

Citation for published version:
Dogan, H & Shokrani, A 2023, 'Investigation of chatter detection with sensor-integrated tool holders based on strain measurement', *Procedia CIRP*, vol. 117, pp. 157-162. https://doi.org/10.1016/j.procir.2023.03.028

DOI:

10.1016/j.procir.2023.03.028

Publication date: 2023

Document Version Publisher's PDF, also known as Version of record

Link to publication

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Procedia CIRP 00 (2023) 000-000

19th CIRP Conference on Modeling of Machining Operations

Investigation of chatter detection with sensor-integrated tool holders based on strain measurement

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Abstract

Machining chatter is one of the most critical issues that restrict the productivity in milling of thin wall workpieces. Sensor-integrated tool/tool holders, which provide data collection during cutting, can be employed for online chatter detection. Recently, there has been an increasing number of strain-measurement-based smart tool holders, which can measure bending moments and/or torque. Although accelerometer-integrated tool holders have been tested, sensor-integrated tool holders based on strain measurement have not been evaluated for the chatter detection in milling. This paper investigates the potential of chatter avoidance using a commercial sensor-integrated tool holder based on strain measurement.

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Peer review under the responsibility of the scientific committee of the 19th CIRP Conference on Modeling of Machining Operations.

Keywords: Monitoring; Chatter; Milling; Vibration

1. Introduction

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Chatter is one of the most important issues that have to 27 be avoided for high productivity in machining operations. The 28 present of chatter can result in damage to the tool or surface in-29 tegrity of the part. It is possible to avoid chatter by applying of-30 fline or online techniques. Offline techniques are mostly based 31 on the stability prediction and setting parameter (e.g., spindle 32 speed, depth of cut, helix angle) according to the stability pre-33 diction [1]. However, stability prediction requires system iden-34 tification such as modal parameters obtained via impulse test 35 [2]. This requires equipment and expert knowledge in this sub-36 ject. Moreover, the material removal and/or moving parts of the 37 machine can affect the dynamic behaviour of the system leading 38 to inaccuracy in chatter prediction.

Online chatter detection methods are mostly based on the on-40 set chatter detection in real time. Once the chatter is detected, 41 it can be avoided by applying chatter avoidance techniques [3–42 6]. Smith and Delio [4] adjusted spindle speed by matching the 43 dominant frequency to the tooth passing frequency. Bediaga et 44 al. [6] developed a spindle speed selection algorithm based on 45 the detection chatter and the lobe number where the cutting is 46 conducted. They experimentally proved the effectiveness of the 47 proposed algorithm by using a built-in microphone for chat-48 ter detection. Accelerometers and dynamometers as well as mi-49

crophones have been mostly used for chatter detection [7, 8]. Kuljanic et al. [9] investigated different sensors for chatter detection performance in milling operations. They indicated that a multisensor system consisting of an axial force sensor and accelerometer provided the best performance. The axial cutting force in their experiments was measured with a rotating dynamometer. Both rotating [10] and plate-type dynamometers [11] have been effectively employed for chatter detection.

Monitoring cutting forces for not only chatter but also other factors in machining operations such as tool wear condition and surface integrity has become very important to maximise productivity and work quality. Cutting forces can be used not only for process monitoring but also for decision-making regarding the machining performance. Therefore, there is an increasing number of studies focusing on the sensor-integrated tool and tool holders for measuring cutting forces. Xie et al. [12] incorporated six capacitive sensors into a standard tool holder to measure triaxial cutting forces and torque for milling and drilling operations. In a different study [13], the authors integrated a MEMS accelerometer as well as capacitive sensors to include the acceleration for tool condition monitoring. Luo et al. [14] developed an indexable tool embedded thin film sensors under each insert. This enabled the cutting forces in three directions to be measured for tool condition monitoring. In order to reduce manufacturing costs, low-cost strain gauges have been extensively utilised for force/torque measurement in tool holders. Qin et al. [15] developed a tool holder using semiconductor¹⁰² strain gauges to measure axial cutting force and torque during milling operations. They suggested that the tool holder can po-¹⁰³ tential be used for chatter detection and tool wear monitoring.¹⁰⁴ Recently, Zhang et al. [16] utilised semiconductor strain gauges¹⁰⁵ to develop a sensory tool holder for cutting forces and torque¹⁰⁶ measurements. In addition to the use of strain gauges for cut-¹⁰⁷ ting forces and torque measurement, Rizal et al. [17] integrated¹⁰⁸ an accelerometer and a thermocouple into the tool holder and¹⁰⁹ tool for real time condition monitoring in milling operations.

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Although accelerometer-integrated tool holders have been 111 evaluated to improve chatter performances [18, 19], investi-112 gation for the use of sensor-integrated tool holders based on₁₁₃ strain measurement for chatter detection has received very lim-114 ited attention. Suprock et al. [20] proposed using the torque data₁₁₅ collected from a sensor-integrated tool holder instrumented by 116 strain gauges for chatter frequency prediction. However, they117 only considered the torque data in their work. To the authors' 118 knowledge, the evaluation of cutting forces measured by the 119 strain gauges integrated into a tool holder for chatter detection₁₂₀ has not been investigated. In this paper, a commercial sensory₁₂₁ tool holder, SPIKE [21], which uses strain gauges to monitor₁₂₂ bending moments, axial force, and torsion, will be evaluated for₁₂₃ chatter detection. The bending moments measured by SPIKE₁₂₄ provide the radial cutting forces scaled by a constant. Thus, the 125 bending moments will be directly used for the representation of 126 the radial cutting forces. The obtained signals from the sensory 127 tool holders will be evaluated in the frequency domain for the 128 chatter detection.

The rest of the paper is organised as follows. Section 2 intro-130 duces the theoretical model for prediction of stability in milling 131 operations. The experimental setup and the procedure are ex-132 plained in Section 3. Section 4 presents the results and discus-133 sion. Finally, a conclusion is drawn in Section 5.

2. Theory for milling stability prediction

Milling stability can be predicted applying different methods such as the zero-order approach [22], the temporal finite element analysis [23], semi-discretization method [24], and multifrequency approach [25]. Among them, the zero-order approach is applied in this paper since it provides an accurate prediction for cuts with high immersion as in this study. The depth of cut for the stability limit is defined as [22]:

$$a_{lim} = -\frac{2\pi}{N_t K_t} \Lambda_{Re} \left(1 + \left(\frac{\sin(\omega_c \tau)}{1 - \cos(\omega_c \tau)} \right)^2 \right)$$
 (1)

where N_t , K_t , and τ are the number of flutes, the tangential milling force coefficient, and the tooth period, respectively. $\Lambda_{Re^{139}}$ and ω_c are the real part of the eigenvalues and the chatter fre-140 quency which are the functions of the frequency response func-141 tion of the milling system. The details for τ , Λ , and ω_c are given 142 in ref [22]. Experimental results will be collected in Section 3143 and stability prediction obtained by using Eq. 1 will be pre-144 sented in Section 4 together with the experimental results.

3. Experimental setup and procedure

The milling setup consisting of an end mill cutter and Aluminium workpiece, as shown in Fig. 1, was used for the evaluation of the chatter detection performance. A 3 flutes solid carbide end mill with 12 mm diameter and overhang of 120 mm was employed so that the cutting tool was the most flexible part in the milling system. A SPIKE sensory tool holder capable of measuring tool bending moments at 2.5 kHz sampling rate was used. This represents common scenarios in machining of aerospace components using long and slender cutting tools. An Al6061-T6 aluminium alloy workpiece with the dimension of $100 \times 50 \times 30 \text{ mm}^3$ was rigidly clamped to the worktable. Two accelerometers attached on the workpiece (Dytran 3263A2) and the spindle housing (Monitron MTN/1020), and a microphone were also utilised for the comparison of the chatter detection performance. The data from the accelerometers and the microphone were collected by NI 9775 data acquisition system with 20 kHz sampling rate, whereas the sampling rate for the sensory tool holder was 2.5 kHz. The chatter frequency due to the cutting tool system is generally higher than can be detected with this sampling unless a large tool overhang is used. However, chatter frequencies in this range is common for flexible workpiece milling. The setup with a long overhang reflects the same dynamics as one for a flexible workpiece, which is sometimes the case in the common machining scenario.

All experiments were performed on a XYZ machining center with a 13 kW spindle. An impulse hammer test was performed to the tool tip installed on the spindle. The first natural frequencies and the damping ratios in *x* and *y* directions were identified as 608 Hz and 613 Hz, and 0.011 and 0.016, respectively. Stability lobe diagram was created for Al6061-T6 aluminium alloy and the milling parameters in Table 1 by using Eq. 1 for the milling system as shown in Fig. 1. Following this, milling experiments were carried in dry cutting and a cut length of 100 mm by removing the material from the long side of the workpiece in each cut.

Table 1. Tool geometries and cutting parameters.

| Milling parameters | | |
|---------------------|-----------------------|--|
| Tool diameter | 12 mm | |
| Tool overhang | 120 mm | |
| Tool helix angle | 30° | |
| Feed per tooth | 0.05 mm | |
| Flute number | 3 | |
| Milling type | Down milling | |
| Radial depth of cut | 6 mm (Half immersion) | |

The sensory tool holder provides the bending moments (BMs) in both x- and y-directions, which can be turned into cutting forces by considering the lever arm length (distance from the strain gauges on the tool holder and the tip of the tool) as well as the torsion and the axial force. Therefore, four different signals collected from the sensory tool holder. In addition the accelerometers and microphone signals were evaluated for chatter detection. Experiments were conducted for four differ-

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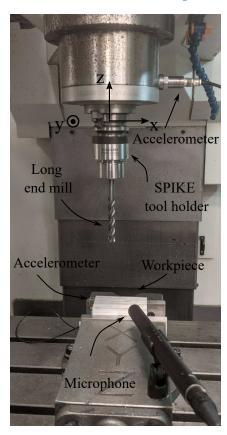


Fig. 1. Experimental setup consisting of a long end mill, an Aluminium work-169 piece, a sensory tool holder, two accelerometers, and a microphone.

ent spindle speeds and increasing axial depth of cut until chat-174 ter onset was detected from one of the sensors (the sensory tool175 holder, accelerometers, or microphone). Following this proce-176 dure, the sets of experiments in this study are presented in Ta-177 ble 2.

Table 2. Experimental sets

| Spindle speed (N) | Axial depth of cut (a_p) |
|-------------------|---------------------------------------|
| 2400 (rpm) | 0.05, 0.1, 0.2, 0.3, 0.4, 0.6, 1 (mm) |
| 3250 (rpm) | 0.05, 0.1, 0.2, 0.3, 0.4, 0.6 (mm) |
| 4400 (rpm) | 0.05, 0.1, 0.5 (mm) |
| 5500 (rpm) | 0.05, 0.1, 0.2, 0.3, 0.5 (mm) |

It is well known that in the case of chatter, the chatter frequency dominates the frequency spectrum. Chatter detection was realised by observing the frequency spectrum after each cut was completed. The frequency spectrum was obtained by applying the Fast Fourier Transform (FFT). Chatter was observed by checking the peaks in the frequency spectrum whether they are different from the spindle and tooth passing frequency, and/or their harmonics.

4. Results and Discussion

Experimental results with the predicted stability limits are given in Fig. 2. Each cut conducted was marked as stable, marginal, or chatter by analysing the data collected from the accelerometers and the microphone. For chatter cases, the data collected by sensory tool holder were evaluated for the use in chatter detection.

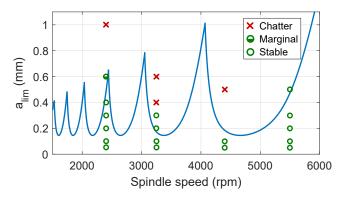


Fig. 2. Predicted stability lobe diagram (blue line) and experimental cuts

The lowest axial depth of cut (a_p) for four spindle speeds in Table 2 resulted in a stable cutting condition. The axial depth of cuts were increased until chatter occurred. In order to eliminate the noise streaming from the sensory tool holder, air cutting was conducted for each spindle speed. Fig. 3 shows the frequency spectrum of the air cutting at 2400 rpm. The spindle frequency and its harmonics in the figure are indicated with a dash line. It was found that the sensory tool holder has noises at frequencies of 357.1 Hz and 714.2 Hz (as demonstrated with diamond in the figure) for all four channels. Other air cutting tests showed that these noises were independent of the spindle speed. They were constant for each spindle speed tested. Rotation of the tool holder can be seen from the peak close to the first spindle frequency.

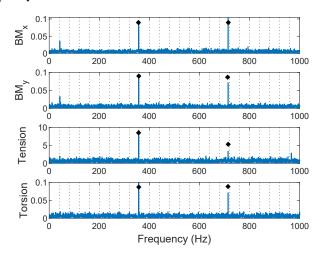


Fig. 3. Frequency spectrum for the bending moments (x and y), tension, and torsion for air cut at 2400 rpm, where the diamond marks indicate the noise frequencies.

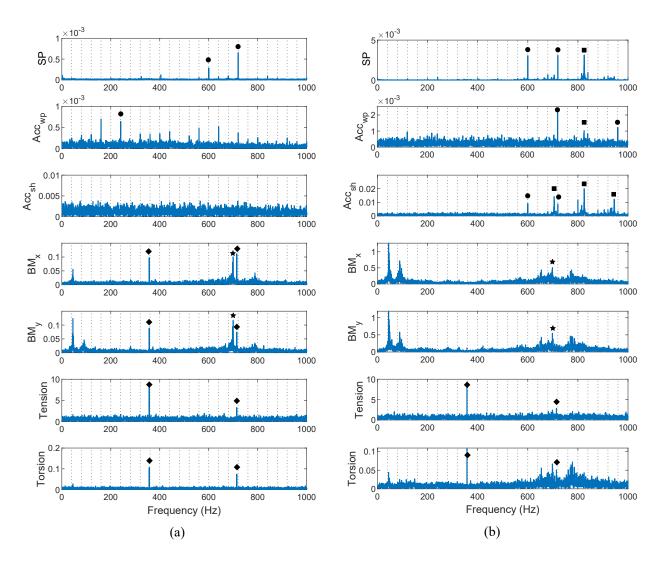


Fig. 4. Frequency spectrum for the sound pressure (Mic), acceleration signals from the workpiece (Acc_{wp}) and the spindle housing (Acc_{sh}), the bending moments, tension, and torsion for (a) a stable cut (N=2400 rpm and $a_p=0.05$ mm) and chatter (N=2400 rpm and $n_p=1$ mm). The dash lines indicate the spindle frequency and its harmonics. The circle, square, diamond, and star signs shows the tooth passing frequency or its harmonics, chatter frequencies, noises existing in the air cutting, and noises occurring in the cut, respectively.

Starting from 0.05 mm, the axial depth of cut was increased to 1 mm. The frequency spectrums for the sound pressure 196 (SP), the accelerations by the accelerometers on the workpiece 197 (Acc_{wp}) and on spindle housing (Acc_{sh}), the bending moments 198 (BM_x and BM_y), tension, and torsion are presented in Fig. 4(a) 199 and (b) for both stable cut (N = 2400 rpm, $a_p = 0.05$ mm) and 200 chatter (N = 2400 rpm, $a_p = 1$ mm), respectively. In stable cut, 201 the sound pressure is dominated by the tooth passing frequen-202 cies (as indicated by a circle in the figure) while the accelera-203 tion signal obtained from the accelerometer on the workpiece 204 shows frequency contents related to the spindle frequency, the 205 tooth passing frequency and their harmonics. The accelerom-206 eter on the spindle housing presents no peak in the frequency 207 domain as the axial depth of cut was very small to generate 208 enough acceleration on the rigid spindle housing. For the sig-209

nals monitored via the small tool holder, another peak differently from ones seen in the air cut (as marked with a star sign in the figure) is observed at 699.5 Hz. Although the frequency is not exactly the same, similar peaks with smaller amplitudes in a frequency range between 700 Hz and 760 Hz were detected for stable cuts at spindle speeds of 3250 rpm, 4400 rpm, and 5500 rpm. It is also worth noting that the first harmonics in the bending moments' frequency spectrum do not exactly match with the spindle frequency. The reason for this could be that the output signals from the sensory tool holder are filtered and post processed as it is a commercial product. Another reason could be the missing data points due to the wireless transmission during the cut. One of these could lead to the frequencies shifted. The peak seen at 699.5 Hz could be the harmonic of that shifted spindle frequency or tooth passing frequency.

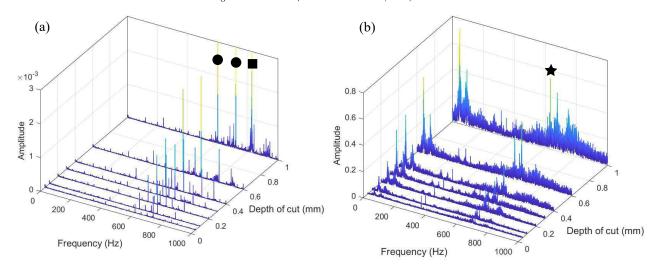


Fig. 5. Frequency spectrum given for all depth of cuts tested at 2400 rpm: (a) the sound pressure and (b) the bending moment in y- direction. The circle, square, and star signs demonstrate the tooth passing frequency or its harmonics, chatter frequencies, and noises occurring in the cut, respectively.

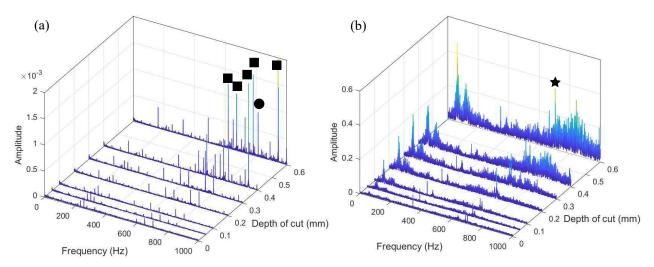


Fig. 6. Frequency spectrum given for all depth of cuts tested at 3250 rpm: (a) the sound pressure and (b) the bending moment in y- direction. The circle, square, and star signs demonstrate the tooth passing frequency or its harmonics, chatter frequencies, and noises occurring in the cut, respectively.

In the case of chatter, acceleration signals and sound pres-228 sure are dominated by the chatter frequencies (as indicated with229 a square mark) in the frequency domain as shown in Fig. 4(b).230 This can be clearly seen from accelerometer on the spindle231 housing and the microphone. However, none of the signals from232 the sensory tool holder dominates the frequency spectrum. For233 the bending moment signals, even though there is an increase in234 the amplitudes at higher harmonics, the most dominant peaks235 are still the ones close to the first and second harmonics of the236 spindle frequency. There is almost no change in the tension sig-237 nal (which indicates the axial force). Similar to the bending mo-238 ments, there is an increase in the amplitudes at higher frequen-239 cies around 800 Hz for the torsion. However, it does not show a240 clear chatter peak as in the sound pressure and the acceleration241 signals.

Frequency responses for all depth of cuts considered in this²⁴³ study for 2400 rpm and 3250 rpm are presented in Fig. 5 and²⁴⁴ Fig. 6. Fig. 5(a) and Fig. 6(a) indicate the frequency spectrum²⁴⁵

of the sound pressure signal and Fig. 5(b) and Fig. 6(b) presents the frequency spectrum of the bending moment signal in y- direction. Similar to results in Fig. 4, the onset chatter can be detected via discrete chatter frequencies dominating the response in the case of sound pressure signal. However, bending moment signal shows only an increase in the amplitude in higher frequencies and the most dominant frequency still occurs around the spindle frequency.

Having evaluated the results presented above, it seems that chatter detection using a sensor-integrated tool holder based on strain measurement is possible by monitoring the amplitudes at higher harmonics. However, chatter detection is not as straightforward as it is with a microphone or an accelerometer where distinct chatter frequencies are observed. Considering other parameters such as progressive tool wear, which leads to an increase in the amplitude at higher harmonics, the chatter detection process becomes more complicated. Furthermore, detection of chatter using the distinct chatter frequencies allows

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utilising easy-to-implement chatter avoidance techniques where 299 the spindle speed is set to the chatter frequency detected [3, 4]. 300 A sensor-integrated tool with the capability of detecting chat- 301 ter frequency as well as the tool bending moment would allow 302 chatter avoidance in real time taking into account the changing 304 cutting geometry and workpiece rigidity as well as detecting the 306 forces acting on the tool and detecting tool wear [26].

5. Conclusion

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The presence of chatter can have detrimental effects on tool₃₁₂³¹¹ life and part quality in machining operation. In this paper, the₃₁₃ use of strain gauge based sensory tool holder for chatter detec-314 [14] tion has been proposed and investigated. The analysis showed³¹⁵ that there was an increase in the amplitude at higher harmonics316 in the bending moment and torsion signals. However, no dis-318 crete chatter frequency could be detected from the bending mo-319 ment and torsion signals. This is despite the evidence of discrete₃₂₀ frequencies in acceleration and sound pressure signals indicat-321 ing chatter. Therefore, easy-to-apply real time chatter avoidance 322 methods where the spindle speed is set according to the chatter and frequency could not be specified. The frequency could not be applied. The most distinctive frequency 325 peak obtained from the sensory tool holder was around the spin-326 dle frequency. However, there is a deviation between the mea-327 [18] sured and the real frequencies. This can potentially be due to 328 the signal filtering, pre and post processing within the hardware 330 and software. This necessitate further investigations which will₃₃₁ be considered in the future work.

Acknowledgements

The authors would like to acknowledge the support of 337 the UK Engineering and Physical Sciences Research Council $_{339}$ through the grant number: EP/V055011/1.

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