

# Excellent energy storage performance in $\text{Bi}_{0.5}\text{Na}_{0.5}\text{TiO}_3$ -based lead-free high-entropy relaxor ferroelectrics via B-site modification

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**Abstract:** Next-generation advanced high/pulsed power capacitors urgently require dielectric materials with outstanding energy storage performance.  $\text{Bi}_{0.5}\text{Na}_{0.5}\text{TiO}_3$ -based lead-free materials exhibit high polarization, but the high remanent polarization and large polarization hysteresis limit their applications in dielectric capacitors. Herein, high-entropy perovskite relaxor ferroelectrics  $(\text{Na}_{0.2}\text{Bi}_{0.2}\text{Ba}_{0.2}\text{Sr}_{0.2}\text{Ca}_{0.2})(\text{Ti}_{1-x}\text{Zr}_x)\text{O}_3$  are designed by adding multiple ions in the A-site and replacing the B-site  $\text{Ti}^{4+}$  with a certain amount of  $\text{Zr}^{4+}$ . The newly designed system showed high relaxor feature and slim polarization–electric ( $P$ – $E$ ) loops. Especially, improved relaxor feature and obviously delayed polarization saturation were found with the increasing of  $\text{Zr}^{4+}$ . Of particular importance is that both high recoverable energy storage density of  $6.6 \text{ J/cm}^3$  and energy efficiency of 93.5% were achieved under  $550 \text{ kV/cm}$  for the ceramics of  $x = 6$ , accompanying with excellent frequency stability, appreciable thermal stability, and prosperous discharge property. This work not only provides potential dielectric materials for energy storage applications, but also offers an effective strategy to obtain dielectric ceramics with ultrahigh comprehensive energy storage performance to meet the demanding requirements of advanced energy storage applications.

**Keywords:**  $(\text{Bi}_{0.5}\text{Na}_{0.5})\text{TiO}_3$ ; high-entropy perovskite ceramics; relaxor ferroelectrics (RFEs); polarization saturation; energy storage density

## 1 Introduction

Owing to charming characteristics such as ultra-high power density, swift charge–discharge speed, long lifespan, and excellent thermal stability, ceramic dielectric capacitors have been widely utilized in numerous advanced high/pulsed power electronic systems [1–3]. Nevertheless, their storage density is unable to meet the great requirement of miniaturization and integration [4]. Generally, the energy storage performance of a dielectric capacitor is evaluated by the recoverable energy-storage density ( $W_{\text{rec}}$ ) and energy storage efficiency ( $\eta$ ), which can be calculated from the integral of polarization–electric ( $P$ – $E$ ) field loop by Eqs. (1)–(3):

$$W_{\text{tot}} = \int_0^{P_m} E dP \quad (1)$$

$$W_{\text{rec}} = \int_{P_r}^{P_m} E dP \quad (2)$$

$$\eta = \frac{W_{\text{rec}}}{W_{\text{tot}}} \times 100\% \quad (3)$$

where  $W_{\text{tot}}$  is total energy storage density,  $P_m$  is the saturated polarization,  $P_r$  is the remanent polarization, and  $E$  is the applied electric field [5,6]. Based on the above equations, it can be deduced that the high energy storage density requires high breakdown strength ( $E_b$ ), large  $P_m$ , and minimal  $P_r$ .

Relaxor ferroelectrics (RFEs) exhibit a slim hysteresis loop with large  $P_m$  and near-zero  $P_r$  due to the existence of polar nanoregions (PNRs), making them possess both high  $W_{\text{rec}}$  and  $\eta$  [7,8]. Generally, PNRs can be obtained by breaking long-range ordered domains in ferroelectrics (FEs), experimentally realized by doping heterogeneous ions to cause local compositional inhomogeneity and ion disorder [9,10]. Based on this consideration, a large amount of  $\text{BaTiO}_3$ - and  $(\text{Bi}_{0.5}\text{Na}_{0.5})\text{TiO}_3$ -based RFE materials has been developed, such as  $\text{BaTiO}_3$ – $\text{CaZrO}_3$  [11],  $\text{BaTiO}_3$ – $\text{Bi}(\text{Mg}_{2/3}\text{Nb}_{1/3})\text{O}_3$  [12],  $(\text{Bi}_{0.5}\text{Na}_{0.5})\text{TiO}_3$ – $\text{BaTiO}_3$  [13],  $(\text{Bi}_{0.5}\text{Na}_{0.5})\text{TiO}_3$ – $\text{SrTiO}_3$  [14],  $(\text{Bi}_{0.5}\text{Na}_{0.5})\text{TiO}_3$ – $\text{AgNb}_{0.5}\text{Ta}_{0.5}\text{O}_3$  [15], and  $(\text{Bi}_{0.5}\text{Na}_{0.5})\text{TiO}_3$ – $\text{NaNbO}_3$  [16], which greatly optimized energy storage performance. However, the above relaxor systems are hard to further improve the ion disorder by chemical doping due to the Gibbs phase rule, which leads to the restriction of relaxor feature [17,18].

Recently, “high-entropy ceramics” (HECs), which consist of five or more ionic oxides that are mixed in a near equiatomic

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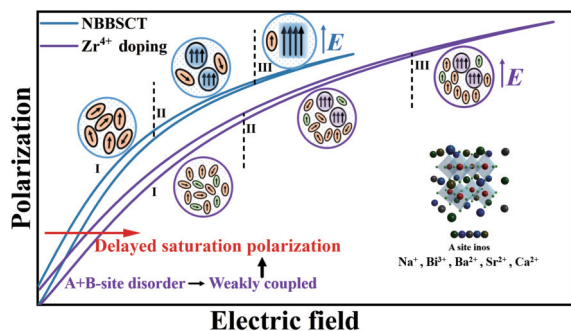
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ratio, have received great attention due to their unique composition, structure, and potential electrical properties [19]. In HECs, due to the existence of an ordered sub-lattice, the differentiation between cation lattice sites is small since each has the same immediate surroundings [20]. Therefore, a large number of quasi-equivalent sites in a crystal with an intermediate sub-lattice will increase the distribution homogeneity of cations [21]. Of particular importance is that, random distributed multi-elements result in compositional disorder that reduces short-range order. Thus, it is easier to form isolated polar nanoclusters rather than long-range ordered domains in a dielectric HECs matrix. This characteristic makes it more likely to obtain a high relaxor feature and benefit for good energy storage performance [10,22]. This has been experimentally confirmed in some (K,Na)NbO<sub>3</sub>-[23], Bi<sub>4</sub>Ti<sub>3</sub>O<sub>12</sub>-[24] based ferroelectrics, in which highly disorder distributed ions were observed, which showed great slimmer *P*-*E* loops, significantly improved energy storage density, and efficiency.

Bi<sub>0.5</sub>Na<sub>0.5</sub>TiO<sub>3</sub> possesses high spontaneous polarization, which makes it promising for energy storage applications, but the large remanent polarization and hysteresis restrict its usage. By deliberately doping multiple ions (Ba<sup>2+</sup>, Sr<sup>2+</sup>, Ca<sup>2+</sup>) with different ionic radii and valence states in the A site and forming homogeneous solid solution, new high-entropy ceramics, (Na<sub>0.2</sub>Bi<sub>0.2</sub>Ba<sub>0.2</sub>Sr<sub>0.2</sub>Ca<sub>0.2</sub>)TiO<sub>3</sub> (NBBSCT), were developed [25]. Due to the random distribution of different ions, the local compositional disorder occurs and generates PNRs. Nevertheless, the polarization still tends to saturate at the electric field far prior to their respective dielectric breakdown strength, due to the fast growth of PNRs to form micro-domains, as shown in Fig. 1. This feature restricts its further improvement in energy storage density, despite the high energy storage efficiency. That is to say, delaying the polarization saturation is of particular importance for improving the energy storage properties in the NBBSCT system.

It should be noticed that the local compositional disorder and PNRs of NBBSCT system are mainly caused by the aliovalence A-site ions. In fact, the B-site ions also contribute to the relaxor feature in a ferroelectric system [23]. On the basis of the A-site disorder, an additional B-site disorder may further break the size of PNRs and weaken the coupling between PNRs. The highly broken and weak coupled PNRs may restrict their growth into micro-domains under high electric fields, thereby leading to slimmer *P*-*E* loops and further prolonged polarization saturation, as shown in Fig. 1.

It is reported that zirconium (Zr) is one of the most explored isovalent substitutions for titanium (Ti). Zhu *et al.* [26] indicated that Zr<sup>4+</sup> modified (Bi<sub>0.5</sub>Na<sub>0.5</sub>)TiO<sub>3</sub>-based ceramics exhibited superior energy storage properties, owing to the optimization of *E*<sub>b</sub> and delaying of polarization saturation. Meanwhile, the



**Fig. 1** Schematic design strategy of high-entropy ceramics to tailor *P*-*E* loops and associating changes of PNRs.

substitution of Ti<sup>4+</sup> with Zr<sup>4+</sup> is also an effective modification method in the perovskite ferroelectric ceramic system to promote the generation of PNRs [27]. Based on the above discussion, Zr<sup>4+</sup> was selected to introduce into NBBSCT ceramics to further regulate relaxor properties and delay polarization saturation in this work. Encouragingly, the designed high-entropy ceramics exhibited high relaxor feature and significantly prolonged polarization saturation. Of particular importance is that the 6 mol% Zr<sup>4+</sup> modified NBBSCT ceramics exhibited high *W*<sub>rec</sub> of 6.6 J/cm<sup>3</sup> and ultra-high  $\eta$  of 93.5%. Our work proves that a B-site modification strategy on the basis of A-site high-entropy disorder is also an effective way of improving energy storage density.

## 2 Experimental

(Na<sub>0.2</sub>Bi<sub>0.2</sub>Ba<sub>0.2</sub>Sr<sub>0.2</sub>Ca<sub>0.2</sub>)(Ti<sub>1-x%</sub>Zr<sub>x%</sub>)O<sub>3</sub> (*x* = 0, 2, 4, 6, 8, 10, abbreviated as NBBSCT-*x*Z) ceramics, were synthesized by a conventional solid-state process. The raw materials were high-purity commercial powders of Na<sub>2</sub>CO<sub>3</sub> (99.8%), Bi<sub>2</sub>O<sub>3</sub> (99%), BaCO<sub>3</sub> (99%), SrCO<sub>3</sub> (99%), CaCO<sub>3</sub> (99%), TiO<sub>2</sub> (98%), and ZrO<sub>2</sub> (99.99%) (Sinopharm Chemical Reagent Co., Ltd., China). The powders were weighed based on stoichiometric ratio and then ball-milled for 12 h by 200 r/min. After drying, the mixed powders were calcined at 950–1000 °C for 4 h to get a pure phase. Then a second ball-milling for 12 h at 200 r/min was applied, after which the calcined powders were pressed into plates with a diameter of 8 mm and a thickness of ~1 mm, followed by further cold isostatic pressing under 300 MPa to improve density. The pellets were sintered at 1200–1250 °C for 4 h. For a dielectric measurement, the as-sintered pellets were polished into ~0.6 mm in thickness with both surfaces coated with silver electrodes. For ferroelectric and charge–discharge measurements, the thickness was polished to 0.10 mm with a silver electrode of 2.0 mm in diameter. The silver electrode was sintered at 600 °C for 30 min.

The phase structure of the NBBSCT-*x*Z ceramics was analyzed by an X-ray powder diffractometer (SmartLab-3 kW, Rigaku Ltd., Japan) with Cu K $\alpha$  radiation. The temperature dependences of dielectric permittivity and dielectric losses were measured by a precision impedance analyzer (E4990A, Keysight, USA). The impedance spectra were tested by an electrochemical impedance spectroscopy (1260AC and 1287AC, UK), connecting a muffle furnace with the test temperatures change from 625 to 725 °C, and the test frequency ranged from 0.1 Hz to 1 MHz. The polarization versus electric field (*P*-*E*) hysteresis loops and current versus electric field (*I*-*E*) hysteresis loops were conducted by a ferroelectric tester (TF Analyzer 3000, aixACCT, Germany). The charge–discharge energy density was measured by a charge–discharge apparatus (PK-CPR1801–10015, Polyk Technology, USA). The selected-area electron diffractions were recorded through a transmission electron microscope (TEM; TECNAL G2 F30, FEI, USA).

## 3 Results and discussion

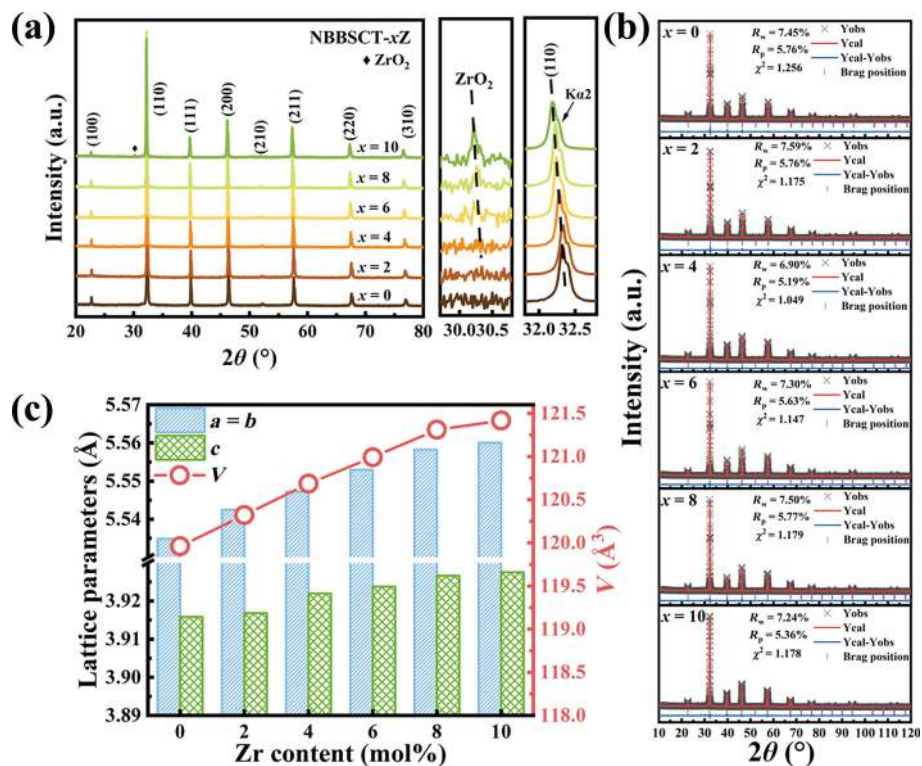
Figure 2(a) shows X-ray diffraction (XRD) patterns of NBBSCT-*x*Z ceramics, in which the peaks relevant to *K*<sub>02</sub> (*K*<sub>02</sub> ray is a kind of radiation generated when electrons move from the L layer to the K layer) are marked out. A typical perovskite structure can be detected for all samples, only a small amount of ZrO<sub>2</sub> comes out when *x*=10. This indicates the Zr<sup>4+</sup> ions are well dissolved into the NBBSCT matrix till *x*=10. It should be noticed that the (110) peak gradually shifts to the low diffraction angles with the increase of the Zr<sup>4+</sup> content, owing to the fact that Ti<sup>4+</sup> (CN = 6, *R*<sub>Ti</sub> = 0.605 Å) is substituted by Zr<sup>4+</sup> (CN = 6, *R*<sub>Zr</sub> = 0.72 Å) with larger ionic radii

[28] where  $R_{Ti}$  means the radii of Ti<sup>4+</sup> and  $R_{Zr}$  means the radii of Zr<sup>4+</sup>. To obtain the detailed lattice parameters, XRD Rietveld refinements were carried out by the GSAS software, as shown in Fig. 2(b) [15]. The Rietveld refinement results are listed in Table 1, and the lattice parameters ( $a$ ,  $b$ ,  $c$ ) and volume ( $V$ ) are drawn in Fig. 2(c). All compositions are well-constrained to the  $P4bm$  space group, indicating Zr<sup>4+</sup> does not change the basic structure of NBBST. The lattice parameters and volume increase continuously with the addition of Zr<sup>4+</sup>, as a result of its larger ionic radius.

To illustrate temperature-induced phase transition in NBBST- $x$ Z ceramics, the temperature vs. dielectric permittivity ( $\epsilon_r$ ) and dielectric loss ( $\tan\delta$ ) spectra are measured and shown in Figs. 3(a)–3(f). Obvious dielectric peaks (the corresponding temperature called as  $T_m$ ) are observed in all samples, associated with remarkable peaks in dielectric loss, as the phase structure transforms from ferroelectric (FE) to paraelectric (PE) phases. All dielectric peaks show evident frequency dispersion, giving a sign of a relaxor feature. As the increase of the Zr<sup>4+</sup> content, the dielectric peaks gradually broaden and are compressed, with  $T_m$  slightly shifting downward to room temperature (RT) (Figs. 3(g)–3(i)). In addition,  $\epsilon_m$  shows a general decrease with the increase of the Zr<sup>4+</sup> content (Fig. 3(i)), as a result of the lower electronic polarizability of Zr<sup>4+</sup> compared to Ti<sup>4+</sup> which reduces the sensitivity

of response of Zr<sup>4+</sup> to the electric field [29].

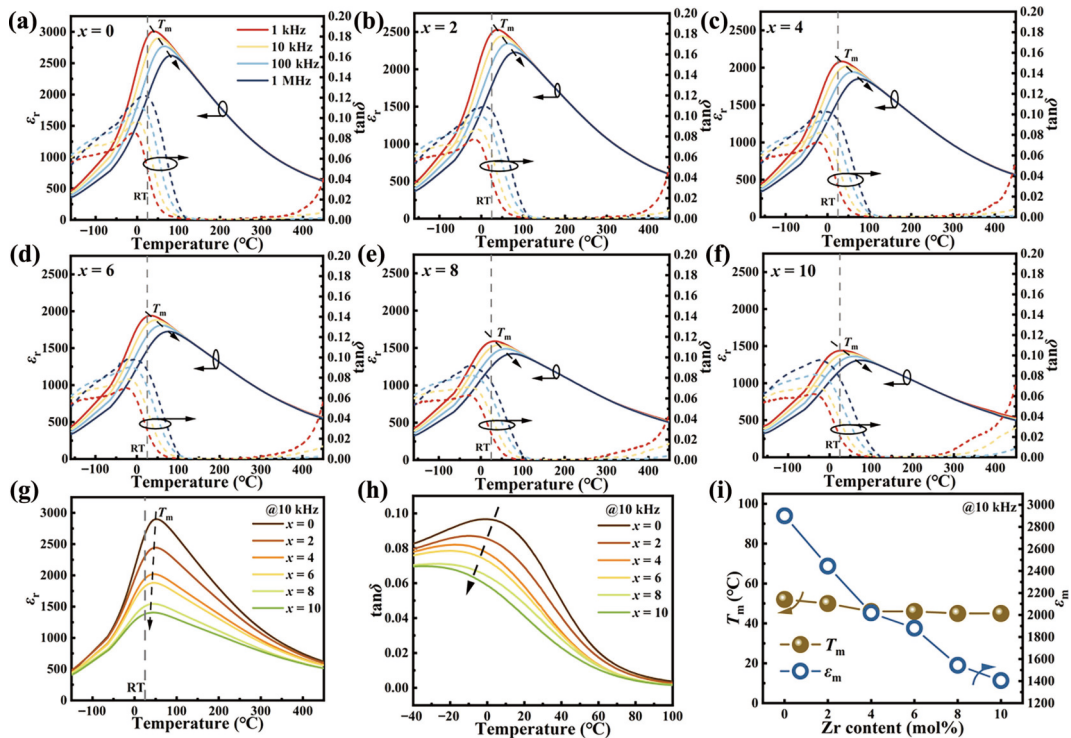
To further estimate the relaxation characteristic, the relaxor factor ( $\gamma$ ) is calculated according to the reformed Curie–Weiss law (Eq. (A.1)) [30, 31]. The fitting lines are shown in Fig. 4(a), which shows good reliability.  $\gamma$  exhibits a slight increase from 1.77 for  $x = 0$  to a maximal value of 1.85 for  $x = 10$ , indicating high and slightly improved diffuseness of the phase transition and relaxor behavior. This concept can be further consolidated by the frequency dispersion ( $\Delta T = T_m(1 \text{ MHz}) - T_m(1 \text{ kHz})$ ) of  $T_m$  [31], which exhibits a large temperature span and slightly increases from  $\sim 41^\circ\text{C}$  for  $x = 0$  to  $\sim 45^\circ\text{C}$  for  $x = 10$ , as shown in Fig. 4(b). It should be noticed that, even though an increase of  $\gamma$  and  $\Delta T$  is observed after the Zr<sup>4+</sup> modification, the variations are actually not significant for both. To further determine the effect of the Zr<sup>4+</sup> content on diffuseness, the normalized dielectric permittivity ( $\epsilon_r/\epsilon_m$ ) vs. temperature ( $T$ ) curves are figured, as shown in Fig. 4(c). Herein, the parameters  $T_{R-L}$  and  $T_{R-H}$  ( $R = 1/2, 2/3$ ;  $T_{R-L}$  and  $T_{R-H}$  represent the span between  $T_m$  and the temperature where  $\epsilon_r/\epsilon_m$  is  $R$  of the maximum value from the low-temperature and the high-temperature branches of the peak, respectively) to describe the width of the FE–PE dielectric peak around  $T_m$  [32,33] as given in Fig. 4(c). Generally, larger  $T_{R-L}$  and  $T_{R-H}$  indicate a slower phase transition process and higher relaxor feature [33]. Both  $T_{R-L}$  and  $T_{R-H}$  broaden apparently with the increase of the Zr<sup>4+</sup> content, as



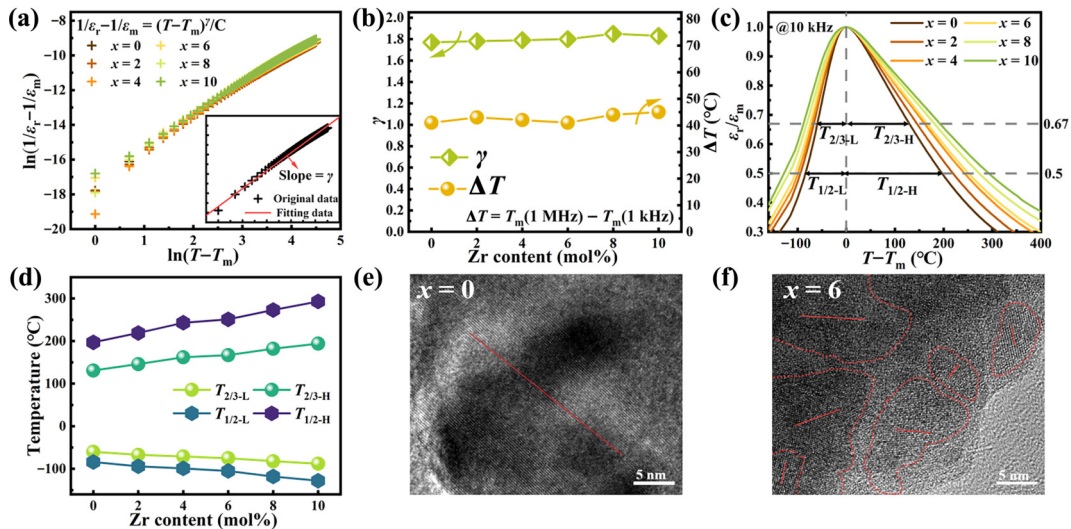
**Fig. 2** (a) XRD pattern of NBBST- $x$ Z ceramics at  $2\theta = 20^\circ$ – $80^\circ$ . (b) Rietveld refinements of XRD data where  $R_{wp}$  is the reliability factors of weighted pattern,  $R_p$  is the reliability factors of pattern, and  $\chi^2$  is the goodness-of-fit indicator. (c) Lattice parameters ( $a$ ,  $b$ ,  $c$ ), and lattice volume ( $V$ ) derived from XRD Rietveld refinements.

**Table 1** Refined structural parameters of NBBST- $x$ Z ceramics

$x$	Space group	Lattice parameter (Å)	$V$ (Å <sup>3</sup> )	$R_{wp}$ (%)	$R_p$ (%)	$\chi^2$
0	$P4bm$	$a = 5.5349, b = 5.5349, c = 3.9158$	119.961	7.45	5.76	1.256
2	$P4bm$	$a = 5.5425, b = 5.5425, c = 3.9168$	120.321	7.59	5.76	1.175
4	$P4bm$	$a = 5.5472, b = 5.5472, c = 3.9220$	120.686	6.90	5.19	1.049
6	$P4bm$	$a = 5.5530, b = 5.5530, c = 3.9238$	120.992	7.30	5.63	1.147
8	$P4bm$	$a = 5.5583, b = 5.5583, c = 3.9266$	121.311	7.50	5.77	1.179
10	$P4bm$	$a = 5.5601, b = 5.5601, c = 3.9275$	121.417	7.24	5.36	1.178



**Fig. 3** Dielectric properties of NBBST- $x$ Zr ceramics: temperature dependence of dielectric permittivity and loss of ceramics: (a)  $x = 0$ , (b)  $x = 2$ , (c)  $x = 4$ , (d)  $x = 6$ , (e)  $x = 8$ , and (f)  $x = 10$ , where the solid lines respectively present dielectric permittivity while the dot lines present dielectric loss; (g) composition dependence of  $\epsilon_r$  and  $\tan\delta$ ; (h) composition dependence of  $\tan\delta$  from  $-40$  to  $100$  °C; (i) composition dependence of  $T_m$  and  $\epsilon_m$ .



**Fig. 4** (a) Plots of  $\ln(1/\epsilon_r - 1/\epsilon_m)$  as a function of  $\ln(T - T_m)$  at 10 kHz. (b) Composition dependence of  $\gamma$  and  $\Delta T$ . (c)  $\epsilon_r/\epsilon_m$  as a function of  $(T - T_m)$  for different compositions at 10 kHz where the inset is expanded curves. (d) Composition dependent corresponding parameters  $T_{R-L}$  and  $T_{R-H}$  ( $R = 1/2, 2/3$ ). TEM images taken from (e) NBBST and (f) NBBST-6Zr ceramics.

shown in Fig. 4(d). This phenomenon, plus the change of  $\gamma$  and  $\Delta T$ , gives an obvious sign that the zirconium additive actually contributes to the enhancement of the relaxor feature. In addition, Figs. 4(e) and 4(f) give TEM images of the ceramics of  $x = 0$  and  $x = 6$ . The ceramics of  $x = 0$  show an apparent parallel larger microregion, while the one of  $x = 6$  exhibits the smaller nanoregions with diverse directions (see the red circles), revealing the high structural inhomogeneity at the nanoscale with the introduction of zirconium additive. This phenomenon indicates that the doping of  $Zr^{4+}$  could further reduce the domain size, which is in favor of enhanced relaxor properties of the ceramics. The strong relaxor feature hinders PNRs from forming long-range

ferroelectric domains under an electric field and enables the domains easier switch back to the original state, which may delay the polarization saturation and result in a slim  $P$ - $E$  loop, thereby leading to high energy storage density and efficiency.

The energy storage density is closely associated with high breakdown strength. To evaluate the value of the breakdown strength, Weibull distribution is adopted to analyze the data obtained by breakdown measurement at room temperature. Based on Eqs. (A.2.1) and (A.2.2) in the Appendix [34], Weibull distribution is fitted and shown in Fig. 5(a).  $E_b$  increases from 408 kV/cm for  $x = 0$  and reaches a maximum of 513 kV/cm for  $x = 6$ , which exhibits a tendency to decrease by further increasing the

Zr<sup>4+</sup> content, as shown in Fig. 5(b). To explore the inner mechanism of the effect of Zr<sup>4+</sup> on the breakdown strength, the room-temperature electrical resistivity ( $\rho$ ) is measured as a function of the Zr<sup>4+</sup> content, as displayed in Fig. 5(c). All samples exhibit high electrical resistivity, indicating good electrical insulation properties. It is interesting that  $\rho$  increases first and then decreases with the increasing amount of Zr<sup>4+</sup>, which reaches a maximum at  $x = 6$ . The high-temperature complex impedance spectra also exhibit a similar tendency to the room temperature electrical resistivity, in which the radius of a semicircle arc increases first and then decreases after Zr<sup>4+</sup> doping, as shown in Fig. 5(d). Also, the complex impedance tested results at other temperatures are shown in Fig. S1 in the Electronic Supplementary Material (ESM), in which the radius of the semicircle arc decreases with increasing the temperature. After Arrhenius fitting (Fig. 5(e)), the electrical conductivity activation energy ( $E_a$ ) is obtained and presented in Fig. 5(f). The calculated  $E_a$  is around 1.85–1.98 eV with the change of the Zr<sup>4+</sup> content, revealing an oxygen vacancy-controlled conducting mechanism ( $0.5 \text{ eV} \leq E_a \leq 2.0 \text{ eV}$ ) in the measuring temperature range [35–37]. Analogous to the change of electrical resistivity,  $E_a$  increases first with the addition of Zr<sup>4+</sup> and then declines at a high Zr<sup>4+</sup> level, reaching a maximum at  $x = 6$ . Larger  $E_a$  means a higher barrier for the migration/hopping of oxygen vacancies, which contributes to good electrical insulation property and accounts for the high electrical breakdown strength at  $x = 6$ .

Figure 6(a) shows the composition dependence of  $P$ - $E$  loops for the as-prepared ceramics, in which all compositions exhibit slim  $P$ - $E$  loops. It is interesting that significantly delayed polarization saturation is observed for the high Zr<sup>4+</sup> doping compositions. To qualitatively evaluate the degree of delayed polarization saturation, the ratio of  $W_{\text{rec}}$  against the electric field ( $W_{\text{rec}}/E$ ) is calculated and depicted in Fig. 6(b).  $W_{\text{rec}}/E$  increases with an enhancement of the electric field and quickly reaches a platform with a maximum value of  $\sim 8.5 \text{ J}/(\text{cm}^2 \cdot \text{V})$  at a critical electric field of around 150 kV/cm. In comparison, the compositions with Zr<sup>4+</sup> additives exhibit much higher critical electric field and platform value, for example, the composition of  $x = 6$  exhibits an obviously increased critical electric field over 200 kV/cm and high maximum  $W_{\text{rec}}/E$  of 11.8  $\text{J}/(\text{cm}^2 \cdot \text{V})$ . The improved critical electric field and platform value imply obvious

delayed saturation polarization, which makes the materials promising for achieving higher energy storage density. Meanwhile, it should be noted that at lower electric fields, the polarization for the low Zr<sup>4+</sup> doping compositions is moderately large, of which the increasing rate is limited at higher fields. In other words, the low Zr<sup>4+</sup> doping compositions possess large polarization nonlinearity. However, for the high Zr<sup>4+</sup> doping compositions, this effect is weakened. To quantitatively describe the polarization nonlinearity, the tangent dielectric constant change ( $\partial P/\partial E$ , TPC calculated from the polarization upswing and downswing) of the charge-discharge curve is employed as Eq. (4):

$$\text{TPC} = \frac{\text{TP}(E) - \text{TP}(0)}{\text{TP}(0)} \times 100\% \quad (4)$$

where  $\text{TP}(0)$  and  $\text{TP}(E)$  represent the tangent permittivity at the electric field strength of 0 and  $E$ , respectively. As exhibited in Fig. 6(c), for the high Zr<sup>4+</sup> content components, TPC is higher under the same electric field. In other words, for the same value of TPC, the ceramics with the higher Zr<sup>4+</sup> content require a large applied electric field, which further confirms the conclusion that the polarization nonlinearity (or high polarization saturation field) gradually decreases with the increase of Zr<sup>4+</sup> [38]. Figure 6(d) shows unipolar  $P$ - $E$  loops of all compositions under an electric field prior to respective breakdown strength. Small hysteresis with low  $P_r$  is observed in all  $P$ - $E$  loops, in accordance with the high RFE feature for all compositions. Based on the  $P$ - $E$  loops,  $W_{\text{rec}}$  and  $\eta$  are calculated and shown in Fig. 6(e).  $W_{\text{rec}}$  is 4.1  $\text{J}/\text{cm}^3$  for  $x = 0$ , which increases with increasing the Zr<sup>4+</sup> content and reaches a maximum of 6.6  $\text{J}/\text{cm}^3$  for  $x = 6$ . However, a further addition of Zr<sup>4+</sup> reduces the energy storage density. Of particular importance is that all compositions exhibit high  $\eta$  over 90%, especially ultrahigh  $\eta$  of 93.5% achieved for  $x = 6$ . Furthermore, the  $P$ - $E$  loops keep slim under various electric fields for the composition of  $x = 6$  (Fig. 6(f)), which leads to a linear increase of the energy storage density and ultrahigh  $\eta$  of beyond 90% with the increase of the electric field (Fig. 6(g)). The above results prove that the strategy of introducing Zr<sup>4+</sup> to improve the relaxor feature and delay polarization saturation is effective for enhancing  $W_{\text{rec}}$ . In addition, in comparison with some other state-of-the-art lead-free perovskite bulk ceramics, the NBBST-6Zr ceramics exhibit an

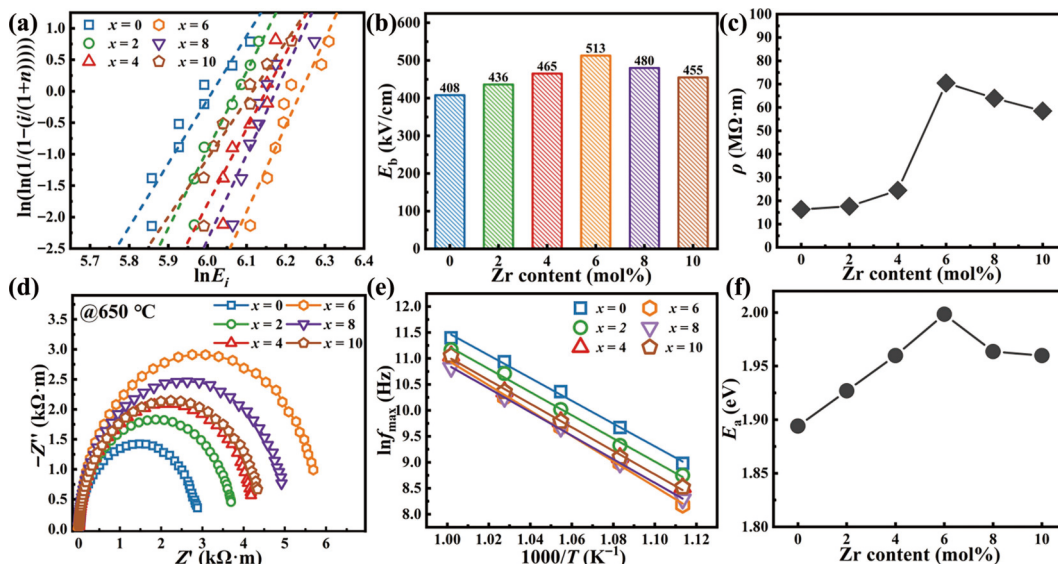
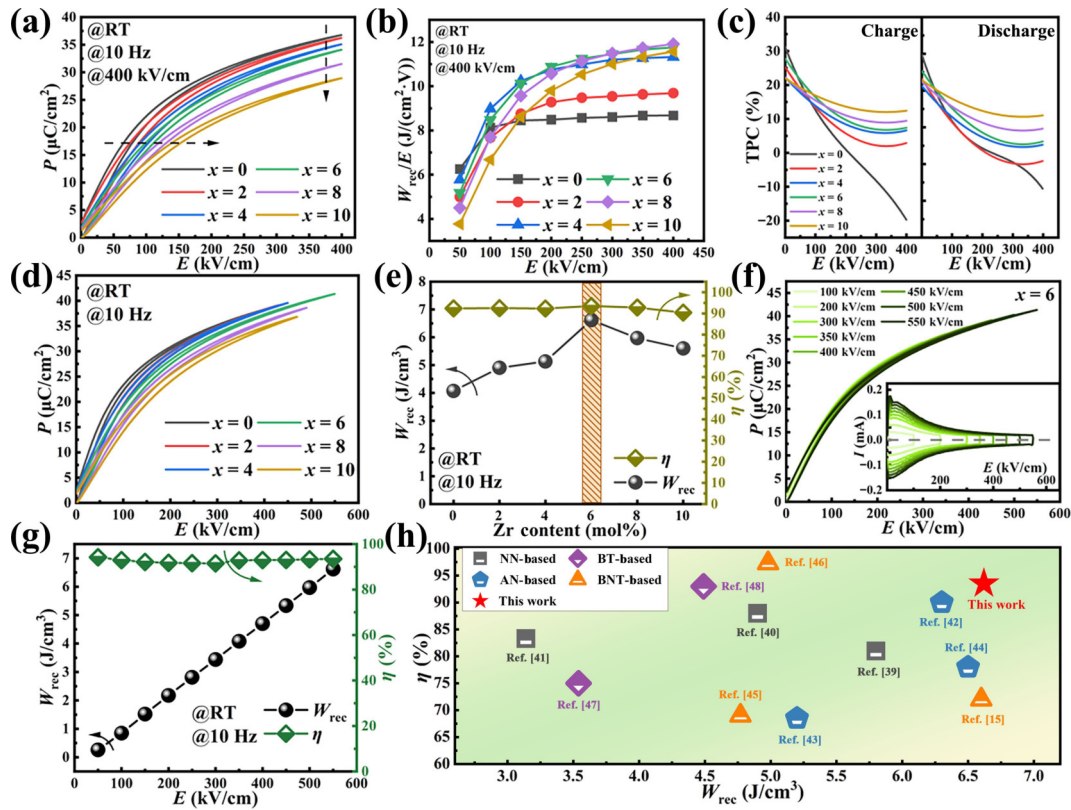


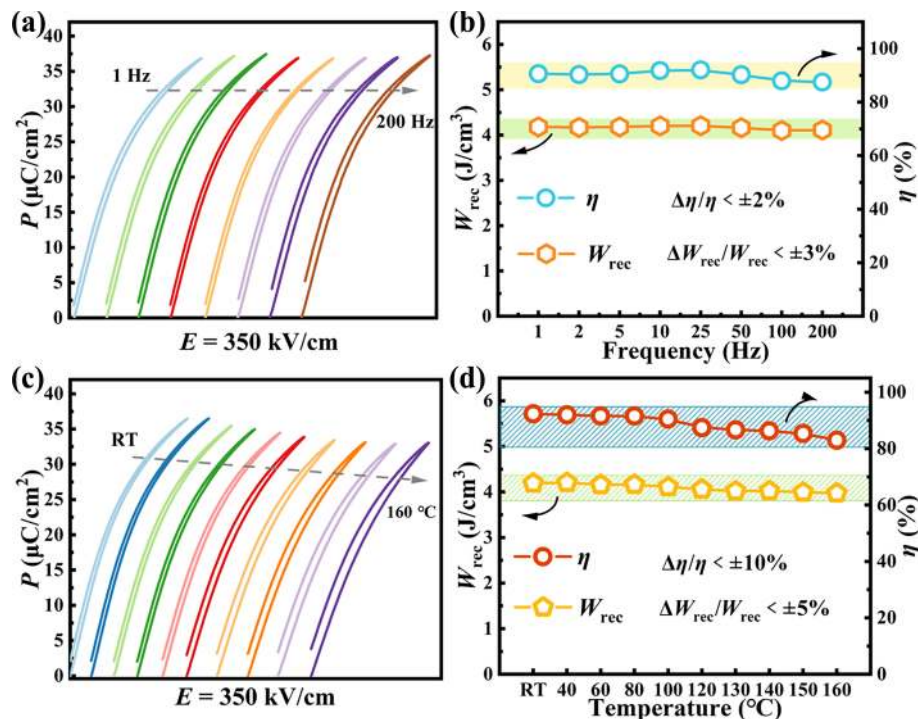
Fig. 5 Comparison of (a) Weibull distribution of breakdown field, (b)  $E_b$  obtained by Weibull distribution, (c)  $\rho$  (room-temperature resistivity), (d) complex impedance tested under 650 °C, (e) Arrhenius lines ( $\ln f_{\text{max}}$  vs.  $1000/T$ ) where  $f_{\text{max}}$  means the frequency at which the maximum ( $-Z''$ ) value is obtained, and (f)  $E_a$ .

obvious advantage in keeping both high  $\eta$  and  $W_{\text{rec}}$ , as shown in Fig. 6(h). All the above properties indicate it is an attractive candidate for energy storage applications [15,39–48].

From an application perspective, the stability of dielectric materials is also an essential bench index that should be considered. Figure 7(a) shows the frequency dependence of the  $P$ - $E$  loops



**Fig. 6** (a) Unipolar  $P$ - $E$  loops when achieving the same electric field. (b) Electric field dependence of  $W_{\text{rec}}/E$  for all compositions at the same electric field. (c) Relationship between tangent dielectric constant and external electric field in charge and discharge curves. (d) Unipolar  $P$ - $E$  loops for all compositions measured prior to each breakdown strength. (e)  $Zr^{4+}$  content dependence of  $W_{\text{rec}}$  and  $\eta$ . (f) Electric field dependence of unipolar  $P$ - $E$  loop (the inset gives  $I$ - $E$  curves). (g) Energy storage properties under breakdown strength of NBBST-6Z ceramics. (h) Comparison of  $W_{\text{rec}}$  and  $\eta$  values with some of state-of-the-art lead-free perovskite bulk ceramics.



**Fig. 7** Energy storage performance for NBBST-6Z ceramics: (a)  $P$ - $E$  loops and (b) corresponding energy storage properties at various frequencies under 350 kV/cm at room temperature. (c)  $P$ - $E$  loops and (d) corresponding energy storage properties at various temperatures under 350 kV/cm at fixed frequency of 10 Hz.

under a fixed electric field of 350 kV/cm for the composition of  $x = 6$ . Over the frequency range from 1 to 200 Hz, the  $P$ - $E$  loops maintain slim with slight fluctuation for  $P_m$  and  $P_r$ . Thus,  $W_{\text{rec}}$  keeps very stable in the range of 4.1–4.2 J/cm<sup>3</sup> and high  $\eta$  of ~90% (Fig. 7(b)), demonstrating good frequency stability. Meanwhile, energy storage devices often work in extreme and/or high-temperature environments, and the temperature stability is also a pivotal evaluation parameter. Figure 7(c) shows the temperature dependence of the  $P$ - $E$  loops under 350 kV/cm for the composition of  $x = 6$ , in the temperature range from RT to 160 °C. Slim  $P$ - $E$  loops are observed at various temperatures, with a small decrease in maximum polarization. It is interesting that  $W_{\text{rec}}$  keeps very stable around 4.1 J/cm<sup>3</sup>, showing a minimum variation of less than 5% (Fig. 7(d)), which indicates excellent thermal stability. Besides, even though the energy storage efficiency exhibits a certain reduction due to an enhanced leakage at high temperatures, high  $\eta$  of 83% is still obtained at 160 °C.

In addition, the charge–discharge performance is also a very important criterion to evaluate the practicability of a capacitor. To evaluate the feasibility of the NBSCT-6Z ceramics, pulse charge–discharge measurements are conducted under various conditions, as shown in Fig. 8. Figures 8(a) and 8(b) display the overdamped charge–discharge performance for the composition of  $x = 6$ . The discharge energy density ( $W_{\text{dis}}$ ) increases significantly with the enhancement of the electric field and reaches a maximum of 6.3 J/cm<sup>3</sup> is obtained under 500 kV/cm, consistent with the results calculated from the  $P$ - $E$  loops. Moreover, 90% of the stored energy can be released in less than 11  $\mu\text{s}$  ( $t_{0.9}$ ), which shows fast discharge speed. Meanwhile, Figs. 8(c) and 8(d) show the temperature dependence of  $W_{\text{dis}}$  and  $t_{0.9}$  under 350 kV/cm for the composition of  $x = 6$  in the temperature range from RT to 160 °C.  $W_{\text{dis}}$  stays relatively stable in the range of 3.5–4.1 J/cm<sup>3</sup> with a minor variation of 12% when the temperature rises from RT to 160 °C. Also,  $t_{0.9}$  also keeps stable in the range of 6.9–7.9  $\mu\text{s}$  with a minor variation of 10%. The phenomenon indicates good thermal stability.

## 4 Conclusions

(Na<sub>0.2</sub>Bi<sub>0.2</sub>Ba<sub>0.2</sub>Sr<sub>0.2</sub>Ca<sub>0.2</sub>)(Ti<sub>1-x%</sub>Zr<sub>x%</sub>)O<sub>3</sub> high-entropy relaxor ferroelectric bulk ceramics were prepared. The phase structure, dielectric, and ferroelectric analysis indicated that the addition of Zr<sup>4+</sup> could drastically tune the relaxor feature, which contributed to delayed polarization saturation. High  $W_{\text{rec}}$  of 6.6 J/cm<sup>3</sup> with ultra-high  $\eta$  of 93.5% was realized in the ceramics of  $x = 6$ . Meanwhile, the ceramics of  $x = 6$  also demonstrated excellent frequency and thermal stability, as well as good charge–discharge performance, which indicates that it is promising for energy storage applications. This work provides an effective strategy to enhance both energy storage density and efficiency of ceramic capacitors.

## Appendix

The diffuseness parameter ( $\gamma$ ) is fitted by the modified Curie–Weiss law (Eq. (A.1)):

$$1/\varepsilon_r - 1/\varepsilon_m = (T - T_m)^\gamma / C \quad (1 \leq \gamma \leq 2) \quad (\text{A.1})$$

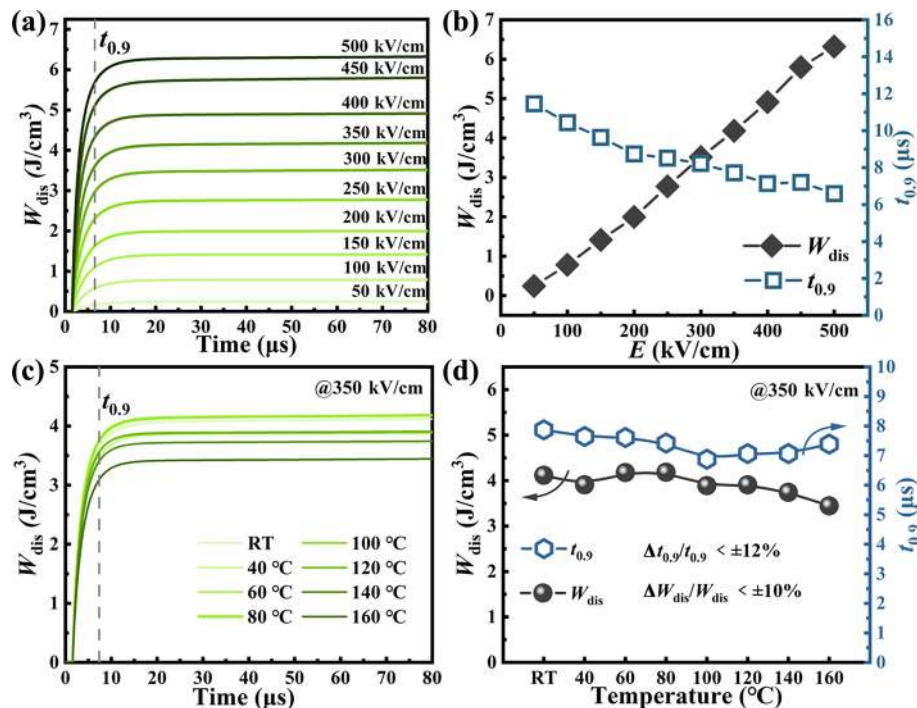
where  $\varepsilon_m$  denotes the dielectric maximum and  $T_m$  is its temperature.  $\gamma = 1$  describes the typical ferroelectric behavior which completely follows Curie–Weiss law, and  $\gamma = 2$  represents the ideal relaxor ferroelectric which undergoes a complete diffuse phase transition. The value of  $\gamma$  could reveal the ferroelectric to relaxor behaviour in the respective range of 1–2, and the larger value of  $\gamma$  reflects the better relaxor performance.

Weibull distribution is calculated from Eqs. (A.2.1) and (A.2.2):

$$X_i = \ln E_i \quad (\text{A.2.1})$$

$$Y_i = \ln \left( \ln \left( 1 / \left( 1 - \frac{i}{n+1} \right) \right) \right) \quad (\text{A.2.2})$$

where  $E_i$  is the breakdown field of the  $i$ th sample arranged in the



**Fig. 8** Charge and discharge performance for NBSCT-6Z ceramics: (a) time dependence of  $W_{\text{dis}}$  under various electric fields and (b) calculated  $W_{\text{dis}}$  and  $t_{0.9}$ . (c) Time dependence of  $W_{\text{dis}}$  at different temperatures under 350 kV/cm and (d) as-calculated  $W_{\text{dis}}$  and  $t_{0.9}$  at different temperatures.

ascending order, and  $n$  is the total number. A linear relationship will be displayed in  $X_i$  and  $Y_p$  with a shape parameter value ( $\beta$ ) assessing the fluctuation of the materials' synthetic quality.

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### Declaration of competing interest

The authors have no competing interests to declare that are relevant to the content of this article.

### Electronic Supplementary Material

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