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Statistical Image Differences, Degradation Features, and Character Distance Metrics

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Abstract. Document image quality is degraded through processes such as scanning, printing, and photocopying. The resulting bilevel image degradations can be categorized based either on observable degradation features or on degradation model parameters. The image degradation features can be related mathematically to model parameters. In this paper we statistically compare pairs of populations of degraded character images created with different model parameters. The probability that the character populations were degraded by the same model parameters correlates with the relationship between observable degradation features and the model parameters. Two metrics of character difference are used: Hamming distance and moment feature distance. Knowledge of under which conditions characters will be similar and when they will be different can influence the choice of parameters for future experiments.

Key words: Degradation model – Point spread function – Binarization threshold

1 Introduction

Document image quality is degraded as the ideal conceptual image is changed to form physical and electronic images through processes such as scanning, printing and photocopying. This paper discusses bilevel degradations in the context of the scanning process. For the bilevel processes, two observable image degradations were described in [3]–[7]. These degradations are the amount an edge is displaced from its original location and the amount of erosion in a black or white corner. The variables that cause these image degradations can be related to the functional form of the degradation model: the Point Spread Function (PSF), the associated PSF width, and the binarization threshold.

From a calibrated model, one can predict how a document image will look after being subjected to the appropriate printing and scanning processes and, therefore, predict system performance. Large training sets of synthetic characters can be created using the model when the model parameters are matched to the source document. This can increase recognition accuracy. It also eases the burden of hand segmenting and labeling data. Models of the degradation process, along with estimates of the parameters for these models, can be combined to make a decision on whether a given document should be entered by hand or sent to an Optical Character Recognition (OCR) routine [8,14,15]. A model will allow researchers to conduct controlled experiments to improve OCR performance. Knowledge of the system model parameters can also be used to determine which documents originated from the same source and, when the model includes multiple printing/scanning steps, which document was the original and which was a later generation copy.

The degradation model used for this research is convolution followed by thresholding [1]. The two most significant parameters affecting degradations of bilevel images are the point spread function (PSF) width and the binarization threshold [9]. Each pair of these values will affect an image differently. However, several combinations of these parameters will affect images in a similar fashion. The PSF accounts for the blurring caused by the optics of the scanner. Its functional form is not constrained, but needs to be specified. A form that is circularly symmetric is usually chosen so its width is determined by one parameter. The size is in units of pixels, which allows the model to be used for scanning at any optical resolution. The threshold converts the image to a bilevel image. This is often done in software, and a global threshold is assumed. The units for the threshold are absorptance. The variations in the resulting bilevel bitmaps come largely from phase effects [13].

Several methods have been proposed to calibrate this model from bilevel images [2,4,6,7]. The resulting parameter estimates will never be error-free. However, not all errors are equally bad. Some will produce characters that have similar appearances. These are likely to result in similar feature measurements and be more likely to

have the same response from an OCR system. This type of estimation error can be treated differently than estimation errors that result in a larger change in the character appearance. This paper explores the amount that character images will change statistically as the model parameters used in their generation vary and how these model parameters are related to image degradation features.

Kanungo et al. [11] proposed a method of validating degradation models. This was achieved through a nonparametric two-sample permutation test. It decided whether two images originating from the same source are close enough to each other to have passed through the same sequence of systems. The application he proposed was to decide whether a model of a character degradation produced characters that were "close" to a set of "real" characters generated by physical printing and scanning. This testing could validate the degradation model and the choice of model parameters. The underlying statistical method is not restricted to comparing real and synthetic characters. Consequently, the two images could also be two real images, or two synthetic images. This statistical testing procedure can also be used to determine which parameters of the degradation model created the sample of characters. Another statistical device, the power function, was used to choose between algorithm variables.

Kanungo et al. demonstrated their method using a bit flipping and morphological degradation model [11] and in a separate experiment [10] also using Baird's convolution and thresholding model. They measured the difference between 10 point, 300 or 400-dpi Computer Modern Roman e's with the Hamming distance as they separately varied each of the model parameters. Their approach of statistically comparing character populations is applied in this paper to the convolution and thresholding degradation model shown in Figure 1. The parameters in this model are the point spread function (PSF) width, w, and the binarization threshold, Θ. Both populations of character images were synthetically generated. Both model parameters were varied in combination to see their joint effects and to see by how much the character images created with different model parameters will vary over the regions of the joint parameter space.

This paper starts by describing two image degradations and how they relate quantitatively to the degradation model parameters. It then describes the experiment conducted using Kanungo's non-parametric permutation test to mathematically illustrate the size of the difference between two sets of degraded characters created using our model with different parameters. We then describe how the difference between character images is related to the degradation features.

2 Image Degradations:

Each model parameter set will produce a different character image. Examples of the characters that are produced for 600 dpi 12-point sans-serif font 'W' over a range of PSF widths and binarization thresholds are
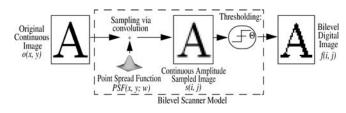

Fig. 1. Scanner model used to determine the value of the pixel (i, j) centered on each sensor element.
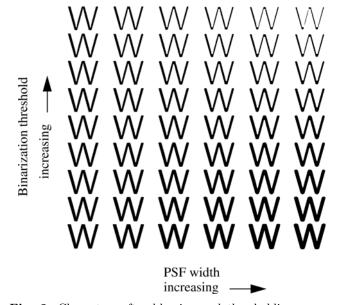

Fig. 2. Characters after blurring and thresholding over a range of PSF widths, w, and binarization thresholds, Θ. A broad range of character appearances can be seen, but some characters have general similarities.

shown in Figure 2. Some of the degradations that are introduced are common to multiple characters, such as the final thickness of the character strokes, but each character is slightly different. Two primary image degradations associated with bilevel processes were defined in [4–6]. These are the edge displacement and the erosion of a black or white corner. All these degradations are functions of the degradation model parameters, w and Θ.

During scanning, the profile of an edge changes from a step to an edge spread function, ESF, through convolution with the PSF. This is then thresholded to reform a step edge, Figure 3. The amount an edge was displaced after scanning, δ_c, was shown in [3,4] to be related to w and Θ by

$$\delta_c = -wESF^{-1}(\Theta). \tag{1}$$

The edge spread determines the change in stroke width after scanning. An infinite number of (w, Θ) values could produce any one δ_c value. Equation (1) holds when edges are considered in isolation, for example when the edges are separated by a distance greater than the support of the PSF. Figure 4 shows how the values of (w, Θ) vary for 5 different constant δ_c values for each of two
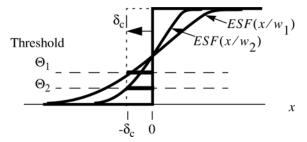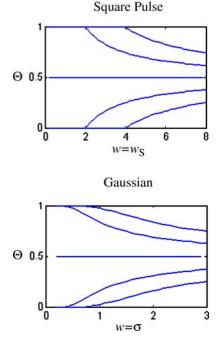
Fig. 3. Edge after blurring with a generic PSF of two widths, w. Two thresholds that produce the same edge shift δ_c are shown.
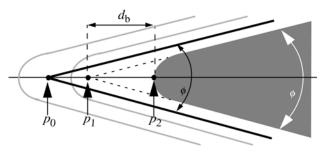

Fig. 4. Loci of constant edge spread, $\delta_c =$[-2 -1 0 1 2] (from top to bottom), for two PSF functional forms.

PSF shapes. A positive threshold value will produce a negative edge displacement. The curves for δ_c and -δ_c are symmetric around the $\Theta=1/2$ line. If $\Theta=1/2$, then $\delta_c=0$ for all values of w.

The other pair of bilevel image degradations are the amount of erosion seen in a black or a white corner after scanning [4,6]. These degradations are caused by the interaction of the two edges, but also include the displacement of the individual edges. The erosion of a corner can occur in any of the three forms shown in Figure 5. Point p_0 is the apex of the original corner. Point p_2 is the point along the angle bisector of the new rounded corner where the blurred corner equals the threshold value. Point p_1 is the point where the new corner edges would intersect if extrapolated. The distance

$$d_b = \overline{p_1 p_2} \qquad (2)$$

is not the erosion from the original corner location, but it does represent the degradation actually seen on the corner, and this quantity can be measured from bilevel

Fig. 5. The blurred corner (grey area and lines) may be displaced from the original corner position (black line) in three different ways. The visible erosion, d_b, is calculated the same for all three.

document images. The corner erosion distance, d_b, depends on the threshold, the PSF width, and the functional form similar to the edge displacement above.

The corner erosion distance is a combination of the distance from the original corner to the extrapolated corner, $\overline{p_1 p_0}$, which is based on the edge spread δ_c, and the distance along the angle bisector from the original corner to where the amplitude of the blurred corner equals the threshold, $\overline{p_1 p_2}$. Thus

$$d_b = \overline{p_1 p_2} = \overline{p_1 p_0} + \overline{p_0 p_2} \qquad (3)$$
$$= \frac{-wESF^{-1}(\Theta)}{sin(\phi/2)} + f_b^{-1}(\Theta; w, \phi)$$

where

$$f_b(d_{0b}; w, \phi) = \int_{x=0}^{x=\infty} \int_{y=-xtan\frac{\phi}{2}}^{y=xtan\frac{\phi}{2}} PSF(x-d_{0b}, y; w)dydx. \qquad (4)$$

As with edge displacement, a given amount of corner erosion can also occur for an infinite number of (w, Θ) values. The erosion of a white corner is defined similarly and results in

$$d_w(w, \Theta) = d_b(w, 1 - \Theta). \qquad (5)$$

Samples of constant d_b and d_w are shown in Figure 6.

3 Experiment

Experiments were run to statistically compare characters in pairs of populations each made with different parameters based on the method proposed by Kanungo et al. [11]. In the experiments presented in this paper, the two populations, X and Y, are both composed of synthetically generated characters created by the blurring and thresholding model with varying phase offsets [13]. The characters in population X were created with PSF width and binarization threshold parameters (w_0, Θ_0), and those in population Y with (w_1, Θ_1). The null hypothesis that these sets of characters have been drawn from populations with a common set of parameters was compared to the alternate hypothesis that they have been drawn from populations with different parameters:
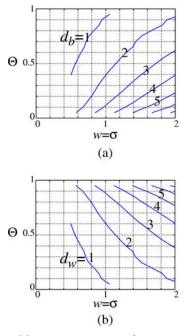
$$H_N : (w_0, \Theta_0) = (w_1, \Theta_1) \qquad (6)$$

Fig. 6. Observable erosion contours for constant erosion on (a) a black corner, d_b, and (b) on a white corner, d_w. Loci are for a Gaussian PSF and $\phi = \pi/4$.
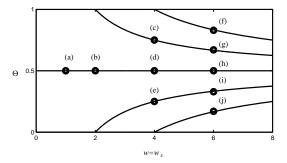
$$H_A : (w_0, \Theta_0) \neq (w_1, \Theta_1). \tag{7}$$

Each experiment consisted of the following steps:

1. Create a set of synthesized characters $X = \{x_1, x_2, ..., x_{2M}\}$ with the model parameters of $\{w_0, \Theta_0, PSF\}$.
2. Using the permutation test method, calculate the null distribution of the population and choose a threshold, d_0, to make the misdetection rate or significance level, ε, about 5%.
3. Create a set of synthesized degraded characters $Y = \{y_1, y_2, ..., y_{2M}\}$ of the same character class, using parameters $\{w_1, \Theta_1, PSF\}$.
4. Randomly permute the sets X and Y and select M characters from each.
5. Measure the distance between characters in sets X and Y to compute the distance D_k between the sets of $\{x_{k1}, x_{k2}, ..., x_{kM}\}$ and $\{y_{kM+1}, y_{kM+2}, ..., y_{k2M}\}$.
6. Repeat steps (4) and (5) K times and get K distances $D_1, D_2, ..., D_K$.
7. Compute the probability of $P\{D_k \geq d_0\} = \#\{k|D_k \geq d_0\}/K$.

The distance between individual characters was measured using the Hamming distance. The distance between sets of characters, D_k, was calculated using the trimmed mean nearest-neighbor distance. The parameter K was set to 1000. Steps (3)-(7) were repeated for several parameter sets (w_1, Θ_1) in the vicinity of (w_0, Θ_0) to generate a two-dimensional power function. This will show how likely it is that a change in system parameters will cause the characters to differ by our metric.

Experiments were conducted around several initial parameter combinations (w_0, Θ_0) to see how the location in the (w, Θ) space affects the results. The combinations of initial points (w_0, Θ_0) that were used are

Fig. 7. Set of (w_0, Θ_0) values used as null hypotheses in the sequence of experiments.

shown in Figure 7. These points were chosen to give a range of edge displacements $\delta_c = \{-2, -1, 0, 1, 2\}$ for the initial characters and to fill the (w, Θ) space. The initial character image used was a 600-dpi 12-point sans-serif 'W'. The PSF form was a square pillbox with a base width $w = w_s$.

The two-dimensional power functions for several (w_0, Θ_0) are shown as contour images in Figure 8. These contours show the place where the probability of rejecting the null hypothesis is constant over a range of alternate parameters (w_1, Θ_1). The probability of rejecting the null hypothesis is less than 0.1 in the centers of the contour areas. It is 1 in the area outside of the contour lines. The blockiness in the contour shapes is caused by the quantization in the range of (w_1, Θ_1) values used in the experiments and the Matlab interpretation of the contour.

The constant reject probabilities have a shape similar to the constant edge spread contours shown in Figure 4. This is more easily seen in Figure 9, where the hypothesis reject probability contours from Figure 8 have been superimposed on plots of the δ_c loci. The edge spread degradation has the predominant effect on the appearance of a character visually [5] and, from these results, also statistically.

To show the sensitivity of this procedure, consider the corresponding sets of characters in Figure 10a and b which are created with parameters that are very close. All the characters in set a were generated with a common set of model parameters $(w_a, \Theta_a) = (0.4, 0.50)$. The characters in set b were produced with model parameters $(w_b, \Theta_b) = (0.4, 0.55)$. While these two pairs of model parameters are very close, and the characters in sets a and b appear similar, the null hypothesis that the populations from which these characters came were generated with the same parameters was rejected with probability equal to 1. In [5] it was proposed that characters with a common δ_c value would appear most similar to humans, while other degradation features, such as d_b and d_w, change the character's appearance less. This similarity is now quantified through statistical testing.

Maintaining a constant δ_c increases the probability of the characters appearing similar, but they are only similar within a small range of (w, Θ) values. Figure 11 shows sample characters with pairs having a common δ_c. The
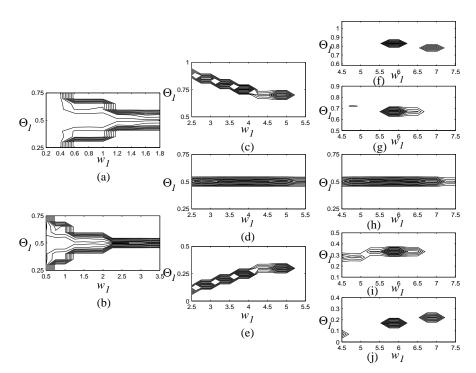
Fig. 8. Probability of rejecting null hypotheses with the letter 'W' using the Hamming distance between characters. (a) $(w_0, \Theta_0) = (1.0, 0.5)$, (b) $(2.0, 0.5)$ (c) $(4.0, 0.75)$, (d) $(4.0, 0.5)$, (e) $(4.0, 0.25)$, (f) $(6.0, 0.83)$, (g) $(6.0, 0.67)$, (h) $(6.0, 0.5)$, (i) $(6.0, 0.33)$, (j) $(6.0, 0.17)$. The interior regions have a probability of less than 0.1.
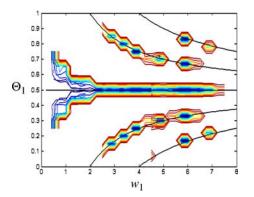

Fig. 9. Composite showing results from Figure 8 superimposed over constant δ_c lines.
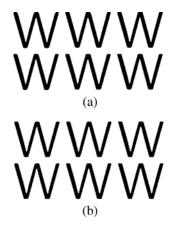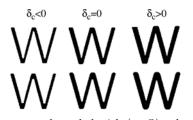

Fig. 10. Synthetic characters created at two (w, Θ) combinations with varying phase offsets. (a) $(w, \Theta) = (0.4, 0.50)$, (b) $(w, \Theta) = (0.4, 0.55)$. The characters in the two sets look the same but are decided to be from different parameter sets with probability of 1.

first column shows $\delta_c < 0$, the middle $\delta_c = 0$, the right $\delta_c > 0$. For characters with a positive δ_c (low threshold), the characters have thicker strokes, whereas with negative δ_c, the characters have thinner strokes. The pairs of characters in Figure 11 look similar, but the differences can be easily seen because the model parameters used to create them are very different, more so than in Figure 10. The places where the characters with common δ_c differ most is at the corners.

While the δ_c value has remained the same, the corner erosion and thus the character appearance is different. For $\delta_c > 0$, $(\Theta < 1/2)$ the d_b isolines are almost perpendicular to the δ_c isolines, and for $\delta_c < 0$ $(\Theta > 1/2)$ the d_w isolines are almost perpendicular to the δ_c isolines. When w and $|\Theta - 1/2|$ are large, a small change in (w, Θ)

Fig. 11. Characters degraded with (w, Θ) values to produce negative, zero and positive δ_c values. Each character has a different (w, Θ) .

will produce a larger change in the d_b and d_w values (see Figure 6). This causes the size of the region of low probability of rejecting the null hypothesis in Figure 8f,g,i and j to be smaller than the corresponding regions in Figure 8c and e.

A similar set of experiments was run using a 600-dpi 12-point sans-serif 'O' over a subset of the cases used for the letter 'W'. The 'O' character has approximately the same stroke width for the whole character but contains no corners. The resulting power function contours are shown in Figure 12. When the plots are compared to the plots for the corresponding null hypothesis for the 'W' shown in Figure 8a,c,e,g,h and i, the appearance of the same general shape can be seen. What is different, particularly for $(w_0, \Theta_0) = (6, 0.67)$ and $(6, 0.33)$, is the probability of rejecting the null hypothesis being less than 1 extends for a larger range of values for the letter 'O'. This is due to the absence of corners. The degradation seen in the characters is only due to the edge spread for a large range of (w, Θ) values. With an absence of corners, no corner erosion is present. However, the edge spread was defined for edges that are isolated from each other, and when the PSF width is large enough, this premise is no longer valid [12]. The edges will interfere, and an effect similar to the corner erosion will occur degrading the character images. The corner erosion is a special case of two edges spreading with interference, where the overlap occurs at any PSF support width because the distance between the edges at the corners is zero.

Another experiment was conducted to degrade 12-point 300-dpi sans-serif 'W' characters. Now the width of the strokes in pixels is significantly smaller than before. The results are shown in Figure 13. Again the general shape of the power function contours matched the countours of Figure 8 and the edge displacement lines. Because the stroke widths for the 300-dpi characters were significantly smaller in pixels than for the 600-dpi characters of earlier experiments, the extent of the power function contours was smaller too.

To see whether this effect was restricted to use of the Hamming distance for measuring difference between character images, the same set of experiments was repeated for the 300-dpi 'W', but the distance between individual characters was measured using the distance between the corresponding moment feature vectors. The moments that were used are eight central moments. The resulting two dimensional power functions are shown in Figure 14. The same basic shape as was seen earlier for the Hamming distance (Figures 8 and 13) is also present here. The similarities follow the constant δ_c regions. The similarity regions are small when θ is greater than 0.5 because the characters are smaller than previously.

For lower thresholds the moment feature distance lead to larger regions of similarity than present when the Hamming distance metric was used. The black corners on the upper left and right of the 'W' are most likely to erode because they have a smaller angle measure, ϕ. Changing the value of a single pixel at these corners of the 'W' has a larger effect on the change in the moment features than changing a single pixel at an interior corner location where the corners happen to be white.

Therefore the model paramters that have a constant d_b are more likely to be considered similar than for model parameters with a constant d_w (see Figure 6).

4 Conclusion

A statistical test was conducted to compare the similarity between groups of characters synthetically generated as the parameters (w, Θ) were varied over the two-dimensional parameter space. Prior experiments [11] varied individual degradation parameters and evaluated the size of the power function to choose between algorithm variables. In this paper the focus is on the interaction between the model parameters. Analysis showed that the amount of variation in the characters correlated highly with the change in the edge spread degradation, δ_c. This edge spread can be quantified in terms of the degradation system model parameters (w, Θ). This relationship was present for two similarity metrics: Hamming distance and moment feature distance.
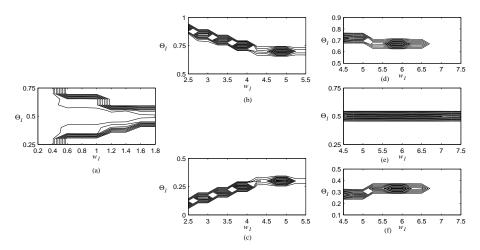
Degradation models may be used in the future to generate synthetic characters for use in OCR experiments. This research can be used to decide how to distribute model parameters if we want to experiment with characters with small differences, or larger differences that are evenly distributed. Experiments were conducted with the characters 'W' and 'O' at two effective scanning resolutions. This gives more insight on how the shape of a character will influence the variation in the resulting bitmap. Characters with many corners, thin strokes, or variable width strokes will remain similar over a smaller range of (w, Θ) values.

The statistical difference between characters could also be used as a metric of model parameter estimation error. When estimating the degradation model parameters, errors along the δ_c isolines will not produce as large of a difference in the characters generated with the model as would an error perpendicular to these isolines, especially for characters with fewer corners. Because w and Θ are not in the same units, conventional metrics like Euclidean or city-block are not reasonable for combining errors in these two estimates. Also, simply adding a scaling factor will not necessarily help because we do not know how to equate width and threshold units and there may not be a linear relationship between the two units. But if we measure error in units of character difference, we can use this information to fine tune the defect model, better predict what the true model paramters should be, and evaluate the accuracy and effectiveness of the model. This could lead to meaningful improvements in performance.

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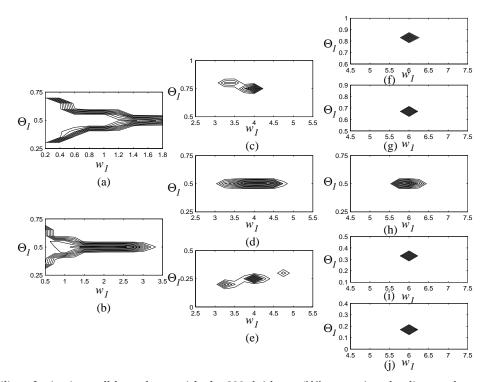

Fig. 13. Probability of rejecting null hypotheses with the 300-dpi letter 'W' measuring the distance between characters with the Hamming distance. (a) $(w_0, \Theta_0) = (1.0, 0.5)$, (b) $(2.0, 0.5)$ (c) $(4.0, 0.75)$, (d) $(4.0, 0.5)$, (e) $(4.0, 0.25)$, (f) $(6.0, 0.83)$, (g) $(6.0, 0.67)$, (h) $(6.0, 0.5)$, (i) $(6.0, 0.33)$, (j) $(6.0, 0.17)$. The center regions of each contour have a probability of less than 0.1.

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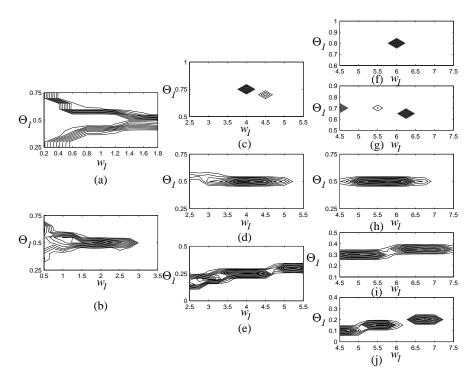8. L. R. Blando, J. Kanai, and T. A. Nartker. Prediction of OCR accuracy using simple features. In *Proc. of*

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Fig. 14. Probability of rejecting null hypotheses with the 300-dpi letter 'W' using the distance between moment feature vectors. (a) $(w_0, \Theta_0) = (1.0, 0.5)$, (b) $(2.0, 0.5)$ (c) $(4.0, 0.75)$, (d) $(4.0, 0.5)$, (e) $(4.0, 0.25)$, (f) $(6.0, 0.83)$, (g) $(6.0, 0.67)$, (h) $(6.0, 0.5)$, (i) $(6.0, 0.33)$, (j) $(6.0, 0.17)$. The center regions of each contour have a probability of less than 0.1.

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