

**İSTANBUL TECHNICAL UNIVERSITY ★ INSTITUTE OF SCIENCE AND TECHNOLOGY**

**MULTIDISCIPLINARY DESIGN OPTIMIZATION OF AEROSPACE  
STRUCTURES WITH STATIC AEROELASTIC CRITERIA**

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**Programme : Aeronautics and Astronautics Engineering**

**JUNE 2008**

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**Date of submission : 05 May 2008**

**Date of defence examination : 09 June 2008**

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**JUNE 2008**

**İSTANBUL TEKNİK ÜNİVERSİTESİ ★ FEN BİLİMLERİ ENSTİTÜSÜ**

**UÇAK-UZAY YAPILARININ STATİK AEROELASTİK KRİTER İLE ÇOK  
DİSİPLİNLİ TASARIM OPTİMİZASYONU**

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**Tezin Enstitüye Verildiği Tarih : 05 Mayıs 2008**

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**HAZİRAN 2008**

## ACKNOWLEDGEMENT

Although this thesis seems only my work, numerous people contributed to the production of this thesis. I am grateful to those people who have made this thesis possible by supporting and encouraging me.

First of all, I wish to express my gratitude to my colleague Arda Yanangönül to be always with me by listening and answering by never-ending questions in a constructive way. I would like to thank for his support.

I also want to express my gratitude to my advisor, Assistant Professor Melike Nikbay for her support and guidance during my graduate. It was a pleasure for me to work in her career project.

Many thanks to my colleague Ahmet Aysan.

Much appreciation to the academic staff of the Aeronautics and Astronautics Faculty of the İstanbul Technical University for sharing their valuable knowledge and experience.

Thank you to The Scientific and Technological Research Council of Turkey – TÜBİTAK for financial support during my graduate with the National Scholarship Program for the Graduate Students. This study is also partly financed by the TÜBİTAK career project titled “Analysis and Reliability Based Design Optimization of Fluid-Structure Interaction Problems Subject to Instability Phenomena” with grant number 105M235.

I am pleased to thank Informatics Institute of İstanbul Technical University for letting me use their facilities.

Thank you to Mauro Poian and Rosario Russo from ESTECO Italy for their assistance and patience to help me to prepare the core of my study.

I would like to express my deep appreciation and thanks to the general manager of the DENAK Ship Management&Agency Serdar Akçalı to help me have a new vision of life and education. Without him I could not be successful in my academic career.

Many friends have helped me stay sane through my graduate. Their support and care helped me overcome all the difficulties. I greatly value their friendship and I deeply appreciate their belief in me.

Most importantly, none of this would have been possible without the love and patience of my family Mustafa, Şerife and Korhan Öncü. I would like to express my heart-felt gratitude to my family.

Finally, a special appreciate to Melis...for her love, support, patience and understanding....

June 2008

Levent ÖNCÜ

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## ABBREVIATIONS

<b>2D</b>	: Two-dimensional
<b>3D</b>	: Three-dimensional
<b>AGARD</b>	: Advisory Group for Aerospace Research and Development
<b>ALE</b>	: Arbitrary Lagrangian Eulerian
<b>ARW-2</b>	: Aeroelastic research wing two
<b>CA</b>	: Computational aeroelasticity
<b>CAD</b>	: Computer aided design
<b>CFD</b>	: Computational fluid dynamics
<b>CSD</b>	: Computational structural dynamics
<b>DLR</b>	: Institute for Aerodynamics and Flow Technology
<b>DNS</b>	: Direct numerical simulation
<b>FEA</b>	: Finite element analysis
<b>FEM</b>	: Finite element method
<b>FSI</b>	: Fluid structure interaction
<b>MDO</b>	: Multi-Disciplinary optimization
<b>MLS</b>	: Moving Least Squares
<b>MO</b>	: Multi objective
<b>MOGA</b>	: Multi objective genetic algorithm
<b>MpCCI</b>	: Mesh based Parallel Code Coupling Interface
<b>NSGA-II</b>	: Non dominated sorting genetic algorithm two
<b>RANS</b>	: Reynolds averaged Navier-Stokes
<b>Ref</b>	: Reference
<b>SQP</b>	: Sequential quadratic programming
<b>TSD</b>	: Transonic small disturbance

## NOMENCLATURE

$\alpha$	: Angle of attack
$\rho$	: Fluid mass density
$\gamma$	: Adiabatic index
$\nu_{12}, \nu_{13}, \nu_{23}$	: Poisson's ratios in the principal directions
$\Lambda_{c/4}$	: Sweep at the quarter chord
$\lambda$	: Taper ratio
$b / 2$	: Half span
$c_{ip}$	: Chord of the wing tip
$c_{root}$	: Chord of the wing root
$C_p$	: Pressure coefficient
$[D]$	: Damping matrix
$E$	: Total energy
$E_{11}, E_{22}, E_{33}$	: Young's moduli in the principal directions
$F$	: Flux vector
$f, g, h$	: Cartesian components of flux vector
$F_a$	: Aerodynamic force
$F_e$	: External force
$G_{12}, G_{13}, G_{23}$	: Shear moduli in the principal directions
$g(s)$	: Set of inequality constraints
$h(s)$	: Set of equality constraints
$k_{ij}$	: Spring constant between node i and its neighbor j
$[K]$	: Stiffness matrix
$L / D$	: Lift over drag value
$M$	: Total mass of the wing
$[M]$	: Mass matrix
$n_i$	: Number of neighboring nodes connected to node i
$P_t$	: Parent population
$Q$	: Source terms (body forces)
$Q_i$	: Child population
$R_i$	: Combined population
$s$	: Set of parameters
$s_L$	: Lower bound of $s$
$s_u$	: Upper bound of $s$
$u, v, w$	: Velocity components x-y-z directions respectively

$u_{\max}$	: Maximum displacement of the wing
$u$	: Displacement
$\dot{u}$	: First time derivative of displacement
$\ddot{u}$	: Second time derivative of displacement
$U$	: Conservative variables
$\Delta\bar{x}_j, \Delta\bar{x}_i$	: Displacement of node i and its neighbor j

# **MULTIDISCIPLINARY DESIGN OPTIMIZATION OF AEROSPACE STRUCTURES WITH STATIC AEROELASTIC CRITERIA**

## **SUMMARY**

Multi-disciplinary design analysis and optimization has attracted attention in the past two decades. There are many studies done with academic codes but there are few examples of studies done with fully commercial softwares on aeroelastic optimization. This study aims to fill this need.

In this thesis aeroelastic optimization is performed on a basic experimental wing model based on AGARD 445.6 elastic wing configuration to obtain the objectives maximum lift over drag ratio and minimum weight of the wing. A static aeroelastic criteria is given as a design constraint to satisfy the maximum tip deflection. Sweep angle at the quarter chord and the taper ratio of the wing are used as design parameters for this study. Moreover, a genetic algorithm NSGA-II is used to control the optimization process.

The optimization study is done by using the Multi-Objective Design Environment (mode)FRONTIER 4.0 optimization software with the user written scripts to perform this study: ABAQUS 6.7-1 finite element solver script to prepare the computational structural dynamics (CSD) model, FLUENT 6.3.26 and GAMBIT 2.2.30 scripts to prepare the computational fluid dynamics (CFD) model and Mesh based Parallel Code Coupling Interface-MpCCI 3.0.6 script to perform loosely coupled aeroelastic analysis.

Aeroelastic analysis is done by employing a staggered algorithm in a loosely coupled approach. Aerodynamic surface pressures are converted to nodal forces and transferred to the CSD code, then under these forces static analysis is performed and nodal displacements are transferred to CFD code as mesh motion. This process is controlled by MpCCI 3.0.6 software.

The results from the structural, fluid and aeroelastic fields are used to compare the results with the numerical and the wind tunnel data of the AGARD 445.6 wing. Once the wing is validated with the literature data, the aeroelastic optimization study is performed.

The pareto set for the optimum designs are obtained at the end of the aeroelastic optimization study to choose the best design configuration. The effect of the design variables on objective functions and their relationship are examined by using the optimization problem results.

# UÇAK-UZAY YAPILARININ STATİK AEROELASTİK KRİTER İLE ÇOK DİSİPLİNLİ TASARIM OPTİMİZASYONU

## ÖZET

Son yirmi yılda çok disiplinli analiz ve optimizasyon konuları büyük bir oranda ilgi çekmektedir. Aeroelastik optimizasyon konusunda akademik kodlarla yapılan bir çok çalışmaya rastlamak mümkünken, tamamiyle ticari kodlarla yapılan çalışmalara daha az rastlanmaktadır. Bu çalışma bu ihtiyacı doldurmak için bir şans vermiştir.

Bu tez çalışmasında aeroelastik optimizasyon AGARD 445.6 elastik kanat konfigürasyonundan yola çıkılarak basit bir kanat için en yüksek taşıma/sürüklenme oranı ve en düşük kütle amaç fonksiyonlarına ulaşmak için yapılmıştır. Tasarım kısıtı olarak bir statik aerolastik kriter olan en yüksek uç yer değiştirmesi verilmiştir. Kanadın çeyrek veterdeki ok açısı ve sivrilme oranı tasarım parametreleri olarak atanmıştır. Ayrıca bu çalışmada optimizasyon döngüsünü kontrol etmek için bir genetik algoritma olan NSGA—II algoritması kullanılmıştır.

Optimizasyon çalışması çok amaçlı tasarım ortamı (mode)FRONTIER 4.0 optimizasyon yazılımı kullanılarak yapılmıştır. Bu çalışmayı yapmak için çeşitli betikler yazılmıştır: ABAQUS 6.7-1 sonlu eleman çözücüsü betiği yapısal modeli hazırlamak için, FLUENT 6.3.26 ve GAMBIT 2.2.30 betikleri hesaplamalı akışkanlar dinamiği (HAD) modelini hazırlamak için ve çözüm ağı tabanlı paralel kod eşleme arayüzü MpCCI 3.0.6 ise gevşek bağlaşımlı aeroelastik analizleri yürütmek için kullanılmıştır.

Aeroelastik analizler bir sıralı“staggered” algoritma kullanılarak gevşek bağlaşımlı olarak çözülmüştür. Aerodinamik yüzey yükleri düğüm bazlı kuvvetlere çevrilerek yapısal çözücüye aktarılmakta, bu yükler altında yapılan statik analiz sonucunda oluşan yer değiştirmeler ise akışkan koduna çözüm ağı hareketi olarak gönderilmektedir. Bu çevrim MpCCI 3.0.6 yazılımı tarafından kontrol edilmektedir.

Yapısal, akışkan ve aeroelastik analizler sonunda alınan sonuçlar AGARD 445.6 kanadı üstüne yapılmış önceki sayısal ve rüzgar tüneli verileri ile karşılaştırılmıştır. Karşılaştırmadan sonra geçerliliği onaylanan kanat kullanılarak aeroelastik optimizasyon çalışması yapılmıştır.

Aeroelastik optimizasyon sonunda en uygun çözümü seçebilmek için pareto kümesi oluşturulmuştur. Tasarım değişkenlerinin amaç fonksiyonları üzerindeki etkileri ve aralarında ilişki sonuçlar değerlendirilerek yapılmıştır.

## **1. MULTIDISCIPLINARY DESIGN AND AEROELASTICITY**

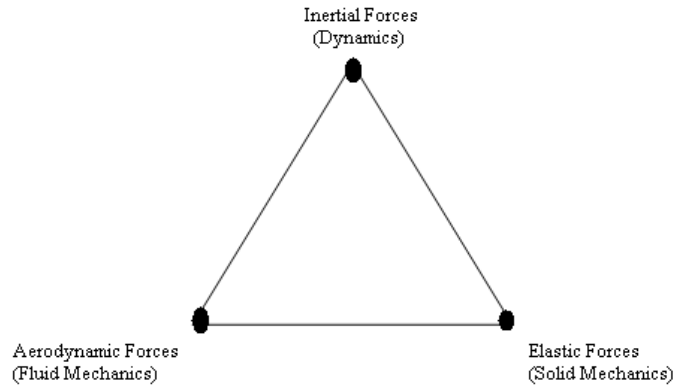
### **1.1 What is multidisciplinary design?**

To develop new and complex design technologies in aerospace industry, high levels of integration between different disciplines like aerodynamics, structural dynamics, propulsion, control, acoustics, heat transfer are needed. Since the behaviors of these disciplines are mutually interactive, they cannot be thought separately. When at least two or more disciplines interact, the nature of the evolved problem is defined as “multi-disciplinary” and the design problem regarding to these disciplines is named as “multi-disciplinary design”.

One of the most commonly studied areas regarding multi-disciplinary design is the interaction between a flexible structure and the fluid surrounding the structure which is known as “Fluid Structure Interaction (FSI)”. FSI gives rise to a deep diversity of phenomena with applications of many engineering areas, such as, the stability of an aircraft wing, design of bridges, the flow of blood through arteries [1].

### **1.2 Aeroelasticity**

One of the most important fields of FSI problems is “aeroelasticity”. According to Bisplinghoff et al [2] aeroelasticity is the *phenomena which exhibit appreciable reciprocal interaction (static or dynamic) between aerodynamic forces and the deformations induced thereby in the structure of a flying vehicle, its control mechanisms, or its propulsion systems*. According to the Collar’s definition in 1946 aeroelasticity could be shown as a triangle shown in Figure 1.1. More definition about the aeroelasticity can be found in [3-5].



**Figure 1.1 :** Aeroelastic triangle of Collar

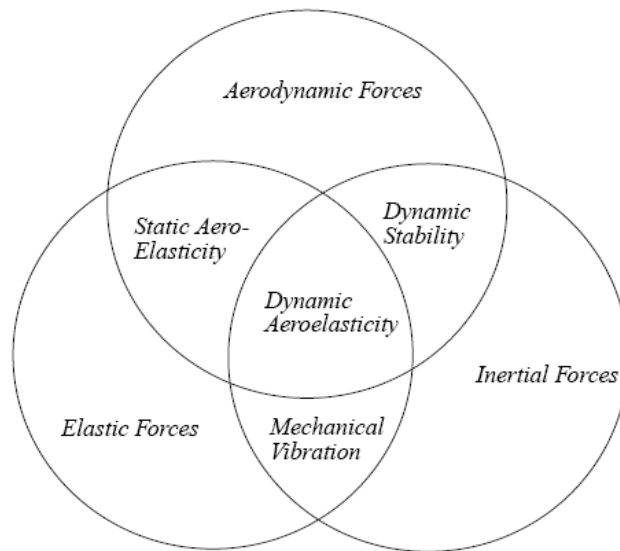
The problems of aeroelasticity have proved to be among the most important design leading concerns in the past decades. Aeroelastic problems occur because the structure is not totally rigid, it has a flexible nature. When external aerodynamic forces act on a flexible structure, they will deform the structure because of the inertial and elastic forces acting on the structure as seen in Figure 1.2. Moreover, this deformation in the flexible structure will lead to additional aerodynamic loads.



**Figure 1.2 :** Deformation of wing due to aerodynamic loads

Aeroelasticity can be grouped in two parts: Static aeroelasticity and dynamic aeroelasticity. Figure 1.3 shows the behavior of an aeroelastic problem and the result of the interaction forces that forms the aeroelastic concept.





**Figure 1.3 :** Aeroelastic forces and their interaction

Static aeroelasticity deals with problems like divergence and control reversal. The static deformation of the structure leads to a different aerodynamic load distribution on the structure. The divergence occurs at a speed called divergence speed and it deflects the lifting surface. The increase in the load leads to an increase in the deflection of the structure and after a point (divergence speed) the structure comes to a failure. Control reversal is the loss of the control surface because of the structural deformation of that surface.

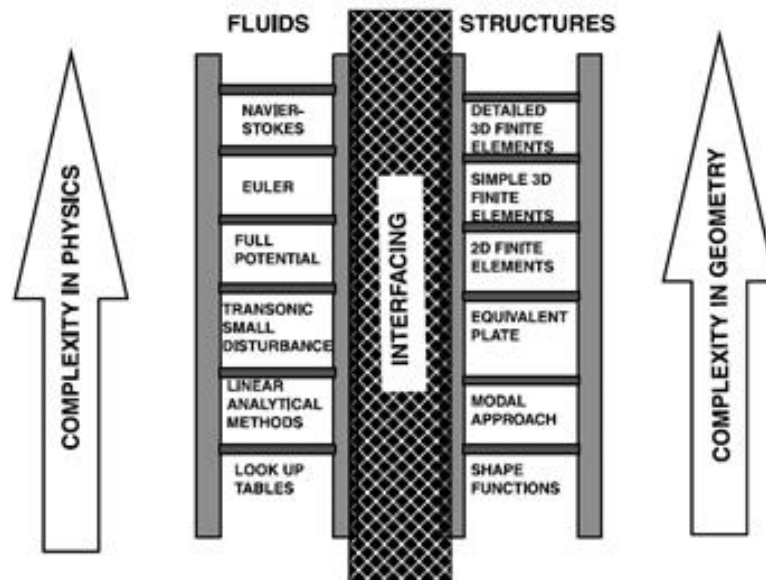
Dynamic aeroelasticity deals with problems like flutter and dynamic response. Flutter is an oscillatory dynamic instability of the structure because of the elasticity of the structure and the mass distribution. Moreover, flutter becomes extremely catastrophic at high speeds flights. The speed that flutter occurs is called the flutter speed. Dynamic response of an aircraft is its response to a transient force such as gusts or other dynamic loads.

### **1.3 Computational aeroelasticity**

The result to investigate the aeroelastic problems is the emergence of the aeroelastic codes to simulate the physics of the fluid-structure interaction. Since the area deals with both fluid and structure, the governing equations (or domains) have to be coupled by using efficient algorithms. In order to solve aerodynamic side of the problem computational fluid dynamics (CFD) codes and for the structural dynamics side computational structural dynamics (CSD) codes are developed. The coupling of

a CFD and a CSD code in a computational manner is defined as “computational aeroelasticity (CA)” [6].

Complexity of an aeroelastic problem depends on not only the theory or method which will be used to solve the aerodynamic and structural forces but also the interfacing between these forces. For the CFD side look up tables, linear analytical methods, transonic small disturbance, full potential or high fidelity Euler/Navier-Stokes solver can be used. For the CSD side shape functions, modal approach, 2D finite elements, simple 3D finite elements or high fidelity 3D finite element codes can be used. Figure 1.4 is taken from Guruswamy’s review work for the fluid-structure problems to understand the complexity of the FSI problems [7].



**Figure 1.4 :** Levels of fidelity in FSI modeling

## **2. COMPUTATIONAL AEROELASTICITY LITERATURE REVIEW**

### **2.1 What is computational aeroelasticity?**

The problems of aeroelasticity have been proved to be among the most important design leading concerns in aircraft design in the past decades. Since the area deals with both the fluid and the structure, the governing equations (or domains) have to be coupled using efficient algorithms. This review of literature will make use of the surveys published in the past few years to demonstrate where the field of aeroelasticity is heading to. Then, published work of several prominent authors in the field is examined.

As previously expressed, a major problem in aeroelasticity is the transformation of physical data between fluid and structure models (i.e., pressure and displacement field). While the structural model could be simple, this may not be the case with fluid model or vice versa. Thus, different methods are used to couple and evaluate the models. There are three methods of coupling the two models as mentioned in the work of Kamakoti et al [10] and Smith et al [8].

The first of these is the fully coupled method where the governing equations of the fluid and structure domain is written as a single set of equations and solved. Usually, the structural model is simple such as plates and beams while the fluid solver uses Navier-Stokes equations [8]. Fully coupling is usually considered computationally expensive and generally used for 2D models (such as beams and plates).

The second one is the the “closely coupled method” which is widely used. In this method, the transformation of the data between two domains is done by different modules and transformed at each step. The fluid is usually modeled using Euler/Navier-Stokes and the solid can be modeled by using finite elements such as solids, beams, shells and plates. Since the coupling is done with the transformation of data at each iterative step, the fluid and structural models can be changed according to the model [8].

The last method is the loosely coupled one. In loosely coupled method fluid and structure problems are taken as two sub-systems with external interactions between them. It is the simplest coupling type of FSI problems. It also allows designer to use validated in house codes for the simulation of fluid-structure interactions.

Another difficulty arises when interpolating/extrapolating the data between fluid and structure models. Such a difficulty can be overcome with an algorithm selected from a number of efficient ones. This subject is reviewed extensively in [8-10]. It can be said a number of efficient algorithms exist for certain types of problems, but as suggested in [8], multiquadratic biharmonic and thin-plate splines algorithms stood as the most promising ones.

## **2.2 Review of aeroelastic studies in the past decade**

Huttsell, Schuster, et al [9] evaluated some aeroelastic codes used to solve divergence, flutter, control surface buzz and a number of other aeroelastic problems. One of the codes is CAP-TSD which solves three dimensional transonic small disturbance potential flow equations (inviscid, compressible) for partial and complete aircraft configurations. The structure is modeled as thin plates and represented with modal shapes. No mesh movement is necessary so the code is computationally efficient. Another code is ENS3DAE which uses the Euler/Navier-Stokes equations to solve the fluid. It includes two different turbulence models and uses mode shapes to represent the structure. It incorporates dynamic mesh algorithms and is usually run on an 8-10 processor computer. The last one is CFL3DAE which also solves Navier-Stokes equations and uses mode shapes that represent the structure linearly. The primary difference between CFL3DAE and ENS3DAE is that the first uses finite volumes as the second one uses central finite difference formulation. Several models including an aeroelastically tailored model, an F-15 flutter model and an AV8B wind tunnel model are employed to solve different problems (that has nonlinear behaviors) and evaluate the codes. The results obtained are in favor of CAP-TSD for simple geometrical and physical models. Otherwise, CFL3DAE is more robust since it has more recent mesh and turbulence formulation with a better algorithm. However, it is suggested that the Euler/Navier-Stokes solution of the flow should be limited to static phenomena since it is computationally expensive for dynamical problems.

Dowell, Carlson et al [11] suggested two different reduced-order models for highly nonlinear aeroelastic problems. These methods are; “the proper orthogonal decomposition method” which is analogous to structural modes and “the harmonic balancing model” which involves solving the Navier-Stokes or Euler equations without having to integrate time integrations to predict dynamic behavior. The two models are solved for the flow over a cylinder and the results are compared. The results show good agreement with the experimental data.

Farhat [12] addresses some issues related to computational problems in aeroelasticity. He concluded that the stability of arbitrary Lagrangean/Eulerian formulation of Navier-Stokes or Euler equations is proved and a mature way to represent dynamic meshes. It is also suggested that the spring method or co-rotational method is used as mesh deformation algorithms. The AERO code which is presented as an example of the mentioned accomplishments proved to solve a complete aircraft configuration giving valuable insight to aeroelastic problems.

In the study of Gordnier et al [13], a nonlinear structural solver is coupled with a Navier-Stokes solver to model aeroelastic effects on an isotropic plate. The finite element model is based on the von Karman plate equations for an isotropic plate and the mesh is composed of uniform elements with four nodes. The structural solver is first validated for both clamped and pinned models, then the aeroelastic problem of the plates are solved. It is stated that the results are in good agreement with experimental data.

Lohner et al [14], has addressed the coupling issue and suggested using ALE scheme for discretization of the fluid/structure domain and obtained efficient dynamic meshes. Attention is also directed to some drawbacks of the ALE formulation in certain cases.

Massjung [15], used 2D Euler and von Karman equations for fluid and structure modelling respectively for solving flutter and bifurcation problems. The domains are discretized with a so called “energy budget of the continuous problem” method and predictor strategies and fixed-point iterations are employed for coupling. The method is validated for the aeroelasticity of a plate. It is also shown that the discrete geometric conservation law for predicting the stability of dynamic grids proposed by

Farhat and Lesoinne is in compliance with the energy method used. The results show that the convergence of the solution is directly dependent on the time step taken.

Newman, et al [16], has done a nonlinear aeroelastic wing analysis by solving nonlinear Euler equations for subsonic, transonic and supersonic flows. The structure is modeled with tetrahedrons allowing complex geometries. A convergence criterion is established with “interaction analysis control” where the interaction between two domains is terminated when this criterion is satisfied. As a result, only 10% more time is required for solving when compared to static wing analysis. It is also noted that unstructured solid mesh allowed observing the stress gradients along the structure which is impossible with modal representation.

In the work of Suleman et.al. [17], the structure is modeled with co-rotational finite element theory and a staggered algorithm (improved serial staggered) proposed by Farhat and Lesoinne is used. The results show that the co-rotational theory can predict the limit cycle oscillations that are related with geometric nonlinearities which otherwise is predicted as unstable behavior when linear structural models are used.

In the work of Liu et.al. [18], the static aeroelastic computations for the AGARD wing is performed. The structural model is represented as modal shapes and the flow is solved with Euler/Navier-Stokes equations. The interpolation between the moving grids is achieved with spline matrixes. The original code used (ACES3D) is originally designed for solving dynamic behavior so the code is modified so that time-accurate terms are ignored. This approach is disadvantageous if large deformations occur so a relaxation method is employed to get convergence of the solution for these geometries. The code partitions the flow domain into multiple blocks that are distributed over a number of parallel processors so that computational efficiency is maintained. The results show that only 10% more time is needed for static aeroelastic solution when compared to a rigid solution. The relaxation method proves to be useful to get convergence of the solution when the model endures large deformations.

In the work of Gruswamy et.al. [19], the divergence speed, aileron reversal problems are investigated for a wing with a control surface. The flow is solved with Reynolds averaged Navier-Stokes (RANS) formulation while the aeroelastic equations of

motions is solved using Rayleigh-Ritz method which uses assumed modes to find aeroelastic displacements. The flow equations are solved using an upwind differencing scheme. From the results, it is shown that in the transonic regime the Navier-Stokes equations could predict the aeroelastic behavior well though a better turbulence model could lead to better predictions.

In the work of Relva et.al. [20], an integrated solution method is proposed by Newmann and Newman et al [21] such that the fluid and structure equations are solved separately and matched at boundaries. The method is compared to domain decomposition methods which utilizes several domains while the present approach only employs two domains (fluid and structure) and interfaces them at the boundaries of these two domains (i.e.: the surfaces of the structures). The structure and the flow are modeled with finite elements and the Euler equations. The aerodynamic forces are transferred at the boundaries of the domains by using lumped forces technique.

The configuration is a full aspect ratio wing with a truss frame. Spring method is used to move the surface mesh. System convergence criterion is the rms of the wing surface deflections. The analysis is run for three different flow conditions including subsonic, transonic and supersonic and loss of lift is observed especially for the transonic case.

In the work of Karpel et.al. [22], dynamic equations for the modal representation of the structure are solved by converging the solution to a steady state by introducing an artificial structural damping. The configuration is a rocket with fins at the back. Euler equations are solved for inviscid flow. Modal equations are used to overcome the singularity problem in a free-free configuration. The analysis is run for a stream speed of 3.5 Mach and an angle of attack of 5 degrees. The results show that while the aeroelastic deflections can be neglected, the lift distribution and moment coefficient changes significantly.

In the work of Schuster et.al. [23], the static aeroelastic analysis of an aeroelastically tailored wing is performed. The aim is to predict vortices, shock waves, separated flow in an unsteady flow using Navier-Stokes equations. The code used includes its own grid generating technique which is called zonal grids. Either the influence coefficient or modal equations can be used to solve static deflections. It is argued that though the influence coefficient model demands much more memory and storage

(convergence requires more grid points) when compared to modal equations, the influence coefficient model gives more reliable results and worth the extra time. A simple algebraic method is used to deflect the grid. The pressure coefficients and aeroelastic deflections are calculated. The results show that the turbulence model (Baldwin-Lomax model) used predicts the flow separation location aft when compared to the experimental data. The pressure coefficients seem to correlate with the experimental pressure coefficients.

In the study of Liu et al [24], the closely coupled method utilizes multiple grids and multiple domains to predict static aeroelastic behavior. The grids are interfaced using the spline matrix interpolation method. The test case is a cantilevered wing (AGARD 445.6). The spring method is used to deflect the grids and the code is parallelized using domain decomposition. Modal equations are used to solve static deflections by using an artificial structural damping ratio that forces the system into steady state. The method proposed works in case of small deformations, but for large deformations a relaxation procedure is utilized to overcome convergence issues. Both the Euler and Navier-Stokes equations are used to solve the flow and the solutions are compared. Significant differences between the two solutions arose such as flow separation prediction, twist and pressure coefficients.

In Guruswamy et al's work [25], an arrow-like experimental configuration is used for unsteady transonic static aeroelastic computations. Both rigid and flexible solutions are obtained and compared. The effect of flap deflection on the aeroelastic characteristics is considered. An artificial damping term is introduced to dynamic modal equations to converge the solution to steady state forcefully. The wing is modelled as a flat plate and aeroelastic deflections at various stations along the span and pressure distribution are evaluated. The results show that significant lift loss (compared to rigid solution) related with aeroelastic behavior is observed. It is concluded that the computed solution correlates well with the experimental data.

Guruswamy et al [26], argued that the use of wing box structure made modal equations impractical since it would be difficult to find a mode shape compatible with the aeroelastic deflection of the structure that includes a wing box. Instead finite element analysis is employed using different kind of elements. Further, the structure can have composite material properties which would be difficult to implement with modal representation. The in-plane motions of the membrane elements used to model



panels are neglected, a so called static condensation method is used and chord wise rigidity is assumed to decrease computation time. Several schemes for transferring aerodynamic loads on the structure are proposed in the work. It is concluded that promising static aeroelastic results are obtained and the most important outcome of the work is assumed to be the usage of full finite element model which is advantageous since stress distribution is also obtained for the structure.

Kamakoti et al [27], developed a pressure based solver for aeroelastic problems. Full Navier-Stokes is solved for the AGARD 445.6 wing model and a membrane model without compressibility effects. The membrane structure is modeled using shell elements using hyper elastic Mooney's law. Multiple grids are used to solve structure and fluid equations and the interfacing is done with linear interpolation and extrapolation. The domain is divided into blocks for parallelization and new methods such as numerical diffusion for convection and pressure terms are used. As the turbulence model, the widely used k- $\epsilon$  model is adopted. The aerodynamics is solved to obtain pressure on surface of the structure so that these values are converted to nodal forces acting on the structure. As in similar studies, the cross section of the AGARD wing is assumed to be rigid which leads to easy prediction of twist and spanwise deflection. Pressure distribution and aeroelastic deflections are computed for both models.

Posadzy et al [31] used the CFD solver TAU developed in Institute for Aerodynamics and Flow Technology (DLR) and the CSD solver MF3 to study the both static and the dynamic aeroelastic behavior of the AGARD 445.6 wing in a loosely coupled manner. TAU code is a three dimensional code based on finite volume scheme for solving Reynolds-averaged Navier-Stokes (RANS) equations.

Cavagna et al [32] in their study used an interfacing method that can be applied on unmatching meshes based on Moving Least Squares (MLS). Conversation of momentum and energy between the disciplines are kept by using MLS. They used FLUENT for the fluid solver and the MSC-NASTRAN for the structural solver for the aeroelastic analysis of the AGARD 445.6 wing. They used a user defined function (UDF) to implement the grid deformation and scheme for the Crank-Nicolson algorithm for FLUENT.

Feng and Soulaïmani [33] developed a nonlinear computational aeroelasticity model using tight coupling algorithms. They used an Euler based nonlinear CFD solver and a linear CSD solver to use this algorithm. Moreover, they used a matcher for the fluid-structure interface to transfer the displacement and the loads. For the dynamic mesh motion they used the ALE formulation.

Kuntz and Menter [34] used the commercial software packages to perform an aeroelastic analysis of the AGARD 445.6 wing. The high fidelity non-linear finite element solver ANSYS and the general purpose finite volume based CFD code CFX-5 are used for the fluid-structure problem. Mesh based Parallel Code Coupling Interface (MpCCI) [35] is used for the interfacing and data transfer between CSD and CFD solvers. Also, in this thesis study, MpCCI will be used for the aeroelastic analysis and more information about the MpCCI will be given in the following chapters.

Thirifay and Geuzaine [36] studied the AGARD 445.6's aeroelastic problems both with steady and the unsteady approximations in a loosely coupled method. In their study they used a three dimensional unstructured CFD solver developed in CANAERO and a CSD solver "the SAMCEF Mecano code" [37] for their analysis. They used the ALE method for the moving mesh method. MpCCI is used for the aeroelastic code coupling tool.

Yosibash et al [38] designed an interface to couple a parallel spectral/hp element fluid solver "Nektar" with the hp-FEM solid solver "StressCheck" for the direct numerical solution (DNS) over a wing. They validated their method on the well documented AGARD 445.6 wing. ALE formulation is used for the fluid-structure coupling. They used the one-way coupling method with linear assumption for the structural response and the two-way coupling method which considers the non-linear effects of the structure. As the solvers are run on different platforms they used sockets for the data transfer.

Love et al [39] used the Lockheed's unstructured CFD solver SPLITFLOW and the MSC/NASTRAN CSD solver for the aeroelastic computations of an F-16 model in a max-g pull-up maneuver. They used a loosely coupled method for the analysis. Data transfers between the codes are done by using Multi-Disciplinary Computing Environment (MDICE).

Heinrich et al [40] used the DLR'S unstructured TAU code with MSC/NASTRAN finite element solver for the aeroelastic analysis of an A340 like aircraft. MpCCI is used for the loosely coupling of these codes.

More information about the success, progress and challenge of computational aeroelasticity can be found on the review work of Schuster et al [58].

### **2.3 Conclusion**

In the last 20 years, significant advances have been gained in the field of aeroelasticity as seen from above studies. The first studies generally aimed at solving the flow around a rigid structure. (These studies were not included in the review.) With more computational power, the theory of the solvers shifted from the simple models such as transonic disturbance model to Euler and/or full Navier-Stokes equations with turbulence models. This led the way to predict complex flows with turbulence, flow separation, viscosity, compressibility etc. After these studies, the time had come to inspect the fluid-structure interaction. In the first years of the field, simple structural models were used to predict static elastic deflection. As more computational power is gained in time, finite element analysis for complex structures became more favored. Later on, the work was more focused on the problems of aeroelastic modeling such as the interfacing of the fluid and structure domains, faster algorithms for solving the flow and structure equations, algorithms for grid generation and deflection, grid generation for complex models.

As the number of solvers increased, the need for experimental data arose to validate these codes. The wind-tunnel models are specifically designed to collect data related with flow and aeroelastic behavior. The most used and widely known ones are the AGARD 445.6 aeroelastic configuration, the aeroelastic research wing (ARW-2) and an arrow-like configuration [28-30].

Some of the work in the field of aeroelasticity is summarized in Table 2.1. It includes the details such as the fluid and structure model, interfacing technique, grid moving method etc.

The aeroelastic problems which MpCCI is used for the coupling interface are given in Table 2.2 for a better look-up.

**Table 2.1:** Review of some methodologies for aeroelastic applications

<u>Author</u>	<u>CFD Solver</u>	<u>Structural Solver</u>	<u>Moving Mesh Algorithm</u>	<u>Interfacing Method</u>
Cunningham et al <sup>[27]</sup>	TSD	Modal	none	None
Robinson et al <sup>[27]</sup>	Euler	Modal	Spring Method	None
Lee-Rausch and Batina <sup>[27]</sup>	Navier-Stokes	Modal	Spring Method	None
Soulaimani <sup>[27]</sup>	FEM Based	(Commercial)	ALE	None
Liu, et al <sup>[24]</sup>	Euler	FEA	TFI	Spline method
Farhat and Lessoine <sup>[27]</sup>	Navier-Stokes	FEA	ALE	Conservative geometric law
Kamakoti et al <sup>[27]</sup>	Navier-Stokes	Bernoulli-Euler Beam	TFI	Linear Interpolation & Extrapolation
Guruswamy et al <sup>[26]</sup>	Navier-Stokes	FEA	Grid Generation	Local Conservation Scheme
Newmann et al <sup>[16]</sup>	Euler	FEA	Spring Method	Lumped forces technique
Liu et al <sup>[18]</sup>	Euler or Navier-Stokes	Modal	AIM3D (Grid remesher)	Spline Method
Schuster et al <sup>[23]</sup>	Euler or Navier-Stokes	Influence Coefficient or Modal	Algebraic Shearing	None

**Table 2.2:** Review of some couplings done by MpCCI

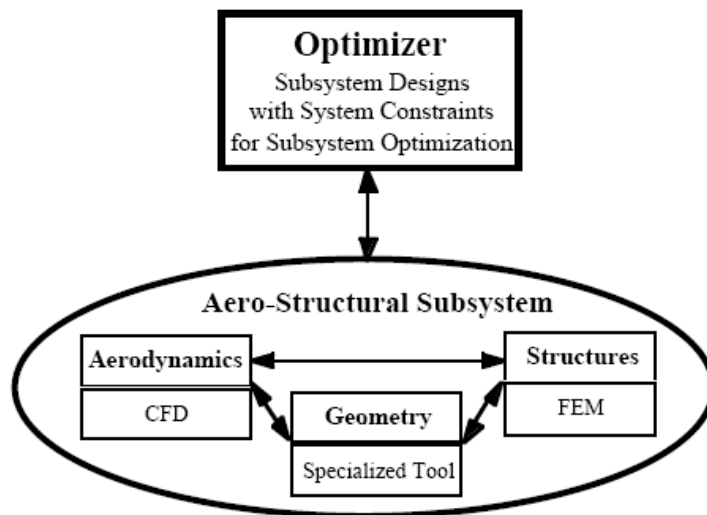
<b><u>Author</u></b>	<b><u>CFD Solver</u></b>	<b><u>Structural Solver</u></b>	<b><u>Interfacing Method</u></b>
Kuntz and Menter <sup>[34]</sup>	CFX-5	ANSYS	MpCCI
Thirifay and Geuzine <sup>[36]</sup>	CANAERO's CFD	MSC/NASTRAN	MpCCI
Heinrich et al <sup>[40]</sup>	DLR's TAU	MSC/NASTRAN	MpCCI

### 3. MULTIDISCIPLINARY DESIGN OPTIMIZATION

#### 3.1 Need for multidisciplinary design optimization

Aircraft design is a complex engineering process that depends on the interaction of different disciplines so that the system of these disciplines must be thought as a coupled system.

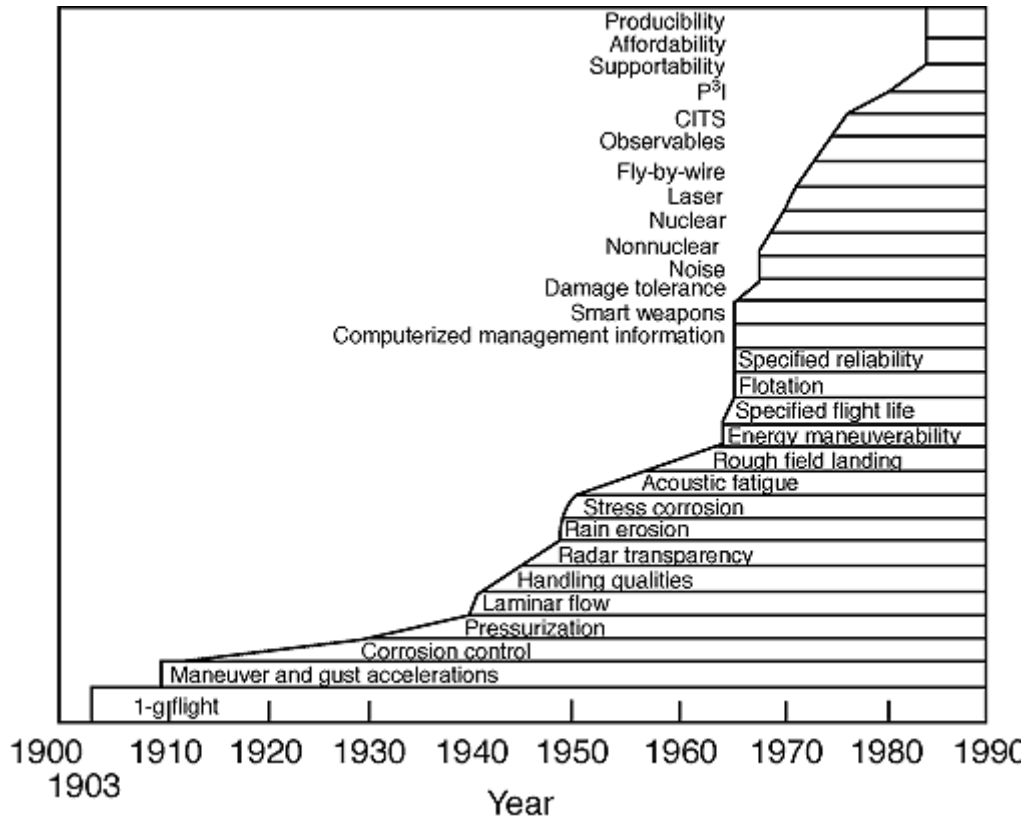
The nature of a coupled system is that one design variable can be used by other disciplines or an output for one discipline could be input for the other disciplines. For instance, design of an aircraft wing with low weight would improve the aerodynamics performance but this will increase the flexibility of the wing which may lead to aeroelastic instability. Such a system can be solved by aeroelastic optimization. A simple representation of aero-structural optimization is shown in the following figure.



**Figure 3.1** : Simple aero-structural optimization scheme [60]

Therefore, this contradictory situation in aircraft design optimization process disciplines such as aerodynamics, structural dynamics, propulsion, flight controls, etc. must be thought as a whole system to find the optimized design. Moreover design requirements have increased with the parallel increase in computer

technology. Figure 3.2 shows the increase in the aircraft design requirements over time.



**Figure 3.2 :** Design requirements expansion [43]

Increase in the design requirements, complexity and the computational cost issues regarding to the multi-disciplinary design are resulted in a concept referred as “Multi-Disciplinary Optimization (MDO)”. According to the Alexandrov and Lewis [41] MDO is defined as “*systematic approach to optimization of complex, coupled engineering systems*”. For more definition and aspects about MDO can be found in Sobieszczanski-Sobieski’s survey work [42].

Solution of MDO problems can be done by using gradient based or gradient-free algorithms. For the gradient based algorithms search direction is found by using derivatives (sensitivities). For gradient-free algorithms (like genetic algorithms) rule based or random combinations of the design variables are produced in a population to find the optimum solution.

### 3.2 Aeroelastic optimization literature review

The simultaneous optimization of the aerodynamic and the structural disciplines is the one of the most studied topic in MDO [42]. While obtaining the minimum weight objective, the structure generally becomes more elastic and aerodynamic loading on the structure changes. This generally yields aerodynamic loading problems. Solution procedure of the aeroelastic optimization problem can be just done by a correct prediction of aerodynamic and structural loads.

First studies on the coupled aerodynamic and structural analyses were based on simple tools based on linear theories such as panel methods and beam elements. [44-50]. Dovi et al [49] used laminated plate formulation for the structural analyses and the lifting surface formulation for the aerodynamic analyses to perform aeroelastic analyses of a supersonic transport aircraft. Whitflow and Bennett [44] used a nonlinear full potential analysis code and a linear structural analysis to investigate the static aeroelastic analysis of a three-dimensional wing. Moreover, Pitman and Giles [46] used an equivelant plate structural analysis method for the structural analyses part of a three-dimensional wing's aeroelastic design. Friedman [48] used thin walled, rectangular box section to represent the structural members at each span-wise station with a finite element method implementation.

Because of the fact that linear theories have some fallbacks at transonic regimes, more capable finite element and finite volume methods have been developed for the analyses. Advances in the computational field played a vital role in this development. High fidelity codes are used in single discipline optimization problems for structural [59] and aerodynamic fields [51-57]. In the studies of Burgreen and Baysal [51] and Korivi et al [52] Euler equations were used for the aerodynamic optimization. Navier-Stokes equations are used in the studies of Kim et al [57] and Sasaki et al [53] for the aerodynamic optimization of a wing.

As the high fidelity codes used in the optimization problems for one discipline are successful, multidisciplinary optimization studies have been performed by using these codes. Aeroelastic optimization studies have been widely studied. Mostly inviscid Euler equations are used for the computational time issues for these studies.

Newman and Anderson [61] used 3D unstructured Euler code FUN3D and finite element analysis to perform the aeroelastic solution for the aeroelastic optimization



of ONERA 6 wing. For the linear structural analysis it is known that stiffness matrix is symmetric and positive definite. For the derivation of the output functions Automatic Differentiation of FORtran (ADIFOR) and for the derivatives complex step method is used. For the mesh motion they used the spring analogy method.

Gumbert et al [62] performed their coupled analysis for a simple 3D wing by using a linear finite element structural solver and an inviscid Euler solver CFL3D. They used the simultaneous aerodynamic analysis and design optimization environment SAADO to perform the optimization process. Gradients for the aerodynamic part are calculated by ADIFOR. They found maximum lift over drag ratio with constraints on maximum payload, root bending, pitching moment and minimum section thickness, leading edge radius. Moreover, sequential quadratic programming algorithm was used for the optimization.

Giunta and Sobieszczanski-Sobieski [63] have done their aeroelastic analysis and optimization study by using government/commercial and off-the-shelf softwares. The NASA Langley's finite element analysis- optimization package GENESIS and Euler solver CFL3D, finite element solver MSC/NASTRAN and geometry translators G/COTS were used. 64 optimization parameters were used to describe the wing planform and shape to minimize the drag while lift and the chord length at the wing leading edge break location constraints are used. They used SQP method for the optimization of a high speed civil transport (HSCT) wing.

Barcelos et al [64] developed an Schur-Newton-Krylov method to find the gradients for a nonlinear fluid structure problem. They studied quasi-static aeroelastic analysis of ARW2 wing. Inviscid Euler flow was modeled with a 2<sup>nd</sup> order finite volume discretization with Roe flux scheme. They used a parallel PC cluster environment with 8 processors with double precision. Their optimization problem was to minimize the drag-to-lift ratio subjected to constraints on both for the aerodynamic (lift-to-weight change ratio) and the structural (vertical displacements and von Mises stress) sides.

One of the latest work on aeroelastic design optimization has been performed by Barcelos and Maute [73] with a gradient based algorithm. Structure was modeled with a geometrically nonlinear finite element method. Navier-Stokes equations on

moving grids augmented by turbulence models were used to define the flow field. Optimization problem is similar to one used in [64].

More work on aeroelastic optimization with inviscid flow can be found in [65-68].

Optimization problems can be generally solved by gradient-based algorithms or gradient-free algorithms. In this study optimization problem will be solved by using a genetic algorithm which is a gradient-free algorithm. Some of the aeroelastic optimization problems solved by gradient based algorithms are well described in [69-72].

In the work of Maute et al [69] multidisciplinary optimization of a wing was done by using a sequential quadratic programming algorithm to find the gradients. Optimization variables are determined by an analytical approach. In another study of Maute et al [70] and Nikbay [71] gradients were found by an adjoint approach for coupled sensitivity analysis.

Genetic algorithms can also be used instead of gradient-based algorithms for the aeroelastic optimization problems. Genetic algorithms are found to be robust for finding the global optimum [76]. Since, genetic algorithms do not need to calculate the gradients, they are easier to implement. Multidisciplinary optimization studies based on genetic algorithms are well defined in [74-79].

Kim et al [74] used both genetic and gradient based algorithm to perform a multidisciplinary design optimization of a supersonic fighter wing. They used Euler equations for the CFD part and a 2D plate model for the structural model.

Oyama et al [75] applied genetic algorithm to a practical 3D shape optimization for aerodynamic design of an aircraft wing. CFD part is solved by Navier-Stokes equations. Maximizing the lift over drag ratio was the goal of the study with subject to a structural constraint. To reduce the computation time they used a parallel computer with 166 vector-processing elements.

Garrier [77] worked on construction of an automated MDO system for the wing design of a HSCT (High-Speed Civil Transport) aircraft. Both gradient algorithms SQP and a stochastic genetic algorithm GADO (Genetic Algorithm for Continuous Design Optimization) were used during in his study. The multi-disciplinary analysis process was composed of part of modules with simple in-house codes. ONERA CFD solver elsA, commercial mesh generator ICEM-Cfd and commercial FEM code

MSC/NASTRAN were used to perform the analysis. A python code was written to automate the analysis process. The objective of this study was to maximize the aircraft range with subjected to multiple design constraints from various disciplines.

Another design optimization of a wing with genetic algorithms was studied by Sasaki et al [53]. Their objective functions were minimizing the drag in supersonic and transonic flight and minimizing the bending moment at the wing root. A total of 66 design variables were used to define the wing shape. Moreover, a Navier-Stokes solver was used during the analysis.

Obayashi [78] used multiple-objective genetic algorithm (MOGA) for the multidisciplinary optimization of transonic wing planform. Minimizing aerodynamic drag, minimizing wing weight and maximizing fuel weight stored in wing tank were the objectives of the study. They put some constraints for the problem. On the aerodynamics side lift should be greater than the given aircraft wing and on the structural side structural strength should be greater than the aerodynamic loads.

Kim et al [79] also performed multi-objective and multidisciplinary optimization of a supersonic fighter wing. They used genetic algorithm. Moreover, control of the multiple objectives was done by defining weights for the objective functions.

### **3.3 Conclusion**

In aerospace industry the design requirements have increased widely with respect to the economical and technological issues. Interaction of different disciplines is put into a concept called multidisciplinary design (MDO). One of the most studied fields in MDO concept is aeroelastic optimization. For the solution of this problem optimization algorithms based on gradient and non-gradient algorithms like genetic algorithms are used. In this thesis, both algorithms will be used and a comparison will be done between them.

## 4. COMPUTATIONAL AEROELASTIC PROCEDURE

### 4.1 Computational structural dynamics solver

In this thesis study ABAQUS finite element solver is used for the structural solver. ABAQUS is a commercial software package of finite element analysis software for computational mechanics modeling and simulations [83]. All of the structural analyses are done by linear static analysis approximation. Finite element method (FEM) is based on dividing a whole structure into smaller domains. The solution procedure for a FEM in structural analysis can be given as follows;

The first step is the processing step. In this step, the finite element model is built, the constraints and loads are defined. Moreover, mesh is prepared in this step. Next step is FEA solver step. In this step, the model is assembled and the system of equations are solved. Last step is the post-processing step. In this step the results are sorted and displayed.

The equations of motion for a structure can be written as follows in a generalized way;

$$[M]\{\ddot{u}\}+[D]\{\dot{u}\}+[K]\{u\}=\{F_a\}+\{F_e\} \quad (4.1)$$

Where;

$[M]$  is the mass matrix

$[D]$  is the damping matrix

$[K]$  is the stiffness matrix

$u$  is the displacement column matrix

$(\dot{\quad})$   $(\ddot{\quad})$  are the time derivatives

$\{F_a\}$  is the aerodynamic force column matrix

$\{F_e\}$  is the external load column matrix

In this study where the analysis will be performed as static analysis the time terms with the time derivatives of the equation (4.1) will be neglected. Moreover, in the aeroelastic analysis only the aerodynamic forces will be taken into account.

Therefore, by using the assumptions above the system of linear equations generated by the finite element method can be written as follows;

$$[K]\{u\} = \{F_a\} \quad (4.2)$$

Displacements will be calculated by ABAQUS by using the aerodynamic loads calculated from the flow solver.

#### 4.2 Computational fluid dynamics solver

In this study aerodynamic loads will be calculated by FLUENT commercial computational fluid dynamics solver. FLUENT is used for modeling fluid flow both for structured and unstructured grids by using Navier-Stokes/Euler equations [84]. A finite volume based approach is used to define the discrete equations. FLUENT has two solvers: a segregated and a coupled solver [84]. The segregated solver is for modeling the low speed or incompressible flow. In this thesis, since the flow will be in transonic regime and the compressibility effects should be taken into account, the coupled solver will be used [84].

The fluid solver of the FLUENT solves the governing equations of continuity, momentum and energy simultaneously [84]. In this study flow will be assumed as inviscid and Euler equations will be used. This is a valid approximation for high Reynolds number flows according to the Prandtl's boundary layer analysis. Moreover, according to the Barcelos and Maute [73] inviscid flow models gives acceptable results for maximizing the lift/drag optimization problems for transonic cruise conditions.

The general Euler equations, in conservation form can be written as follows;

$$\frac{\partial U}{\partial t} + \bar{\nabla} \cdot \bar{F} = Q \quad (4.3)$$

where;

$U$  defines the conservative variables

$Q$  is the source term without heat sources just considers the body forces

$F$  is the flux vector with Cartesian components  $(f, g, h)$  given by;

$$f = \begin{vmatrix} \rho u \\ \rho u^2 + p \\ \rho uv \\ \rho uw \\ u(E + p) \end{vmatrix} \quad g = \begin{vmatrix} \rho v \\ \rho vu \\ \rho v^2 + p \\ \rho vw \\ v(E + p) \end{vmatrix} \quad h = \begin{vmatrix} \rho w \\ \rho wu \\ \rho wv \\ \rho w^2 + p \\ w(E + p) \end{vmatrix} \quad (4.4)$$

Here;

$\rho$  is the fluid mass density

$u, v, w$  are the velocity components

$E$  is the total energy per unit volume defined by,

$$E = \rho e + \frac{1}{2} (u^2 + v^2 + w^2) \quad (4.5)$$

As seen from Euler equations there are six unknowns  $u, v, w, p, E, \rho$  but only five equations to solve the system. Therefore, one more equation is needed to solve the set of equations. It is the well known perfect gas law equation given below;

$$p = \rho e \gamma - 1 \quad (4.6)$$

where;

$\gamma$  is the adiabatic index and is taken as 1.4

Governing equations are non-linear and coupled. In FLUENT in order to get convergence several iterations are performed [84]. Iterations are;

1. Depending on the current solution, fluid properties are updated.
2. Continuity, energy and momentum equations are solved simultaneously.
3. Convergence control is done.

This procedure is applied until the convergence criteria are met.

#### 4.2.1 Remeshing methods

In FLUENT mesh motion is accomplished according to the motion defined at the boundaries of the volume mesh. There are three mesh motion methods in FLUENT [84].

- Spring based smoothing method
- Dynamic layering
- Local remeshing methods

#### 4.2.1.1 Spring based smoothing method

Spring based smoothing method can be used to update a cell or a face zone whose boundary is deforming. Two mesh nodes of an edge are idealized as a network of interconnected springs. A force is formed proportional to the displacement along all the springs connected to the node. The force on a mesh node is defined as follows by the Hook's Law[84].

$$\vec{F}_i = \sum_j^{n_i} k_{ij} \Delta\vec{x}_j - \Delta\vec{x}_i \quad (4.7)$$

$\Delta\vec{x}_j, \Delta\vec{x}_i$  are the displacements of node i and its neighbor j  
 $n_i$  is the number of neighboring nodes connected to node i  
 $k_{ij}$  is the spring constant between node i and its neighbor j

The spring is defined as;

$$k_{ij} = \frac{1}{\sqrt{|\vec{x}_i - \vec{x}_j|}} \quad (4.8)$$

The net force should be zero at equilibrium. Then the mesh motion is solved by an iterative way by using the displacements at the boundaries till convergence.

#### 4.2.1.2 Dynamic layering

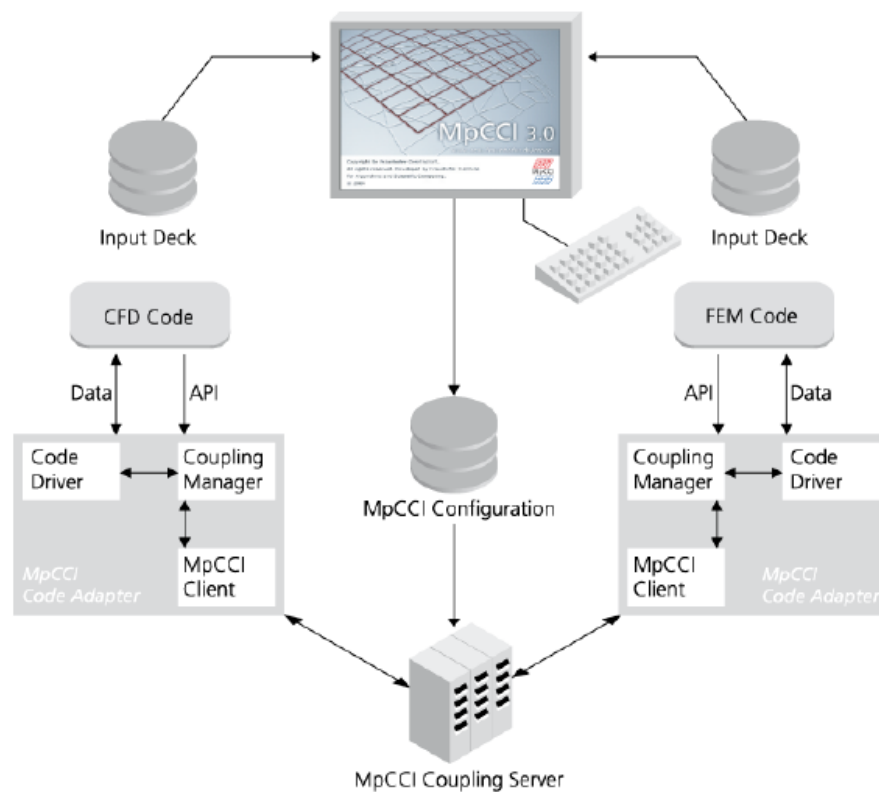
In our study CFD mesh is unstructured and with triangular elements. As this method is used for the wedges or hexahedras, in our study it will not be used [84].

#### 4.2.1.3 Local remeshing methods

Normally, FLUENT uses spring based smoothing method for the triangular meshes but when the displacements are large, this can lead to invalidation of the mesh and convergence problems. This problem is solved by checking the skewness of the elements [84].

### 4.3 Aeroelastic coupling

In this study MpCCI (Mesh-based Parallel Code Coupling Interface) as an aeroelastic coupling interface is used. MpCCI gives the opportunity to couple high fidelity simulation codes for multi-physics simulations. The advantage of using MpCCI is that it enables the exchange of data transfer between nonmatching meshes of CFD and CSD codes in a multi-physics simulation [85]. Coupling process is shown in the following figure.



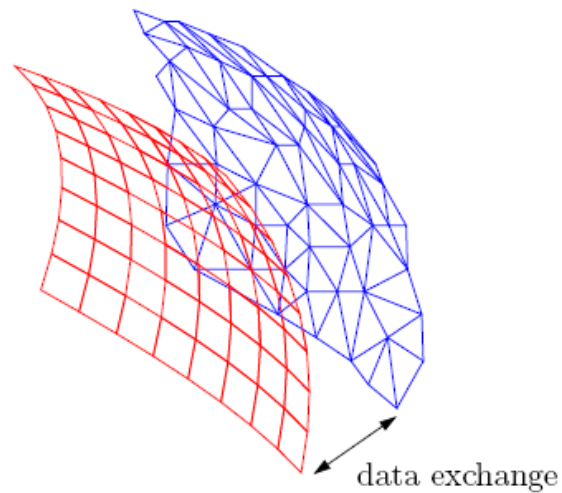
**Figure 4.1 :** MpCCI coupling process [85]

#### 4.3.1 Coupling regions

MpCCI supports several types of coupling regions and spaces. Line, surface or volume coupling depending on the element definitions can be done in two or three dimensional space.



### 4.3.2 Data exchange

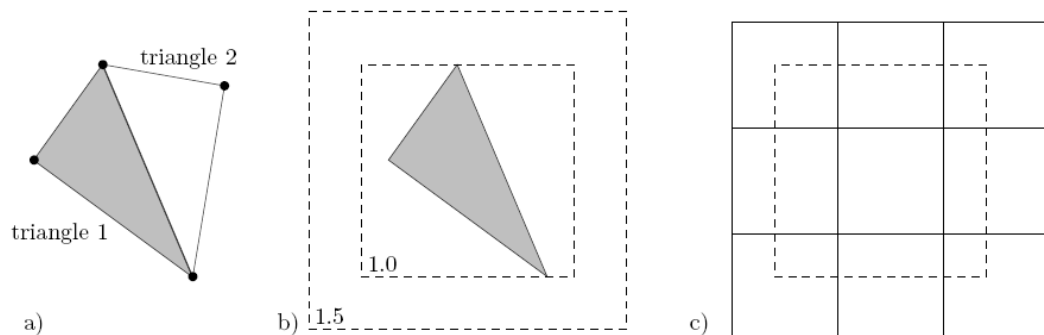


**Figure 4.2 :** Data exchange for unmatching grids [85]

Data exchange process can be grouped into three phases.

#### 4.3.2.1 Pre-contact search

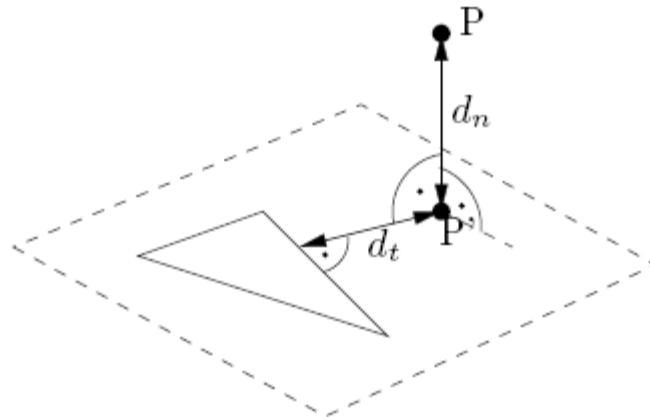
First of all to make the contact search easier the elements are split into triangles in 2D or tetrahedras in 3D.(a) Search for the elements is done by using the “Bucket Search” algorithm of MpCCI [85]. Then, each triangle is bounded by a box which includes the triangle.(b) After that step, “buckets” are formed by dividing the space into smaller squares or cubes. (c) Finally, a list is formed by listing the closer triangles to the bucket to use for the further steps for data transfer. Pre-Contact Search can be seen easily in the figure below.



**Figure 4.3 :** Pre-contact search [85]

#### 4.3.2.2 Minimal distance

Point-element relationships are used in the minimal distance algorithm. A list of triangles which belong to elements was formed in the pre-contact search step. In this step, the best triangle corresponding to the best element is determined and chosen. Relative positions of the triangles and the node P is used in this process [85]. Projection of the point P is taken onto the surface of each triangle as seen in the figure.



**Figure 4.4 :** Element selection [85]

#### 4.3.2.3 Intersection

Alternative way for association of the elements is based on the element-element association. In this algorithm, elements again divided into the smaller triangles, a bounding box is formed for the triangles and buckets are formed. Intersected areas are stored in a list with the results of the pre-contact search [85].

#### 4.3.2.4 Flux and field interpolation

Interpolation of the quantities (displacement, force, pressure,...) can be done by using a flux or field interpolation method [85]. In flux interpolation, the integral is preserved by adapting the value to the element sizes. This method is used for example for forces. In field interpolation, a conservative transfer is ensured by keeping the value of the elements. It is used for example for pressures.

### 4.4 Aeroelastic code coupling with MpCCI

To perform an aeroelastic coupling with MpCCI, four steps are defined [85].

- **Preparation of Model Files**

In this step FLUENT and ABAQUS models are prepared separately. The definition of the coupling surfaces (i.e. upper wing, lower wing, tip for a wing) are given in this step. Then, model files are written in input files for the CFD and CSD codes.

- **Definition of the Coupling Process**

The most important step of the aeroelastic coupling process is the definition of the coupling process step. FLUENT and ABAQUS models of the wing are chosen via user interface. Then, coupling regions described above, transfer quantities (nodal displacements from the CSD code and the pressure values from the CFD code) and the coupling algorithms are selected.

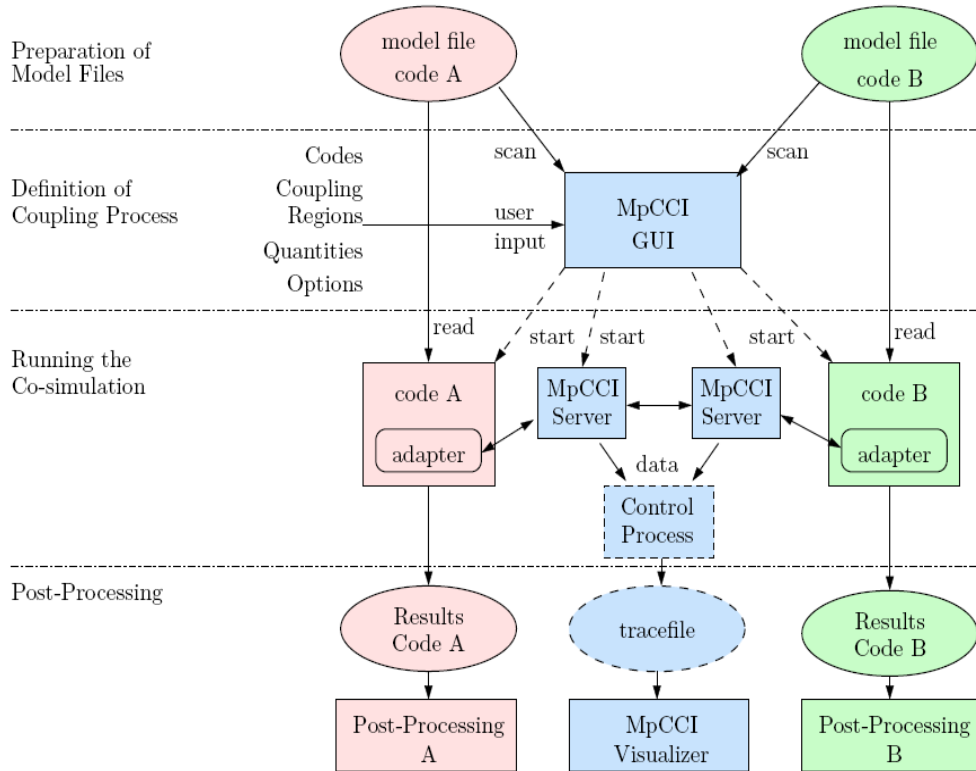
- **Running the Co-Simulation**

In this step aeroelastic analyses are performed. MpCCI controls the rest of the coupling process till to the specified coupling iterations or time.

- **Post-Processing**

Finally, the results for both CFD and the CSD code are examined by using the codes own post-processing tools.

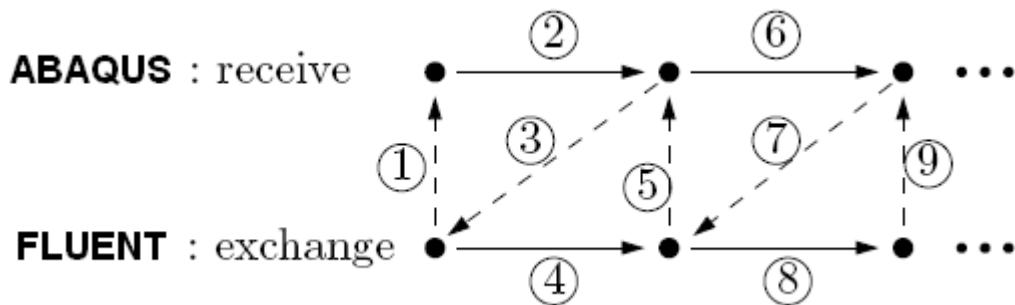
The aeroelastic coupling process written above is given in Figure 4.5. Code A represents the CFD solver FLUENT and code B represents the CSD solver ABAQUS.



**Figure 4.5 :** Aeroelastic coupling process [85]

#### 4.5 Aeroelastic coupling algorithm and solution procedure

In this study a staggered algorithm is used for the aeroelastic coupling. Ten aeroelastic couplings (data transfer) are performed during each optimization iteration. Staggered algorithm used in this study is given below in Figure 4.6.



**Figure 4.6 :** Staggered algorithm for the aeroelastic coupling [85 ]

After all the models are prepared, the solution procedure for the aeroelastic coupling can be divided into steps seen in Figure 4.6.

1. CFD code calculates the surface pressures and maps these pressures as nodal forces to the CSD code.
2. CSD code calculates the deformation of the structure under these pressure loads.
3. Calculated nodal displacement values are mapped onto the CFD modal as mesh displacements and mesh is updated.
4. CFD code performs the analysis.

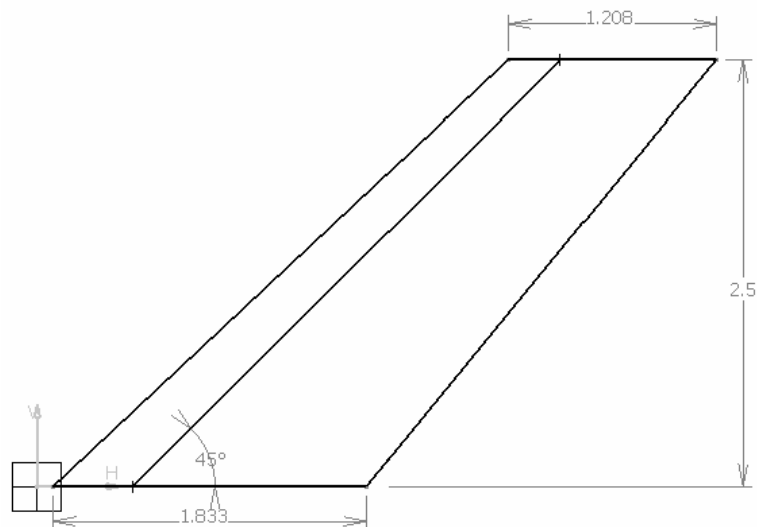
This solution strategy is performed until a specified coupling time or a number iterations is reached.

## 5. TEST CASE FOR AEROELASTIC COUPLING WITH MpCCI

### 5.1 Geometric model of AGARD 445.6 aeroelastic wing

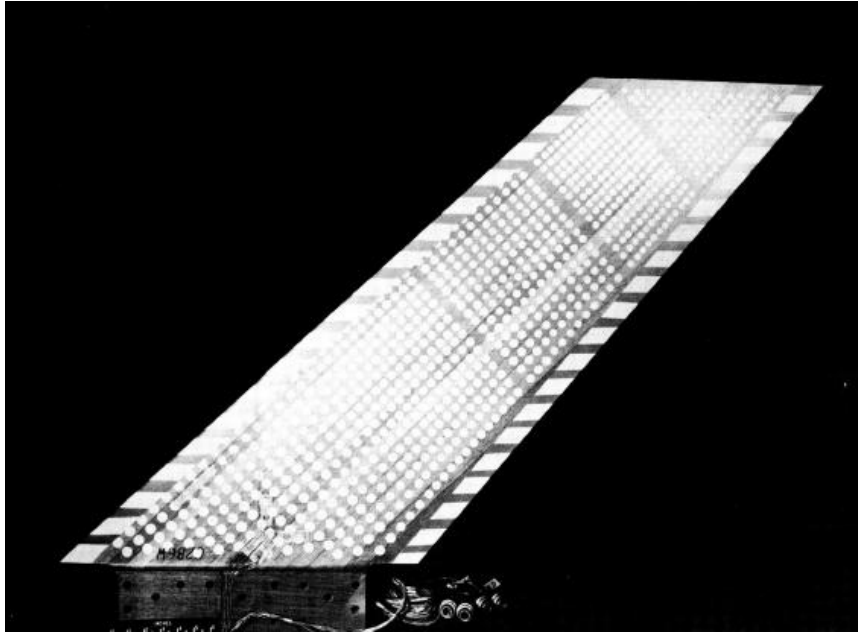
In this study the wing geometry used for the aeroelastic analysis is chosen as the well-known AGARD (Advisory Group for Aerospace Research and Development) 445.6 wing [28]. This wing is the first aeroelastic configuration that is tested by Yates et al [80] in the Transonic Dynamics Tunnel (TDT) at the NASA Langley Research Center.

The AGARD 445.6 wing is a swept-back wing with a quarter-chord sweep angle of 45 degrees. Cross sections of the wing are NACA 65A004 airfoils. The wing has a taper ratio of 0.66 and an aspect ratio of 1.65. Moreover, it is a wall-mounted model made with laminated mahogany. The wing's parametric CAD model prepared with CATIA V5 is given in Figure 5.1.



**Figure 5.1 :** AGARD 445.6 wing geometry

There are 2 models of the AGARD 445.6 wing: solid and weakened model. In this study weakened model of the wing given in Figure 5.2 below is used.



**Figure 5.2 : AGARD 445.6 weakened model**

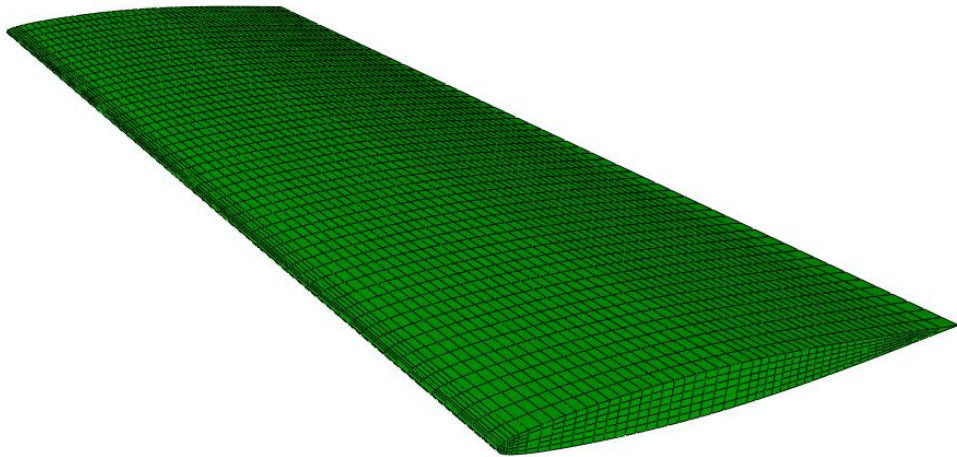
### **5.2 CSD model of the AGARD 445.6 weakened model and validation**

The finite element model of the wing is formed in ABAQUS by using 19,610 linear hexahedral structural elements. Static aeroelastic analysis and modal analysis are performed. The wing is fixed from root for every degree of freedom (DOF). The material properties of the wing are taken from the work of Yosibash et al [38] for the solid model and applied for the weakened model by using interpolation. The material properties of the wing are given in table below. The fiber orientation of the wood is taken along span inclined 45 degrees.

**Table 5.1:** AGARD 445.6 Material properties

	Weakened Model 3
$E_{11}$ (MPa)	3671
$E_{22}$ (MPa)	240
$E_{33}$ (MPa)	401
$G_{12}$ (MPa)	321
$G_{13}$ (MPa)	409
$G_{23}$ (MPa)	136
$\nu_{12}$	0.034
$\nu_{13}$	0.033
$\nu_{23}$	0.326

The finite element model of the wing is given in the following Figure 5.3.



**Figure 5.3 :** The finite element model of the AGARD 445.6 wing

The AGARD 445.6 weakened model is modeled for the first four frequencies. In order to validate the wing model, a modal analysis is performed to compare the results of Yates et al [28]. The results of the modal analysis are tabularized in the Table 5.2.

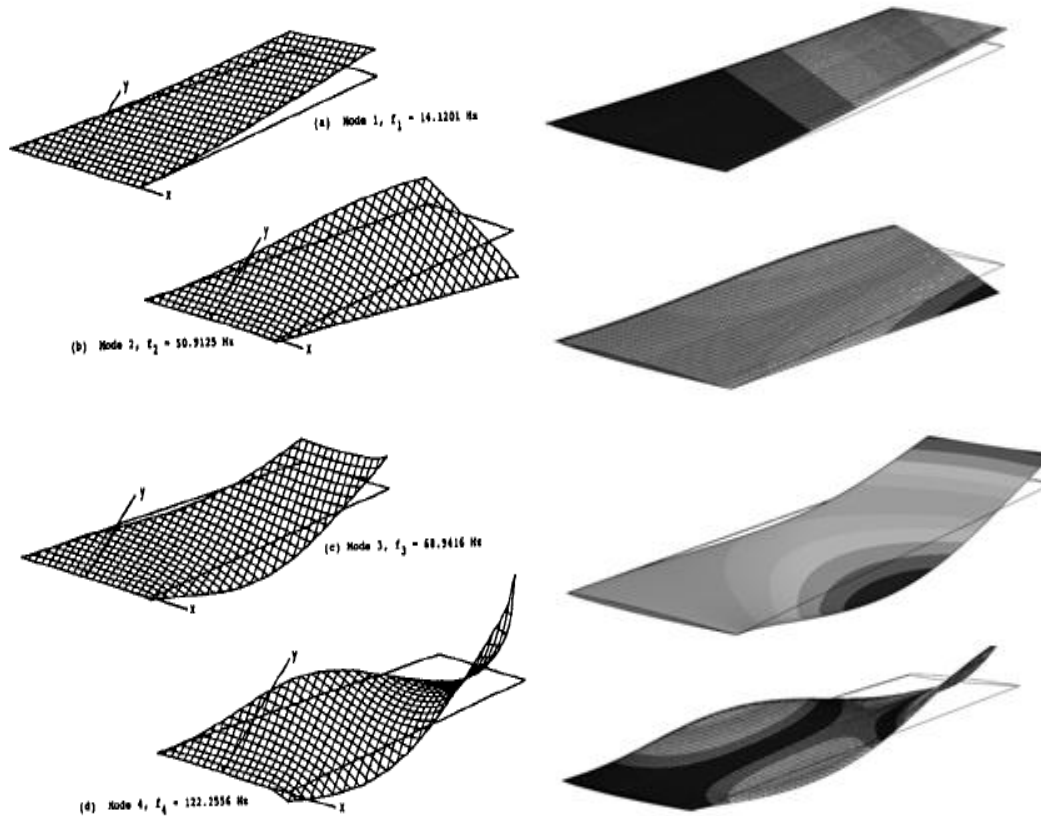


**Table 5.2:** Frequency comparison for weakened model

Frequency no.	Reference approach [Hz]	Present study [Hz]	Error (%)
f1	9.59	9.58	0.16
f2	38.16	36.88	3.34
f3	48.34	47.72	1.28
f4	91.54	91.11	0.47
f5	118.11	119.87	1.48

As seen from Table 5.2 the results are well agreed with the results of Yates [28]. The error for the first five frequencies of the modelled AGARD 445.6 wing is below 5%. Moreover, except for the 2<sup>nd</sup> frequency the errors are below 1.5%.

In the Figure 5.4 the modes shapes on the left belongs to the reference study of the Yates [28] and the mode shapes on the right belongs to current study.



**Figure 5.4 :** Mode shapes comparison

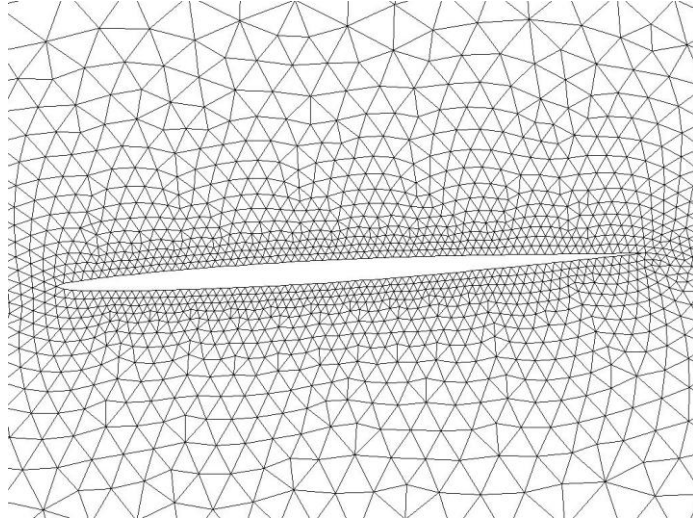
As seen from the results the mode shapes belong to the 1<sup>st</sup> bending, 1<sup>st</sup> torsion, 2<sup>nd</sup> bending and 2<sup>nd</sup> torsion from top to down respectively.

In conclusion, the results of the modal analysis show us that our model is free of numerical and modeling errors and can be used for the rest of the study.

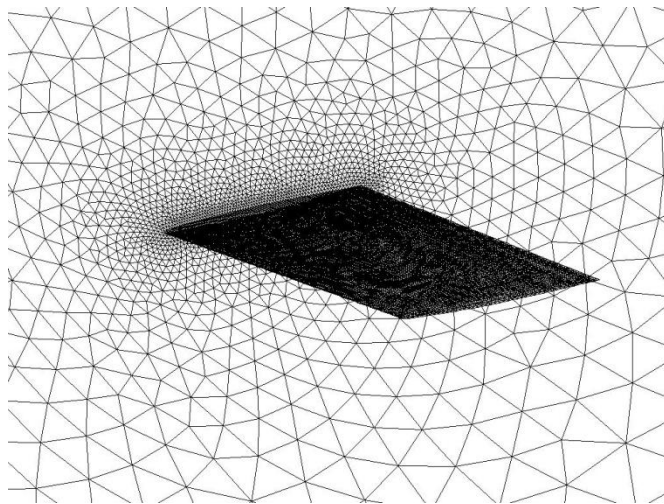
### **5.3 CFD model of the AGARD 445.6 weakened model**

The computational grid of the wing was constructed in GAMBIT preprocessing software by using tetrahedral elements. The computational grid has 691,000 cells, 1.35 million faces.

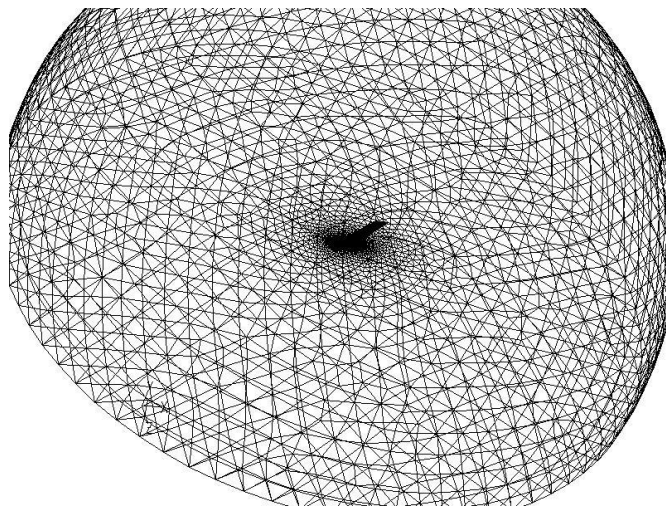
The flow is modeled as inviscid by using Euler equations and the free stream velocity is 0.85 Mach. A 5° of angle of attack is given for the wing geometry. The boundary conditions of the wing surfaces are given as wall and the flow field is given as pressure far field in FLUENT. In the pressure far field the angle of attack is given as cosine and sine of the angle of attack. The computational grid used in the static aeroelastic analysis is given in the following figures.



**Figure 5.5 :** Close up mesh cross section



**Figure 5.6 :** Wing model and wing root

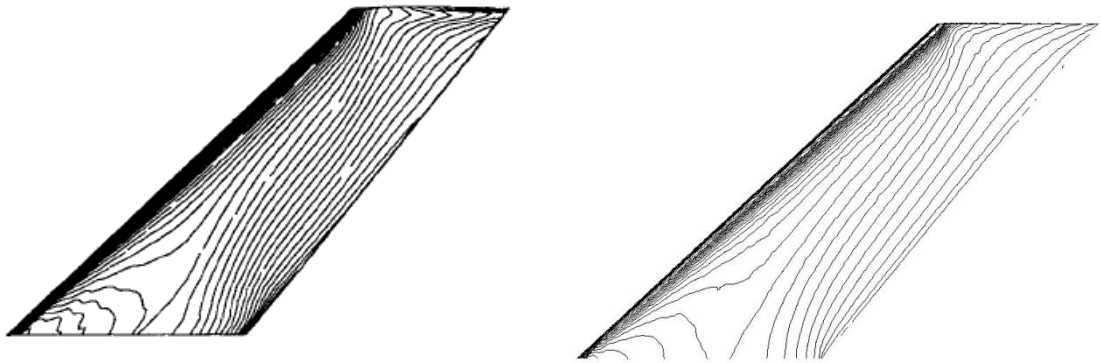


**Figure 5.7 :** Pressure far field computational grid

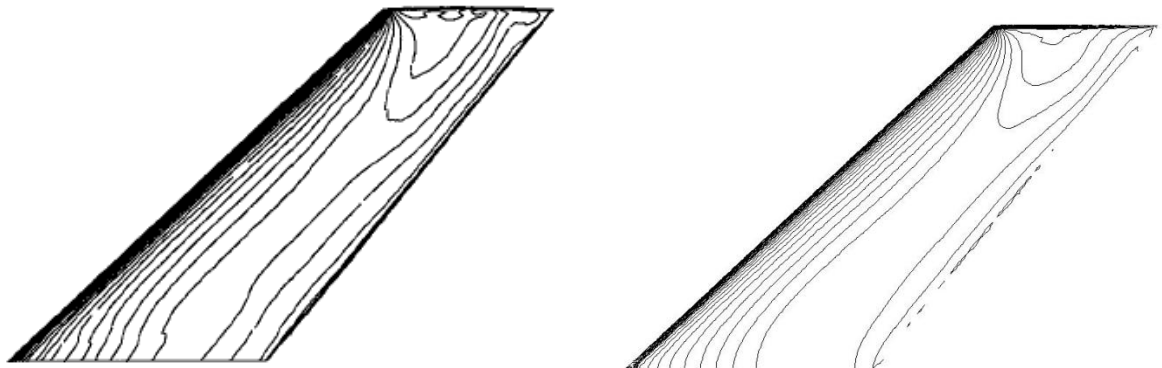
#### 5.4 Aeroelastic analysis results

First of all, to validate the aeroelastic wing model, an aeroelastic analysis was performed via MpCCI. The CFD and CSD model of the wing is given to the MpCCI and transfer quantities (surface pressures from the CFD and nodal displacements from the CSD) were selected. The solution algorithm used in this static aerolastic coupling is the staggered algorithm that is described deeply in the section 4.5.

The results are compared with the results of Liu et al [24]. The pressure contours on the upper and lower surface of the wing are given in the following figures respectively. On the left side of the figures 5.8 to figure 5.11 the results are from the Liu et al 's work for the AGARD 445.6 wing [24] and on the right side of the figures the results are from the present study.

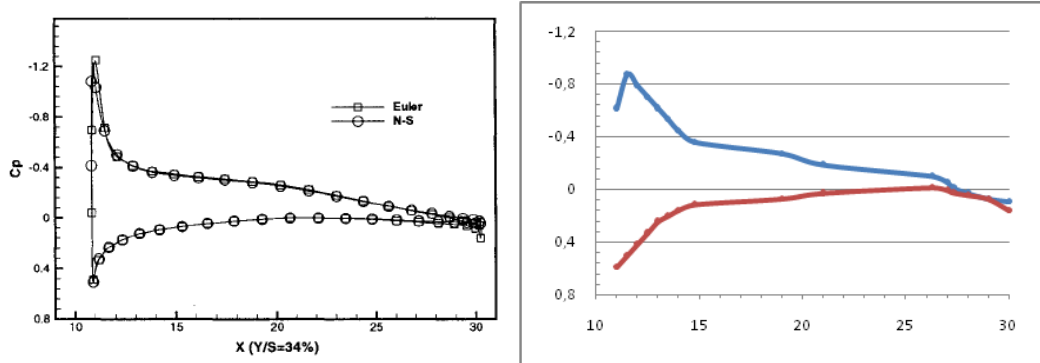


**Figure 5.8 :** Pressure distributions on the upper wing surface

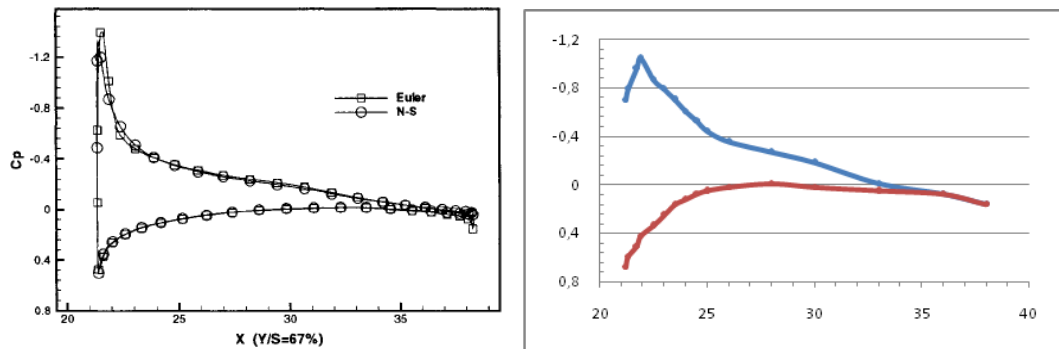


**Figure 5.9 :** Pressure distributions on the lower wing surface

As seen from the figures the pressure contours are well fit with the reference results. Moreover, the distribution of the pressure coefficients at 34% and 67% span are given in the following figures respectively.



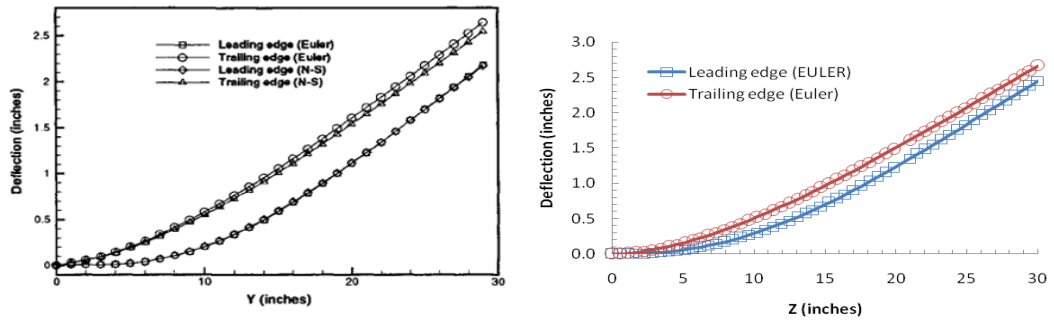
**Figure 5.10 :** Pressure coefficient distribution at 34% span (X in inches)



**Figure 5.11 :** Pressure coefficient distribution at 67% span (X in inches)

As seen from the figures 5.10 and 5.11 the suction picks differ with the results of Liu et al [24]. For the  $\eta = 0.34$ , where  $\eta$  is the nondimensional spanwise coordinate, Liu et al [24] predicted a suction peak of -1.26 at 1% chord location of the upper wing surface whereas in the present study a suction peak of -0.92 at 3.5% chord location was predicted. Moreover for  $\eta = 0.67$  a suction peak of -1.41 at 1% (nasil goruluyor) chord location was predicted on the upper wing surface by Liu et al [24] whereas in the present study a suction peak of -1.05 at 4.5% (nasil goruluyor) chord location was predicted. The results are well agreed with the results of the reference except for the leading edge suction sections for the upper wing surface. This difference can be the result of the mesh type used in the studies or due to the solver used in the studies.

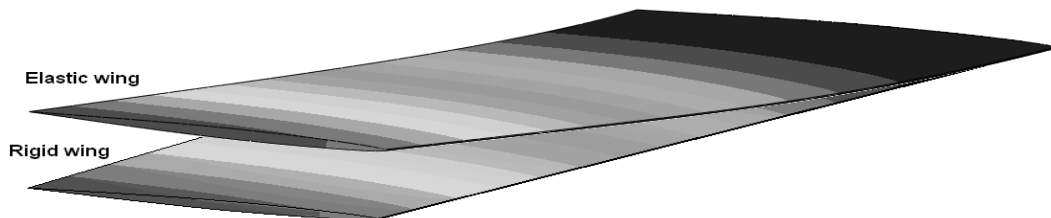
The last compared result is vertical deflection of the wing along span relative to the wing root. The deflection results are given in the following Figure 5.12 and 5.13.



**Figure 5.12 :** Vertical deflection of the wing along span relative to the wing root

As seen from the figures 5.12 and 5.13 the out of plane deformation behaviour for the wing is well agreed the with the results of the Liu et al [24]. There are slight differences for the leading edge section. This can be due to the different methods used in two different studies. In the present study a 3D finite element analysis software is used to find the displacement values whereas in the work of Liu et al [24] used a modal structural method in order to predict the displacement values.

Below in the figure 5.13 the wing’s initial and equilibrium positions are given. As expected due to the aerodynamic loads the wing’s vertical deflection along span relative to the wing root is upwards.



**Figure 5.13 :** Wing’s initial and equilibrium positions

## **6. MULTIDISCIPLINARY MULTI-OBJECTIVE DESIGN OPTIMIZATION**

In recent years, design optimization of complex aircraft structures for maximum performance and minimum weight has been a challenging research area for aircraft manufacturer companies. The multi-objective task of attaining minimum weight and cost with maximum reliability of structure is one of the most time-consuming phases of an aircraft design project. Therefore, robust computational methodologies are strongly required in order to increase the efficiency and success of this design phase. A strong and easy-to-apply methodology can be developed by implementing the numerical optimization techniques directly into the everyday-used analysis tools that have been well and commonly employed in aerospace engineering. Numerical optimization is an iterative scheme to reach the most desired design within a design space bounded by the lower and upper limits of optimization variables. The design criteria defined as functions of optimization variables have to be evaluated at each optimization iteration as variables are updated. Thus, optimization studies require a high number of sequential analyses automatically and needs longer computational time as compared to only analysis studies. For that reason, a serious research is focusing on developing more efficient optimization algorithms for problems with large analysis size. For only optimization purposes simpler analysis models can be preferred in the iterative process and parametric geometries can be used to reduce the number of optimization variables that can sufficiently describe a problem.

In this study multi-objective and multidisciplinary optimization will be performed for a wing configuration. As the optimization driver the multiobjective design environment (mode) FRONTIER software will be used for its efficient optimization algorithms.

### **6.1 Formulation of optimization problems**

A generic optimization problem associated with a given system can be formulated as;

$$\begin{aligned}
& \min_{s \in S} z(s) \\
& h(s) = 0 \quad h(s) \in R^{n_h} \\
& g(s) \leq 0 \quad g(s) \in R^{n_g} \\
& S = \{s \in R^{n_s} \mid s_L \leq s \leq s_U\}
\end{aligned} \tag{6.1}$$

Where;

$s$  is a set of  $n_s$  abstract parameters restricted by lower and upper bounds  $s_L$  and  $s_U$ ,  
 $z$  is a cost function of interest,

$h$  is a set of  $n_h$  equality constraints

$g$  is a set of  $n_g$  inequality constraints.

## 6.2 Design variables

The set of optimization variables ( $s$ ) are the values that affect the optimization problem. These can be geometry parameters like taper, sweep, aspect ratio or thickness values like shell thicknesses of the wing. They can be either bounded with lower and upper bounds or unbounded. Moreover, design variables can be continuous like wing span, chord or can be discrete like number of ribs, spars.

The main geometry for the optimization problem in this thesis, is based on the AGARD 445.6 wing described in the previous chapters. As the design variables, taper ratio and the quarter chord sweep are selected. When these variables are changed, the fiber orientation on the structural model, the average chord and the planform area values will also change respectively. But these variables will not be used as direct optimization (design) variables; they will be calculated according to the values of sweep and taper and will be used as input variables.

**Table 6.1:** Optimization variables

Design Variables	Lower Bound	Upper Bound
taper ratio	0.1	0.5
sweep (degrees)	0	50



### 6.3 Constraints

A constraint is a condition that must be satisfied during the design. If the constraint is satisfied the design is called feasible if not infeasible. For example, designer may want the lift to be greater than or equal to the aircraft's weight or does not want the maximum stress to exceed the value of the material's yield stress value.

In this study only one constraint is given. It is the maximum deformation of the wing tip due to the aerodynamic loads over the wing. The deformation at the tip should not exceed the one tenth of the wing span.

**Table 6.2:** Constraints

Constraints	Less Than
Maximum tip deflection (mm)	76

### 6.4 Objective functions

An objective function is the goal of the optimization problem that we want to minimize or maximize. For example, minimizing weight, displacement, stress or maximizing L/D, lift coefficient,...

Most of the optimization problems are single objective or can be formulated as single objective through summation of the multi-objective functions by using weight factors. In this study there are two objective functions and for the multiobjective optimization problems the algorithm will try to find the pareto front.

The objective functions for this study are maximizing the L/D ratio and minimizing the weight.

**Table 6.3:** Objective functions

Objective Functions	Goal
L/D	max
weight	min

## 6.5 Optimization problem

The overall optimization problem for this thesis work can be formulated as

$$\begin{aligned} & \text{minimize} && M(s) \\ & && s \in S \\ & \text{maximize} && L / D(s) \\ & && s \in S \\ & \text{subject to} && \\ & && u_{\max} \leq 76mm \\ & \text{with respect to} && \\ & && 0 \leq \Lambda_{c/4} \leq 50 \\ & && 0.1 \leq \lambda \leq 0.5 \end{aligned} \tag{6.2}$$

where;

$M$  is the total mass of the wing

$L / D$  is the lift over drag value for the wing

$u_{\max}$  is the maximum deformation of the wing tip

$\Lambda_{c/4}$  is the sweep value at the quarter chord

$\lambda$  is the taper ratio defined as;

$$\lambda = \frac{c_{tip}}{c_{root}} \tag{6.3}$$

## 6.6 Optimization algorithms

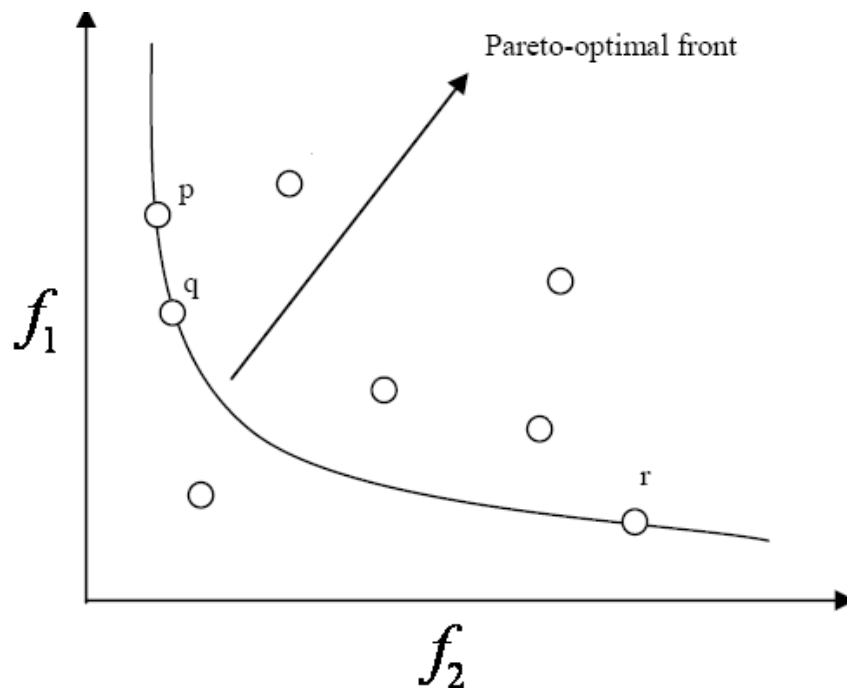
Optimization problems can be generally solved by either gradient based algorithms or evolutionary algorithms. In this study multi objective optimization problem will be solved by genetic algorithm which is an evolutionary algorithm.

Evolutionary algorithms or genetic algorithms use the evolution theory to perform optimization. A population evolves over generations to adapt to an environment by selection, mutation and crossover. [81]

There are three important terms corresponding to the genetic algorithms which are fitness, individual and genes. Fitness refers to the objective function, individual refers to the design candidate and genes refer to the design variables.

Multiobjective (MO) optimization tries to find the components of a vector-valued objective function whereas the single objective optimization tries to find the single valued objective function. [53] In MO problems, solution is a set of solutions called “pareto-optimal set”.

In the following figure it is seen that point “p” has a minimal  $f_2$  but maximum  $f_1$ . On the other hand, point “r” has a minimal in  $f_1$  but maximum  $f_2$ . These two points are not the solution when both of the objectives are considered. The solutions on the curve between “p” and “r” are known as pareto-optimal front. Every pareto optimal point in the set is an equally acceptable solution for a MO optimization problem. [86]



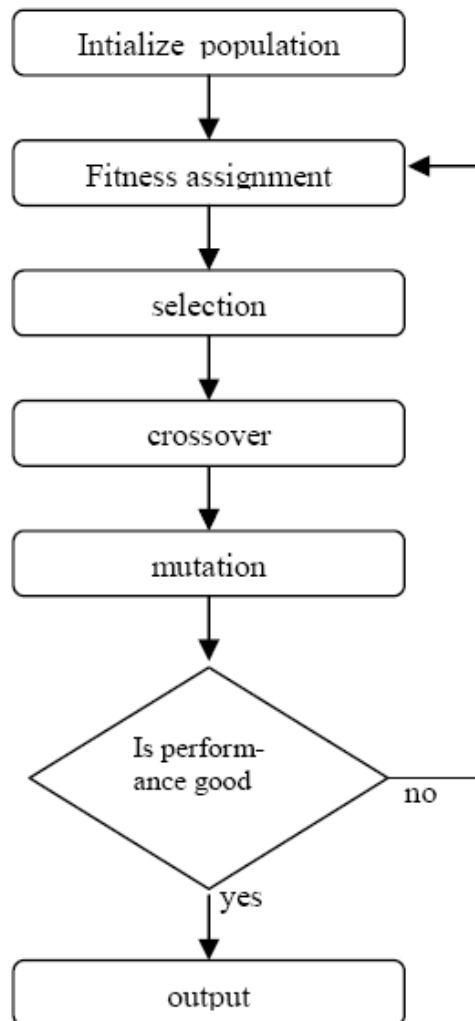
**Figure 6.1** : Pareto optimal solutions

The application of the evolutionary algorithms to a MO optimization problem can be solved by using a multiobjective genetic algorithm (MOGA). Genetic algorithms are capable of finding the global optima within complex design spaces whereas gradient based algorithms can sometimes get stuck at the local optima points.

Genetic algorithms can be used almost for every optimization problem, where gradient based algorithms may have some limitations. Gradient based algorithms needs the gradient information to compute the search direction to move in the design space that’s why they need the existence of derivatives. However, if once applicable,

gradient based algorithms may be much more computationally efficient with respect to the genetic algorithms.

Genetic algorithms do not need to start from a point whereas gradient based algorithms need a starting point. Genetic algorithms do not operate on design variables directly. They use binary representation of the parameters. A basic structure of a genetic algorithm according to the Ghosh and Dehuri [81] is given in the following figure.



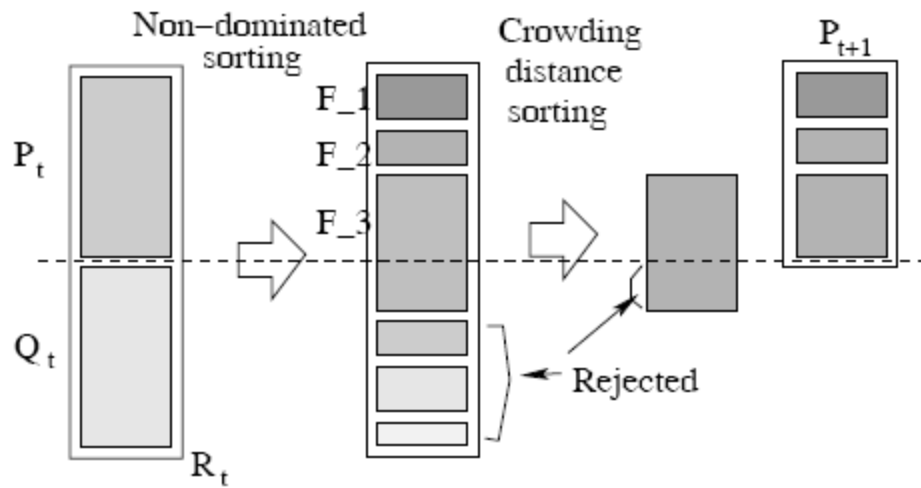
**Figure 6.2 :** Basic structure of genetic algorithm

### **6.6.1 Non-dominated sorting genetic algorithm (NSGA-II)**

The scheduler used in this study is the implementation of Deb et al [82] which is “Non-dominated Sorting Genetic Algorithm”. NSGA-II is a fast and elitist multiobjective evolutionary algorithm [86]. The main features of the algorithm are [86];

- It implements a fast non-dominated sorting procedure and it reduces the computational time according to the classical non-dominated sorting algorithms.
- Elitism is implemented in the NSGA-II for multiobjective search. From the start of the initial population elitism is used to form all of the populations.
- Crowding distance, which finds the density of solutions in the objective space, is used. Moreover, it uses a crowded comparison operator for the selection process.

The work diagram of NSGA-II is given in the following figure [82].



**Figure 6.3 :** Work diagram of NSGA-II

- First a combined population  $R_t$  is formed by combining the child population  $Q_t$  and parent population  $P_t$ . The population  $R_t$  is in size of  $2N$ .
- $$R_t = P_t \cup Q_t \quad (6.4)$$
- Then  $R_t$  population is sorted due to the non-domination. Elitism is satisfied as the previous and current population is included in  $R_t$ .
  - New population  $P_{t+1}$  is formed by using the solutions of different non-dominated fronts  $F_1, F_2, F_3, \dots$  according to their rank and crowded comparison operator. Best non-dominated front is first, then the second best non-dominated front and so on.

- The new population  $P_{t+1}$  of size N is used to form the new population of  $Q_{t+1}$  by using selection, crossover and mutation.

### 6.7 modeFRONTIER optimization workflow

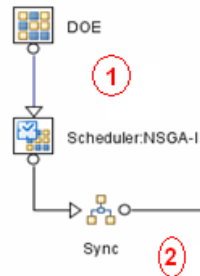
For the aeroelastic optimization problem several commercial softwares were used during the optimization process in this thesis. The employed software and why they are used are tabularized in the Table 6.4 below.

**Table 6.4:** Software employed in the aeroelastic optimization process

Software	Why it is used?
CATIA V5	Parametric CAD model of the wing
GAMBIT v2.3.16	Preprocessor for the CFD analysis, mesh generation
FLUENT v6.3.26	3D CFD flow solver to solve inviscid flow and CFD post-processing tool
ABAQUS v6.7-1	3D FEA structural solver to perform static analysis and CSD post-processing tool
MpCCI v3.0.6	Mesh based aeroelastic coupling interface to transfer loads between CFD- CSD and control the aeroelastic coupling
modeFRONTIER v4.0	Multi objective optimization software to perform aeroelastic optimization with genetic algorithm NSGA-II

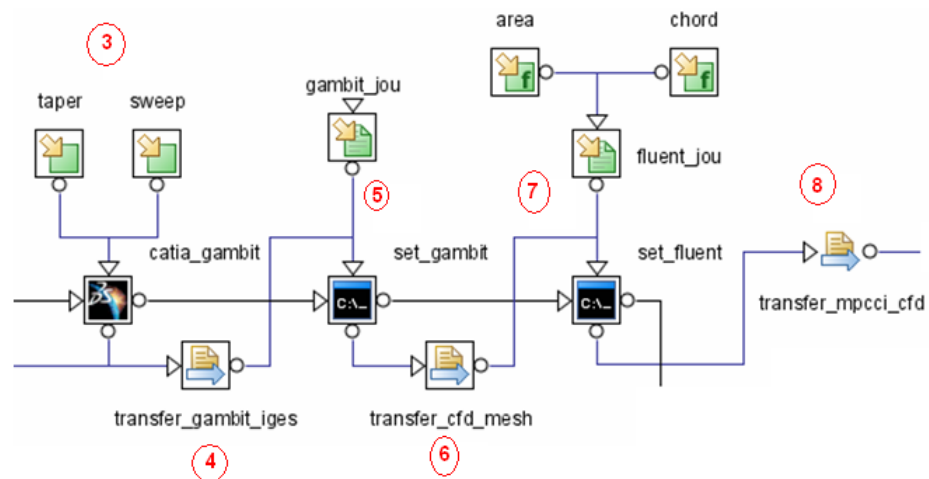
In order to perform an optimization study a workflow should be prepared in modeFRONTIER to control the optimization process. In this workflow the optimization variables (their limits and increments), scheduler, design of experiments, objectives, constraints, output variables and the softwares are defined.

Optimization workflow is prepared to automate the multiobjective multidisciplinary optimization problem. Once the workflow is run, it controls the optimization process automatically by using the well prepared script files and models. The working procedure of the diagram can be explained by splitting into parts as follows;



**Figure 6.4 : Scheduler**

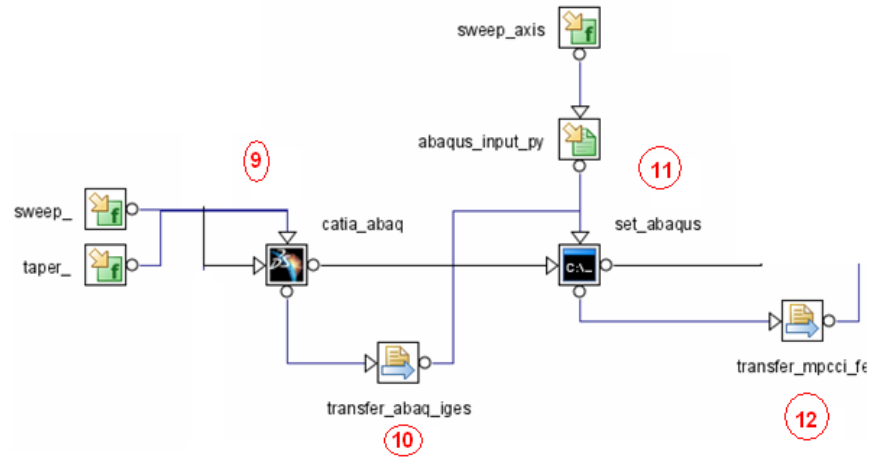
- 1) The scheduler NSGA-II determines the design variables and optimization iteration begins.
- 2) Synchronization starts



**Figure 6.5 : CFD branch**

- 3) Optimization variables are changed via CATIA V5 node by using the parametric CAD model.
- 4) The geometric model transferred as iges format to GAMBIT CFD pre-processor
- 5) GAMBIT uses the journal file given in the Appendix A.1 and prepares solution grid for CFD and gives the boundary conditions.
- 6) GAMBIT transfers the mesh file to FLUENT

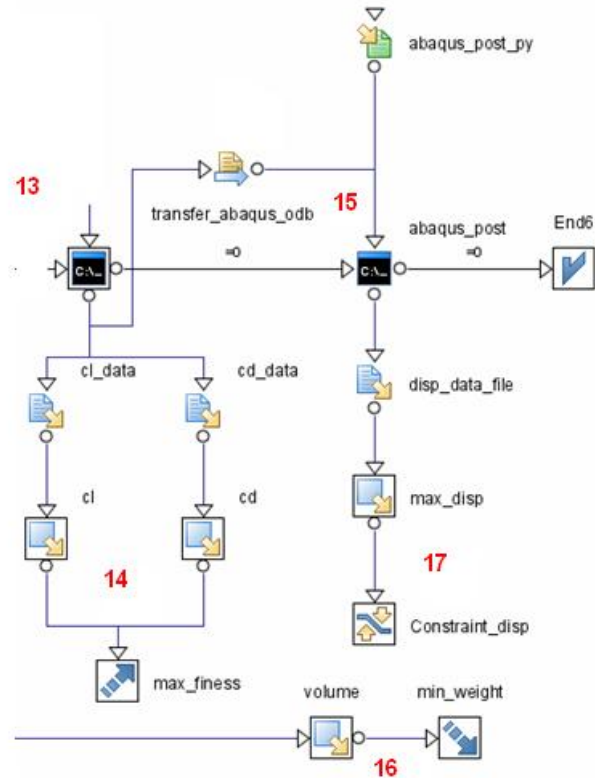
- 7) As the area and the average chord of the wing changes in every design iteration, FLUENT calculates them by using the design variables and imports the mesh files. Then it prepares the flow model and gives boundary conditions via journal file given in Appendix A.2.
- 8) FLUENT transfers the case file to MpCCI for the aeroelastic analysis.



**Figure 6.6 : CSD branch**

- 9) Optimization variables are changed via CATIA V5 node by using the parametric CAD model.
- 10) The geometric model transferred as iges format to ABAQUS FEA
- 11) ABAQUS changes the fiber orientation of the wing by using the sweep value and prepares the structural model for the aeroelastic analysis by using the Python script given in Appendix A.3.
- 12) ABAQUS transfers the input file to MpCCI for the aeroelastic analysis.





**Figure 6.7 :** Aeroelastic analysis, post processing and optimization

- 13) Aeroelastic coupling is performed via MpCCI by using the FLUENT and ABAQUS models in batch mode.
- 14) The results for the objective function (maximize L/D) is stored.
- 15) Aeroelastic analysis result file for the ABAQUS is transferred to ABAQUS for post-processing and getting the displacement constraint result.
- 16) The value of the wing weight is calculated via the multiplication of the volume information from the CATIA V5 and the material density.
- 17) modeFRONTIER controls the constraint violation.
- 18) NSGA-II controls the optimization process.
- 19) New iteration process starts.

This cycle goes on until the specified number of iterations or populations have reached. After all the calculations have been performed the pareto optimal set is found and by using the decision tools of modeFRONTIER a suitable design is found. The optimization workflow is given in the following figure for the whole optimization process.

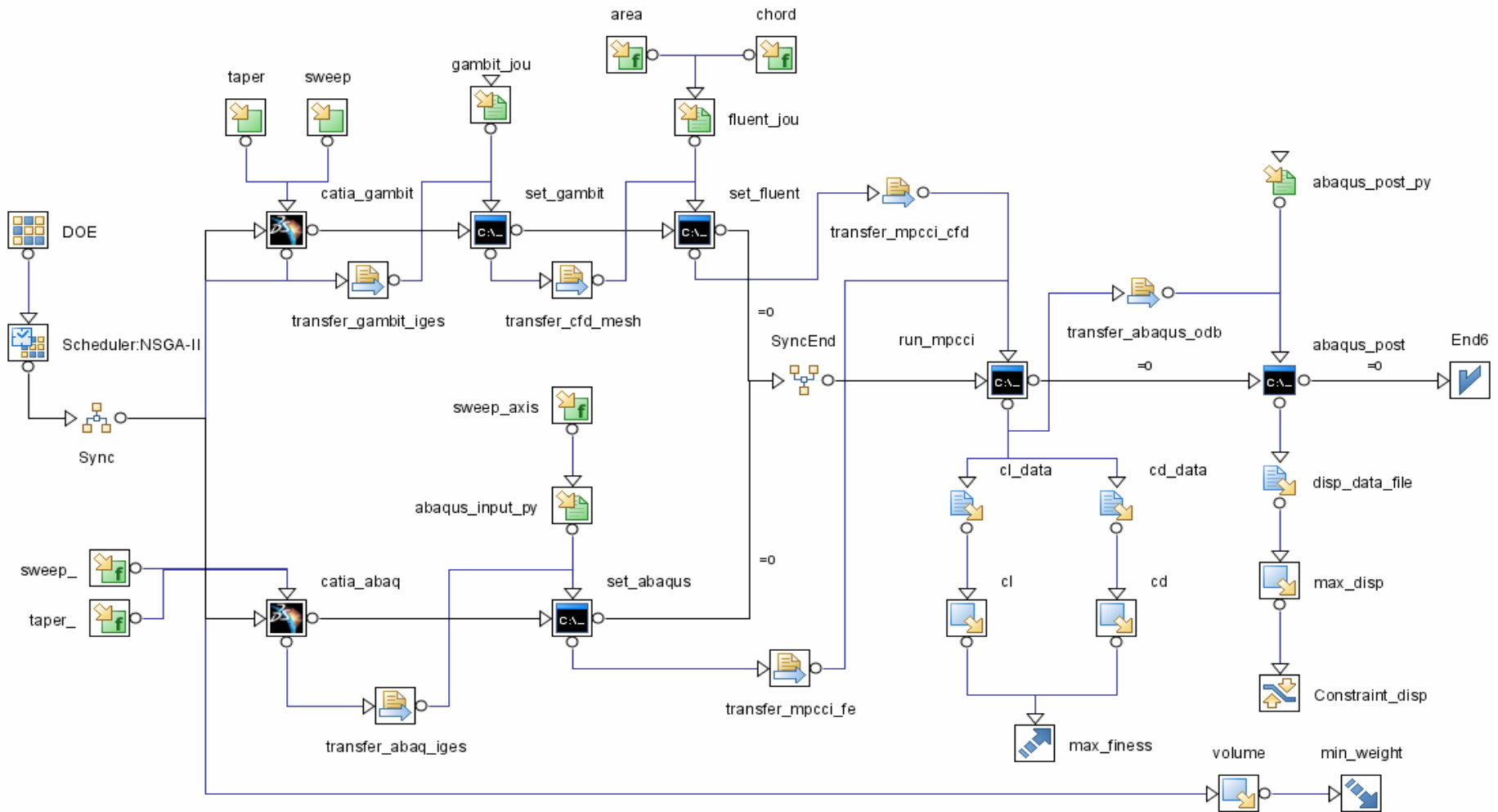


Figure 6.8 : Optimization workflow

## 7. OPTIMIZATION RESULTS

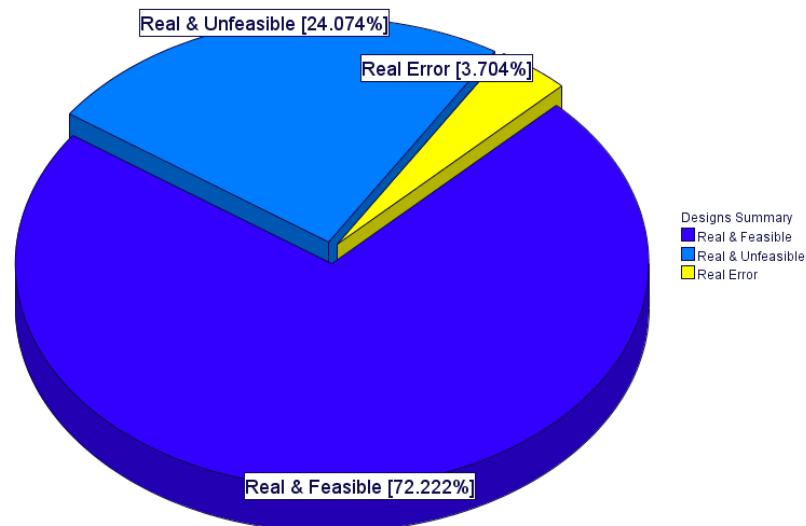
### 7.1 Results for the optimization problem

In this study a number of 12 design of experiments (DOE) with Sobol sequence which is capable of distributing the experiments uniformly in the design space [86] and 17 number of generations for the NSGA-II are defined. A total number of 204 designs is generated for the optimization problem.

$$\text{Total design number} = \text{DOE} * \text{Generations} \quad (7.5)$$

Solution of the problem took 23 hours 51 minutes on a workstation with Microsoft Windows XP operating system. The system has 2 Gb of RAM and 250 Gb of harddisk.

There are 108 different individual designs distributed as shown in the following figure.



**Figure 7.1 :** Design summary

78 designs (72% of all designs) were found to be feasible that satisfies the constraint condition given in the optimization problem and 26 designs (24% of all designs) are

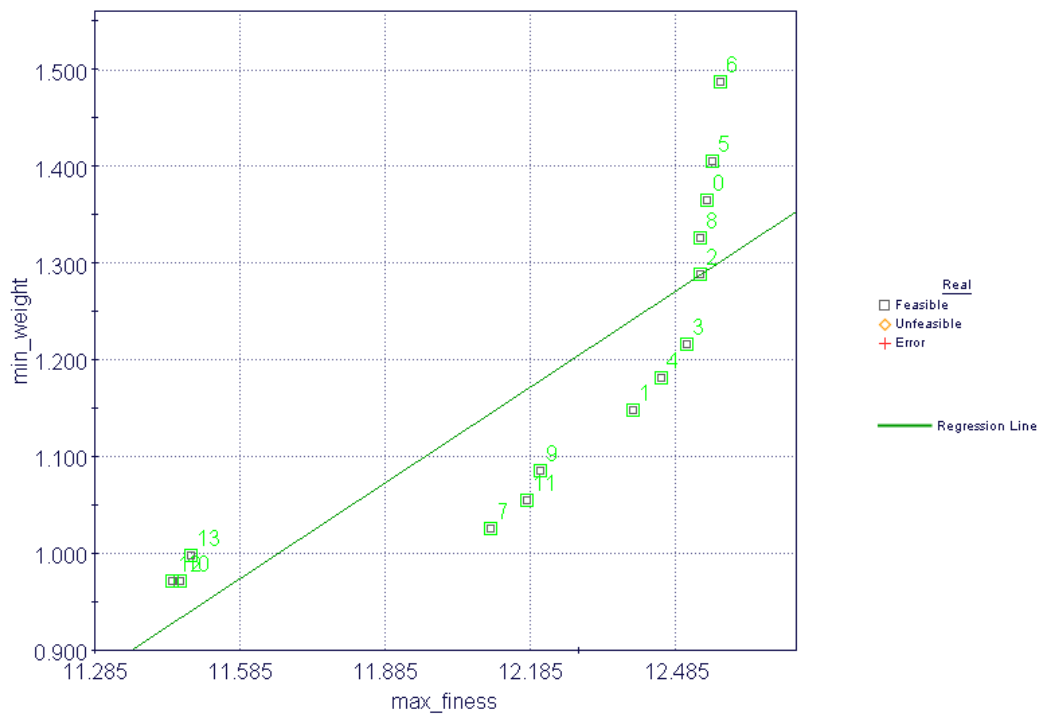
unfeasible that did not satisfy the constraint condition. Moreover, there are 4 error designs (4% of all designs) that did not give any solution because of modeling or computational errors in the optimization workflow.

As described before, for the multiobjective optimization problems there is no single solution because of the nature of the problem. There is a set of solutions called pareto front set. There are 14 designs in the pareto front set for this optimization problem. These pareto designs are tabularized in the following table. Designs for the whole study is given in the Appendix C.

**Table 7.1:** Pareto designs

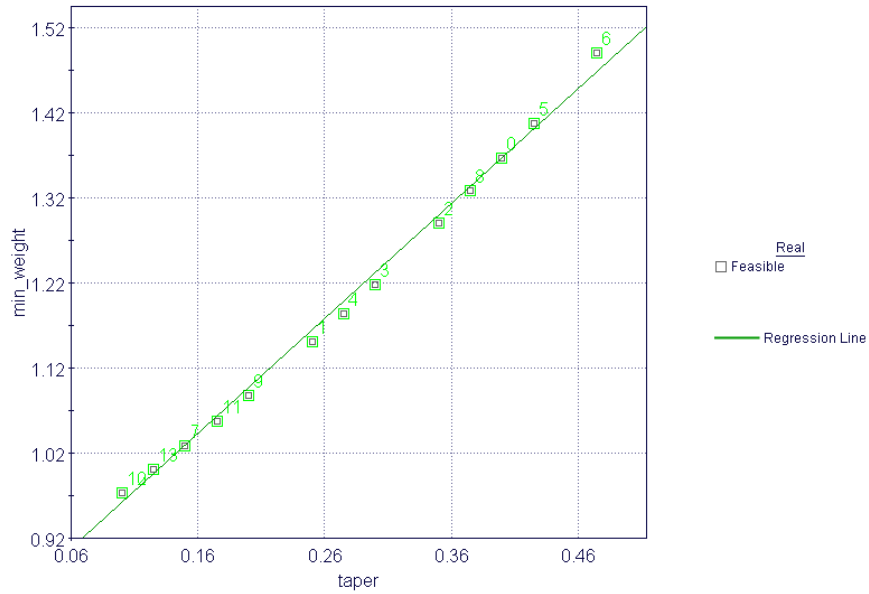
<b>Pareto</b>	<b>Sweep (degree)</b>	<b>Taper</b>	<b>Cd</b>	<b>Cl</b>	<b>max_finess</b>	<b>min_weight (kg)</b>	<b>displacement (mm)</b>
0	38	0.4	0.0303	0.3799	12.5465	1.3654	65.1492
1	36	0.250	0.0328	0.4062	12.3959	1.1488	72.5629
2	38	0.350	0.0308	0.3856	12.5339	1.2888	68.5509
3	38	0.300	0.0313	0.3917	12.5063	1.2166	72.1564
4	38	0.275	0.0317	0.3946	12.4528	1.1821	74.4686
5	38	0.425	0.0300	0.3767	12.5583	1.4053	63.4759
6	38	0.475	0.0295	0.3706	12.5754	1.4885	60.6254
7	30	0.150	0.0363	0.4395	12.1014	1.0262	73.2844
8	38	0.375	0.0305	0.3827	12.5341	1.3266	66.7753
9	32	0.200	0.0350	0.4274	12.2043	1.0853	70.6557
10	6	0.100	0.0405	0.4640	11.4589	0.9715	57.9876
11	32	0.175	0.0353	0.4301	12.1746	1.0552	73.3374
12	2	0.100	0.0401	0.4585	11.4429	0.9715	56.5783
13	6	0.125	0.0403	0.4622	11.4817	0.9983	55.6719

The remaining task for the optimization problem is to choose a suitable design from the pareto set. All of the designs given in the Table 7.1 are the acceptable optimum solutions of the problem but with different weights for the corresponding objectives. For example an aerodynamics engineer can prefer the design with maximum lift over drag ratio whereas a structural engineer can choose the design with minimum weight. The relation between the objectives are given in the scatter chart of the modeFRONTIER in the following Figure 7.2

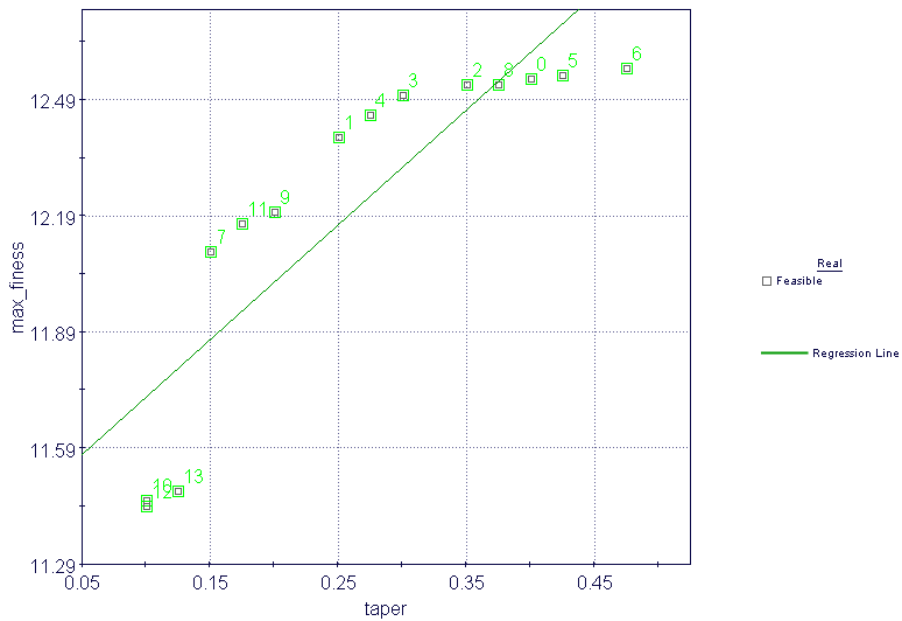


**Figure 7.2 :** Scatter chart minimum weight vs maximum L/D

As seen from the Figure 7.2 the relationship between the objectives of maximum lift over drag ratio and minimum weight is non-linear. A quadratic function can describe this relationship. To investigate the relationship between the taper ratio and objective functions is given in the following Figures 7.3 and 7.4.

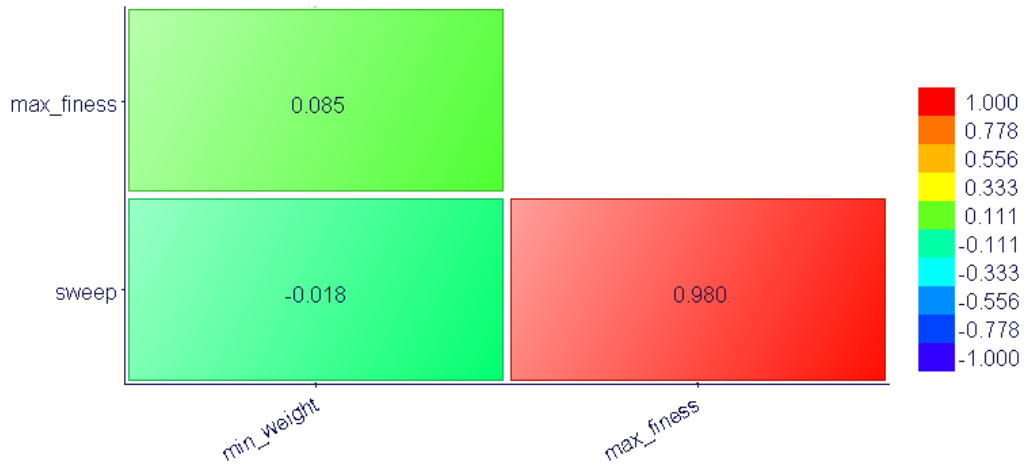


**Figure 7.3 :** Scatter chart for taper ratio vs minimum weight



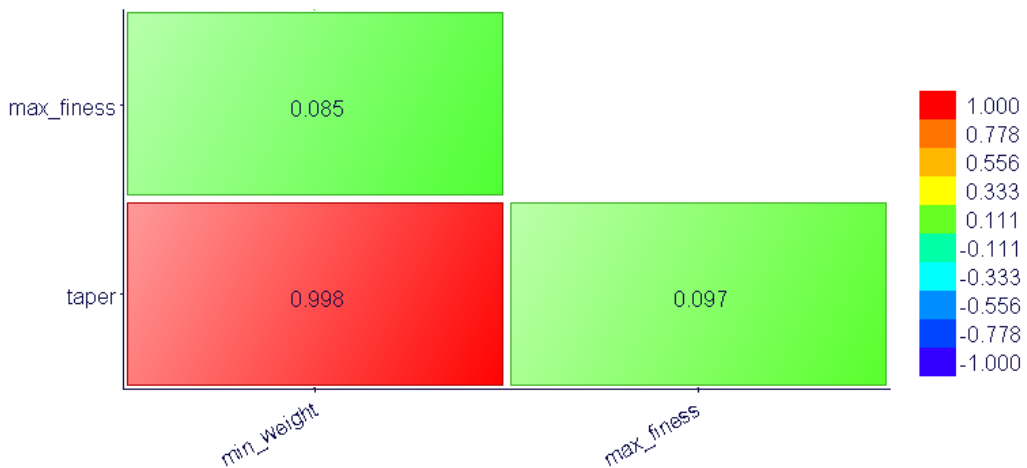
**Figure 7.4 :** Scatter chart for taper ratio vs maximum L/D

As seen from the Figure 7.3 there is a linear relationship between the taper ratio and the objective function of minimum weight whereas as seen from the Figure 7.4 there exists a non-linear relationship between the taper ratio and the objective function of maximum lift over drag ratio. The correlation between the optimization variables and the objective functions are given in the following Figures 7.5 and 7.6. In the correlation charts the value changes between -1 and 1. If the value is 1 it means the variables are perfectly positively correlated else if the value is -1 it means the variables are perfectly negatively correlated.



**Figure 7.5 :** Correlation matrix (sweep-max L/D-min weight)

In Figure 7.5 it is clearly seen that sweep and the maximum lift over drag ratio are almost positively correlated with a value of 0.980. Moreover, sweep and the objective function of minimum weight is negatively correlated with a value of -0.018.



**Figure 7.6 :** Correlation matrix (taper-max L/D-min weight)

As seen from Figure 7.6 the correlation between the taper ratio and the objective of minimum weight is almost perfectly positive with a value of 0.998. There is a positive correlation with value of 0.097 exists between the taper ratio and maximum lift over drag ratio.

Three designs are selected from the pareto set for the optimum design for this study. Design number six is the best solution for maximum L/D value, design number ten is the best solution for minimum weight and design number nine is in between. The results are tabularized below.

**Table 7.2:** Results for the selected pareto designs

Pareto	Sweep (degree)	Taper	Cd	Cl	max_finess	min_weight (kg)	displacement (mm)
6	38	0.475	0.0295	0.3706	12.5754	1.4885	60.6254
9	32	0.200	0.0350	0.4274	12.2043	1.0853	70.6557
10	6	0.100	0.0405	0.4640	11.4589	0.9715	57.9876

The structural results (initial and equilibrium positions of the wing, displacement residual) and the fluid dynamics results (pressure coefficients on the upper and lower wing) for the design number 9 from the pareto set is given in the Appendix B.

## 7.2 Conclusion

In this thesis aeroelastic optimization is performed on a basic experimental wing model based on AGARD 445.6 elastic wing configuration to obtain the objectives of maximum lift over drag ratio and minimum weight of the wing. A static aeroelastic criteria is given as a design constraint to satisfy the maximum tip deflection. Sweep angle at the quarter chord and the taper ratio of the wing are used as optimization parameters for this study. Moreover, a genetic algorithm NSGA-II is used to control the optimization process.

The pareto set for the optimum designs are obtained at the end of the aeroelastic optimization study to choose the best design configuration. The effect of the design variables on objective functions and their relationship are examined by using the modeFRONTIER 4.0's decision tools.

Thus, a strong and easy to apply multi-disciplinary optimization methodology is successfully developed by implementing the numerical optimization techniques directly into the everyday used commercial analysis tools that have been well and commonly employed in CFD and CSD disciplines in aerospace engineering.

The future work for this study is to apply the parallel computation technology in both CSD and CFD parts in the already developed methodology. More complicated aircraft wing geometries and more detailed optimization problems can be studied



with the advantages of parallelization. Finally, the study will be extended to dynamic aeroelasticity problems with applications to aeroelastic optimization based on flutter analysis.

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## **APPENDICES**

### **APPENDIX A : Scripts for the modeFRONTIER Optimization Workflow**

**APPENDIX A.1 : GAMBIT Script to Prepare the Fluid Mesh**

## APPENDIX A.1

```
/ Journal File for GAMBIT 2.2.30, Database 2.2.14, ntx86 BH04110220
/ File opened for write
undo begingroup
/ Importing IGES file using InterOp translator version 12
import iges \
  ".\agard_gambit.igs" \
  scale 1 native
undo endgroup
edge create "leading_line" straight "vertex.1" "vertex.3"
edge create "trailing_line" straight "vertex.2" "vertex.4"
face create "root_face" wireframe "edge.4" "edge.1" real
face create "tip_face" wireframe "edge.3" "edge.2" real
face create "upper_face" wireframe "leading_line" "edge.4" "trailing_line" \
  "edge.3" real
face create "lower_face" wireframe "leading_line" "edge.1" "trailing_line" \
  "edge.2" real
volume create "wing_volume" stitch "upper_face" "lower_face" "root_face" \
  "tip_face" real
volume create "sphere" radius 8500 sphere
window modify shade
window modify shade
window modify noshade
face create "circular_face" radius 8500 zxplane circle
volume split "sphere" faces "circular_face" connected
volume delete "sphere" lowertopology
volume subtract "volume.3" volumes "wing_volume"
default set "GRAPHICS.GENERAL.CONNECTIVITY_BASED_COLORING" numeric
1
default set "GRAPHICS.GENERAL.CONNECTIVITY_BASED_COLORING" numeric
0
sfunction create sourcefaces "tip_face" "upper_face" "lower_face" startsize \
  6 growthrate 1.3 sizelimit 400 attachvolumes "volume.3" fixed
sfunction bgrid attachvolumes "volume.3"
volume mesh "volume.3" tetrahedral size 1
physics create "upper_wing_surf" btype "WALL" face "upper_face"
physics create "lower_wing_surf" btype "WALL" face "lower_face"
physics create "tip" btype "WALL" face "tip_face"
physics create "simetri" btype "SYMMETRY" face "circular_face"
physics create "far_field" btype "PRESSURE_FAR_FIELD" face "face.5"
export fluent5 "agard.msh"
```

**APPENDIX A.2 : FLUENT Script to Prepare the Flow Model**

## APPENDIX A.2

```
file/read-case agard.msh
grid/scale 0.001 0.001 0.001
grid/reorder/reorder-domain
define/models/viscous/inviscid yes
define/materials/change-create air
air
yes
ideal-gas
define/operating-conditions/operating-pressure 0
define/boundary-conditions/pressure-far-field
0.85
320
0.997
0
0.087
solve/monitors/residual print yes
solve/initialize/compute-defaults pressure-far-field
report/reference-values/compute pressure-far-field
report/reference-values/area 0.353148
report/reference-values/length 0.562
surface/plane-surf-aligned span-0.34
4
0.259
surface/plane-surf-aligned span-0.67
4
0.51
solve/monitors/force/lift-coefficient
yes
upper_wing_surf
lower_wing_surf
yes
yes
no
no
0.087
0
0.996
solve/monitors/force/drag-coefficient
yes
upper_wing_surf
lower_wing_surf
yes
yes
no
no
0.996
0
0.087
file/write-case agard.cas
exit
```

### **APPENDIX A.3 : ABAQUS Script to Prepare the Structural Model**

### APPENDIX A.3

```
#
# Abaqus/CAE Version 6.7-1 replay file
# Run by oncu
#

# from driverUtils import executeOnCaeGraphicsStartup
# executeOnCaeGraphicsStartup()
#: Executing "onCaeGraphicsStartup()" in the site directory ...
from abaqus import *
from abaqusConstants import *
session.Viewport(name='Viewport: 1', origin=(0.0, 0.0), width=181.640625,
    height=212.40234375)
session.viewports['Viewport: 1'].makeCurrent()
session.viewports['Viewport: 1'].maximize()
from caeModules import *
from driverUtils import executeOnCaeStartup
executeOnCaeStartup()
Mdb()
#: A new model database has been created.
#: The model "Model-1" has been created.
session.viewports['Viewport: 1'].setValues(displayedObject=None)
iges = mdb.openIges(
    './agard_abaqus.igs',
    msbo=False, trimCurve=DEFAULT, scaleFromFile=OFF)
mdb.models['Model-1'].PartFromGeometryFile(name='agard_abaqus',
    geometryFile=iges, dimensionality=THREE_D, type=DEFORMABLE_BODY,
    convertToAnalytical=1, stitchEdges=1, convertToPrecise=1)
p = mdb.models['Model-1'].parts['agard_abaqus']
mdb.models['Model-1'].Material(name='Material-1')
mdb.models['Model-1'].materials['Material-1'].Density(table=((4.07282e-10, ),
))
mdb.models['Model-1'].materials['Material-1'].Elastic(
    type=ENGINEERING_CONSTANTS, table=((3671.25, 240.3, 401.63, 0.034,
0.033,
    0.326, 321.35, 409.46, 136.5), ))
mdb.models['Model-1'].HomogeneousSolidSection(name='Section-1',
    material='Material-1', thickness=1.0)
p = mdb.models['Model-1'].parts['agard_abaqus']
c = p.cells
cells = c.getSequenceFromMask(mask=('[#1 ]', ), )
region = regionToolset.Region(cells=cells)
p = mdb.models['Model-1'].parts['agard_abaqus']
p.SectionAssignment(region=region, sectionName='Section-1', offset=0.0)
p = mdb.models['Model-1'].parts['agard_abaqus']
p.DatumAxisByPrincipalAxis(principalAxis=XAXIS)
p = mdb.models['Model-1'].parts['agard_abaqus']
p.DatumAxisByPrincipalAxis(principalAxis=YAXIS)
p = mdb.models['Model-1'].parts['agard_abaqus']
p.DatumAxisByPrincipalAxis(principalAxis=ZAXIS)
p = mdb.models['Model-1'].parts['agard_abaqus']
d = p.datums
p.DatumAxisByRotation(line=d[3], axis=d[5], angle=45.0)
```



```

p = mdb.models['Model-1'].parts['agard_abaqus']
d1 = p.datums
p.DatumCsysByTwoLines(CARTESIAN, line1=d1[6], line2=d1[4], name='Datum
csys-1')
p = mdb.models['Model-1'].parts['agard_abaqus']
c = p.cells
cells = c.getSequenceFromMask(mask=('[#1 ]', ), )
region = regionToolset.Region(cells=cells)
p = mdb.models['Model-1'].parts['agard_abaqus']
datums = p.datums[7]
p.MaterialOrientation(region=region, orientationType=SYSTEM, localCsys=datums)
#: Specified material orientation has been assigned to the selected regions.
a = mdb.models['Model-1'].rootAssembly
a = mdb.models['Model-1'].rootAssembly
a.DatumCsysByDefault(CARTESIAN)
p = mdb.models['Model-1'].parts['agard_abaqus']
a.Instance(name='agard_abaqus-1', part=p, dependent=ON)
p = mdb.models['Model-1'].parts['agard_abaqus']
p = mdb.models['Model-1'].parts['agard_abaqus']
c = p.cells
pickedCells = c.getSequenceFromMask(mask=('[#1 ]', ), )
v, e, d = p.vertices, p.edges, p.datums
p.PartitionCellByPlaneThreePoints(cells=pickedCells, point1=p.InterestingPoint(
    edge=e[2], rule=MIDDLE), point2=p.InterestingPoint(edge=e[3], rule=MIDDLE),
    point3=p.InterestingPoint(edge=e[1], rule=MIDDLE))
p = mdb.models['Model-1'].parts['agard_abaqus']
c = p.cells
pickedCells = c.getSequenceFromMask(mask=('[#1 ]', ), )
v, e, d = p.vertices, p.edges, p.datums
p.PartitionCellByPlaneThreePoints(cells=pickedCells, point1=p.InterestingPoint(
    edge=e[11], rule=MIDDLE), point2=p.InterestingPoint(edge=e[4],
    rule=MIDDLE), point3=p.InterestingPoint(edge=e[12], rule=MIDDLE))
p = mdb.models['Model-1'].parts['agard_abaqus']
c = p.cells
pickedCells = c.getSequenceFromMask(mask=('[#4 ]', ), )
v1, e1, d1 = p.vertices, p.edges, p.datums
p.PartitionCellByPlaneThreePoints(cells=pickedCells, point1=p.InterestingPoint(
    edge=e1[18], rule=MIDDLE), point2=p.InterestingPoint(edge=e1[21],
    rule=MIDDLE), point3=p.InterestingPoint(edge=e1[16], rule=MIDDLE))
p = mdb.models['Model-1'].parts['agard_abaqus']
c = p.cells
pickedCells = c.getSequenceFromMask(mask=('[#8 ]', ), )
v, e, d = p.vertices, p.edges, p.datums
p.PartitionCellByPlaneThreePoints(cells=pickedCells, point1=p.InterestingPoint(
    edge=e[5], rule=MIDDLE), point2=p.InterestingPoint(edge=e[4], rule=MIDDLE),
    point3=p.InterestingPoint(edge=e[27], rule=MIDDLE))
p = mdb.models['Model-1'].parts['agard_abaqus']
c = p.cells
pickedCells = c.getSequenceFromMask(mask=('[#8 ]', ), )
v1, e1, d1 = p.vertices, p.edges, p.datums
p.PartitionCellByPlaneThreePoints(cells=pickedCells, point1=p.InterestingPoint(
    edge=e1[36], rule=MIDDLE), point2=p.InterestingPoint(edge=e1[31],
    rule=MIDDLE), point3=p.InterestingPoint(edge=e1[28], rule=MIDDLE))
p = mdb.models['Model-1'].parts['agard_abaqus']
c = p.cells

```

```

pickedCells = c.getSequenceFromMask(mask=('[#10 ]', ), )
v, e, d = p.vertices, p.edges, p.datums
p.PartitionCellByPlaneThreePoints(cells=pickedCells, point1=p.InterestingPoint(
    edge=e[6], rule=MIDDLE), point2=p.InterestingPoint(edge=e[41],
    rule=MIDDLE), point3=p.InterestingPoint(edge=e[4], rule=MIDDLE))
p = mdb.models['Model-1'].parts['agard_abaqus']
c = p.cells
pickedCells = c.getSequenceFromMask(mask=('[#1 ]', ), )
v1, e1, d1 = p.vertices, p.edges, p.datums
p.PartitionCellByPlaneThreePoints(cells=pickedCells, point1=p.InterestingPoint(
    edge=e1[4], rule=MIDDLE), point2=p.InterestingPoint(edge=e1[5],
    rule=MIDDLE), point3=p.InterestingPoint(edge=e1[11], rule=MIDDLE))

#mesh algoritmasi secimi
p = mdb.models['Model-1'].parts['agard_abaqus']
c = p.cells
pickedRegions = c.getSequenceFromMask(mask=('[#ff ]', ), )
p.setMeshControls(regions=pickedRegions, technique=SWEEP,
    algorithm=MEDIAL_AXIS)

#gruplamalar

#bc
p = mdb.models['Model-1'].parts['agard_abaqus']
f = p.faces
faces = f.getSequenceFromMask(mask=('[#10281050 #14 ]', ), )
p.Set(faces=faces, name='bc')
#: The set 'bc' has been created (8 faces).
#profil mesh seed
p = mdb.models['Model-1'].parts['agard_abaqus']
e = p.edges
edges = e.getSequenceFromMask(mask=('[#b049410 #21212290 ]', ), )
p.Set(edges=edges, name='profil_mesh')
#: The set 'profil_mesh' has been created (16 edges).
#span mesh seed
p = mdb.models['Model-1'].parts['agard_abaqus']
e = p.edges
edges = e.getSequenceFromMask(mask=('[#400822 #109102 ]', ), )
p.Set(edges=edges, name='span_mesh')
#: The set 'span_mesh' has been created (9 edges).

#mesh part seedler
#profil seed
p = mdb.models['Model-1'].parts['agard_abaqus']
e = p.edges
pickedEdges = e.getSequenceFromMask(mask=('[#b049410 #21212290 ]', ), )
p.seedEdgeBySize(edges=pickedEdges, size=6.0)
#span seed
p = mdb.models['Model-1'].parts['agard_abaqus']
e = p.edges
pickedEdges = e.getSequenceFromMask(mask=('[#400822 #109102 ]', ), )
p.seedEdgeBySize(edges=pickedEdges, size=20.0)

```

```

#enlemesine seedler
p = mdb.models['Model-1'].parts['agard_abaqus']
e = p.edges
pickedEdges = e.getSequenceFromMask(mask=('[#40002004 #400 ]', ), )
p.seedEdgeByNumber(edges=pickedEdges, number=3)
p = mdb.models['Model-1'].parts['agard_abaqus']
e = p.edges
pickedEdges = e.getSequenceFromMask(mask=('[#4800000 #2000000 ]', ), )
p.seedEdgeByNumber(edges=pickedEdges, number=4)

#mesh part
p = mdb.models['Model-1'].parts['agard_abaqus']
p.generateMesh()

#coupling surface
a = mdb.models['Model-1'].rootAssembly
s1 = a.instances['agard_abaqus-1'].faces
side1Faces1 = s1.getSequenceFromMask(mask=('[#adc76b8e #6b ]', ), )
a.Surface(side1Faces=side1Faces1, name='coupling_syrface')
#: The surface 'coupling_syrface' has been created (24 faces).

#meshi goster
a = mdb.models['Model-1'].rootAssembly
a.regenerate()
session.viewports['Viewport: 1'].assemblyDisplay.setValues(mesh=ON)
session.viewports['Viewport: 1'].assemblyDisplay.meshOptions.setValues(
    meshTechnique=ON)
a = mdb.models['Model-1'].rootAssembly
session.viewports['Viewport: 1'].setValues(displayedObject=a)
p = mdb.models['Model-1'].parts['agard_abaqus']
session.viewports['Viewport: 1'].setValues(displayedObject=p)
session.viewports['Viewport: 1'].partDisplay.setValues(mesh=ON)
session.viewports['Viewport: 1'].partDisplay.meshOptions.setValues(
    meshTechnique=ON)

#statik analiz ayari incrementation
mdb.models['Model-1'].StaticStep(name='Step-1', previous='Initial',
    timeIncrementationMethod=FIXED, initialInc=0.1, noStop=OFF)
session.viewports['Viewport: 1'].assemblyDisplay.setValues(step='Step-1')

#bc ankastre
a = mdb.models['Model-1'].rootAssembly
region = a.instances['agard_abaqus-1'].sets['bc']
mdb.models['Model-1'].EncastreBC(name='BC-1', createStepName='Step-1',
    region=region)

#gruplamalar

a = mdb.models['Model-1'].rootAssembly
e1 = a.instances['agard_abaqus-1'].edges
edges1 = e1.getSequenceFromMask(mask=('[#0 #8000 ]', ), )
a.Set(edges=edges1, name='span_deflection')
#: The set 'span_deflection' has been created (1 edge).
a = mdb.models['Model-1'].rootAssembly

```

```

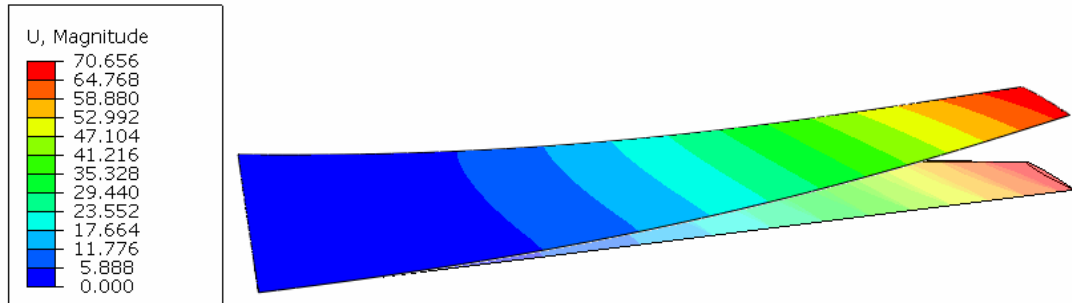
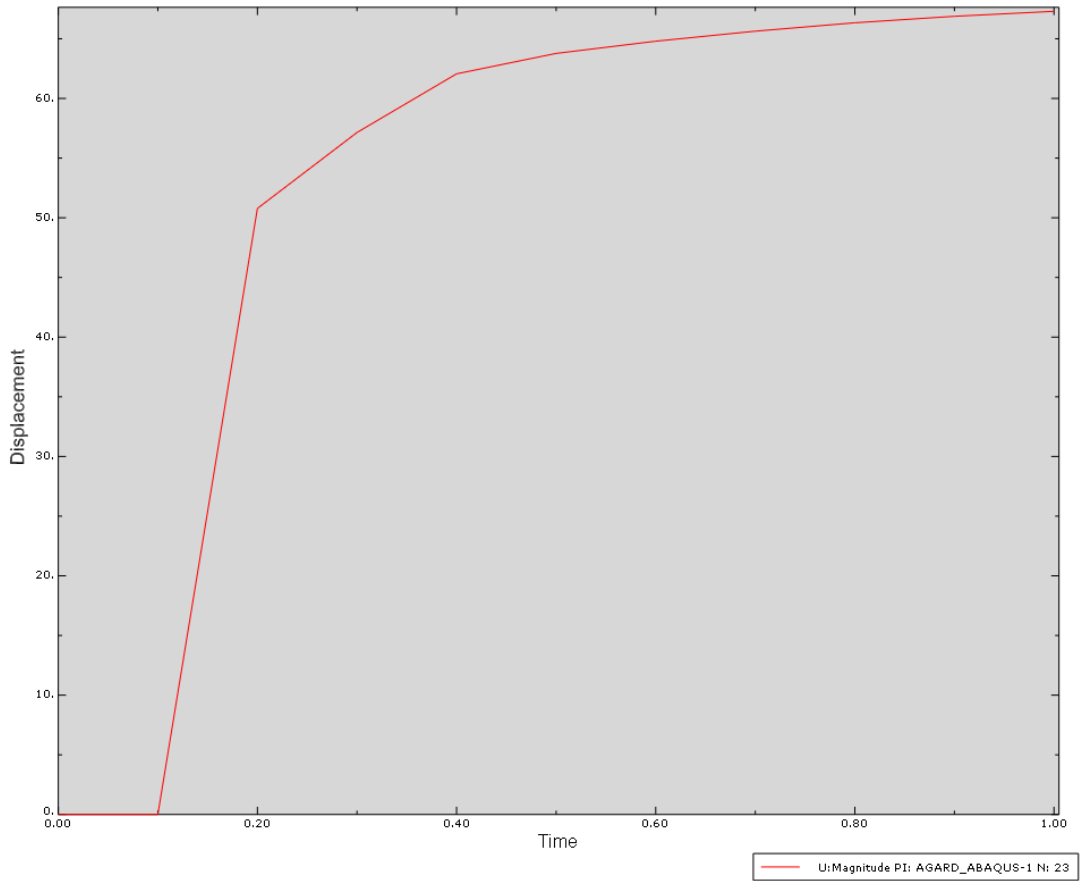
e1 = a.instances['agard_abaqus-1'].edges
edges1 = e1.getSequenceFromMask(mask=('[#0 #100000 ]', ), )
a.Set(edges=edges1, name='span_deflect_c_4')
#: The set 'span_deflect_c_4' has been created (1 edge).
a = mdb.models['Model-1'].rootAssembly
v1 = a.instances['agard_abaqus-1'].vertices
verts1 = v1.getSequenceFromMask(mask=('[#20 ]', ), )
a.Set(vertices=verts1, name='leading_point')
#: The set 'leading_point' has been created (1 vertex).
a = mdb.models['Model-1'].rootAssembly
v1 = a.instances['agard_abaqus-1'].vertices
verts1 = v1.getSequenceFromMask(mask=('[#200000 ]', ), )
a.Set(vertices=verts1, name='trailing_point')
#: The set 'trailing_point' has been created (1 vertex).

#history outputs
regionDef=mdb.models['Model-1'].rootAssembly.sets['span_deflection']
mdb.models['Model-1'].HistoryOutputRequest(name='span_deflect',
    createStepName='Step-1', variables=('U1', 'U2', 'U3'), region=regionDef,
    sectionPoints=DEFAULT, rebar=EXCLUDE)
regionDef=mdb.models['Model-1'].rootAssembly.sets['span_deflect_c_4']
mdb.models['Model-1'].HistoryOutputRequest(name='span_deflect_c_4',
    createStepName='Step-1', variables=('U1', 'U2', 'U3'), region=regionDef,
    sectionPoints=DEFAULT, rebar=EXCLUDE)
regionDef=mdb.models['Model-1'].rootAssembly.sets['leading_point']
mdb.models['Model-1'].HistoryOutputRequest(name='leading_point',
    createStepName='Step-1', variables=('U1', 'U2', 'U3'), region=regionDef,
    sectionPoints=DEFAULT, rebar=EXCLUDE)
regionDef=mdb.models['Model-1'].rootAssembly.sets['trailing_point']
mdb.models['Model-1'].HistoryOutputRequest(name='trailing_point',
    createStepName='Step-1', variables=('U1', 'U2', 'U3'), region=regionDef,
    sectionPoints=DEFAULT, rebar=EXCLUDE)

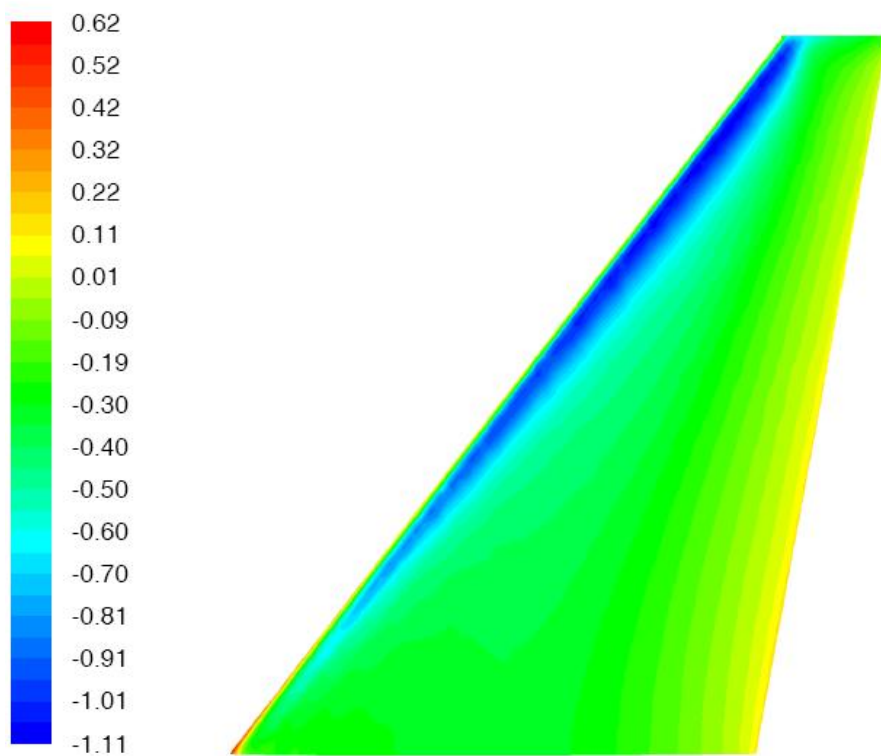
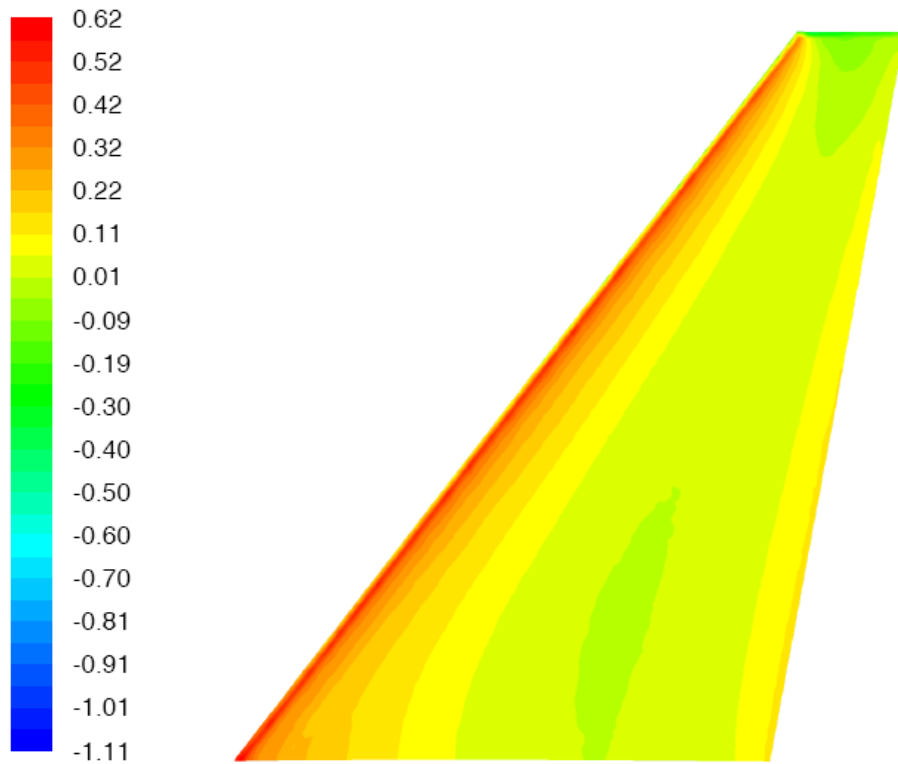
#write abaqus input file
mdb.Job(name='agard', model='Model-1', type=ANALYSIS,
explicitPrecision=SINGLE,
    nodalOutputPrecision=SINGLE, description="",
    parallelizationMethodExplicit=DOMAIN, multiprocessingMode=DEFAULT,
    numDomains=1, userSubroutine="", numCpus=1, preMemory=256.0,
    standardMemory=256.0, standardMemoryPolicy=MODERATE, scratch="",
    echoPrint=OFF, modelPrint=OFF, contactPrint=OFF, historyPrint=OFF)
mdb.jobs['agard'].writeInput(consistencyChecking=OFF)
#: The job input file has been written to "agard.inp".

```

**APPENDIX B : Results for the Selected Pareto Design #9**



**Figure B.1** : Structural analysis results for  $\Lambda_{c/4} = 32$  and  $\lambda = 0.2$



**Figure B.2 :** Pressure coefficients for lower and upper wing surfaces respectively for  $\Lambda_{c/4} = 32$  and  $\lambda = 0.2$

**APPENDIX C : Total Designs for the Optimization Problem**



**Table B.1:** Design summary

Design ID	Sweep	Taper	cd	cl	Displacement	L/D	Weight
0	26	0.30	0.0358	0.4302	54.63	12.03	1.22
1	12	0.20	0.0395	0.4573	52.04	11.58	1.09
2	38	0.40	0.0303	0.3799	65.15	12.55	1.37
3	18	0.35	0.0366	0.4315	45.84	11.78	1.29
4	44	0.15	0.0296	0.3742	110.95	12.64	1.03
5	6	0.45	0.0363	0.4175	38.71	11.49	1.45
6	32	0.25	0.0344	0.4214	65.69	12.24	1.15
7	16	0.48	0.0353	0.4132	39.88	11.71	1.49
8	42	0.28	0.0297	0.3750	87.32	12.63	1.18
9	2	0.38	0.0372	0.4259	41.07	11.46	1.33
10	28	0.18	0.0368	0.4431	67.80	12.05	1.06
11	8	0.23	0.0392	0.4523	48.86	11.53	1.12
12	2	0.33	0.0377	0.4324	42.95	11.46	1.25
13	16	0.45	0.0356	0.4176	40.89	11.72	1.45
14	28	0.20	0.0365	0.4393	64.85	12.03	1.09
15	12	0.38	0.0370	0.4304	42.46	11.62	1.33
16	12	0.25	0.0387	0.4498	48.68	11.62	1.15
17	10	0.20	0.0395	0.4566	51.24	11.56	1.09
18	32	0.35	0.0332	0.4079	58.31	12.28	1.29
19	26	0.28	0.0361	0.4339	56.24	12.03	1.18
20	40	0.18	0.0316	0.3949	91.71	12.51	1.06
21	30	0.25	0.0352	0.4270	62.63	12.14	1.15
22	46	0.28	0.0275	0.3524	105.52	12.83	1.18
23	28	0.15	0.0370	0.4454	70.65	12.04	1.03
24	32	0.33	0.0335	0.4107	59.77	12.27	1.25
25	30	0.20	0.0358	0.4340	67.64	12.12	1.09
26	36	0.25	0.0328	0.4062	72.56	12.40	1.15
27	12	0.15	0.0400	0.4630	56.16	11.56	1.03
28	10	0.40	0.0368	0.4261	40.94	11.57	1.37
29	36	0.30	0.0322	0.4001	68.40	12.41	1.22
30	14	0.25	0.0386	0.4495	49.38	11.65	1.15
31	22	0.25	0.0374	0.4438	54.44	11.88	1.15
32	38	0.35	0.0308	0.3856	68.55	12.53	1.29
33	28	0.40	0.0339	0.4107	50.69	12.12	1.37
34	30	0.10	0.0367	0.4432	80.85	12.06	0.97

36	38	0.30	0.0313	0.3917	72.16	12.51	1.22
37	30	0.18	0.0360	0.4364	70.25	12.12	1.06
38	22	0.20	0.0380	0.4507	58.50	11.86	1.09
39	20	0.18	0.0388	0.4563	58.91	11.76	1.06
40	4	0.25	0.0388	0.4458	46.71	11.49	1.15
41	38	0.28	0.0317	0.3946	74.47	12.45	1.18
42	34	0.10	0.0352	0.4289	88.51	12.20	0.97
43	36	0.18	0.0335	0.4141	80.73	12.35	1.06
44	30	0.30	0.0346	0.4204	58.98	12.15	1.22
45	28	0.45	0.0333	0.4033	48.27	12.13	1.45
46	36	0.45	0.0305	0.3817	58.48	12.50	1.45
47	38	0.25	0.0319	0.3975	77.00	12.46	1.15
48	46	0.30	0.0272	0.3498	103.06	12.86	1.22
49	34	0.30	0.0330	0.4078	64.74	12.34	1.22
50	22	0.30	0.0367	0.4364	51.15	11.88	1.22
51	46	0.18	0.0282	0.3597	117.76	12.77	1.06
52	20	0.15	0.0392	0.4602	61.49	11.75	1.03
53	28	0.35	0.0346	0.4183	53.43	12.09	1.29
54	28	0.25	0.0359	0.4330	60.36	12.06	1.15
55	36	0.15	0.0338	0.4162	84.38	12.32	1.03
56	38	0.43	0.0300	0.3767	63.48	12.56	1.41
57	38	0.48	0.0295	0.3706	60.63	12.58	1.49
58	20	0.25	0.0378	0.4461	52.99	11.81	1.15
59	44	0.25	0.0288	0.3665	98.27	12.72	1.15
61	30	0.15	0.0363	0.4395	73.28	12.10	1.03
62	32	0.28	0.0341	0.4176	63.48	12.24	1.18
63	36	0.28	0.0325	0.4033	70.46	12.42	1.18
64	38	0.33	0.0311	0.3888	70.29	12.49	1.25
65	28	0.28	0.0355	0.4296	58.28	12.11	1.18
66	36	0.20	0.0333	0.4116	77.90	12.35	1.09
67	14	0.48	0.0355	0.4141	39.30	11.66	1.49
68	38	0.18	0.0326	0.4046	85.32	12.42	1.06
69	38	0.38	0.0305	0.3827	66.78	12.53	1.33
70	48	0.33	0.0260	0.3359	112.74	12.93	1.25
71	34	0.43	0.0316	0.3913	56.66	12.38	1.41
72	46	0.20	0.0280	0.3579	114.08	12.76	1.09
73	4	0.28	0.0385	0.4418	45.38	11.47	1.18

75	6	0.48	0.0360	0.4140	37.94	11.49	1.49
76	46	0.48	0.0257	0.3336	89.57	12.98	1.49
77	32	0.20	0.0350	0.4274	70.66	12.20	1.09
78	38	0.15	0.0328	0.4069	88.90	12.39	1.03
79	30	0.38	0.0336	0.4097	54.20	12.21	1.33
80	36	0.40	0.0312	0.3876	61.27	12.44	1.37
81	38	0.45	0.0298	0.3741	62.09	12.55	1.45
82	34	0.45	0.0314	0.3880	55.26	12.36	1.45
83	32	0.10	0.0360	0.4365	84.23	12.13	0.97
84	48	0.20	0.0269	0.3458	126.71	12.85	1.09
85	30	0.28	0.0349	0.4238	60.78	12.14	1.18
87	30	0.23	0.0355	0.4306	65.06	12.13	1.12
88	46	0.35	0.0268	0.3457	98.34	12.90	1.29
89	38	0.10	0.0332	0.4099	97.79	12.34	0.97
90	32	0.23	0.0348	0.4239	67.75	12.19	1.12
91	6	0.10	0.0405	0.4640	57.99	11.46	0.97
93	50	0.43	0.0239	0.3146	117.46	13.14	1.41
95	4	0.48	0.0360	0.4128	37.80	11.46	1.49
96	32	0.18	0.0353	0.4301	73.34	12.17	1.06
97	14	0.20	0.0393	0.4569	52.90	11.63	1.09
98	34	0.15	0.0347	0.4246	79.84	12.25	1.03
99	22	0.43	0.0351	0.4168	44.73	11.87	1.41
100	6	0.30	0.0382	0.4399	44.49	11.51	1.22
101	36	0.38	0.0314	0.3908	62.94	12.45	1.33
102	2	0.10	0.0401	0.4585	56.58	11.44	0.97
103	6	0.13	0.0403	0.4622	55.67	11.48	1.00
104	34	0.35	0.0324	0.4012	61.17	12.38	1.29
105	28	0.10	0.0375	0.4497	78.10	11.99	0.97
106	6	0.15	0.0401	0.4596	53.38	11.47	1.03
107	34	0.38	0.0322	0.3978	59.49	12.34	1.33

## **RESUME**

Levent ÖNCÜ was born in March 6<sup>th</sup>, 1983 in Zonguldak, TURKEY. He had his high school education in Zonguldak Atatürk Anatolian High School (ZAAL) and Zonguldak Science High School (ZFL). He graduated 2<sup>nd</sup> place in the graduating class of Aeronautical Engineering Department of İstanbul Technical University (İTÜ) Aeronautics and Astronautics Faculty in 2006. He attended the Von Karman Institute's Short Training Program in Brussels, BELGIUM. He had the National Scholarship Program for the Graduate Students of The Scientific and Technological Research Council of Turkey (TÜBİTAK-BAYG) during his graduate study. He is now going on his graduate in Aeronautical Engineering and working as a researcher in the TÜBİTAK project 105M235 "Analysis and Reliability Based Design Optimization of Fluid-Structure Interaction Problems Subject to Instability Phenomena".