



Zhen, T., Zhao, D., Lin, Z. , Flynn, D., Zhao, W. and Tian, D. (2024)  
Balanced Reward-inspired Reinforcement Learning for Autonomous  
Vehicle Racing. In: 6th Annual Learning for Dynamics & Control  
Conference (L4DC 2024), Oxford, 15-17 July 2024, pp. 628-640.

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# Balanced Reward-inspired Reinforcement Learning for Autonomous Vehicle Racing

**Zhen Tian**

2620920Z@STUDENT.GLA.AC.UK

*James Watt School of Engineering, University of Glasgow, Glasgow, G12 8QQ, U.K.*

**Dezong Zhao**

DEZONG.ZHAO@GLASGOW.AC.UK

*James Watt School of Engineering, University of Glasgow, Glasgow, G12 8QQ, U.K.*

**Zhihao Lin**

2800400L@STUDENT.GLA.AC.UK

*James Watt School of Engineering, University of Glasgow, Glasgow, G12 8QQ, U.K.*

**David Flynn**

DAVID.FLYNN@GLASGOW.AC.UK

*James Watt School of Engineering, University of Glasgow, Glasgow, G12 8QQ, U.K.*

**Wenjng Zhao**

WENJING.ZHAO@POLYU.EDU.HK

*Department of Civil Environmental Engineering, Hong Kong Polytechnic University, Hong Kong, China*

**Daxin Tian**

DTIAN@BUAA.EDU.CN

*School of Transportation Science and Engineering, Beihang University, Beijing 100191, China*

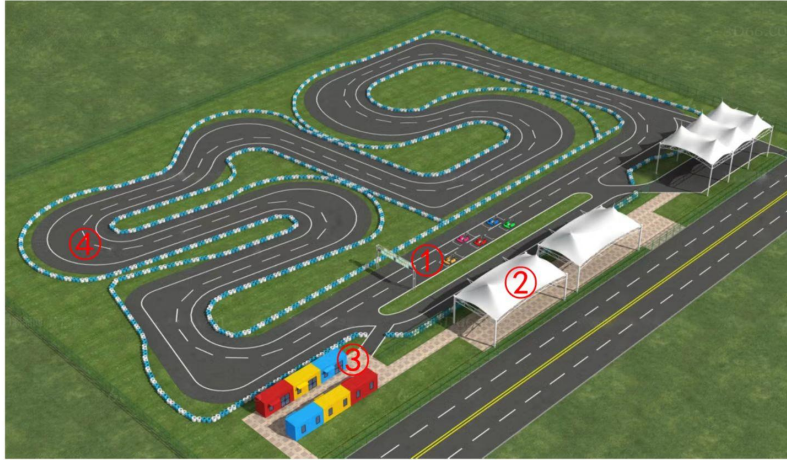
## Abstract

Autonomous vehicle racing has attracted extensive interest due to its great potential in autonomous driving at the extreme limits. Model-based and learning-based methods are being widely used in autonomous racing. However, model-based methods cannot cope with the dynamic environments when only local perception is available. As a comparison, learning-based methods can handle complex environments under local perception. Recently, deep reinforcement learning (DRL) has gained popularity in autonomous racing. DRL outperforms conventional learning-based methods by handling complex situations and leveraging local information. DRL algorithms, such as the proximal policy algorithm, can achieve a good balance between the execution time and safety in autonomous vehicle competition. However, the training outcomes of conventional DRL methods exhibit inconsistent correctness in decision-making. The instability in decision-making introduces safety concerns in autonomous vehicle racing, such as collisions into track boundaries. The proposed algorithm is capable to avoid collisions and improve the training quality. Simulation results on a physical engine demonstrate that the proposed algorithm outperforms other DRL algorithms in achieving safer control during sharp bends, fewer collisions into track boundaries, and higher training quality among multiple tracks.

**Keywords:** Autonomous vehicle racing, local planning, proximal policy optimization, balanced reward function.

## 1. Introduction

Autonomous vehicle racing has become an emerging field that combines the excitement of human vehicle racing and the state-of-the-art technologies in autonomous driving. Autonomous racing vehicles are expected to drive through complex tracks by exploring the limits of speed and decision-making. On the other hand, autonomous racing also escalates the entertaining value of the competition, by showcasing the amazing capabilities of autonomous vehicles. One of the main motivations for autonomous racing is to bridge the gap between the current level of autonomous driving and human driving at extreme limits.



① Start/End point ② Rest Area ③ Preparation Region ④ Racing Lane

Figure 1: Sketch of a closed-loop vehicle racing environment.

## 1.1. Motivation

Traditional vehicle racing is a challenging sport that requires reliable decision making, precise control, and robust perception. As illustrated in Figure 1, the racing track represents a complex and dynamic environment with varying properties such as track width, curvature, and surface conditions. In traditional vehicle racing, human drivers often encounter unexpected disturbances due to posture, viewing habits, and other factors [1]. Therefore, it is desirable to improve the driving safety by minimizing the affect of these disturbances during the racing. To this end, two main approaches are considered. The first approach involves optimizing the physical structures of the racing vehicle based on aerodynamics [2] [3]. The second approach involves designing robust control strategies from the online training. Recently, the growing interest of autonomous racing is demonstrated by several events such as Roborace [4] and Indy Autonomous Challenge [5]. In autonomous racing, the first stage is to obtain the driving environment information via perception. In autonomous racing competitions, the racing environment may equip with different perception levels. Therefore, to cope with diverse perception conditions, autonomous racing vehicles should not heavily depend on perception schemes.

Perception schemes for autonomous racing can be broadly classified into local perception and global perception. Global perception methods, such as [6], can assist the decision and planning of racing vehicles [6, 7, 8]. Nonetheless, excessively depending on global perception introduces certain drawbacks. For example, sensor failure or communication loss may prevent the vehicles from obtaining global information. Besides, competition organizers may limit the use of global perception to increase the difficulty and excitement of the races [9]. Therefore, it is required to develop methods that can enhance the racing vehicles to perceive local environments without global perception [10]. Model-based methods rely on predefined models or extra processes, such as Gaussian Process to quantify the uncertainty [11]. As a comparison, learning-based methods use data driven approaches to learn the optimal driving manner from data [12] [13]. Reinforcement learning (RL) is a powerful technique that learns optimal control commands from the training without global information [14, 15, 16]. Therefore, RL is capable to adapt to the local conditions of the environ-

ment [17]. Recently, Deep reinforcement learning (DRL) has been developed for high dimensional complex tasks. To enhance the autonomy level and reduce the reliance on perception, this paper would use DRL to achieve safe autonomous racing.

## 1.2. Related Works

State-of-the-art results of using DRL have been demonstrated in autonomous vehicles [18, 19, 20, 21]. Recently, a set of DRL algorithms with exceptional performance have attracted interest, such as Q-Learning [22], deep deterministic policy gradient (DDPG) [23], and proximal policy optimization (PPO) algorithms [24] [25].

In Q-Learning, the state-action value function is applied to determine the best action in a given state [26]. Correct actions are selected by Q-Learning in autonomous driving despite numerous safety constraints [27]. However, only simple tasks and scenarios were considered and tested in [27], without considering bends and more complex tasks. Moreover, another drawback of Q-Learning is the relatively low training efficiency [28].

DDPG uses deep neural networks to approximate the control policy [29]. With the suitability for handling high-dimensional data, multiple demonstrations of using DDPG have been given in autonomous driving [30]. For example, a DDPG model was proposed for safety driving within an end-to-end architecture [30]. Improved DDPG models have been proposed to improve training efficiency and results [31] [32]. However, the key issue is that DDPG gives an absolute result from the control policy. The absolute result hinders the exploration of more possible actions and restricts the adaptability in diverse driving scenarios.

PPO approximates the control policy in a probability distribution and offers fast strategy exploration improvements over DDPG [33]. PPO has been used to create control models for multi-agent driving scenarios [34]. PPO has been developed to generate smart driving strategies that balance safety and efficiency for crowded highway traffic [35]. In PPO, the traditional reward function uses a fixed ratio of averaged reward and current reward. The traditional reward function does not account for the influence of historical data on the current states in some cases. This leads to local high profits but global low profits. Hence, a reward function with a global perspective is needed.

## 1.3. Problem Statement and Contributions

DRL methods have greater potential than model-based methods in autonomous racing since they can better imitate the process of human decision making. However, The training results are unstable because the training guidance unbalances the local and global profits. To this end, a balanced reward-inspired PPO (BRPPO) is proposed in this paper. To optimize the future steps, a balanced reward function is proposed to consider both the historical and the prospective actions. The proposed reinforcement learning using PPO with the balanced reward function is illustrated in Figure 2. The whole algorithm is composed of offline training and real-time control. The decision network produces control commands in offline training, while the experience network generates real-time control commands. In offline training, the decision network learns to generate control commands based on the balanced rewards. The primary contributions are

- A balanced reward function is applied to deal with safety issues, such as collision during sharp bends. The number of collisions of sharp bends are significantly reduced.

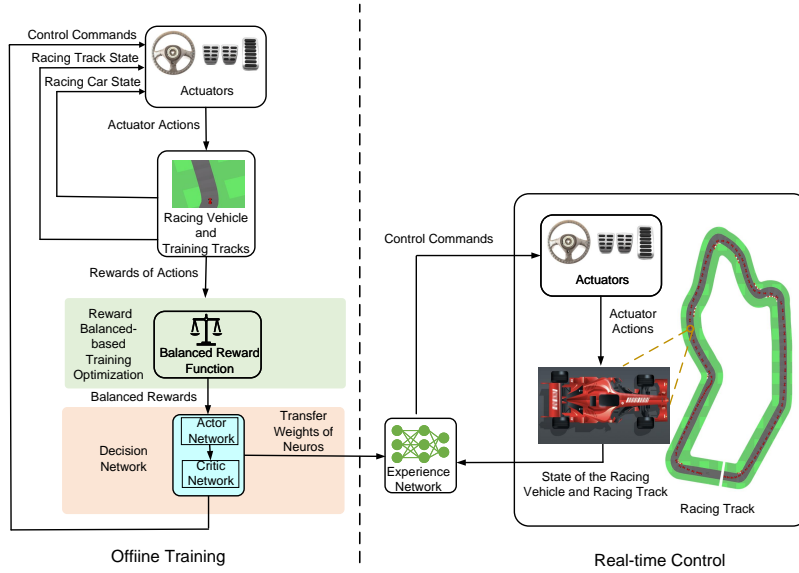


Figure 2: Diagram of the autonomous racing algorithm using the proposed BRPPO.

- The proposed BRPPO increases the training quality by balancing the historical and current rewards, enabling the autonomous racing vehicle to choose appropriate actions from the global perspective.

The rest of the paper is organized as follows: Section II introduces the decision network including the network structure and the control policy update process. Section III presents the details of balanced reward function. Section IV demonstrates the simulation results. Section V draws the conclusions.

## 2. Decision Network

The decision network is to generate safe and efficient control commands during training. The decision network consists of a set of actor-critic network that receives the balanced rewards of actions. The control policy in the actor-critic network compares the candidate control commands and choose the best one based on their relative advantages.

### 2.1. Network Structure

The decision network is composed of two actor-critic networks, which select actions based on the states of the racing vehicle. The actor-critic network is a neural network that integrates the control policy and the evaluation of control commands. The control policy selects control commands for less collisions. The evaluation of control commands is to estimate the relative advantage of the control commands. The relative advantage is served as a reference for updating the actor-critic network. The actor-critic network can be divided into the actor network (AN) and the critic network (CN). The AN and CN have similar structures, while the AN is to generate candidate control commands and the CN is to access the relative advantages for each candidate control command. The AN consists of an input layer, a series of convolutional layers, a linear layer and an output layer. The input

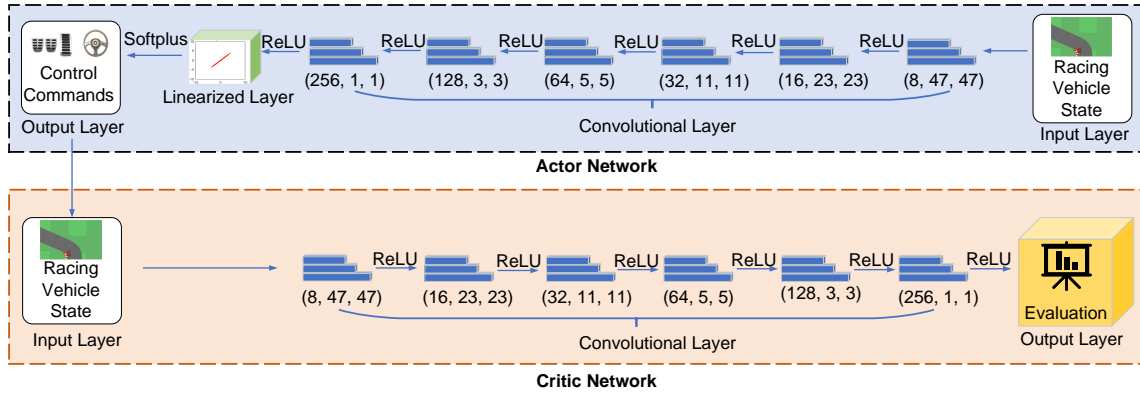


Figure 3: Structure of the actor-critic network.

layer receives the current state of the racing vehicle. The convolutional layers extract features from the driving states at each step. The linear layer adds linearity to the actor-critic network during the training. The output layer generates the control commands. The rectified linear unit (ReLU) layer applies the ReLU function to the output of the preceding layer. The ReLU function implements the operation  $\max(x, 0)$  on each input tensor element, where  $x$  represents the input element. The objective of ReLU layer is to introduce non-linearity into the actor-critic network during training. The expression format of convolution layer  $CL$  is expressed as

$$CL = (A, B, C) \quad (1)$$

where  $A$ ,  $B$  and  $C$  indicate the number of input channels, the number of output channels and the kernel size, respectively. The CN is composed of an input layer, a series of convolutional layers and an output layer. The input layer takes the output from AN and the current state of the vehicle as inputs. The convolutional layers extract features from the driving states and the corresponding control commands at each step. The output layer selects the best control commands based on their evaluation under the current state. The best control commands are then sent to the actuators. To generate a convincing evaluation, the relative advantage aims to reflect long-term advantages and spans a time period  $T$ . Hence, the CN compares the performance of a set of selected control commands with the average performance from the starting point  $t$  to  $t+T$ . The actor-critic network structure is illustrated in Figure 3.

## 2.2. Control Policy Update of the Decision Network

The control policy is determined by the weights of the neurons in the decision network. Therefore, the weights of the neurons should be adjusted to optimize the control policy. Figure 4 shows an example of a learning process involving a single racing sequence. The autonomous racing vehicle starts from the starting point with the maximum score. During the racing process, two types of losses including safety loss and efficiency loss are defined. When the autonomous racing vehicle reaches the finish point, a final score is calculated. Then, a score comparator compares the final score with a predefined expected score. If the final score is higher than the expected score, the

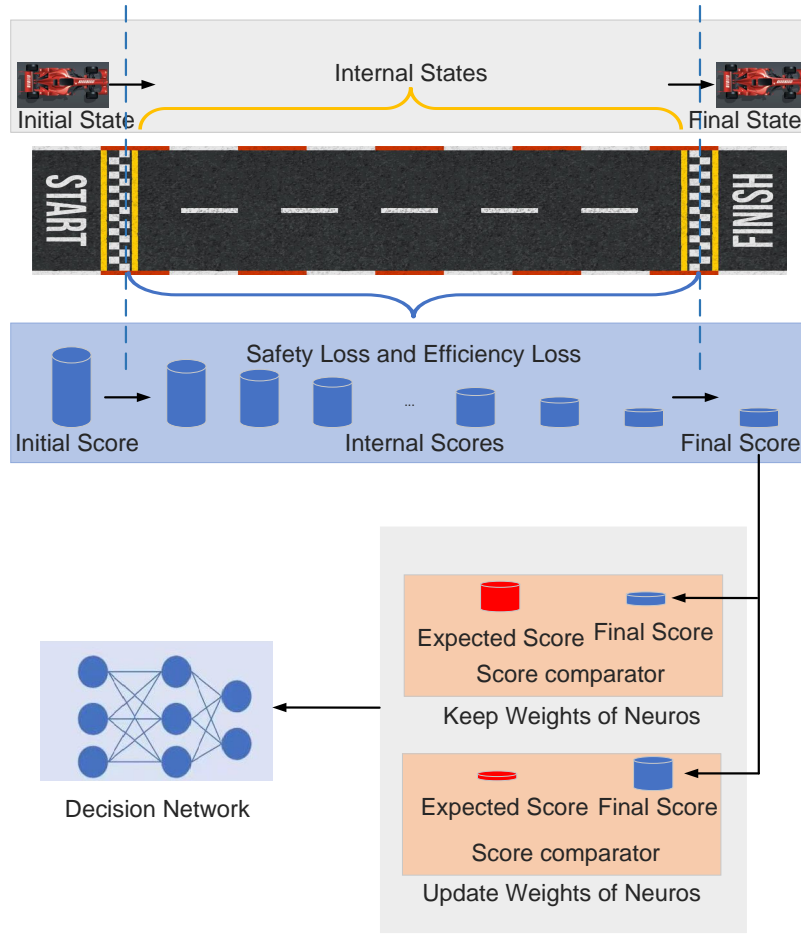


Figure 4: Control policy update of the decision network.

weights of the neurons in the decision network are updated. Otherwise, the weights of the neurons are not updated, as the performance does not meet the expected level.

### 3. Balanced Reward Function

The reward function is used to evaluate the actions selected by the decision network. During the racing, the laptime and collision frequency are the two main factors that affect the performance of the competitors. The laptime reflects the effectiveness of the actions, while the collision frequency reflects the safety of the actions. Therefore, a good reward function for racing should guide the decision network to select actions that can minimize collisions with the track boundaries. However, the traditional reward functions assigns equal weight to each step. The averaged reward is greatly influenced by previous high-reward actions. Therefore, the averaged reward is not able to balance the historical and current rewards. The averaged reward function is defined as

$$r_{\text{ave}} = 0.99r_{\text{ave}} + 0.01r_{\text{current}} \quad (2)$$

where  $r_{\text{ave}}$  and  $r_{\text{current}}$  are the averaged reward for historical states and the reward of the current state, respectively. Collisions during large and series bends at high speeds are the main safety concerns. The reward function should pay more attention to these critical single steps, which are called corner rewards. However, the averaged reward cannot focus on dangerous scenarios effectively, as the averaged reward gives equal weights to all historical steps. To address this issue, a hyper parameter is introduced to balance the average reward and the corner rewards. With the hyper parameter, a balanced reward function is proposed to consider both the historical and current rewards

$$r = (1 - \gamma)r_{\text{ave}} + \gamma r_{\text{current}} \quad (3)$$

where  $r$  represents the total reward under the current state of the racing vehicle,  $\gamma$  is a hyper parameter that directs the racing vehicle to prioritize random corners. With calibration, a value of  $\gamma$  that emphasizes most risky corners can be acquired. Therefore,  $\gamma$  promotes a safety-aware and forward-looking strategy, allowing the vehicle to predict possible dangers. Constraints on the learning speed are also required to be restrained within a fair range during each update. To improve the stability in learning, a clipped surrogate objective is used to control the learning speed. The clipped surrogate objective prevents significant adjustments of neurons that might result in control policy divergence. The clipped surrogate objective is employed to update the policy network. The clipped surrogate objective is defined as

$$L_{\text{clip}} = \min(R * A, \text{clip}(R, 1 - \epsilon, 1 + \epsilon) * A) \quad (4)$$

where  $R$  represents the proportion of the new policy probability to the old policy probability, and the  $\text{clip}()$  function ensures that each component of the gradient is bounded between  $1 - \epsilon$  and  $1 + \epsilon$ .  $A$  is obtained from the actor-critic networks, and  $\epsilon$  is a self-defined hyper-parameter constraining the amplitude of alterations for the learning parameters during each iterative update.

## 4. Simulation Results

The simulations are designed to evaluate the safety of the BRPPO in different driving scenarios. To generalize the training results, racing tracks are randomly selected from the candidate tracks. The training quality of the BRPPO and two other DRL algorithms have been evaluated by their training scores on five racing tracks. The racing performance at critical bends, the number of collisions into track boundaries on five racing tracks with the BRPPO are compared and analyzed.

### 4.1. Simulation Environment

The training and testing environment employed is Box2D, which is a widely adopted open-source physics engine. The Box2D is designed to simulate and animate two-dimensional rigid-body dynamics [36]. In Box2D, the racing vehicle is modeled as a rigid body, consisting of several connected shapes, such as the chassis and wheels. The racing vehicle is connected to a controller that generates control commands in terms of acceleration and steering based on a set of physical rules. Furthermore, the physical engine enables the simulation of suspension systems and enhances the fidelity of the simulation. In order to reduce the computing burden of BRPPO, a bicycle model [37] is used for the racing vehicle in Box2D

$$\dot{x} = V \cos(\varphi + \beta) \quad (5)$$



$$\dot{y} = V \sin(\varphi + \beta) \quad (6)$$

$$\dot{\varphi} = \frac{V}{l_r} \sin(\beta) \quad (7)$$

$$\dot{V} = a \quad (8)$$

$$\beta = \tan^{-1}\left(\frac{l_r}{l_f + l_r} \tan(\delta_f)\right) \quad (9)$$

where  $x$  and  $y$  represent the coordinates of vehicle's centre of mass,  $l_r$  is the length between the center of mass and vehicle's rear axle,  $l_f$  is the length between the center of mass and vehicle's front axle,  $\beta$  is the angle of the velocity with respect to the longitudinal axis of the vehicle,  $\psi$  represents the yaw angle.  $a$  and  $\delta_f$  are chosen as the inputs.  $a$  is the vehicle longitudinal acceleration

$$a = F_{\text{throttle,max}} u_{\text{throttle}} / M \quad (10)$$

where  $F_{\text{throttle,max}}$  and  $u_{\text{throttle}}$  are the maximum force of engine and the input level of throttle gate, respectively.  $M$  is the mass of the vehicle.  $\delta_f$  the is steering angle given by

$$\delta_f = \delta_{\text{max}} u_{\text{steering}} \quad (11)$$

where  $\delta_{\text{max}}$  is the maximum angle of steering and  $u_{\text{steering}}$  is the input of steering level. Therefore, the states of the vehicle can be changed by adjusting the inputs  $u_{\text{steering}}$  and  $u_{\text{throttle}}$ .

## 4.2. Evaluation of the Results

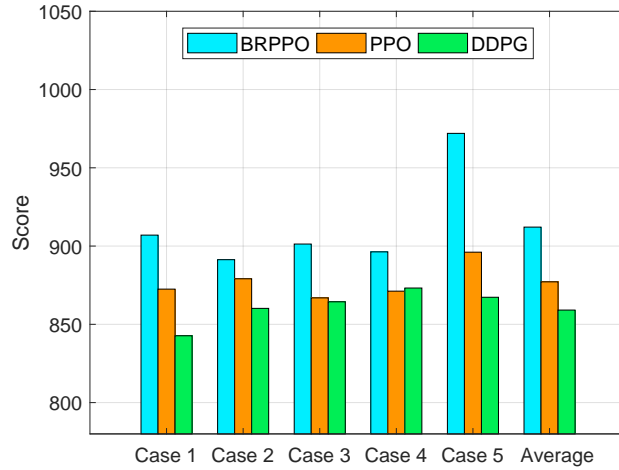


Figure 5: Scores for Cases 1 to 5 of using BRPPO, PPO and DDPG.

The BRPPO algorithm is compared against two popular benchmark algorithms, PPO and DDPG, to assess the racing safety and training quality. To ensure convincing simulation results, five different racing tracks are used in simulations. The five different racing tracks are correspond to Case 1 through Case 5, respectively.

As illustrated in Figure 5, both the PPO and DDPG were outperformed by the BRPPO in terms of scores and average score from Cases 1 to 5. The BRPPO algorithm achieves higher scores than the PPO and DDPG algorithms in each case. The main reason for the superior performance of the BRPPO algorithm is that the safety and efficiency losses are reduced during the racing. The safety loss is minimized by the balanced reward function, which enhances the training quality of the algorithm and prevents collisions. Figure 6 illustrates how BRPPO, PPO, and DDPG react to

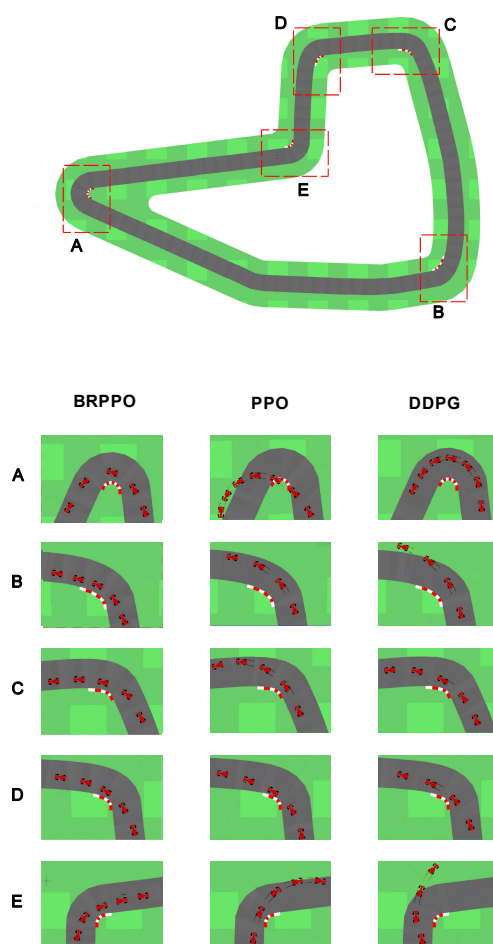


Figure 6: Driving performance of using BRPPO, PPO and DDPG in Case 5.

dangerous bends in a testing case. There are five bends from *A* to *E* in this case. Bend *A* has a high curvature, which makes it challenging to drive through. Bends *B* and *C* are the normal bends, which require moderate control. Bends *D* and *E* are close to each other, which increases the difficulty of steering. It can be seen that the BRPPO drives safer than the other two algorithms, as it travels within the boundaries and stays close to the inner side of curve when possible. At bend *A*, PPO deviates from the driving area, which causes a high safety loss. The DDPG follows the outer side of the track, which increases its efficiency loss. At bend *B*, the DDPG also leaves the driving area, which leads to a high safety loss. At bend *C* and *D*, the BRPPO stays in the center of the track, which balances the safety and efficiency objectives. The DDPG moves closer to the inner

Table 1: Number of Collisions of Using BRPPO, PPO, and DDPG

Index of Tracks	Number of Collisions		
	BRPPO	PPO	DDPG
Track 1	<b>0</b>	2	4
Track 2	<b>0</b>	3	2
Track 3	<b>0</b>	4	4
Track 4	<b>0</b>	4	2
Track 5	<b>0</b>	4	4

side of the track boundary, which improves its efficiency performance. Bends  $C$  and  $D$  suggest that the BRPPO is willing to sacrifice some efficiency profits to avoid collisions. At bend  $E$ , both PPO and DDPG exit the driving area, which results in a high safety loss. Table I compares the times of accidents that BRPPO, PPO, and DDPG touch the boundaries from Cases 1 to 5. The results in Table I show that the BRPPO makes fewer collisions. Therefore, the proposed BRPPO algorithm is superior in handling the complexities in racing and achieves better overall performance.

## 5. Conclusion

This paper proposed a balanced reward-inspired PPO algorithm for autonomous racing, aiming to improve the training scores and driving performance of the racing vehicle. To enhance the attention to critic steps, a balanced reward function is used to balance the historical and current rewards during the training. The algorithm is trained and tested on a physical rules-based platform that simulates the real driving environment. Comparisons among BRPPO and other two representative DRL algorithms were conducted, showing that the proposed algorithm outperforms in terms of higher average scores and fewer collisions. In the future, extensive research will be conducted in several aspects, including 1) verifying the racing ability of BRPPO under more uncertain conditions, 2) optimizing the racing process considering diverse objectives such as riding comfort, and 3) extending the algorithm to team competitions of autonomous racing vehicles.

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