figure 8. The fairly straight lines obtained indicated largely random errors, with some bias due to square-law detector saturation. For the $E_{\rm rms}$ values, the standard deviation

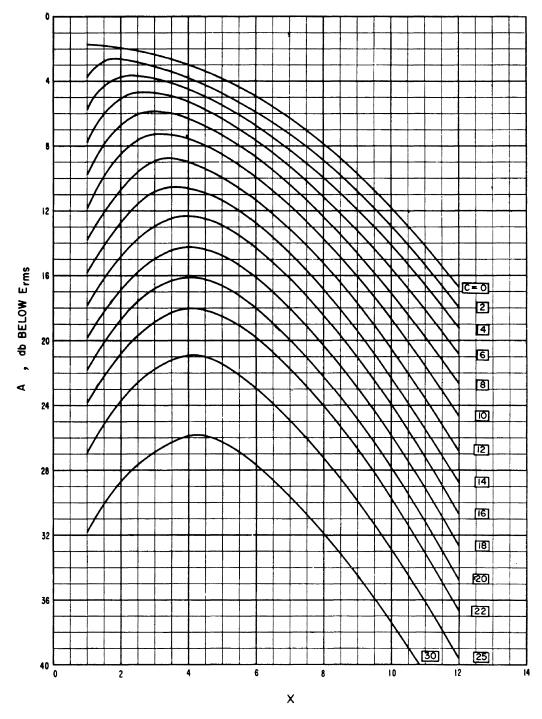


FIGURE 4. A versus X and C.

was about 1.1 db, with an average error of -0.4 db. Ninety percent of the values were within ± 2 db of the mean. For the $E_{\rm ave}$ values, the standard deviation was about 0.8 db, with an average error of +0.2 db. Ninety percent of the values were within ± 1.5 db of the mean. For the $E_{\rm log}$ values, the standard deviation was about 1.4 db, with an average error of +0.6 db. Ninety percent of the values were within ± 2.5 db of the mean.

An effort was made to correlate the error with dynamic range between the 0.0001 percent and 99

percent intercepts of the amplitude-probability distributions. The same data were divided into classintervals and the medians of the class-intervals which contained sufficient samples for statistical significance were plotted against dynamic range in decibels in figure 9. The best straight-line fit indicates good correlation of error with dynamic range, a negative error for $E_{\rm rms}$ and a positive error for $E_{\rm ave}$ and $E_{\rm log}$. The error in $E_{\rm rms}$ at 85-db dynamic range varied from -2.7 to +2.1 with a median value of about 1 db.

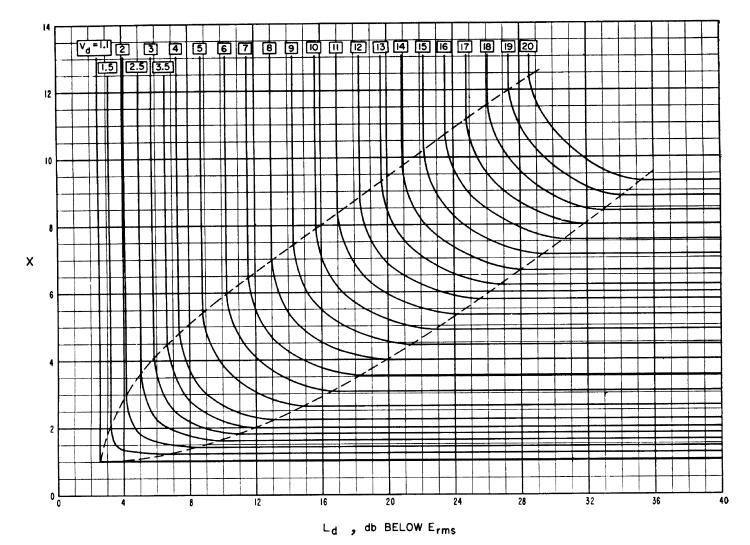


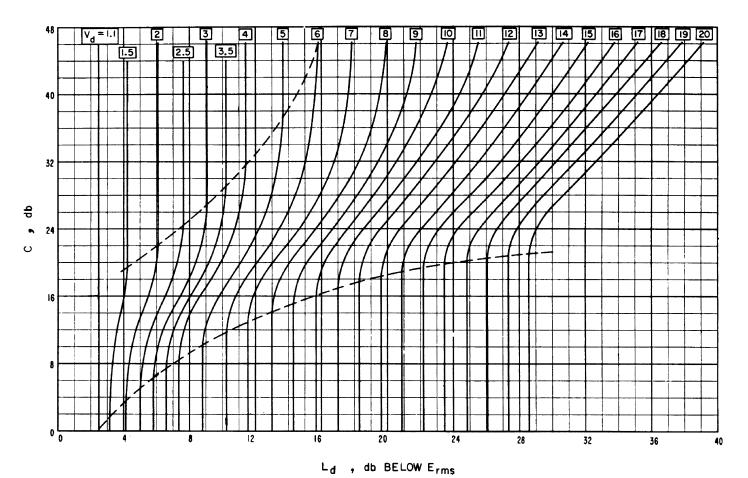
FIGURE 5. X versus Ld and Vd.

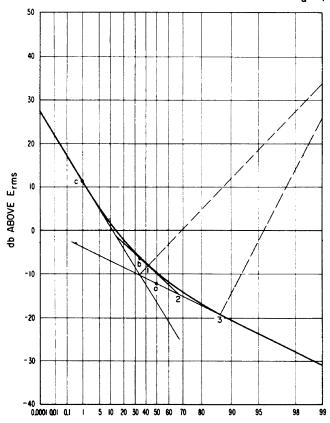
Figures 10 and 11 show the influence of errors in the moments measured by the ARN-2 on distributions determined from the moments. In these figures, the measured moments are indicated as E'_{rms} etc., and the moments obtained from the simultaneously measured distribution are indicated by the same symbols without the primes. The examples chosen contain errors typically measured by the ARN-2. In figure 10, the errors in the measured moments are small and the distribution derived from the slightly erroneous ARN-2 moments fits the measured points with negligible error. In figure 11, the dynamic range is wider with correspondingly larger errors in the ARN-2 measured moments. Thus, the departure of the distribution derived from the ARN-2 measured moments is greater. These departures, though significant are not considered excessive in view of the fact that they are of the same order of magnitude as the changes in the noise itself during an hour.

Thus, it can be concluded that this is a satisfactory method of deriving the complete amplitude-probability distribution from statistical moments, since the departures from the true distribution will be small when the moments are measured accurately.

6. Bandwidth Considerations

The foregoing method of obtaining an amplitude-probability distribution from the three measured moments results in a distribution which is only valid for the bandwidth in which the moments were measured. Fulton [8] developed a method of bandwidth conversion which was accurate for the high-amplitude, low-probability portion of the distribution, but failed to convert the lower portion of the curve as accurately since it was an empirical method based upon insufficient measurements. A study is now in progress for a more accurate method of bandwidth conversion.





PERCENTAGE OF TIME ORDINATE IS EXCEEDED FIGURE 7. Amplitude-probability distribution determined for $V_d\!=\!4.5~{\rm db}$ and $L_d\!=\!9.2~{\rm db}$.

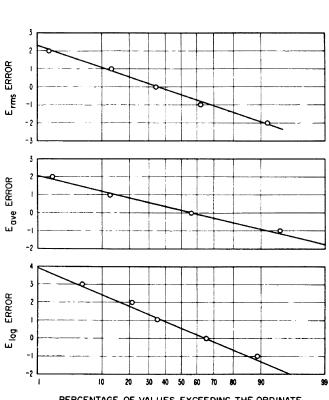


FIGURE 6. C versus Ld and Vd.

PERCENTAGE OF VALUES EXCEEDING THE ORDINATE FIGURE 8. Distribution of errors of measured moments.

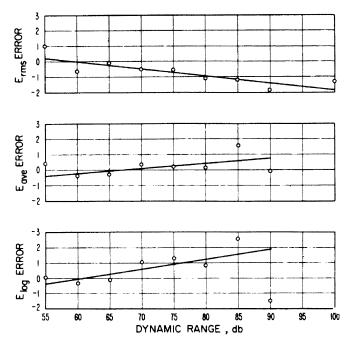


FIGURE 9. Error of measured moments versus dynamic range.

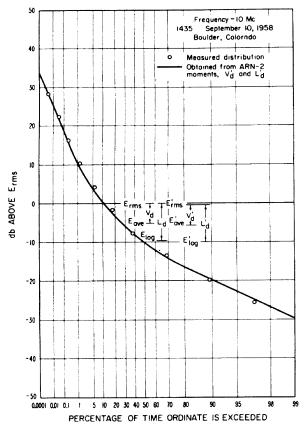


FIGURE 10. Comparison of measured distribution with that obtained from moments measured by ARN-2.

BOULDER, Colo.

(Paper 64D1-37)

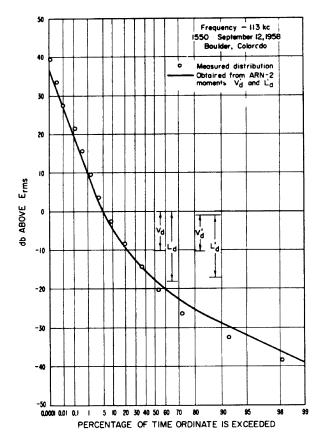


FIGURE 11. Comparison of measured distribution with that obtained from moments measured by ARN-2.

7. References

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