

Temperature effects on the molecular Raman backscatter cross-sections due to narrow-band interference filters

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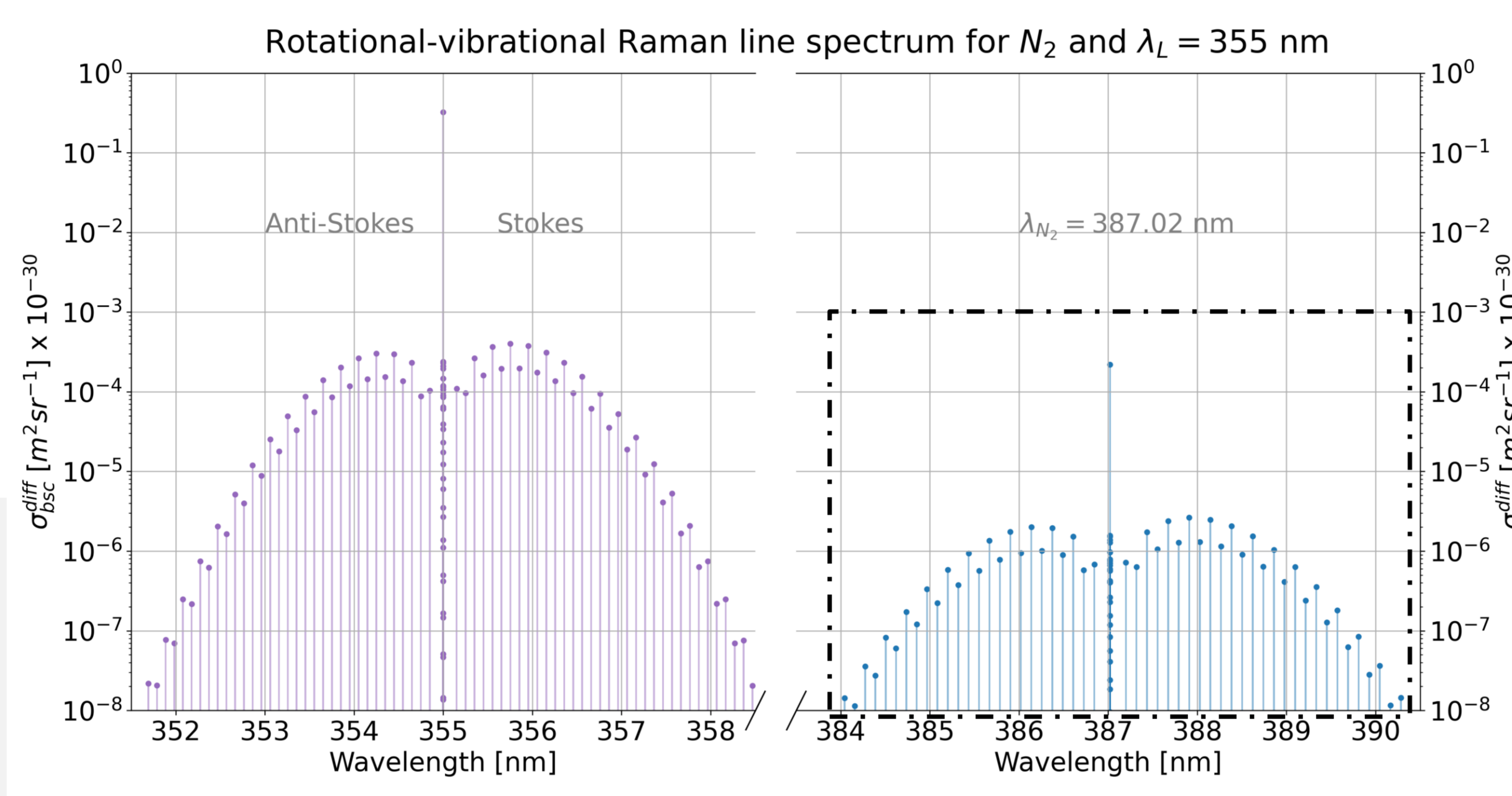
Introduction

When electromagnetic radiation interacts with molecules, elastic and inelastic scattering processes occur. In contrast to elastic scattering, the wavelength and the state of polarization of scattered photons may change when they are scattered inelastically. In this abstract we will focus on the inelastic scattering processes, the so-called Raman scattering. In particular, we investigate the effect of atmospheric temperature on the molecular rotational-vibrational (ro-vibrational) Raman backscatter cross-section which may occur after transmission of the backscattered radiation through narrow-band interference filters (IF). To analyze the consequence of the **changing temperature** we apply the equations published by M. Adam [1] to calculate the **temperature dependent ro-vibrational Raman backscatter cross-section for the N₂ molecule at 387 nm (laser wavelength of 355 nm)**. These equations have been implemented and evaluated as part of the Algorithm for Rayleigh and Raman calculations (ARC) that has been developed within ACTRIS [5].

Here, we show how the central wavelength and bandwidth of the IF affects the molecular Raman backscattering cross-section of N₂ for different temperature conditions.

Methodology

Figure 1. Pure rotational Raman backscatter spectrum of N₂ (left) and respective ro-vibrational Raman spectral lines for N₂ (right) in a dry standard atmosphere.



Filtering

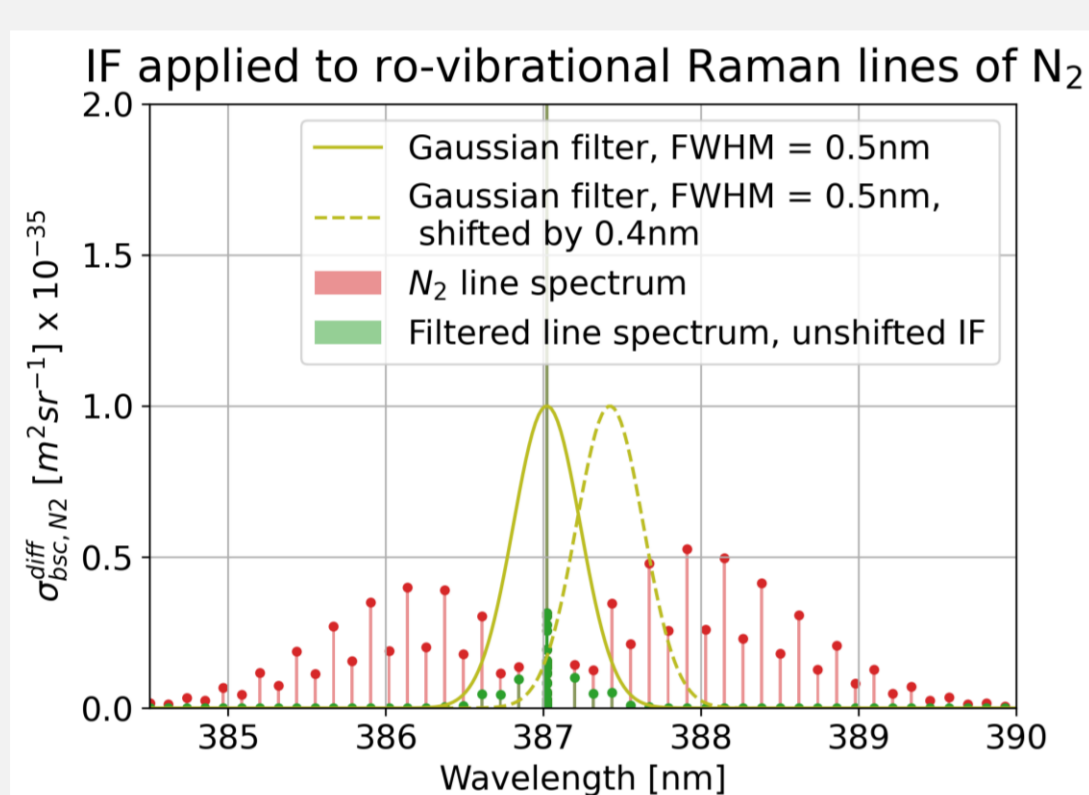


Figure 2. Application of a centered and a shifted Gaussian shaped IF.

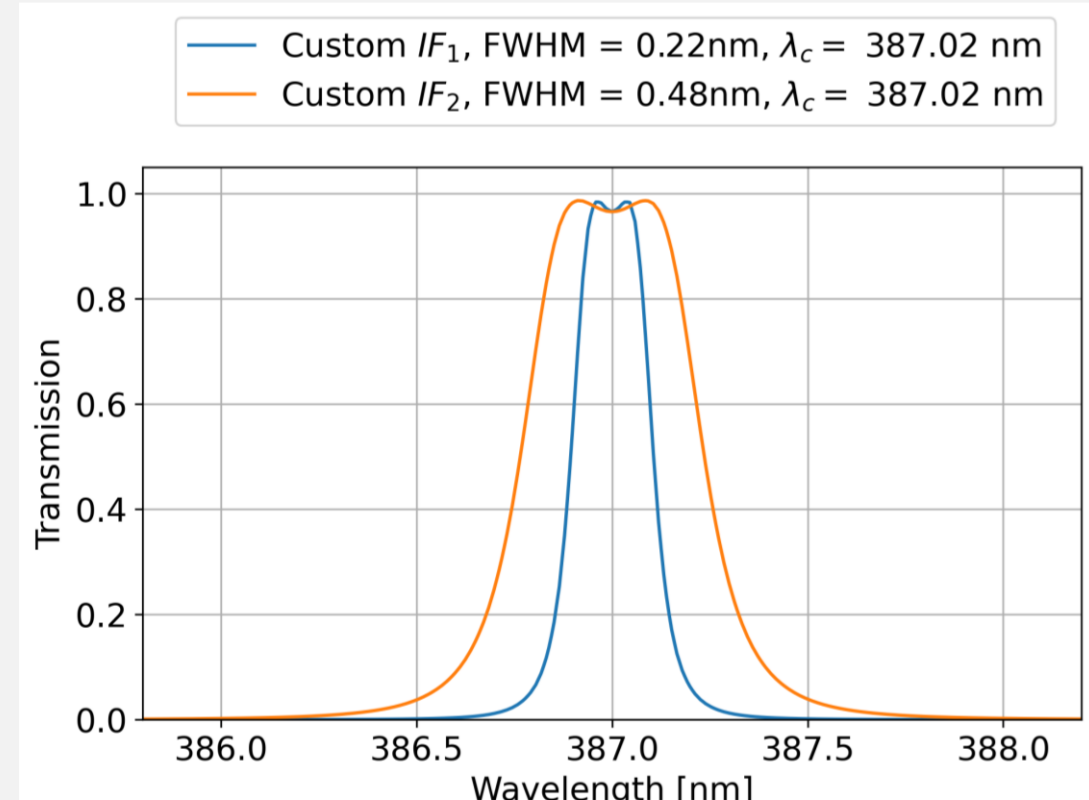


Figure 3. Custom double cavity IF.

Apply filter to ro-vibrational spectrum (highlighted in Fig. 1 with the dashed square)

$$\sigma_{bsc,i}^{eff} = \sigma_{bsc,i} \cdot T_{IF}(v_0 - v_{vib} + \Delta v_j)$$

Calculate relative deviation of effective backscatter cross-section due to temperature variation. Compared are the effective backscatter cross-section values at the two most extreme temperatures.

$$\chi [\%] = \frac{\sigma_{bsc,N_2}^{eff}(15\text{km}) - \sigma_{bsc,N_2}^{eff}(0\text{km})}{\sigma_{bsc,N_2}^{eff}(0\text{km})} \cdot 100$$

Initial equations

1. Differential backscatter cross section (SI-units)

$$\left(\frac{\partial \sigma}{\partial \Omega}\right)_{T,J} = \frac{\pi^2}{\epsilon_0^2} \cdot (v_0 - v_{vib} + \Delta v_j)^4 \cdot F_{MB}(T,J) \Phi_j'$$

2. Total backscatter cross section

$$\sigma_{bsc,i} = c_{N_2} \cdot \sum_j \left(\frac{\partial \sigma}{\partial \Omega}\right)_{T,J}$$

- T: Temperature
- J: Rotational quantum number
- c_{N₂}: Atmospheric molar fraction of N₂
- v_{0,vib,j}: Relevant wavenumbers (laser, rotational and vibrational transitions)
- F_{MB}: Maxwell-Boltzmann distribution
- Φ_j': Platzek-Teller coefficient for ro-vibrational Raman scattering

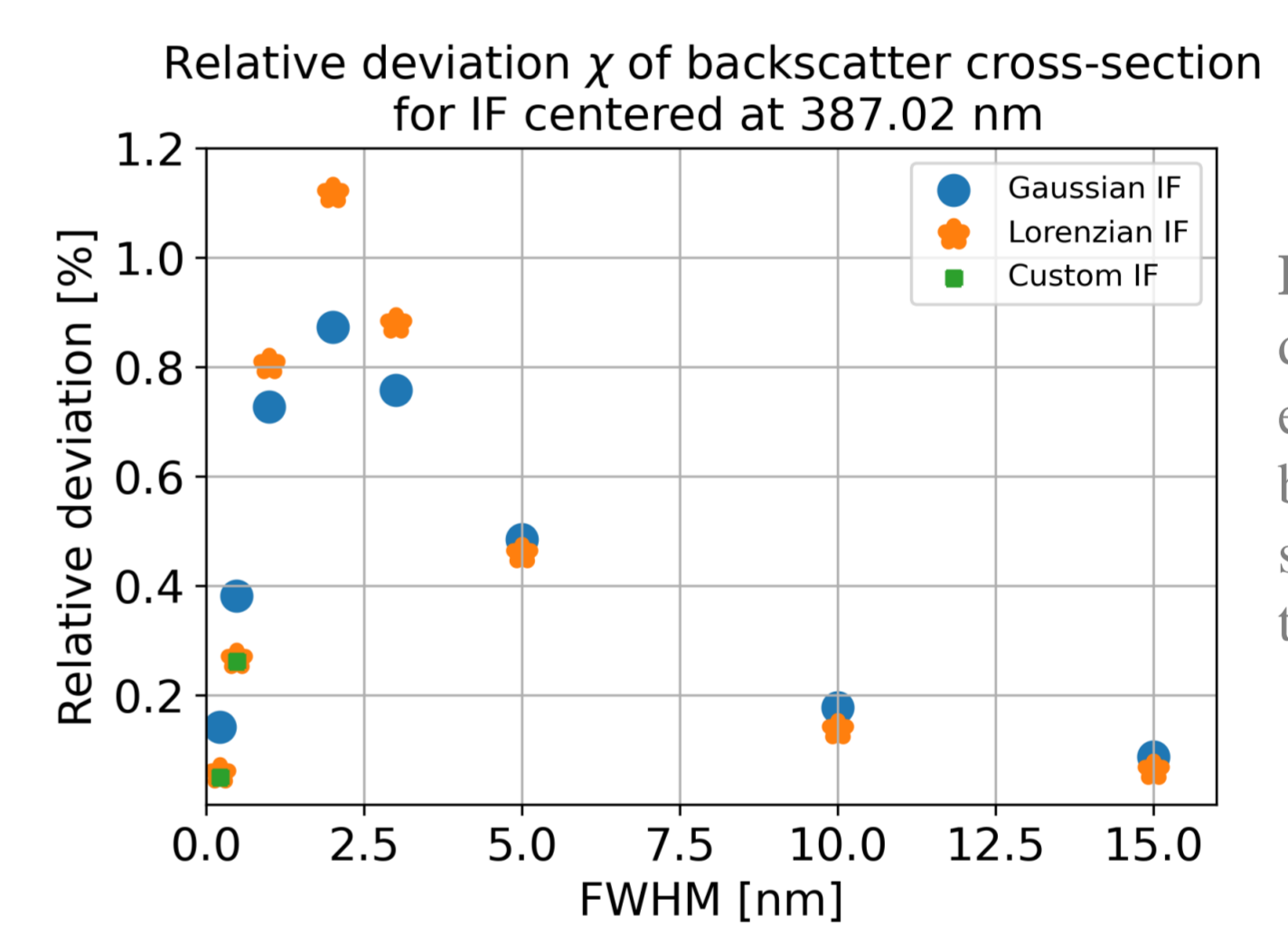


Figure 5. Relative deviation χ of the effective total backscatter cross-section due to temperature differences.

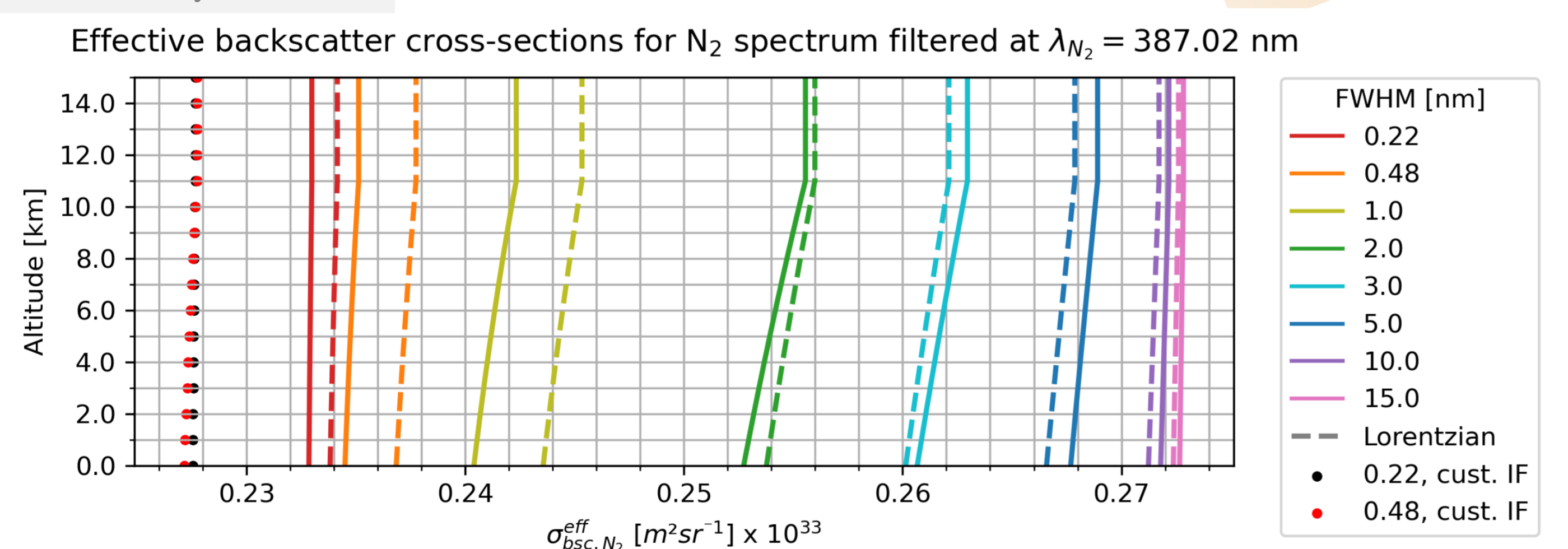


Figure 4. Effective backscatter cross-section variation along altitude from 0 to 15 km. Full lines correspond to Gaussian shaped filters, dashed lines to Lorentzian shaped filters and dotted lines to double cavity IF.

Summarizing plot

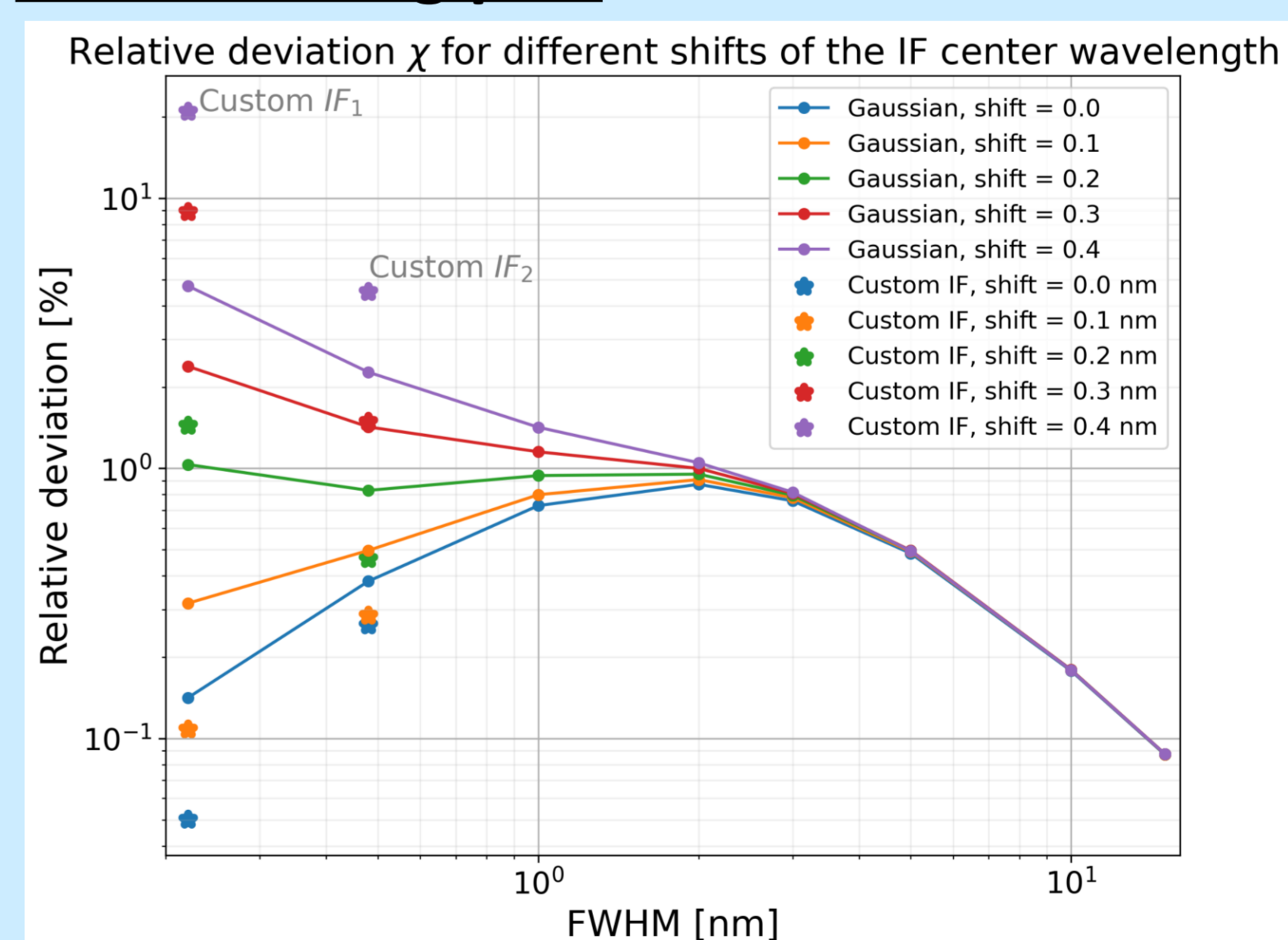


Figure 6. Relative deviation χ of the effective backscatter cross-section for two different double-cavity IF and different Gaussian shaped IF of different bandwidth shifted with respect to the central line of the ro-vibrational spectrum of N₂. Lorentzian shaped IF show a very similar behavior as the Gaussian ones. Consequently, they are spared here.

Conclusion

- Temperature dependence of the effective backscatter cross-section when using narrow-band IF applied to the N₂ Stokes ro-vibrational Raman spectrum
- For filters with narrow bandwidth (≤ 1 nm) or broad bandwidth (≥ 5 nm) the effective ro-vibrational backscatter cross-section is affected by less than 0.5% due to temperature changes from the atmosphere (temperature range: 288.15 K (0 km) – 216.65 K (15 km))
- Wavelength shifted IF (see Fig. 2 and Fig. 6): The IF shift can lead to temperature variations of the backscatter cross-section up to 11% for very narrow IF. The temperature variations are small ($\chi < 0.5\%$) for IF with bandwidths broader than 5 nm
- The transmission curve of the IF leads to temperature variations less than 0.2% of the backscatter cross-section

Future work

- Include more real IF bandwidths
- Use all three common lidar wavelengths
- Consider effect on the systematic error on lidar products (aerosol extinction and lidar ratio)
- **Conclude to recommendations for IF usage**

Acknowledgements, References

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