doi:10.1088/0953-8984/21/3/035109

The structure of calcium metaphosphate glass obtained from x-ray and neutron diffraction and reverse Monte Carlo modelling

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Received 8 October 2008, in final form 12 November 2008 Published 10 December 2008 Online at stacks.iop.org/JPhysCM/21/035109

Abstract

The short range structure of $(CaO)_{0.5}(P_2O_5)_{0.5}$ glass has been studied using x-ray and neutron diffraction and modelled using the reverse Monte Carlo method. Using this combination of techniques has allowed six interatomic correlations to be distinguished and fitted to obtain a set of bond lengths and coordination numbers that describe the structure of the glass. The glass consists of metaphosphate chains of phosphate tetrahedra and each phosphate unit has two non-bridging oxygen atoms available for coordination with Ca. The Ca–O correlation was fitted with two peaks at 2.35 and 2.86 Å, representing a broad distribution of bond lengths. The total Ca–O coordination is 6.9 and is consistent with distorted polyhedral units such as capped octahedra or capped trigonal prisms. It is found that most non-bridging oxygen atoms are bonded to two calcium atoms. All of these observations are consistent with Hoppe's model for phosphate glasses. Furthermore, the medium range order is revealed to consist of phosphate chains intertwined with apparently elongated clusters of Ca ions, and the Ca–O and Ca–P correlations contributed significantly to the first sharp diffraction peak in x-ray diffraction.

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(Some figures in this article are in colour only in the electronic version)

1. Introduction

Historically, phosphate glasses had limited applications due to their poor durability, but the discovery in recent decades of a number of durable phosphate glasses has motivated many further studies [1]. Phosphate glasses are versatile because their properties can be tailored by altering their composition. This adaptability has enabled them to be used in lasers and optical systems [2], sensors, solid-state batteries, hermetic seals [3, 4], and biomaterials [5, 6]. Current developments in biomaterials are aimed at making them degrade and play an active role in tissue regeneration. Phosphate glasses have been found to be suitable candidates as they completely dissolve in aqueous media at a rate that can be controlled by the chemistry of the glass [5]. It is also possible to include ions routinely found in the human body that would be released when the glass was dissolved and then used to help rebuild the hard or soft tissue.

In particular, calcium phosphates have been under study as biocompatible glasses, glass ceramics and fibres due to their chemical similarity to the hydroxyapatite found in bone [7–10]. It has been found that the properties of these glasses are more highly dependant on the local atomic environment of calcium than on the phosphate network [1]. It is therefore important to understand the local structure of the calcium in glasses from the calcium phosphate system.

The primary features of the phosphate network in phosphate glasses were explained in an influential model by Van Wazer [11]. This is based on the PO_4 tetrahedra having two types of oxygen atoms, bridging oxygen (O_b) and non-bridging oxygen (O_{nb}) . A fully polymerized phosphate network has three O_b atoms and one O_{nb} atom per phosphate tetrahedra. When a network-modifier cation, such as Ca, is added to the network, the proportion of O_{nb} increases at the expense of O_b . Important refinements of this model have been added by Hoppe [12]. The network modifier coordinates

with O_{nb} atoms, and the coordination of the cation with multiple phosphate tetrahedra leads to an effect called a repolymerization. The system stabilizes when all the O_{nb} atoms are coordinated with one network-modifier cation. When the concentration of modifier cations is increased further their coordination with O_{nb} atoms increases leading to a drastic change in the glass properties around 20 mol% divalent metal oxide. This model is extended to describe the structure of less polymerized networks such as metaphosphates.

The present study concerns the calcium phosphate glass with composition $(CaO)_{0.5}(P_2O_5)_{0.5}$. The O/P ratio of this glass is 3 making it a metaphosphate. metaphosphate composition each phosphate tetrahedra has on average two O_b atoms linking to other phosphate units and two Onb atoms available for calcium coordination. IR and Raman spectroscopy results for metaphosphate glasses show a dominance of Q^2 groups (where Q^n refers to a PO₄ tetrahedra with connectivity of n) [13]. This is supported by ^{31}P NMR results for Ca phosphate glass that show a great majority of Q^2 groups in the metaphosphate composition [14]. Previous studies of calcium metaphosphate glass have failed to agree on the coordination of the calcium with oxygen, values vary between 6 and 8 [1, 15, 16, 3]. This is mainly due to the difficulty in distinguishing the Ca-O correlation from others in the diffraction data.

Previous modelling studies of phosphate glasses have used molecular dynamics (MD) and, reverse Monte Carlo (RMC) modelling. Such studies of glass structure can provide heuristic support for experimental results by providing a valid threedimensional model structure, and can use a range of data to help reveal structural features not easily discerned from isolated data sets. RMC gives excellent agreement with diffraction data, but does not always produce smooth short range order, whereas the contrary can be said of MD, due to the different approaches used in the two methods. MD modelling of phosphate glass has been very limited, being reported only for Li [17], Na [18], Mg, Zn and Pb [19], and Tb [20] metaphosphate glasses. RMC modelling has been more common, being reported for Zn, Sr, Ba, Na and K [21], Li [22], Mg and Co [23], K [24], Zn [25-27] and lanthanides [28, 29]. There has only been one reported model for Ca metaphosphate glass in 1987, [21], being a preliminary RMC study which used only x-ray diffraction data.

In this study neutron diffraction data reported in [30] and new x-ray diffraction data is used to obtain more robust and detailed structural information. Reverse Monte Carlo modelling of both x-ray and neutron diffraction data has been used to help identify and distinguish the different correlations. The model is constructed based on known structural characteristics of phosphate networks, such as the geometry of the basic phosphate unit, and then refined to match the experimental diffraction data. The individual pairwise correlation functions may then be separated and quantitatively identified. This approach of combining computer simulations with more than one set of experimental data helps to avoid misinterpretation of data and has enabled more structural information to be extracted than is possible from any one technique alone.

2. Method

The melt-quenched glass sample was prepared using calcium carbonate (CaCO₃, 99+%, BDH) and phosphorus pentoxide (P_2O_5 , 97%, BDH). The precursors were heated in a Pt/10%Rh crucible (71040, Johnson Matthey) at 300 °C for 30 min, then raised to 600 °C for 30 min and then 1100 °C for 60 min, using a Carbolite furnace (RHF 1500, UK). The molten glass was then poured into a graphite mould that had been heated to 370 °C and left to cool to room temperature [30].

The density of the sample was determined by helium pycnometry using a Quantachrome Multipycnometer. The sample has a density of 2.61 ± 0.05 g cm⁻³, equivalent to a number density of 0.071 atoms Å⁻³.

2.1. X-ray diffraction

The x-ray diffraction data was collected on Station 9.1 of the Synchrotron Radiation Source (SRS), Daresbury Laboratory. The finely powdered samples were enclosed inside a 0.5 mm thick circular metal annulus with Kapton windows and mounted in $\theta/2\theta$ transmission geometry. The wavelength was set at $\lambda=0.4858$ Å (calibrated using the K-edge of an Ag foil); this wavelength provides data to a high value of momentum transfer ($Q_{\rm max}\sim23$ Å $^{-1}$ where $Q=4\pi\sin\theta/\lambda$). The data was then analysed using software written in-

The data was then analysed using software written inhouse. The first stage is the application of corrections for the polarization of the x-ray beam, the variation in sample thickness with incident angle, and background scattering. Corrections for the absorption, Compton scattering, the self-scattering and the sharpening function are then made. The resultant scattering intensity, i(Q), can reveal structural information via a Fourier transform to obtain the total pair correlation function, as in (1).

$$T_X(r) = 2\pi^2 \rho_N r + \int_{Q_{\min}}^{Q_{\max}} M(Q) Q i_X(Q) \sin(Qr) dQ \quad (1)$$

where r is the atomic separation between atoms, ρ_N is bulk number density and M(Q) is a window function, applied to reduce the Fourier transform termination artefacts that arise from the finite range of Q. Here a Hanning window function has been used.

In order to obtain the structural information directly from the experimental data, each possible pairwise combination of elements i and j is represented by a pair correlation function $p_{ij}(r)$ that is then fitted to the data. The Q space simulation of each pair correlation function $p_{ij}(Q)$ is generated using (2).

$$p_{ij}(Q) = N_{ij}\omega_{ij}\sin Qr_{ij}\exp[-0.5Q^2\sigma_{ij}^2](c_jQr_{ij})^{-1}.$$
 (2)

The sum of these $p_{ij}(Q)$ is equivalent to the $i_X(Q)$ in (1) and is Fourier transformed using (1) for comparison to the experimental real-space data $T_X(r)$, having been subjected to exactly the same Fourier transform effects.

The parameters in (2) are the coordination number N_{ij} , the atomic separation r_{ij} , and the disorder factor σ_{ij} . These are varied in the fitting procedure. The parameter c_j is the concentration of atom type j and ω_{ij} is the weighting function

that accounts for the variation in scattering strength of different atom types, as defined in (3).

$$\omega_{ij} = \frac{(2 - \delta_{ij})c_ic_jf_i(Q)f_j(Q)}{\left[f(\overline{Q})\right]^2}.$$
 (3)

2.2. Neutron diffraction

The neutron diffraction data [30] was collected on the GEM diffractometer on the ISIS spallation neutron source at the Rutherford Appleton Laboratory, UK. Time-of-flight data was collected over a wide range of Q (up to 40 Å $^{-1}$). The samples were in the form of 8 mm diameter rods therefore no container was required. The program GUDRUN was used to reduce and correct the data [31].

The principles of neutron diffraction have much in common with those for x-rays, and equations of the same form are used in the analysis. A key difference originates from the neutrons interacting with nuclei as scattering centres rather than electron clouds as for x-rays. In neutron diffraction the real-space total correlation function T(r) is given by (4), where b_i is the scattering length that describes how strongly the target nuclei scatter neutrons. The value of b_i used for a given element is an average over the natural abundance of isotopes for that element. Here a Lorch window function is used.

$$T_N(r) = 4\pi \rho_N r \left(\sum_i c_i b_i\right)^2 + \frac{2}{\pi} \int_{Q_{min}}^{Q_{max}} M(Q) Q i_N(Q) \sin(Qr) dQ.$$
 (4)

Structural information is then obtained from the experimental data using the same method as for the x-ray diffraction data. Each type of atom pair is modelled by a pair correlation function as defined in (2). For neutron diffraction the weighting factors are defined in (5).

$$\omega_{ij} = (2 - \delta_{ij})c_i c_i b_i b_j. \tag{5}$$

The accuracy of information obtained from fitting pair correlation functions depends on correctly assigning the atom types to i and j for all the peaks $p_{ij}(r)$, including those that overlap. Accurate results can be obtained once all peaks are identified and accounted for. The fitting was then optimized by using a nonlinear least squares fitting algorithm to find the parameters R_{ij} , N_{ij} and σ_{ij} which give best agreement with experiment.

2.3. Reverse Monte Carlo modelling

Reverse Monte Carlo is a method for structural modelling which makes it possible to generate three-dimensional models that are consistent with experimental data. RMC is a useful technique as the models developed agree quantitatively with all available experimental data as well as with constraints that represent our existing knowledge of the system, for example: density, atomic radii, approximate bond lengths [32].

A model is defined as a set of N virtual atoms in a box at the density corresponding to that of the real material.

The diffraction pattern is calculated based on the current configuration and then compared to the experimental data. A random walk approach is taken in search of a set of atom positions that is consistent with experimental data [33]. The partial structure factors, $i_{ij}(Q)$, are calculated using (6), from these the total structure factor, i(Q), is calculated using (7), where $g_{ij}(r)$ are the partial pair distribution functions.

$$Qi_{ij}(Q) = 4\pi\rho \int_0^\infty rg_{ij}(r)\sin(Qr)\,\mathrm{d}r \tag{6}$$

$$i(Q) = \sum_{ij} c_i c_j b_i b_j i_{ij}(Q). \tag{7}$$

The standard RMCA program has been used to model the atomic structure against both x-ray and neutron diffraction data [32]. The route taken to build the model can affect its success so care is taken to ensure the result is in agreement with known information about atomic structure. Here the following technique has been used to construct a model of 1080 atoms.

- (1) A random configuration of 240 P atoms was generated. Then chains of P atoms were created by constraining the P–P coordination number, $N_{P-P} = 2$.
- (2) 240 bridging oxygen atoms (O_b) were added at the midpoints of nearest neighbour P–P pairs.
- (3) 480 non-bridging oxygen atoms (O_{nb}) were added randomly.
- (4) A metaphosphate structure was obtained using the constraints $N_{\rm O_b-P}=2$, $N_{\rm P-O_b}=2$, $N_{\rm O_{nb}-P}=1$, $N_{\rm P-O_{nb}}=2$.
- (5) Constraints were also applied to the bond angles so that they were centred on $\theta_{\rm O-P-O}=109^{\circ}$ and $\theta_{\rm P-O_b-P}=135^{\circ}$.
- (6) The 120 calcium atoms were then added randomly and constraints were made against non-physical solutions such as $N_{\text{Ca-O}} = 0, 1, 2, 3 \text{ or } 4$.
- (7) The RMC method was then used to fit the model to the experimental i(Q), with $\Delta Q = 0.05 \text{ Å}^{-1}$, and $Q_{\text{max}} = 22.9 \text{ Å}^{-1}$ and 40 Å⁻¹ for x-ray and neutron diffraction data respectively.

RMC uses distance parameters to define the distance of closest approach R_{\min} (called cut offs), and coordination constraints are defined using a distance representing a maximum in the nearest neighbour separation for the given atom pairs, R_{\max} . The distance parameters R_{\min} and R_{\max} used in the construction of the model were obtained from existing knowledge of phosphate glasses [1] and data on phosphate crystal structures from the crystallographic database provided by the STFCs chemical database service (CDS) [34]. The values of R_{\min} and R_{\max} used in the present study are shown in table 2.

3. Results

3.1. XRD and ND

The experimental x-ray and neutron diffraction data is shown in Q-space in figure 1 and in real space in figures 2 and 3. Table 1

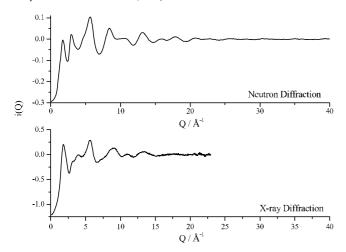


Figure 1. The Q-space interference function, i(Q) obtained from neutron diffraction (top [30]) and x-ray diffraction (bottom).

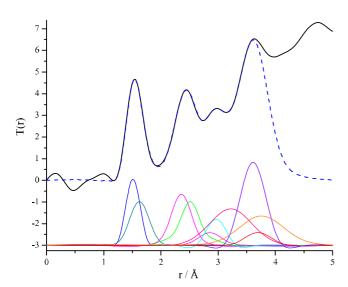


Figure 2. The total pair distribution function, T(r), (solid line) together with fit (dashed line) from the x-ray diffraction. The individual pair distribution functions are also shown off-set by -3, the final peak is fitted as a background.

shows the sequence of interatomic correlations (between atom types i and j) which was used to fit the x-ray and neutron diffraction data, and the values obtained for the structural parameters (distance R_{ij} , number of neighbouring atoms N_{ij} , and standard deviation in distance σ_{ij}). The individual interatomic correlations, $p_{ij}(r)$, are also shown in figures 2 and 3 where they are off-set for clarity. An additional peak is visible at high R that is not reported in the table as it is not representative of a real feature, it is used to reduce the effect of high R correlations on the fitting of the Ca–Ca correlation.

The XRD and ND data were fitted separately with the same sequence of interatomic correlations. Table 1 shows the highly consistent fitting parameters obtained, with only one difference exceeding ± 0.02 Å in R. This larger difference in the value of R for the O–O correlation is understandable considering the low weighting this correlation has in XRD.

The first interatomic correlation is P-O at an average distance of 1.55 Å. In phosphates this is split into shorter

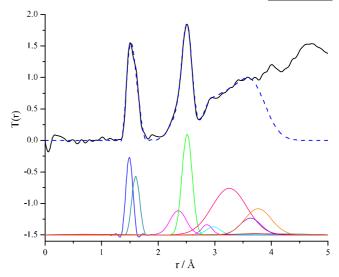


Figure 3. The total pair distribution function, T(r), (solid line) together with fit (dashed line) from the neutron diffraction data. The individual pair distribution functions are also shown off-set by -1.5, the final peak is fitted as a background.

Table 1. Structural parameters derived from fitting T(r) to x-ray and neutron diffraction data.

	X-ray diffraction			Neutron diffraction		
Correlation	R (Å) (±0.02)	<i>N</i> (±0.2)	σ (Å) (±0.01)	R (Å) (±0.02)	<i>N</i> (±0.2)	σ (Å) (±0.01)
P-O _{nb}	1.51	1.9	0.03	1.49	2.0	0.02
P-O _b	1.62	1.9	0.12	1.60	1.9	0.04
Ca-O	2.36	5.2	0.14	2.35	5.2	0.14
$O \cdots O$	2.51	4.0	0.10	2.51	4.0	0.07
Ca-O	2.86	1.8	0.17	2.86	1.7	0.08
$P\cdots P$	2.97	2.0	0.14	2.97	2.0	0.11
$O \cdots O$	3.22	8.2	0.31	3.26	8.2	0.30
$P \cdots Ca$	3.61	4.3	0.22	3.63	4.2	0.18
$Ca \cdots Ca$	3.70	2.1	0.23	3.70	2.1	0.32

bonds to non-bridging oxygen atoms (O_{nb}) and longer bonds to bridging oxygen atoms (O_b). This split is clearly seen as a shoulder at high r in neutron diffraction, but discernible only as asymmetry in XRD. The fit results show $N_{P-O}=3.9$, agreeing within uncertainty with the value of $N_{P-O}=4$ expected for phosphate tetrahedra, and this is split between two O_{nb} and two O_b as expected for a metaphosphate glass. The observed average distances of 1.50 and 1.61 Å for $P-O_{nb}$ and $P-O_b$ correlations are in good agreement with results for diffraction of other metaphosphate glasses [35].

On the basis of the P–O coordination, two related correlations can be confidently defined. Firstly the O–P–O correlations due to phosphate tetrahedra (with tetrahedral O–P–O angle of $\sim 109^{\circ}$) would have a distance of ~ 2.54 Å and an average coordination $N_{\rm O-O}$ of 4 (average of two $O_{\rm nb}$ with N=3 and one $O_{\rm b}$ with N=6). Secondly the P–O–P correlations due to chains of phosphate tetrahedra (with typical P–O–P angle of $\sim 135^{\circ}$ [36]) would have a distance of 2.99 Å and a coordination of two. The results of fitting are in good agreement with these expectations. They are also in agreement with results for diffraction of other metaphosphate glasses [35].

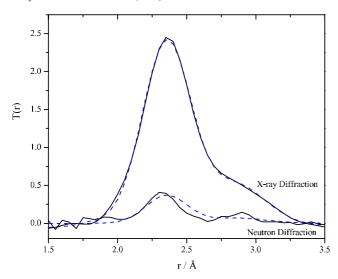


Figure 4. The individual pair distribution function for Ca–O extracted from the T(r) by subtracting the fit for all the other correlations, demonstrating the broad spread in bond length and hence the need to fit it with two peaks.

A second type of cation–oxygen bond is present in the structure, Ca–O, and this gives the second shortest correlation. These bonds are typically ~ 2.4 Å in length, but they can show a wide spread due to flexibility in the coordination of Ca [37]. Due to the length of Ca-O bonds, the Ca-O correlation overlaps with the O-P-O correlation at 2.51 Å. This is visible as a shoulder on the low r side of the peak in neutron diffraction, and as an asymmetry to low r in the x-ray diffraction. The difficulty lies in identifying Ca–O correlations which may extend under the O-P-O correlation and up to distances as high as 3 Å. Figure 4 shows the Ca–O correlation extracted from the experimental data by subtracting the fit of all the other correlations. It shows a wide distribution in bond distance with a second feature at higher r. This requires allowing an additional peak in the fitting between the O-P-O and P-O-P correlations to fit the residual correlations hidden beneath them.

Considering the role of Ca in the structure, there are an additional three correlations which can be safely predicted from the Ca–O correlation. These are the O–Ca–O, Ca–O–P and the Ca–O–Ca correlations. The O–Ca–O correlations are due to polyhedral units of Ca coordinated by N oxygen atoms, referred to as CaO_N . The observed O–Ca–O distance of \sim 3.24 Å is in agreement with data from the Chemical Database Service [34] and the coordination of \sim 8.2 is close to the value of 8 expected for an oxygen which is part of two CaO_6 octahedra and has nearest neighbours with four oxygen atoms from each. From the correlation distance an O–Ca–O bond angle of 81.6° is calculated which is close to that of 90° for an octahedron and is in agreement with the capped trigonal prism structure described by Rothammel $et\ al\ [16]$ for Ca metaphosphate crystal.

The two remaining correlations are P-O-Ca and Ca-O-Ca. The distances of these are difficult to estimate, but will be longer than P-O-P distances due to the longer Ca-O bonds. The increasing number of overlapping correlations at

Table 2. Structural parameters derived from the RMC fitting to x-ray and neutron diffraction data. Also listed are the cut offs used in the development of the model.

Correlation	R (Å) (±0.03)	N (±0.3)	Cut offs Min R (A	Å) Max R (Å)
D.O	1.71	2.00	1 40	1.00
P–O _b	1.61	2.00	1.48	1.80
$P-O_{nb}$	1.53	1.99	1.36	1.80
Ca-O _{nb}	2.41	4.97	2.05	2.70
$O_b \cdots O_b$	2.52	1.85	2.20	2.85
$O_b \cdots O_{nb}$	2.51	3.97	2.20	2.85
$O_{nb} \cdot \cdot \cdot \cdot O_{nb}$	2.51	2.07	2.20	2.85
Ca-O _{nb}	2.99	0.66	2.70	3.20
$P\cdots P$	2.93	2.00	2.75	3.20
$O_{nb} \cdot \cdot \cdot O_{nb}$	3.35	3.85	2.85	3.80
$P \cdot \cdot \cdot Ca$	3.64	2.80	3.20	4.20
$Ca \cdots Ca$	3.66	1.78	3.20	4.20
			_	

the longer distances also makes the fitting less reliable. For these reasons the correlations are not often quoted in previous work; however, the use of a combination of techniques makes it possible to identify them here. The P-O-Ca correlation is at an average distance of 3.62 Å. Comparing this with the typical P-O and Ca-O bond lengths, this indicates a P-O-Ca bond angle between 105° and 140°, a reasonable result for a modifier cation in a phosphate network. If it is assumed that the Ca is only bonded to the O_{nb.} then the P-Ca coordination number of 4.2 implies each O_{nb} is bonded to two Ca–oxygen polyhedral units. These results are comparable to the crystal structure in which the average distance between P and Ca is 3.56 Å and the P-Ca coordination number is 3.5 [16]. The Ca-Ca distance of 3.70 Å is comparable to the crystal structure, however, the crystal also has longer Ca-Ca distances extending up to 4.7 Å. Such longer Ca–Ca distances are likely to have been masked in the glass diffraction data by overlapping correlations at distances beyond 3.5 Å. Taking into account only the shorter Ca-Ca distances less than 4 Å, the Ca-Ca coordination of 2 also matches well with the crystal data.

3.2. RMC modelling

Figure 5 shows the result obtained for RMC modelling of the ND and XRD data in Q space. As expected, due to the RMC method, a very good fit is obtained. The RMC model obtained is illustrated in figure 6. This model consists of chains of phosphate tetrahedra, as expected for a realistic metaphosphate structure, and was achieved by use of suitable constraints in RMC modelling, discussed in section 2. By analysing the model the individual pair correlation functions were isolated and structural parameters were found for each. These are listed in table 2 where R is the average bond length within the first nearest neighbour peak (defined by the interval between R_{\min} and R_{\max} in table 2) and N corresponds to the area of the peak. Note that these correlations of atom types i and j follow the same sequence as discussed in the peak fitting analysis presented above, which provides a selfconsistent confirmation that the assignment of correlations is sound. Figure 7 shows the interatomic correlations generated from the coordinates of the model. These are noisier than the peaks used in the peak fitting because they come from the

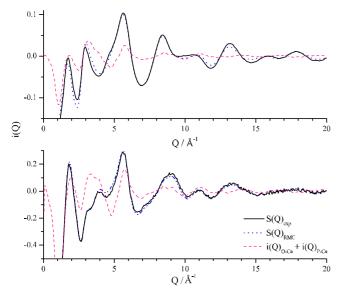


Figure 5. RMC fit to experimental i(Q): (top) RMC compared to neutron diffraction data, (bottom) RMC compared to x-ray diffraction data.

positions of a relatively small number of model atoms, rather than average structural parameters used in peak fitting. In particular, the P–O correlation has a sharp peak before its $R_{\rm max}$ value of 1.8 Å that comes from an especially tight constraint. This effect is acceptable in RMC because the constraint is modelling a feature of phosphate glasses that is known with great confidence.

The model can be analysed to obtain some additional structural information. The phosphate network and the PO₄ tetrahedra are well-defined due to the bond angle constraints used, as shown in figure 8. The network is 100% Q^2 due to the connectivity constraint used in model building. This constraint was motivated by NMR results [30] which show Q^2 units can join to form (closed) rings or (open) chains. The number of three-member rings in the model is only ten, so over 80% of

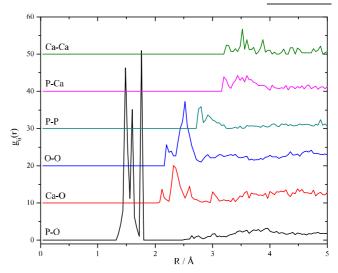


Figure 7. The pair correlations from the RMC fit to experimental data. The P–O, Ca–O and O–O correlations are the sum from O_b and O_{nb} . Each correlation is off-set by an additional 10 units.

the Q^2 tetrahedra are in chains, and inspection of the model showed there were two large fragments.

The Ca–O coordination is an interesting result, because this was only constrained to be $N \ge 5$ in the modelling (based on Ca coordination less than 5 being relatively unknown [38]). The Ca–O correlation in the model shows a broad distribution with most distances around 2.35 Å and some up to 3.0 Å, as was also seen in the peak fitting of x-ray and neutron diffraction data. The Ca–O coordination of 5.6 is less than that found by diffraction, but 55% of the Ca atoms have a coordination of 6 or 7, as shown in figure 9.

The O-Ca-O bond angle has been analysed and is shown in figure 8. It shows a distribution similar to that expected for 6 coordinated Ca, with a peak around 90° associated with adjacent O in the structural unit, and a second peak at a higher angle from O on the opposite sides of the structural unit. A regular octahedron would have peaks at 90° and 180°, and the

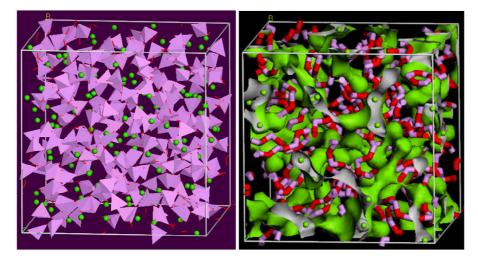


Figure 6. The RMC model. The left image shows the phosphate units as tetrahedra (in the electronic version these are purple) and the calcium ions as isolated spheres (green). The right image shows the -P-O-P-O- backbone (purple and red chain) and the Ca clusters as a surface (green).

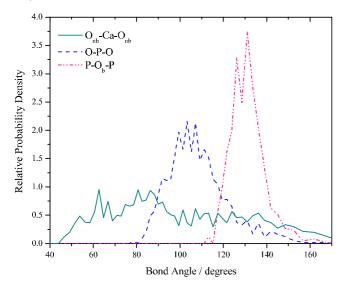


Figure 8. The RMC models bond angle distributions for O_{nb} –Ca– O_{nb} , P– O_b –P and the average of all the O–P–O.

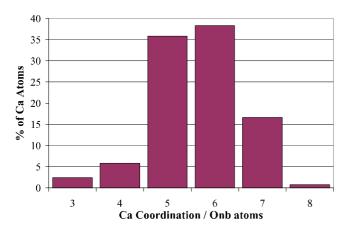


Figure 9. The Ca-O coordination distribution from the RMC model.

broadened nature of the second peak implies a more distorted octahedral unit in the model.

The P-Ca correlation distance and coordination number are in agreement with the diffraction results, including the average P-O-Ca bond angle of 127°. The Ca-O-Ca correlation has greater statistical variability, which makes it difficult to extract information concerning the broad distribution in Ca-Ca distances discussed earlier. However, the Ca-Ca correlation does seem to show a first nearest neighbour peak with average distance of 3.66 Å with coordination number of 1.8, which supports the Ca-Ca peak assignment used in fitting the diffraction data.

4. Discussion

For the phosphate network, all the parameters confirm the tetrahedral structure and the Q^2 speciation as expected for the metaphosphate composition. These parameters are also in agreement with Hoppe's model for the structure of phosphate glasses [12]. A previous NMR study of the same sample

indicated 96% Q^2 and 4% Q^1 [30], and such a distribution would imply a slight increase in the number of P–O_{nb} bonds, with $N_{\rm P-O_{nb}}=2.04$ and $N_{\rm P-O_{b}}=1.96$, but such a small effect, if real, is beyond the level of uncertainty in the present results.

The diffraction experiments have differentiated two Ca–O bond lengths, a shorter distance of \sim 2.36 Å has a coordination of \sim 5.2 and a longer distance of \sim 2.86 Å has a coordination of ~ 1.8 . Our previous study using ND alone [30] only identified the first correlation as Ca-O and the second peak was fitted with another O-O correlation but no physical description could be given. Crystallographic data has shown the longer Ca-O bond lengths exist in crystals and it is commonly found for calcium in oxide structures to have oxygen atoms at longer distances [34]. Such a two-peak fitting of cation oxygen correlations has previously been used in diffraction studies of various phosphate and silicate glasses [39], and in particular in zinc and magnesium metaphosphates [40], lanthanum metaphosphate [41] and potassium phosphate [24]. Molecular dynamics models of calcium silicate [42] and calcium aluminate [43] glasses also show that Ca-O nearest neighbour peak has an asymmetric shape with shoulder extending to \sim 3 Å.

The total Ca–O coordination number of \sim 7.0 found here is in agreement with Hoppe *et al* [15]. This coordination can relate to three possible types of polyhedral structures: the pentagonal bipyramid, the capped trigonal prism, and the capped octahedron. Calcium metaphosphate crystal of the same composition has the capped trigonal prism structure [16]. This type of structure is similar to a distorted octahedron, but with an additional atom. The distribution of Ca–O bond lengths from diffraction can be considered in relation to the bond valence of Ca. This is the way in which the total valence of 2 for Ca, $v_{\text{tot}} = 2$, is distributed among the N_{ij} Ca–O bonds of length R_{ij} . The valence associated with an individual Ca–O bond, $v_{\text{Ca-O}}$, is given by (8) [44].

$$v_{\text{Ca-O}} = \exp\left(\frac{1.967 \,\text{Å} - R_{\text{Ca-O}}}{0.37 \,\text{Å}}\right).$$
 (8)

Applying this to the diffraction results gives 5.2 bonds of length 2.36 Å and bond valence $v_{\rm Ca-O}=0.35$, and 1.8 bonds of length 2.86 Å and bond valence $v_{\rm Ca-O}=0.09$, with a total bond valence of 1.96 as expected for a Ca²⁺ cation.

The coordination of Onb to Ca can be considered by looking at the Ca-O coordination number from diffraction. The Ca-O coordination number can be converted into the O-Ca coordination using the relation $c_i N_{ij} = c_j N_{ji}$ (derived from (2)), and this gives an average value of ~ 1.17 for all oxygen atoms. It is assumed that the Ob have zero coordination with Ca as the repulsion from two P⁵⁺ atoms bonded to the O_b would make it energetically unfavourable to also be bonded to a Ca²⁺. Thus, since the O_b are not coordinated to Ca, the average O_{nb} coordination to Ca will be ~ 1.75 , which means that approximately three quarters of O_{nb} are bonded to two Ca rather than just one Ca. In comparison the RMC results show the model has an average O-Ca coordination number of 1.4 which implies that approximately half of the O_{nb} are coordinated to one Ca and half are coordinated to two Ca. Note that since each P has two O_{nb}, the aforementioned result implies that each P should be coordinated to \sim 3.4 Ca. In fact, the P···Ca coordination of \sim 4.2 in both the diffraction data and the RMC model is somewhat larger, which may mean that the P···Ca nearest neighbour peak has been somewhat overestimated. However, all of these results nevertheless point to a majority of O_{nb} being coordinated to two Ca.

With this information, a valence model can be developed. The metaphosphate composition means there are two phosphate units per Ca²⁺ cation, and hence there are four O_{nb} per Ca²⁺, each with a bond valence of 0.5, available to form Ca-O bonds. A bond valence model for 6 coordinated Ca was discussed by Hoppe in which two Onb each form one Ca-O bond with $v_{\text{Ca-O}} = 0.5$, and two O_{nb} each form two Ca-O bonds, with $v_{\text{Ca-O}} = 0.25$. From (8), the former would have bond lengths of 2.22 Å, and the latter would have bond lengths of 2.48 Å, and so no long Ca-O bonds would be expected. The diffraction results in the present study indicate a Ca-Onb coordination of 7, requiring 3 out of 4 O_{nb} to form two Ca–O bonds. Again, if the latter had $v_{\text{Ca-O}} = 0.25$, no long Ca-O bonds would be expected. A plausible alternative scenario is that two O_{nb} each form two Ca-O bonds with $v_{Ca-O} = 0.4$ and $v_{\text{Ca-O}} = 0.1$. From equation (8), the latter would have bond lengths of 2.8 Å, so long Ca–O bonds would be expected, which is consistent with the diffraction results.

The foregoing discussion has been primarily concerned with short range order, but it is also important to consider medium range order. This is concerned with structural correlations on scales of several nearest neighbour distances. As previously commented, on this scale the phosphate network consists of metaphosphate chains. Figure 6 highlights the 'backbone' of the phosphate chains, i.e. P-O_b-P-O_b-P. Also as previously commented, many Onb are bonded to two Ca, and this creates Ca clusters, i.e. Ca-O_{nb}-Ca-O_{nb}-Ca. The Ca clusters can be described in terms of the type of connections between two adjacent CaO_N polyhedra in the cluster, and this enables an estimate of the typical Ca-Ca correlation distances involved. If the typical Ca-O_{nb} distance is $R_{\text{Ca-O}} \sim$ 2.4 Å, the distances of neighbouring Ca will be approximately $\sqrt{2R_{\text{Ca-O}}} \sim 3.4 \text{ Å if CaO}_N$ polyhedra are edge-sharing, and $2R_{\text{Ca-O}} \sim 4.8 \text{ Å if CaO}_N$ polyhedra are corner-sharing. The information on Ca-Ca correlations from diffraction and RMC results is limited to the first Ca-Ca correlations at a distance of ~ 3.6 Å, and these correspond to edge-sharing of CaO_N polyhedra. The Ca clusters can also be described in terms of their shape, but there is no quantitative way to do this. Instead, the clusters have been illustrated visually in figure 6 by defining a surface that encloses all model Ca atoms which are within 5 Å of each other, a distance which includes both edge-sharing and corner-sharing of CaO_N polyhedra. The appearance of the clusters is somewhat elongated, which is compatible with the presence of phosphate chains.

Another much examined aspect of medium range order in oxide glasses is the first sharp diffraction peak (FSDP), which is the lowest-Q peak in the diffraction pattern i(Q) and is found at $Q=1.8 \text{ Å}^{-1}$ in both ND and XRD. The FSDP is frequently considered to be indicative of structural correlations over medium range length scales. For example, the FSDP in rare earth metaphosphate glasses is associated

with rare earth–rare earth correlations [28]. The present RMC model enables us to examine the contribution to i(Q) from different interatomic correlations. For x-ray diffraction, the two correlations which contribute the most to the shape of the FSDP are Ca···P and Ca–O correlations, as shown in figure 5. (For neutron diffraction, the effect is less pronounced due to the different weighting factors, as also shown in figure 5.) Since the Ca···P and Ca–O correlations are influenced by the spatial relationship between the phosphate backbone (P, O) and the Ca clusters (Ca), it seems reasonable to say that the FSDP is influenced by the medium range order for the case of calcium metaphosphate glass.

It has been possible by the combination of techniques, to develop a set of structural parameters for calcium metaphosphate glass that agrees with x-ray and neutron diffraction, RMC modelling, and Hoppe's conceptual model. The use of RMC modelling has allowed us to confirm the identity of all the correlations, and therefore obtain more comprehensive structural information. This is especially true in the case of the calcium which has previously been masked by the phosphate network.

5. Conclusions

High quality x-ray and neutron diffraction data have been combined with RMC modelling to give structural parameters for calcium metaphosphate glass, including six interatomic correlations up to a distance of 3.6 Å. A well-defined metaphosphate structure has been confirmed by first and second neighbour correlations and bond angles within the phosphate network, including two different P-O bonds that distinguish bridging and non-bridging oxygen atoms. The combination of techniques has enabled the identification of correlations involving Ca that overlap with those from the phosphate network, and there are two Ca-O correlations, indicating a wide distribution of bond lengths as commonly seen for Ca in oxide glasses. The calcium is found to be coordinated with seven oxygen atoms, the same number as in calcium metaphosphate crystal, where Ca has a capped trigonal prism coordination. The coordination of Ca to only non-bridging oxygen atoms has been demonstrated in the RMC model, and inspection shows that most non-bridging oxygen atoms are coordinated to two Ca. These observations are all consistent with Hoppe's model for the structure of phosphate glasses. Furthermore, the medium range order is revealed to consist of phosphate chains intertwined with apparently elongated clusters of Ca ions, and the Ca-O and Ca · · · P correlations contribute significantly to the FSDP in xray diffraction.

Acknowledgments

The authors wish to acknowledge funding from the EPSRC (EP/E006337/1), support and beamtime from the STFC, and the use of the EPSRC Chemical Database Service at Daresbury.

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