

Alignment–Rheology Relationship of Biosourced Rod-Like Colloids and Polymers under Flow

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S Supporting Information

ABSTRACT: Fluids composed of biosourced rod-like colloids (RC) and rod-like polymers (RP) have been extensively studied due to various promising applications relying on their flow-induced orientation (e.g., fiber spinning). However, the relationship between RC and RP alignment and the resulting rheological properties is unclear due to experimental challenges. We investigate the alignment—rheology relationship for a variety of biosourced RC and RP, including cellulose-based particles, filamentous viruses, and xanthan gum, by simultaneous measurements of the shear viscosity and fluid anisotropy under rheometric shear flows. For each system, the RC and RP contribution to the fluid viscosity, captured by the specific viscosity η_{sp} , follows a universal trend with the extent of the RC and RP alignment independent of concentration. We further exploit this unique rheological-structural link to retrieve a dimensionless parameter (β) directly proportional to η_{sp} at zero



shear rate $(\eta_{0,sp})$, a parameter often difficult to access from experimental rheometry for RC and RP with relatively long contour lengths. Our results highlight the unique link between the flow-induced structural and rheological changes occurring in RC and RP fluids. We envision that our findings will be relevant in building and testing microstructural constitutive models to predict the flow-induced structural and rheological evolution of fluids containing RC and RP.

INTRODUCTION

Biosourced rod-like colloids (RC) and rod-like polymers (RP) have excellent mechanical and optical properties and are often regarded as sustainable and biocompatible building blocks.¹⁻ These features have been exploited to form novel materials $^{8-10}$ with applications in biomedical¹¹⁻¹⁴ and food engineer-Classical examples of biosourced RC that can be ing.¹ produced in industrially relevant quantities comprise cellulose nanofibrils, cellulose nanocrystals, and protein nanofibrils. Nonetheless, these RC are characterized by a polydisperse contour length which complicates the prediction of their flow behavior. In contrast, filamentous viruses are monodisperse RC suited for fundamental studies regarding the dynamics of rodlike object dispersions.^{21,22} Biosourced RP comprises a myriad of polyelectrolytes, including xanthan gum, carboxymethyl cellulose, and hyaluronic acid, in aqueous environments that promote a rod-like conformation of the polymer chain (i.e., salt-free solutions at pH far from the isoelectric point of the functional group).²³ In most applications (e.g., inkjet printing, extrusion, and fiber spinning), controlling the flow-induced orientation and the resulting rheological properties of RC dispersions and RP solutions is crucial to achieve the desired functional and mechanical properties. The shear rheology of biosourced RC and RP fluids has been investigated extensively.²⁴⁻²⁸ However, the link between RC and RP alignment and the resulting rheological properties (e.g., shear viscosity) has not yet been completely elucidated. On this front, using rheo-small angle neutron scattering (rheo-SANS),

Förster et al.²⁹ showed a direct relationship between the shear viscosity (η) and the orientational order of worm-like micelles and elongated block copolymers under rheometric shear flow. Specifically, all the systems investigated by Förster et al.²⁹ followed a unique exponential decrease of η with the enhanced particle alignment, captured by the structural order parameter (S), as $\eta \propto e^{-AS}$, with A being an empirical fitting parameter. A similar exponential relationship was shown for monodisperse filamentous viruses by Lang et al. using a rheo-SANS setup.^{30,31} More recently, Calabrese et al.,³² coupling microfluidics with flow-induced birefringence (FIB) could verify the exponential viscosity decay with the increasing extent of particle alignment, in analogy with the studies of Förster et al.²⁹ and Lang et al.^{30,31} Nonetheless, it is unclear to what extent this exponential relationship is a general feature of RC and RP fluids. In other studies, the extent of RC/RP alignment and the resulting shear viscosity have been investigated (via FIB and rheo-scattering) but have not been directly linked.^{33–38} In the present work we explore the relationship between RC and RP alignment and the resulting rheological

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properties (alignment-rheology relationship) for a wide variety of naturally derived RC and RP with significantly distinct morphology, length scales, and flexibility. As model biosourced RC, we use cellulose nanocrystals (CNC), TEMPO-oxidized cellulose nanofibrils (OCNF) with two different average contour lengths, and a filamentous virus (*Pseudomonas* phage, Pf1). As biosourced RP, we use the polyelectrolyte xanthan gum (XG) in salt-free aqueous solutions. In this medium, the XG chains adopt a rod-like conformation due to intrachain electrostatic repulsion.^{39,40}

Rigid Rod Theory. A suitable theoretical framework to describe the behavior of RC dispersions and RP solutions is given by the Doi-Edwards (DE) theory developed for monodisperse rigid rods in a continuum medium.^{41,42} The DE theory defines distinct concentration regimes based on the number of rod-like objects per unit volume, $\nu = (4\phi)/(d^2L\pi)$ (in m⁻³), where L is the contour length, d is the diameter, and ϕ the volume fraction of the particles. The onset of the semidilute regime is defined as $\nu^* = L^{-3}$, while the onset of the concentrated regime is $\nu^{**} = L^{-2}d^{-1}$. Alternatively, ν^* and ν^{**} can be expressed in terms of concentration (c) with units of mg/mL as $c^* = \rho_p \pi d^2 / (4L^2)$ and $c^{**} = \rho_p \pi d / (4L)$, respectively, by knowing the particle density (ρ_p) . In the dilute regime (i.e., $\nu/\nu^* = c/c^* < 1$), the rotational diffusion coefficient is $Dr \equiv Dr_0 = \frac{3k_bT \ln(L/d)}{\pi \eta_b L^3}$, where k_b is the Boltzmann constant, T is the absolute temperature, and η_s is the solvent viscosity.⁴¹ Importantly, Dr_0 does not account for interparticle interactions; thus, it is independent of the particle concentration (see dashed line in Figure 1). In the semidilute



Figure 1. Theoretical normalized rotational diffusion coefficient $(Dr/Dr_0, \text{ solid blue line})$ and zero-shear rate specific viscosity $(\eta_{0,sp}, \text{ solid black line})$. The Dr/Dr_0 and $\eta_{0,sp}$ are computed using L = 1000 nm, d = 3 nm, and K = 1300 in eqs 1 and 2, respectively. The dashed blue line indicates $Dr/Dr_0 = 1$ and the colored area indicates the concentration above which the rods are confined in a tubelike confinement as envisioned by the DE theory.

regime (i.e., $\nu^* < \nu < \nu^{**}$), the DE theory assumes the rods as confined in an imaginary tube, where the tube represents the available space for the rods to rotate along their main axis unconstrained by the neighboring rods.⁴¹ In this regime, the DE theory gives the rotational diffusion coefficient as^{41,42}

$$Dr = Dr_0 K (\nu L^3)^{-2}$$
(1)

where K is a dimensionless prefactor dictating the scaling transition from dilute to semidilute regime. From the

simulation and experiments of monodisperse and rigid RC, it has been reported that $K = 1300^{21,31,43}$ However, RC

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has been reported that $K = 1300.^{-0.515}$ However, RC flexibility has been shown to affect K. Indeed, for the semiflexible Pf1, K = 2300 has been reported.^{21,31} The DE theory gives the zero-shear rate specific viscosity $\eta_{0,sp}$ as^{31,44}

$$\eta_{0,\text{sp}} = \frac{(\eta_0 - \eta_{\text{s}})}{\eta_{\text{s}}} = \frac{\nu \pi L^3}{90 \ln L/(2d)} + \frac{\nu^3 \pi L^9}{30K \ln L/(2d)}$$
(2)

where η_0 is the limiting shear viscosity at $\dot{\gamma} \rightarrow 0$. Plotting $\eta_{0,sp}$ as a function of $\nu/\nu^* = c/c^*$, considering a representative rodlike particle (L = 1000 nm and d = 3 nm) and K = 1300 in eq 2, two distinct regimes are observed (Figure 1). At relatively low concentrations, $\eta_{0,sp} \propto \nu/\nu^* = c/c^*$, while at relatively high concentrations, $\eta_{0,\text{sp}} \propto (\nu/\nu^*)^3 = (c/c^*)^3$ (see Figure 1). Importantly, $\eta_{0,sp}$ follows the dilute scaling up to ν/ν^* = $c/c^* \sim 10$. This indicates that the rod-like particles are practically unconfined up to $\nu/\nu^* = c/c^* \sim 10$. At $\nu/\nu^* = c/c^*$ \gtrsim 40, the rod-like particles are confined by the neighboring particles, following the scaling $\eta_{0,sp} \propto (\nu/\nu^*)^3 = (c/c^*)^3$ based on the tube assumption. Analogous to $\eta_{0,sp}$, the Dr/Dr_0 scaling (solid blue line in Figure 1, based on eq 1) intercepts with Dr_0 at $\nu/\nu^* = c/c^* \sim 40$, implying that the rod-like particles interact significantly with each other at $\nu/\nu^* = c/c^* \gtrsim 40.^{21}$ The scalings $Dr/Dr_0 \propto (\nu/\nu^*)^{-2}$ and $\eta_{0,sp} \propto (\nu/\nu^*)^3$ are expected to be valid in the limiting case where the underlying tube assumption, from the DE theory, holds (see Figure 1).

MATERIALS AND METHODS

Materials. An aqueous CNC stock dispersion was purchased from CelluForce (NCV100, Montreal, Canada, pH 6.3). Two distinct OCNF (OCNF-L and OCNF-S) produced via TEMPO-mediated oxidation^{45,46} were donated (Nippon Paper Group, Japan) as aqueous dispersions: OCNF-L with a degree of oxidation of 1.3-1.6 mmol/g, and OCNF-S with a degree of oxidation of 1.5-1.9 mmol/g. A Pf1 aqueous dispersion (10 mM K-phosphate buffer (pH 7.6), 2 mM MgCl₂ and 0.05% NaN₃) was purchased from ASLA biotech (Latvia). A 10 mg/mL XG aqueous stock was prepared via dissolution of XG powder (Keltrol T Plus, CP Kelco, Japan) in deionized water. Each concentration series was prepared gravimetrically using a microbalance by the dilution of the respective stock. XG solutions and OCNF dispersions were prepared in deionized water. Pf1 dispersions were prepared in Tris-EDTA buffer (10 mM Tris-HCl, 1 mM disodium EDTA, pH 8.0, Sigma-Aldrich, BioUltra). CNC dispersions were prepared in a solvent composed of a glycerol:water mixture containing 60 vol % glycerol (Sigma-Aldrich, 99%). Glycerol was added to the aqueous solution to enhance the solvent viscosity and shift the onset of CNC alignment to lower shear rate values, extending the experimental window of measurable flow-induced alignment.

Steady Shear Rheo-Optical Measurements. Rheo-optical measurements were performed using a stress-controlled rheometer (Discovery HR-3, TA Instruments, U.S.A.) with a modular microscope accessory (MMA, TA Instruments, U.S.A.), schematically shown in Figure 2a. The rheometer is equipped with an upper Peltier plate (UPP, TA Instruments, U.S.A.) for temperature control and a glass bottom plate for optical access. A blue-light LED passes a linear polarizer before being focused at the upper rotating plate with a 5× objective lens. The beam is reflected by the top rotating plate (radius r = 20 mm), passes through the optically transparent bottom plate, an orthogonal linear polarizer (i.e., analyzer), and the image is recorded with a digital camera, in the given order. The top rotating plate is polished, with an estimate roughness of ~100 nm to act as a mirror. Due to the crossed polarizers, only light that experiences a phase shift reaches the camera. Such a phase shift is caused by the birefringence



Figure 2. (a) Schematic of the rheo-optical setup. (b) Exemplary image acquired at the center of the plate (x = y = 0 mm) for a 4 mg/mL cellulose nanocrystals (CNC) dispersion in glycerol/water mixture (60 vol % glycerol) at a shear rate at the edge of the plate of $\dot{\gamma} = 900 \text{ s}^{-1}$. The flow direction is indicated by the yellow arrow. The dashed lines indicate the specific angle at which the light intensity is maximum (Θ_m). (c) Representative normalized intensity (*I*), after background subtraction, acquired in the region of interest (ROI) as a function of shear rate for a 5 mg/mL CNC dispersion in 60 vol % glycerol. The images for the lowest and highest shear rate ($\dot{\gamma} = 0.1$ and 900 s⁻¹) are shown as insets in (c).

of the fluid (Δn) , associated in our experiments with a preferential orientation of the RC/RP. As the light enters perpendicular to the plate and thereby flow direction, this configuration probes the RC/RP projection in the vorticity-velocity plane (x-y plane, Figure 2). At a particular radial distance from the center of the plate (i.e., x = y = 0), the light intensity depends on the angle Θ along the circumference, yielding a typical cross-shaped pattern, as shown in Figure 2b for a representative sample.^{47,48} Thus, at a given distance from the center of the plate along the Θ angle (e.g., the yellow arrow in Figure 2b), the probed light intensity follows a repeating increase-decrease trend with Θ . To increase sensitivity, the spatially averaged light intensity is measured at a specific angle Θ_m where the light intensity is maximum, as illustrated in Figure 2b by the dashed white lines. Additionally, to use the full range of the bit depth of the camera, intensity of the source LED light and pixel gain are adjusted for each sample. A region of interest (ROI) of rectangular shape located at a distance $W \approx 0.35$ mm from the edge of the plate (red rectangles in the insets of Figure 2c) is selected to retrieve the background subtracted and spatially averaged light intensity (I). Details of the measurement technique are included in the Supporting Information (Section S1). The ROI location is chosen to exploit the maximal shear rate while avoiding possible interference occurring at the edge of the plate due to the liquid-air interface and the liquid meniscus. Additionally, the ROI is chosen to be as parallel as possible to the edge of the rotating upper plate to minimize shear rate variation along the radial direction. Within the ROI, the shear rate experienced by the fluid element is $\dot{\gamma} \simeq \Omega(r - W)/h$, where Ω (rad/s) is the angular velocity of the rotating upper plate and *h* is the height of the sample (Figure 2a). The shear rate in the ROI is comparable to the shear rate at the edge of the plate $\left(\dot{\gamma} = \frac{\Omega r}{h}\right)$ computed by the software of the rheometer (TRIOS software, with $\approx 1.5\%$ difference), thus we consider the shear rate at the edge of the plate as representative shear rate for both the rheological and the optical measurements. An exemplary measurement of the recorded, spatially averaged light intensity after background subtraction (I) as a function of shear rate ($\dot{\gamma}$) is shown in Figure 2c for 5 mg/mL CNC in a glycerol/water mixture containing 60 vol % glycerol.

 $\Delta n = \frac{\lambda}{2\pi h} \arcsin\left(\sqrt{\frac{I}{I_{\rm in}}}\right) \approx \frac{\lambda}{2\pi h} \sqrt{\frac{I}{I_{\rm in}}}$ (3)

with *h* the optical path, equal to the height of the sample (300 μ m), I_{in} the intensity of the LED light source $(I_{in} \gg I)$, and λ the wavelength of the light source.⁴⁷ Since h, λ , and I_{in} are kept constant in our experiment, $\Delta n \propto \sqrt{I}$. Additionally, $\Delta n \propto S$, where S is the structural order parameter obtained from rheo-SAS (small angle scattering) experiments, computed by the anisotropy of the two-dimensional scattering patterns, $^{49-52}$ hence, $\sqrt{I} \propto \Delta n \propto S$. This proportionality enables a direct comparison of our experiments with the literature on flow-induced birefringence and rheo-SAS of RC and RP fluids. The experimental window for \sqrt{I} is limited by (i) the detectability of light above the background noise at relatively low RC/RP concentrations and relatively low shear rates and (ii) sensor saturation at relatively high RC/RP concentrations and high shear rates. Simultaneously to the optical measurements, the steady state shear viscosity (η) of the sample is obtained within an operational window set by the lower torque limit (0.2 μ Nm) at low shear rates and inertia limits at relatively high shear rates. All of the experiments were performed at 25 + 0.01 °C.

RC and RP Characterizations. The morphology of the RC was characterized via atomic force microscopy (AFM, dimension ICON3 ScanAsyst, Bruker, U.S.A.). Dilute dispersions were deposited (~10 μ L) on a freshly cleaved mica substrate (Mica AFM disk, Bruker, U.S.A.) and left at rest for ~60 s. Subsequently, the excess material was washed with deionized water and air-dried. For Pf1, the mica substrate was functionalized with (3-Aminopropyl)triethoxysilane (APTES) prior to their deposition as described by Diener et al.⁵³ Representative AFM images are shown in Figure 3 for Pf1 (a), CNC (b), OCNF-S (c), and OCNF-L (d). From imaging analysis, a characteristic contour length $\langle L \rangle$ (obtained from the volume averaged length, $\langle L \rangle = \frac{\sum_{i}^{n} L_{i}^{4}}{\sum_{i}^{n} L_{i}^{3}}$), the diameter *d* and the persistence length l_{p} of the rod-like particles were extracted (summarized in Table 1).

the rod-like particles were extracted (summarized in Table 1). Additionally, we defined a polydisperisty index as PDI = $\langle L \rangle / \langle L_n \rangle$, where $\langle L_n \rangle$ is the number-averaged contour length.⁵⁴ The RC and RP flexibility is captured by the number of persistence length segments per contour length, as $N_p = \langle L \rangle / l_p$. The persistence length, l_p ,

The light intensity I at Θ_m is related to the birefringence Δn via



Figure 3. AFM (dimension ICON3 ScanAsyst, Bruker, U.S.A.) images of the rod-like colloids (RC) used in this study: (a) Pf1, (b) CNC, (c) OCNF-S, and (d) OCNF-L. The insets show exemplary RC with a scale bar of 100 nm.

Table 1. Relevant Parameters for the Biosourced RC and RP Used in This Work^a

| | Pf1 | XG | OCNF-S | OCNF-L | CNC |
|--------------------------|-------------------|--------------------|--------|--------|-------|
| $\langle L \rangle$ (nm) | 1960 | 1651 ⁵⁴ | 254 | 878 | 477 |
| d (nm) | 6.6 ⁴⁴ | 2.1 ⁵⁸ | 7.9 | 2.7 | 4.8 |
| $l_{\rm p}$ (nm) | 370 | 417 ⁵⁴ | 704 | 222 | 7000 |
| $N_{ m p}$ | 5.3 | 4.0 | 0.4 | 4.0 | 0.1 |
| PDI | 1.0 | 1.2^{54} | 1.7 | 2.0 | 1.8 |
| c* (mg/mL) | 0.013 | 0.002 | 1.140 | 0.011 | 0.119 |
| c** (mg/mL) | 3.97 | 1.50 | 36.64 | 3.62 | 11.86 |
| c (mg/mL) | 0.2-4 | 1 - 7 | 5-30 | 3-11 | 0.5-5 |

^{*a*}Representative parameters for XG are obtained from literature. The range of concentrations (*c*) of RC and RP investigated via rheo-optics are given in the bottom row.

determining the length of the rigid rod-like segments composing the RC, was determined using the mean-squared end-to-end distance (MSED) method for a worm-like chain model within the FiberApp routine (details in Usov and Mezzenga⁵⁵). Exclusively for XG, the characteristic dimensions are obtained from the literature because special experimental protocols are necessary for imaging of isolated XG chains using AFM, something that is outside the scope of the present study. From $\langle L \rangle$ and d, we estimate $c^* = \rho_{\rm p} \pi d^2 / (4 \langle L \rangle^2)$ and $c^{**} = \rho_p \pi d/(4 \langle L \rangle)$, respectively, by using a representative RC/RP density $\rho_p = 1500 \text{ mg/mL}$ for all the RC and RP investigated (Table 1).^{44,56,57} We note that c^* and c^{**} must be regarded indicatively, as RC/RP flexibility and polydispersity are not considered in their estimation. To obtain structural information about the shear-induced RC and RP orientation, we investigated a concentration range that enables the measurement of the shear-dependent light intensity, \sqrt{I} , due to the fluid birefringence. These concentration ranges, summarized in Table 1, mainly fall in the semidilute regime, except for XG and OCNF-L, where the shear-dependent \sqrt{I} was mostly measurable in the concentrated regime. For XG solutions at $c \gtrsim 2$ mg/mL, the pronounced excluded volume interactions were

corroborated by the presence of nematic ordering of the sample at rest (see Supporting Information (Section S2)).

RESULTS AND DISCUSSION

Flow-Induced Alignment of RC and RP. Simultaneous measurements of the steady shear viscosity and fluid anisotropy for the RC dispersions and RP solutions are shown in Figure 4. Since \sqrt{I} is linked with the number of aligned RC and RP through the optical path, we normalize the spatially averaged intensity as $\sqrt{I}/(c/c^*)$, referred to as reduced intensity (top row Figure 4).⁵⁹ To isolate the RC and RP contribution to the overall viscosity, we consider the specific viscosity, $\eta_{sp} = (\eta(\dot{\gamma}) - \eta_s)/\eta_s$ (bottom row of Figure 4). Generally, the reduced intensity increases with the increasing shear rate $\dot{\gamma}$ (top row in Figure 4). This indicates that more l_p segments of the RC and RP align preferentially with the flow as $\dot{\gamma}$ increases.⁶⁰ Specifically, $\sqrt{I}/(c/c^*)$ increases with a strong $\dot{\gamma}$ -dependence around the onset of measurable intensity. Contrarily, at relatively high shear rates, $\sqrt{I}/(c/c^*)$ follows a less pronounced increase with $\dot{\gamma}$, indicating that the RC and RP approach the maximum extent of alignment. These two regimes are particularly evident for Pf1 dispersions at high concentrations, where $\sqrt{I}/(c/c^*)$ reaches a plateau at high values of $\dot{\gamma}$ (e.g., Pf1 at the highest concentration). Additionally, the onset of fluid anisotropy (i.e., $\sqrt{I} > 0$) shifts progressively to lower values of $\dot{\gamma}$ with the increasing RC and RP concentration. This is due to the increasing level of confinement experienced by each RC and RP as the concentration increases, resulting in a decreasing critical shear rate for the onset of RC/RP alignment. For the XG solutions with nematic ordering at rest (i.e., at the highest concentrations, $c/c^* > 1000$), the $\sqrt{I}/(c/c^*)$ as a function of the shear rate undergoes an abrupt change in slope at $\dot{\gamma} \approx 10^{-1}$ s^{-1} . This behavior is possibly associated with two distinct dynamical processes occurring at relatively low and high shear rates. At low shear rates, the sharp increase of $\sqrt{I}/(c/c^*)$ with the shear rate is linked to the simultaneous breakage/ alignment of the nematic domains and the alignment of the XG backbone. Conversely, at high shear rates, the nematic domains break and the $\sqrt{I}/(c/c^*)$ trend can be associated uniquely to the alignment of XG backbone. These distinct dynamical processes occurring at relatively low and high shear rates are also supported by the presence of textured and homogeneous patterns in the raw images at low and high shear rates, respectively (see Supporting Information, Section S2).

From the rheological point of view, all dispersions are shearthinning, characterized by a decreasing η_{sp} with increasing $\dot{\gamma}$ (bottom row, Figure 4). The most shear-thinning dispersions are the Pf1, XG, and OCNF-L, following a slope of $\sim -3/4$ for a large range of shear rate. In comparison, the shorter CNC and OCNF-S appear less shear thinning with a slope of $\sim -1/$ 3. We note that for all the systems investigated, the zero-shear viscosity plateau at $\dot{\gamma} \rightarrow 0$ (η_0) can not be probed within the operational window of the rheometer.

Specific Viscosity Scaling. To link the extent of RC and RP alignment (captured by \sqrt{I}) and the viscosity as a function of the shear rate, we plot the specific viscosity (η_{sp}) versus the reduced intensity ($\sqrt{I}/(c/c^*)$) in the top row of Figure 5. For all RC and RP investigated, the specific viscosity decreases with the increasing $\sqrt{I}/(c/c^*)$. Thus, as the extent of particle

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Figure 4. Reduced intensity $\sqrt{I}/(c/c^*)$ (top row) and specific viscosity η_{sp} (bottom row) as a function of shear rate, $\dot{\gamma}$: (a) Pf1, (b) XG, (c) OCNF-S, (d) OCNF-L, and (e) CNC at different concentrations, given in normalized form as c/c^* . The triangles in the bottom row indicate the reference slopes of η_{sp} as a function of $\dot{\gamma}$.



Figure 5. Specific viscosity η_{sp} (top row) and rescaled specific viscosity η_{sp}/β (bottom row) as a function of the reduced intensity $\sqrt{I}/(c/c^*)$, both obtained at matching values of shear rate. (a) Pf1, (b) XG, (c) OCNF-S, (d) OCNF-L, and (e) CNC at different concentrations given in normalized form as c/c^* .

alignment increases, the fluid viscosity decreases. In addition, for a given RC or RP system, the overall shape of the curves appears to be self-similar independently of the concentration. Thus, we try to collapse the viscosity data for each dispersion by introducing a scaling factor β to the specific viscosity, as $\eta_{\rm sp}/\beta$ (see bottom row in Figure 5). To determine the scaling factor β for each RC or RP system, a reference $\eta_{\rm sp}$ versus the respective $\sqrt{I}/(c/c^*)$ curve is chosen at an intermediate

concentration, referred to as $\eta_{\text{sp,ref}}$. All the η_{sp} curves are then interpolated, and β is obtained for each concentration from the median of the ratio of the viscosity curves, $\eta_{\text{sp}}/\eta_{\text{sp,ref}}$. Since we keep our analysis at the scaling level, the choice of the reference curve ($\eta_{\text{sp,ref}}$) is arbitrary, and it does not significantly alter the β scaling.

The bottom row of Figure 5 shows the rescaled viscosity (η_{sp}/β) as a function of $\sqrt{I}/(c/c^*)$. For each RC and RP



Figure 6. (a) Measured scaling factor β (left axis, blue symbols) as a function of Pf1 concentration (c/c^*) compared with the theoretical $\eta_{0,sp}$ based on eq 2 (right axis, black line). (b–e) Scaling factor β as a function of concentration c/c^* for the other RC and RP fluids investigated. The lines are power law fits describing the scaling of β with RC and RP concentration.

system, the curves obtained at different concentrations collapse into a master curve using the rescaled viscosity. Surprisingly, a single master curve captures each RC and RP systems well, ranging from the rigid CNC $(N_p < 1)$ to the more flexible Pf1 and XG $(N_p > 1)$, covering a wide concentration range. It is worth noting that all the RC and RP systems investigated share a similar trend of the reduced viscosity (η_{sp}/β) as a function of the reduced intensity $(\sqrt{I}/(c/c^*))$ despite their differences in contour length, flexibility, concentration range, and chemical composition (bottom row, Figure 5). This suggests that the relationship between the specific viscosity and the alignment of RC and RP is ruled by the same underlying mechanism. Specifically, our data can be described reasonably well with an exponential function at intermediate value of \sqrt{I} (see Supporting Information, Section S3), in analogy to the exponential relationship between shear viscosity and the structural order parameter S obtained from rheo-SANS experiments on fd-viruses^{30,31} and block copolymers.²⁹

The idea of collapsing the $\eta_{\rm sp}$ versus $\sqrt{I}/(c/c^*)$ by introducing the scaling factor β to $\eta_{\rm sp}$ (as $\eta_{\rm sp}/\beta$), is inspired by the method introduced by Förster et al.,²⁹ and later used by Lang et al.,^{30,31} for the analysis of rheo-SANS experiments of RC dispersions. Specifically, they showed that by plotting η/η_0 as a function of *S*, the curves could collapse onto a single master curve for several concentrations within the semidilute regime. In the method introduced by Förster, η_0 is a scaling factor for the shear viscosity (i.e., η/η_0), analogously to the scaling factor β to $\eta_{\rm sp}$ in our analysis (i.e., $\eta_{\rm sp}/\beta$); thus, we expect that $\beta \propto \eta_{0,\rm sp}$.

We compare β obtained for the monodisperse Pf1 against the $\eta_{0,sp}$ prediction based on the DE theory using the known Pf1 dimensions (specified in Table 1) and K = 2300, as previously reported for Pf1, in eq 2 (Figure 6a).³¹ Overall, the theoretical prediction captures the experimental trend, suggesting $\beta \propto \eta_{0,sp}$. At relatively high values of c/c^* , $\beta \propto (c/c^*)^3$ indicating interparticle confinement and that the tube assumption from the DE theory holds. As the concentration decreases, a scaling transition toward $\beta \propto c/c^*$ is approached due to the increased rotational freedom of the Pf1. For CNC, OCNF-S, OCNF-L, and XG we refrain from a quantitative comparison of β as a function of c/c^* with Doi's theory. The main challenge to quantitatively capture the scaling behavior for these systems stems from their polydispersity and the contribution that each size population has on the collective dynamics. As such, for these systems, we discuss the trend of β as a function of c/c^* only qualitatively. Given the proportionality $\beta \propto \eta_{0,sp}$, we interpret the β scaling with RC and RP concentrations in terms of confinement, analogously to $\eta_{0,sp}$ as a function of c/c^* . Specifically, a scaling of 1 (i.e., $\beta \propto c/c^*$) indicates an unconstrained rotational motion of the RC or RP, while a scaling of 3 (i.e., $\beta \propto (c/c^*)^3$) implies a constrained RC or RP rotational motion, where the DE tube assumption holds.

The scaling parameter β as a function of c/c^* for the other systems investigated are shown in Figure 6b–e. For CNC (Figure 6b), the data can be well described by the scaling of 1 ($\beta \propto c/c^*$), suggesting that within the concentration range investigated the CNC are not significantly interacting. Indeed, for the same CNC source, signature of interparticle interactions were only detected above our investigated concentration rage (i.e., $c \geq 5$ mg/mL).^{61,62} For OCNF-S and OCNF-L, the data follow a scaling of 3 ($\beta \propto (c/c^*)^3$), suggesting a pronounced interparticle confinement as expected from the DE theory in the semidilute regime (Figure 6c,d).

It is important to note that although the different polydispersity $(2 \ge PDI \ge 1)$ and flexibility $(5.3 \ge N_p \ge$ 0.1) of the investigated RC systems, we recover the expected power law dependence with concentration according to Doi's theory (i.e., 1 and 3). This suggests that for concentrations below the onset of the nematic phase features of polydispersity and a small extent of flexibility, $N_p \sim 1$, can be still captured, at least qualitatively, within the "tube" framework. Differently from the exponent based on the DE theory in either the dilute and semidilute regime, the XG solutions follow the scaling of $3.5 \ (\beta \propto (c/c^*)^{3.5})$. This is likely because most of the XG solutions investigated are in the concentrated regime with nematic ordering at rest (Supporting Information, Section S2).

CONCLUSIONS

We simultaneously measure the shear viscosity and flowinduced alignment of a library of biosourced rod-like colloids (RC) and rod-like polymers (RP) under rheometric shear flow. For each system, the specific viscosity η_{sp} follows a universal trend with the extent of the RC and RP alignment (as captured by \sqrt{I}) that is concentration independent. We exploit this universality to retrieve β_i , a dimensionless parameter directly proportional to specific zero-shear viscosity, $\eta_{0,sp}$. For the RC fluids, we find good agreement of the $\eta_{0,sp}$ scaling as a function of concentration according to the Doi-Edwards theoretical prediction for rigid rods in the dilute and semidilute regime, regardless of the different polydispersity and flexibility of the investigated RC. Additionally, we find that, to some extent, the decreasing η_{sp} as a function of \sqrt{I} can be captured by an exponential function for all the RC/RP fluids investigated. Although previous experiments have suggested such unique exponential decay of the shear viscosity as a function of RC alignment, we confirm that such a relationship is a general characteristic of RC and RP, independent of their polydispersity, aspect ratio, flexibility, and contour length. These results underlay the unique interlink between the flow-dependent rheological and structural properties of these liquids, providing solid guidelines for engineering processes involved with the controlled anisotropy of RC and RP fluids.

ASSOCIATED CONTENT

③ Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.biomac.3c00347.

Section S1 contains details on the measurement technique. Section S2 shows evidence of the presence of nematic ordering in XG solutions for the concentration range investigated. Section S3 shows the data presented in Figure 5 in a semilogarithmic representation (PDF)

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Notes

The authors declare no competing financial interest.

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