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This is an **author produced version** of a paper published in:

Psychological Methods (2023): 1 – 65

DOI: <https://doi.org/10.1037/met0000590>

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Dimensionality assessment in bi-factor structures with multiple general factors: a network psychometrics approach

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The published version of this manuscript is in *Psychological Methods* and can be accessed at <https://doi.org/10.1037/met0000590>.

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Author note

Funding: This research was supported by Grant PSI2017-85022-P (Ministerio de Ciencia, Innovación y Universidades, Spain) and the UAM IIC Chair Psychometric Models and Applications. Luis Eduardo Garrido is supported by Grant 2018-2019-1D2-085 from the Fondo Nacional de Innovación Desarrollo Científico y Tecnológico (FONDOCYT) of the Dominican Republic. The results of this work were presented in the XVII Congress of the Spanish Association of Methodology for the Social Sciences (AEMCCO XVII) and the manuscript was published as a preprint in the psyarxiv repository at <https://psyarxiv.com/2ujdk/>.

Conflicts of interest: None.

Material and data availability: The `bifactor` package is available at <https://github.com/Marcosjnez/bifactor> and all the files necessary to reproduce the simulation data, analyses, and figures can be found at <https://osf.io/u7qwj/>. The data used in this manuscript is open-access and was obtained from <https://osf.io/72zp3/>

Abstract

The accuracy of factor retention methods for structures with one or more general factors, like the ones typically encountered in fields like intelligence, personality, and psychopathology, has often been overlooked in dimensionality research. To address this issue, we compared the performance of several factor retention methods in this context, including a network psychometrics approach developed in this study. For estimating the number of group factors, these methods were the Kaiser criterion, empirical Kaiser criterion, parallel analysis with principal components (PA_{PCA}) or principal axis, and exploratory graph analysis with Louvain clustering (EGA_{LV}). We then estimated the number of general factors using the factor scores of the first-order solution suggested by the best two methods, yielding a “second-order” version of PA_{PCA} (PA_{PCA-FS}) and EGA_{LV} (EGA_{LV-FS}). Additionally, we examined the direct multilevel solution provided by EGA_{LV} . All the methods were evaluated in an extensive simulation manipulating nine variables of interest, including population error. The results indicated that EGA_{LV} and PA_{PCA} displayed the best overall performance in retrieving the true number of group factors, the former being more sensitive to high cross-loadings, and the latter to weak group factors and small samples. Regarding the estimation of the number of general factors, both PA_{PCA-FS} and EGA_{LV-FS} showed a close to perfect accuracy across all the conditions, while EGA_{LV} was inaccurate. The methods based on EGA were robust to the conditions most likely to be encountered in practice. Therefore, we highlight the particular usefulness of EGA_{LV} (group factors) and EGA_{LV-FS} (general factors) for assessing bi-factor structures with multiple general factors.

Keywords: *Dimensionality Assessment, Exploratory Bi-Factor Analysis, Exploratory Graph Analysis, Hierarchical Data, Parallel Analysis*

1 Introduction

Dimensionality assessment plays a central role in psychometrics, as it constitutes one of the cornerstone decisions during test validation. It is known that a wrong assessment misguides the construction and refinement of psychological instruments, undermining also the interpretability of the results from the forthcoming data analysis. However, simulation studies that focus on bi-factor structures with multiple general factors are lacking in dimensionality research, and it is uncertain how to proceed when assessing the dimensionality of these structures. This comes as a surprise given the current popularity of bi-factor models in fields like intelligence (Beaujean, 2015), personality (Abad et al., 2018), and psychopathology (Bornovalova et al., 2020), where psychometric theories often comprise multiple general factors.

If we had reliable methods for assessing such complex structures, we could test the evidence in favor or against the theories underpinning these fields. Therefore, the aim of this study was three-fold: firstly, investigating for the first time the capability of some popular factor retention methods to uncover the number of group factors in bi-factor structures with one or multiple general factors. The second goal of the study involved testing the performance of two new methods that we developed to detect the number of general factors in these structures. Finally, the third goal consisted of showing how these methods can be applied to uncover the hierarchical structure of the HEXACO-100 using open data.

2 Bi-factor structures with multiple general factors

The main feature of bi-factor models is that items are allowed to simultaneously load on a collection of group factors (e.g., generosity and tolerance), also called specific factors, and one general factor (e.g., agreeableness), with the group factors representing narrower traits that explain the common variance that is left after accounting for the general factor (Reise, 2012).

Although the development of exploratory bi-factor techniques is still an active line of research, with proposals involving analytic rotation criteria (Jennrich & Bentler, 2011) and

26 target-based procedures (Abad et al., 2017; Garcia-Garzon et al., 2019), they have been
27 recently generalized to cover more than one general factor. Some examples are the two-tier
28 hierarchical model of Tian and Liu (2021) and the exploratory bi-factor model with multiple
29 general factors of Jiménez et al. (2022; Figure 1). These generalizations have the advantage of
30 estimating several bi-factor structures in a single model, uncovering relationships that would
31 remain hidden if we performed independent bi-factor analyses for each domain of the factor
32 structure (e.g., correlations and cross-loadings among the general factors).

33 The incorporation of multiple general factors to the bi-factor model reflects the consensus
34 that many psychological phenomena are hierarchically organized, with the semantic content
35 of narrow traits being subsumed into broader, multiple general factors.¹ In fact, there
36 have already been some efforts to explore and test these hierarchical organizations, such as
37 the Hierarchical Taxonomy of Psychopathology (HiTOP; Kotov et al., 2017; Ringwald et
38 al., 2021), which is a dimensional alternative to the Diagnostic and Statistical Manual of
39 Mental Disorders (DSM) that conceptualizes psychopathology across different strata, namely
40 symptoms, syndromes, sub-factors, and spectra. Detecting the organization of such general
41 traits is essential to make a comprehensive assessment of the main pathological features
42 of patients as well as to facilitate the communication of diagnoses among mental health
43 researchers and professionals. In these regards, the bi-factor model provides a way to the
44 estimation of general traits that are concomitant to the narrower ones.

45 Despite recent advancements in exploratory bi-factor analysis, its application still requires
46 a decision regarding the number of group and general factors to extract. Up to now, simulation
47 studies including general factors are scarce and usually focus on structures with second-order
48 general factors instead of on the broader class of bi-factor structures. Bi-factor models
49 are only equivalent to second-order models when proportionality constraints between the
50 group and general factors are satisfied (Mansolf & Reise, 2016), so simulations covering the
51 specific bi-factor case are required to understand what factor retention methods are suited to

¹Along the manuscript, we adopt the nomenclature of Yung et al. (1999) and Molenaar (2016), who considered the bi-factor and the higher-order models as particular cases of hierarchical structures.

52 assess unrestricted hierarchical organizations. In this context, some researchers have already
53 investigated the behavior of parallel analysis methods (Crawford et al., 2010; Green et al.,
54 2015, 2016, 2018; Levy et al., 2021). However, the extent to which other factor retention
55 methods work for this purpose is unknown and the quality of the recovery of the number of
56 general factors remains largely untested.

57 **3 Dimensionality assessment methods**

58 To overcome the lack of dimensionality assessment research in bi-factor structures with
59 multiple general factors, we designed an exhaustive simulation study. In this section, we
60 review the rationale behind all the factor retention methods that we decided to include in
61 the simulation to estimate the number of group factors. We also mention their qualities and
62 pitfalls as reported in the simulation literature. Finally, we describe a new procedure to
63 determine the number of general factors.

64 **3.1 The Kaiser Criterion**

65 The Kaiser criterion (K1; Kaiser, 1960), also known as the eigenvalue-greater-than-one
66 criterion, is one of the first and most popular factor retention methods. According to K1, the
67 first k greater-than-one eigenvalues of a correlation matrix are indicative of k factors. This
68 criterion was devised under the rationale that substantive factors should explain at least more
69 variance than the average variance of the variables, which is one for correlation matrices, and
70 to prevent the estimated factors from having negative reliability (Cliff, 1988). However, K1
71 gives an asymptotic lower bound for the number of true dimensions (Guttman, 1954). At
72 the sample level, its low accuracy has been replicated by a large body of simulation research
73 (Auerswald & Moshagen, 2019; Ruscio & Roche, 2011; Yeomans & Golder, 1982; Zwick &
74 Velicer, 1986).

75 The poor performance of K1 can be attributed to the bias of the sample eigenvalues.

76 The first sample eigenvalue is the maximum value obtained from the optimization problem
77 $\operatorname{argmax}_{\mathbf{x} \in \mathbb{Q}} \mathbf{x}^\top \mathbf{S} \mathbf{x}$, where \mathbf{S} is the sample correlation matrix and \mathbf{x} is estimated from the set of
78 unit vectors \mathbb{Q} . Subsequent eigenvalues are estimated similarly, but constraining the new
79 estimated vectors (i.e., eigenvectors) to remain orthogonal to all the previous ones. This
80 serial dependency results in the first sample eigenvalues being upwardly biased, as they have
81 more variance to capitalize on by chance with fewer constraints. Thus, the bias of the sample
82 eigenvalues is inversely related to the sample size and positively related to the number of
83 variables, as there is more noise in small samples with a large number of variables, leading K1
84 to overestimate the true number of factors.

85 However, learning this important shortcoming has not prevented the widespread use of K1.
86 Goretzko et al. (2021) reviewed the exploratory factor analysis literature published between
87 2007 and 2017 in two psychological journals with a special focus on test development and
88 found that K1 was the most common method either when several factor retention methods
89 were simultaneously used (55.6%) and when a single method was used (10.5%). To our
90 knowledge, the performance of K1 has not been investigated in the presence of general factors
91 in a bi-factor context.

92 3.2 The Empirical Kaiser Criterion

93 Braeken and Assen (2017) proposed the Empirical Kaiser Criterion (EKC), a modification of
94 K1 that considers the serial dependency between the sample eigenvalues. EKC compares the
95 sample eigenvalues to reference eigenvalues (λ^{EKC}) that are sequentially computed under a
96 null model with no latent factors. Asymptotically, if the variables are normally distributed,
97 the eigenvalues of the sample correlation matrix follow the Marčenko-Pastur distribution
98 (Marčenko & Pastur, 1967). Hence, Braeken and Assen (2017) set the first reference eigenvalue
99 under the null model (λ_1^{EKC}) to the expected value of the first sample eigenvalue from the
100 Marčenko-Pastur distribution, $(1 + \sqrt{J/n})^2$, where n is the sample size and J is the number
101 of variables. The subsequent reference eigenvalues, λ_j^{EKC} for $j = \{2, 3, \dots, J\}$, are then

102 computed multiplying this value by the average variance that is left after taking out the first
 103 $j - 1$ factors, $(J - \sum_{j=0}^{j-1} \lambda_j)/(J - j + 1)$, where $\lambda_0 = 0$. The resulting reference eigenvalues
 104 can then be interpreted as an estimate of the population value of λ_j if the null model of
 105 conditional independence was true after accounting for $j - 1$ factors.

106 Altogether, the overall formula for computing the reference eigenvalues can be written as

$$\lambda_j^{EKC} = \max \left(\frac{J - \sum_{j=0}^{j-1} \lambda_j}{J - j + 1} (1 + \sqrt{J/n})^2, 1 \right). \quad (1)$$

107 Notice that the minimum reference eigenvalue is set to one to guarantee that, at the population
 108 level, K1 and EKC match in the number of factors to retain, representing a lower bound for
 109 the true number of factors (Guttman, 1954).

110 EKC has been suggested to be more robust than parallel analysis in conditions involving
 111 few variables per factor and high factor correlations (Auerswald & Moshagen, 2019; Braeken
 112 & Assen, 2017) and in the presence of cross-loadings in multivariate normal data (Li et al.,
 113 2020). However, its performance has not been tested in bi-factor structures.

114 **3.3 Parallel Analysis**

115 Parallel analysis (PA; Horn, 1965) has been considered the gold-standard method for dimen-
 116 sionality assessment for many decades, with many simulation studies recommending its use
 117 for either continuous (Fabrigar et al., 1999; Lim & Jahng, 2019; Zwick & Velicer, 1986) and
 118 ordinal data (Garrido et al., 2016, 2013; Timmerman & Lorenzo-Seva, 2011). PA would
 119 emulate the sampling process of the original correlation matrix if no latent factors were
 120 present, controlling the impact that the sample size and the number of variables bear in
 121 the magnitude of the eigenvalues. Similarly to the EKC method, PA compares the sample
 122 eigenvalues to reference eigenvalues obtained by simulating data from a null model, with
 123 the first k sample eigenvalues greater than their corresponding reference eigenvalues being
 124 indicative of k meaningful factors.

125 The reference eigenvalues can be computed in many ways. In the original formulation,
126 Horn (1965) performed principal component analysis in a large number of $n \times J$ matrices
127 of uncorrelated normally distributed random variables, using the average of the empirical
128 distribution of the eigenvalues as the reference eigenvalues. Later proposals involved the use
129 of the 95th percentile of the empirical distribution instead of the mean (Buja & Eyuboglu,
130 1992; Glorfeld, 1995), the resampling of the observed data matrix for generating new random
131 data (PA_{PCA}; Buja & Eyuboglu, 1992), the replacement of principal components either by
132 principal axis factoring (PA_{PAF}; Humphreys & Ilgen, 1969) or minimum rank factor analysis
133 (Timmerman & Lorenzo-Seva, 2011), and the assessment of each j factor in a sequential
134 manner, taking the $j - 1$ factor model as the null model for generating random data (Green
135 et al., 2012).

136 Several simulation studies comparing different versions of PA have found that even though
137 no single method outperformed others in all conditions, PA_{PCA} presented the highest overall
138 accuracy (Lim & Jahng, 2019; Xia, 2021). However, other authors support employing PA_{PAF}
139 instead, arguing that it outperforms PA_{PCA} under conditions with multiple correlated factors
140 (Crawford et al., 2010; Keith et al., 2016). In the particular case of structures including
141 general factors (in both second-order and bi-factor structures), Crawford et al. (2010) found
142 that PA_{PCA} tended to recover the number of general factors while PA_{PAF} accurately recovered
143 the number of group factors. However, Lim and Jahng (2019) noted that this superiority
144 vanishes when the realistic condition of population error is included. This current controversy
145 prompted the examination of both methods in our simulations.

146 Finally, concerning the cut-off value needed to derive the reference eigenvalues, Xia (2021)
147 showed that the performance of PA_{PCA} using the 95th percentile was more robust to model
148 misspecification than the mean value. In contrast, the mean of the empirical eigenvalues was
149 more robust to multiple correlated factors. These results are explained by stringent cut-offs
150 ignoring minor factors and larger cut-offs avoiding the collapse of correlated factors.

151 **3.4 Exploratory Graph Analysis**

152 Network psychometrics is an alternative method to factor analysis to model and interpret
153 psychological data. In a network model, a random variable is a node connected to other
154 nodes by edges representing their relationship after conditioning on all the other variables. In
155 the same way that factor models are commonly displayed with diagrams, networks models
156 are visualized with a graph containing all the nodes and edges connecting them, with nodes
157 belonging to the same cluster being placed closer, and edge's thickness representing the
158 strength of the associations between the nodes (Figure 2).

159 For multivariate normal data, the most straightforward way to model such pairwise
160 relationships among the variables is using their partial correlations. This is the simplest way
161 of estimating a Gaussian Graphical Model (GGM; Epskamp et al., 2018). However, Epskamp
162 and Fried (2017) warned that when two variables are conditionally independent, the partial
163 correlation matrix usually reflects spurious relationships due to sampling variation, leading
164 to large standard errors and unstable parameter estimates. As a solution, regularization
165 techniques such as the graphical least absolute shrinkage and selection operator (GLASSO;
166 Friedman et al., 2008) are used to estimate sparse partial correlations. GLASSO regularization
167 contains a tuning parameter controlling the sparsity of the network that is selected by
168 minimizing a complexity function such as the Extended Bayesian Information Criterion
169 (EBIC; Chen & Chen, 2008). With this approach, small partial correlations are shrunk
170 towards zero, yielding a more parsimonious and interpretative network with more unconnected
171 nodes reflecting conditional independence. Latent factors underlying the data can then be
172 related to clusters of nodes, with edges within a cluster being stronger than between clusters
173 (Golino & Epskamp, 2017). Such reciprocity between clusters of nodes and latent variables
174 is not only justified by the fact that network models are statistically consistent with factor
175 models under certain conditions (Bork et al., 2021) but also supported by empirical research
176 and simulation studies (Golino & Demetriou, 2017; Golino, Shi, et al., 2020).

177 Network psychometrics provides a foundation for Exploratory Graph Analysis (EGA;

178 Golino & Epskamp, 2017) as a factor retention method. Firstly, EGA estimates the partial
179 correlations between the variables by fitting a GGM with the GLASSO regularization and then
180 applies a community detection algorithm for weighted networks to classify items into clusters.
181 Usually, the clustering is achieved by maximizing *modularity*, an index measuring the extent
182 to which nodes within a cluster are more connected than between clusters. Christensen et al.
183 (2020a) performed a simulation comparing eight clustering algorithms and found that the
184 Louvain (Blondel et al., 2008) and Walktrap (Pons & Latapy, 2006) algorithms (both based
185 on modularity) attained the best overall results in identifying the true number of dimensions.

186 Interestingly, the Louvain algorithm can also provide a direct estimate of the number of
187 general factors. However, despite this appealing feature, no EGA method has ever been tested
188 in bi-factor structures.

189 **4 Assessing the number of general factors**

190 If the number of group factors and their configural structure were known, we could roughly
191 estimate the number of general factors by summing or averaging the items corresponding to
192 each scale and then employing any previous factor retention method over the resulting scores.
193 However, this strategy is unrealistic because the group-factor dimensionality and the factor
194 pattern are often unknown or unclear.

195 One alternative is Goldberg's Bass-Ackwards method (Goldberg, 2006), a sequential
196 top-down approach that starts by estimating a unidimensional exploratory factor model and
197 continues extracting and rotating more factors until no variable primarily loads on a factor.
198 Then, the factor scores for each factor solution are estimated, and their correlations are used
199 to build a hierarchical representation of all the factor solutions, with the first-factor solution
200 depicted at the top, followed by the two rotated factors solution, and so on. Then, high
201 correlations between an upper and a lower-order factor indicate the perpetuation of the factor
202 down the hierarchy. In contrast, medium correlations between a certain upper and lower-order

203 factor indicate that the former was split to yield the latter, narrower factor.

204 An inconvenient of the Bass-Ackwards method is that it rests on a top-down approach,
205 assessing first the higher-order factors in the hierarchy. Condon et al. (2020) warned that
206 top-down approaches are at risk of missing important features of the factor structure. For
207 instance, they are unable to identify the presence of gaps in content concerning the higher-
208 order domains and are also susceptible to the jingle-jangle fallacy (e.g., we are at risk of
209 labeling with different names the same trait down the hierarchy (jingle) and using the same
210 label for different traits (jangle)). In contrast, they argue for a bottom-up approach that
211 starts by assessing all the traits or nuances that exhaust a domain, taking into account item
212 complexity and facilitating item revision and content expansion.

213 An example of a bottom-up approach is the one proposed by Golino, Jotheeswaran, et al.
214 (2020). First, the authors estimated the number of group factors using EGA. Secondly, they
215 estimated a loading matrix for the group factors from the fitted network and obliquely rotated
216 the structure employing geomin. Finally, they used the resulting first-order latent factor
217 correlation matrix to perform a second-order EGA, yielding an estimation of the number
218 of general factors. However, this procedure was developed to investigate the relationship
219 between several cognitive and health-related variables in the context of aging research, and no
220 exhaustive simulation was performed to test its accuracy under different scenarios of interest.

221 In this study, we followed a bottom-up method based on the correlation between the factor
222 scores of the group factors, as they are expected to reflect the latent dependencies between
223 the general factors. We would like to remark that we are not the first in suggesting nor using
224 factor scores from lower-order factors to determine the number of general factors (see Friborg
225 et al., 2009 and Milfont & Duckitt, 2004). However, previous proposals were not fully explicit
226 or included steps that did not align with what we understand for best practices (e.g., using
227 composites of items for estimating the factor scores, performing orthogonal rotation, or using
228 K1 to assess the number of general factors). The solution that we propose is straightforward
229 and can be obtained through the following steps: (a) estimate the number of group factors

230 with some factor retention method; (b) perform an oblique exploratory factor analysis of the
231 observed correlation matrix extracting the number of group factors suggested in the previous
232 step; (c) estimate the factor scores with some method that contemplates correlated factors
233 (e.g., Thurstone’s regression method); and (d) estimate the number of general factors on the
234 factor scores using the same factor retention method employed in the first step.

235 **5 Methods**

236 **5.1 Simulation design**

237 Following a similar design to these found in Abad et al. (2017), Garcia-Garzon et al. (2021),
238 and Jimenez et al. (2021), nine variables were manipulated to create realistic full-rank
239 bi-factor structures with one or multiple general factors: (a) number of general factors (N.GF:
240 1, 2, 3); (b) correlation between the general factors (COR.GF: 0, .30); (c) sample size (N:
241 500, 1000, 2000, 5000); (d) number of group factors per general factor (N.GRF: 4, 5, 6); (e)
242 number of variables per group factor (VAR.GRF: 4, 6, 8, 10); (f) factor loadings on the general
243 factors (LOAD.GF: low, medium); (g) factor loadings on the group factors (LOAD.GRF: low,
244 medium); (h) model error or misfit (MF: zero, close); and (i) cross-loadings among the group
245 factors (CROSS.GRF: 0, .15, .30). These variables were crossed to yield a final number of
246 5760 conditions, after removing the incompatible conditions in which the number of general
247 factors was set to one but the correlation between the general factors was not zero.

248 Factor loadings ranged from .30 to .50 for the low condition and from .40 to .60 for
249 the medium condition. The loadings on the general factors were sampled from a uniform
250 distribution, whereas the loadings on the group factors varied by equal increments across
251 their variables (e.g., for the low condition with four items per group factor, the population
252 factor loadings were .30, .37, .43, and .50). To create conditions with cross-loadings, the item
253 with the greatest loading on each group factor had a cross-loading of .15 or .30 in another
254 group factor. We maintained the communality constant by subtracting a small value from

255 the remaining non-zero item loadings to make the conditions with and without cross-loadings
256 comparable (see Abad et al., 2017). To illustrate how the data were simulated under these
257 conditions, Table 1 shows a randomly generated loading pattern matrix corresponding to a
258 bi-factor model before and after introducing the cross-loadings. Bi-factor structures with
259 more than one general factor were created by simply joining these single bi-factor structures.

260 **5.2 Population misfit**

261 In real situations, the population correlation matrix between the variables does not resemble
262 the correlation matrix reproduced by the true model parameters (MacCallum, 2003). In
263 other words, all models are misspecified because of many unmodeled minor factors explaining
264 some common item variance. According to this perspective, the true number of factors
265 underlying a population correlation matrix corresponds to the number of major factors, and
266 the resulting population misfit is interpreted as trivial, nonsubstantive common variance. In
267 our simulations, population misfit was created following the method proposed by Cudeck and
268 Browne (1992). This method generates small random values that are added to the population
269 implied correlation matrix such that fitting a confirmatory factor model with unweighted least
270 squares (ULS) reproduces the intended amount of misfit while preserving a global minimum
271 at the original model parameters, as long as the error is not excessive.

272 We selected the population standardized root mean square residual (SRMR) as the
273 indicator of the amount of global misfit, following Shi et al. (2018) and Ximénez et al. (2022).
274 Shi et al. (2018) investigated the behavior of the population SRMR under different types
275 and degrees of model misspecification to suggest a corrected cut-off for the population SRMR
276 that corresponds to a close-fitting model. They established that a close-fitting model at
277 the population level exists when (1) the largest absolute value of the standardized residual
278 covariance matrix ≤ 0.10 , and (2) $\text{SRMR} \leq 0.05 \times \bar{R}^2$, where \bar{R}^2 is the average communality
279 of the manifest variables in the population. For example, for conditions with medium
280 loadings (.50) on both group and general factors, an exact close fit is achieved if SRMR

281 $= 0.05 \times (0.50^2 + 0.50^2) = 0.025$, and the absolute value of the largest residual is $\leq .10$.

282 The choice of the SRMR was motivated by several reasons. Firstly, the easiness of
283 interpretation of the index. Second, the estimated SRMR is more robust than RMSEA and
284 CFI to different estimation methods, like maximum likelihood and ULS (Xia & Yang, 2019).
285 Finally, the unbiased SRMR is less sensitive than other fit indexes to many of the variables
286 manipulated in the current simulation (i.e., *incidental parameters*; Saris et al., 2009), like the
287 number of items or the number of factors (Fan & Sivo, 2007; Shi et al., 2018; Ximénez et al.,
288 2022). For completeness, we also carried out the simulations without population error to use
289 the results as a baseline for comparison.

290 **5.3 Data generation and analysis**

291 Simulations were run in the R programming language, version 4.2.2 (R Core Team, 2022). A
292 population correlation matrix for each condition was created and stored using the `sim_factor`
293 function from the R package `bifactor`, version 0.1.0 (Jimenez, Abad, Garcia-Garzon, Garrido,
294 et al., 2022). Regarding the conditions involving population error, Cudeck and Browne (1992)
295 warned that their method only ensures a global minimum at the intended discrepancy value
296 when the generated error is small enough. Hence, to confirm that close fit was ascertained
297 in each condition, a confirmatory factor analysis using the true model specification was
298 fitted with ULS, and the resulting SRMR was compared with the intended SRMR at a
299 tolerance of $1e-09$. Similarly, we also checked whether the estimated parameters were equal to
300 the population parameters. The `sim_factor` function was iterated until a positive definite
301 correlation matrix with error was obtained and satisfied the aforementioned requirements.
302 Table A1 in the Appendix displays the average and worst misfit values across every variable
303 level for SRMR, as well as two additional fit indices (CFI and RMSEA), and the maximum
304 absolute residual.

305 Once the population structures were created, we extracted 50 random samples from a
306 multivariate normal distribution for each population correlation matrix using the function

307 `mvrnorm` from the R package `MASS`, version 7.3-57 (Venables & Ripley, 2002). The methods
308 that we tested to identify the number of group factors in these samples were K1, EKC, PA_{PCA} ,
309 PA_{PAF} , and EGA_{LV} . As our simulations included model error and at the same time the group
310 factors were correlated due to the presence of the general factors, we decided to conduct
311 PA_{PCA} and PA_{PAF} with both the mean and the 95th percentile cutoffs. In addition, we decided
312 to test EGA with the Louvain algorithm (EGA_{LV}) because it performs at least as well as the
313 Walktrap algorithm and potentially provides a solution with multilevel clusters (Christensen
314 et al., 2020a). That is, the Louvain algorithm creates clusters of items that, in turn, may
315 be grouped into higher-order clusters. Thereby, the lowest-level cluster that EGA_{LV} provided
316 was used to estimate the number of group factors, while the highest-level cluster, when it
317 existed, was taken to be an estimate of the number of general factors. Another important
318 detail of EGA_{LV} is that it performs an initial check using the Leading Eigenvector community
319 detection algorithm (LE; Newman, 2006) on the raw correlation matrix. LE is a clustering
320 method that also aims to maximize modularity. To achieve this, the LE algorithm creates a
321 *modularity matrix* (i.e., a matrix containing the difference between the observed and random
322 edges' strengths), computes its first eigenvector, and chooses the partition that maximizes
323 the modularity index in terms of this first eigenvector. This maximization is obtained when
324 the positive values of the eigenvectors are classified in one cluster and the negatives ones
325 are classified in the other cluster. According to Christensen et al. (2020a), LE provides an
326 adequate balance between correctly recovering one and more than one factors. As such, if LE
327 delivered one factor, the data was judged to be unidimensional. Contrary, when it estimated
328 more than one factor, the Louvain algorithm was applied instead.

329 We developed two new methods based on factor scores to estimate the number of general
330 factors, following the second-order procedure described before, yielding an hierarchical version
331 of both PA (PA_{PCA-FS}) and EGA (EGA_{LV-FS}). For these methods, we performed two oblique
332 factor analyses with ULS, extracting the number of factors suggested by PA_{PCA} and EGA_{LV} and
333 rotating the solution with direct oblimin. Then, we computed the factor scores of each solution

334 using Thurstone’s regression method. On the one hand, we decided to use factor scores instead
335 of the factor correlations because the latter would require the assumption of a particular
336 distribution for the factors in order to simulate data for parallel analysis. On the other hand,
337 we chose the Thurstone’s scores because they maximize validity (i.e., the correlation between
338 the factor scores and their corresponding factors), so the proportion of indeterminacy in the
339 factor scores is minimized (Grice, 2001). Finally, for EGA_{LV-FS} , we used EGA_{LV} on the factor
340 scores obtained from the first-order solution and extracted the highest-level cluster provided
341 by the Louvain algorithm (using the same LE check for unidimensionality as in the previous
342 step).

343 We used the function `parallel` from the R package `bifactor` to conduct the methods
344 based on parallel analysis. For all the parallel analysis methods, 100 random datasets
345 were created by within-variable permutation of the empirical dataset to obtain the mean
346 and 95th percentile of the eigenvalues under the null model of no latent factors. For the
347 implementation of EGA_{LV} , we used the function `EGA` from the `EGAnet` package, version 1.1.0
348 (Golino & Christensen, 2022). Importantly, the `EGA` function does not provide the complete
349 hierarchical solution but automatically returns the dimensions that correspond to the highest-
350 level cluster of the hierarchy. Hence, when the LE algorithm determined that the data was
351 not unidimensional, we analyzed the estimated network with the `cluster_louvain` function
352 from the R package `igraph`, version 1.3.1 (Csardi & Nepusz, 2006), to obtain the complete
353 multilevel organization as estimated by the Louvain algorithm.

354 Following Garrido et al. (2016) and Golino, Shi, et al. (2020), three indices were calculated
355 to diagnose the accuracy of the methods. The first index is the hit rate (HR) or the proportion
356 of correct dimensionality assessments. While HR reflects each method’s accuracy, it does
357 not provide information about the direction of the errors. We thus computed the mean bias
358 error (MBE), conceptualized as the average difference between the estimated dimensionality
359 and the true dimensionality, with positive and negative values reflecting overextraction and
360 underextraction of the true number of factors, respectively. Additionally, as these errors may

cancel out in specific conditions, we also computed the mean absolute error (MAE), which takes the mean of the absolute error values. Analyses of variance (ANOVA) estimating up to third-order interactions among all the experimental conditions were carried out using the absolute error as the outcome. The partial omega squared (Ω^2) was then used as an effect size to measure each model coefficient’s importance. We decided to report all the main effects and only the interactions whose corresponding Ω^2 values were greater than .14 or close to this threshold for at least one method, following Cohen’s criterion for a large effect (Cohen, 1988).

All the simulated data, analysis code, and research materials are available at <https://osf.io/u7qwj/>.

6 Results

Firstly, we present the marginal accuracies, biases, and absolute errors obtained by each factor retention method with respect to the true number of group factors. Then, we describe the two and third-order interactions that were found for each method. Thirdly, we describe the same results for the recovery of the number of general factors.

Our results suggested that the mean and the 95th percentile cut-points behaved similarly across all the levels of the variables in each parallel analysis method. Hence, for simplicity’s sake, we will only describe the results of PA_{PCA} and PA_{PCA-FS} with the mean value and those of PA_{PAF} with the 95th percentile. This decision was motivated by the fact that the mean value was slightly more accurate than the 95th percentile for PA_{PCA} and PA_{PCA-FS} whereas the 95th percentile was slightly more accurate than the mean value for PA_{PAF} .

6.1 Recovery of the number of group factors

Overall, EGA_{LV} was the method with the highest hit rate in detecting the number of group factors (HR = .86), closely followed by PA_{PCA} (HR = .83), and then by EKC (HR = .70), PA_{PAF} (HR = .64), and K1 (HR = .60; Table 2). If no population model error existed, PA_{PAF}

385 would have been considered the best method, with an almost perfect hit rate of .98. However,
386 its accuracy was severely impacted when considering model error ($HR[MF = \text{close}] = .29$). In
387 a similar vein, EKC and K1 also experimented a strong deterioration under this condition,
388 with absolute drops in accuracy of .45 and .32, respectively. In fact, EKC would have been
389 considered the second best method if no population error was simulated, with a hit rate of
390 .93. On the other hand, the effect of model error on PA_{PCA} was moderate, whereas $EGALV$
391 remained robust to population error.

392 The number of general factors was a critical variable in our results. Under one general
393 factor, the hit rates of $EGALV$ and PA_{PCA} were above .95. Whereas increasing the number
394 of general dimensions from one to three decreased the hit rate of K1 by .29 points, those
395 of $EGALV$ and PA_{PCA} by about .20 points, and that of EKC by .16 points, PA_{PAF} moderately
396 increased its accuracy. However, the accuracy of PA_{PAF} in conditions with three general
397 factors ($HR[N.GF = 3] = .65$) was still inferior to those of $EGALV$ ($HR[N.GF = 3] = .76$)
398 and PA_{PCA} ($HR[N.GF = 3] = .74$). On the other hand, all the factor retention methods were
399 impaired by the presence of correlations between the general factors, with $EGALV$ presenting
400 the highest performance in this situation ($HR[COR.GF = .30] = .84$).

401 However, $EGALV$ did not always perform best. While it attained almost perfect accuracy
402 in simple structures ($HR[CROSS.GRF = 0] = .99$), it showed drops of .10 ($HR = .89$) and .29
403 points ($HR = .70$) when the size of the cross-loadings increased to .15 and .30, respectively.
404 On the contrary, PA_{PCA} was only moderately affected by the presence of high cross-loadings,
405 with the former attaining the best average performance across high cross-loadings conditions
406 ($HR[CROSS.GRF = .30] = .79$). Conversely, PA_{PAF} , K1, and EKC were not affected by item
407 complexity, but their performances were still inferior to those of $EGALV$ and PA_{PCA} in the
408 presence of medium and high cross-loadings.

409 Increasing the number of group factors per general factor negatively affected all the
410 methods. $EGALV$ and PA_{PAF} were only moderately affected, with the former retaining the
411 highest accuracy across all the levels. However, K1, EKC, and PA_{PCA} were more affected by

412 the increase in the number of group factors from four to six, showing declines of .16, .12, and
413 .10 points in accuracy, respectively. On the other hand, increasing the number of variables per
414 group factor also increased the accuracy of all the methods but K1, EKC, and PA_{PAF} . EKC
415 and K1 were the most accurate methods across conditions with four variables per group factor
416 with hit rates of .91 and .90, respectively, but the worst across conditions with eight and ten
417 variables ($HR[VAR.GRF = 10] = .42$ and $HR[VAR.GRF = 10] = .34$, respectively). Conversely,
418 PA_{PCA} benefited by switching from four to six variables per group factor ($HR[VAR.GRF = 4]$
419 $= .60$; $HR[VAR.GRF = 6] = .89$), but further increases in the number of variables per group
420 factor did not produce substantial gains in accuracy². Concerning EGA_{LV} , it obtained the best
421 hit rate in conditions with the maximum number of variables per group factor ($HR[VAR.GRF$
422 $= 10] = .96$).

423 We further identified three results of interest. When switching from medium to low loadings
424 on the group factors, PA_{PCA} , K1, EGA_{LV} , and EKC were negatively impacted, with respective
425 hit rate drops of .17, .16, .13, and .07 points, respectively. Again, EGA_{LV} was the best
426 method across the most unfavorable condition (e.g., $HR[LOAD.GRF = low] = .80$). Secondly,
427 concerning the loadings on the general factors, lower loadings were moderately associated with
428 higher hit rates for PA_{PCA} with an absolute increase of .09 points, but negatively impacted K1
429 and EKC with drops of .16 and .05 points, respectively. EGA_{LV} remained unaffected to the
430 magnitude of the loadings on the general factors, whereas PA_{PAF} was robust to the magnitude
431 of the general and group factor loadings. Lastly, the sample size was positively related to the
432 hit rate of all the factor retention methods, with PA_{PAF} being again the exemption. While
433 PA_{PAF} presented a good average performance across small sample sizes ($HR[N = 500] =$
434 $.80$), it drastically underperformed as the sample size increased (e.g., $HR[N = 5000] = .51$).
435 Interestingly, sample size had very little influence on EGA_{LV} , and for conditions with a sample
436 size of 2000 or greater, PA_{PCA} slightly outperformed EGA_{LV} with a hit rate about .90. K1

²We verified that this lack of improvement for PA_{PCA} was due to the presence of population error. Removing the conditions with population error yielded a clearer increasing monotonic relationship between the hit rate and VAR.GRF.

437 and EKC benefited from increased sample sizes but only achieved an overall hit rate over .80
438 across conditions with a sample of size 5000.

439 The results for the mean bias error (MBE; Table 3) revealed that, following the HR
440 results, EG_{LV} and PA_{PCA} were the least biased methods. EG_{LV} and PA_{PCA} underestimated the
441 number of factors, with overall MBEs of -0.29 and -0.44, respectively. EG_{LV} underextracted
442 the most in conditions involving few variables per group factor ($MBE[VAR.GRF = 4] =$
443 -0.76) and high cross-loadings ($MBE[CROSS.GRF = .30] = -0.75$). The worst performance
444 of PA_{PCA} was observed under weakly defined group factors ($MBE[VAR.GRF = 4] = -1.46$;
445 $MBE[LOAD.GRF = low] = -0.82$) and low sample size ($MBE[N = 500] = -1.14$). Contrary to
446 the underestimation of the previous methods, K1, PA_{PAF} , and EKC overextracted across all
447 the variable levels with the exemption of PA_{PAF} and EKC in conditions with no population
448 error, in which they were unbiased, and EKC in the conditions with the minimum number
449 of variables per group factor. Their overall MBEs were 2.07, 1.58, and 0.63, respectively,
450 with K1 being particularly prone to overextraction in situations involving small sample size
451 ($MBE[N = 500] = 4.84$), large factor structures ($MBE[VAR.GRF = 10] = 4.64$; $MBE[N.GF$
452 $= 3] = 3.45$; $MBE[N.GRF = 6] = 2.96$), and low loadings on both the general and group
453 factors ($MBE[LOAD.GF = low] = 2.95$; $MBE[LOAD.GRF = low] = 2.95$). K1 only showed
454 an acceptable performance for the conditions involving the maximum sample size and the
455 minimum number of variables per group factor. The performance of PA_{PAF} was particularly
456 hindered in large sample size conditions ($MBE[N = 5000] = 3.75$), population structures with
457 population error ($MBE[MF = close] = 3.17$), and correlated general factors ($MBE[COR.GF =$
458 $.30] = 2.51$). Despite PA_{PAF} not being influenced by the number of variables per group factor
459 in terms of accuracy, the MBE indicated that it overextracted more factors the more variables
460 defined a group factor. In the end, PA_{PAF} only showed an acceptable overall performance for
461 population structures without error and across conditions with the minimum sample size.
462 Globally, EKC was less biased than K1 and PA_{PAF} , but it overextracted factors with the
463 maximum number of variables per group factor ($MBE[VAR.GRF = 10] = 1.46$) and when

464 population error was present ($MBE[MF = \text{close}] = 1.23$).

465 Because the estimation biases may cancel out when computing marginal means, we
466 further assessed the precision of the factor retention methods with the MAE (Table A2 in
467 the Appendix). However, the MAE followed a similar pattern to the MBE across all the
468 manipulated levels and will not be further discussed.

469 As the overall performances of K1, EKC, and PA_{PAF} were much worse than those of PA_{PCA}
470 and EGA_{LV} in the presence of population error, in Table 4, we only show the Ω^2 effect sizes
471 obtained for PA_{PCA} and EGA_{LV} from the analysis of variance³. PA_{PCA} was most sensitive
472 to VAR.GRF, a variable also involved in all the large two-way and three-way interactions.
473 These interactions showed that the effect of other variables (LOAD.GF, LOAD.GRF, N, and
474 N.GF) was smaller as the number of variables per group factor increased. Lower loadings
475 on the group factors were very detrimental when the group factors were defined by fewer
476 variables, especially in smaller samples ($\Omega^2[\text{VAR.GRF} \times N \times \text{LOAD.GRF}] = .22$).
477 Similarly, having more general factors was increasingly deleterious when fewer variables
478 loaded on the group factors, particularly when the sample size was smaller (Figure 3(b);
479 $\Omega^2[\text{VAR.GRF} \times N \times N.GF] = .18$). Noteworthy, for samples of size 1000 or larger and at least six
480 indicators per group factor, the negative effect of having lower loadings on the group factors and
481 more general factors was small. Another three-way interaction indicated that PA_{PCA} tended to
482 underperform more with lower loadings on the group factors when fewer variables defined them
483 and when there were more general factors (Figure 4; $\Omega^2[\text{VAR.GRF} \times N.GF \times \text{LOAD.GRF}] =$
484 $.16$). In other words, with an increasing number of general factors, more indicators per group
485 factor might be needed if their quality is low. Finally, an interaction indicated that higher
486 loadings on the general factors were more detrimental when the group factors were defined by
487 only a few items (Figure 5; $\Omega^2[\text{VAR.GRF} \times \text{LOAD.GF}] = .19$). That is, better-defined group
488 factors counterbalanced the effect induced by the presence of stronger general factors (e.g.,
489 higher correlations among the variables that loaded on the same general factor but different

³Readers interested in the most relevant effect sizes found for K1, EKC, and PA_{PAF} can find them in the Table A3 from the Appendix.

490 group factors).

491 Concerning EGA_{LV} , the results of the ANOVA revealed that it was sensitive to the number
492 of variables per group factor, the number of general factors, and the presence of cross-loadings
493 among the group factors. All the effects produced by these variables were smaller on EGA_{LV}
494 than on PA_{PCA} , except those involving cross-loadings. When there were no cross-loadings,
495 EGA_{LV} remained robust to weakly defined group factors (i.e., few variables per group factor with
496 low loadings), and larger factor structures. Small cross-loadings started to become detrimental
497 only in structures with three general factors or low loadings on the group factors if the number
498 of variables per group factor was eight or smaller. However, the effect of high cross-loadings
499 was very detrimental when the group factors had fewer variables in structures with more than
500 one general factor (Figure 6(a); $\Omega^2[\text{VAR.GRF} \times \text{CROSS.GRF} \times \text{N.GF}] = .22$) or with lower
501 loadings on the group factors (Figure 6(b); $\Omega^2[\text{VAR.GRF} \times \text{CROSS.GRF} \times \text{N.GF}] = .13$).
502 Such detrimental effect of cross-loadings, in interaction with the aforementioned variables,
503 was small whenever eight or more variables defined each group factor.

504 **6.2 Recovery of the number of general factors**

505 Despite the good performance of the lowest-level cluster of EGA_{LV} in identifying the number
506 of group factors, it only identified a higher layer of clusters in 42% of the simulated datasets.
507 Even in these cases, it often provided a wrong estimation of the number of general factors,
508 with an overall hit rate of .24. Therefore, we did not seek to analyze this method in further
509 analyses. Similarly, K1, EKC, and PA_{PAF} were inaccurate for detecting the number of group
510 factors in situations of model misfit, so they were not further considered, as explained before.
511 In contrast, the estimation of the number of general factors was extraordinarily accurate
512 using either PA_{PCA-FS} or EGA_{LV-FS} . These methods presented hit rates close to one and mean
513 absolute errors close to zero across all the variable levels (Tables 2 and 4). The minimum
514 marginal hit rates and maximum marginal mean absolute errors for PA_{PCA-FS} happened in the
515 conditions with few variables per group factor (HR = .97, MAE = 0.04, VAR.GRF = 4) and

516 small sample size ($HR = .97$, $MAE = 0.03$, $N = 500$). On the other hand, EGA_{LV-FS} had an
517 almost perfect performance across all the variable levels. Interestingly, none of the estimated
518 Ω^2 effect sizes for either method were high (Table 4). For PA_{PCA-FS} , the maximum Ω^2 value
519 associated with a main effect was 0.03, and for EGA_{LV-FS} , 0.01.

520 7 The HEXACO-100 Inventory

521 The HEXACO-100 Inventory (Lee & Ashton, 2018) is an instrument that was designed to
522 display a robust hierarchical structure of personality traits. It aims to measure 25 personality
523 traits (i.e., group factors) and six domains (i.e., general factors) using 100 items, four items
524 by trait. The domains (G) and traits (S) are listed as follows: Emotionality (G1), Fearful-
525 ness (S1), Anxiety (S2), Dependence (S3), Sentimentality (S4); Extraversion (G2), Social
526 Self-Esteem (S5), Social Boldness (S6), Sociability (S7), Liveliness (S8); Conscientiousness
527 (G3), Organization (S9), Diligence (S10), Perfectionism (S11), Prudence (S12); Openness to
528 Experience (G4), Aesthetic Appreciation (S13), Inquisitiveness (S14), Creativity (S15), Uncon-
529 ventionality (S16); Agreeableness (G5), Forgiveness (S17), Gentleness (S18), Flexibility (S19),
530 Patience (S20); Honesty-Humility (G6), Sincerity (S21); Fairness (S22), Greed-Avoidance
531 (S23), Modesty (S24). The 25th factor is interstitial and corresponds to Altruism. This factor
532 is not embedded in the hierarchical organization of the HEXACO personality theory, so it
533 was not considered in the forthcoming analyses.

534 To investigate this hypothetical structure of 24 group factors and six general factors, we
535 used a sample of 647 undergraduate students enrolled in an Australian university (Anglim
536 et al., 2022; Wood et al., 2022). Dimensionality and statistical analyses in this sample
537 were done in R (R Core Team, 2022) under the 4.2.2 version. The hierarchical exploratory
538 graph analysis (i.e., EGA_{LV} and EGA_{LV-FS}) was performed with the `hierEGA` function from the
539 `EGAnet` package (Golino & Christensen, 2022), version 1.2.4, whereas the hierarchical parallel
540 analysis (i.e., PA_{PCA} and PA_{PCA-FS}) was done with the `parallel` function from the `bifactor`

541 package (Jimenez, Abad, Garcia-Garzon, Garrido, et al., 2022), version 0.1.0.

542 The data and script to run the analysis are available in the online repository <https://osf.io/u7qwj/>. The specific commands for executing the hierarchical methods are as follows:

```
# Load the Student data from the OSF repository:
student <- as.matrix(read.csv("article/analysis/student.csv"))
library(EGAnet) # Load the library to perform hierarchical EGA
hierega <- hierEGA(student, scores = "factor")
library(bifactor) # Load the library to perform hierarchical PA
hierPA <- parallel(student, hierarchical = TRUE, PA = "PCA", mean = TRUE)
```

544 Hierarchical exploratory graph analysis yielded 24 group factors and five general factors,
545 whereas hierarchical parallel analysis resulted in 13 group factors and five general factors
546 using both the mean and the 95th percentile. Such a large discrepancy between EGA_{LV} and
547 PA_{PCA} in the number of group factors may be due to a number of reasons that were not
548 considered in the current simulation: first, in our simulation design we considered structures
549 up to three general factors whereas in this empirical example there could be even six according
550 to theory. Second, while the simulated data were continuous and normally distributed, the
551 HEXACO-100 data is ordinal in nature, which may bear a greater impact on PA_{PCA} than
552 EGA_{LV}. Third, considering the size of the factor structure, the sample size and the number
553 indicators per group factor were low. These conditions were the ones that most impacted the
554 performance of PA_{PCA} in the simulation, producing underfactoring. As shown in the panel
555 b of Figure 3, the combination of four indicators per group factor and a sample size of 500,
556 which are the characteristics that resemble most the HEXACO-100 data, already produced a
557 mean absolute error around five in structures with three general factors. Thus, looking at
558 this pattern, it would not be surprising that PA_{PCA} errs by more than ten group factors in
559 structures with five or six general factors. A last reason that may impact the performance of
560 PA_{PCA} is the presence of causal relations between the group factors (Franco et al., 2022).

561 For these reasons, and because the group-factor dimensionality obtained from EGA_{LV}
562 matched the HEXACO-100 theory, we fitted a bi-factor model with 24 group factors and five
563 general factors using the GSLiD algorithm (Jimenez et al., 2021). GSLiD is a recent method
564 for conducting exploratory bi-factor analysis with multiple general factors that consists of
565 iteratively refining a partially specified target until no further refinement is required. Moreover,
566 GSLiD can penalize the correlations between the group factors and estimate a model with
567 only correlated general factors, so that the item variance explained by the general and group
568 factors can be properly disentangled, providing more interpretable results than completely
569 oblique and orthogonal solutions.

570 Tables A4 and A5 from the Appendix display the estimated loading matrix and factor
571 correlations between the general factors, respectively. We considered item loadings higher
572 than .25 and factor correlations higher than .20 to be substantive. As expected by the
573 HEXACO-100 theory, the items corresponding to Emotionality, Extraversion, Conscientious-
574 ness, and Openness to Experience loaded on distinctive general factors (except item 35 for
575 Conscientiousness and item 62 for Openness to Experience), whereas the items pertaining to
576 Agreeableness and Honesty-Humility loaded on a single general factor. On the other hand, 81
577 items (84%) loaded on their expected group factors. The indicators that did not conform
578 to the theoretical pattern are listed next: item 2 (Fearfulness), items 17, 18, 19, and 20
579 (Social Self-Esteem), item 29 (Liveliness), items 38 and 40 (Diligence), items 46, 47, and 48
580 (Prudence), items 61, 62, and 64 (Unconventionality), and item 69 (Gentleness). Finally, the
581 absolute values of the correlations between the general factors were low-to-moderate, ranging
582 from .25 to .34.

583 In conclusion, the underlying structure of the HEXACO-100 (excluding the Altruism
584 facet) is compatible with a theoretical model of 24 group factors and 5 general factors (Figure
585 7), with low-to-moderate loadings and factor correlations. Notwithstanding, we would like
586 to remark that this empirical example was developed for illustrative purposes and that a
587 more exhaustive analysis of the HEXACO-100 data is required to ascertain its underlying

588 structure. For instance, a complete workflow would include checking for item redundancies
589 (Christensen et al., 2020b), assessing the stability of the hierarchical solution by means of
590 techniques such as bootstrapping (Christensen & Golino, 2019), and interpreting the clusters.
591 This is a complex work that is worth an independent study.

592 **8 Discussion**

593 Dimensionality assessment is one of the most important decisions that researchers face in
594 test development and validation. It is well known that wrong dimensionality assessments
595 can severely bias item parameter estimates and undermine the validity of test scores (Fava
596 & Velicer, 1992, 1996). Moreover, bi-factor analysis applications would be better justified
597 when empirical evidence supports the dimensionality of the data at lower and higher levels of
598 organization, revealing information that can be used for the posterior model specification and
599 statistical analysis.

600 Unfortunately, theory is not always enough to ascertain the number of factors underlying a
601 dataset, and factor retention methods become necessary. Today, there is little information on
602 how to assess the dimensionality of structures with factors subsumed into broader, higher-order
603 factors, like those encountered in intelligence, personality, and psychopathology. While many
604 bi-factor methods with either one or multiple general factors have been developed recently to
605 estimate large and complex structures that account for the presence of general factors (Abad
606 et al., 2017; Cai, 2010; Garcia-Garzon et al., 2019, 2020; Jennrich & Bentler, 2011; Jimenez
607 et al., 2021; Nájera et al., 2021), we still lack evidence-based recommendations on how to
608 assess the dimensionality of this kind of structures. This is a crucial limitation because all of
609 these methods assume that the number of group and general factors are known.

610 Hence, in this study we investigated for the first time the performance of some classical
611 and recent factor retention methods to uncover the number of group and general factors in
612 bi-factor structures up to three general factors. Overall, we found that EGA_{LV} was the most

613 accurate, precise, and robust method for estimating the number of group factors, followed by
614 PA_{PCA} , which was sensitive to various conditions, namely the number of variables per group
615 factor, sample size, and loadings on the group and general factors.

616 These results align with previous research showing that PA_{PCA} underestimates the number
617 of factors in conditions involving small samples and large factor structures with weakly
618 defined group factors (Braeken & Assen, 2017; Garrido et al., 2013; Yang & Xia, 2015).
619 Notwithstanding, the performance of PA_{PCA} was very high whenever the sample size was
620 above 1000, and the number of variables per group factor was six or higher. Our findings also
621 agree with previous results in which EGA was highly robust to unfavorable conditions, albeit
622 using the Walktrap clustering algorithm instead of Louvain (Cosemans et al., 2021; Golino &
623 Epskamp, 2017; Golino, Shi, et al., 2020). The other tested factor retention methods, K1,
624 EKC, and PA_{PAF} , did not perform well in estimating the number of group factors when the
625 population structures contained misfit and were not further examined.

626 Interestingly, sample size and model misfit had little influence on EGA_{LV} . A possible
627 explanation for the latter finding is that the GLASSO penalization shrinks towards zero small
628 partial correlations that appear due to trivial common variance attributable to population
629 error. However, the performance of EGA_{LV} was not perfect. It was sensitive to high cross-
630 loadings, particularly in factor structures with more than one general factor and weakly
631 defined group factors. This sensitivity of EGA_{LV} to high cross-loadings could be due to the
632 fact that the Louvain algorithm does not allow overlapping clusters (Blanken et al., 2018;
633 Christensen et al., 2020a). In other words, items cannot be simultaneously classified in more
634 than one cluster, which increases the probability of incorrect placements if high cross-loadings
635 exist.

636 Within the parallel analysis methods, many researchers have suggested that PA_{PAF} is
637 more suitable than PA_{PCA} for correlated psychological data, both theoretically and empirically
638 (Crawford et al., 2010; Green et al., 2012; Keith et al., 2016). Particularly, Crawford et
639 al. (2010) found that PA_{PAF} performed better than PA_{PCA} under multiple correlated factors,

640 second-order general factors, and bi-factor models. However, they did not consider the role of
641 population error in their simulations. As revealed in our results and in other studies such
642 as Lim and Janhg (2019) and Xia (2021), the accuracy of PA_{PAF} greatly diminishes in the
643 presence of trivial population misfit and only outperforms other methods if, and only if, no
644 population error exists. Unfortunately, some sort of population misfit is always expected to
645 exist in applied settings. Moreover, PA_{PAF} tended to overextract factors with higher sample
646 sizes and an increasing number of variables per group factor. Therefore, we consider that
647 PA_{PAF} is inappropriate for evaluating the dimensionality of bi-factor structures with one or
648 multiple general factors. Contrary, PA_{PCA} was only moderately affected by the presence of
649 close misfit, a result that is also consistent with previous research (Lim & Jahng, 2019; Xia,
650 2021). On the other hand, using either the mean value or the 95th percentile as the cut-off
651 for computing the reference eigenvalues did not result in a practical difference for PA_{PCA} .

652 Overall, although EKC was better than K1, it showed a worse performance than EGA_{LV}
653 and PA_{PCA} to most of the experimental conditions (Table A3, Appendix). This result was
654 explained by its high sensibility to population error and a tendency to overextract factors the
655 more variables defined the group factors. This pattern was also observed for K1, resulting in
656 even lower hit rates and biased estimates. Thus, these results agree with several decades of
657 simulation research in that K1 should never be used for dimensionality assessment, especially
658 in large factor structures like the ones often encountered in bi-factor applications.

659 Regarding the estimation of the general factors, we found that when EGA_{LV} estimated
660 more than one layer of clusters, the number of factors suggested by the highest-level cluster
661 was mostly inaccurate. On the contrary, EGA_{LV-FS} and PA_{PCA-FS} had an almost perfect accuracy
662 across all the conditions, especially the former. More concretely, EGA_{LV-FS} produced an equal
663 or higher performance than PA_{PCA-FS} and was highly robust to all the experimental conditions.

664 Globally, these results suggest that the number of general factors could be estimated
665 accurately even when EGA_{LV} and PA_{PCA} failed to determine the correct number of group
666 factors. Notwithstanding, despite these encouraging results, a note of caution should be

667 raised: we do not recommend applying these hierarchical methods blindly. These methods
668 should only be considered when the correlations between the factor scores are not trivially
669 small. In other words, we recommend inspecting the first-order factor correlation matrix
670 before interpreting the estimates provided by $E_{GA_{LV-FS}}$ and PA_{PCA-FS} . Otherwise, we would be
671 at risk of inferring the presence of general factors when there is no more variance to explain
672 beyond the one accounted for the first-order factors.

673 To illustrate how the proposed hierarchical dimensionality analyses can be done in R
674 software, we analyzed a real dataset concerning the personality traits of the HEXACO-100
675 Inventory, which is intended to measure 24 hypothetical facets (measured by four items each)
676 embedded within six general domains. Whereas PA_{PCA} yielded a too conservative estimation
677 of the number of group factors (13), $E_{GA_{LV}}$ estimated 24, as expected by the theory. The
678 defective performance of PA_{PCA} can be explained by the low sample size ($N = 647$) and few
679 indicators per group factor of the HEXACO-100, conditions in which PA_{PCA} was more prone
680 to underfactor in the simulation. Contrary, both PA_{PCA-FS} and $E_{GA_{LV-FS}}$ suggested five general
681 factors. To investigate the factor structure of the HEXACO-100, we conducted an exploratory
682 bi-factor analysis with 24 group factors and five general factors using the GSLiD algorithm
683 (Jimenez et al., 2021). As a result, the estimated loadings resembled most of the HEXACO-100
684 theory. Interestingly, the items pertaining to the Agreeableness and Honesty-Humility scales
685 merged in a single general domain, whereas most of the group factors were recovered (e.g.,
686 21 of the 24 group factors were defined by at least two of their theoretical indicators).

687 An advantage of our hierarchical proposals over Goldberg’s Bass-Ackwards method is
688 that they are based on a bottom-up approach. We first focus on estimating the number of
689 lower-order factors and then proceed with the higher-order ones. This way, we are able to
690 identify the nuances that make up the more general traits, encouraging the analysis of item
691 content and domain’s breadth (Condon et al., 2020; Möttus et al., 2020). We also remark that
692 $E_{GA_{LV-FS}}$ is somewhat similar to the second-order method proposed by Golino, Jotheeswaran,
693 et al. (2020). The main differences between our and their approach are that we used the

694 lowest-level cluster provided by the Louvain algorithm instead of Walktrap and analyzed the
695 correlation matrix between the factor scores instead of the correlation matrix between the
696 rotated factors, which does not require computing the factor scores. Future simulation studies
697 may consider including the method of Golino, Jotheeswaran, et al. (2020) to check whether it
698 performs as well as EGA_{LV-FS} .

699 This simulation study tried to emulate real data with conditions involving population
700 misfit and cross-loadings, but it has some limitations: first, we only generated continuous
701 data from multivariate normal distributions. With categorical data, polychoric correlation
702 matrices, and skewed distributions, the performance of all the methods should deteriorate,
703 and the extent to which this would happen is unknown. If this is the case, it would also be
704 interesting to compare alternative factor or network scoring methods to establish which are
705 optimal for the recovery of the number of general factors. Second, we only generated factor
706 structures up to three general factors, whereas some cases of psychological data may contain
707 more. This limitation was due to the fact that controlling population misfit in conditions
708 involving more than three general factors is a difficult task, as larger factor structures produce
709 correlation matrices closer to nonpositiveness. Forthcoming work will be needed to solve these
710 technical issues inherent to bi-factor structures with multiple general factors. Notwithstanding,
711 the current simulation is the first one that systematically investigates the dimensionality
712 assessment of factor structures with a varying number of general factors, and it is a good first
713 step toward developing tools for factor retention in fields like intelligence, personality, and
714 psychopathology, where the statistical models usually display a hierarchical configuration.

715 Although the specific factor structures simulated in this study are bi-factor, it is important
716 to note that second-order structures can be interpreted as bi-factor structures with propor-
717 tionality constraints between the general and group factors (Jimenez et al., 2021). In other
718 words, second and higher-order structures are constrained versions of bi-factor structures
719 and, as such, our simulation setup provides results that are generalizable to a larger range
720 of hierarchical structures. Hence, we think that the hierarchical factor retention methods

721 developed here will help to disentangle the different levels of organization of complex data in
722 the broad field of individual differences regardless of the specific factor model (i.e., bi-factor
723 or higher-order). These factor analytic models require a decision regarding the number of
724 factors to extract, we also believe that these hierarchical methods can help to justify or guide
725 model specification in applied research.

726 In conclusion, we aimed to provide applied researchers with accurate methods that can
727 help them to uncover hierarchical structures in their data, and our results suggest that parallel
728 analysis with principal component analysis and exploratory graph analysis with the Louvain
729 algorithm, when applied to items and then to the first-order factor scores, offer a good
730 recovery of the dimensionality of the hierarchical structure. As different variables impact these
731 two methods, researchers may use them in tandem or according to the known or plausible
732 characteristics of their data. Noteworthy, EGA_{LV} not only was the best method in terms
733 of accuracy, precision, and robustness for the conditions most likely to be encountered in
734 practice, but also provides a classification of items into factors, offering a richer dimensionality
735 assessment that can be easily compared with the theoretical expectations of the factor
736 structure. Furthermore, the stability of the EGA_{LV} and EGA_{LV-FS} latent solutions can be
737 readily ascertained using bootstrap procedures currently available (Christensen & Golino,
738 2021). Thus, we highlight the particular usefulness of EGA_{LV} and EGA_{LV-FS} for assessing
739 bi-factor structures with one or multiple general factors. Finally, much more attention should
740 be considered to the number of group factors, as the second-order methods depend on this
741 quantity, and they are harder to estimate than the number of general factors.

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Table A1. Marginal fit indices for each variable level. The mean value is displayed in bold, and the single worst fit value is displayed in parentheses.

Variable	SRMR	RMSEA	CFI	Absolute residuals
<u>N.GF</u>				
1	.0209 (.0263)	.0266 (.0298)	.9933 (.9902)	.0711 (.0998)
2	.0209 (.0266)	.0217 (.0288)	.9869 (.9801)	.0803 (.0997)
3	.0209 (.0263)	.0214 (.0274)	.9808 (.9702)	.0789 (.0999)
<u>COR.GF</u>				
0	.0209 (.0266)	.0219 (.0298)	.9865 (.9702)	.0777 (.0999)
.30	.0209 (.0264)	.0216 (.0281)	.9846 (.9732)	.0782 (.0995)
<u>VAR.GRF</u>				
4	.0209 (.0266)	.0224 (.0298)	.9851 (.9702)	.0739 (.0988)
6	.0209 (.0264)	.0218 (.0288)	.9857 (.9716)	.0774 (.0999)
8	.0209 (.0261)	.0215 (.0273)	.9860 (.9730)	.0793 (.0993)
10	.0209 (.0259)	.0214 (.0270)	.9862 (.9727)	.0809 (.0998)
<u>N.GRF</u>				
4	.0209 (.0266)	.0220 (.0298)	.9868 (.9754)	.0758 (.0997)
5	.0209 (.0263)	.0217 (.0291)	.9857 (.9729)	.0783 (.0994)
6	.0209 (.0263)	.0216 (.0293)	.9847 (.9702)	.0795 (.0999)
<u>CROSS.GRF</u>				
0	.0209 (.0262)	.0217 (.0298)	.9857 (.9702)	.0771 (.0999)
.15	.0209 (.0264)	.0218 (.0294)	.9859 (.9717)	.0778 (.0995)
.30	.0209 (.0266)	.0218 (.0295)	.9856 (.9713)	.0787 (.0998)
<u>LOAD.GRF</u>				
low	.0187 (.0224)	.0194 (.0248)	.9874 (.9770)	.0707 (.0988)
medium	.0231 (.0266)	.0241 (.0298)	.9841 (.9702)	.0851 (.0999)
<u>LOAD.GF</u>				
low	.0186 (.0220)	.0194 (.0252)	.9840 (.9702)	.0704 (.0992)
medium	.0231 (.0266)	.0241 (.0298)	.9875 (.9780)	.0854 (.0999)
Total	.0209 (.0266)	.0218 (.0298)	.9857 (.9702)	.0779 (.0999)

Note. N.GF = number of general factors; COR.GF = correlation between general factors; VAR.GRF = number of indicators per group factor; N.GRF = number of group factors per general factor; CROSS.GRF = cross-loadings in the group factors; LOAD.GRF = loadings on the group factors; LOAD.GF = loadings on the general factors.

Table A2. Mean absolute error (MAE) across each variable level for each factor retention method.

Variable	Group factors							General factors			
	Kaiser		PA _{PAF}		PA _{PCA}		EGALV	PA _{PCA-FS}		EGALV	EGALV-FS
	K1	EKC	mean	95 th	mean	95 th		mean	95 th		
<u>MF</u>											
zero	1.57	0.09	0.02	0.02	0.48	0.57	0.31	0.01	0.02	2.83	0.00
close	2.59	1.28	3.84	3.19	0.50	0.59	0.31	0.01	0.02	2.89	0.00
<u>N</u>											
500	4.87	0.83	0.44	0.27	1.14	1.37	0.31	0.04	0.07	3.42	0.00
1000	2.27	0.90	1.00	0.68	0.47	0.56	0.32	0.01	0.01	2.94	0.00
2000	0.86	0.68	2.12	1.72	0.23	0.26	0.31	0.00	0.00	2.64	0.00
5000	0.33	0.33	4.17	3.76	0.12	0.13	0.30	0.00	0.00	2.42	0.01
<u>N.GF</u>											
1	0.42	0.31	2.43	1.99	0.07	0.10	0.02	0.00	0.00	1.07	0.00
2	1.52	0.59	1.73	1.42	0.34	0.41	0.15	0.01	0.01	2.78	0.00
3	3.48	0.96	1.88	1.60	0.85	0.99	0.61	0.02	0.04	3.82	0.01
<u>COR.GF</u>											
0	1.62	0.40	1.24	0.99	0.40	0.48	0.28	0.01	0.02	2.49	0.00
.30	2.77	1.12	2.97	2.54	0.62	0.73	0.35	0.02	0.03	3.40	0.00
<u>VAR.GRF</u>											
4	0.15	0.14	0.91	0.67	1.46	1.73	0.77	0.04	0.08	2.17	0.01
6	0.99	0.32	1.66	1.34	0.30	0.37	0.29	0.00	0.00	3.04	0.00
8	2.55	0.83	2.31	1.94	0.11	0.13	0.11	0.00	0.00	3.15	0.00
10	4.64	1.46	2.85	2.47	0.09	0.09	0.05	0.00	0.00	3.07	0.00
<u>N.GRF</u>											
4	1.24	0.46	1.60	1.29	0.26	0.33	0.18	0.01	0.02	2.27	0.01
5	2.03	0.68	1.93	1.60	0.47	0.56	0.31	0.01	0.02	2.79	0.00
6	2.98	0.92	2.27	1.93	0.73	0.86	0.44	0.01	0.02	3.51	0.00
<u>CROSS.GRF</u>											
0	2.06	0.69	2.00	1.67	0.38	0.47	0.01	0.01	0.02	2.88	0.00
.15	2.06	0.69	1.96	1.64	0.49	0.59	0.15	0.01	0.03	2.93	0.00
.30	2.12	0.68	1.83	1.51	0.60	0.69	0.76	0.01	0.02	2.76	0.01
<u>LOAD.GRF</u>											
low	2.98	0.83	1.93	1.57	0.85	1.01	0.50	0.02	0.04	2.70	0.01
medium	1.19	0.54	1.94	1.64	0.13	0.15	0.11	0.00	0.00	3.01	0.00
<u>LOAD.GF</u>											
low	2.97	0.78	1.69	1.35	0.28	0.35	0.29	0.00	0.00	3.07	0.00
medium	1.20	0.59	2.18	1.86	0.70	0.81	0.32	0.02	0.04	2.64	0.01
<u>Total</u>	2.08	0.69	1.93	1.61	0.49	0.58	0.31	0.01	0.02	2.86	0.00

Note. K1 = Kaiser eigenvalue greater-than-one criterion; EKC = Empirical Kaiser Criterion; PA_{PAF} = Parallel analysis with principal axis factoring; PA_{PCA} = Parallel analysis with principal components; PA_{PCA-FS} = Parallel analysis with principal components on the first-order factor scores; EGA = Exploratory Graph Analysis; EGALV = EGA with Louvain; EGALV-FS = EGA with Louvain on the first-order factor scores; MF = population misfit; N = sample size; N.GF = number of general factors; COR.GF = correlation between general factors; VAR.GRF = number of indicators per group factor; N.GRF = number of group factors per general factor; CROSS.GRF = cross-loadings in the group factors; LOAD.GRF = loadings on the group factors; LOAD.GF = loadings on the general factors.

Table A3. Partial omega squared coefficients (Ω^2) from the ANOVAs on the absolute error for the recovery of the group factors for all the nine main effects, and for the remaining coefficients whose $\Omega^2 \geq .14$ in at least one factor retention method.

Variable	Kaiser		PAPAF		PAPCA		EGALV
	K1	EKC	mean	95th	mean	95th	
Main effects							
VAR.GRF	0.84	0.36	0.30	0.30	0.57	0.62	0.22
N	0.84	0.09	0.62	0.64	0.39	0.46	0.00
N.GF	0.72	0.12	0.05	0.04	0.29	0.31	0.18
LOAD.GF	0.58	0.02	0.05	0.06	0.15	0.16	0.00
LOAD.GRF	0.58	0.04	0.00	0.00	0.35	0.40	0.12
N.GRF	0.47	0.07	0.06	0.06	0.13	0.15	0.04
MF	0.31	0.44	0.75	0.71	0.00	0.00	0.00
COR.GF	0.09	0.17	0.47	0.45	0.00	0.00	0.00
CROSS.GRF	0.00	0.00	0.00	0.00	0.03	0.03	0.28
Two-way interactions							
VAR.GRF \times N	0.75	0.05	0.36	0.36	0.44	0.48	0.01
N \times N.GF	0.63	0.01	0.07	0.05	0.20	0.23	0.00
VAR.GRF \times N.GF	0.60	0.03	0.06	0.05	0.28	0.30	0.14
N \times LOAD.GF	0.44	0.04	0.03	0.03	0.06	0.07	0.00
VAR.GRF \times LOAD.GRF	0.42	0.01	0.00	0.00	0.45	0.48	0.09
VAR.GRF \times LOAD.GF	0.42	0.00	0.00	0.00	0.19	0.19	0.00
N \times LOAD.GRF	0.41	0.03	0.00	0.00	0.26	0.30	0.00
VAR.GRF \times N.GRF	0.34	0.02	0.00	0.00	0.11	0.12	0.02
N \times N.GRF	0.32	0.00	0.03	0.04	0.9	0.11	0.00
N.GF \times LOAD.GRF	0.30	0.01	0.04	0.03	0.16	0.17	0.08
N.GF \times LOAD.GF	0.30	0.00	0.02	0.01	0.05	0.05	0.00
VAR.GRF \times MF	0.20	0.35	0.31	0.32	0.01	0.01	0.00
N.GF \times N.GRF	0.18	0.00	0.02	0.01	0.06	0.06	0.02
LOAD.GF \times LOAD.GRF	0.14	0.00	0.00	0.00	0.09	0.09	0.00
N \times MF	0.02	0.06	0.62	0.64	0.00	0.00	0.00
MF \times COR.GF	0.10	0.17	0.47	0.45	0.00	0.00	0.00
N \times COR.GF	0.00	0.01	0.36	0.39	0.00	0.00	0.00
VAR.GRF \times COR.GF	0.04	0.10	0.13	0.13	0.00	0.00	0.00
VAR.GRF \times CROSS.GRF	0.00	0.00	0.00	0.00	0.05	0.05	0.33
N.GF \times CROSS.GRF	0.00	0.00	0.00	0.00	0.01	0.00	0.20
Three-way interactions							
VAR.GRF \times N \times N.GF	0.47	0.04	0.03	0.02	0.18	0.19	0.01
VAR.GRF \times N \times LOAD.GF	0.22	0.05	0.00	0.00	0.04	0.04	0.00
VAR.GRF \times N \times LOAD.GRF	0.20	0.07	0.00	0.00	0.21	0.23	0.00
VAR.GRF \times N \times N.GRF	0.18	0.01	0.01	0.01	0.07	0.07	0.00
VAR.GRF \times N.GF \times LOAD.GRF	0.16	0.00	0.01	0.01	0.17	0.16	0.05
N \times N.GF \times LOAD.GF	0.16	0.02	0.00	0.00	0.02	0.02	0.00
VAR.GRF \times N.GF \times LOAD.GF	0.15	0.00	0.00	0.00	0.04	0.04	0.00
N \times N.GF \times LOAD.GRF	0.13	0.01	0.00	0.00	0.11	0.11	0.00
N \times MF \times COR.GF	0.00	0.01	0.36	0.39	0.00	0.00	0.00
VAR.GRF \times N \times MF	0.02	0.03	0.34	0.34	0.00	0.00	0.00
VAR.GRF \times N \times COR.GF	0.00	0.00	0.19	0.20	0.00	0.00	0.00
VAR.GRF \times MF \times COR.GF	0.04	0.10	0.13	0.13	0.00	0.00	0.00
VAR.GRF \times CROSS.GRF \times N.GF	0.00	0.00	0.00	0.00	0.01	0.01	0.22
VAR.GRF \times CROSS.GRF \times LOAD.GRF	0.00	0.00	0.00	0.00	0.01	0.01	0.13

Note. K1 = Kaiser eigenvalue greater-than-one criterion; EKC = Empirical Kaiser Criterion; PAPAF = Parallel analysis with principal axis factoring; PAPCA = Parallel analysis with principal components; EGALV = Exploratory graph analysis with Louvain; MF = population misfit; N.GF = number of general factors; COR.GF = Correlation between general factors; N = sample size; VAR.GRF = Number of indicators per group factor; N.GRF = number of group factors per general factor; CROSS.GRF = cross-loadings in the group factors; LOAD.GF = loadings on the general factors; LOAD.GRF = loadings on the group factors.

Table A4. Estimated loadings for the HEXACO-100 with 24 group factors (excluding the Altruism facet). Loadings with absolute values greater than .25 are shown in bold and underlined. Each facet encompasses 4 items delineated between horizontal bars.

Item	General factors					Group factors																							
	G1	G2	G3	G4	G5	S1	S2	S3	S4	S5	S6	S7	S8	S9	S10	S11	S12	S13	S14	S15	S16	S17	S18	S19	S20	S21	S22	S23	S24
1	<u>0.56</u>	-0.03	0.01	-0.01	0.03	<u>0.48</u>	-0.01	-0.01	-0.06	0.01	-0.04	0.03	0.07	-0.03	0.04	0.02	0.09	0.01	0.03	-0.07	0.07	0.00	0.01	0.05	0.02	0.04	-0.07	0.07	0.07
2	<u>-0.66</u>	0.00	-0.05	-0.10	0.03	-0.10	0.07	0.05	0.04	-0.03	0.24	-0.07	-0.05	0.04	-0.02	-0.07	0.02	0.01	0.08	0.05	0.24	-0.03	-0.01	0.09	0.01	0.00	-0.06	0.04	0.03
3	<u>-0.32</u>	-0.03	0.18	-0.06	-0.04	<u>-0.65</u>	0.06	-0.02	0.03	-0.01	0.08	0.09	0.02	0.02	0.14	0.07	0.02	0.05	0.13	-0.03	0.08	0.01	0.03	0.03	-0.04	0.08	0.06	0.00	-0.02
4	<u>0.51</u>	0.04	0.02	0.04	0.02	<u>0.30</u>	0.04	-0.09	-0.04	-0.06	-0.06	-0.02	0.04	0.10	0.00	0.00	-0.09	0.00	-0.03	-0.05	0.03	-0.03	0.04	0.00	-0.08	0.01	-0.07	0.04	<u>0.25</u>
5	<u>-0.31</u>	<u>0.26</u>	-0.01	0.05	0.01	0.00	<u>-0.49</u>	0.01	-0.02	-0.05	0.00	-0.02	0.13	0.06	-0.01	-0.01	0.12	-0.15	-0.01	-0.05	0.02	0.10	-0.05	-0.05	0.14	-0.08	-0.08	-0.02	-0.05
6	<u>0.64</u>	-0.17	-0.03	-0.01	0.11	-0.07	<u>0.41</u>	-0.07	-0.04	0.05	-0.03	0.05	-0.06	0.00	0.05	0.05	0.09	-0.10	0.01	0.07	0.03	0.04	-0.05	0.02	0.07	0.05	0.00	0.01	-0.02
7	<u>-0.61</u>	0.15	0.13	0.00	-0.10	0.16	<u>-0.27</u>	0.00	-0.05	-0.01	0.01	-0.01	0.08	0.03	-0.02	0.01	0.01	0.03	0.04	-0.06	0.05	0.02	-0.02	0.04	0.04	0.00	-0.03	0.03	0.04
8	<u>0.63</u>	-0.09	-0.06	0.02	0.09	0.04	<u>0.39</u>	0.04	0.04	-0.07	-0.06	0.01	0.02	0.01	0.01	0.03	0.11	0.00	0.03	0.02	0.03	-0.03	0.06	0.02	0.01	-0.03	-0.03	0.00	-0.03
9	<u>0.46</u>	0.10	0.02	0.10	0.09	-0.01	0.00	<u>0.49</u>	0.14	0.07	0.01	0.14	-0.03	0.00	0.05	0.00	0.05	0.07	0.05	0.02	-0.07	0.00	0.00	0.00	0.08	0.12	-0.08	0.00	0.15
10	<u>-0.30</u>	<u>-0.39</u>	-0.02	0.12	-0.08	-0.01	-0.03	<u>-0.61</u>	-0.05	0.04	-0.05	-0.04	-0.02	0.03	0.01	0.03	0.08	0.12	0.07	0.02	0.09	-0.02	0.10	-0.01	0.05	-0.01	-0.04	0.03	-0.04
11	<u>-0.47</u>	-0.03	-0.02	-0.04	-0.09	0.04	0.02	<u>-0.35</u>	0.02	-0.11	0.07	-0.07	0.12	0.05	-0.04	0.09	0.00	-0.06	0.05	-0.05	0.23	-0.10	0.02	-0.10	0.04	-0.11	0.06	0.05	-0.05
12	<u>0.44</u>	<u>0.26</u>	0.04	-0.01	0.03	0.01	-0.04	<u>0.70</u>	0.04	-0.06	0.03	0.09	0.05	0.01	-0.02	0.09	-0.02	0.03	-0.04	0.08	-0.03	0.01	0.01	-0.02	-0.06	-0.01	0.04	0.01	-0.03
13	<u>0.46</u>	0.07	-0.02	-0.07	-0.24	-0.09	0.06	0.02	<u>0.50</u>	-0.01	0.10	-0.09	-0.04	0.01	-0.01	0.10	-0.08	0.06	0.02	0.10	0.08	0.01	0.05	0.05	0.08	0.01	0.01	-0.05	-0.04
14	<u>-0.56</u>	-0.17	0.04	0.03	0.15	0.05	0.03	-0.13	<u>-0.37</u>	0.02	0.04	-0.08	-0.08	-0.02	-0.01	0.09	0.03	0.01	0.06	0.00	<u>0.42</u>	0.00	-0.04	-0.01	0.08	0.03	0.05	-0.05	0.03
15	<u>0.50</u>	0.07	0.03	0.01	-0.15	-0.01	-0.01	0.13	<u>0.50</u>	0.06	-0.03	0.02	0.04	0.05	0.07	0.01	0.02	0.07	0.00	0.02	-0.10	0.06	0.07	0.05	-0.03	0.01	0.02	0.01	-0.01
16	<u>0.50</u>	0.08	-0.07	0.01	-0.02	0.03	0.02	0.22	<u>0.32</u>	-0.03	-0.01	0.09	0.04	-0.01	0.07	0.03	0.00	0.07	-0.01	0.09	-0.01	-0.05	0.08	-0.02	0.08	-0.09	-0.07	0.03	-0.07

Note. G1 = Emotionality; G2 = Extraversion; G3 = Conscientiousness; G4 = Openness to Experience; G5 = Agreeableness / Honesty-Humility; S1 = Fearfulness; S2 = Anxiety; S3 = Dependence; S4 = Sentimentality; S5 = Social Self-Esteem; S6 = Social Boldness; S7 = Sociability; S8 = Liveliness; S9 = Organization; S10 = Diligence; S11 = Perfectionism; S12 = Prudence; S13 = Aesthetic Appreciation; S14 = Inquisitiveness; S15 = Creativity; S16 = Unconventionality; S17 = Forgiveness; S18 = Gentleness; S19 = Flexibility; S20 = Patience; S21 = Sincerity; S22 = Fairness; S23 = Greed-Avoidance; S24 = Modesty.

Table A4 (Continuation).

Item	General factors					Group factors																							
	G1	G2	G3	G4	G5	S1	S2	S3	S4	S5	S6	S7	S8	S9	S10	S11	S12	S13	S14	S15	S16	S17	S18	S19	S20	S21	S22	S23	S24
17	-0.13	<u>0.60</u>	-0.22	-0.05	-0.02	0.04	-0.06	0.00	0.17	0.03	-0.11	-0.06	0.16	-0.01	0.03	-0.02	0.01	-0.02	-0.10	-0.03	<u>0.25</u>	0.03	-0.03	-0.06	0.01	0.03	0.00	-0.02	0.03
18	0.05	<u>-0.68</u>	0.03	0.00	0.02	0.12	0.01	0.00	0.05	0.02	-0.05	0.05	0.05	-0.04	0.10	0.00	-0.04	0.02	-0.03	-0.01	0.02	-0.03	-0.04	0.03	-0.04	-0.03	-0.07	0.08	-0.14
19	0.15	<u>0.57</u>	-0.04	-0.08	0.03	-0.11	-0.02	-0.04	0.07	0.09	-0.01	0.02	-0.12	0.05	-0.05	-0.09	0.12	0.08	-0.14	0.03	0.12	-0.03	<u>0.29</u>	0.01	<u>0.25</u>	0.01	0.00	-0.05	0.14
20	0.14	<u>-0.57</u>	0.20	-0.01	0.14	-0.09	0.22	0.02	-0.05	0.11	0.10	0.23	-0.06	0.07	-0.01	0.01	0.03	0.05	0.05	0.09	-0.02	0.00	0.06	0.01	-0.03	0.00	0.11	-0.06	0.01
21	0.04	<u>-0.48</u>	0.04	0.20	-0.13	0.00	0.00	0.00	0.02	-0.02	<u>-0.52</u>	-0.06	0.05	0.07	-0.08	0.02	0.04	0.02	0.04	0.01	0.14	0.02	-0.02	-0.03	0.09	0.09	0.08	0.06	0.07
22	0.01	<u>0.57</u>	0.08	0.00	0.05	-0.08	-0.07	-0.04	0.01	-0.01	<u>0.48</u>	<u>0.29</u>	-0.03	0.04	0.01	0.06	-0.04	0.06	0.02	0.10	0.06	0.00	-0.09	-0.03	-0.03	0.03	0.04	0.02	0.08
23	<u>0.31</u>	<u>-0.36</u>	0.04	0.13	-0.10	0.05	0.10	-0.07	0.05	0.02	<u>-0.45</u>	-0.13	-0.04	0.06	-0.04	0.12	0.02	-0.07	0.04	-0.03	0.10	-0.06	0.03	0.00	0.02	-0.02	-0.06	0.03	-0.02
24	-0.11	<u>0.43</u>	-0.01	-0.08	0.13	-0.04	0.05	0.00	0.01	0.01	<u>0.67</u>	0.10	-0.02	-0.06	0.07	-0.01	0.05	-0.06	0.06	0.13	0.02	0.04	-0.03	0.09	-0.01	0.01	0.03	0.03	-0.01
25	0.11	<u>0.51</u>	0.08	0.09	-0.01	-0.11	-0.05	0.10	0.02	0.00	0.09	<u>0.58</u>	0.03	-0.05	0.02	-0.03	-0.07	-0.05	-0.01	-0.03	-0.03	-0.01	0.07	-0.02	0.06	-0.04	0.00	0.02	-0.02
26	0.10	<u>0.54</u>	0.04	0.05	-0.01	0.11	-0.01	0.08	-0.03	0.03	0.15	<u>0.49</u>	-0.04	-0.02	0.05	0.01	-0.02	0.08	0.06	0.10	0.02	0.03	0.03	-0.04	-0.04	0.05	0.02	0.00	0.05
27	0.14	<u>0.55</u>	0.11	0.07	0.08	-0.02	0.10	0.15	0.02	-0.05	0.01	<u>0.61</u>	0.03	0.00	0.00	0.05	-0.01	-0.12	-0.05	-0.02	-0.04	0.04	0.09	-0.03	0.05	0.01	0.04	0.10	-0.06
28	-0.19	<u>-0.39</u>	-0.03	0.04	0.10	-0.01	-0.08	-0.04	-0.05	0.04	-0.24	<u>-0.31</u>	0.00	-0.01	0.03	0.00	0.02	0.04	0.08	0.06	0.07	0.02	-0.05	0.05	0.03	-0.11	-0.05	-0.03	-0.04
29	0.02	<u>-0.69</u>	-0.03	-0.07	0.06	0.00	-0.07	0.05	-0.01	0.03	-0.11	0.04	-0.16	0.01	-0.05	0.02	0.03	0.03	-0.07	-0.18	0.19	-0.05	-0.18	-0.06	0.02	0.02	-0.06	-0.03	-0.01
30	0.06	<u>-0.50</u>	0.04	0.04	<u>0.27</u>	-0.04	0.10	0.01	-0.04	-0.05	-0.01	0.20	<u>-0.31</u>	-0.10	-0.01	-0.01	0.03	0.02	0.06	0.04	0.10	0.06	-0.20	0.03	-0.07	0.01	0.03	0.03	0.03
31	-0.01	<u>0.63</u>	-0.07	-0.02	-0.16	0.12	-0.18	0.03	0.12	0.05	-0.16	-0.05	<u>0.37</u>	0.02	0.04	-0.03	-0.01	0.08	0.07	-0.01	0.08	0.07	0.03	0.09	0.01	0.15	-0.15	0.06	-0.02
32	0.00	<u>0.58</u>	-0.06	0.06	0.01	-0.04	0.01	0.01	-0.08	-0.10	0.00	0.09	<u>0.32</u>	0.04	<u>0.33</u>	0.01	0.07	0.05	0.10	0.10	0.00	0.14	-0.02	0.02	-0.09	-0.05	-0.07	0.00	0.06

Note. G1 = Emotionality; G2 = Extraversion; G3 = Conscientiousness; G4 = Openness to Experience; G5 = Agreeableness / Honesty-Humility; S1 = Fearfulness; S2 = Anxiety; S3 = Dependence; S4 = Sentimentality; S5 = Social Self-Esteem; S6 = Social Boldness; S7 = Sociability; S8 = Liveliness; S9 = Organization; S10 = Diligence; S11 = Perfectionism; S12 = Prudence; S13 = Aesthetic Appreciation; S14 = Inquisitiveness; S15 = Creativity; S16 = Unconventionality; S17 = Forgiveness; S18 = Gentleness; S19 = Flexibility; S20 = Patience; S21 = Sincerity; S22 = Fairness; S23 = Greed-Avoidance; S24 = Modesty.

Table A4 (Continuation).

Item	General factors					Group factors																							
	G1	G2	G3	G4	G5	S1	S2	S3	S4	S5	S6	S7	S8	S9	S10	S11	S12	S13	S14	S15	S16	S17	S18	S19	S20	S21	S22	S23	S24
33	0.07	-0.03	<u>0.26</u>	-0.04	0.06	-0.04	0.00	0.02	-0.02	0.00	0.06	0.04	0.02	<u>-0.78</u>	0.01	0.03	0.01	-0.02	0.06	0.12	0.09	0.03	-0.02	0.07	-0.04	0.01	0.03	-0.05	-0.04
34	0.05	-0.04	<u>0.60</u>	-0.06	0.04	0.08	0.08	0.01	0.00	0.13	-0.02	0.00	-0.14	<u>-0.43</u>	0.05	0.06	-0.13	0.03	0.06	0.04	-0.02	0.10	-0.07	0.05	0.03	-0.07	0.08	0.00	-0.04
35	-0.01	0.22	-0.24	0.06	0.15	0.04	0.01	0.01	0.04	0.02	-0.07	0.01	-0.01	<u>0.77</u>	0.08	0.01	0.00	0.01	0.06	0.05	0.05	0.06	-0.05	-0.02	0.06	-0.02	-0.02	0.06	-0.01
36	0.13	0.02	<u>-0.56</u>	0.09	-0.02	-0.07	-0.04	-0.07	-0.06	0.03	0.01	0.02	0.04	<u>0.30</u>	0.04	-0.02	<u>0.44</u>	-0.02	-0.01	-0.05	0.05	-0.04	0.02	0.03	0.00	0.03	0.05	0.00	0.10
37	0.11	0.11	<u>-0.63</u>	-0.06	0.02	-0.03	0.07	0.03	0.06	0.06	0.09	0.06	0.05	0.00	<u>0.56</u>	0.08	-0.08	0.06	0.00	-0.02	0.13	-0.06	-0.04	0.06	-0.02	0.06	0.06	-0.05	0.03
38	0.15	-0.21	<u>0.56</u>	-0.08	0.11	0.02	0.02	-0.01	-0.06	<u>0.36</u>	-0.08	0.05	0.01	-0.08	-0.24	0.05	-0.05	-0.02	-0.02	-0.02	-0.02	0.03	0.00	0.01	-0.01	0.00	-0.04	0.06	0.09
39	0.07	0.22	<u>-0.38</u>	-0.09	0.12	-0.03	0.07	-0.02	-0.01	<u>0.26</u>	0.07	-0.08	-0.01	-0.03	<u>0.46</u>	0.10	-0.01	-0.03	-0.04	0.11	0.01	0.06	0.10	0.01	0.04	-0.05	0.04	0.04	0.03
40	0.07	-0.14	<u>0.66</u>	0.07	0.03	0.08	0.03	-0.01	-0.01	0.04	0.01	0.04	0.04	-0.01	-0.22	-0.14	-0.02	0.03	0.08	-0.04	0.09	0.08	0.00	0.01	0.01	0.04	0.01	0.07	-0.02
41	0.18	-0.07	<u>-0.50</u>	-0.07	0.07	0.12	0.01	-0.05	0.10	0.00	-0.11	0.11	-0.04	-0.01	0.06	<u>0.40</u>	0.06	-0.01	0.07	0.03	-0.02	-0.05	-0.07	0.02	-0.06	0.04	0.02	0.00	0.02
42	-0.03	0.11	<u>0.55</u>	0.11	0.00	0.07	-0.03	0.02	-0.06	0.08	-0.07	0.04	-0.01	-0.01	0.07	<u>-0.41</u>	0.11	-0.24	-0.07	-0.06	0.04	0.05	-0.07	0.01	0.00	0.06	0.10	0.03	0.08
43	-0.06	-0.07	<u>-0.34</u>	-0.02	0.05	-0.06	0.00	0.08	-0.06	0.11	-0.13	0.02	-0.06	-0.08	0.09	<u>0.57</u>	0.05	0.00	0.02	-0.02	0.09	0.00	0.01	0.05	0.07	0.05	-0.04	0.08	0.01
44	0.19	-0.03	<u>-0.46</u>	-0.01	<u>0.25</u>	-0.03	0.08	0.02	0.03	0.06	0.07	-0.04	0.12	0.17	0.07	<u>0.36</u>	0.02	0.04	-0.06	0.11	0.13	0.10	-0.01	0.00	0.03	0.07	-0.02	0.02	0.05
45	-0.04	0.06	<u>0.60</u>	-0.08	-0.11	-0.10	0.00	0.01	0.08	-0.02	-0.05	0.12	0.04	-0.02	0.00	0.00	<u>-0.38</u>	0.02	-0.12	0.14	0.13	-0.05	0.00	0.00	-0.05	0.02	-0.03	0.02	0.17
46	-0.09	0.00	<u>-0.39</u>	0.04	<u>-0.27</u>	0.08	-0.03	-0.08	-0.09	-0.10	-0.11	0.00	0.06	-0.01	-0.23	-0.02	0.03	0.04	0.01	-0.06	0.21	0.02	-0.07	0.06	0.10	0.01	-0.05	0.09	-0.05
47	0.13	0.05	<u>0.61</u>	-0.02	0.01	-0.07	-0.12	0.00	0.06	-0.06	0.03	0.08	0.05	0.12	0.23	0.00	0.00	0.03	-0.11	0.10	-0.09	-0.07	0.03	-0.02	-0.11	0.02	-0.08	-0.01	0.20
48	0.05	-0.11	<u>0.57</u>	-0.01	0.17	0.10	-0.02	-0.01	0.00	0.00	-0.06	0.21	0.07	0.01	<u>0.35</u>	-0.06	0.04	-0.08	0.01	0.04	-0.02	0.10	-0.04	0.01	-0.09	0.05	-0.09	-0.02	-0.06

Note. G1 = Emotionality; G2 = Extraversion; G3 = Conscientiousness; G4 = Openness to Experience; G5 = Agreeableness / Honesty-Humility; S1 = Fearfulness; S2 = Anxiety; S3 = Dependence; S4 = Sentimentality; S5 = Social Self-Esteem; S6 = Social Boldness; S7 = Sociability; S8 = Liveliness; S9 = Organization; S10 = Diligence; S11 = Perfectionism; S12 = Prudence; S13 = Aesthetic Appreciation; S14 = Inquisitiveness; S15 = Creativity; S16 = Unconventionality; S17 = Forgiveness; S18 = Gentleness; S19 = Flexibility; S20 = Patience; S21 = Sincerity; S22 = Fairness; S23 = Greed-Avoidance; S24 = Modesty.

Table A4 (Continuation).

Item	General factors					Group factors																							
	G1	G2	G3	G4	G5	S1	S2	S3	S4	S5	S6	S7	S8	S9	S10	S11	S12	S13	S14	S15	S16	S17	S18	S19	S20	S21	S22	S23	S24
49	0.02	-0.01	0.02	0.69	-0.03	-0.07	-0.07	-0.01	-0.04	0.05	0.05	-0.04	0.03	-0.05	0.02	0.05	-0.01	-0.30	0.02	-0.28	0.01	0.03	-0.05	0.04	-0.01	-0.02	0.06	0.01	0.00
50	-0.07	0.05	-0.01	0.45	0.04	0.03	-0.06	0.00	-0.06	0.01	0.07	0.01	0.05	0.00	-0.01	-0.04	-0.05	-0.44	0.00	-0.29	0.04	-0.04	0.01	-0.10	0.10	0.02	-0.08	0.04	-0.02
51	-0.05	-0.02	0.01	-0.60	0.06	0.04	-0.09	0.02	-0.04	0.05	0.08	-0.07	0.06	-0.05	0.05	-0.06	-0.03	0.47	0.04	-0.01	0.02	0.04	-0.09	-0.08	0.08	0.05	0.03	0.08	0.08
52	0.02	-0.08	0.03	-0.34	-0.18	-0.06	0.07	0.04	0.14	0.24	-0.01	-0.08	0.05	0.04	0.02	0.03	0.06	0.27	0.13	0.22	0.07	0.00	0.05	-0.03	0.04	0.04	0.00	0.00	-0.15
53	-0.06	-0.02	0.04	-0.28	-0.06	-0.08	-0.08	-0.10	-0.01	0.09	0.02	0.03	0.06	0.02	-0.03	-0.02	0.03	0.06	0.57	0.05	0.01	-0.01	-0.02	-0.01	0.03	-0.03	-0.02	0.00	0.08
54	0.11	0.11	0.07	0.58	-0.04	-0.01	0.03	-0.04	-0.03	-0.05	-0.08	0.01	-0.06	0.03	0.03	-0.08	0.01	-0.02	-0.39	0.02	0.06	-0.02	0.00	-0.04	-0.03	-0.02	0.00	0.09	-0.04
55	0.09	0.04	0.05	0.52	0.05	0.01	-0.10	0.03	0.06	0.08	0.01	0.08	0.09	0.04	-0.04	-0.08	-0.02	-0.01	-0.34	0.06	-0.07	-0.02	0.01	0.00	0.06	-0.08	-0.04	-0.06	0.05
56	-0.05	0.06	0.00	-0.45	0.02	-0.03	0.08	-0.03	-0.04	-0.06	-0.06	0.03	-0.27	-0.04	-0.01	-0.04	0.07	0.04	0.49	0.00	0.05	-0.04	-0.08	0.01	-0.08	0.06	-0.05	-0.06	-0.01
57	0.02	0.16	0.08	-0.33	0.05	-0.05	0.08	0.07	0.02	0.02	0.07	0.02	0.10	-0.03	0.06	0.03	-0.05	0.03	0.12	0.65	0.07	-0.04	0.00	-0.12	0.03	-0.02	-0.02	0.01	0.09
58	0.04	-0.02	-0.01	-0.62	-0.05	0.01	0.05	0.04	0.04	0.12	0.00	0.04	0.05	-0.05	-0.01	0.01	0.09	0.02	-0.14	0.51	-0.10	-0.01	0.00	0.07	0.03	-0.01	0.00	-0.02	0.03
59	0.01	-0.07	0.02	0.43	0.00	-0.05	-0.05	-0.07	-0.01	0.02	0.00	-0.02	0.02	-0.04	0.00	0.00	0.08	0.04	0.15	-0.72	0.03	0.05	0.01	0.09	-0.01	-0.04	0.09	-0.03	-0.13
60	0.01	-0.11	-0.08	0.34	0.08	0.02	0.11	-0.01	0.04	-0.07	-0.10	-0.03	0.00	0.11	-0.06	0.04	0.41	0.03	0.02	-0.41	0.06	0.01	0.04	0.04	0.03	0.08	-0.06	0.08	-0.03
61	-0.11	-0.08	-0.07	0.52	0.06	0.23	0.02	0.06	0.03	-0.03	-0.05	-0.02	0.04	0.02	0.04	-0.19	0.06	0.08	0.05	-0.07	-0.04	-0.04	-0.03	-0.17	0.03	0.06	-0.17	0.05	0.07
62	-0.02	0.11	0.21	-0.25	0.16	-0.03	0.01	-0.03	-0.04	-0.13	0.13	0.10	-0.04	-0.04	0.11	0.08	0.00	0.05	0.08	0.41	0.10	0.04	0.01	0.11	0.05	0.01	0.07	-0.06	-0.02
63	0.01	0.08	0.18	-0.35	-0.05	-0.13	-0.16	-0.10	0.00	0.03	0.03	0.04	-0.14	-0.03	0.10	0.09	-0.15	0.01	0.08	0.26	0.26	0.07	0.08	0.17	0.04	-0.06	0.04	-0.10	-0.06
64	-0.01	-0.01	0.00	0.62	0.08	0.00	-0.01	-0.03	0.00	-0.04	-0.04	0.10	0.20	0.03	0.00	-0.08	0.06	-0.02	-0.06	-0.19	-0.02	-0.05	-0.07	-0.14	-0.03	-0.02	0.03	0.04	0.03

Note. G1 = Emotionality; G2 = Extraversion; G3 = Conscientiousness; G4 = Openness to Experience; G5 = Agreeableness / Honesty-Humility; S1 = Fearfulness; S2 = Anxiety; S3 = Dependence; S4 = Sentimentality; S5 = Social Self-Esteem; S6 = Social Boldness; S7 = Sociability; S8 = Liveliness; S9 = Organization; S10 = Diligence; S11 = Perfectionism; S12 = Prudence; S13 = Aesthetic Appreciation; S14 = Inquisitiveness; S15 = Creativity; S16 = Unconventionality; S17 = Forgiveness; S18 = Gentleness; S19 = Flexibility; S20 = Patience; S21 = Sincerity; S22 = Fairness; S23 = Greed-Avoidance; S24 = Modesty.

Table A4 (Continuation).

Item	General factors					Group factors																							
	G1	G2	G3	G4	G5	S1	S2	S3	S4	S5	S6	S7	S8	S9	S10	S11	S12	S13	S14	S15	S16	S17	S18	S19	S20	S21	S22	S23	S24
65	0.07	-0.05	-0.08	0.07	<u>0.38</u>	0.03	-0.04	-0.13	0.13	0.05	0.08	-0.01	-0.06	-0.03	0.02	0.09	0.13	0.04	0.03	0.01	0.06	<u>-0.44</u>	0.02	0.06	-0.04	-0.06	0.07	0.00	0.00
66	0.06	-0.14	-0.05	0.02	<u>0.53</u>	0.03	0.09	-0.01	0.05	0.01	-0.06	0.05	0.07	0.02	-0.03	-0.04	0.01	-0.01	-0.01	-0.07	0.07	<u>-0.61</u>	0.02	0.00	-0.01	-0.02	0.00	-0.03	-0.02
67	-0.01	0.10	0.09	-0.02	<u>-0.57</u>	0.03	0.05	-0.02	0.09	-0.01	0.06	-0.01	-0.01	-0.01	-0.03	0.00	0.05	-0.02	-0.01	0.00	0.01	<u>0.58</u>	0.01	-0.02	0.01	0.04	0.00	0.08	0.07
68	0.04	0.17	0.00	0.00	<u>-0.42</u>	-0.02	-0.07	0.01	0.07	0.07	0.00	0.10	0.07	-0.02	0.04	0.01	0.06	0.05	0.00	-0.06	0.09	<u>0.61</u>	0.07	-0.05	0.03	-0.08	0.02	0.05	0.06
69	0.13	-0.06	0.02	0.08	<u>-0.52</u>	0.00	-0.02	-0.05	0.02	0.00	-0.09	0.03	0.03	-0.02	0.08	-0.09	0.05	0.00	0.06	0.02	0.24	0.01	0.20	-0.02	0.07	0.09	0.09	0.08	0.06
70	-0.01	-0.04	0.00	0.07	<u>-0.56</u>	0.01	0.11	-0.07	-0.05	0.05	-0.06	0.10	0.06	-0.01	0.01	0.04	-0.02	0.07	0.00	0.05	<u>0.26</u>	0.12	<u>0.38</u>	-0.02	-0.03	0.04	0.03	0.01	-0.02
71	0.07	-0.03	0.07	-0.11	<u>-0.42</u>	-0.05	0.03	-0.03	0.14	0.08	0.02	0.12	0.07	0.00	0.05	0.08	-0.04	-0.07	-0.01	-0.01	0.11	<u>0.27</u>	<u>0.54</u>	-0.02	0.02	0.01	0.09	-0.09	-0.06
72	-0.10	0.02	-0.04	-0.02	<u>0.65</u>	-0.05	-0.04	-0.07	-0.07	0.13	0.11	-0.01	0.02	0.01	0.05	-0.01	-0.06	0.03	0.03	-0.06	0.13	0.04	<u>-0.42</u>	0.08	-0.08	-0.11	-0.05	-0.12	-0.03
73	-0.05	0.09	0.10	-0.04	<u>-0.34</u>	-0.03	0.04	-0.04	-0.01	0.07	-0.07	0.03	-0.01	0.06	0.06	0.06	0.00	-0.09	-0.09	-0.05	<u>0.28</u>	0.07	0.10	<u>-0.46</u>	0.01	0.08	0.00	0.05	0.00
74	0.05	-0.09	-0.09	0.00	<u>0.44</u>	-0.08	0.08	-0.07	0.06	-0.01	0.00	0.01	0.01	-0.09	0.05	-0.05	0.03	-0.04	0.02	0.01	0.10	-0.02	-0.06	<u>0.36</u>	-0.24	-0.02	-0.03	-0.12	-0.05
75	0.03	0.00	0.02	-0.11	<u>0.57</u>	0.05	-0.01	0.04	-0.09	0.05	0.03	-0.11	0.07	-0.03	0.02	0.04	-0.04	0.01	-0.06	-0.02	0.04	-0.03	-0.01	<u>0.41</u>	0.06	-0.01	-0.10	-0.07	-0.02
76	0.00	0.02	0.11	0.00	<u>0.48</u>	0.03	0.06	0.05	0.12	0.00	0.03	0.01	0.00	-0.01	0.08	0.10	0.13	-0.08	-0.01	-0.09	-0.11	-0.03	-0.05	<u>0.43</u>	-0.11	0.01	0.03	0.05	-0.02
77	-0.01	-0.03	0.09	0.03	<u>0.54</u>	0.01	-0.01	0.01	0.00	0.02	0.07	0.08	-0.07	-0.03	0.07	-0.05	0.00	0.03	0.07	0.03	0.04	0.03	-0.08	0.04	<u>-0.66</u>	-0.03	-0.03	0.04	0.00
78	0.08	0.08	0.16	-0.04	<u>0.55</u>	0.08	-0.01	0.09	0.02	-0.09	0.02	-0.04	0.06	-0.07	0.08	0.06	0.06	0.02	-0.02	-0.06	-0.04	-0.10	0.00	0.02	<u>-0.41</u>	-0.10	-0.03	0.04	0.11
79	-0.06	0.08	-0.05	-0.03	<u>-0.40</u>	0.11	-0.06	0.04	0.08	-0.05	-0.02	0.05	-0.01	-0.02	0.00	0.09	0.01	-0.05	0.05	0.07	0.11	0.06	0.04	-0.03	<u>0.59</u>	-0.08	0.03	0.13	0.05
80	-0.16	0.01	0.05	0.02	<u>-0.51</u>	0.02	0.01	-0.03	-0.05	-0.02	-0.04	0.00	0.08	0.00	0.01	-0.10	0.07	0.09	0.05	-0.03	0.09	0.23	-0.03	0.08	<u>0.35</u>	0.12	0.02	0.06	0.14

Note. G1 = Emotionality; G2 = Extraversion; G3 = Conscientiousness; G4 = Openness to Experience; G5 = Agreeableness / Honesty-Humility; S1 = Fearfulness; S2 = Anxiety; S3 = Dependence; S4 = Sentimentality; S5 = Social Self-Esteem; S6 = Social Boldness; S7 = Sociability; S8 = Liveliness; S9 = Organization; S10 = Diligence; S11 = Perfectionism; S12 = Prudence; S13 = Aesthetic Appreciation; S14 = Inquisitiveness; S15 = Creativity; S16 = Unconventionality; S17 = Forgiveness; S18 = Gentleness; S19 = Flexibility; S20 = Patience; S21 = Sincerity; S22 = Fairness; S23 = Greed-Avoidance; S24 = Modesty.

Table A4 (Continuation).

Item	General factors					Group factors																							
	G1	G2	G3	G4	G5	S1	S2	S3	S4	S5	S6	S7	S8	S9	S10	S11	S12	S13	S14	S15	S16	S17	S18	S19	S20	S21	S22	S23	S24
81	0.03	0.09	0.17	-0.05	0.35	-0.02	0.08	0.01	0.04	-0.14	0.03	0.02	0.06	-0.06	-0.06	0.06	0.10	-0.01	-0.02	-0.03	0.10	0.09	0.09	-0.04	0.08	0.62	0.01	0.06	0.12
82	0.05	-0.08	-0.19	-0.08	-0.31	0.06	0.02	-0.04	0.06	-0.07	-0.02	0.01	0.08	-0.06	-0.03	0.05	0.02	-0.01	-0.06	0.06	0.03	-0.06	0.02	0.01	-0.02	-0.58	-0.08	0.01	-0.03
83	-0.05	-0.21	-0.13	0.09	-0.31	-0.01	0.07	0.04	0.02	-0.05	-0.03	-0.05	0.06	-0.06	-0.06	0.04	0.06	0.01	-0.02	-0.03	0.05	0.02	-0.04	0.04	0.08	-0.51	-0.18	-0.14	0.00
84	0.05	0.01	0.23	0.05	0.29	0.04	0.07	0.12	-0.01	0.03	-0.07	0.06	0.10	0.01	-0.01	0.07	0.03	0.04	0.02	0.03	0.04	-0.06	0.01	-0.01	0.09	0.57	0.11	0.10	0.09
85	-0.01	-0.06	-0.20	-0.16	-0.32	0.02	-0.06	0.03	0.03	-0.01	0.06	-0.14	0.02	0.07	0.00	0.09	0.08	0.05	-0.06	-0.03	0.12	-0.04	-0.02	-0.02	-0.06	-0.19	-0.42	-0.10	-0.02
86	-0.12	0.02	0.30	0.03	0.43	-0.11	0.05	0.01	-0.03	-0.07	0.00	0.01	0.02	0.06	0.04	-0.01	0.00	0.01	0.00	-0.06	0.07	-0.04	0.14	-0.01	0.04	0.06	0.63	0.10	-0.04
87	-0.25	0.00	0.29	0.04	0.39	-0.04	0.02	0.01	0.02	0.02	-0.01	-0.02	-0.04	-0.04	-0.04	-0.01	0.07	0.07	-0.08	0.03	0.00	-0.03	0.04	-0.02	0.06	0.07	0.67	0.01	0.00
88	-0.12	-0.03	0.29	-0.05	0.26	-0.01	-0.01	-0.02	-0.01	0.02	0.05	0.03	-0.06	-0.07	0.00	-0.03	0.01	-0.02	0.02	-0.01	0.05	0.04	-0.06	-0.04	-0.03	0.08	0.66	0.01	0.07
89	-0.09	0.20	0.09	0.19	0.33	-0.02	0.08	0.02	0.02	0.03	-0.04	0.00	0.01	0.04	-0.04	-0.01	0.05	0.05	0.03	-0.09	0.00	0.01	-0.06	-0.03	-0.01	0.04	0.03	0.65	0.13
90	-0.02	0.20	-0.04	0.07	0.44	0.07	-0.02	-0.08	0.02	-0.04	-0.01	0.04	0.09	0.07	-0.04	-0.01	-0.03	-0.05	-0.06	0.01	0.02	0.08	0.02	0.04	0.08	0.11	0.02	0.67	0.07
91	0.04	-0.09	0.07	-0.11	-0.60	-0.02	0.04	0.00	0.09	0.01	0.02	0.00	0.06	0.02	0.02	0.02	0.01	-0.04	0.05	0.08	0.02	-0.02	-0.25	0.13	-0.09	0.04	0.04	-0.42	0.07
92	0.09	0.19	0.08	0.08	0.41	0.04	-0.02	0.00	0.04	0.00	0.05	0.06	0.00	0.01	0.01	0.04	0.02	0.02	-0.02	-0.02	0.00	0.00	0.03	-0.08	-0.03	0.04	0.12	0.70	0.06
93	0.32	-0.26	0.00	0.03	-0.42	-0.04	-0.10	-0.03	0.02	-0.02	0.02	0.10	0.11	-0.01	0.05	-0.02	0.08	0.03	-0.08	-0.11	0.05	-0.09	0.04	0.04	-0.10	0.01	-0.09	-0.06	-0.40
94	-0.31	-0.02	0.08	0.00	0.41	0.08	-0.08	0.09	-0.11	-0.06	0.01	0.08	0.10	-0.04	0.07	-0.10	0.03	0.03	0.11	0.08	0.10	0.02	-0.03	-0.08	0.07	0.01	-0.02	0.12	0.39
95	-0.08	0.16	-0.04	-0.01	0.50	0.01	-0.05	0.08	-0.03	0.16	0.05	0.02	0.00	0.05	0.02	0.06	0.01	-0.06	0.05	0.06	0.06	0.06	0.03	0.06	0.03	0.16	0.04	0.29	0.47
96	0.28	-0.13	-0.01	0.00	-0.48	-0.06	-0.06	-0.04	-0.03	0.06	0.00	0.00	-0.02	-0.03	-0.02	0.01	0.00	-0.03	0.08	-0.01	0.09	-0.12	0.01	0.05	-0.07	-0.13	0.03	-0.17	-0.45

Note. G1 = Emotionality; G2 = Extraversion; G3 = Conscientiousness; G4 = Openness to Experience; G5 = Agreeableness / Honesty-Humility; S1 = Fearfulness; S2 = Anxiety; S3 = Dependence; S4 = Sentimentality; S5 = Social Self-Esteem; S6 = Social Boldness; S7 = Sociability; S8 = Liveliness; S9 = Organization; S10 = Diligence; S11 = Perfectionism; S12 = Prudence; S13 = Aesthetic Appreciation; S14 = Inquisitiveness; S15 = Creativity; S16 = Unconventionality; S17 = Forgiveness; S18 = Gentleness; S19 = Flexibility; S20 = Patience; S21 = Sincerity; S22 = Fairness; S23 = Greed-Avoidance; S24 = Modesty.

Table A5. Estimated factor correlations between the general factors for the HEXACO-100. Correlations with absolute values greater than .20 are shown in bold and underlined.

	G1	G2	G3	G4	G5
G1	-				
G2	-0.17	-			
G3	0.03	-0.15	-		
G4	<u>0.21</u>	-0.06	0.01	-	
G5	<u>0.34</u>	<u>-0.25</u>	0.13	0.15	-

Note. G1 = Emotionality; G2 = Extraversion; G3 = Conscientiousness; G4 = Openness to Experience; G5 = Agreeableness / Honesty-Humility.

Table 1. Simulated loadings for a condition with one general factor, four group factors and medium loadings on both the general and group factors. When cross-loadings (underlined) were included, small values were subtracted from the loadings on the general and group factors to maintain the original communality (\mathbf{h}^2).

Item	Simple structure						Cross-loadings					
	G	S1	S2	S3	S4	\mathbf{h}^2	G	S1	S2	S3	S4	\mathbf{h}^2
1	.45	.60				.57	.40	.56			<u>.30</u>	.57
2	.47	.53				.51	.47	.53				.51
3	.51	.47				.48	.51	.47				.48
4	.58	.40				.50	.58	.40				.50
5	.44		.60			.55	.39	<u>.30</u>	.56			.55
6	.58		.53			.62	.58		.53			.62
7	.59		.47			.56	.59		.47			.56
8	.53		.40			.44	.53		.40			.44
9	.53			.60		.64	.48		<u>.30</u>	.56		.64
10	.41			.53		.45	.41			.53		.45
11	.44			.47		.41	.44			.47		.41
12	.44			.40		.35	.44			.40		.35
13	.54				.60	.65	.49			<u>.30</u>	.56	.65
14	.48				.53	.51	.48				.53	.51
15	.55				.47	.52	.55				.47	.52
16	.50				.40	.41	.50				.40	.41
Avg.						.51						.51

Table 2. Marginal hit rates across each variable level for each factor retention method.

Variable	Group factors						General factors					
	Kaiser		PAPAF		PAPCA		EGALV	PAPCA-FS		EGALV	EGALV-FS	
	K1	EKC	mean	95th	mean	95th		mean	95th			
<u>MF</u>												
zero	.76	.93	.98	.98	.86	.84	.87	.99	.98	.10	1.00	
close	.44	.48	.21	.29	.81	.80	.86	.99	.99	.09	1.00	
<u>N</u>												
500	.33	.62	.72	.79	.68	.64	.84	.97	.95	.06	1.00	
1000	.55	.66	.63	.69	.85	.83	.86	.99	.99	.09	1.00	
2000	.72	.73	.53	.57	.90	.89	.87	1.00	1.00	.11	1.00	
5000	.81	.81	.50	.51	.91	.91	.89	1.00	1.00	.13	1.00	
<u>N.GF</u>												
1	.78	.81	.52	.58	.95	.94	.98	1.00	1.00	.00	1.00	
2	.61	.71	.60	.66	.87	.85	.91	.99	.99	.02	1.00	
3	.49	.65	.62	.65	.74	.73	.76	.98	.98	.22	.99	
<u>COR.GF</u>												
0	.67	.67	.64	.69	.87	.86	.88	.99	.99	.09	1.00	
.30	.50	.61	.52	.56	.77	.76	.84	.99	.98	.10	1.00	
<u>VAR.GRF</u>												
4	.90	.91	.59	.67	.60	.56	.75	.97	.94	.25	.99	
6	.68	.79	.59	.64	.89	.87	.83	1.00	1.00	.13	1.00	
8	.48	.62	.59	.63	.93	.92	.92	1.00	1.00	.01	1.00	
10	.34	.49	.60	.62	.92	.92	.95	1.00	1.00	.00	1.00	
<u>N.GRF</u>												
4	.68	.77	.61	.67	.88	.87	.90	.99	.98	.10	1.00	
5	.60	.70	.59	.64	.84	.82	.86	.99	.99	.10	1.00	
6	.52	.65	.57	.61	.78	.76	.83	.99	.99	.10	1.00	
<u>CROSS.GRF</u>												
0	.61	.72	.60	.65	.87	.86	.99	.99	.98	.07	1.00	
.15	.60	.71	.60	.64	.84	.82	.89	.99	.98	.08	1.00	
.30	.59	.69	.58	.63	.79	.78	.70	.99	.99	.14	.99	
<u>LOAD.GRF</u>												
low	.52	.67	.59	.64	.75	.72	.80	.98	.97	.18	.99	
medium	.68	.74	.60	.63	.92	.91	.93	1.00	1.00	.02	1.00	
<u>LOAD.GF</u>												
low	.52	.68	.60	.66	.88	.87	.86	1.00	1.00	.07	1.00	
medium	.68	.73	.59	.62	.79	.77	.87	.98	.97	.13	1.00	
<u>Total</u>	.60	.70	.59	.64	.83	.82	.86	.99	.99	.10	1.00	

Note. K1 = Kaiser eigenvalue greater-than-one criterion; EKC = Empirical Kaiser Criterion; PAPAF = Parallel analysis with principal axis factoring; PAPCA = Parallel analysis with principal components; PAPCA-FS = Parallel analysis with principal components on the first-order factor scores; EGA = Exploratory Graph Analysis; EGALV = EGA with Louvain; EGALV-FS = EGA with Louvain on the first-order factor scores; MF = population misfit; N = sample size; N.GF = number of general factors; COR.GF = correlation between general factors; VAR.GRF = number of indicators per group factor; N.GRF = number of group factors per general factor; CROSS.GRF = cross-loadings in the group factors; LOAD.GRF = loadings on the group factors; LOAD.GF = loadings on the general factors.

Table 3. Mean bias error (MBE) across each variable level for each factor retention method.

Variable	Group factors						General factors				
	Kaiser		PAPAF		PAPCA		EGALV	PAPCA-FS		EGALV	EGALV-FS
	K1	EKC	mean	95th	mean	95th		mean	95th		
<u>MF</u>											
zero	1.56	0.02	0.01	-0.01	-0.48	-0.57	-0.30	-0.01	-0.02	0.64	0.00
close	2.58	1.23	3.83	3.17	-0.40	-0.49	-0.29	-0.01	-0.02	0.70	0.00
<u>N</u>											
500	4.84	0.62	0.40	0.16	-1.13	-1.37	-0.26	-0.03	-0.07	1.48	0.00
1000	2.25	0.88	1.00	0.68	-0.44	-0.54	-0.31	0.00	-0.01	0.86	0.00
2000	0.85	0.67	2.12	1.72	-0.16	-0.20	-0.31	0.00	0.00	0.39	0.00
5000	0.33	0.33	4.17	3.76	-0.01	-0.02	-0.30	0.00	0.00	-0.05	-0.01
<u>N.GF</u>											
1	0.41	0.31	2.43	1.99	-0.07	-0.10	0.02	0.00	0.00	-0.88	0.00
2	1.51	0.56	1.73	1.41	-0.31	-0.39	-0.14	0.00	-0.01	0.12	0.00
3	3.46	0.84	1.86	1.54	-0.75	-0.89	-0.61	-0.02	-0.04	2.00	-0.01
<u>COR.GF</u>											
0	1.61	0.34	1.23	0.96	-0.40	-0.48	-0.26	-0.01	-0.02	0.40	0.00
.30	2.76	1.05	2.96	2.51	-0.49	-0.61	-0.35	-0.01	-0.02	1.08	0.00
<u>VAR.GRF</u>											
4	0.09	-0.10	0.88	0.59	-1.46	-1.73	-0.76	-0.04	-0.08	1.41	-0.01
6	0.99	0.31	1.65	1.32	-0.29	-0.36	-0.28	0.00	0.00	1.20	0.00
8	2.55	0.83	2.31	1.94	-0.04	-0.07	-0.10	0.00	0.00	0.40	0.00
10	4.64	1.46	2.85	2.47	0.05	0.03	-0.04	0.00	0.00	-0.33	0.00
<u>N.GRF</u>											
4	1.23	0.44	1.60	1.28	-0.24	-0.31	-0.17	-0.01	-0.02	-0.26	-0.01
5	2.02	0.63	1.92	1.58	-0.42	-0.51	-0.29	-0.01	-0.02	0.61	0.00
6	2.96	0.81	2.25	1.88	-0.65	-0.77	-0.42	-0.01	-0.02	1.67	0.00
<u>CROSS.GRF</u>											
0	2.06	0.66	2.00	1.66	-0.33	-0.42	0.00	-0.01	-0.02	0.20	0.00
.15	2.06	0.64	1.95	1.62	-0.43	-0.53	-0.14	-0.01	-0.03	0.62	0.00
.30	2.09	0.58	1.81	1.47	-0.55	-0.65	-0.75	0.00	-0.01	1.19	-0.01
<u>LOAD.GRF</u>											
low	2.95	0.71	1.90	1.52	-0.82	-0.98	-0.48	-0.02	-0.04	1.32	-0.01
medium	1.19	0.54	1.94	1.64	-0.05	-0.08	-0.11	0.00	0.00	0.03	0.00
<u>LOAD.GF</u>											
low	2.97	0.71	1.68	1.34	-0.24	-0.31	-0.28	0.00	0.00	0.80	0.00
medium	1.17	0.54	2.16	1.82	-0.63	-0.75	-0.31	-0.02	-0.04	0.55	-0.01
<u>Total</u>											
	2.07	0.63	1.92	1.58	-0.44	-0.53	-0.29	-0.01	-0.02	0.67	0.00

Note. K1 = Kaiser eigenvalue greater-than-one criterion; EKC = Empirical Kaiser Criterion; PAPAF = Parallel analysis with principal axis factoring; PAPCA = Parallel analysis with principal components; PAPCA-FS = Parallel analysis with principal components on the first-order factor scores; EGA = Exploratory Graph Analysis; EGALV = EGA with Louvain; EGALV-FS = EGA with Louvain on the first-order factor scores; MF = population misfit; N = sample size; N.GF = number of general factors; COR.GF = correlation between general factors; VAR.GRF = number of indicators per group factor; N.GRF = number of group factors per general factor; CROSS.GRF = cross-loadings in the group factors; LOAD.GRF = loadings on the group factors; LOAD.GF = loadings on the general factors.

Table 4. Partial omega squared coefficients (Ω^2) from the ANOVAs on the absolute error for all the nine main effects, and for the remaining coefficients whose $\Omega^2 \geq .14$ or close in at least one factor retention method.

Coefficients	Group factors		General factors	
	PA _{PCA}	EGALV	PA _{PCA-FS}	EGALV-FS
Main effects				
VAR.GRF	0.57	0.22	0.03	0.01
N	0.39	0.00	0.02	0.00
N.GF	0.29	0.18	0.01	0.00
LOAD.GF	0.15	0.00	0.01	0.00
LOAD.GRF	0.35	0.12	0.01	0.00
N.GRF	0.13	0.04	0.00	0.00
MF	0.00	0.00	0.00	0.00
COR.GF	0.00	0.00	0.00	0.00
CROSS.GRF	0.03	0.28	0.00	0.01
Two-way interactions				
VAR.GRF \times LOAD.GRF	0.45	0.09	0.03	0.01
VAR.GRF \times N	0.44	0.01	0.06	0.00
VAR.GRF \times N.GF	0.28	0.14	0.02	0.01
N \times LOAD.GRF	0.26	0.00	0.02	0.00
N \times N.GF	0.20	0.00	0.01	0.00
VAR.GRF \times LOAD.GF	0.19	0.00	0.02	0.00
N.GF \times LOAD.GRF	0.16	0.08	0.01	0.00
VAR.GRF \times CROSS.GRF	0.05	0.33	0.00	0.02
N.GF \times CROSS.GRF	0.01	0.20	0.00	0.01
Three-way interactions				
VAR.GRF \times N \times LOAD.GRF	0.21	0.00	0.06	0.00
VAR.GRF \times N \times N.GF	0.18	0.01	0.04	0.00
VAR.GRF \times N.GF \times LOAD.GRF	0.17	0.05	0.02	0.01
VAR.GRF \times N.GF \times CROSS.GRF	0.01	0.22	0.00	0.02
VAR.GRF \times LOAD.GRF \times CROSS.GRF	0.01	0.13	0.00	0.01

Note. PA_{PCA} = Parallel analysis with principal components; PA_{PCA-FS} = Parallel analysis with principal components on the first-order factor scores; EGA = Exploratory graph analysis; EGALV = EGA with Louvain; EGALV-FS = EGA with Louvain on the first-order factor scores. MF = population misfit; N.GF = number of general factors; COR.GF = Correlation between general factors; N = sample size; VAR.GRF = Number of indicators per group factor; N.GRF = number of group factors per general factor; CROSS.GRF = cross-loadings in the group factors; LOAD.GF = loadings on the general factors; LOAD.GRF = loadings on the group factors;

Figure 1. Illustration of a bi-factor model with two general factors (G) and four group factors (S) for twelve indicators (X). The grey arrows represent cross-loadings among the group factors, with each group factor having an indicator that cross-load on another group factor.

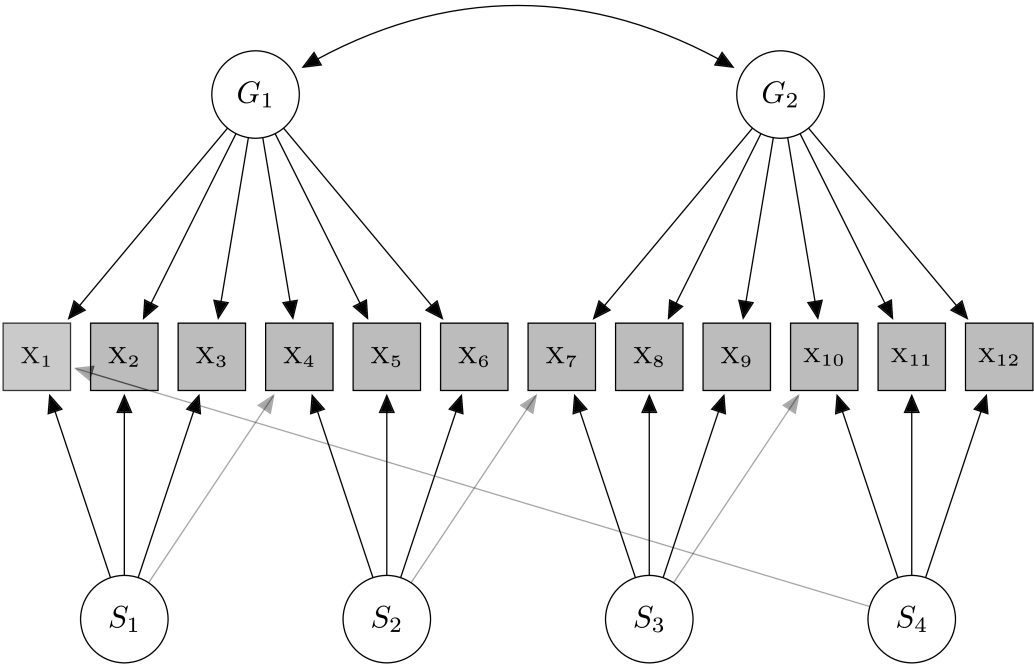


Figure 2. Graph of a network estimated with a Gaussian Graphical Model and GLASSO. Each color represents a factor and the items were clustered with the Louvain algorithm.

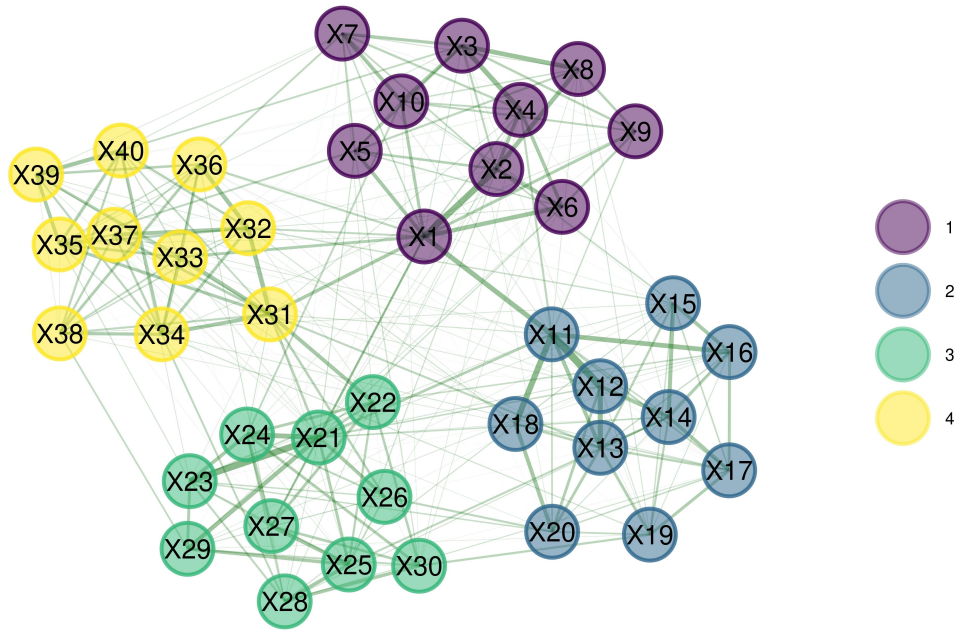


Figure 3. Mean Absolute Error (MAE) for the number of group factors for the PA_{PCA} method, as function of the number of variables per group factor, sample size (N), and the loadings on the group factors (LOAD.GRF; panel a) or the number of general factors (N.GF; panel b).

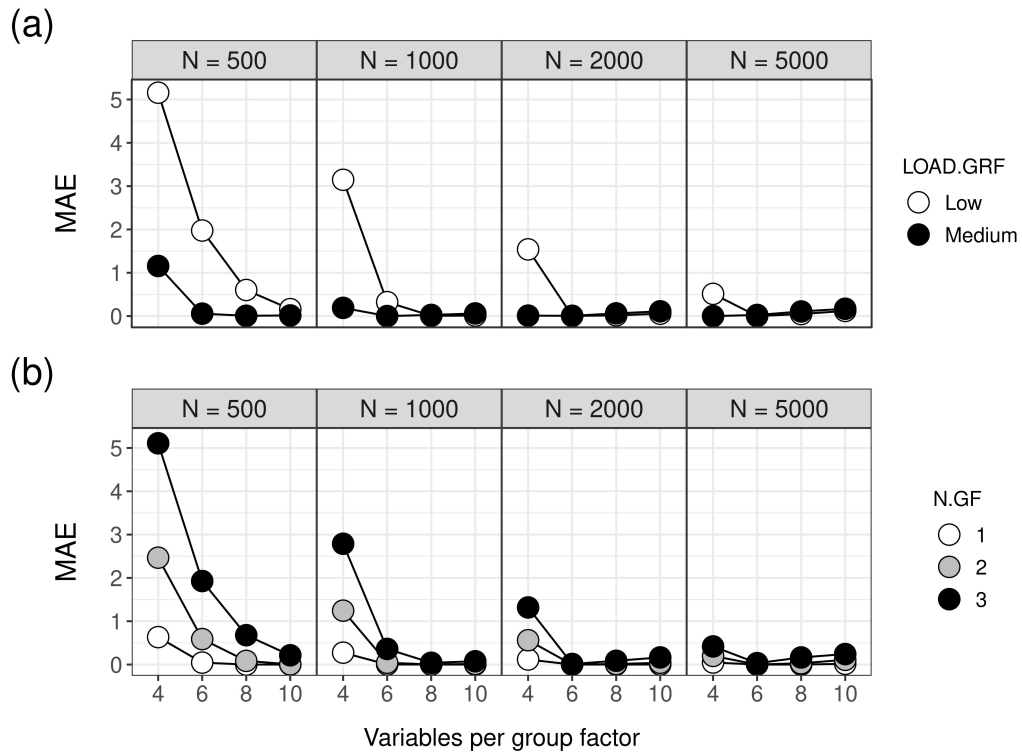


Figure 4. Mean Absolute Error (MAE) for the number of group factors for the PA_{PCA} method, as function of the number of variables per group factor, the number of general factors (N.GF), and the loadings on the group factors (LOAD.GRF).

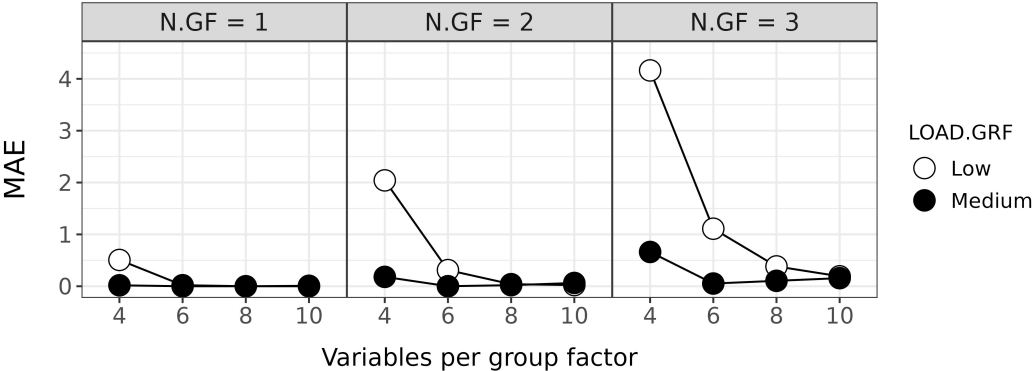


Figure 5. Mean Absolute Error (MAE) for the number of group factors for the PA_{PCA} method, as function of the number of variables per group factor and the loadings on the general factors (LOAD.GF).

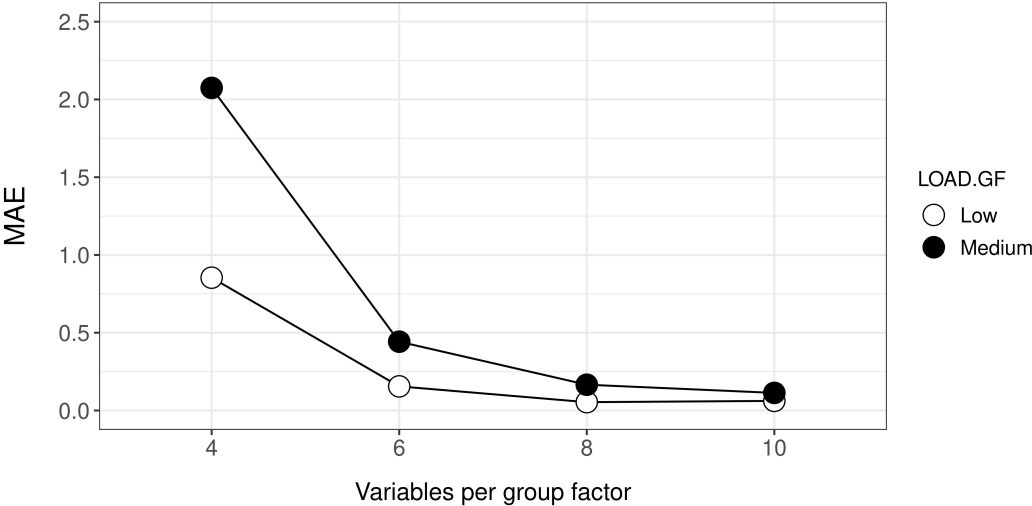


Figure 6. Mean Absolute Error (MAE) for the number of group factors for the E_{GALV} method, as function of the number of variables per group factor, cross-loadings on the group factors (CROSS.GRF), and the number of general factors (N.GF; panel a) or the loadings on the group factors (LOAD.GRF; panel b).

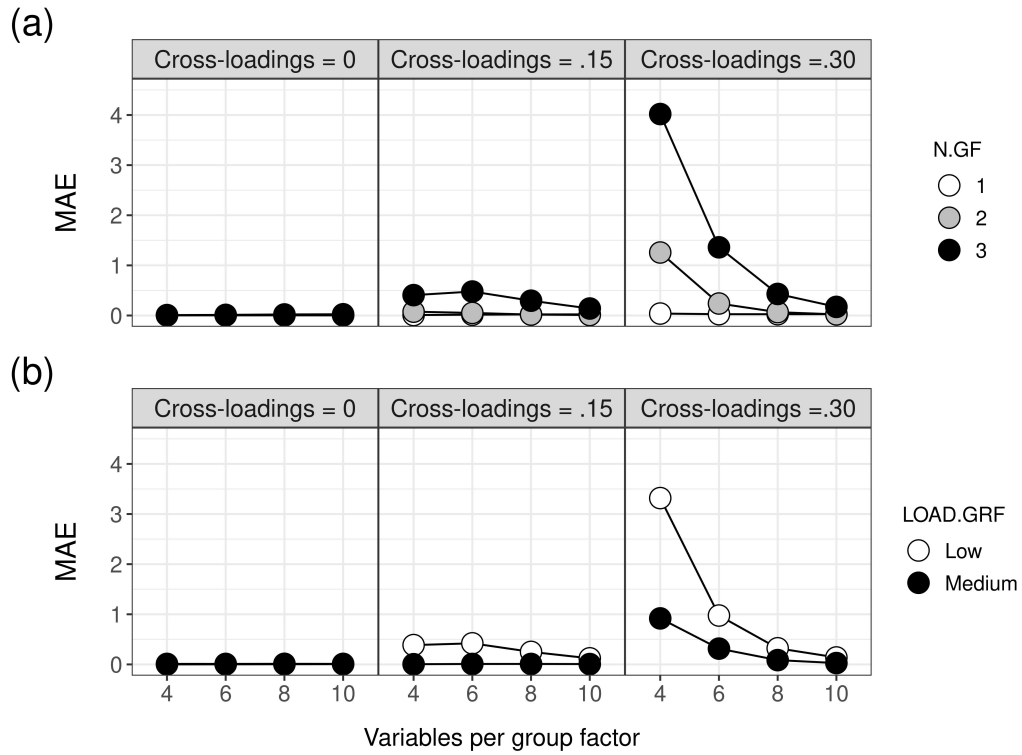


Figure 7. Factor loadings for the HEXACO-100 data (excluding the Altruism scale) from an exploratory bi-factor analysis with five general factors and 24 group factors estimated with GSLiD. For simplicity, the absolute value of the factor loadings is shown.

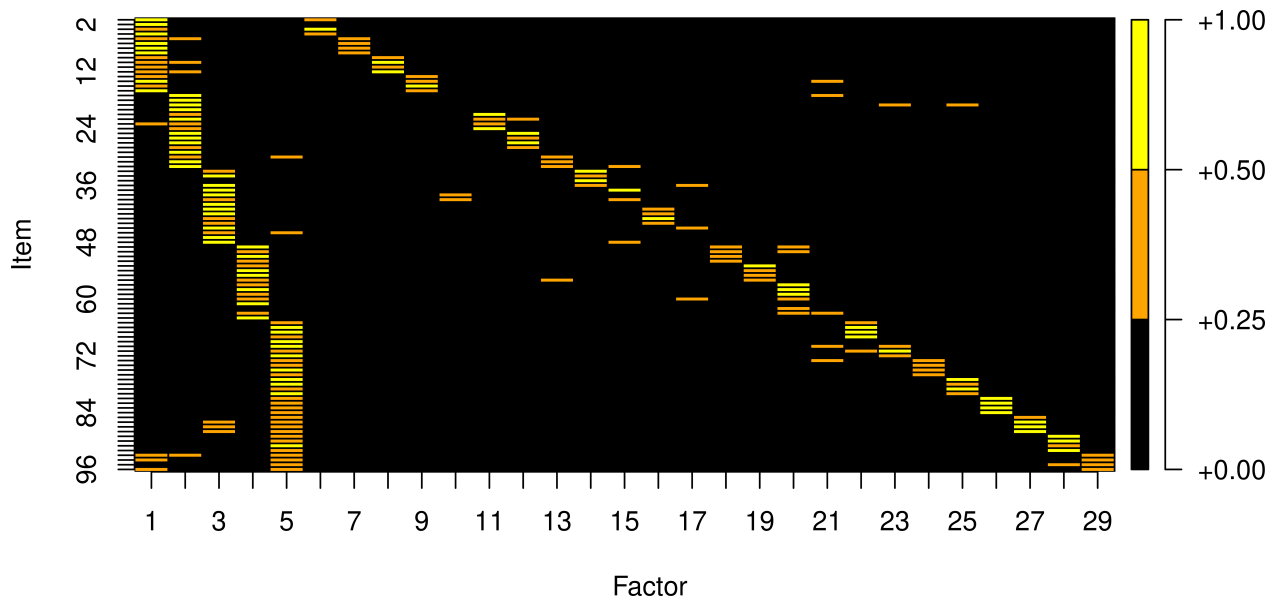


Figure captions

Figure 1. Illustration of a bi-factor model with two general factors (G) and four group factors (S) for twelve indicators (X). The grey arrows represent cross-loadings among the group factors, with each group factor having an indicator that cross-load on another group factor.

Figure 2. Graph of a network estimated with a Gaussian Graphical Model and GLASSO. Each color represents a factor and the items were clustered with the Louvain algorithm.

Figure 3. Mean Absolute Error (MAE) for the number of group factors for the PA_{PCA} method, as function of the number of variables per group factor, sample size (N), and the loadings on the group factors (LOAD.GRF; panel a) or the number of general factors (N.GF; panel b).

Figure 4. Mean Absolute Error (MAE) for the number of group factors for the PA_{PCA} method, as function of the number of variables per group factor, the number of general factors (N.GF), and the loadings on the group factors (LOAD.GRF).

Figure 5. Mean Absolute Error (MAE) for the number of group factors for the PA_{PCA} method, as function of the number of variables per group factor and the loadings on the general factors (LOAD.GF).

Figure 6. Mean Absolute Error (MAE) for the number of group factors for the $EGALV$ method, as function of the number of variables per group factor, cross-loadings on the group factors (CROSS.GRF), and the number of general factors (N.GF; panel a) or the loadings on the group factors (LOAD.GRF; panel b).

Figure 7. Factor loadings for the HEXACO-100 data (excluding the Altruism scale) from an exploratory bi-factor analysis with five general factors and 24 group factors estimated with GSLID. For simplicity, the absolute value of the factor loadings is shown.