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ANALYSIS OF COUPLING EFFECTS IN SEATED BODY BIODYNAMIC RESPONSES TO MULTI-AXIS VIBRATION

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Introduction

The biodynamic responses of seated body exposed to whole-body vibration (WBV) have been mostly studied under single-axis vibration, except for a few very recent studies. The responses to single-axis fore-aft and vertical vibration have shown considerable sagittal plane motions and magnitudes of cross-axis responses. The reported biodynamic responses to multi-axis vibration, however, suggest negligible coupled effects of multi-axis vibration^{1,2}, although coupled motions of the body are clearly perceived by subjects and observed by experimenters³. This raises concerns over suitability of the data analysis method used in deriving multi-axis vibration biodynamic responses. This study examines the current data analysis method, primarily based on H₁ estimator, and an alternate H₃ estimator for analyses of responses to uncorrelated multiaxis vibration. The relative effectiveness of the H₃ estimator in emphasizing the coupling effects of multi-axis vibration is demonstrated through analyses of apparent mass (APMS) and seat-to-head-transmissibility (STHT) data to dual-axis (xz) vibration.

Methods

Majority of the studies have reported biodynamic responses derived using the H₁ method based on cross-spectral density (CSD) of the measured signals, such that: $H_{kl} = \frac{s_{a_k b_l}}{s_{a_k}}; k=x, y, z \text{ and } l=x, y, z$

$$H_{kl} = \frac{s_{a_k b_l}}{s_{a_k}}; k=x, y, z \text{ and } l=x, y, z$$
 (1)

Where $H_{kl}(j\omega)$ defines the complex direct (k=l) or cross-axis $(k\neq l)$ APMS or STHT function, $S_{a_kb_l}$ is CSD of the response (force measured at the driving-point or the head acceleration along direction l, l=x,y,z) and the input acceleration a_k (k=x,y,z) with autospectral density of S_{α_k} . A few studies have also employed power-spectral density (PSD) or root-mean-square (RMS) methods, which yield identical magnitude results under single axis vibration. Using the linear system theory, the total response along each axis under multi-axis vibration can be considered as the sum of both the direct- and cross-axis responses to individual axis, such that: $\overline{H}_k = \frac{s_{a_k} \overline{s}_k}{s_{a_k}} = \sum_l \frac{s_{a_k} \overline{s}_{kl}}{s_{a_k}}$

$$\overline{H}_{k} = \frac{S_{a_{k}}\overline{b}_{k}}{S_{a_{k}}} = \sum_{l} \frac{S_{a_{k}}b_{kl}}{S_{a_{k}}} \tag{2}$$

Where \overline{H}_k is total biodynamic response along axis k, $S_{\alpha_k \overline{b}_k}$ defines CSD of total response to input along k, $S_{\alpha_k b_{kl}}$ is CSD of either direct (k=l) or cross $(k\neq l)$ component of response along k to single axis excitation along l and b_{kl} is response along k due to excitation along l. In multi-axis experiments, the vibrations applied along individual axis are uncorrelated $(S_{\alpha_k \alpha_l} = 0)$, which would lead to $S_{\alpha_k b_{kl}} = 0$ $(k \neq l)$. Consequently, the biodynamic responses derived using H₁ method would not account for the contributions of the crossaxis components observed under single axis vibration. The PSD method considers autospectral density of response alone and could thus appropriately account for cross-axis components, while it would not provide the phase data. Alternatively, the H₃ estimator combines the advantages of both the H₁ and PSD methods, by incorporating the cross-axis components and providing the phase information, and is given by:

$$H_k = \sqrt{\frac{s_{\alpha_k \overline{b}_k}}{s_{\alpha_k}} \frac{s_{\overline{b}_k}}{s_{\overline{b}_k \alpha_k}}} \tag{3}$$

The suitability of H₃ estimator is investigated through analyses of STHT and APMS data acquired with 9 seated subjects exposed to individual x and z-axis and combined xz axes.

Results

Fig. 1 compares the mean vertical APMS and STHT responses obtained under single-axis vibration using the H₁ method, and under dual-axis vibration using H₁ and H₃ estimators. The dual-axis responses derived using H₁ are quite comparable to the single-axis responses, particularly in APMS, as reported^{1,2}. The H₃ method, on the other hand, shows greater coupling effect of the dual-axis vibration by emphasizing contributions due to cross-axis responses observed under single-axis vibrations, which are evident at lower frequencies. The results obtained using H₃ method also support the response attained through superposition of direct and cross axis responses to single-axis vibration³. The H₃ method is thus considered better suited for the analysis of biodynamic response data to uncorrelated multi-axis vibration and the study of coupling effects.

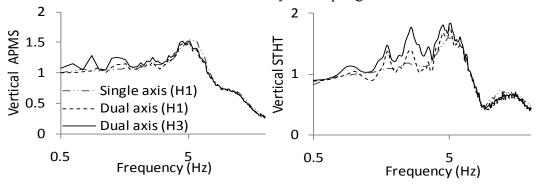


Fig. 1: Comparisons of single- and dual-axis vertical APMS and STHT responses.

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