

1 Improved dynamic geomagnetic rigidity cutoff modeling: testing predictive
2 accuracy

3 Mark A. Clilverd

4 Physical Sciences Division, British Antarctic Survey (NERC), Cambridge, United Kingdom

5 Craig J. Rodger

6 Department of Physics, University of Otago, Dunedin, New Zealand

7 Tracy Moffat-Griffin

8 Physical Sciences Division, British Antarctic Survey (NERC), Cambridge, United Kingdom

9 Pekka T. Verronen

10 Finnish Meteorological Institute, Helsinki, Finland.

11 **Abstract.** In the polar atmosphere, significant chemical and ionization changes occur during
12 solar proton events (SPE). The access of solar protons to this region is limited by the
13 dynamically changing geomagnetic field. In this study we have used riometer absorption
14 observations to investigate the accuracy of a model to predict K_p -dependent geomagnetic rigidity
15 cutoffs, and hence the changing proton fluxes. The imaging riometer at Halley, Antarctica is
16 ideally situated for such a study, as the rigidity cutoff sweeps back and forth across the
17 instrument's field of view, providing a severe test of the rigidity cutoff model. Using
18 observations from this riometer during five solar proton events, we have confirmed the basic
19 accuracy of this rigidity model. However, we find that the model can be improved by setting a
20 lower K_p limit (i.e., $K_p=5$ instead of 6) at which the rigidity modeling saturates. We also find that
21 for $L>4.5$ the apparent L -shell of the beam moves equatorwards. In addition, the Sodankyla Ion
22 and Neutral Chemistry model is used to determine an empirical relationship between integral

23 proton precipitation fluxes and nighttime ionosphere riometer absorption, in order to allow
24 consideration of winter time SPEs. We find that during the nighttime the proton flux energy
25 threshold is lowered to include protons with energies of >5 MeV in comparison with >10 MeV
26 for the daytime empirical relationships. In addition, we provide an indication of the southern and
27 northern geographic regions inside which SPEs play a role in modifying the neutral chemistry of
28 the stratosphere and mesosphere.

29

29 1. Introduction

30 Solar proton events (SPEs) are a major space weather phenomena that can produce hazardous
31 effects in the near-Earth space environment. The occurrence of SPEs varies during the 11-year
32 solar activity cycle. In active years, especially during the falling and rising phases of the solar
33 cycle, SPEs may average one per month, but during solar minimum years the occurrence is very
34 low, e.g., ~ 1 per year. SPEs cause 'upsets' to Earth-orbiting satellites, increased radiation
35 exposure levels for humans onboard spacecraft and high-altitude aircraft, ozone depletions and
36 disruption to HF/VHF communications in mid- and high-latitude regions. A detailed
37 understanding of all these impacts depends upon knowledge of the dynamic rigidity cutoffs as
38 SPE particles are partially guided by the geomagnetic field. Higher rigidities are required for a
39 particle to reach lower geomagnetic latitudes, and thus all particles with rigidities larger than the
40 minimum can penetrate to that latitude (and all higher latitudes). The geomagnetic cutoff rigidity
41 is a dynamic quantity depending on the Earth's internal and external magnetic fields [*Smart and*
42 *Shea, 2003; Kress et al., 2004*].

43 Experimental measurements of geomagnetic cutoff rigidities have generally been based on
44 satellite observations. Few experimental studies have derived cutoffs during the most disturbed
45 conditions during geomagnetic storms. Theoretical calculations have primarily focused on
46 tracing particles through models of the Earth's field producing grids of estimated cutoff rigidities
47 distributed over the Earth at a given altitude [e.g., *Smart and Shea, 2001*]. *Birch et al.* [2005]
48 used satellite measurements of the edge of the polar cap sampled four times each day, and found
49 that cutoff latitudes reduce by $5\text{-}8^\circ$ during storms. They compared the results with particle-
50 tracing models, which underestimated the effects of a severe storm. *Rodger et al.* [2006] used the
51 model of K_p -dependent geomagnetic rigidity cutoff energies based on the Tysganenko-89
52 magnetic field model [*Smart and Shea, 2001*], to investigate for the first time, detailed
53 comparisons of theoretical cutoff rigidities and ground-based measurements during a large

54 geomagnetic disturbance. Energy cutoffs on satellite derived proton fluxes were used to calculate
55 the predicted cosmic noise absorption levels for the Halley imaging riometer (IRIS) during a
56 single SPE event in November 2001. The predicted absorption levels showed good agreement
57 with those experimentally observed for low and mid levels of geomagnetic disturbance levels
58 ($K_p < 5$). However, in very disturbed conditions ($K_p \approx 7-9$) the rigidity energy cutoffs indicated by
59 the IRIS observations appeared to saturate around those predicted for $K_p \approx 6$ by the particle-
60 tracing approach. This suggested that the geomagnetic latitude limit for the penetration of SPE
61 protons during large geomagnetic storms is rather more poleward than had been indicated
62 previously.

63 Imaging riometer systems (IRIS) like the one at Halley, Antarctica, are well suited for
64 examining geomagnetic cutoffs, because the receiver arrays provide an image of the ionospheric
65 absorption levels in a $200 \text{ km} \times 200 \text{ km}$ horizontal region above the instrument by measuring the
66 absorption of cosmic radio noise at a given frequency (usually 20-40 MHz). Using riometers it
67 has previously been shown that there is an empirical relationship between the square root of the
68 integral proton flux ($>10 \text{ MeV}$) and cosmic noise absorption (CNA) in daytime, at least when
69 geomagnetic cutoff effects do not limit the fluxes [Kavanagh *et al.*, 2004]. The same study
70 concluded that variations in the spectral hardness of the SPE proton flux and atmospheric
71 collision frequencies do not cause significant departures from the linear relationship observed.

72 In this paper we examine ground-based measurements during five SPEs, based on the
73 observations from the imaging riometer at Halley, Antarctica, which is situated such that the
74 rigidity cutoff sweeps back and forth across the instrument's field of view during each SPE. We
75 calculate riometer absorption, using input proton fluxes modified by rigidity cutoff calculations,
76 and contrast the varying, predicted and observed, rigidity cutoffs during each geomagnetic
77 disturbance. We also use the Sodankyla Ion and Neutral Chemistry (SIC) model to determine an
78 empirical relationship between integral proton precipitation fluxes and nighttime ionosphere

79 riometer absorption to complement the daytime relationship already published, and to study
80 rigidity effects during winter time SPEs.

81 **2. Experimental Setup**

82 The riometer utilizes the absorption of cosmic radio noise by the ionosphere [*Little and*
83 *Leinbach, 1959*] to measure the enhancement of D-region electron concentration by energetic
84 charged particle precipitation [*Stauning, 1996*]. The riometer technique compares the strength of
85 the cosmic radio noise signal received on the ground to the normal sidereal variation referred to
86 as the quiet-day curve to produce the cosmic noise absorption. The instantaneous ionospheric
87 absorption in decibels is derived from the ratio of the prevailing signal level to this curve
88 [*Krishnaswamy et al., 1985*]. In typical operations the absorption peaks near 90 km altitude,
89 where the product of electron density and neutral collision frequency maximizes. In this paper
90 we consider experimental observations from selected beams of an imaging riometer located at
91 Halley (75.6°S, 26.32°W, $L=4.6$), as shown in Figure 1.

92 At Halley the system is a snow-buried 49-beam imaging riometer, operating at 38.2 MHz and
93 sampled every 1 sec [*Rose et al., 2000*]. Several receivers are multiplexed through a phased array
94 of 64 crossed-dipole antennas to achieve narrow beam scanning of the D region. The beam width
95 is 13°. In the meridian plane the most equatorward and poleward beams intersect the D region
96 ionosphere about 1° north (equatorward) and south (poleward) from the vertical central beam,
97 respectively. Absorption values for obliquely orientated (non-vertical) beams are automatically
98 corrected to vertical following the technique described by *Hargreaves and Jarvis* [1986].

99 In this study we analyze data collected at Halley during five SPEs. The SPE periods are July
100 2000, November 2000, two periods in November 2001, and October 2003. Prior to, and after
101 these events the Halley imaging riometer performance was severely limited by snow buildup as

102 the IRIS was buried [*Rose et al.*, 2000] as a result of ever-increasing snow accumulation on the
 103 antenna array.

104

105 **3. Estimates of Rigidity Cutoffs**

106 It has been recognized for some time that geomagnetic rigidity cutoffs are well-ordered in terms
 107 of the McIlwain L -parameter [*Smart and Shea*, 1994; *Selesnick et al.*, 1995]. The L -variation of
 108 the geomagnetic rigidity cutoff has been determined for quiet times from $\approx 10,000$ nuclei
 109 observations made by the MAST instrument on the SAMPEX satellite [*Ogliore et al.*, 2001].
 110 These authors report that the geomagnetic rigidity cutoffs, R_c , for quiet times are given by

$$111 \quad R_c = 15.062 L^{-2} - 0.363 \quad (\text{in GV}) \quad (1)$$

112 representing average conditions for $K_p=2.3$. As noted above, dynamic vertical cutoff rigidities
 113 dependent upon magnetic activity levels have been determined by particle-tracing [*Smart and*
 114 *Shea*, 2003] using the K_p -dependent Tsyganenko magnetospheric field model. These authors
 115 have reported that the change of proton cutoff energy with K_p is relatively uniform over the range
 116 of the original *Tsyganenko* (1989) model ($K_p < 5$), but the cutoff changes introduced by the
 117 *Boberg et al.* [1995] extension to higher K_p is non-linear such that there are large changes in
 118 proton cutoff energy for a given L -value at large K_p values. *Rodger et al.* [2006] made use of the
 119 K_p -dependent variations in the effective vertical cutoff energies at a given IGRF L -value at
 120 450 km altitude determined from this modeling [*Smart et al.*, Fig. 5, 2003], but with a slight
 121 modification to ensure that the geomagnetic rigidity cutoff varies as $15.062 L^{-2}$, as observed in
 122 the SAMPEX experimental data. Note that the change in cutoff energy with geomagnetic activity
 123 is strongly non-linear at the highest disturbance levels. In order to interpolate down to lower
 124 altitudes (e.g., 100 km), *Rodger et al.* [2006] followed the approach outlined by *Smart and Shea*
 125 [2003] again using the IGRF determined L -value. This exploits the basic relationship between R_c
 126 and L , i.e.,

$$R_c = V_k L^{-2} \quad (2)$$

127 where V_k is an altitude independent constant. Thus by knowing the value of V_k for the IGRF L -
 128 value at 450 km altitude above a given location, one can determine R_c at 100 km once one knows
 129 the L -value for that location at 100 km altitude. In the Rodger-approach the upper limit for K_p in
 130 the rigidity model is $K_p=6$. When K_p exceeds this level then it is forced to $K_p=6$ in the rigidity
 131 calculations, a limit selected through contrast with the November 2001 experimental
 132 observations.

134 The rigidity cutoff relationship developed by *Smart and Shea* [2003], and tested and improved
 135 by *Rodger et al.* [2006] is further investigated here using a series of SPEs observed by the
 136 imaging riometer at Halley.

137

138 **4. Daytime riometer data and calculated absorption**

139 Figure 2 shows three days of experimentally-observed cosmic noise absorptions recorded by
 140 two of the meridional beams of the Halley IRIS instrument (i.e., pointing N-S) during the 8-11
 141 November 2000 SPE with 15 min averaging. In the upper panel CNA are shown for the IRIS
 142 southernmost beam 1 ($L=4.80$, solid line, which we term the "poleward beam"), and in the
 143 middle panel the northernmost beam 7, ($L=4.32$, long dashed line, which we term the
 144 "equatorward beam"). The beams map to the ionosphere so as to be viewing $\sim 1^\circ$ north and south
 145 in latitude (i.e. $75.6^\circ\text{S} \pm 1^\circ$). These two beams represent the two most extreme locations for
 146 rigidity cutoff effects that the instrument can observe. The bottom panel shows the variation of
 147 K_p during the SPE. In addition, both the upper and middle panels show the variation of the non-
 148 cutoff absorption that would be expected if there were no influence of rigidity on the proton
 149 fluxes into the atmosphere (short dashed line) based on the relationship between daytime
 150 absorption and proton fluxes developed by *Kavanagh et al.* [2004], i.e., using $\text{Absorption} = 0.09 \times$
 151 $(>10 \text{ MeV proton flux})^{0.5}$. This line therefore represents the variation of the proton fluxes

152 throughout the event. The equivalent absorption levels using rigidity affected proton fluxes
153 determined through the approach outlined in section 3 for each beam location are also shown
154 (asterisk in the south, diamond in the north), again calculated using the *Kavanagh et al.* [2004]
155 relationship. The time resolution of these calculations is limited to 3-hours because of the K_p
156 dependence of the rigidity cutoff model.

157 The SPE of 8-11 November 2000 generated peak GOES proton fluxes of $14,800 >10$ MeV
158 protons $\text{cm}^{-2} \text{str}^{-1} \text{s}^{-1}$ at 16 UT on 9 Nov, and a peak K_p of 6^+ at 9-12 UT on 10 Nov. As such, this
159 event occurred during a moderate geomagnetic storm. During November the atmosphere above
160 Halley, Antarctica, is fully sunlit and thus the use of the *Kavanagh et al.* [2004] daytime
161 absorption relationship is appropriate. In the southern (poleward) beam absorption levels of
162 ~ 4 dB are observed during the period of highest proton fluxes, while in the northern
163 (equatorward) beam absorption levels of ~ 2 dB are observed. These values are generally in good
164 agreement with the estimated absorption levels when the effects of varying rigidity cutoffs are
165 included, and significantly below the non-cutoff levels of ~ 8 dB absorption. When the proton
166 fluxes are very low the predicted absorption remains close to zero whatever the K_p level, thus it
167 is only possible to compare the predicted absorption with the observed absorption when the
168 proton fluxes are elevated. For the SPE of 8-11 November 2000 this is after 00 UT on 9 Nov,
169 lasting until the end of 10 Nov. Of the fifteen 3-hourly bins, 5 show significant over estimates
170 (~ 2 dB) in the predicted absorption in the southern (poleward) beam, while only 2 over estimates
171 occur in the northern (equatorward) beam. The remaining periods show reasonable agreement
172 between the predicted and observed absorption levels typically to within ± 0.5 dB. Periods where
173 the absorption is higher than the predicted absorption level are likely to be influenced by
174 additional factors such as electron precipitation [*Shirochkov et al.*, 2004], which leads to
175 additional absorption on top of the proton-induced absorption, and are therefore not well
176 described by the proton-only *Kavanagh et al.* [2004] relationship. One example of this

177 occurrence is 00-06 UT on 9 November 2000, where higher than predicted absorption is seen on
178 both beams.

179 There are two periods where the data and theory disagree during the 8-11 November 2000
180 event. At 6-12 UT on 10 Nov K_p reaches 6, and the theoretical absorption levels are the same as
181 the non-cutoff case, i.e., a very high proportion of the proton fluxes should be impacting the
182 atmosphere above the riometer. But, both the northern and southern beam absorption levels
183 indicate that there is still significant rigidity cutoff influence at this time. The second anomalous
184 period occurs at 14 UT on 9 Nov in the southern (poleward) beam. The theoretical absorption
185 levels increase from ~ 2 dB to ~ 4 dB in response to a small increase in K_p from <2 to 3^+ . This is
186 not seen in the observed absorption.

187 Figures 3, 4, and 5 show plots in the same format as Figure 2, and represent SPEs occurring
188 during 26-29 November 2000, 5-8 November 2001, and 28-31 October 2003 respectively. The
189 peak proton >10 MeV fluxes were 942, 31700, and 29500 protons $\text{cm}^{-2} \text{str}^{-1} \text{s}^{-1}$ while the
190 maximum K_p values were 6^+ , 9^- , and 9 respectively. Thus Figure 3 represents a small SPE, and
191 Figures 4 and 5 represent two very large SPEs, with the latter cases associated with very large
192 geomagnetic disturbances.

193 Although the proton fluxes are significantly lower during the 26-29 November 2000 SPE when
194 compared with the 8-11 November 2000 event, the maximum K_p values are the same (6^+). Thus
195 these two events are comparable in many ways. Figure 3 shows that the theoretical absorption
196 levels in the southern (poleward) and northern (equatorward) beams are over estimated in
197 comparison with the absorption data, particularly when $K_p \approx 6$ in the northern (equatorward)
198 beam, and $K_p = 4-6$ in the southern (poleward) beam. This is particularly apparent when the
199 proton fluxes are high, and the absorption levels significantly elevated. Of the twenty three 3-
200 hourly bins where proton fluxes are high, 9 show significant over estimates ($\sim 0.5-1$ dB) in the

201 predicted absorption in the southern (poleward) beam, while only 5 over estimates occur in the
202 northern (equatorward) beam.

203 The two large storms shown in Figure 4 and 5 have a wider range of K_p values, but follow
204 similar patterns of behavior as Figure 3. The northern (equatorial) beam shows good agreement
205 between the theoretical absorption and the observed data until $K_p \sim 6$. Under these conditions the
206 theoretically determined rigidity cutoffs predict very little influence of cutoff rigidity (i.e., low
207 cutoff energies) on the proton fluxes and thus high absorption levels, but the observed absorption
208 levels are more consistent with $K_p \sim 5$ and thus a significant influence due to rigidity cutoffs
209 limiting the proton fluxes. The southern (poleward) beam shows good agreement between
210 theoretical absorption levels and observed absorption for very high K_p ($K_p > 6$), but over estimated
211 absorptions when $K_p = 4-6$. During high K_p ($K_p > 6$) the theory predicts, and the observations show,
212 that there is little or no cutoff rigidity affect on the absorption levels for this beam location. Of
213 the twenty three 3-hourly bins where proton fluxes are high in Figure 4, six show significant over
214 estimates (~ 2 dB) in the predicted absorption in the southern (poleward) beam, while only 3 over
215 estimates occur in the northern (equatorward) beam. Of the nineteen 3-hourly bins where proton
216 fluxes are high in Figure 5, five show significant over estimates (~ 2 dB) in the predicted
217 absorption in the southern (poleward) beam, while 8 over estimates occur in the northern
218 (equatorward) beam. This represents an unusual event because the northern beam is less well
219 modeled than the southern beam. The primary reason is because of the unusually long-lasting
220 very high K_p levels leading to less errors in the southern beam in comparison with the northern
221 beam.

222 The Halley riometer data during the SPE of 5-8 November 2001 was previously used to test the
223 improved rigidity cutoff calculations developed by *Rodger et al.* [2006]. The cutoff rigidities
224 were applied to the proton fluxes in the same way as this study, but the SIC model was used to
225 calculate the riometer absorption instead of using the empirical relationship as we do here.

226 Comparing Figure 4 in this study with Figure 7 of *Rodger et al.* [2006] shows that combining the
227 empirical relationship with rigidity modified proton fluxes agrees closely with the SIC model
228 results. In addition, the right panel of Figure 3 of *Rodger et al.* [2006] showed that the
229 absorptions calculated by the SIC model in the absence of rigidity cutoff effects reproduces the
230 empirical relationship reported by *Kavanagh et al.* [2004].

231 So far we have described riometer absorption observed during four SPEs that occurred during
232 the southern hemisphere summer, and thus under daytime conditions. In the next section we
233 determine a nighttime relationship between proton fluxes and riometer absorption in order to
234 investigate rigidity cutoff effects during polar winter nighttime conditions.

235 **5. Nighttime riometer absorption using the Sodankylä Ion and Neutral Chemistry Model**

236 As in *Rodger et al.* [2006] we use the SIC model to produce lower ionospheric electron density
237 profiles during SPEs, but this time in the winter-time (i.e. nighttime) *D*-region above the Halley
238 Bay IRIS instrument. During the daytime it is possible to calculate the non-cutoff riometer
239 absorption using >10 MeV proton fluxes through the empirical relationship of *Kavanagh et al.*
240 [2004], confirmed using the SIC model by *Rodger et al.* [2006]. Here we want to investigate the
241 relationship between proton fluxes and riometer absorption during nighttime conditions in order
242 to investigate rigidity cutoff effects during polar winter conditions.

243 We assume that the proton spectra at the top of the atmosphere will be determined only by the
244 fluxes of experimentally observed proton flux spectra reported by GOES-borne instruments at
245 geosynchronous altitude. The angular distribution of the protons is assumed to be isotropic over
246 the upper atmosphere, which is valid close to the Earth [*Hargreaves*, 1992]. A SIC modeling run
247 has also been undertaken without any proton forcing (i.e., zero proton fluxes), reasonable at
248 Halley for low K_p conditions. The results of the no-forcing "control" SIC-run allow the
249 calculation of "quiet-time" conditions.

250 Each run of the SIC model is based on a neutral background atmosphere given by MSISE-90
251 and provides concentration profiles of neutral and ionic species. Following *Banks and Kockarts*
252 [1973; Part A, p. 194], we calculate the electron collision frequencies of N₂, O₂, and He from
253 MSIS and of O and H from SIC using the neutral temperature profile of MSIS, which we can
254 assume to be equal to electron temperature below 100 km. Electron density is obtained from SIC
255 by subtracting the sum of negative ion concentrations from the sum of positive ion
256 concentrations. Finally, we use the method of *Sen and Wyller* [1960] to compute differential
257 absorption dL/dh and integrate with respect to height. This method takes the operational
258 frequency of the riometer into account and assumes a dipole approximation for the geomagnetic
259 field to obtain the electron gyrofrequency at the respective altitude and latitude.

260 The Sodankylä Ion and Neutral Chemistry (SIC) model is a 1-D chemical model designed for
261 ionospheric D-region studies, solving the concentrations of 65 ions, including 29 negative ions,
262 and 15 neutral species at altitudes across 20–150 km. This study makes use of SIC version 6.9.0.
263 The model has recently been discussed by *Verronen et al.* [2005], building on original work by
264 *Turunen et al.* [1996] and *Verronen et al.* [2002]. A detailed overview of the model was given in
265 *Verronen et al.* [2005]. We summarize here to provide background for this study.

266 In the SIC model several hundred reactions are implemented, plus additional external forcing
267 due to solar radiation (1–422.5 nm), electron and proton precipitation, and galactic cosmic
268 radiation. Initial descriptions of the model are provided by *Turunen et al.* [1996], with neutral
269 species modifications described by *Verronen et al.* [2002]. Solar flux is calculated with the
270 SOLAR2000 model (version 2.27) [*Tobiska et al.*, 2000]. The scattered component of solar
271 Lyman- α flux is included using the empirical approximation given by *Thomas and Bowman*
272 [1986]. The SIC code includes vertical transport [*Chabrillat et al.*, 2002] which takes into
273 account molecular [*Banks and Kockarts*, 1973] and eddy diffusion with a fixed eddy diffusion
274 coefficient profile. The background neutral atmosphere is calculated using the MSISE-90 model

275 [Hedin, 1991] and tables given by Shimazaki [1984]. Transport and chemistry are advanced in
276 intervals of 5 or 15 minutes. While within each interval exponentially increasing time steps are
277 used because of the wide range of chemical time constants of the modeled species.

278 Daytime absorption has been shown to be described by proton fluxes with energies >10 MeV.
279 However, during nighttime conditions the undisturbed D-region has lower electron number
280 densities, such that lower energy protons are expected to play a significant role. Nighttime
281 ionization conditions are more complicated than during the day, with a negative charge transition
282 from electrons to negative ions occurring at sunset [Verronen *et al.*, 2006] as a result of changes
283 in atomic oxygen. Thus we would expect different relationships between absorption and solar
284 proton fluxes at night than during the day. Figure 6 shows the relationship found between SIC
285 calculated polar nighttime riometer absorption and proton fluxes with energies >5 MeV, taken
286 from the proton fluxes which occurred during the January 2005 SPE. These calculations indicate
287 that nighttime absorption is proportional to $(>5 \text{ MeV proton flux})^{0.75}$. This finding differs from
288 the daytime relationship, not only in the power, but also the proton flux threshold. This agrees
289 with previous work on nighttime absorption calculations, which suggested a threshold of 1-5
290 MeV [Sellers *et al.*, 1977], although both day and night calculations in that study used a square
291 root power relationship. A lower threshold of >5 MeV during nighttime means that K_p would
292 have to be lower in order to cutoff the same fraction of the proton fluxes as during the day. The
293 lower energy threshold is also consistent with the riometer absorption coming from higher
294 altitudes during the night than the day.

295 During the period when IRIS data from Halley is available there was one significant SPE in
296 nighttime conditions. In Figure 7 we show the observed and calculated absorption during the
297 large SPE of 13-16 July 2000. The format of the plot is the same as Figures 2-5. To calculate the
298 theoretical absorption values we have used the relation $\text{Absorption} = 0.001 \times (>5 \text{ MeV proton}$
299 $\text{flux})^{0.75}$. The plot shows that the theoretical and observed absorption values agree well, with

300 overestimates in the theoretically predicted absorptions occurring only on the southern
301 (poleward) beam when $K_p > 7$. No significant periods of over estimation occur on the northern
302 (equatorward) beam. Of the eleven 3-hourly bins where proton fluxes are high in Figure 7, five
303 show significant over estimates (~ 0.5 dB) in the predicted absorption in the southern (poleward)
304 beam, while four over estimates occur in the northern (equatorward) beam.

305 Notably there are almost no data points in Figure 7 where either the predicted absorption or the
306 observed absorption reach the same levels as the non-cutoff values during high proton fluxes
307 (mainly 15 July). This is despite very high K_p values, and is partly as a result of the rigidity
308 model limiting K_p to a maximum of 6, and also a result of the >5 MeV energy threshold used
309 during the night. At the latitude of Halley IRIS northern (equatorward) beam the proton cutoff
310 energy limit for $K_p=6$ is ~ 9 MeV [Rodger *et al.*, 2006]. This means that protons with energies
311 >9 MeV will reach to the latitude of this beam, but energies less than that will not be able to
312 make it so far equatorward. During the day, when a >10 MeV proton flux energy threshold for
313 the absorption calculation applies, and the K_p -dependent rigidity cutoff is ~ 9 MeV, 100% of the
314 >10 MeV GOES proton fluxes will penetrate to that location, and thus contribute to the riometer
315 absorption. However, during the night when a >5 MeV proton flux energy threshold applies, and
316 the K_p -dependent rigidity cutoff is ~ 9 MeV, the calculations predict that only ~ 30 -90% of the
317 >5 MeV GOES proton fluxes penetrate to that location and contribute to the riometer absorption.
318 Note that the 30-90% range is determined by the proton spectra, i.e., what percentage of the total
319 proton number flux is greater than the rigidity cutoff energy. Thus at nighttime the only time that
320 the predicted absorption gets close to the non-rigidity cutoff levels is on those occasions when
321 the proton spectrum is very hard, i.e., there are high fluxes of protons with high energy
322 (>10 MeV) in comparison with the lower energy protons (5-10 MeV).

323

324 7. Discussion

325 We have investigated the rigidity cutoff model developed by *Rodger et al.* [2006] based on
326 previous work by *Smart and Shea* [2003]. Using a study of riometer absorption data during four
327 daytime SPEs, i.e., high latitude summer measurements where the Sun is above the horizon all
328 the time, we have shown that it is possible to reproduce the riometer data using a simple
329 empirical relationship based on the incident proton fluxes, and a K_p -limited rigidity calculation.

330 For the southern (poleward) beam of the Halley IRIS $K_p=6$ represents a rigidity cutoff energy of
331 0.0 MeV, and once $K_p=6$ is reached the predicted absorption is the same as the non-rigidity
332 absorption levels. This can be seen in Figure 3 at the beginning of 27 Nov 2000, where the
333 asterisks (rigidity calculation) overlap the short dashed line values (non-rigidity calculation).
334 However, the observed absorption is not consistent with this picture, and when $K_p>4$ the
335 predicted absorption is also over estimated. This suggests that the rigidity cutoff limit ($K_p=6$,
336 0.0 MeV for the southern beam) needs to be higher than the proton flux energy threshold
337 (10 MeV in daytime). Either decreasing the K_p "saturation" limit, or lowering the proton flux
338 energy threshold can achieve this.

339 During the two large SPEs, when K_p approached 9, the southern (poleward) beam absorption
340 was close to that of the calculated rigidity and non-rigidity cutoff absorption levels (Figures 4
341 and 5), whereas this was not true when $K_p=4-6$ in the previous analysis. This clearly indicates
342 that the $K_p=6$ saturation limit to the rigidity cutoff model is too low and needs to be higher.

343 For the northern (equatorward) beam of the Halley IRIS $K_p=6$ represents a rigidity cutoff
344 energy of 9 MeV, thus the rigidity cutoff energy and the proton flux energy threshold (10 MeV)
345 are similar, and when $K_p=6$ is reached the predicted absorption values are the same as the non-
346 rigidity levels. However, the observed absorption does not reach the non-rigidity level during
347 high proton fluxes, and as a result this suggests that the $K_p=6$ saturation limit is too high or the
348 absorption threshold is too high.

349 Absorption data from the single nighttime SPE (July 2000) is reasonably modeled using a
350 >5 MeV proton flux energy threshold. The behavior of the observed absorption on the southern
351 (poleward) beam is very similar to the daytime examples in that the predicted absorption is over
352 estimated when $K_p \geq 6$. This is because at $K_p = 6$ the rigidity cutoff energy is 0.0 MeV which is
353 lower than the proton flux energy threshold of >5 MeV. The northern (equatorward) beam
354 behavior is slightly different from the daytime case because for $K_p = 6$ the rigidity cutoff energy
355 (9 MeV) is more than the proton flux energy threshold (>5 MeV), and thus although the
356 predicted absorption is still an overestimate at high K_p , it is not as large as the maximum non-
357 cutoff case.

358 Using the rigidity cutoff model of *Rodger et al.* [2006] and empirical estimates of riometer
359 absorption from proton fluxes we have been able to reproduce the absorption seen by the Halley
360 riometer at two L -shells ($L=4.32$ and 4.80). Typically reasonable estimates of absorption were
361 made 58-74 % of the time for the southern (poleward) beam, and 65-87 % of the time for the
362 northern (equatorward) beam. The success of the *Rodger et al.* [2006] rigidity cutoff model is
363 dependent on a balance between the rigidity cutoff energy for the protons at any given L -shell,
364 and the proton flux energy threshold for the protons. At the times when the empirical estimates
365 are in error there is usually an over estimate in the predicted absorption levels, caused by the
366 $K_p = 6$ saturation limit used in the rigidity cutoff calculation. In order to improve the success rate
367 for the northern (equatorward) beam the K_p saturation limit in the rigidity model would have to
368 be decreased to $K_p = 5.5$ or the daytime proton flux energy threshold decreased to >5 MeV. For
369 the southern beam changing the K_p saturation limit to 5 would be more appropriate, but no
370 changes of the daytime proton flux energy threshold would make any significant effect.

371 Changing the proton flux energy threshold introduces significant difficulties in modeling the
372 riometer absorption because of hysteresis in the relationship between the proton fluxes and
373 absorption for any proton flux energy threshold values other than 10 MeV during the day and

374 5 MeV during the night. Thus we restrict ourselves here to investigate the effects of the K_p
375 saturation limit used in the rigidity cutoff calculation. Figure 8 shows the northern and southern
376 beam absorption during the solar proton event of 05-08 November 2001. The figure is the same
377 format as Figure 4, except that the saturation limit has been changed to $K_p=5$, and the location of
378 the southern (poleward) beam moved by 0.6° equatorwards. These changes have the effect of
379 increasing the rigidity cutoff energy for the northern beam from 9 MeV to 28 MeV, and
380 increasing the rigidity cutoff energy for the southern beam from 0.0 MeV to 8 MeV. In practice
381 this means that the northern beam does not achieve the non-rigidity cutoff absorption maximum
382 during this storm, in agreement with the observations. Generally the Halley northern
383 (equatorward) beam will not achieve the non-rigidity cutoff absorption maximum unless the
384 proton spectrum is very hard and has little flux between 10-28 MeV. The southern beam will still
385 experience absorption at the non-cutoff maximum, but the more equatorward location of the
386 beam results in lower levels of absorption when K_p is just below the saturation limit. Both of
387 these effects result in much better agreement between the calculated absorption and the observed
388 absorption for this large geomagnetic storm in comparison with the results shown in Figure 4.

389 However, for moderately disturbed solar proton events, where K_p remains close to the
390 saturation limit the calculated absorption is not in such good agreement with the observations.
391 Figure 9 shows the adjusted absorption for the 26-29 November 2000 period to be contracted
392 with Figure 3. The $K_p=5$ saturation limit has reduced the northern beam absorption, and reduced
393 the southern beam absorption when K_p is close to the $K_p=5$ saturation limit. However, during
394 higher K_p the southern beam does not experience the maximum non-rigidity cutoff absorption
395 levels that the relocated beam calculations predict. Overall there is a 50% decrease in the number
396 of 3-hour data bins that previously showed poor agreement between the calculated and observed
397 absorption.

398 The adjustments to the rigidity cutoff calculations made here are relatively subtle. By changing
399 the location of the southern (poleward) beam better agreement between theory and observations
400 is obtained at times, and this indicates that initially the two beam locations were too far apart
401 (i.e., smaller than the 2° of latitude assumed initially). The adjusted location for the southern
402 (poleward) beam represents a separation from the northern beam of 1.4° of latitude, which can be
403 interpreted as indicating that the dominant altitude that the absorption is occurring at lower
404 altitude i.e., 60 km instead of the 90 km initially assumed. The lower K_p saturation limit
405 improves the agreement between theory and observations, particularly on the northern
406 (equatorward) beam during most geomagnetic conditions. The K_p change has little effect on the
407 southern (equatorward) beam, which appears more sensitive to changes in beam location. This
408 suggests that at $L > 4.5$, and for high K_p , significant changes in L -shell location have occurred for
409 the beam, in particular that the geographic location of the beam has moved to a lower L -shell.
410 Some of this change can be accommodated by the lowering of the peak absorption altitude of the
411 southern beam, which equates to a shift equatorwards for this riometer beam as K_p increases and
412 greater latitudinal penetration of proton fluxes occur.

413 For large geomagnetic storms, such as that of 05-08 November 2001, the adjustments made
414 here to the *Rodger et al.* [2006] rigidity cutoff model allow us to improve the absorption
415 estimates. In Figure 10 we plot the predicted southern hemisphere absorption levels during the
416 high proton flux period that occurred at 00 UT on 06 Nov 2001, when K_p reached 8^+ . This
417 calculation was undertaken using the improved rigidity cutoff model. The plot shows the region
418 of high absorption with levels of 14 dB, where all protons with energies greater than 10 MeV can
419 access the polar atmosphere (i.e., rigidity cutoff effects are unimportant to the riometer
420 absorptions). Surrounding this contour is an outer region where the absorption levels gradually
421 reduce to the limits of detectability for most riometers (roughly 0.1 dB). This can be thought of

422 as an extreme example of SPE-produced riometer absorptions, occurring when both K_p and
423 proton fluxes are very high. The outer zone of rigidity influenced absorption lies mostly at 50°S ,
424 except in the region of the Antarctic Peninsula where it is located at $\sim 70^\circ\text{S}$. From the riometer
425 absorption calculations we can see that the transition in access levels for energetic protons to the
426 stratosphere and mesosphere is controlled by geomagnetic rigidity, with the shift from no-access
427 to total access occurs over the range $L=3-4.5$, or across $\sim 10^\circ$ of latitude. For locations which are
428 equatorward of the limits of the outer zone shown in Figure 10, SPEs should never lead to
429 significant changes in riometer data. This provides an indication as to the limits inside which
430 SPEs can play a role in modifying the neutral chemistry of the stratosphere and mesosphere
431 [Verronen, 2005].

432

433 **8. Summary**

434 In the polar atmosphere, significant chemical and ionization changes occur during solar proton
435 events. The access of solar protons to this region is limited by the dynamically changing
436 geomagnetic field. In this study we have used riometer absorption observations to investigate the
437 accuracy of a model to predict K_p -dependent geomagnetic rigidity cutoffs, and hence the
438 changing proton fluxes. The imaging riometer at Halley, Antarctica is ideally situated for such a
439 study, as the rigidity cutoff sweeps back and forth across the instrument's field of view,
440 providing a severe test of the rigidity cutoff model. Specifically we investigate the accuracy of
441 the rigidity cutoff model developed by Smart and Shea [2003], and improved by Rodger et al.
442 [2006]. Using observations from the Halley riometer during five solar proton events, we have
443 confirmed the basic accuracy of this rigidity model. However, we have shown that although the
444 rigidity cutoff model can be used to reasonably estimate the absorption due to precipitating
445 proton fluxes, it can be further improved by setting a lower K_p limit (i.e. $K_p=5$ instead of 6) at

446 which the rigidity process saturates. We also find that for $L > 4.5$ there is significant change in the
447 geomagnetic location of a riometer beam during a large geomagnetic storm, such that the
448 apparent L -shell of the beam moves equatorward. This is in part explained by the decreasing
449 altitude of peak riometer absorption as protons penetrate more readily at higher K_p into the
450 rigidity dominated zone.

451 We have also used the Sodankyla Ion and Neutral Chemistry model to determine an empirical
452 relationship between integral proton precipitation fluxes and nighttime ionosphere riometer
453 absorption, in order to allow consideration of winter time SPEs. We find that during the
454 nighttime the proton flux energy threshold is lowered to protons with energies of >5 MeV in
455 comparison with >10 MeV during the daytime.

456 Where both K_p and proton fluxes are very high the transition in access levels for energetic
457 protons to the stratosphere and mesosphere is controlled by geomagnetic rigidity, with the shift
458 from no-access to total access occurs over the range $L=3-4.5$, or across $\sim 10^\circ$ of latitude. The
459 outer zone of rigidity influenced absorption lies mostly at 50°S , except in the region of the
460 Antarctic Peninsula where it is located at $\sim 70^\circ\text{S}$. In the northern hemisphere this will equate to
461 $\sim 45^\circ\text{N}$. These latitude bounds provide an indication as to the limits inside which SPEs can play a
462 role in modifying the neutral chemistry of the stratosphere and mesosphere.

463

464 **Acknowledgments.** CJR and MAC would like to thank Lauren Farnden of Dunedin for her
465 support. This research was supported by the New Zealand International Science and Technology
466 (ISAT) Linkages Fund. The Halley IRIS system was funded in part by a grant from the National
467 Science Foundation to the University of Maryland, and by the Natural Environment Research
468 Council (NERC).

469

469 **References**

- 470 Banks, P. M., and G. Kockarts, *Aeronomy*, vol. B, chap. 15, Academic Press, 1973.
- 471 Birch, M. J., J. K. Hargreaves, A. Senior, and B. J. I. Bromage (2005), Variations in cutoff
472 latitude during selected solar energetic proton events, *J. Geophys. Res.*, 110, A07221,
473 doi:10.1029/2004JA010833.
- 474 Boberg, P. R. Jr., E. O. Flückiger, and E. Kobel, Geomagnetic transmission of solar energetic
475 protons during the geomagnetic disturbances of October 1989, *Geophys. Res. Lett.*, 22(9),
476 1133-1136, 10.1029/95GL00948, 1995.
- 477 Chabrillat, S., G. Kockarts, D. Fonteyn, and G. Brasseur, Impact of molecular diffusion on the
478 CO₂ distribution and the temperature in the mesosphere, *Geophys. Res. Lett.*, 29, 1-4, 2002.
- 479 Hargreaves, J. K., *The solar-terrestrial environment*, Atmospheric and Space Science Series,
480 Cambridge University Press, Cambridge, UK, 1992.
- 481 Hargreaves, J. K., and M. J. Jarvis, The multiple riometer system at Halley, Antarctica, *British*
482 *Antarctic Surv. Bull.*, 72, 13-23, 1986.
- 483 Hedin, A. E., Extension of the MSIS Thermospheric model into the middle and lower
484 Atmosphere, *J. Geophys. Res.*, 96, 1159-1172, 1991.
- 485 Kavanagh, A. J., S. R. Marple, F. Honary, I. W. McCreia, and A. Senior , On solar protons and
486 polar cap absorption: constraints on an empirical relationship, *Ann. Geophys.*, 22(4), 1133-
487 1147, 2004.
- 488 Kress B. T., M. K. Hudson, K. L. Perry, and P. L. Slocum, Dynamic modeling of geomagnetic
489 cutoff for the 23–24 November 2001 solar energetic particle event, *Geophys. Res. Lett.*, 31,
490 L04808, doi:10.1029/2003GL018599, 2004.
- 491 Krishnaswamy, S., D. L. Detrick, and T. J. Rosenberg, The inflection point method of
492 determining riometer quiet day curves, *Radio Sci.*, 20, 123-136, 1985.

- 493 Little, C. G, and H. Leinbach, The riometer - a device for the continuous measurement of
494 ionospheric absorption, *Proceedings of the IRE*, 47, 315-319, 1959.
- 495 Ogliore, R. C., R. A. Mewaldt, R. A. Leske, E. C. Stone, and T. T. von Rosenvinge, A direct
496 measurement of the geomagnetic cutoff for cosmic rays at space station latitudes, *Proceedings*
497 *of ICRC 2001*, 4112-4115, Copernicus Gesellschaft, 2001.
- 498 Rodger, C. J., M. A. Clilverd, P. T. Verronen, Th. Ulich, M. J. Jarvis, and E. Turunen, Dynamic
499 geomagnetic rigidity cutoff variations during a solar proton event, *J. Geophys. Res.*, 111,
500 A04222, doi:10.1029/2005JA011395, 2006.
- 501 Rose, M. C., M. J. Jarvis, M. A. Clilverd, D. J. Maxfield, and T. J. Rosenberg, The effect of
502 snow accumulation on imaging riometer performance, *Radio Sci.*, 35, 1143-1153, 2000.
- 503 Selesnick, R. S., A. C. Cummings, J. R. Cummings, R. A. Mewaldt, E. C. Stone, and T. T. von
504 Rosenvinge, Geomagnetically trapped anomalous cosmic rays, *J. Geophys. Res.*, 100, 9503-
505 9518, 1995.
- 506 Sellers, B., F. A. Hanser, M. A. Stroschio, and G. K. Yates (1997), The night and day
507 relationships between polar cap riometer absorption and solar protons, *Radio Sci.*, 12, 779-
508 789.
- 509 Sen, H. K., and A. A. Wyller, On the generalization of the Appleton-Hartree magnetoionic
510 formulas, *J. Geophys. Res.*, 65, 3931-3950, 1960.
- 511 Shimazaki, T., *Minor Constituents in the Middle Atmosphere (Developments in Earth and*
512 *Planetary Physics, No 6)*, D. Reidel Publishing Co., Dordrecht, Netherlands, 1984.
- 513 Shirochkov, A., L. N. Makarova, S. N. Sokolov, and W. R. Sheldon (2004), Ionospheric effects
514 of the simultaneous occurrence of a solar proton event and relativistic electron precipitation as
515 recorded by ground-based instruments at different latitudes, *J. Atmos. Sol. Terr. Phys.*, 66,
516 1035– 1045.

- 517 Smart, D. F., and M. A. Shea, Geomagnetic cutoffs - a review for space dosimetry applications,
518 *Adv. Space Res.*, 14(10), 787-796, 1994.
- 519 Smart, D. F., and M. A. Shea, Comparison of the Tsyganenko model predicted and measured
520 geomagnetic cutoff latitudes, *Adv. Space Res.*, 28(12), 1733-1738, 2001.
- 521 Smart, D. F., and M. A. Shea, The space developed dynamic vertical cutoff and its applicability
522 to aircraft radiation dose, *Adv. Space Res.*, 32(1), 103-108, 2003.
- 523 Smart, D. F., M. A. Shea, M. J. Golightly, M. Weyland, and A. S. Johnson, Evaluation of the
524 dynamic cutoff rigidity model using dosimetry data from the STS-28 flight, *Adv. Space Res.*,
525 31(4), 841-846, 2003.
- 526 Stauning, P., Ionospheric investigations using imaging riometer observations, in *Review of Radio*
527 *Science 1993-1996*, edited by W. R. Stone, pp. 157-161, Oxford Univ. Press, Oxford,
528 England, 1996.
- 529 Thomas, L., and M. R. Bowman, A study of pre-sunrise changes in negative ions and electrons in
530 the D-region, *J. Atmos. Terr. Phys.*, 4, 219, 1986.
- 531 Tobiska, W. K., T. Woods, F. Eparvier, R. Viereck, L. D. B. Floyd, G. Rottman, and O. R.
532 White, The SOLAR2000 empirical solar irradiance model and forecast tool, *J. Atmos. Terr.*
533 *Phys.*, 62, 1233-1250, 2000
- 534 Tsyganenko, N. A., Determination of magnetospheric current system parameters and
535 development of experimental geomagnetic models based on data from IMP and HEOS
536 satellites, *Planet. Space Sci.*, 37, 5-20, 1989.
- 537 Turunen, E., H. Matveinen, J. Tolvanen, and H. Ranta, D-region ion chemistry model, in *STEP*
538 *Handbook of Ionospheric Models*, edited by R. W. Schunk, pp. 1-25, SCOSTEP Secretariat,
539 Boulder, Colorado, USA, 1996.

540 Verronen, P. T., E. Turunen, Th. Ulich, and E. Kyrölä, Modelling the effects of the October 1989
541 solar proton event on mesospheric odd nitrogen using a detailed ion and neutral chemistry
542 model, *Ann. Geophys.*, 20, 1967-1976, 2002.

543 Verronen, P. T., A. Seppälä, M. A. Clilverd, C. J. Rodger, E. Kyrölä, C.-F. Enell, Th. Ulich, and
544 E. Turunen, Diurnal variation of ozone depletion during the October-November 2003 solar
545 proton event, *J. Geophys. Res.*, 110(A9), doi:10.1029/2004JA010932, 2005.

546 Verronen, P. T., Th. Ulich, E. Turunen, and C. J. Rodger (2006), Sunset transition of negative
547 charge in the D-region ionosphere during high-ionization conditions, *Ann. Geophys.*, 24, 187-
548 202.

549

550 _____

551 M. A. Clilverd and T. Moffat-Griffin, Physical Sciences Division, British Antarctic Survey,
552 High Cross, Madingley Road, Cambridge CB3 0ET, England, U.K. (e-mail: macl@bas.ac.uk;
553 tmof@bas.ac.uk)

554 C. J. Rodger, Department of Physics, University of Otago, P.O. Box 56, Dunedin, New
555 Zealand. (email: crodger@physics.otago.ac.nz).

556 P. T. Verronen, Earth Observation, Finnish Meteorological Institute, P.O. Box 503 (Erik
557 Palménin aukio 1), FIN-00101 Helsinki, Finland. (email: pekka.verronen@fmi.fi).

558

559 CLILVERD ET AL.: IMPROVED RIOMETER RIGIDITY CUTOFFS

560

561

561 **Figure 1.** Map showing the region in Antarctica in which our study is undertaken. The square
 562 marks the location of Halley (75.6°S, 26.32°W, $L=4.6$), while the open circles show the northern
 563 (equatorward) and southern (poleward) IRIS riometer beams used in our study.

564 **Figure 2.** [Upper panel] The variation of the non-cutoff absorption that would be expected if
 565 there were no influence of rigidity on the proton fluxes into the atmosphere (short dashed line)
 566 during 08-11 November 2000, compared with the observed absorption on the Halley IRIS
 567 southernmost beam 1 ($L=4.80$, solid line). [middle panel] The variation of the non-cutoff
 568 absorption as in the upper panel (short dashed line), compared with the observed absorption on
 569 the northernmost beam 7, ($L=4.32$, long dashed line). The equivalent absorption levels using
 570 rigidity affected proton fluxes for each beam location are also shown (asterisk in the south,
 571 diamond in the north). [bottom panel] The variation of K_p during the SPE period. The horizontal
 572 dotted line represents the K_p saturation limit used in the rigidity model calculations.

573 **Figure 3.** As Figure 2 but for 26-29 November 2000

574 **Figure 4.** As Figure 2 but for 05-08 November 2001

575 **Figure 5.** As Figure 2 but for 28-31 October 2000

576 **Figure 6.** Comparison between the SIC calculated nighttime cosmic noise absorption for the
 577 Halley IRIS parameters and >5 MeV proton fluxes (crosses). The grey columns indicate the
 578 number of samples in each energy range (as labeled). A linear fit indicates a clear relationship
 579 between the riometer absorption and the proton fluxes.

580 **Figure 7.** As Figure 2, but using the nighttime empirical absorption/proton flux relationship for
 581 the wintertime SPE, 13-16 July 2000.

582 **Figure 8.** As Figure 2, but using $K_p=5$ instead of $K_p=6$ as the cutoff limit for 05-08 November
 583 2001, and with the southern (equatorward) beam moved to a lower L -shell.

584 **Figure 9.** As Figure 2, but using $K_p=5$ instead of $K_p=6$ as the cutoff limit for 26-29 November
 585 2000, and with the southern (equatorward) beam moved to a lower L -shell.

586 **Figure 10.** Map of the predicted levels of absorption globally for the peak fluxes during 06 Nov
587 2001 based on the improved K_p -dependent geomagnetic rigidity cutoff model.

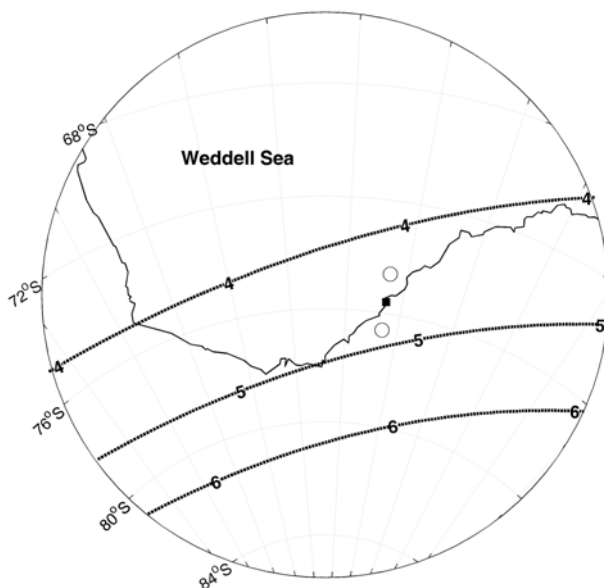
588

589

589

590

591



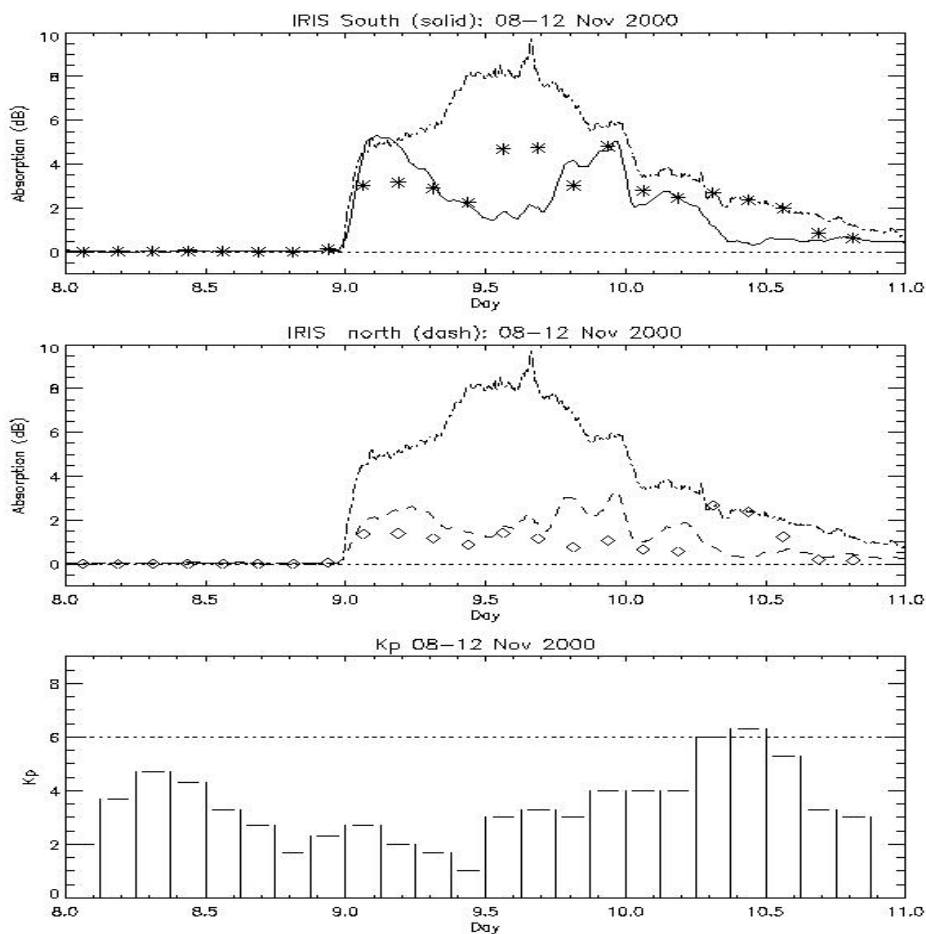
592

593 **Figure 1.** Map showing the region in Antarctica in which our study is undertaken. The square
594 marks the location of Halley (75.6°S , 26.32°W , $L=4.6$), while the open circles show the northern
595 (equatorward) and southern (poleward) IRIS riometer beams used in our study.

596

597

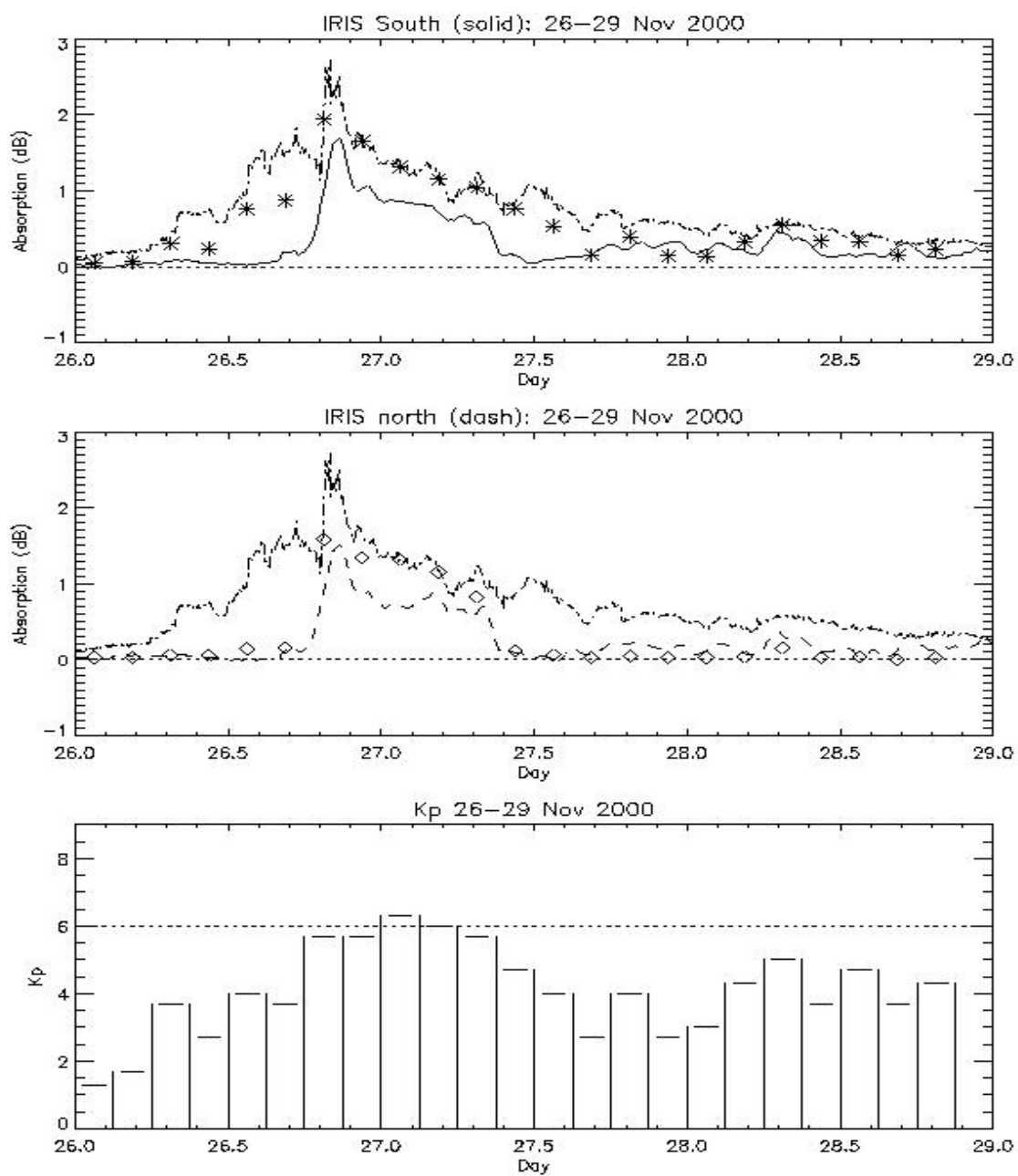
597



598

599 **Figure 2.** [Upper panel] The variation of the non-cutoff absorption that would be expected if
 600 there were no influence of rigidity on the proton fluxes into the atmosphere (short dashed line)
 601 during 08-11 November 2000, compared with the observed absorption on the Halley IRIS
 602 southernmost beam 1 ($L=4.80$, solid line). [middle panel] The variation of the non-cutoff
 603 absorption as in the upper panel (short dashed line), compared with the observed absorption on
 604 the northernmost beam 7, ($L=4.32$, long dashed line). The equivalent absorption levels using
 605 rigidity affected proton fluxes for each beam location are also shown (asterisk in the south,
 606 diamond in the north). [bottom panel] The variation of K_p during the SPE period. The horizontal
 607 dotted line represents the K_p saturation limit used in the rigidity model calculations.

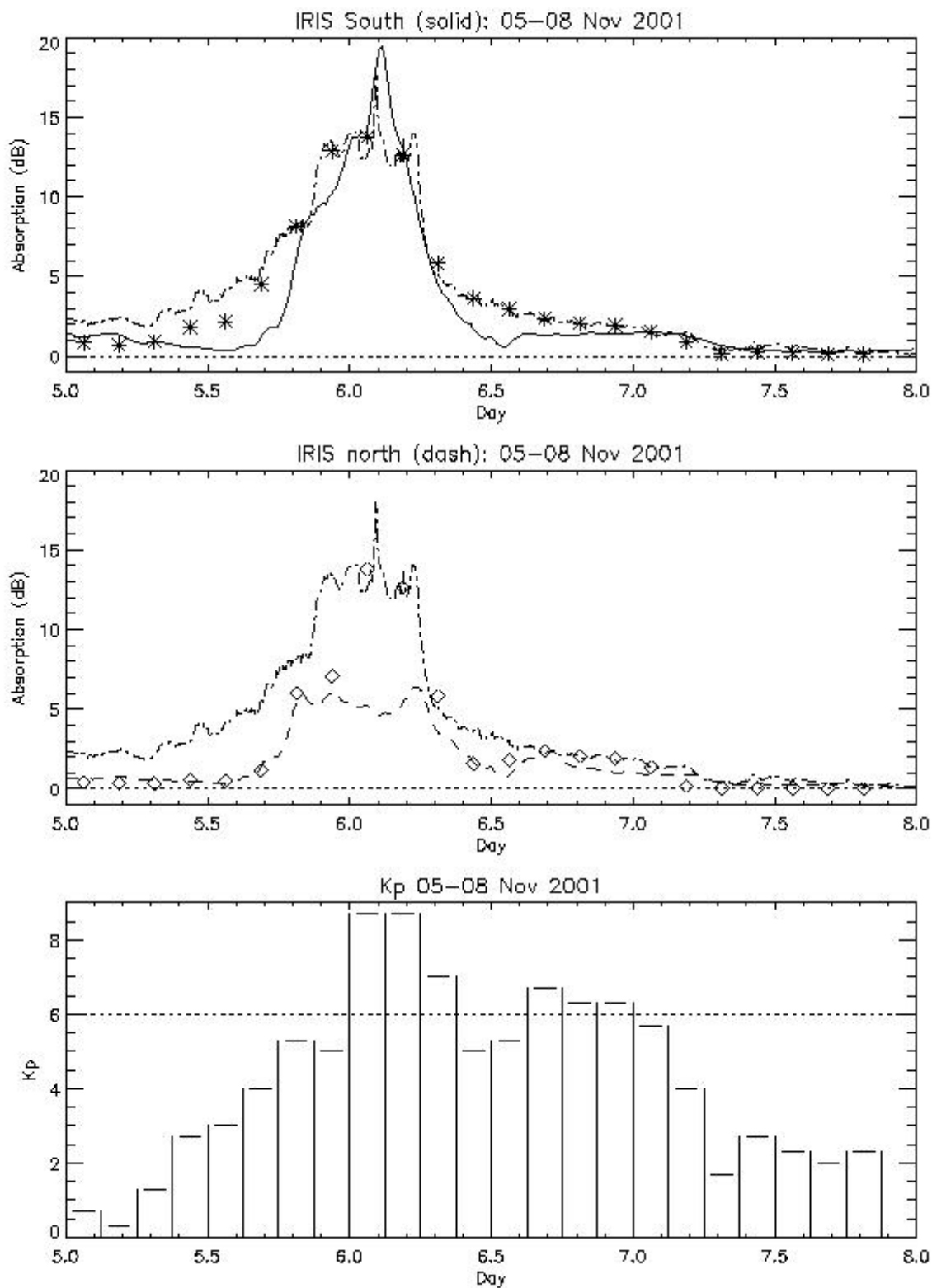
608



609

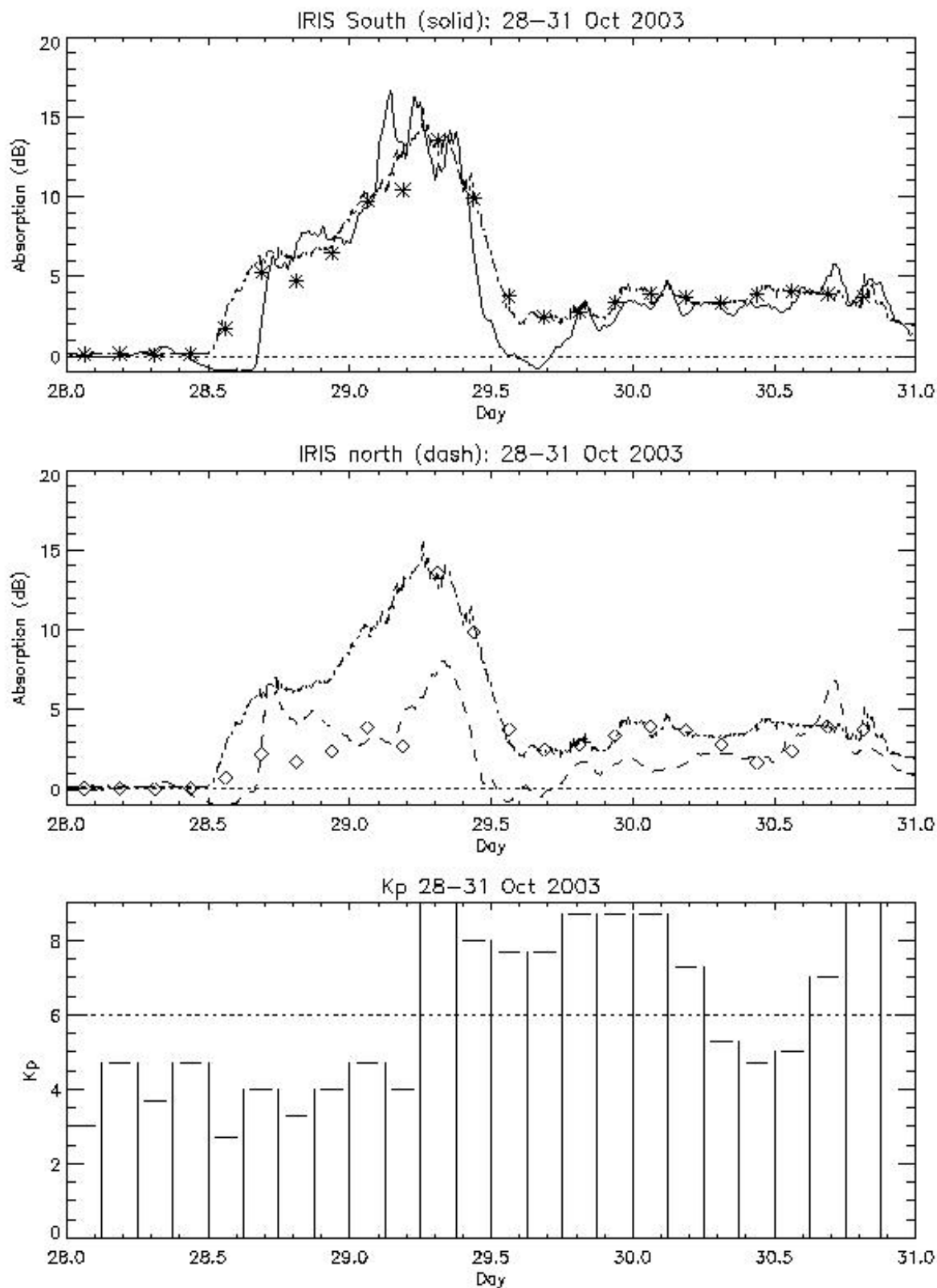
610 **Figure 3.** As Figure 2 but for 26-29 November 2000.

611



611
612

613 **Figure 4.** As Figure 2 but for 05-08 November 2001

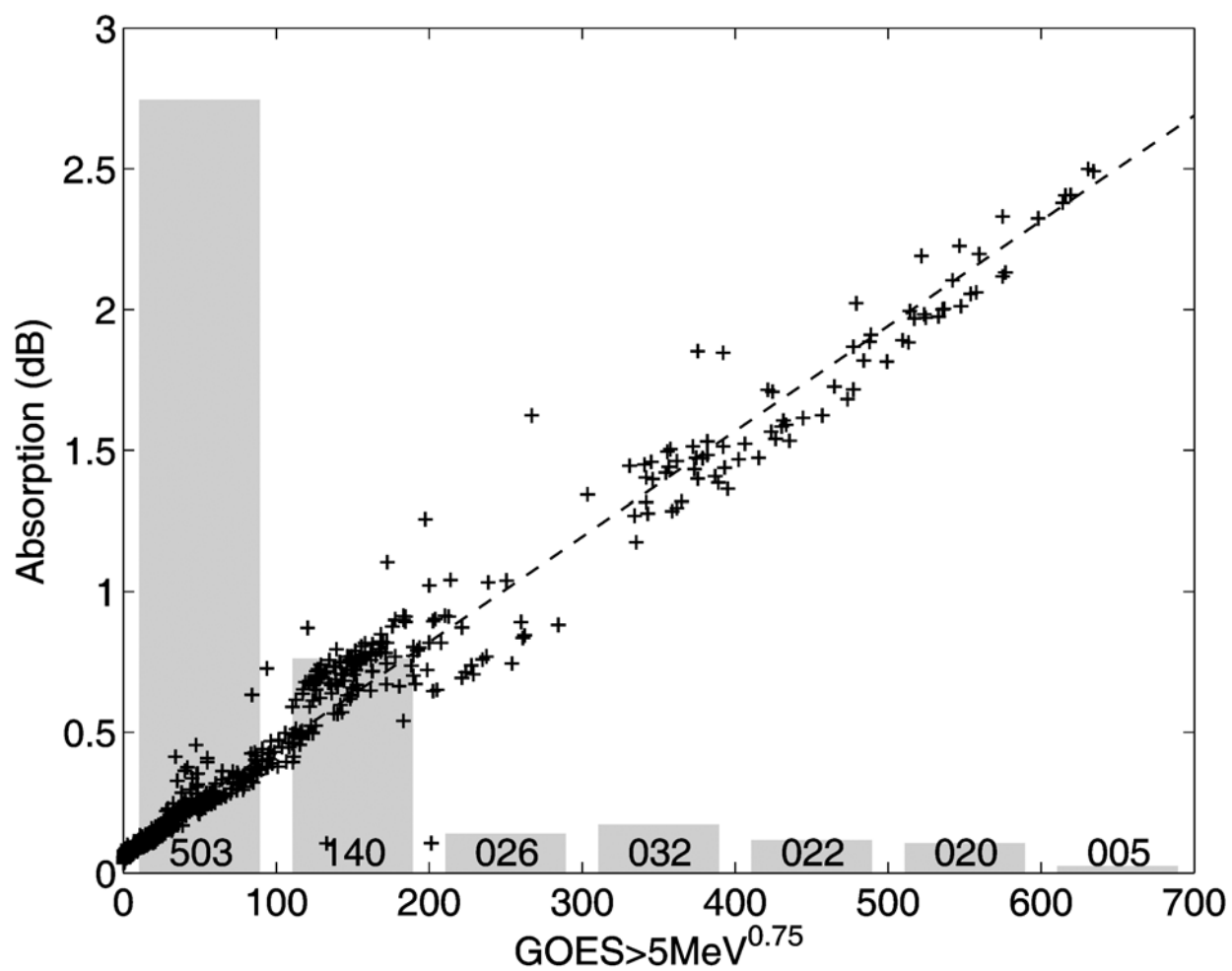


614

615 **Figure 5.** As Figure 2 but for 28-31 October 2003.

616

616

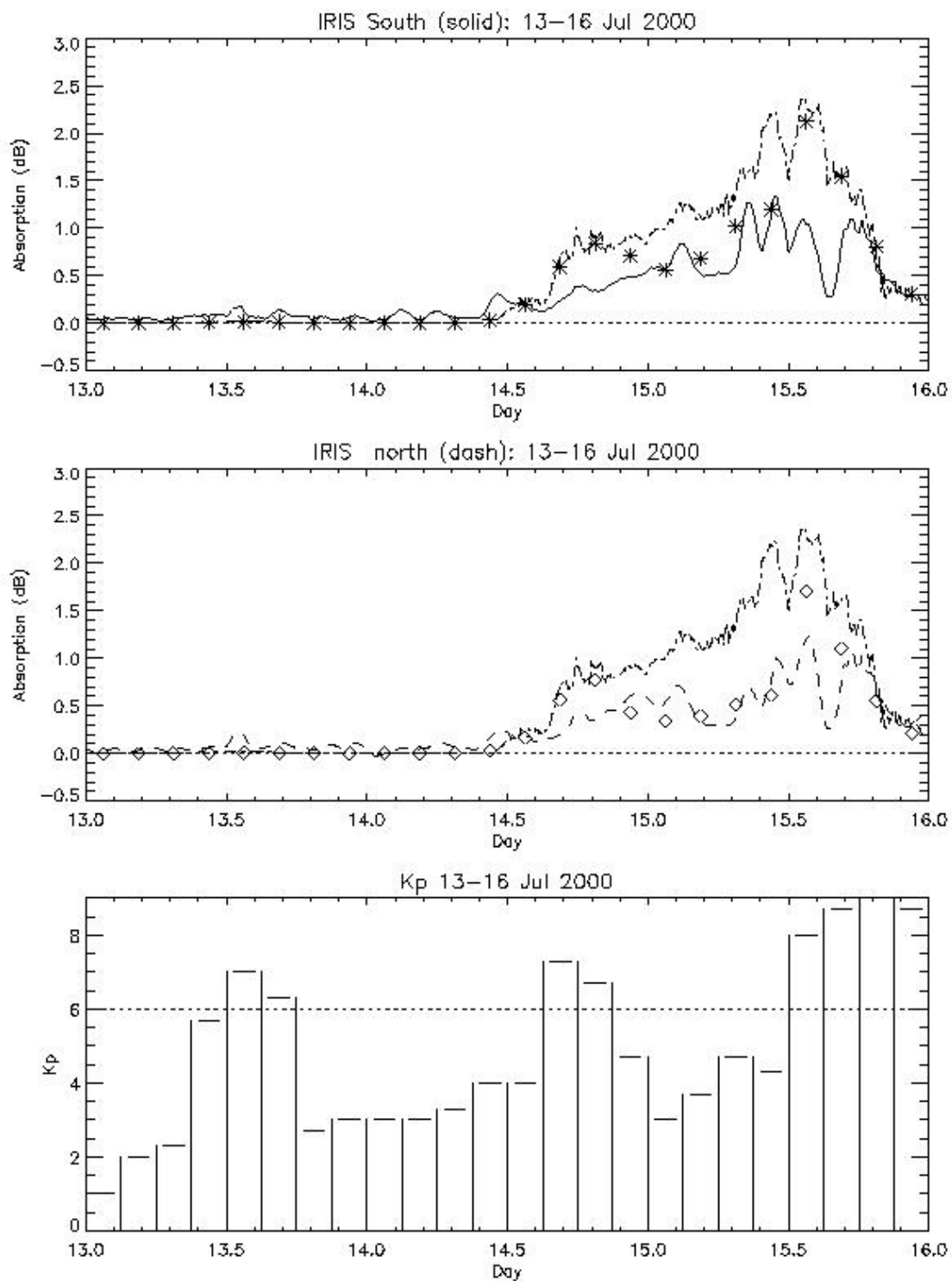


617

618 **Figure 6.** Comparison between the SIC calculated nighttime cosmic noise absorption for the
 619 Halley IRIS parameters and >5 MeV proton fluxes (crosses). The grey columns indicate the
 620 number of samples in each energy range (as labeled). A linear fit indicates a clear relationship
 621 between the riometer absorption and the proton fluxes.

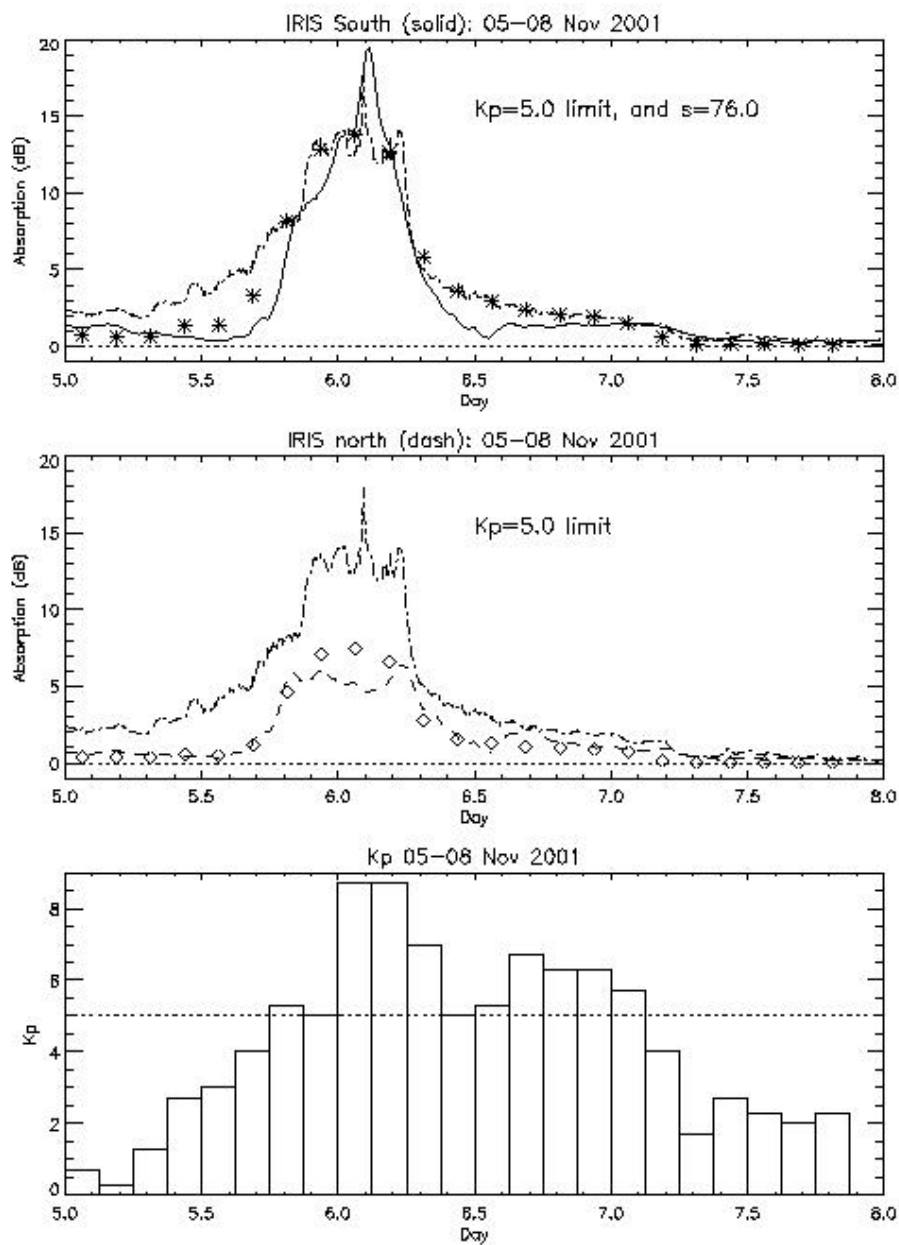
622

623



624

625 **Figure 7.** As Figure 2, but using the nighttime empirical absorption/proton flux relationship for
 626 the wintertime SPE, 13-16 July 2000.

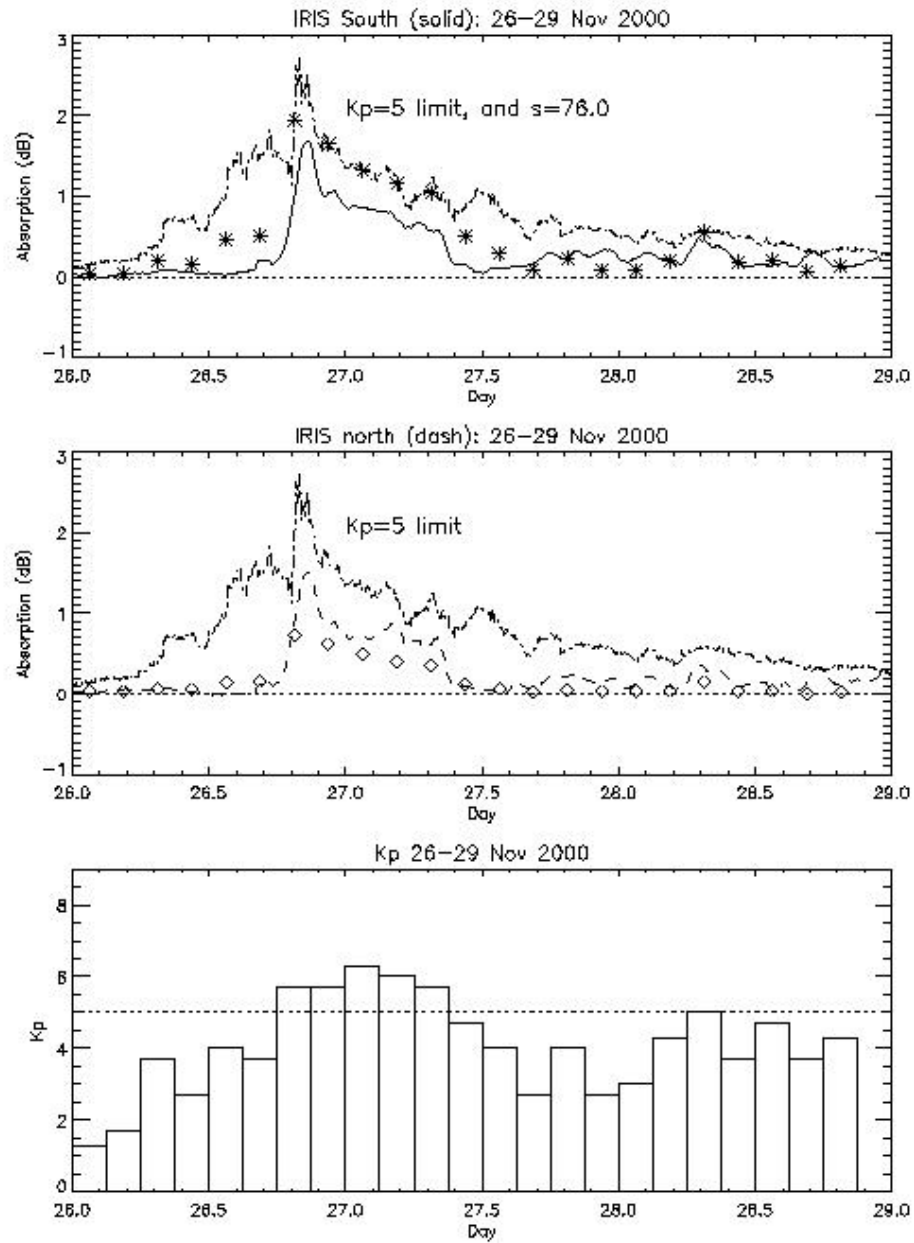


627

628 **Figure 8.** As Figure 2, but using $K_p=5$ instead of $K_p=6$ as the cutoff limit for 05-08 November

629 2001, and with the southern (equatorward) beam moved to a lower L -shell.

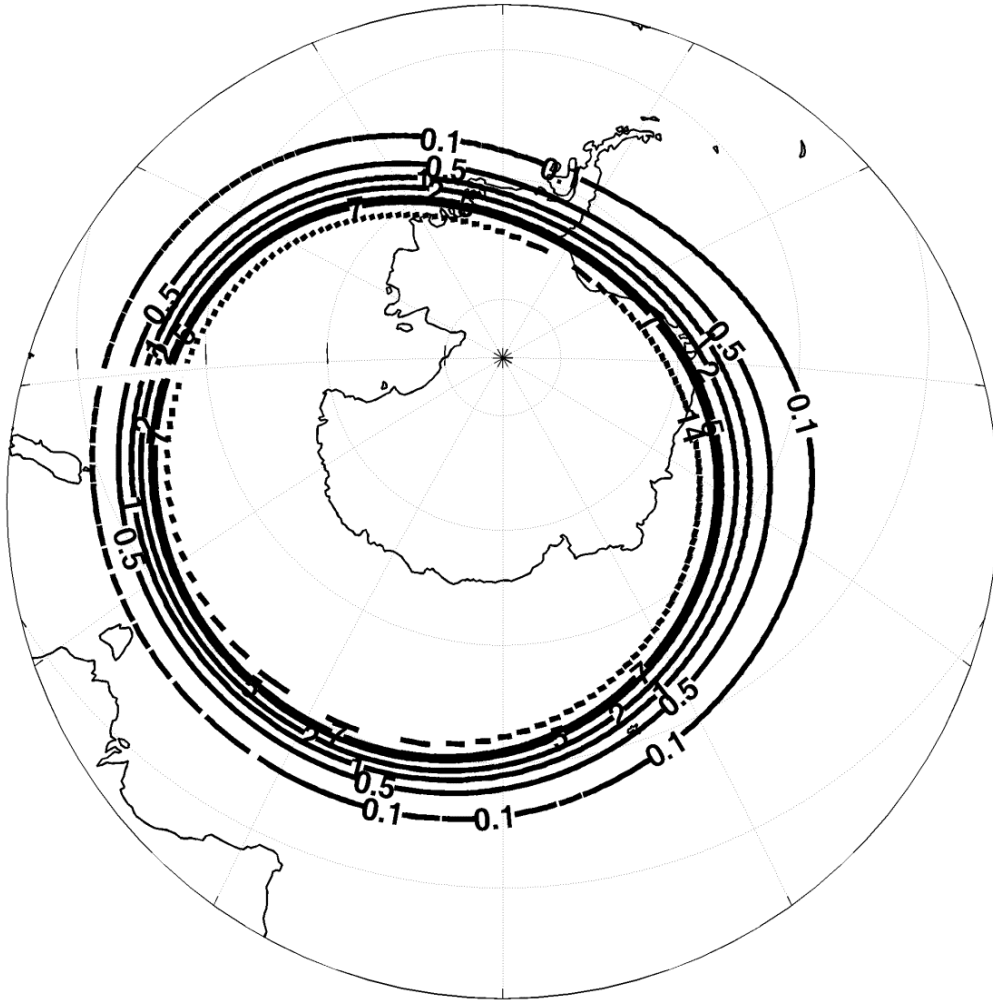
630



630

631 **Figure 9.** As Figure 2, but using $K_p=5$ instead of $K_p=6$ as the cutoff limit for 26-29 November632 2000, and with the southern (equatorward) beam moved to a lower L -shell.

633

6 Nov 2001 0UT, Peak Daytime Riometer absorptions: $K_p=8.70$ 

633

634 **Figure 10.** Map of the predicted levels of absorption globally for the peak fluxes during 06 Nov635 2001 based on the improved K_p -dependent geomagnetic rigidity cutoff model.