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Sandra Pinelas • Michel Chipot • Zuzana Dosla  
Editors

# Differential and Difference Equations with Applications

Contributions from the International  
Conference on Differential & Difference  
Equations and Applications

 Springer

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# Preface

For five days from July 4 to 8, 2011, more than 230 mathematicians from 50 countries attended the International Conference on Differential and Difference Equations and Applications, held at Azores University, Ponta Delgada, Portugal.

This conference was held in honour of Professor Ravi P. Agarwal for his contributions to science and, in particular, to the mathematical community.

The scientific aim of this conference was to bring together mathematicians working in various disciplines of differential and difference equations and their applications. There were 11 plenary lectures, 21 main lectures, and 198 communications about the current research in this field. This volume contains 60 selected original papers which are connected to research lectures given at the conference. Each paper has been carefully reviewed.

We take this opportunity to thank all the participants of the conference and the contributors to these proceedings. Our special thanks belong to the Department of Mathematics, Azores University, Ponta Delgada, Portugal, for the sincere hospitality. We are also grateful to the Scientific and Organizing Committees for all the effort in the preparation of the conference.

We hope that this volume will serve researchers in all fields of differential and difference equations.

Amadora, Portugal  
Zürich, Switzerland  
Brno, Czech Republic

Sandra Pinelas  
Michel Chipot  
Zuzana Dosla



# Contents

## Part I Main Speakers

<b>Two-Term Perturbations in Half-Linear Oscillation Theory</b> .....	3
Ondřej Došlý and Simona Fišnarová	
<b>Capillary Forces on Partially Immersed Plates</b> .....	13
Robert Finn	
<b>Singular Problems for Integro-differential Equations in Dynamic Insurance Models</b> .....	27
Tatiana Belkina, Nadezhda Konyukhova, and Sergey Kurochkin	
<b>Oscillatory Properties of Solutions of Generalized Emden–Fowler Equations</b> .....	45
R. Koplatadze	
<b>On Conforming Tetrahedralisations of Prismatic Partitions</b> .....	63
Sergey Korotov and Michal Křížek	
<b>Swarm Dynamics and Positive Dynamical Systems</b> .....	69
Ulrich Krause	
<b>Periodic Solutions of Differential and Difference Systems with Pendulum-Type Nonlinearities: Variational Approaches</b> .....	83
Jean Mawhin	
<b>Two-Dimensional Differential Systems with Asymmetric Principal Part</b> .....	99
Felix Sadyrbaev	
<b>Hyperbolicity Radius of Time-Invariant Linear Systems</b> .....	113
T.S. Doan, A. Kalauch, and S. Siegmund	

<b>Oscillation Criteria for Delay and Advanced Difference Equations with Variable Arguments</b> .....	127
I.P. Stavroulakis	
<b>Positive Solutions of Nonlinear Equations with Explicit Dependence on the Independent Variable</b> .....	147
J.R.L. Webb	
<b>Existence Results for a System of Third-Order Right Focal Boundary Value Problems</b> .....	165
Patricia J.Y. Wong	
<b>Forced Oscillation of Second-Order Impulsive Differential Equations with Mixed Nonlinearities</b> .....	183
A. Özbekler, and A. Zafer	
<b>From the Poincaré–Birkhoff Fixed Point Theorem to Linked Twist Maps: Some Applications to Planar Hamiltonian Systems</b> .....	197
Anna Pascoletti and Fabio Zanolin	
<b>Part II Contributions</b>	
<b>Pullback Attractors for NonAutonomous Dynamical Systems</b> .....	217
María Anguiano, Tomás Caraballo, José Real, and José Valero	
<b>Uniform Estimates and Existence of Solutions with Prescribed Domain to Nonlinear Third-Order Differential Equation</b> .....	227
Irina Astashova	
<b>A Second-Order Difference Scheme for a Singularly Perturbed Reaction-Diffusion Problem</b> .....	239
Basem S. Attili	
<b>Parametric Dependence of Boundary Trace Inequalities</b> .....	249
Giles Auchmuty	
<b>On Properties of Third-Order Functional Differential Equations</b> .....	255
Blanka Baculíková and Jozef Džurina	
<b>On the Structure of Two-Layer Cellular Neural Networks</b> .....	265
Jung-Chao Ban, Chih-Hung Chang, and Song-Sun Lin	
<b>Linear Integral Equations with Discontinuous Kernels and the Representation of Operators on Regulated Functions on Time Scales</b> .....	275
Luciano Barbanti, Berenice Camargo Damasceno, Geraldo Nunes Silva, and Marcia Cristina Anderson Braz Federson	
<b>Strong Solutions to Buoyancy-Driven Flows in Channel-Like Bounded Domains</b> .....	283
Michal Beneš	



**Infinite-Horizon Variational Principles and Almost Periodic Oscillations** ..... 293  
 Joël Blot and Abdelkader Bouadi

**A Note on Elliptic Equations Involving the Critical Sobolev Exponent** .... 311  
 Gabriele Bonanno, Giovanni Molica Bisci, and Vicențiu Rădulescu

**Sign-Changing Subharmonic Solutions to Unforced Equations with Singular  $\phi$ -Laplacian** ..... 321  
 Alberto Boscaggin and Maurizio Garrione

**Nonlinear Difference Equations with Discontinuous Right-Hand Side**..... 331  
 Pasquale Candito and Roberto Livrea

**Pullback Attractors of Stochastic Lattice Dynamical Systems with a Multiplicative Noise and Non-Lipschitz Nonlinearities** ..... 341  
 Tomás Caraballo, Francisco Morillas, and José Valero

**Discrete-Time Counterparts of Impulsive Hopfield Neural Networks with Leakage Delays** ..... 351  
 Haydar Akça, Valéry Covachev, and Zlatinka Covacheva

**A Symmetric Quantum Calculus** ..... 359  
 Artur M.C. Brito da Cruz, Natália Martins, and Delfim F.M. Torres

**Stability of Nonlinear Differential Systems with Right-Hand Side Depending on Markov’s Process** ..... 367  
 Irada Dzhalladova

**Oscillation of Third-Order Differential Equations with Mixed Arguments** ..... 375  
 Jozef Džurina and Blanka Baculíková

**On Estimates for the First Eigenvalue of the Sturm–Liouville Problem with Dirichlet Boundary Conditions and Integral Condition** .... 387  
 Svetlana Ezhak

**Boundary Value Problems for Schrödinger Operators on a Path Associated to Orthogonal Polynomials**..... 395  
 A. Carmona, A.M. Encinas, and S. Gago

**Centers in a Quadratic System Obtained from a Scalar Third Order Differential Equation** ..... 405  
 Adriana Buică, Isaac A. García, and Susanna Maza

**Three Solutions for Systems of  $n$  Fourth-Order Partial Differential Equations** ..... 411  
 Shapour Heidarkhani

<b>The Fučík Spectrum: Exploring the Bridge Between Discrete and Continuous World</b> .....	421
Gabriela Holubová and Petr Nečesal	
<b>The Displacement of a Sliding Bar Subject to Nonlinear Controllers</b> .....	429
Gennaro Infante and Paolamaria Pietramala	
<b>Abstract Bifurcation Theorems and Applications to Dynamical Systems with Resonant Eigenvalues</b> .....	439
Vladimir Jačimović	
<b>Oscillation of Difference Equations with Impulses</b> .....	449
Fatma Karakoç	
<b>On Estimates of the First Eigenvalue for the Sturm–Liouville Problem with Symmetric Boundary Conditions and Integral Condition</b> .....	457
Elena Karulina	
<b>On Polyhedral Estimates for Trajectory Tubes of Differential Systems with a Bilinear Uncertainty</b> .....	465
Elena K. Kostousova	
<b>Analysis and Computational Approximation of a Forward–Backward Equation Arising in Nerve Conduction</b> .....	475
P.M. Lima, M.F. Teodoro, N.J. Ford, and P.M. Lumb	
<b>Multiple Solutions for a Class of Degenerate Quasilinear Elliptic Systems</b> .....	485
G.A. Afrouzi and S. Mahdavi	
<b>A Symmetric Nörlund Sum with Application to Inequalities</b> .....	495
Artur M.C. Brito da Cruz, Natália Martins and Delfim F.M. Torres	
<b>Numerical Range and Bifurcation Points of a Family of Rational Function</b> .....	505
Helena Melo and João Cabral	
<b>Existence of Solutions for a Class of Semilinear Elliptic Systems via Variational Methods</b> .....	517
G.A. Afrouzi and M. Mirzapour	
<b>Periodic Boundary Value Problems For Systems of First-Order Differential Equations with Impulses</b> .....	525
M. Mohamed, H.S. Ahmad, and M.S.M. Noorani	
<b>Numerical Methods for Multi-term Fractional Boundary Value Problems</b> .....	535
N.J. Ford and M.L. Morgado	

**Topological Structures for Studying Dynamic Equations on Time Scales** . 543  
 Bonita A. Lawrence and Ralph W. Oberste-Vorth

**Existence of Nonoscillatory Solutions of the Discrete FitzHugh-Nagumo System** ..... 551  
 Ana Pedro and Pedro Lima

**On Extinction Phenomena for Parabolic Systems** ..... 561  
 T. Gramchev, M. Marras, and S. Vernier-Piro

**Conjugacy of Discrete Semidynamical Systems in the Neighbourhood of Invariant Manifold** ..... 571  
 Andrejs Reinfelds

**$\Gamma$ -Convergence of Multiscale Periodic Energies Depending on the Curl of Divergence-Free Fields** ..... 579  
 Hélia Serrano

**A Geometric Proof of the Existence of Two Solutions of the Bahri-Coron Problem** ..... 589  
 Norimichi Hirano and Naoki Shioji

**Period-Two Solutions to Some Systems of Rational Difference Equations** ..... 599  
 Walter S. Sizer

**Effect of Roughness on the Flow of a Fluid Against Periodic and Nonperiodic Rough Boundaries** ..... 607  
 J. Casado-Díaz, M. Luna-Laynez, and F.J. Suárez-Grau

**A Double Complex Construction and Discrete Bogomolny Equations**..... 615  
 Volodymyr Sushch

**Pseudo-Differential Equations on Manifolds with Non-smooth Boundaries** ..... 625  
 Vladimir B. Vasilyev

**Positive Solutions for a Kind of Singular Nonlinear Fractional Differential Equations with Integral Boundary Conditions** ..... 639  
 Junfang Zhao and Hairong Lian

**Functional Aspects of the Hardy Inequality: Appearance of a Hidden Energy** ..... 653  
 J.L. Vázquez and N.B. Zographopoulos