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Liquid Cooling of Fuel Cell Powered Aircraft: The Effect of Coolants on Thermal Management

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40 **ABSTRACT**

41

42 *Electric propulsors powered by Proton Exchange Membrane Fuel Cells (PEMFCs) offer a net zero solution to*
43 *aircraft propulsion. Heat generated by the PEMFCs can be transferred to atmospheric air via a liquid*
44 *cooling system; however, the cooling system results in parasitic power and adds mass to the propulsion*
45 *system, thereby affecting system specific power. The design of the cooling system is sensitive to the choice*
46 *of liquid coolant and so informed coolant selection is required if associated parasitic power and mass are*
47 *to be minimized.*

48 *Two approaches to selection of coolants for PEMFC-powered aircraft are presented in this paper*
49 *for operating temperatures in the range 80-200°C (this covers low, intermediate, and high temperature*
50 *PEMFCs). The first approach uses a Figure of Merit (FoM) alongside minimum and maximum operating*
51 *temperature requirements. The FoM supports the selection of coolants that minimize pumping power and*
52 *mass while maximizing heat transfer rate. The second approach uses a cooling system model to select*
53 *“Pareto efficient” coolants. A hybrid-electric aircraft using a PEMFC stack is used as a representative case*
54 *study for the two approaches.*

55 *Hydrocarbon-based coolants are shown to be favorable for the case study considered here*
56 *(aromatics for PEMFCs operating at <130°C and aliphatics for PEMFCs operating at >130°C). As the PEMFC*
57 *operating temperature increases, the parasitic power and mass of the Thermal Management System*
58 *(TMS) decreases. Operating at elevated temperatures is therefore beneficial for liquid cooled PEMFC-*
59 *powered aircraft. Nevertheless, there are diminishing performance gains at higher operating*
60 *temperatures.*

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62 **1. INTRODUCTION**

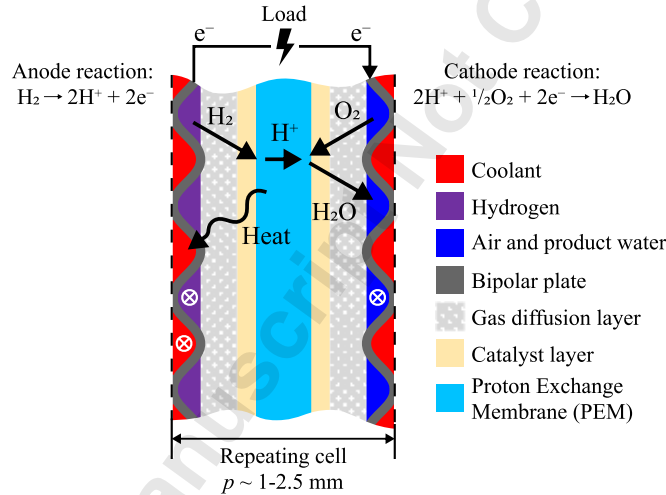
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64 The International Air Transport Association (IATA) and International Civil Aviation
65 Organization (ICAO) have proposed targets for achieving net zero carbon dioxide
66 emissions in aviation by 2050 [1,2]. These targets are driving research and development

67 of low emission aircraft propulsion technologies. The following are the three leading
68 solutions for net zero aircraft propulsion: (1) hydrogen fuel cells, (2) hydrogen
69 combustion, and (3) Sustainable Aviation Fuel (SAF) combustion [3]. The concept of a
70 hydrogen-powered aircraft is not a recent development. In 1937, Heinkel bench-tested
71 the first jet engine (HeS 1), which operated with hydrogen owing to their accelerated
72 development program [4]. The first flight of a hydrogen combustion powered-aircraft
73 took place in 1956, conducted by the US Air Force using a modified B-57 twin-engine
74 bomber [5]. Since the 1950s, kerosene has been the preferred aviation fuel due to its
75 availability, cost, low freezing point, and its suitable combustion properties [6,7].
76 However, kerosene cannot meet net zero emission targets; alternative propulsion
77 systems which achieve net zero carbon dioxide emissions must be developed. One of
78 the leading candidates is a hydrogen fuel cell, electricity is generated through an
79 electrochemical reaction between hydrogen and oxygen. This electricity is then utilized
80 to produce thrust on the aircraft via an electric-powered propulsor. Hydrogen fuel cells
81 achieve superior efficiency, cost reductions, and a lack of particulate and nitrogen oxide
82 emissions compared to both hydrogen and SAF combustion [8,9].

83 Initially designed for space power plants, fuel cell technology was later adapted
84 for and further refined within the automotive industry. Proton Exchange Membrane
85 Fuel Cells (PEMFCs) are the most common fuel cell and display favorable traits for
86 aerospace applications. For example, PEMFCs operating at 80°C are commercially
87 mature, they operate with a high efficiency, and have surpassed 5000 hours of
88 continuous and transient operation (which betters early jet engine technology) [10-13].

89 PEMFCs are categorized as Low Temperature (LT), Intermediate Temperature (IT), and
90 High Temperature (HT). Typical temperature ranges are: LT 80-100°C, IT 100-120°C, and
91 HT 120-250°C [14-16]. Note that these temperature ranges vary somewhat in the wider
92 literature. In this study, the maximum operating cell temperature is set at 200°C due to the
93 low Technology Readiness Level (TRL) of PEMFCs exceeding 200°C. Figure 1 outlines the
94 key components in a PEMFC and the electrochemical reaction, the byproduct being heat
95 and water.
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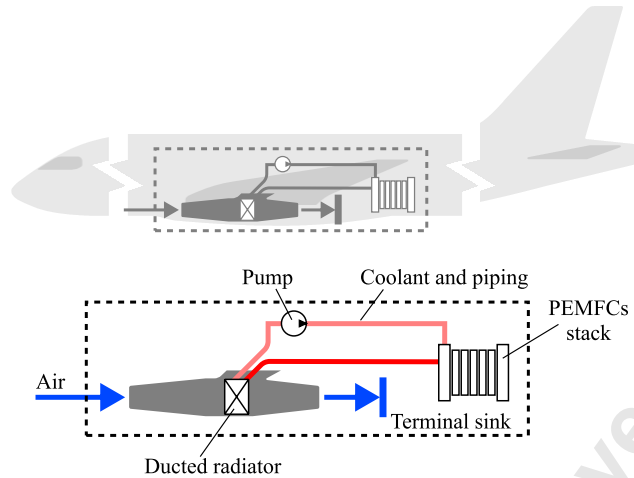
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99 **Figure 1:** Schematic of a Proton Exchange Membrane Fuel Cell (PEMFC) and the
100 electrochemical reaction.
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102 While hydrogen fuel cells show promise, the Thermal Management System
103 (TMS) poses a critical challenge due to the associated parasitic power and mass. The
104 TMS challenge with fuel cell propulsion systems is highlighted by the system specific
105 power [11]. Achieving a system specific power that approaches and exceeds 2 kW/kg is
106 crucial for the market success of regional aircraft (80-165 passengers, <2000 km range,

107 and 0.44-0.72 Mach) [17]. Regional aircraft present market opportunities for fuel cell
108 propulsion systems because they contribute to at least 30% of aviation's carbon dioxide
109 emissions [17]. Estimates place fuel cell propulsion system specific power at ~ 1 kW/kg
110 [11]. To enhance the system specific power and consequently approach the 2 kW/kg
111 target, there are two primary objectives: first, increase the power output without
112 compromising system efficiency, and second reduce the mass of the system. These
113 objectives are strongly dependent on the TMS.

114 Figure 2 illustrates the transfer of the heat generated by a PEMFC stack to the
115 terminal sink (atmospheric air) via a liquid cooling system installed within the aircraft
116 structure. Note that phase-change cooling is beyond the scope of this paper (the
117 interested reader is directed to [18] for associated information). The key components of
118 the liquid cooling system are the radiator, pump, piping and coolant. For a regional
119 aircraft, the cooling system must transfer megawatts of heat to the surrounding air. It
120 must do this while minimizing associated parasitic power and mass to ensure that the
121 specific power level of the propulsion system is adequate. The design of the cooling
122 system (and thereby its parasitic power and mass) is sensitive to the choice of coolant,
123 and so it is important to understand the implications of coolant properties on the
124 cooling system so that an informed selection can be made.

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Figure 2: Notional liquid cooled proton exchange membrane fuel cell propulsion system with a ducted radiator installed under the wing.

131 This paper develops an approach for informed coolant selection and makes
132 recommendations for PEMFCs which require pure hydrogen and operate at
133 temperatures in the range 80-200°C. A review of literature pertinent to coolant
134 selection in the context of PEMFCs is provided in Section 2. A new Figure of Merit (FoM)
135 is outlined in Section 3 and used to screen coolants for high specific heat transfer rate
136 and low pumping power. Section 4 outlines a cooling system model that enables a more
137 refined coolant selection method than the FoM; the model is subsequently used to carry
138 out a sensitivity study on relevant boundary conditions. Liquid coolants are selected via
139 model-informed Pareto fronts for different PEMFC operating temperatures in Section 5.
140 Selection “use cases” for favorable coolants are also included in Section 5 and compared
141 against those obtained from the FoM. Finally, Section 6 addresses the main conclusions.
142 Note that coolant selection is less critical in jet engines as heat energy is dissipated

143 directly to air; nevertheless, the approach presented in this paper could be readily
144 applied to jet engine subsystems.

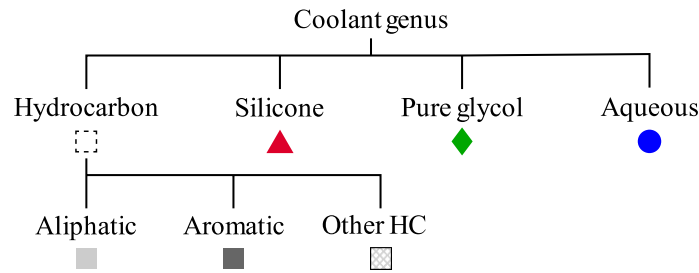
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146 **2. LITERATURE REVIEW**

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148 From an operational standpoint, the ideal coolant should possess
149 thermophysical properties that ensure favorable performance across the entire
150 operating temperature range, while also adhering to safety requirements. The adequacy
151 of thermophysical properties is mainly dependent on the density, dynamic viscosity,
152 thermal conductivity, and specific heat capacity. There are various coolant compositions
153 that have been proposed in the broader literature [19]. Most suppliers of coolants offer
154 hydrocarbons, silicones, pure glycols, and aqueous solutions [20,21]. For this reason,
155 these are included in Figure 3. Aqueous coolants encompass any coolant containing
156 water, while hydrocarbons can be further classified based on chemical structure (details
157 not discussed here) into aliphatic and aromatic types. A coolant is classified as “other
158 HC” (HC – hydrocarbon) if the exact composition is unknown. Recently, much of the
159 literature on coolants has focused on the development of nanofluids [22]. These are not
160 assessed in this paper (and therefore not presented in the ontological plot in Figure 3)
161 due to limited commercial availability and practical challenges [23], such as degradation
162 of nanofluid coolant properties through particle agglomeration [24].

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Figure 3: Coolant ontology. Note – Aliphatic and Aromatic Hydrocarbons may comprise blends, and ‘Other HC’ categorizes Hydrocarbons of unknown composition.

169 The critical requirements of a coolant for a liquid cooled PEMFC operating in an
170 aircraft are detailed in Table 1. These are critical requirements because a coolant must
171 not freeze, boil, auto-ignite, or short circuit across the operating temperature range.
172 The thresholds in Table 1 are:

- 173 1. Min. temperature: The minimum temperature is taken as the freezing point of Jet
174 A-1 [25]. This is a pragmatic threshold as conventional aircraft safely operate with
175 Jet A-1 in subzero conditions. The reader is referred to Barron’s work on aircraft
176 lubrication oil in subzero conditions for further context [26].
- 177 2. Max. temperature: The maximum temperature is defined by the PEMFC operating
178 temperature (80-200°C) plus a margin of 10°C. A 10°C margin is typically used for
179 jet fuel autoignition prevention; the same margin is adopted here but for the
180 boiling point [27]. For example, to select a suitable coolant for a PEMFC stack that
181 operates at 80°C, the boiling point must exceed 90°C. Some of the coolants
182 considered in this study have flash points below the PEMFC operating
183 temperature. For context, Jet A-1 has a minimum flash point of 38°C at ~1 bar but
184 is deemed safe for operation above this temperature because of ignition

185 prevention measures [25,28]. For this reason, the boiling point (rather than flash
186 point) is also employed as the threshold for flammable coolants here.

187 3. Electrical conductivity: The coolant flows through channels, typically pressed into
188 bipolar plates. An electrically conductive coolant will cause current leakage and
189 short circuiting between the electrodes on these bipolar plates. It is therefore a
190 critical requirement to keep the conductivity below 5 $\mu\text{S}/\text{cm}$ [29].

191 **Table 1:** Critical system level requirements for liquid coolants inside a fuel cell
192 powered aircraft.
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Property	Threshold	Unit
Min. temperature	≤ -47	$^{\circ}\text{C}$
Max. temperature	$\geq [80:200]+10$	$^{\circ}\text{C}$
Electrical conductivity	< 5	$\mu\text{S}/\text{cm}$

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196 The effect of coolants on the TMS is the purpose of this paper. Hence, noncritical
197 operational requirements such as chemical compatibility, maintenance requirements,
198 environmental impact, and regulation are not addressed here. It is recommended that
199 such considerations are evaluated prior to the widespread adoption of a particular
200 coolant.

201
202 **3. FIGURE OF MERIT**
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204 Selecting a coolant based purely on its thermophysical properties at expected
205 operating temperatures is desirable in terms of expediency. To do so, a parameter
206 exclusively composed of thermophysical properties must be developed.

207 In 1942, Mouromtseff proposed a ‘factor’ which assesses the ability of a fluid to
208 transfer heat by convection; it is derived from the Dittus-Boelter Nusselt number
209 correlation for turbulent internal flow by grouping fluid properties [30]. Mouromtseff’s
210 ‘factor’ can be rederived for other practical cases by using the corresponding Nusselt
211 number correlation. However, it is unsuitable for selecting coolants with a low pumping
212 power and mass as they are not considered in its derivation. Newton’s law of cooling
213 shows that convective heat transfer rate is dependent on the surface area, temperature,
214 and heat transfer coefficient. Hence, the selection of a coolant via Mouromtseff’s
215 approach does not necessarily maximize the heat transfer rate, as this ‘factor’ only
216 considers the heat transfer coefficient.

217 In 1957, Bonilla proposed several FoMs for coolant selection in the nuclear
218 industry [31]. Bonilla’s FoM captures both the heat transfer rate and pumping power,
219 *i.e.* for a given heat transfer rate it enables coolants which have low pumping powers to
220 be selected. Following Bonilla, Lenert *et al.* (2012) and Ehrenpreis *et al.* (2020) both
221 developed similar FoMs which attempt to minimize pumping power for a given heat
222 transfer rate [32,33]. In addition, Ghajar and Tang (1994) proposed several ratios to
223 assess the relative difference in performance between coolants [34]. FoMs for coolant
224 selection have also been developed in the electronic industry. Green *et al.* (2010)
225 compared air, liquid, and phase-change cooling performance using FoMs that did not
226 consider fluid mass [35].

227 A FoM which includes mass is critical in enabling favorable coolant selection for
228 aerospace applications. It is apparent that none of the above-mentioned FOMs capture

229 the effect of coolant mass and so a new FoM is developed here to assist in selecting
230 coolants for high heat transfer, low pumping power, and low mass applications.
231 Thermophysical properties and pipe flow equations are used to arrive at the FoM
232 (denotated by ϕ) given in Equation (1) – the complete derivation is provided in
233 Appendix A. The FoM maximizes the specific heat transfer rate (\dot{Q}/ρ) for a given
234 pumping power (P_p). The FoM has units of (J/K)(m/kg^{4/3}). The index b does not affect
235 the units as it arises from a correlation between dimensionless numbers.

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$$\phi = \frac{c_p}{\left(\mu^{b/(3-b)}\right)\left(\rho^{(1-b)/(3-b)}\right)} = \frac{c_p}{\mu^{1/14}\rho^{2/7}} \quad (1)$$

238 Blasius's correlation gives values of $b = 1$ and $b = 0.2$ for laminar and turbulent
239 flow respectively [36]. A Reynolds number in the turbulent regime is expected in
240 practice because of the high mass flow rates required for cooling. The FoM for turbulent
241 flow is given in Equation (2).

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$$\phi = \frac{c_p}{\mu^{1/14}\rho^{2/7}} \quad (2)$$

245 To select a favorable coolant, ϕ must be maximized at the anticipated
246 bulk operating temperature. By maximizing ϕ a coolant with a high heat transfer rate
247 and low mass is selected for a given pumping power. Table 2 compares definitions of
248 FoMs from wider literature with the newly proposed FoM from Equation (2). The new
249 FoM captures heat transfer, pressure loss, and mass effects. None of the previous FoMs
250 considered mass, which (as discussed above) is critical in aerospace applications.
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252
253 **Table 2:** Comparison of proposed figure of merits.

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FoM	Maximize for...		Reference
	High	Low	
$\rho^{0.8} k^{0.6} c_p^{0.4} / (\mu^{0.4})$	\bar{h}	—	Mouromtseff [30]
$\rho^2 c_p^{2.8} / (\mu^{0.2})$	\dot{Q}	P_p	Bonilla [31]
$\rho^2 c_p^{1.6} k^{1.8} / (\mu^{1.4})$	\dot{Q}	P_p	Lenert <i>et al.</i> [32]
$\rho^{0.5} c_p^{0.5} k^{0.5} / (\mu^{0.25})$	\dot{Q}	P_p	Ehrenpreis <i>et al.</i> [33]
$c_p / (\mu^{1/14} \rho^{2/7})$	\dot{Q} / ρ	P_p	Current study

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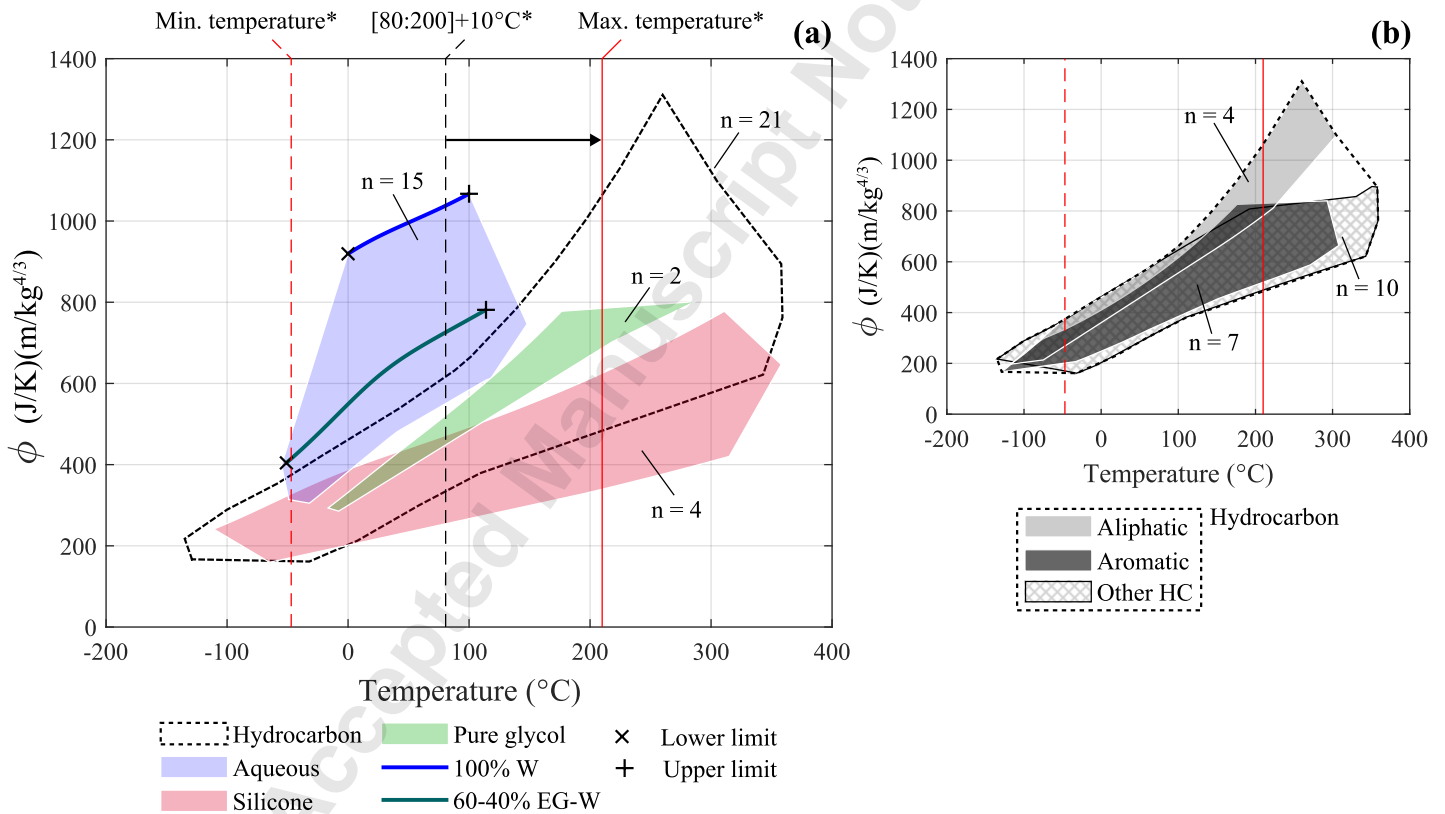
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A database of 43 coolants was constructed from the following references

[20,21,37-40]. These coolants are classified as hydrocarbon (aromatic, aliphatic, and

other HC), pure glycol, silicone, and aqueous. Figure 4 shows FoM regions for these



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Figure 4: (a) Figure of Merit for coolant categories spanning their operating temperature at atmospheric pressure. The dashed line encompasses all of the Hydrocarbons. (b) Magnification of the Hydrocarbons which identifies Aliphatics, Aromatics, and Other HCs. *Refer to Table 1.

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265 coolant categories across their operating temperature at 1 bar; at higher pressure their
266 boiling points increase. The minimum and maximum temperature lines align with those
267 outlined in Table 1. Note that for clarity, the main plot in Figure 4(a) does not distinguish
268 between hydrocarbon types (the hydrocarbon region is broken down into subregions in
269 Figure 4(b)). As is the case for Ashby charts, Figure 4 is intended for broad comparisons
270 required in preliminary design. The temperature spans the freezing point to boiling
271 point for aqueous coolants, and the pour point to boiling point for other coolants. The
272 freezing and pour points are lower limits, and the boiling point is the upper limit. The
273 upper and lower limits form a region's boundary. The addition of more coolants
274 increases confidence in the boundaries of each region – the number of coolants in each
275 genus is denoted by n .

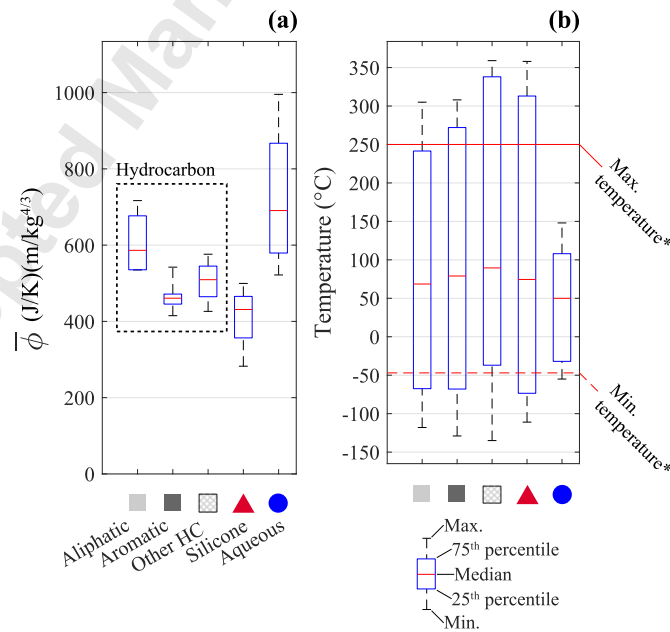
276 It is apparent from Figure 4 that aqueous coolants operating at 80-100°C
277 outperform other coolant categories. Although the temperature range of water is
278 extended by adding glycol, the FoM deteriorates as indicated by the difference between
279 the curves for Water (W) and 60-40% Ethylene Glycol and Water (EG-W). Operating
280 below -47°C is challenging with aqueous coolants. IT and HT-PEMFCs require use of
281 hydrocarbons and silicones to avoid boiling if the coolant pressure is not increased
282 above atmospheric pressure.

283 The average FoM and operating temperatures for coolant categories are
284 compared statistically in Figures 5(a) and 5(b) respectively – note that pure glycol is not
285 included as the $n = 2$ sample does not provide robust statistical outputs. $\bar{\phi}$ is the

286 integrated average bounded by the lower and upper temperature limits for each
 287 coolant; the average FoMs are grouped for each genus to produce the statistics.
 288 Similarly, the temperature statistics are generated from the lower and upper
 289 temperature limits.

290 Aqueous coolants achieve the highest median average FoM of $\bar{\phi} = 691$
 291 $(\text{J/K})(\text{m/kg}^{4/3})$. Aqueous coolants also have the largest interquartile range of $\bar{\phi}$. The large
 292 range is attributed to the large quantity of different aqueous coolant compositions.
 293 However, aqueous coolants have the smallest operating temperature range, which
 294 limits their suitability for IT and HT-PEMFCs. In addition, aliphatic coolants achieve a
 295 higher median $\bar{\phi}$ than other HCs, aromatics, and silicones which makes them more
 296 favorable in general. This performance difference is one of the reasons for the
 297 widespread adoption of polyalphaolefin (PAO) coolants (an aliphatic) in aircraft cooling
 298 installations [37].

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Figure 5: (a) Integrated average Figure of Merit for coolant categories and (b) their operating temperature range. *Refer to Table 1.

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4. SYSTEM MODEL

The FoM cannot capture system-level objectives, which limits its application to initial screening for suitable coolants. A system model is required for a higher fidelity selection. The process of choosing a suitable coolant differs between the FoM and the system model, with the distinctions outlined as follows:

1. The FoM maximizes the ratio of specific heat transfer rate (\dot{Q}/ρ) to the pumping power (P_p) for a given system – it is a metric based on the thermophysical properties of a coolant. Variables that define the condition of the system (mass flow rate, *etc.*) are constants in its derivation.
2. In the system model, the thermophysical properties are varied by changing the coolant. For a given heat transfer rate, the parasitic power and system mass are computed. Coolants are selected if they are “Pareto efficient” solutions.

These approaches achieve the same objective, they select coolants which maximize the heat transfer rate, and minimize the parasitic power and mass. The system model, principal assumptions, boundary conditions, and the sensitivity to relevant boundary conditions are addressed in the following sections.

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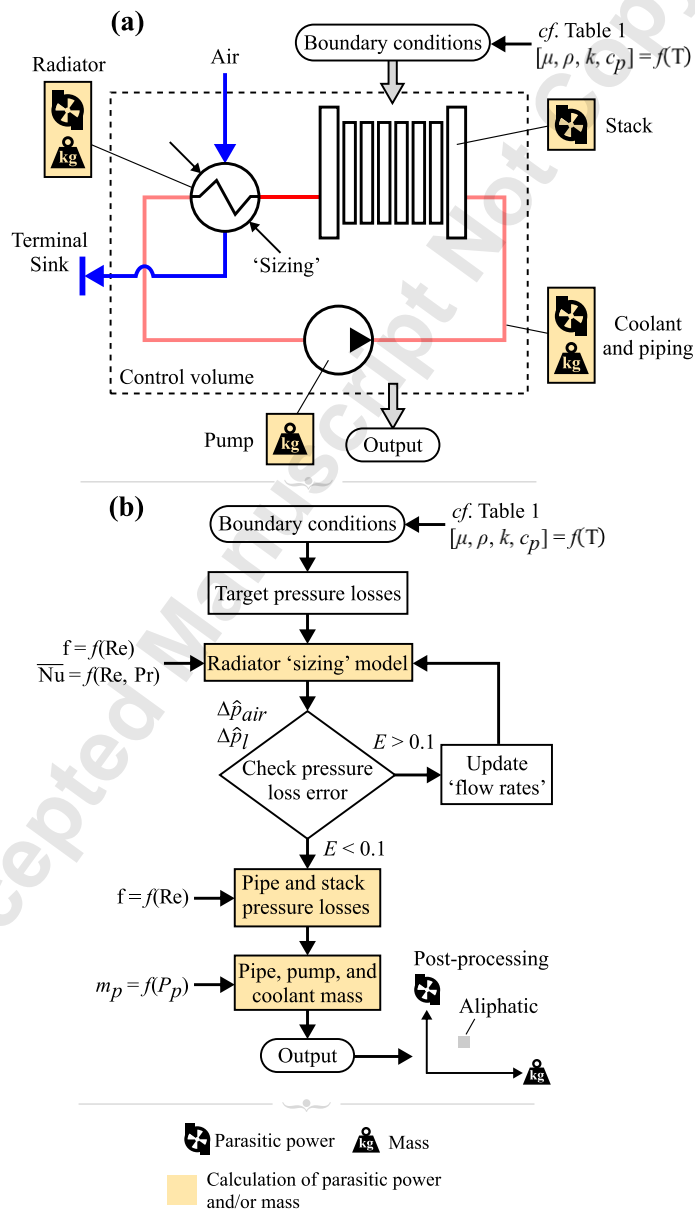
4.1 Summary of the Model

The system model comprises a radiator, stack, piping, and pump, as illustrated in Figure 6(a). These are fundamental TMS components for liquid cooling and so ensure

328 that the coolant selection procedure provides general recommendations. For a detailed
 329 review of different architectures and TMS components the interested reader is referred
 330 to [41]. The flow of data within the model and the key functions that it uses are outlined
 331 in Figure 6(b), with associated details provided below:

- 332 • Indicative boundary conditions for a PEMFC-powered aircraft were set – these
 333 are discussed in §4.4.

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Figure 6: (a) A schematic of the system model including the radiator, stack, piping, coolant and pump. (b) A flowchart of the system model which includes the iterative radiator sizing algorithm.

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- A database was constructed from coolant suppliers. Coolant property data were curve fitted via regression. The coefficients of the fits were preloaded into the model to increase computation speed. Second order polynomials were employed for the density, thermal conductivity, and specific heat capacity. A two-term exponential was used for the dynamic viscosity. The R-squared is >0.95 for every coolant and fit. To define the operational temperature range of a coolant, the freezing, pour, and boiling points were taken from coolant suppliers. Air property data was linearly interpolated from Roger and Mayhew [42].
- The radiator sizing model was derived from London and Kays [43]. Although the heat exchanger characteristics affect the absolute 'size' of the radiator, they are unimportant in assessing the relative performance of the coolants. A crossflow heat exchanger composed of tubes with plate fins (11.32-0.737-SR) was used here [43]. To determine the radiator size, target pressure losses were assigned to both the air and coolant sides. An iterative algorithm was then utilized to achieve the set pressure loss targets. This process involved three stages:
Stage 1. Initialization of the algorithm by assuming the mass flow rate flux was infinitesimal on both the air and coolant sides.
Stage 2. Calculation of the friction factor for pressure loss, and the Colburn j-factor and the Nusselt number for heat transfer using empirical correlations

360 suitable for both the air and coolant sides. On the airside, the friction
361 factor and j-factor data from London and Kays for the 11.32-0.737-SR
362 surface was used. On the coolant side, Churchill's Nusselt correlation was
363 adopted to estimate the heat transfer coefficient in a smooth tube for
364 11.32-0.737-SR [44]. The friction factor for a circular tube was estimated
365 from Haaland's explicit formula [36].

366 Stage 3. Estimation of the pressure loss on each side and recalculation of the new
367 mass flow rate fluxes until the specified target pressure losses were
368 reached. Note, entry and exit loss coefficients were derived from London
369 and Kays. Linear interpolation was used to estimate these coefficients.

370 • A friction factor pipe flow correlation was used to estimate the pressure losses in
371 the stack and piping from Haaland's explicit formula [36] using the calculated
372 coolant mass flow rate from above. The pump mass was then estimated from an
373 empirical correlation derived from [45]. A positive displacement coolant pump was
374 assumed because they are used in fuel systems for aircraft. The correlation
375 presented in Equation (3) includes an electric motor to drive the pump (units of kW
376 and kg). The correlation for the electric motor mass was adopted from [46,47].

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$$m_p = \underbrace{3.40 P_p^{0.437}}_{\text{pump}} + \underbrace{0.889 P_p^{0.900}}_{\text{motor}} \quad (3)$$

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380 • The system pumping power, drag, and mass were calculated. The drag was
381 estimated from the airside pressure loss across the core [43]. The drag estimate did
382 not account for the ramjet thrust generated by heat addition on the airside, a

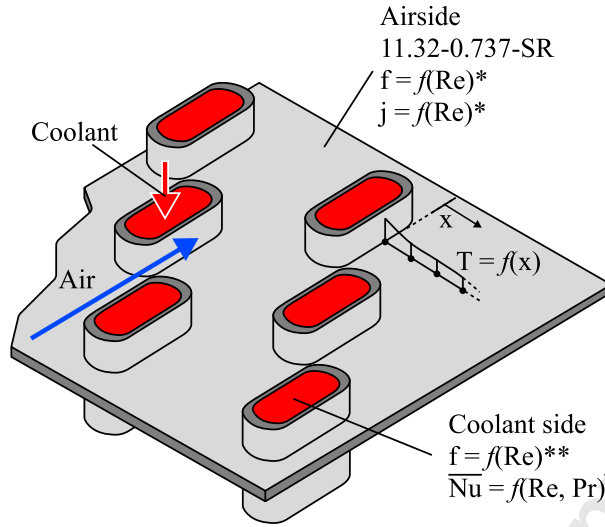
383 phenomenon frequently referred to as the Meredith effect [48]. Drela showed the
384 ramjet thrust is proportional to the freestream Mach number and heat load; both
385 are consistent for different coolants [49]. Different coolants were ranked against
386 each other: coolants which performed favorably were selected and their properties
387 were checked to identify whether they met the critical minimum and maximum
388 temperature requirements. Pareto fronts were generated to assess the trade-off
389 between different objectives, *e.g.* parasitic power and mass for a given heat load.

390 391 **4.1 Principal Assumptions**

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393 The analysis was simplified by making the specific assumptions discussed below,
394 most of which applied to the radiator sizing model.

395 Losses were evaluated in the heat exchanger core. The effect of installation drag
396 was not assessed for simplicity. The dimensions of the core, and hence the packaging of
397 the radiator, are affected by the choice of coolant. A greater core drag corresponds to a
398 larger frontal area owing to the target pressure losses remaining constant between
399 coolants. Any coolant which results in a heat exchanger with an increased core drag and
400 consequently a larger frontal area would in practice also exhibit higher installation drag.
401 Hence, the ranking of coolants would be unchanged if installation drag was accounted
402 for. The minor losses, manifolding, entry, and exit losses are not accounted for in the
403 stack and piping [50].

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Figure 7: A schematic of radiator geometry (11.32-0.737-SR) with the respective correlations. * [43], ** [36], and † [44].

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Figure 7 shows a schematic of the 11.32-0.737-SR heat exchanger geometry adopted from London and Kays [43]. To simplify the analysis, circular tube correlations were used as an approximation for the flat tubes, and the internal flow was assumed to be fully developed. The friction factor and Colburn j-factor data from London and Kays were curve fitted with two-term exponentials. A two-term exponential was chosen for its ability to yield a lower Root Mean Squared Error (RMSE) in comparison to more conventional power laws. London and Kays quote the uncertainty as a nominal $\pm 5\%$ for this data. The fitted curves for 11.32-0.737-SR had a R-squared > 0.95 . London and Kays included three rows in the test article used to produce the correlations for 11.32-0.737-SR. The number of rows affects the prediction of heat transfer and pressure loss, with Zukauskas suggesting that 16 rows are required before the average heat transfer coefficient settles [51]. Hence, the model's prediction of a heat exchanger with more than the three rows used to generate the correlations introduces uncertainty. It should

423 be noted that the model allows a non-integer number of tube rows as an output. This
424 enables minor variations in radiator mass to be captured during coolant ranking, *i.e.* it
425 increases the sensitivity of the analysis. This approach allows a TMS designer to select
426 an appropriate coolant for their application and then proceed to refine the design of the
427 radiator (the 11.32-0.737-SR geometry used here was chosen as baseline – there are
428 many geometries that could be chosen from, and scaling up to the nearest integer of
429 rows for the analysis could lead to sub-optimal coolant selection).

430 431 **4.3 Boundary Conditions for Coolant Selection**

432
433 The boundary conditions used in this study are summarized in Table 3, with
434 associated sensitivities addressed in §4.4. The values are indicative of those for an
435 aircraft operating with a liquid cooled PEMFC powertrain capable of delivering a
436 maximum electrical power of 1 MW. It was assumed that a single stack produced $\dot{W}_1 =$
437 100kW [52]; the powertrain thereby comprised ten stacks to generate the required
438 power. For assumed cell efficiencies of 50%, the total rate of heat generated by the
439 powertrain at maximum power was $\dot{Q} = 1$ MW [53]. The stack geometry was derived
440 from data given by PowerCell, Bargal *et al.*, and Yoshida *et al.* [52,54,55]. Each stack
441 comprised 240 cells of pitch $p = 2.5$ mm, providing a stack length of $L_s = 0.6$ m. Cooling
442 channels inside stacks typically have hydraulic diameters of around a millimeter and
443 undergo multiple passes [56] – here $b_s = 1$ mm and $N = 20$ were used as representative
444 values.

445 Conventional aircraft commonly employ aluminum pipework and radiators [57-
446 59]. As such, material properties for aluminum ($\rho_m = 2800$ kg/m³ and $k_m = 187$ W/mK)

447 were used [36,51]. Ions leaching from aluminum into the coolant pose challenges in fuel
448 cells, which would in practice necessitate the use of deionizers to prevent short-
449 circuiting [60] – the effect of deionizers on thermal performance was not considered
450 here. Representative dimensions for the inlet duct (intake area $A_{in} = 0.5 \text{ m}^2$) and piping
451 (hydraulic diameter $D_h = 100 \text{ mm}$, wall thickness $t = 10 \text{ mm}$, surface roughness $\epsilon = 0.046$
452 mm and length $L_p = 5 \text{ m}$) were informed by preliminary design studies.
453 The radiator was sized for take-off (altitude $h = 0 \text{ ft}$), representing the most demanding
454 performance requirement. At this point, the air-to-coolant temperature difference and
455 Mach number ($M_\infty = 0.2$) are at their minimum, while the heat load is at its 1 MW
456 maximum. This ensures that the selected coolant is suitable for the entire mission
457 profile. To evaluate the worst-case scenario, the International Standard Atmosphere
458 (ISA) was employed, with the ambient temperature increased by $\delta T = 25^\circ\text{C}$ to represent
459 a hot day [61]. The diffuser adiabatic efficiency was taken as $\eta_d = 0.9$ – this is typical of
460 well-designed diffusers [62]. The coolant inlet temperature (T_{in}) was obtained from the
461 stack operating temperature. This temperature depends on the fuel cell MEA, as
462 discussed in §1. A range of 80-200°C is employed here because the TRL of stacks
463 operating >200°C is low. Minimizing the non-uniformity of the MEA surface temperature
464 is crucial to prevent elevated degradation rates [54,63]. The temperature difference on
465 the coolant-side is taken as $\Delta T_l = 20^\circ\text{C}$ to limit this temperature gradient. The coolant-
466 side is assigned a target pressure loss of $\Delta \hat{p}_l = 0.5 \text{ bar}$ across the radiator. While this
467 target is contingent on the design of the system, Topuz *et al.* demonstrated similar
468 pressure losses for a liquid-cooled radiator loop [64]. An allowable pressure loss

469 coefficient is implemented on the airside. This parameter defines the target pressure
 470 loss on the airside as a fraction of the available dynamic pressure; a value of greater
 471 than one corresponds to an airside pressure loss greater than the dynamic pressure. A
 472 baseline value of $\xi = 0.5$ is adopted to ensure that the total pressure aft of the radiator is
 473 maintained above ambient.

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Table 3: System model boundary conditions for coolant selection.

Parameter	Magnitude	Unit
\dot{W}_1	100	kW
\dot{Q}	1	MW
ρ	2.5	mm
L_s	0.6	m
b_s	1	mm
N	20	-
ρ_m	2800	kg/m ³
k_m	187	W/mK
A_{in}	0.5	m ²
D_h	100	mm
t	10	mm
ε	0.046	mm
L_p	5	m
h	0	ft
ΔT_l	20	°C
M_∞	0.2	-
δT	25	°C
η_d	0.9	-
T_{lin}	80:200	°C
$\Delta \hat{p}_l$	0.5	bar
ξ	0.5	-

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479 4.4 Sensitivity to Boundary Conditions

480

481 The following sensitivity analysis shows that the coolant inlet temperature is the

482 boundary condition that provides the largest contribution to total mass (M_t – piping,

483 coolant, and dry radiator core mass) and total power (P_t – pumping power and core
 484 drag). Sensitivity was captured from a full factorial Design of Experiments (DoE) with
 485 two levels (‘low’ and ‘high’) applied to the boundary conditions presented in Table 4
 486 (see references [65,66] for a discussion of the associated DoE methodology). All other
 487 boundary conditions remained at the nominal values provided in Table 3. The boundary
 488 conditions in Table 4 were considered at two-levels as they are the most uncertain
 489 based on preliminary designs and trade studies. By showing that the coolant inlet
 490 temperature is the most important boundary condition, the number of degrees of
 491 freedom is reduced in subsequent analysis and coolant selection is generalized.

492
 493 **Table 4:** Full factorial Design of Experiments with two levels to determine the sensitivity
 494 of total mass and total power to uncertain boundary conditions.
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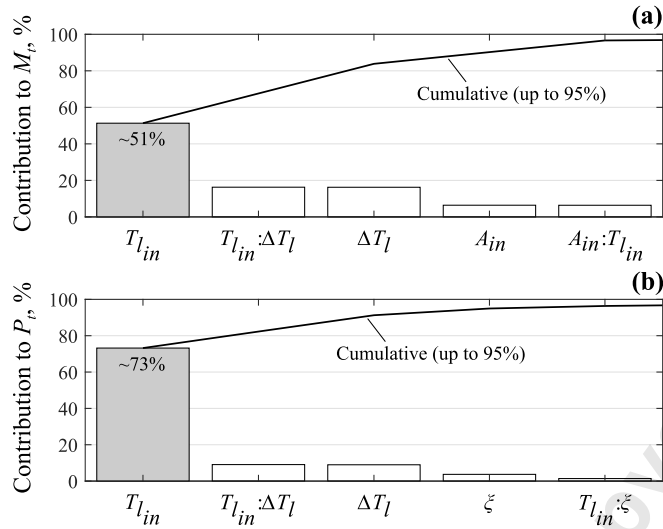
Parameter	Low	High	Unit
A_{in}	0.4	0.6	m ²
T_{in}	80	200	°C
ΔT_l	20	30	°C
$\Delta \hat{p}_l$	0.5	0.8	bar
ξ	0.5	0.8	–

496
 497 The percentage contributions of each main effect and their interactions on the
 498 response variables M_t and P_t are shown in Figure 8 for aliphatic coolant YF-22 PAO
 499 (interacting variables are denoted with a colon). The percentage contributions were
 500 estimated from the sum of the squares; it provides a measure of the contribution of the
 501 main effects and interactions relative to the total sum of squares. Hence, a larger
 502 contribution signifies a model term (main effect or interaction) which has a greater
 503 relative importance on the response variable.

504 Figure 8(a) shows the percentage contribution of the model terms on the total
505 mass. The coolant inlet temperature (highlighted in Table 4) is the most significant
506 model term, accounting for ~50% of the contribution to mass. Figure 8(b) shows the
507 percent contribution on the pumping and core drag power. The coolant inlet
508 temperature accounts for ~70% of contribution to total power. The coolant inlet
509 temperature had the largest contribution of any of the boundary conditions considered
510 in the DoE. Changing the boundary conditions for a fixed coolant inlet temperature will
511 lead to a similar coolant being selected because the other boundary conditions have a
512 minor influence on the mass and power. This enhances the general applicability of the
513 results, allowing the selection of favorable coolants by adjusting the inlet coolant
514 temperature only. The understanding that other boundary conditions exert only a minor
515 influence on the selection process adds robustness to the coolant selection approach.

516 Figure 8 was generated for YF-22 PAO (aliphatic) because it has a high boiling
517 point (>200°C), which allowed contributions to total mass and power to be considered
518 over the full range of T_{in} . Although the contributions do vary for different coolants, the
519 coolant inlet temperature remains the most important. To avoid boiling when
520 comparing the contributions of different coolants, 120°C was used as the high value of
521 the coolant inlet temperature instead of 200°C. Each coolant genus was sampled once
522 with this high value, the minimum contribution to both total mass and power attributed
523 to the coolant inlet temperature was ~30% (a silicone coolant) and the average was
524 ~70%.

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Figure 8: Percent contribution of the model terms on (a) total mass and (b) total power. derived from a full factorial Design of Experiment for an Aliphatic coolant. Up to 95% of the percent contribution is included.

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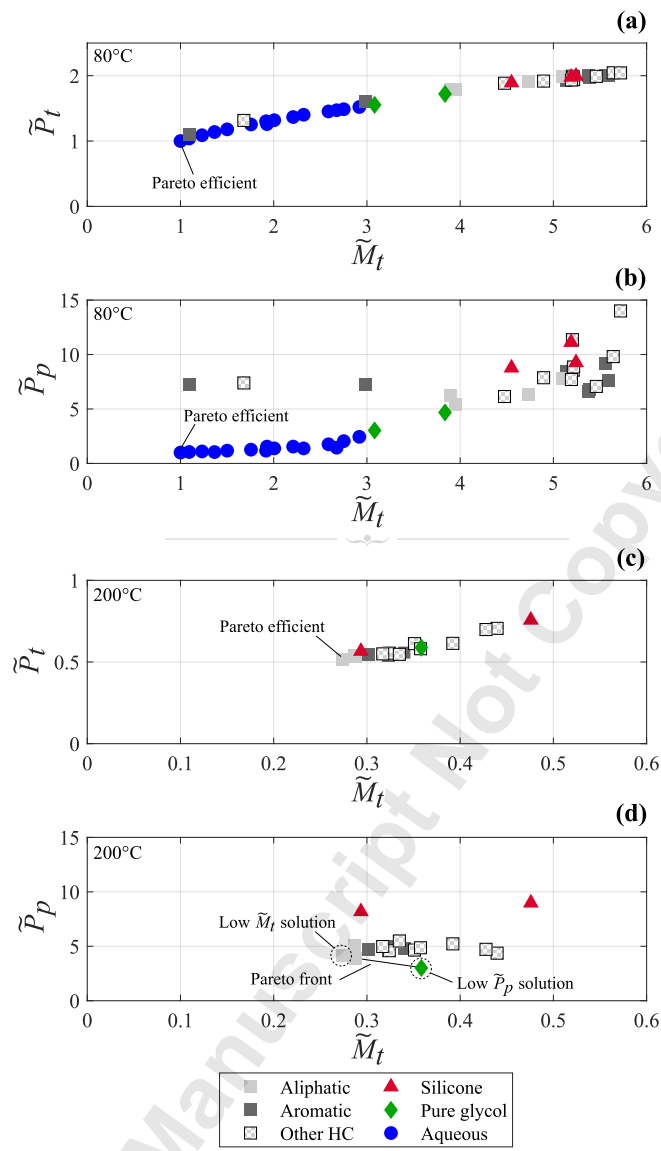
5. SELECTION OF A LIQUID COOLANT

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The maximum and minimum operating temperatures and electrical conductivity requirements for coolants operating on PEMFC-powered aircraft were provided in Table 1. Maximum temperature was applied as a constraint in the selection process used to produce the results shown in Figures 9 and 10. The minimum temperature constraint is specific to aircraft requirements and often operational mitigations can be made. As such, minimum temperature constraints are addressed subsequently in §5.3. Mitigations include the use of electrical heaters, and the design of a freeze tolerant system. Electrical conductivity is also discussed in §5.3. Inhibitors can be introduced to the coolant to reduce the conductivity, and deionizers can be integrated into the system.

545 Figure 9(a) shows normalized total power (\tilde{P}_t – pumping power *and* core drag)
546 versus the normalized total mass (\tilde{M}_t) at 80°C, and Figure 9(b) shows normalized
547 pumping power (\tilde{P}_p) versus the normalized total mass at 80°C. The data is normalized by
548 deionized water at 80°C. Figure 9(a) aids in the selection of favorable coolants for
549 aircraft radiators where freestream velocities are high and drag is important; Figure 9(b)
550 is relevant when the freestream velocity is relatively low and core drag is not important
551 (*e.g.* automotive and marine applications) – these “use cases” are addressed in Table 5.
552 To select a favorable coolant, the powers and mass must be minimized. The most
553 favorable coolant for both Figures 9(a) and 9(b) is deionized water. This coolant is
554 Pareto efficient because it achieves a dominance rank of one. Aqueous coolants perform
555 better than other coolants at 80°C. There are two aromatic outliers, and one other
556 hydrocarbon outlier; these show better performance than most hydrocarbon coolants.
557 This indicates that the composition of hydrocarbon coolants can be tailored to achieve
558 similar performance to aqueous coolants at 80°C if required. Pure glycols show worse
559 performance to aqueous coolants, yet they perform better than most hydrocarbon and
560 silicone coolants.

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Figure 9: Pareto fronts at 80°C for (a) and (b), and 200°C for (c) and (d). Total power versus total mass: (a) and (c). Pumping power versus total mass: (b) and (d). Normalized by deionized water at 80°C. Excludes low temperature threshold.

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Figure 9(c) shows \tilde{P}_t versus \tilde{M}_t at 200°C, and Figure 9(d) shows \tilde{P}_p versus \tilde{M}_t at 200°C. In both figures aqueous coolants are not plotted because they boil below 200°C, which makes them unsuitable for selection. Figure 9(c) shows that aliphatic coolants are Pareto efficient. In Figure 9(d), both aliphatic coolants and a pure glycol form a Pareto

572 front (this is formed when more than one coolant is Pareto efficient). The low \tilde{P}_p and
573 low \tilde{M}_t solutions are circled on the Pareto front. In Figures 9(c) and 9(d) the range in
574 normalized total mass is 0.27 to 0.47. This is smaller than the range in Figures 9(a) and
575 9(b). Hence, the performance difference between coolant compositions is smaller at
576 200°C compared to 80°C.

577

578 **5.1 Selection with Core Drag**

579

580 The full factorial DoE in §4.4 revealed that the coolant inlet temperature (a proxy
581 for the stack temperature) was the parameter with the strongest effect on the total
582 mass and power of the TMS. The model was thereby employed to generate data using
583 coolant inlet temperatures in the range 80-200°C with all other parameters set to the
584 values provided in Table 3. The Pareto efficient coolant(s) were selected for each
585 temperature via dominance ranking.

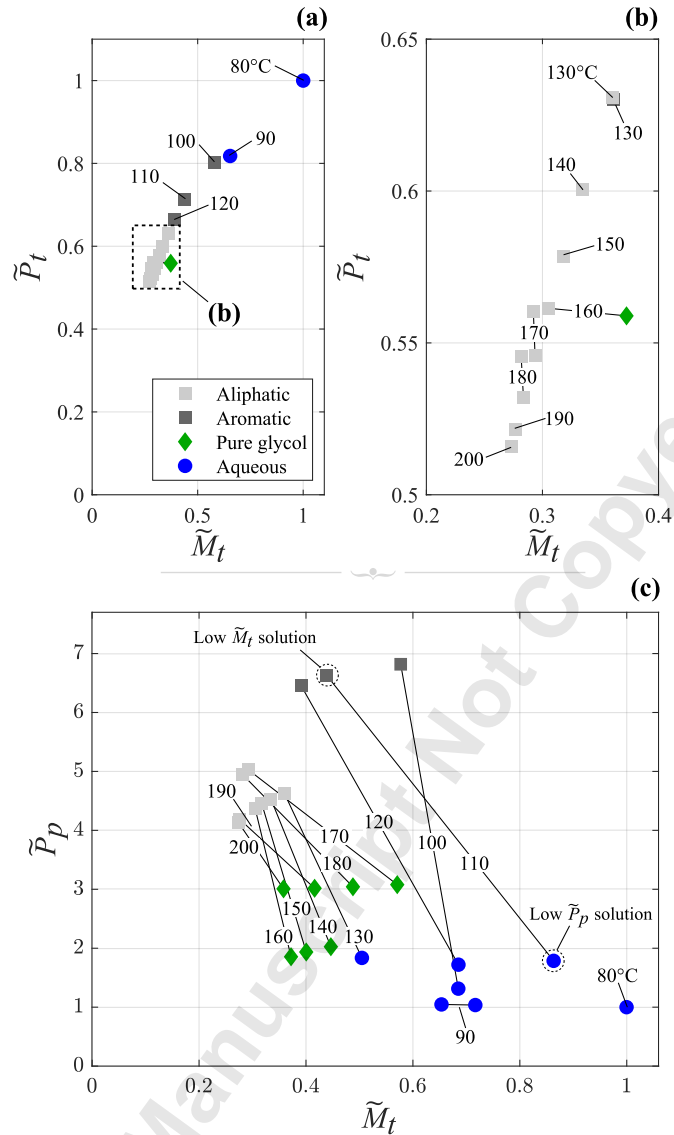
586 Figures 10(a) and 10(b) show \tilde{P}_t versus \tilde{M}_t for the Pareto efficient coolants. Data
587 points were generated at 10°C coolant inlet temperature intervals (these temperatures
588 are labelled on the plots). Pareto fronts are illustrated by a single line connecting
589 coolants from the low \tilde{P}_t to low \tilde{M}_t solutions (*cf.* 160°C, 170°C and 180°C in Figure
590 10(b)). Pareto efficient solutions in between the low \tilde{P}_t and low \tilde{M}_t solutions are omitted
591 to aid visual interpretation. Four significant trends are observed:

592 1. Between 80 and 110°C there is a ~50% reduction in \tilde{M}_t and a ~30% reduction in \tilde{P}_t .

593 This highlights the benefit of using higher-temperature PEMFCs. Note, the

594 percentage reduction in \tilde{P}_t and \tilde{M}_t reduces as the temperature increases.

- 595 2. Aqueous coolants are favorable for LT-PEMFCs operating in the range 80-90°C, but
596 are not optimal for PEMFCs operating at temperatures above 90°C for two reasons:
- 597 • First, they have relatively low boiling points. At elevated temperatures
598 aqueous coolant loops must be pressurized to prevent boiling; this poses
599 challenges for the design of high burst pressure coolant channels and seals
600 within the stack.
 - 601 • Second, cooling systems operating with aqueous coolants need (as predicted
602 by the model) radiators with relatively large frontal areas. This increases core
603 drag and thus \tilde{P}_t .
- 604 3. Aromatic coolants are suited to IT-PEMFCs (100-120°C).
- 605 4. Aliphatic coolants are favorable at HT-PEMFC (120-200°C) operating temperatures.
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Figure 10: Pareto efficient coolants for 80–200°C. (a) Normalized total power versus Normalized total mass. (b) Magnification of (a). (c) Normalized pumping power versus Normalized total mass. The number labels correspond to the operating temperature.

613 **5.2 Selection without Core Drag**

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616 Figure 10(c) shows \tilde{P}_p versus \tilde{M}_t for the Pareto efficient coolants. It is evident
 617 from comparison of Figures 10(a) and 10(c) that core drag has a significant impact on
 the selection of favorable coolants. The trend in Figure 10(c) aligns with the prevalent

618 use of glycol and aqueous coolants in the automotive industry where the freestream
619 velocity (core drag) is small compared to aircraft and the mass is less critical. Note, the
620 low \tilde{P}_p to low \tilde{M}_t solutions are circled for 110°C with the connecting line signifying the
621 Pareto front. Three significant trends are observed:

- 622 1. There is an overall reduction in total mass as the operating temperature increases
623 from 80-200°C. The temperature difference driving the heat transfer between the
624 coolant and ambient air increases as the operating temperature increases – this
625 reduces the required heat transfer surface area in the radiator for a given heat
626 load, i.e. a smaller (and thus lower mass) radiator can be used in the TMS. It is
627 important to note that the trend is not monotonic. For instance, the total mass
628 increases from 100-110°C for aqueous coolants, and from 160-170°C for pure
629 glycol. This is due to changes in coolant composition to satisfy the boiling margin. If
630 the PEMFC operating temperature exceeds the boiling point of a coolant, then that
631 coolant can no longer be considered for selection – this means that a coolant that
632 was deemed sub-optimal at a lower operating temperature may become pareto
633 efficient at a higher operating temperature.
- 634 2. Aqueous coolants begin to boil beyond 130°C. The low \tilde{P}_p Pareto efficient solutions
635 switch from aqueous coolants to pure glycols accordingly.
- 636 3. The Pareto fronts result in a trade-off between \tilde{P}_p and \tilde{M}_t . Aromatic and aliphatic
637 coolants generally result in higher pumping powers and lower total masses
638 compared with aqueous solutions and pure glycols at a specific temperature. For
639 example, at 170°C, $\tilde{P}_p = 5.0$ and $\tilde{M}_t = 0.29$ for the Pareto efficient aliphatic, and $\tilde{P}_p =$

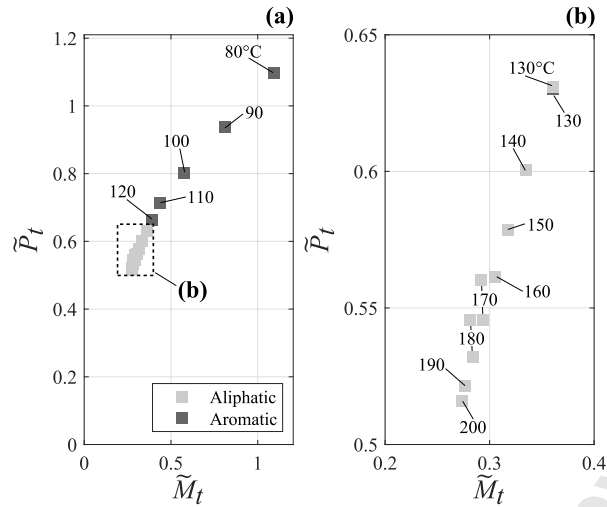
640 3.1 and $\tilde{M}_t = 0.57$ for the Pareto efficient pure glycol – as such the aliphatic would
641 be selected for a low mass use case and the glycol would be selected for a low
642 pumping power use case.

643
644 **5.3 Selection with Core Drag – with the Minimum Temperature and Electrical**
645 **Conductivity Thresholds**

646
647 The minimum temperature constraint from Table 1 was applied to the results in
648 Figures 10(a) and 10(b) to generate Figures 11(a) and 11(b). It is apparent that aqueous
649 and pure glycol solutions are no longer viable – this suggests that hydrocarbon-based
650 coolants are the most suitable for aircraft at a coolant pressure of 1 bar (pressurizing
651 the coolant loop can raise the boiling point of aqueous solutions, but this approach is
652 not considered in this study). Aromatics show favorable performance between 80-
653 130°C while aliphatics outperform them between 130-200°C. Improvements in
654 performance are shown to diminish at elevated temperature and so coolant selection
655 is more important for aircraft powered by LT and IT-PEMFCs than those powered by
656 HT-PEMFCs. Further improvements in system-level performance must come from
657 other developments in the TMS beyond coolant selection and elevated temperatures.

658 Mohapatra and Loiskits report that the electrical conductivity of aromatics and
659 aliphatics is negligible due to their dielectric properties [19]. In contrast, aqueous
660 solutions necessitate the use of inhibitors and deionizers to control electrical
661 conductivity. Hence, the aromatics and aliphatics outlined in Figure 11 also satisfy the
662 electrical conductivity threshold (*cf.* Table 1).

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Figure 11: Pareto efficient coolants for 80–200°C. (a) Normalized total power versus Normalized total mass. (b) Magnification of (a). The number labels correspond to the operating temperature.

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5.4 Use Cases for Coolant Selection

Table 5 outlines several practical cases pertinent to coolant selection for liquid cooled PEMFC applications – the requirements from Table 1 are applied. Case I is the most relevant to aircraft; Cases II and III are relevant to applications where minimizing radiator core drag is not an essential TMS requirement. Applying the methodology developed in this paper to different use cases demonstrates its versatility.

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Table 5: Liquid coolant use cases.

Case	Delineation
I	<u>Aerospace</u> : typified by low mass and low parasitic power. Pareto efficient coolants that minimize \tilde{P}_t and \tilde{M}_t .
II	<u>Automotive</u> : where low mass is prioritized over low pumping power.

Low \tilde{M}_t solutions on the Pareto front that minimize \tilde{P}_p and \tilde{M}_t .

Marine: where low pumping power is prioritized over low mass.

III

Low \tilde{P}_p solutions on the Pareto fronts that minimize \tilde{P}_p and \tilde{M}_t .

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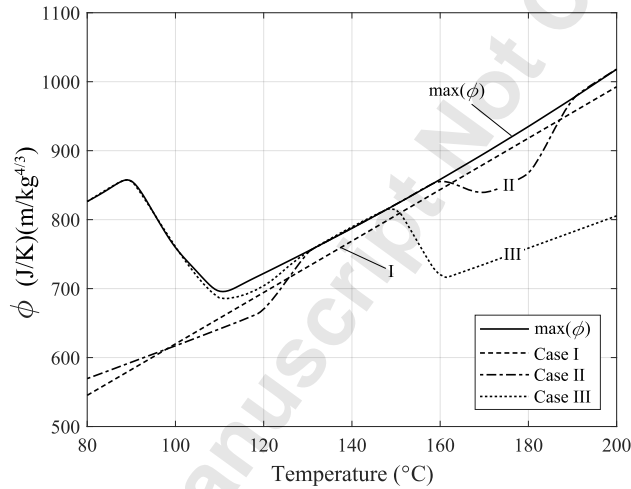
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In §3 the FoM (ϕ) was introduced for expedient screening of coolants. The screening technique involves selecting a coolant by maximizing ϕ at a given operating temperature. Figure 12 plots the maximized ϕ against temperature (the $\max(\phi)$ curve). Equation (1) was used to calculate ϕ for the Pareto efficient coolants for the cases described in Table 5 – these are plotted on Figure 12 for comparative purposes. Cases I and II show agreement with the $\max(\phi)$ for $>110^\circ\text{C}$ and Case III shows agreement with the $\max(\phi)$ for $<150^\circ\text{C}$. Regions where there is a lack of agreement between the $\max(\phi)$ curve and the curves for Cases I to III result from the difference in approach to generating the data used to plot the curves – data for the three use cases are obtained from the model, which captures system-level objectives, whereas data for the $\max(\phi)$ curve is obtained from coolant properties alone (see discussion in §4). While the $\max(\phi)$ curve is useful for screening purposes in preliminary TMS design, the *model* is recommended for higher fidelity selection because it uses the Pareto efficient solutions for the relevant case. For example, at 80°C the Pareto efficient coolant for Case I achieves a 53% decrease in \tilde{M}_t and a 22% decrease in \tilde{P}_t compared to the coolant predicted by $\max(\phi)$ – selecting a coolant with $\max(\phi)$ alone would result in sub-optimal performance.

698 The modeling approach presented in this paper may not be practical where
699 expedient coolant selection is required. In such scenarios, a TMS designer could use the
700 curve from Figure 12 for the case that is most pertinent to their application. The coolant
701 being considered is suitable for the application if ϕ matches the pertinent case at a
702 given temperature (note: the coolant would also have to meet other system specific
703 considerations, such as those in Table 1 for a PEMFC-powered aircraft). It is important to
704 recognize that this approach may not necessarily yield the optimal coolant.

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Figure 12: Cases for selecting suitable coolants. The requirements from Table 1 are applied.

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6. CONCLUSION

714 Two approaches to selection of liquid coolants for Proton Exchange Membrane
715 Fuel Cell (PEMFC) powered aircraft were considered for PEMFCs with operational
716 temperatures in the range 80-200°C. The first approach maximized a Figure of Merit
717 (FoM); the second approach relied on output of Pareto efficient solutions from a

718 physically informed model of the Thermal Management System (TMS). The results from
719 both approaches showed that coolant selection is highly sensitive to the PEMFC stack
720 temperature. The outputs from the model indicated that there is a trade-off between
721 mass and parasitic power of the TMS, and that TMS performance improves at elevated
722 temperatures. The FoM provides a useful method for expediently screening coolants,
723 but the *model* is recommended for optimal coolant selection.

724 The outputs from the model provided two key findings pertinent to PEMFC-powered
725 aircraft:

- 726 1. It was shown for the case study presented here (a hybrid-electric aircraft using a
727 1MW PEMFC stack) that hydrocarbon-based coolants are favorable, with aromatics
728 optimal for coolant inlet temperatures $<130^{\circ}\text{C}$ and aliphatics optimal for coolant
729 inlet temperatures $>130^{\circ}\text{C}$.
- 730 2. There are diminishing gains in performance at elevated temperatures. As such, a
731 step change in system-level performance must come from developments other
732 than coolant selection and increases in operating temperatures.

733 734 **ACKNOWLEDGMENT**

735
736 The authors would like to thank GKN Aerospace for their financial support and
737 expertise, and Matthias Schröder (DLR) for providing the heat exchanger sizing data that
738 enabled a comparison between models in Appendix B.

739 The datasets generated and supporting the findings of this article are obtainable
740 from the corresponding author upon reasonable request.

741

742 **APPENDIX A: FIGURE OF MERIT DERIVATION**

743

744 Firstly, consider the heat transfer rate given in Equation (4); fluid properties are
745 expressed as a separate grouping.

746

747
$$\dot{Q} = c_p \rho \cdot Q \Delta T \quad (4)$$

748

749 The fluid properties depend on the coolant however the flow rate and
750 temperature difference are constant. Equation (5) shows the Darcy-Weisbach equation,
751 it is used to evaluate the pumping power.

752

753
$$\Delta p/L_p = f \frac{\rho V^2}{2 D_h} \quad (5)$$

754

755 The friction factor for fully developed turbulent pipe flow can be expressed as a
756 function of Reynolds number; the form of Blasius's power law approximation is adopted
757 in Equation (6) [36].

758

759
$$f = C/Re^b \quad (6)$$

760

761 Equation (7) relates the pressure loss and friction factor to the pumping power
762 by substituting (5) and (6).

763

764
$$P_p = \left(\frac{CA^{b-2}L_p}{2D_h^{b+1}} \right) \cdot \rho^{1-b} \mu^b \cdot Q^{3-b} \quad (7)$$

765

766 The flow rate in (7) is substituted with (4) to form Equation (8). To select
767 coolants with a low mass, the specific heat transfer rate is adopted; this is analogous to
768 specific strength in material selection. A high specific heat transfer rate corresponds to a
769 high heat transfer rate and low mass.

770

$$771 \quad P_p \propto \left(\frac{\dot{Q}}{\rho}\right)^{3-b} \frac{\rho^{1-b} \mu^b}{c_p^{3-b}} \quad (8)$$

772

773 By manipulating the heat transfer rate with the density of the coolant, the effect

774 of coolant mass is captured. The FoM (denoted by ϕ) is now derived by maximizing

775 the specific heat transfer rate (\dot{Q}/ρ) for a given pumping power – refer to Equation (9).

776

$$777 \quad \phi = \frac{c_p}{\mu^{(b/3-b)} \rho^{(1-b/3-b)}} \propto \frac{\dot{Q}}{\rho} \left(\frac{1}{P_p}\right)^{1/3-b} \quad (9)$$

778

779 For laminar and turbulent flow, $b = 1$ and $b = 0.2$ [36]. The ϕ for a turbulent

780 regime is given in Equation 10. As the friction factor is dimensionless the index b does

781 not affect the units of the FoM. It has units of (J/K)(m/kg^{4/3}).

782

$$783 \quad \phi = \frac{c_p}{\mu^{1/14} \rho^{2/7}} \quad (10)$$

784

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786 APPENDIX A: COMPARISON OF RADIATOR SIZING MODELS

787

788 Industry seldomly releases data pertaining to radiator mass. To aid comparison

789 in the wider literature, the dry radiator core mass predicted by this model is released

790 and it is compared to one developed independently by Schröder *et al.* [67]. A close

791 agreement between these models is not expected given the large uncertainty in the

792 correlations, and the differences in the construction of the models. Nevertheless, the

793 trend is consistent; the dry heat exchanger core mass diminishes monotonically as the

794 inlet coolant temperature increases.

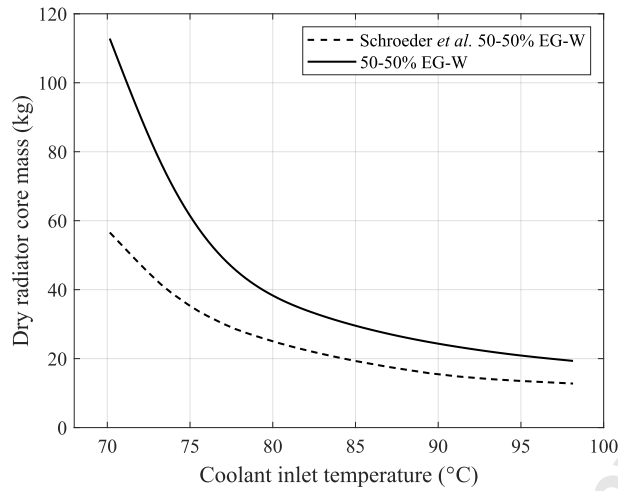
795 Schröder *et al.* employed a crossflow plate-fin heat exchanger with louvered fins
796 and was validated at a single coolant inlet temperature with data from a manufacturer.
797 Louvered fins are used on the airside; the coolant side has no secondary surface and
798 tubes are employed [68,69]. The heat exchanger model proposed in this study is
799 compared to Schröder *et al.* at coolant inlet temperatures from 70-98°C. The boundary
800 conditions used to compare the models are given in Table 6.

801 Figure 13 illustrates the comparison between the models based on the dry
802 radiator core mass using 50-50% EG-W as the coolant. On the airside, louvered fin
803 correlations were employed from London and Kays (3/8-6.06). Note, Schröder *et al.*
804 implemented louvered fin correlations from Chang *et al.* [43,68,69]. On the coolant side,
805 heat transfer and friction factor correlations for tubes were utilized [36,44,70]. Each
806 model relies on different correlations and coolant thermophysical property data. The
807 comparison presented in Figure 13 does not amount to a validation because of these
808 differences. Both models show consistent trends, the ranking of coolants should
809 therefore be reliable between models.

810
811 **Table 6:** Boundary conditions used for both the radiator sizing models.
812

Parameter	Magnitude	Unit
$T_{air_{in}}$	35	°C
$T_{air_{out}}$	50	°C
ΔT_l	10	°C
$p_{air_{in}}$	1	bar
$\Delta \hat{p}_{air}$	0.05	bar
$\Delta \hat{p}_l$	0.1	bar
\dot{Q}	400	kW

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814

815 **Figure 13:** Comparison of the radiator sizing model with 50-50% EG-W to [67]. Dry
 816 radiator core mass versus coolant inlet temperature.
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819 **NOMENCLATURE**

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A	Flow area [m ²]
A_{in}	Duct intake area [m ²]
b	Empirical constant
b_s	Stack cooling channel width [m]
C	Empirical constant
c_p	Coolant specific heat capacity [J/kgK]
D_h	Hydraulic diameter [m]
E	Convergence error
f	Friction factor

h	Altitude [ft]
\bar{h}	Convective heat transfer coefficient [W/m ² K]
j	Colburn j-factor
k	Coolant thermal conductivity [W/mK]
k_m	Radiator thermal conductivity [W/mK]
L_p	Pipe length [m]
L_s	Stack length (along the coolant axis) [m]
m_p	Pump mass [kg]
M_∞	Freestream Mach number
M_t	Total mass (coolant inside the radiator and pipes, dry radiator core, dry pump, and dry pipe mass) [m]
\tilde{M}_t	Normalized total mass*
\overline{Nu}	Nusselt number
N	Number of coolant passes in a bipolar plate
ρ	Fuel cell pitch (distance between bipolar plates) [m]
$\rho_{air_{in}}$	Air inlet pressure [Pa]
P_p	Pumping power [W]
P_t	Total power (pumping and core drag power) [W]
\tilde{P}_p	Normalized pumping power*

\tilde{P}_t	Normalized pumping and core drag power*
Pr	Prandtl Number
Q	Volume flow rate [m ³ /s]
\dot{Q}	Heat transfer rate [W]
Re	Reynolds number
t	Pipe wall thickness [m]
T	Temperature [°C]
$T_{air_{in}}$	Air inlet temperature [°C]
$T_{air_{out}}$	Air outlet temperature [°C]
T_{in}	Coolant inlet temperature [°C]
V	Bulk velocity [m/s]
\dot{W}_1	Power of a single stack [W]
x	Direction axis
δT	International Standard Atmosphere (ISA) temperature deviation (+25°C for hot day) [°C]
Δp	Pressure loss [Pa]
$\Delta \hat{p}_{air}$	Airside pressure loss target [Pa]
$\Delta \hat{p}_j$	Coolant side pressure loss target [Pa]
ΔT	Temperature difference [°C]

ΔT_l	Liquid coolant temperature difference [°C]
ε	Roughness [m]
η_d	Adiabatic diffuser efficiency
ξ	Allowable pressure loss coefficient
μ	Coolant dynamic viscosity [kg/ms]
ρ	Coolant density [kg/m ³]
ρ_m	Pipe and radiator density [kg/m ³]
ϕ	Figure of Merit (FoM) [(J/K)(m/kg ^{4/3})]
$\bar{\phi}$	Average Figure of Merit (FoM) [(J/K)(m/kg ^{4/3})]

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Table Caption List

Table 1	Critical system level requirements for liquid coolants inside a fuel cell powered aircraft.
Table 2	Comparison of proposed figure of merits.
Table 3	System model boundary conditions for coolant selection.
Table 4	Full factorial Design of Experiments with two levels to determine the sensitivity of total mass and total power to uncertain boundary conditions.
Table 5	Liquid coolant use cases.
Table 6	Boundary conditions used for both the radiator sizing models.

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Figure Captions List

Fig. 1	Schematic of a Proton Exchange Membrane Fuel Cell (PEMFC) and the electrochemical reaction.
Fig. 2	Notional liquid cooled proton exchange membrane fuel cell propulsion system with a ducted radiator installed under the wing.
Fig. 3	Coolant ontology. Note – Aliphatic and Aromatic Hydrocarbons may comprise blends, and ‘Other HC’ categorizes Hydrocarbons of unknown composition.
Fig. 4	(a) Figure of Merit for coolant categories spanning their operating temperature at atmospheric pressure. The dashed line encompasses all of

the Hydrocarbons. (b) Magnification of the Hydrocarbons which identifies Aliphatics, Aromatics, and Other HCs. *Refer to Table 1.

Fig. 5 (a) Integrated average Figure of Merit for coolant categories and (b) their operating temperature range. *Refer to Table 1.

Fig. 6 (a) A schematic of the system model including the radiator, stack, piping, coolant and pump. (b) A flowchart of the system model which includes the iterative radiator sizing algorithm.

Fig. 7 A schematic of radiator geometry (11.32-0.737-SR) with the respective correlations. *[43], **[36], and †[44].

Fig. 8 Percent contribution of the model terms on (a) total mass and (b) total power. derived from a full factorial Design of Experiment for an Aliphatic coolant. Up to 95% of the percent contribution is included.

Fig. 9 Pareto fronts at 80°C for (a) and (b), and 200°C for (c) and (d). Total power versus total mass: (a) and (c). Pumping power versus total mass: (b) and (d). Normalized by deionized water at 80°C. Excludes low temperature threshold.

Fig. 10 Pareto efficient coolants for 80–200°C. (a) Normalized total power versus Normalized total mass. (b) Magnification of (a). (c) Normalized pumping power versus Normalized total mass. The number labels correspond to the operating temperature.

Fig. 11 Pareto efficient coolants for 80–200°C. (a) Normalized total power versus Normalized total mass. (b) Magnification of (a). The number labels correspond to the operating temperature.

Fig. 12 Cases for selecting suitable coolants. The requirements from Table 1 are applied.

Fig. 13 Comparison of the radiator sizing model with 50-50% EG-W to [67]. Dry radiator core mass versus coolant inlet temperature.

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