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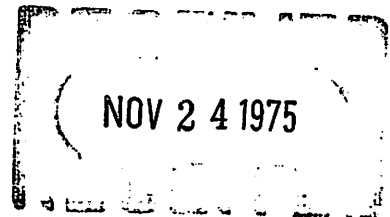
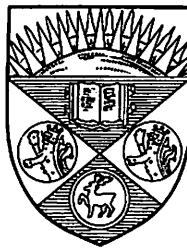
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Discussion Paper 005

THE TIMING OF RESIDENTIAL LAND DEVELOPMENT:
A GENERAL EQUILIBRIUM APPROACH

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RESEARCH PROGRAM:
IMPACT OF THE PUBLIC
SECTOR ON LOCAL ECONOMIES



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1. Introduction

Rapidly rising residential land prices in major North American metropolitan areas have generated a growing amount of public discussion and occasional legislative action. Implicit in much of this discussion seems to be the notion that this rise in land prices is at least partly attributable to the existence of a group of land developers or "speculators."¹ These developers are thought to cause high land prices insofar as they withhold land from sale to builders in hopes of higher prices in the future. The result of this type of investment or speculative behavior is said to be socially undesirable in that it implies a slower rate of land development and higher land prices than are socially acceptable. Further, this process is thought to result in a redistribution of income away from the community at large in favour of the land developers. It is not unnatural, therefore, that this conceptual model of land development should result in legislation to speed development, reduce land prices, and tax away capital gains realized by land developers and other land investors.²

The land development process is not well understood, however, and many of our ideas about the land market are borrowed from analyses of other types of markets.³ These ideas, which form the foundation of our legislative proposals, may be inappropriate for a number of reasons. Unlike housing units or capital goods, for example, the supply of land of given

characteristics (e.g., commuting distance to the city centre) is fixed in the long run in any metropolitan area. Any decision to develop land for residential use, therefore, necessarily reduces the total stock of undeveloped land with these characteristics by the amount of land developed. Since land developer's timing of transactions will clearly reflect this fact, any analysis of land pricing ought to be placed in a dynamic framework.

Perhaps the most important difference between the land market and other markets occurs on the demand side. Consumers receive satisfaction from the flow of services derived from the stock of residential land they own. The flow demand for new residential land in any period is best thought of as a stock adjustment demand. Further, there is virtually no depreciation on land. This implies that increased sales of developed land in the current period will, ceteris paribus, decrease the demand for new residential land in future periods. A developer must realize that sales of land by competitors in the present period will affect the future demand for, and therefore the value of his holdings.

This paper will examine these issues by constructing a formal model of the development process in order to arrive at a better understanding of the timing of residential land development, the change in land prices over time, and the effects of various legislative actions on these variables. Of particular interest will be the relationship between market structure and land prices and the timing of land development. The paper demonstrates that with land in fixed supply, a monopolist is less likely to develop all his land than a competitive development industry within a given time horizon. If demand is sufficient for a monopolist to profitably develop all his land, however, monopoly generally cannot lead to both a slower rate of development and a steeper rate of price appreciation than would occur

under conditions of competition.

Other results of the paper include a demonstration that the institution of a property tax or a capital gains tax must reduce the initial period price of developed land in a competitive situation. It is further shown that a capital gains tax will lead to a higher rate of land development and a higher rate of price appreciation than would prevail in the absence of the tax. Questions of tax incidence and the distinction between Ricardian rents and returns to market power are also dealt with.

The model presented here makes a number of simplifying assumptions in order to focus clearly on the intertemporal patterns of land sales and land prices in a general equilibrium framework.⁴ Perhaps most important, land is assumed to be homogeneous (both physically and spatially) and in fixed supply. Therefore, all land transacted in a given time period must bear the same price. An indirect justification of this approach, which considerably simplifies the mathematical complexity of the model, can be found in Markusen and Scheffman (1975a). In that paper, the authors argue that a meaningful measure of ownership concentration in the urban land market should be formulated in terms of subsets of relatively homogeneous land. A static spatial model is then used to demonstrate that a landowner who owns a "large" percentage of all land at a fixed commuting distance from the city always has potential market power regardless of how small his holdings are as a percentage of all urban land.

2. Demand for Residential Land

Let us begin by constructing a two-period model in which a fixed stock of land, initially held by a group referred to as developers, is prepared for residential construction and sold to consumers over the course

of two time periods.⁵ It is perhaps conceptually useful to think of these two periods as being the present and future, and therefore the periods are not necessarily of equal length. Developers may perform servicing functions such as subdivision, sewer installation, and road building, so serviced land will be referred to as developed land. It is assumed that consumers have no alternative sources of land and that consumers contract for housing construction once they have purchased land.⁶ The purpose of this assumption is to keep a clear distinction between land and housing prices, the former being the focus of this paper.

Let us first consider the determinants and properties of the demand for land of an individual consumer. If we conceive of our model as a small community in the middle of a large free trade region, we can assume that all commodities are traded with the region and the commodity prices to the small community are fixed. These prices are then independent of the price of land, the distribution of income, etc. Various types of housing units that consumers can construct on their land are numbered among these commodities. This assumption that commodity prices are fixed to the community allows us to make use of the composite commodity theorem to aggregate all commodities into a single composite commodity and to express preferences as a function of the composite commodity and the stock of land held by the consumer.⁷ Denoting the composite commodity purchased in time T as C_T and the purchase of land in time T as L_T , the consumer's two period utility function is given by:

$$(1) \quad U = U_0(C_0, L_0) + U_1(C_1, L_0 + L_1)$$

where U_i gives the present value of the flow of utility at $T=i$ and where U_i is assumed to have the usual quasi-concave properties. Additivity is

assumed only for the convenience of graphical exposition. $(L_0 + L_1)$ appears as an argument in U_1 since utility at time $T=1$ is derived from the total amount of land owned by the consumer and not just from land purchased at $T=1$. It is important to remember in what follows that L_1 is the incremental demand for land in period 1. A final assumption of this formulation is that land does not depreciate.

The composite commodity is used as numeraire and community income in period T in terms of C_T is denoted Y_T ,⁸ where Y_T is known with certainty. p_T will denote the price of land in period T in terms of C_T .

The consumer makes consumption plans for both periods by maximizing his two period utility function subject to a budget constraint that discounts future income and expenditures at a rate i . This rate may be an actual mortgage rate or it may include an added premium for risk.⁹ In either case, the budget constraint allows the consumer to borrow or lend subject only to the condition that the present value of the income stream equal the present value of the expenditure stream. The consumer's demand functions are then given as the solution of the problem:

$$(2) \quad \text{Max } U_0(C_0, L_0) + U_1(C_1, L_0 + L_1)$$
$$\text{s.t. } (Y_0 + Y_1(1+i)^{-1} - C_0 - C_1(1+i)^{-1} - p_0L_0 - p_1(1+i)^{-1}L_1) = 0$$

The first order necessary conditions for a maximum are given as follows:

$$(3) \quad \frac{\partial}{\partial C_0} = U_{01} - \lambda \leq 0$$

$$\frac{\partial}{\partial L_0} = U_{02} + U_{12} - \lambda p_0 \leq 0$$

$$\frac{\partial}{\partial C_1} = U_{11} - \lambda(1+i)^{-1} \leq 0$$

$$\frac{\partial}{\partial L_1} = U_{12} - \lambda p_1(1+i)^{-1} \leq 0$$

plus the constraint condition. Two results are of particular interest:

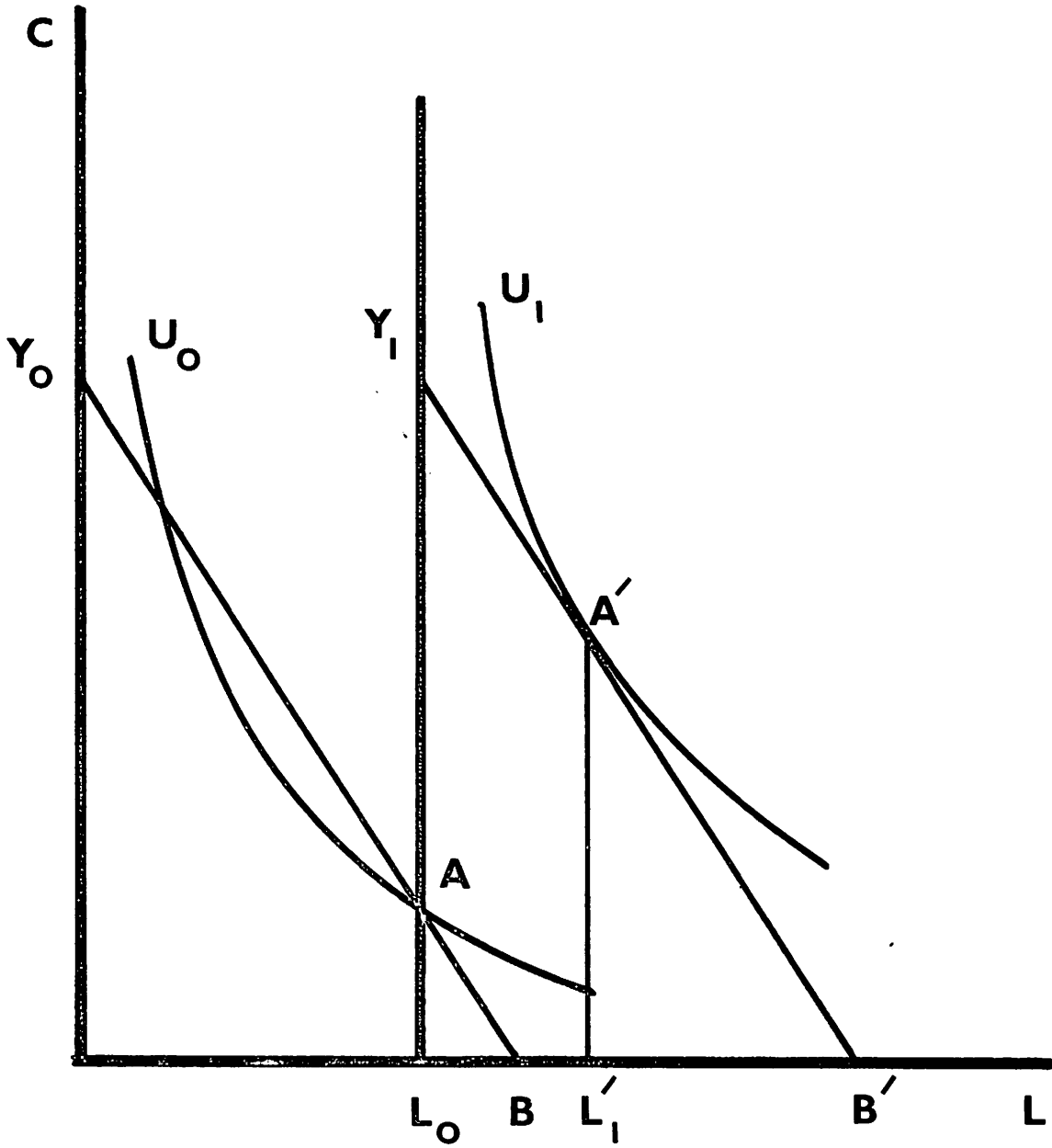
$$(4) \quad \frac{U_{02} + U_{12}}{U_{01}} = p_0 \quad \text{if } C_0, L_0 > 0$$

$$\text{if } p_0 - p_1(1+i)^{-1} \leq 0 \text{ then } L_1 = 0$$

The first equation in (4) states that the marginal rate of substitution between L_0 and C_0 will be less than p_0 . Since L_0 also gives utility at $T=1$, L_0 is purchased past the point where the usual marginal rate of substitution condition holds. The second equation in (4) states that if the price of land is growing as fast as the rate of interest, consumers will wish to purchase all land in $T=0$ since the cost of borrowing is less than the costs imposed by price appreciation.

This situation is shown in Figure I where it is assumed for convenience that $Y_0 = Y_1$, $p_0 = p_1$, and that the consumer does not choose to borrow or lend. The budget line in $T=0$ is given by Y_0B and the optimal consumption bundle, characterized by the marginal rate of substitution less than the price ratio, in $T=0$ is given by A. The consumption bundle for

Figure I



$T=1$ is found by shifting the budget line to Y_1B' . The optimal consumption bundle is now given by point A' with purchases of land in $T=1$ equal to $(L_1' - L_0)$. The sum of U_0 and U_1 give the consumer's total welfare from this allocation. Borrowing an amount X at $T=0$ can be conveniently represented in this diagram by a parallel shift out of Y_0B an amount X on the vertical axis and a parallel shift of Y_1B' equal to $X(1+i)$ in the opposite direction.

Our discussion of the demand functions of an individual consumer lead us to specify market demand functions of the form

$$L_0 = D_0(p_0, p_1, Y_0, Y_1, i)$$

(5)

$$L_1 = D_1(p_0, p_1, Y_0, Y_1, i)$$

where Y_T is the vector of incomes of consumers at time T . Assuming that both C_i and L_i are normal goods, $(\partial D_i / \partial p_i) < 0$. The properties of these demand functions are discussed in more detail in Appendix I. It is sufficient to note here that two additional properties of these demand functions are assumed to hold for the remainder of the paper. First, it is assumed that an increase in the price of land in either period diminishes the total two period demand for land. In other words, $\partial(L_0 + L_1) / \partial p_i < 0$, for $i = 0, 1$. What is ruled out is the possibility that an increase in p_0 , for example, will lead to an increase in L_1 that outweighs the decrease in L_0 . Although this seems to be a reasonable assumption, it is not implied by our previous assumptions. Second, we assume that land in different periods are gross substitutes, i.e., $\partial D_i / \partial p_j > 0$, $i \neq j$.

3. Supply by Developers - Perfect Competition

Developers in this urban area own an amount of land, \bar{L} , which is assumed to encompass the totality of developable land. In this section we assume that each developer owns only a small amount of \bar{L} , so that developers can be assumed to be price takers. The prices of developed land at time zero and one, p_0 and p_1 , are assumed to be known with certainty.

In each period a developer can develop and sell any part of his holdings. The costs of development per unit of land are assumed to be constant and identical in each period, and will be denoted by s . This constant is used to represent such costs as lot servicing and subdivision approval. Any land not developed in a given period earns a return from agricultural production which is assumed to be a constant per unit of land and identical in each period. This agricultural return is denoted by q . Land which is developed during a particular period does not earn any return from agricultural use.

The rate of return on assets judged by developers to be equivalent to land will be denoted by r . The supply of land in each period can now be described as the solution of the problem

$$(6) \quad \max_{\{L_0, L_1\}} p_0 L_0 + p_1 (1+r)^{-1} L_1 - s L_0 - s(1+r)^{-1} L_1 \\ + q(\bar{L} - L_0) + q(1+r)^{-1} (\bar{L} - L_0 - L_1) \\ \text{s.t. } L_0 + L_1 - \bar{L} \leq 0; L_0, L_1 \geq 0$$

The first order conditions for a maximum are¹⁰

$$(7) \quad \partial/\partial L_0 = p_0 - s - q - q(1+r)^{-1} - \lambda \leq 0$$

$$\partial/\partial L_1 = (1+r)^{-1}[p_1 - s - q] - \lambda \leq 0$$

$$L_0 + L_1 - \bar{L} \leq 0$$

where λ is the Lagrangean multiplier associated with the constraint on developable land, with $\lambda \geq 0$.

The first order conditions require that a necessary condition for land to be developed in period i , is that the present value of land developed net of development costs, $\sum (p_i - s_i)(1+r)^{-i}$, must be at least as large as the present value of the land in agricultural use, $\sum_{j=i}^1 q(1+r)^{-j}$. If $\lambda > 0$, then all land is sold over the course of the two periods and λ can be interpreted as the Ricardian rent required for land to be sold at time zero. In this case (7) can be interpreted as requiring that Ricardian rents appreciate at rate r for land to be supplied in each period. Notice that even if all land is not sold in period zero, the land sold in that period can still earn positive Ricardian rents. This result is contrary to the usual analysis of Ricardian rents in static models, where the Ricardian factor can only earn positive rents if demand calls for the total supply. This is another indication of the inappropriateness of using static models to analyze land markets.

Since developed land typically commands a price above its opportunity cost in agriculture, for the remainder of this paper we will assume that $\lambda > 0$. Therefore all land will be developed over the two period horizon. In this case (7) requires that the Ricardian rent at time zero, λ , must grow at rate r for land to be sold in each period. Assuming $\lambda > 0$, the first two equations of (7) give us the following supply characteristics:

$$(8a) \quad (L_0, L_1) = \begin{cases} (\bar{L}, 0), & \text{if } p_0 - p_1(1+r)^{-1} > q + [s - s(1+r)^{-1}] \\ (0, \bar{L}), & \text{if } p_0 - p_1(1+r)^{-1} < q + [s - s(1+r)^{-1}] \\ (L_0, \bar{L} - L_0), L_0 \geq 0, & \text{if } p_0 - p_1(1+r)^{-1} = q + [s - s(1+r)^{-1}] \end{cases}$$

This can also be written

$$(8b) \quad (L_0, L_1) = \begin{cases} (\bar{L}, 0), & \text{if } \frac{p_1 - p_0}{p_0} < r - [q(1+r) + sr]/p_0 \\ (0, \bar{L}), & \text{if } \frac{p_1 - p_0}{p_0} > r - [q(1+r) + sr]/p_0 \\ (L_0, \bar{L} - L_0), L_0 \geq 0, & \text{if } \frac{p_1 - p_0}{p_0} = r - [q(1+r) + sr]/p_0 \end{cases}$$

The interpretation of (8a) and (8b) is straightforward. If land is sold in each period then the rate of price appreciation must be less than r , with the equilibrium rate of price appreciation being an increasing function of p_0 , or equivalently, of λ . Alternatively, developers will be indifferent to sales in the two periods if the difference between the present price of developed land (p_0) and the present value of future price ($p_1(1+r)^{-1}$) is just equal to the agricultural revenue foregone by developing at $T=0$ instead of $T=1$ (q) plus the burden of incurring development costs at $T=0$ rather than at $T=1$ ($s - s(1+r)^{-1}$).

Notice that in an equilibrium where land is sold in each period, prices may fall. This is explained by the fact that although equilibrium requires Ricardian rents to appreciate, since the present value of agricultural production at $T=1$ is less than the present value at $T=0$, developers may not develop at $T=0$ unless p_0 exceeds p_1 . However, the rate of change of prices is algebraically larger the higher the price of developed land (p_0)

relative to the yearly return from agriculture (q). As developed land becomes more and more valuable, positive land sales in each period require a positive rate of price appreciation approaching r , the rate of return on equivalent assets.

4. Market Equilibrium

Given the assumption that demand is sufficient for all land to be developed in the two periods, the following equilibrium conditions will obtain in the land market:

$$(9) \quad D_0 = S_0$$

$$D_1 = S_1$$

$$D_0 + D_1 = S_0 + S_1 = \bar{L}$$

where S_i denotes market supply in period i . Assuming positive sales in each period for the moment, we also have the supply condition:

$$(10) \quad p_0 = p_1(1+r)^{-1} + q + [s - s(1+r)^{-1}]$$

or

$$p_1 = p_0(1+r) - q(1+r) - rs$$

For fixed values of Y_i , we can use equation (5) to write our equilibrium condition as follows:

$$(11) \quad D_0(p_0, p_0(1+r) - q(1+r) - rs) + D_1(p_0, p_0(1+r) - q(1+r) - rs) = \bar{L}$$

Equation (11) reduces the equilibrium conditions to a single equation in one unknown (p_0).

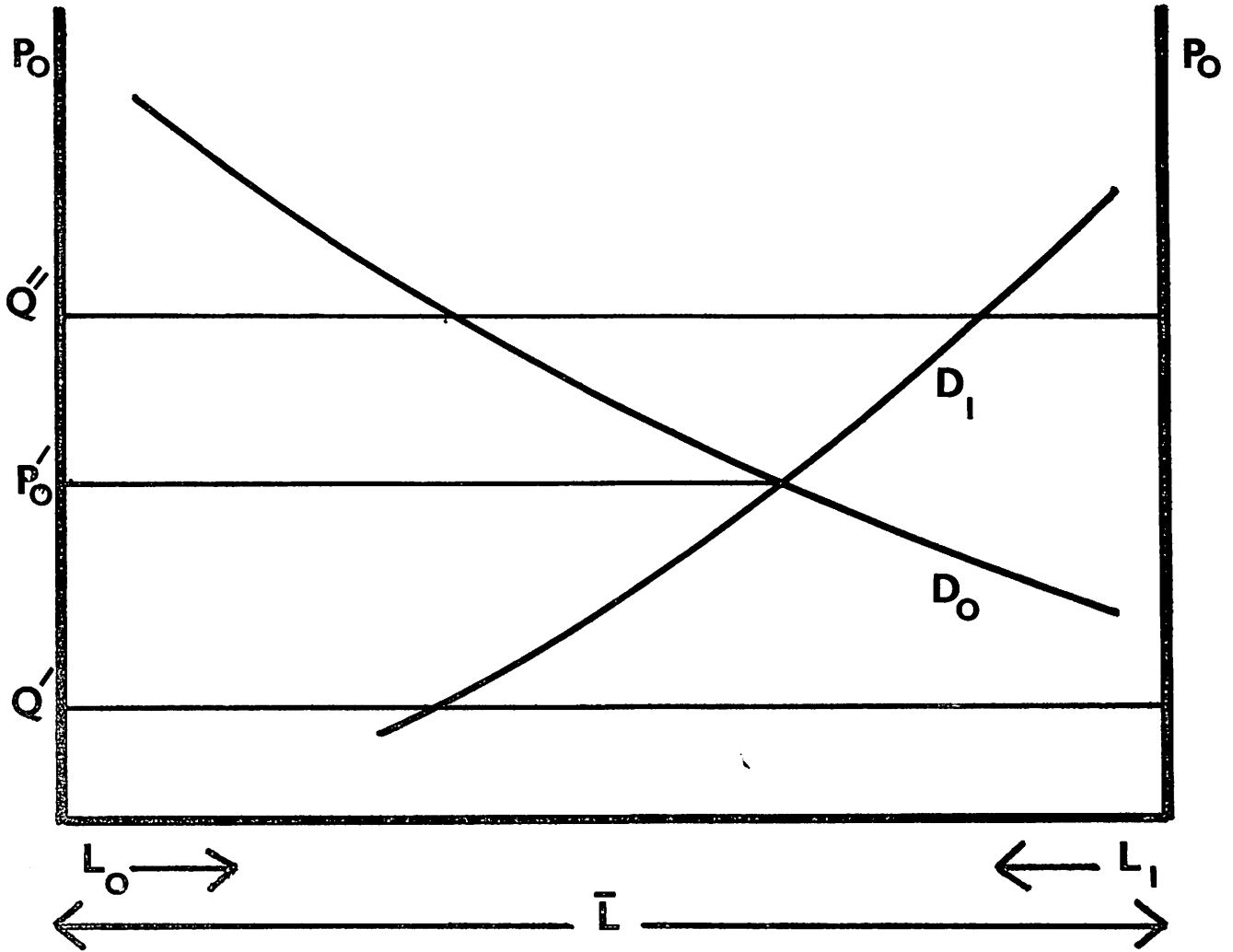
A graphical representation of equation (11) is given in Figure II, where D_0 and D_1 are the first and second period demand curves. We have assumed that a rise in either p_0 or p_1 will, ceteris paribus, cause a decrease in the total demand for $L(\partial(L_0 + L_1)/\partial p_i < 0)$. But equation (10) shows that positive land sales in each period require that p_1 be an increasing linear function of p_0 . It follows, therefore, that the total excess demand for land must decrease as p_0 increases. This condition is satisfied in Figure II where both D_0 and D_1 decrease as p_0 (and therefore p_1) increases. Equilibrium will be at the intersection of D_0 and D_1 provided that $Q = q(1 + (1+r)^{-1}) + s$, representing total opportunity costs, is less than the value of p_0 at this intersection. $Q = Q'$ in Figure II provides an example. If $Q = Q''$ in Figure II, not all of \bar{L} will be developed and the equilibrium values of L_0 and L_1 will be given by the respective intersections of D_0 and D_1 with Q'' .

The solution shown in Figure II is not the only possibility that satisfies the requirement that increases in p_0 and p_1 reduce total excess demand. D_0 may be upward sloping provided that its slope is less than the absolute value of the slope of D_1 . Similarly, D_1 may slope upward provided that its slope is less than the absolute value of the slope of D_0 . These conditions are required by our assumption $d(L_0 + L_1)/dp_i < 0$, since

$$d D_0(p_0, p_0(1+r) - q(1+r) - rs)/dp_0 + d D_1(p_0, p_0(1+r) - q(1+r) - rs)/dp_0 = [D_{00} + D_{10}] + (1+r)[D_{01} + D_{11}] = d(L_0 + L_1)/dp_0 + (1+r)d(L_0 + L_1)/dp_1 < 0.$$

A final possibility is that the two demand curves do not cross. If D_i is the upper curve, a corner solution at $L_i = \bar{L}$ will occur provided that the corresponding price exceeds Q . If the corresponding price is less than Q , equilibrium will occur at the value of L_i where $p_0 = Q$.

Figure II



5. Taxation and Market Equilibrium - Perfect Competition

We will now consider the effect of two different types of taxes on the competitive equilibrium. First consider the effect of a property tax, assessed at an ad valorem rate τ . We assume that developers are taxed on the developed value of their holdings, net of development costs, at the beginning of each period. Therefore competitive supply is given as the solution of

$$(12) \quad \max_{\{L_0, L_1\}} \quad p_0 L_0 + p_1 (1+r)^{-1} L_1 - \tau(p_0 - s)(L_0 + L_1) - \tau(p_1 - s)(1+r)^{-1} L_1 \\ - sL_0 - s(1+r)^{-1} L_1 + q(\bar{L} - L_0) + q(1+r)^{-1} (\bar{L} - L_0 - L_1) \\ \text{s.t. } L_0 + L_1 - \bar{L} \leq 0; \quad L_0, L_1 \geq 0$$

Assuming that demand is sufficient for all land to be developed and for some land to be developed in each period, the first order conditions require

$$(13) \quad p_0 - p_1 (1+r)^{-1} (1 - \tau) = q + [s - s(1+r)^{-1} (1 - \tau)]$$

We assume that consumers must pay property tax at $T=1$ on the value (at $T=1$) of land purchased at $T=0$. Therefore the discounted value of their property tax payments is $\tau p_1 (1+r)^{-1} L_0$. This tax then has the effect of changing the consumer's price of L_0 from p_0 to $p_0 + \tau p_1 (1+r)^{-1}$. Therefore $D_i = D_i(p_0 + \tau p_1 (1+r)^{-1}, p_1)$. For demand to be sufficient for all land to be developed we must have

$$(14) \quad D_0(p_0 + \tau p_1 (1+r)^{-1}, p_1) + D_1(p_0 + \tau p_1 (1+r)^{-1}, p_1) = \bar{L}$$

Differentiating (13) and (14) with respect to τ ,

$$(15) \quad dp_0/d\tau - (1+r)^{-1} (1-\tau)dp_1/d\tau = (s-p_1)(1+r)^{-1}$$

$$(D_{00} - D_{10})dp_0/d\tau + [(D_{01} + D_{11}) + (D_{00} + D_{10})\tau(1+r)^{-1}]dp_1/d\tau$$

$$= -(D_{00} + D_{10})p_1(1+r)^{-1}$$

Solving for $dp_0/d\tau$ and $dp_1/d\tau$ from (15), we have

$$(16) \quad dp_0/d\tau = [(s-p_1)(1+r)^{-1} [(D_{01} + D_{11}) + (D_{00} + D_{10})\tau(1+r)^{-1}]$$

$$- (1+r)^{-2} (1-\tau)p_1(D_{00} + D_{10})]/\Delta$$

$$dp_1/d\tau = -s(1+r)^{-1} (D_{00} + D_{10})/\Delta$$

where Δ is the determinant of the matrix of coefficients of (15).

Given the assumption that a rise in p_i , ceteris paribus, reduces the total two period demand for land ($D_{i1} + D_{j1} < 0$), it follows that $dp_0/d\tau < 0$, $dp_1/d\tau < 0$. Thus the property tax reduces land prices in both periods.

The first order conditions for (12) (assuming land is supplied in each period) can also be written

$$(17) \quad \frac{p_1 - p_0}{p_0} = r + \tau p_1/p_0 - [q(1+r) + s(r+\tau)]/p_0$$

Letting $(\frac{p_1 - p_0}{p_0})^*$ be the equilibrium rate of price appreciation for $\tau = 0$,

and $(\frac{p_1 - p_0}{p_0})^{**}$ be the corresponding rate for $\tau > 0$, (17) can be written

$$(18) \quad (\frac{p_1 - p_0}{p_0})^{**} = (\frac{p_1 - p_0}{p_0})^* + \tau(p_1 - s)/p_0$$

so that the imposition of a property tax increases the equilibrium rate of price appreciation. We would expect that this would result in a higher

equilibrium value for L_0 and a lower value for L_1 than would occur in the absence of the tax. However, since p_0 and p_1 both fall, the effect on equilibrium supplies is ambiguous.¹¹

Next, we can consider a tax on realized capital gains such as the Ontario Land Speculation Tax. Assume that the value of land sales in period $T=1$ in excess of the value of that land had it been sold in period $T=0$ is subject to an ad valorem rate of the tax θ . Since development costs are constant, the developed price may be used as a base. Competitive supply is then given by the solution of the following problem:

$$(19) \quad \max_{\{L_0, L_1\}} p_0 L_0 + p_1(1+r)^{-1} L_1 - \theta(p_1 - p_0)(1+r)^{-1} L_1 - sL_0 \\ - s(1+r)^{-1} L_1 + q(\bar{L} - L_0) + q(1+r)^{-1} (\bar{L} - L_0 - L_1) \\ \text{s.t. } L_0 + L_1 - \bar{L} \leq 0; \quad L_0, L_1 \geq 0$$

where we restrict our treatment to the case where $p_1 > p_0$. Assuming land is supplied in each period, the first order necessary conditions for an interior maximum give:

$$(20) \quad p_0(1 - \theta(1+r)^{-1}) - p_1(1+r)^{-1} (1 - \theta) = q + (s - s(1+r)^{-1})$$

or

$$\frac{p_1 - p_0}{p_0} = \frac{r - [q(1+r) + sr]/p_0}{(1 - \theta)}$$

Differentiating (20) and (5), we have

$$(21) \quad \frac{(1 - \theta + r)}{(1 - \theta)} \frac{dp_0}{d\theta} - \frac{dp_1}{d\theta} = \frac{p_0 - p_1}{1 - \theta}$$

$$(D_{00} + D_{10}) \frac{dp_0}{d\theta} + (D_{01} + D_{11}) \frac{dp_1}{d\theta} = 0 .$$

Solving for $dp_0/d\theta$ and $dp_1/d\theta$ from (21),

$$(22) \quad dp_0/d\theta = \left(\frac{p_0 - p_1}{1 - \theta} \right) (D_{01} + D_{11})/\Delta$$

$$dp_1/d\theta = \left(\frac{p_1 - p_0}{1 - \theta} \right) (D_{00} + D_{10})/\Delta$$

where Δ is the determinant of the matrix of coefficients of (21). Again assuming that $D_{ii} + D_{ji} < 0$, we see that $dp_0/d\theta < 0$, $dp_1/d\theta > 0$. We can also write the second equation of (20) as

$$(23) \quad \left(\frac{p_1 - p_0}{p_0} \right)^{**} = (1 - \theta)^{-1} \left(\frac{p_1 - p_0}{p_0} \right)^*$$

so that the tax also increases the equilibrium rate of price appreciation. Since we have assumed that $D_{ij} > 0$, $i \neq j$ (our assumption of gross substitutes), it is easily seen that $dD_0/d\theta > 0$, $dD_1/d\theta < 0$.

The conclusion here is that, with a fixed stock of land that is to be developed within a given time horizon, a capital gains tax will speed the conversion of undeveloped land into final use. Coincident with this higher rate of development, will be a higher rate of increase in the price of land over time than would occur in the absence of these taxes. If the assumptions of this model are a reasonable description of reality, government policymakers cannot hope to use this tax instrument to simultaneously reduce the rate of increase in land prices and speed development. With land in fixed supply, an increase in the rate of development in initial periods must be paid for by higher prices in later periods.

One final point worth noting concerns the incidence of these taxes. The usual result in a situation where a commodity is in completely inelastic supply is that the supplier bears all of the tax. This is not

generally true in this model, since the intertemporal pattern of supply is altered even though total supply remains constant. The present value of consumer payments for \bar{L} (equal to $p_0 L_0 + p_1 (1+i)^{-1} L_1$) may either increase or decrease following the taxes depending upon the distribution of purchases between $T=0$ and $T=1$ and the change in the equilibrium price ratio, p_1/p_0 .

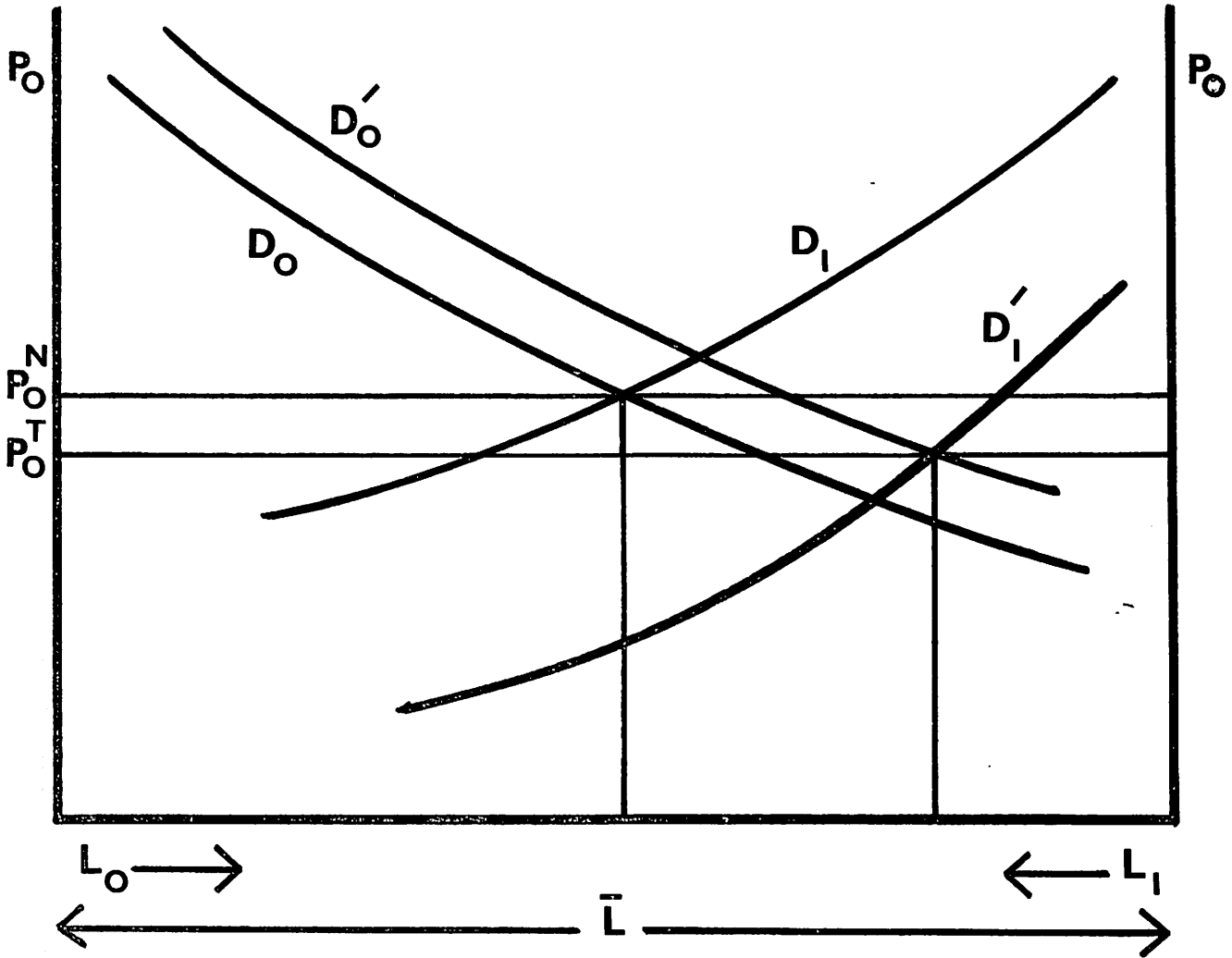
One possible situation for the capital gains tax is shown graphically in Figure III where D_i and D_i' are, respectively, the before and after tax demand curves for period i . p_0^N and p_0^T denote the before and after tax equilibrium prices. The producer equilibrium condition (20) for positive land sales in each period requires that p_1 increase for every value of p_0 . Assuming that L_1 is a normal good, D_1 must decrease at every p_0 as shown in Figure III. Assuming L_0 and L_1 are gross substitutes, D_0 will increase at every p_0 . Because $\partial(L_0 + L_1)/\partial p_1 < 0$, the diagram must be as shown with $p_0^T < p_0^N$.

As a final point, note that this tax on realized capital gains cannot cause a reduction in total land developed. The reason for this is given in equations (7), (8a), and (8b) which show that the equilibrium rate of price appreciation becomes negative as the equilibrium value of p_0 approaches Q . Since this implies negative capital gains, the tax cannot be effective in driving p_0 below Q .

6. Monopoly and Market Equilibrium¹²

As suggested earlier in the paper, a common notion seems to be that conditions of monopoly generally lead to a smaller supply and a higher price for the commodity in question. This section will investigate the rate of land sales to final users and the path of price increases over time under monopoly and compare the results to the competitive equilibrium

Figure III



described earlier.

With incomes fixed, the demand functions in (4) can be expressed in inverse form by

$$(24) \quad p_0 = p_0(L_0, L_1)$$

$$p_1 = p_1(L_0, L_1)$$

It follows from our earlier assumption that $\partial p_i / \partial L_j > 0$ for $i \neq j$.

Profit maximizing sales by the monopolist are given as the solution of:

$$(25) \quad \begin{aligned} \text{Max}_{\{L_0, L_1\}} \quad & p_0(L_0, L_1)L_0 + p_1(L_0, L_1)(1+r)^{-1} L_1 - s L_0 - s(1+r)^{-1} L_1 \\ & + q(\bar{L} - L_0) + q(1+r)^{-1} (\bar{L} - L_0 - L_1) \end{aligned}$$

$$\text{s.t.} \quad L_0 + L_1 - \bar{L} \leq 0; \quad L_0, L_1 \geq 0 .$$

If we define the marginal revenue of land sales in period i as the changes in the present value (evaluated at $T=i$) of total revenue with respect to the change in L_i , the first-order conditions for (25) can be expressed:

$$(26) \quad \begin{aligned} MR_0 &= p_0 + \frac{\partial p_0}{\partial L_0} L_0 + \frac{\partial p_1}{\partial L_0} (1+r)^{-1} L_1 \\ &= p_0 \left(1 + \frac{1}{\eta_{00}} + (1+r)^{-1} \frac{R_1}{R_0} \cdot \frac{1}{\eta_{01}} \right) \leq s + q[1 + (1+r)^{-1}] + \lambda \end{aligned}$$

$$\begin{aligned} MR_1 &= p_1 + \frac{\partial p_1}{\partial L_1} L_1 + (1+r) \frac{\partial p_0}{\partial L_1} L_0 \\ &= p_1 \left(1 + \frac{1}{\eta_{11}} + (1+r) \frac{R_0}{R_1} \frac{1}{\eta_{10}} \right) \leq s(1+r) + q + \lambda \end{aligned}$$

where R_i is total sales revenue in period i ($R_i = p_i L_i$), and η_{ij} is the elasticity of demand in period i with respect to p_j , and λ is the Lagrangean multiplier associated with the constraint on developable land, with $\lambda \geq 0$.

One important result that does follow from the first order conditions is that the monopolist is less likely than the competitor to develop all the land. The competitor will be willing to develop if the developed land price less development costs equals the agricultural opportunity costs. The monopolist will not be willing to develop where marginal revenue less development costs equal the agricultural opportunity cost. Since the average (over $T=0,1$) marginal revenue earned by land must be less than average price, there must be levels of demand for which the competitive industry will develop all the land, but for which the monopolist will not. In such a case, the monopoly price in each period may exceed the corresponding price under competitive conditions.

Assume now that demand is sufficient for all land to be developed within the two periods.¹³ For $\lambda > 0$ in equation (26), the monopolist earns a combination of Ricardian rents and returns to market power. This fact would seem to be quite important in view of the tendency of policymakers to see high land prices only as returns to market power. The solution to (21) can, in this case, be characterized by the following relationships:

$$(27) \quad (L_0, L_1) = \begin{cases} (\bar{L}, 0), & \text{if } MR_0 - MR_1(1+r)^{-1} > q + [s - s(1+r)^{-1}] \\ (0, \bar{L}), & \text{if } MR_0 - MR_1(1+r)^{-1} < q + [s - s(1+r)^{-1}] \\ (L_0, \bar{L} - L_0), L_0 \geq 0, & \text{if } MR_0 - MR_1(1+r)^{-1} = q + [s - s(1+r)^{-1}] \end{cases}$$

The expressions in (27) are the same as those in (8a), except that

prices have been replaced by marginal revenues.

Earlier results have demonstrated that the difference between p_0 and p_1 determines directly the equilibrium pattern of supply. Assuming land is supplied in each period, the last equations of (27) and (8a) provide an explicit comparison of the equilibrium prices under the two market structures. Letting p_i^C denote equilibrium market price in period i under competition, and p_i^M the corresponding price under monopoly, subtracting the conditions for positive supplies in each period in (27) (using (26)) from the equivalent expression in (8a), we have:

$$(28) \quad (p_0^C - p_0^M) - (p_1^C - p_1^M)(1+r)^{-1} \\ = p_0^M \left(\frac{1}{\eta_{00}} + (1+r)^{-1} \frac{R_1}{R_0} \frac{1}{\eta_{01}} \right) - p_1^M (1+r)^{-1} \left(\frac{1}{\eta_{11}} + (1+r) \frac{R_0}{R_1} \frac{1}{\eta_{10}} \right)$$

Since $d(L_0 + L_1)/dp_i < 0$ by assumption, if all land is developed under both competition and monopoly, then $(p_0^C - p_0^M)(p_1^C - p_1^M) < 0$, and $(L_0^C - L_0^M)(L_1^C - L_1^M) < 0$. This is because if the price in each period was higher under monopoly, total demand would be less than \bar{L} . In other words, if the monopoly price at $T=1$ exceeds the competitive price in the same period, then the monopoly price in $T=0$ must be less than the corresponding competitive price if total two period demand is to equal \bar{L} in each case. In such a situation, monopoly will lead to a faster rate of land development and a faster rate of price appreciation than would result under competition. Assuming that the bracketed elasticity expressions in (28) are negative (i.e., that marginal revenue as defined here is less than price in each period), the general result is:

$$(29) \quad \frac{p_0^M \left(\frac{1}{\eta_{00}} + (1+r)^{-1} \frac{R_1}{R_0} \frac{1}{\eta_{01}} \right)}{p_1^M (1+r)^{-1} \left(\frac{1}{\eta_{11}} + (1+r) \frac{R_0}{R_1} \frac{1}{\eta_{10}} \right)} \begin{cases} < 1, p_0^C > p_0^M, L_0^C < L_0^M \\ > 1, p_0^C < p_0^M, L_0^C > L_0^M \\ = 1, p_0^C = p_0^M, L_0^C = L_0^M \end{cases}$$

Under fairly general sets of assumptions, there seems to be no reason for believing that this term would be either greater or less than one. The conclusion of this section, therefore, is that, with a fixed stock of land to be developed within a given time horizon, a monopolist may or may not develop land faster than a perfect competition industry depending upon the relevant elasticities given above. This is explained by the fact that the rate of supply and the rate of price increase work in opposite directions. The optimal trade off between these two depends on these demand elasticities. The only thing we can be certain about is that, unless (29) equals 1, equilibrium prices, rate of price appreciation, and rate of development will be different from the competitive equilibrium. Thus unless (29) equals 1, resources will be misallocated. It is possible, however, that demand conditions exist such that (29) equals 1, implying that the competitive and monopoly solutions are identical. Although the monopolist still has market power, he does not find it profitable to exercise it.

Notice that except in the unusual case that the monopoly and competitive solutions are identical, in one period monopoly profits will necessarily be smaller than the corresponding competitive Ricardian rents! This shows that it would be incorrect to attempt to verify the existence of exercised market power by measuring the profits of large landowners in a given period. If competitive prices were known, the difference between the present value of the monopolist's profits and the present value of

Ricardian rents would measure the present value of the returns to market power.

In Appendix II we present a simple analytic example which compares competitive and monopoly development for linear demand functions.

7. Taxation and Market Equilibrium - Monopoly

The effects of property and capital gains taxes under monopoly conditions will be treated very briefly since these effects depend on demand conditions. The monopolist's problem in the case of the property tax is stated as follows:

$$(30) \quad \text{Max}_{\{L_0, L_1\}} p_0 L_0 + p_1 (1+r)^{-1} L_1 - \tau(p_0 - s)(L_0 + L_1) - \tau(p_1 (1+r)^{-1} - s(1+r)^{-1}) L_1 \\ - sL_0 - s(1+r)^{-1} L_1 + q(\bar{L} - L_0) + q(1+r)^{-1} (\bar{L} - L_0 - L_1)$$

$$\text{s.t. } L_0 + L_1 - \bar{L} \leq 0 \quad L_0, L_1 \geq 0$$

$$p_0 = p_0(L_0, L_1) \quad p_1 = p_1(L_0, L_1)$$

If demand is such that all land is developed and some land is developed in each period, the first order necessary conditions for a maximum give us the following:

$$(31) \quad MR_0^* - MR_1^* (1+r)^{-1} (1-\tau) = q + [s - s(1+r)^{-1} (1-\tau)]$$

$$MR_0^* = p_0 \left[1 + (1-\tau) \left(1 + \frac{L_1}{L_0} \right) \right] \frac{1}{\eta_{00}} + (1+\tau)(1+r)^{-1} \frac{R_1}{R_0} \frac{1}{\eta_{01}}]$$

$$MR_1^* = p_1 \left[1 + \frac{1}{\eta_{11}} + ((1+r) \frac{R_0}{R_1} - \left(\frac{\tau}{1-\tau} \right)) \frac{1}{\eta_{10}} \right]$$

In the case of the capital gains tax, the monopolist's problem is given as follows:

$$(32) \quad \text{Max}_{\{L_0, L_1\}} p_0 L_0 + p_1 (1+r)^{-1} L_1 - \theta (p_1 - p_0) (1+r)^{-1} L_1 - s L_0 - s (1+r)^{-1} L_1 \\ + q(\bar{L} - L_0) + q(1+r)^{-1} (\bar{L} - L_0 - L_1)$$

Assuming again that all land is developed and some land is developed in each period, the first order necessary conditions give us the following:

$$(33) \quad MR'_0 (1 + \theta(1+r)^{-1}) = MR'_1 (1+r)^{-1} (1 - \theta) = q + (s = s(1+r)^{-1})$$

$$MR'_0 = p_0 [1 + (1 - \theta(1+r)^{-1})^{-1} \left(\frac{1}{\eta_{00}} + \frac{R_1}{R_0} \frac{1}{\eta_{01}} \right)]$$

$$MR'_1 = p_1 \left[1 + \frac{1}{\eta_{11}} + (1+\theta)^{-1} \left((1+r) \frac{R_0}{R_1} + \theta \frac{p_0}{p_1} \right) \frac{1}{\eta_{10}} \right]$$

The rate of price appreciation and the pattern of land development resulting from the institution of these taxes in the monopoly case cannot be compared to the no tax equilibrium without specific knowledge of the demand elasticities. As in the case of comparing monopoly equilibrium to competitive equilibrium, we see that the results depend upon the nature of demand. Once again, the explanation lies in the price quantity trade off. In the case of the capital gains tax, for example, tax payments equal $\theta(p_1 - p_0)L_1$. If the monopolist increases sales in $T=0$, L_1 decreases but $(p_1 - p_0)$ must increase. This latter effect is not considered by competitors who take prices as given. Whether or not it is profitable for the monopolist to increase sales at $T=0$ depends on the nature of this trade off. Determinate effects of this tax in the competitive case then become indeterminate in

the monopoly situation.

8. Summary and Conclusions

1. For low levels of demand, a competitive development industry will supply developed land at a price equal to the present value of agricultural returns plus development costs. For higher levels of demand for land in fixed supply, developers will supply land such that the price of developed land appreciates at a rate equal to the developer's discount rate, r , less an amount relating the opportunity costs of land development to current developed land prices. Ricardian rents on land appreciate at rate r and the rate of price appreciation approaches r as the price of developed land becomes high relative to land's yearly return from agriculture. Given the dynamic nature of demand, it is also noted that Ricardian rents on land are generally positive despite the fact that only a small part of total supply may be transacted in any one period.

2. With land in fixed supply, a monopolist is less likely to develop all his land than a competitive development industry within the same time horizon. If demand is sufficient for the monopolist to profitably develop all his land, however, he may develop it faster than the competitive industry. The monopolist's problem is to weigh the trade off between a low rate of development and a high rate of price appreciation. In such a situation, the existence of monopoly power is not sufficient for the exercise of monopoly power and, therefore, for resource misallocation. If market power is exercised and all land is developed, then in one period monopoly profits are lower than the associated competitive Ricardian rents.

3. In the competitive case, a property tax or a capital gains tax

will reduce the initial period price of developed land. The property tax will also reduce the second period price and increase the equilibrium rate of price appreciation. The capital gains tax will lead to a higher rate of development and a higher rate of price appreciation than would prevail in the absence of the tax. The capital gains tax cannot reduce the total amount of land developed over time.

4. In the situation where demand is sufficient for competitive developers to profitably develop all their land, it does not follow that the incidence of these taxes falls entirely on the developers. The optimal trade off depends on the exact nature of consumer demand. Although their total supply is perfectly inelastic, these taxes lead to an inter-period reallocation of development. The present value of total consumer payments for land will be altered and may decrease, a situation that might be termed a negative tax incidence.

5. The effect of these taxes on the monopolist's supply is indeterminate. With an ad valorem tax on capital gains, for example, the monopolist can reduce the quantity component of total capital gains (equal to price change times quantity) only at the expense of increasing the price change component.

Appendix I

This section will provide a discussion of the comparative statics properties derived in the section on demand. A difficulty is that even the assumptions that land in each period is a normal good and that the composite consumption good is a net substitute for land in each period may not guarantee one property of demand that we have assumed. This is the property that a rise in p_0 , ceteris paribus, reduces the total two period demand for land ($\partial(L_0 + L_1)/\partial p_0 < 0$). We will analyze this property for an individual consumer's demand functions. The problem then is that if L_0 and L_1 are gross substitutes, the (positive) pure-cross-substitution effect $(\partial L_1/\partial p_0)_{\bar{u}}$ may outweigh the (negative) pure-own-substitution effect $(\partial L_0/\partial p_0)_{\bar{u}}$ and the income effects $L_0(\partial L_1/\partial Y_0)$. It can be shown, however, that this possibility ceases to exist if the equilibrium rate of price appreciation is high enough.

A well-known demand theorem states that the sum of price-weighted pure-substitution effects must equal zero. In this context, that reduces to

$$(A1) \quad p_0 \left(\frac{\partial L_0}{\partial p_0} \right)_{\bar{u}} + p_1(1+i)^{-1} \left(\frac{\partial L_1}{\partial p_0} \right)_{\bar{u}} + \left(\frac{\partial C_0}{\partial p_0} \right)_{\bar{u}} + (1+i)^{-1} \left(\frac{\partial C_1}{\partial p_0} \right)_{\bar{u}} = 0$$

Since $p_0 > p_1(1+i)^{-1}$ when the equilibrium is characterized by positive land sales in each period, the assumption that the composite consumption good in any period and L_0 are net substitutes $\{(\partial C_i/\partial p_0)_{\bar{u}} > 0\}$ is not sufficient to imply the absolute value of $(\partial L_0/\partial p_0)_{\bar{u}}$ outweighs a positive $(\partial L_1/\partial p_0)_{\bar{u}}$. (The same argument does establish that $\partial(L_0 + L_1)/\partial p_1 < 0$.) The sum of the two effects, however, must become negative as the rate of price appreciation approaches i . Adding the influence of income effects then guarantees that, for a range of rates of price appreciation less than i ,

$\partial(L_0 + L_1)/\partial p_0 < 0$. It should also be noted that this property will hold for all rates of price appreciation that give interior solutions for many types of utility functions such as additive forms.

A second problem referred to in the section on market equilibrium deals with the possibility that all land will be withheld until $T=1$. From the first order conditions in (3), a price configuration such that $L_0 = 0$ implies that $U_{02} + U_{12} - \lambda p_0 < 0$. Manipulation of these conditions gives us the result that $L_0 = 0$ and $L_1 > 0$ if and only if:

$$(A2) \quad \frac{p_1 - p_0}{p_0} < i - \frac{U_{02}}{U_{01}} (1+i)/p_0$$

where U_{02}/U_{01} is the positive marginal rate of substitution between the composite commodity and land in $T=0$. Similarly, the supply conditions given in (8) states that equilibrium will be characterized by $(L_0 = 0, L_1 > 0)$ if and only if:

$$(A3) \quad \frac{p_1 - p_0}{p_0} > r - [q(1+r) + rs]/p_0$$

This equilibrium is less likely the higher the developers' discount rate relative to the consumers' rate and the higher the price of developed land relative to the return from agricultural land use. It should also be noted that with many commonly-used functional forms such as the Cobb-Douglas, the marginal rate of substitution U_{02}/U_{01} , becomes very large as L_0 approaches zero, implying that an equilibrium characterized by $L_0 = 0$ cannot exist.

Appendix II

This section will provide a simple analytic example that shows how the timing of land sales under conditions of monopoly will differ from the timing of land sales under conditions of perfect competition.

The demand functions for land in each period are assumed to be given by the following:

$$(C1) \quad \begin{aligned} L_0 &= \alpha_0 - b p_0 + \gamma b p_1 \\ L_1 &= \alpha_1 - b p_1 + \gamma b p_0 \end{aligned}$$

For the time being, it is assumed that $0 < \gamma < 1$.¹⁴ α_1 might be larger relative to α_0 if, for example, consumer tastes shift in favour of housing over time.

For algebraic simplicity, it is assumed that agricultural opportunity costs and development costs equal zero. The monopolist's problem is to maximize the following function:

$$(C2) \quad \begin{aligned} &\text{Max } p_0(1+r)L_0 + p_1L_1 + \lambda(\bar{L} - L_0 - L_1) \\ &= (\alpha_0 - b p_0 + \gamma b p_1)(1+r)p_0 + (\alpha_1 - b p_1 + \gamma b p_0)p_1 \\ &\quad + \lambda(\bar{L} - (\alpha_0 + \alpha_1) - (1 - \gamma)b p_0 - (1 - \gamma)b p_1) = 0 \\ \\ &\frac{\partial}{\partial p_0} = (\alpha_0 - 2b p_0 + \gamma b p_1)(1+r) + \gamma b p_1 - \lambda(1 - \gamma)b = 0 \\ \\ &\frac{\partial}{\partial p_1} = (\alpha_1 - 2b p_1 + \gamma b p_0) + \gamma b(1+r)p_0 - \lambda(1 - \gamma)b = 0 \end{aligned}$$

Manipulation of these first order conditions gives us the following relationships:

$$(C3) \quad \frac{1}{\sigma} (\alpha_0(1+r) - \alpha_1) = \Delta p_0 - p_1$$

where $\sigma = (2+r)\gamma b + 2b > 0$

$$\Delta = \frac{(2+r)\gamma b + (1+r)2b}{(2+r)\gamma b + 2b} < (1+r)$$

A sufficient (but not necessary) condition for p_1 to be greater than p_0 is that the intercept term be growing faster than the discount rate r . Since $\Delta < (1+r)$, however, this is not sufficient for the equilibrium price ratio to exceed $(1+r)$, the ratio that will prevail in this example under competitive conditions.

The conclusion is that, with linear demand of this type, growth in demand below the market rate of interest will always lead the monopolist to supply less land in initial periods than would be supplied by a competitive market. On the other hand, for growth in demand sufficiently in excess of the discount rate, a monopolist will supply relatively more land in initial periods, leading to a rate of price increase in excess of the discount rate. Allowing the slope coefficients (b) and the cross effects coefficients (γ) to vary between periods will change the numerical values of σ and Δ in (V3) but will not change the direction of the relationship, provided that $\gamma > -2/(2+r)$. γ can, of course, be negative if the pure cross substitution effect is less than the absolute value of the cross income effect.

FOOTNOTES

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¹The term "developer" is often reserved for a land investor who makes improvements to land (e.g., subdivision and lot servicing) before selling that land. "Speculators" on the other hand, are often thought of as land investors who buy and sell land without making improvements in hopes of realizing pure capital gains. Under these definitions, developers may be thought of as speculators who also engage in land improvement. Realizing pure capital gains on land is typically just as much a part of a developer's activities as making profits on land improvements. This paper will, therefore, restrict itself to a consideration of land "developers," who are assumed to pursue profits both from pure capital gains and from land improvements.

²An example of legislation which embodies this view of the land development process is the Ontario Land Speculation Tax, which was enacted in 1974. This Act taxes the capital gains on sales of land which have not been suitably developed by the seller.

³All of the works listed under References in some way deal with the issue of the behavior of land investors and how they perceive demand conditions. See, for example, Bahl (1968), Bentick (1972), Clawson (1962), Morris (1969), and Shoup (1969). For an analysis of land investment when land is a factor of production, see Nichols (1970).

⁴Many of the papers referenced below arrived at questionable results due to their partial equilibrium nature. More specifically, they assume that "demand for land" grows monotonically over time (interpreted to mean an outward shift in Marshallian demand curve) in a way that is most conveniently expressed by a concave function $V(T)$ which gives the value of land holdings at time T (see, for example, Bahl (1968) and Shoup (1969)). This approach assumes away all interesting aspects of the problem and guarantees a number of results a priori. For example, the (unjustified) assumption that $V(T)$ is strictly concave ensures us that the institution of the property tax will reduce the optimal length of time that an investor will hold land. For one attempt to actually explain the equilibrium increase in valuation over time, see Bentick (1972).

⁵For the purposes of this paper, the assumption of two periods is important in that it assumes a fixed time horizon but not in that it assumes only two periods. All conclusions will be essentially valid in a multi-period model. Also, it should be noted that landowners may sell land among themselves as may consumers. Any sale by a landowner to a consumer, however, is assumed to be irreversible.

⁶Although this assumption is admittedly unrealistic, it is true that the building and development industries are often quite separate. In Toronto, for example, few developers have building divisions of any consequence. The building industry is composed of a great many small companies, most of whom buy serviced building lots for immediate construction. Further, total holdings of undeveloped land by individuals and builders is small compared with holdings by development companies. See Markusen and

Scheffman (1975b).

⁷The purpose of this assumption is to reduce the general equilibrium model to the problem of determining a single relative price.

⁸This model is concerned with the determination of relative prices. Changes in nominal prices are found by multiplying through equation (2) in each period by a price index.

⁹Of course, if p_1 is an expected price (a random variable) then plans made at the beginning of the initial period must be revised when the actual price is observed in the second period.

¹⁰Besides r including the appropriate risk premium, this is one point at which simple uncertainty could be introduced into the model. If p_1 is made a random variable reflecting the landowner's expectations, for example, maximization of expected profits will lead to the same condition as given in (7) except that p_1 will be replaced by $E(p_1)$ (the expected value of p_1). If a risk preference function is introduced which is characterized by risk aversion, (7) will be replaced by some expression involving the expected utility of sales revenue.

¹¹It should also be noted that the change in initial period land price in response to the property tax relates to a number of discussions concerning capitalization of the property tax. See, for example, Oates (1969). It should also be noted that government involvement of any sort in the land market creates another form of uncertainty in that government policy is subject to frequent and arbitrary changes. This issue has been

raised by Bahl (1968).

¹²Two recent studies of the Toronto area have suggested that a small number of the large developers own a large percentage of the available land. A candidate running for the provincial parliament of Ontario claimed that two developers owned more than 90% of the available land in London, Ontario (a city of approximately 250,000). As in any discussion of monopoly, the analysis and conclusions developed in this section are applicable in oligopolistic situations if the landowner in question either behaves in a Cournot fashion or has fixed expectations about the reactions of other landowners to his sales behavior. With more sophisticated behavior, a game theoretic approach is needed.

¹³This is not an unreasonable assumption in the context of this perfect certainty model, since otherwise it would mean that the monopolist had intentionally accumulated more land than he planned to sell.

¹⁴This is equivalent to assuming that the pure cross substitution effect is larger than the absolute value of the pure cross income effect.

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