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# Attenuation and focusing of ocean wave energy by a parabolic arc pontoon breakwater in a hybrid energy harvesting system

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## Abstract

In the multifunctional system consisting of point absorber wave energy converters and a pontoon breakwater, the breakwater plays an essential role in attenuating waves on the lee side and amplifying waves for a better energy harvesting on the stoss side. The structure of breakwater is expectedly improved to enhance its wave attenuation and amplification at the same time. Here we present a novel parabolic arc breakwater and show that for a range of typical regular incident waves, it can attenuate more wave elevation and focus high waves in several regions in comparison to a straight breakwater. In further frequency-domain investigations, a special relatively-low frequency associated with the parabolic arc breakwater configuration is found and named as the critical frequency, closed to which splendid attenuation and focusing performance can be achieved. A systematic parametric study on the geometric factors (draft, width, and chord length) of the parabolic arc breakwater is thereafter carried out to examine their influence on the attenuation and focusing performance at the critical frequency. We find that an increase of the draft can reduce the critical frequency greatly so as to let it be within the real sea states, meanwhile slightly affecting the attenuation performance. An increase of the chord length has an uncertain but not large influence on the attenuation performance, whereas it enhances substantially the focusing performance. Simultaneously, an amplification rate up to 3.06 in two relatively-large focal areas in a prescribed deployment zone and an average attenuation rate of approximately 68% in a prescribed protection zone could be obtained in a commonly observed coastal wave.

*Keywords:* parabolic arc breakwater; wave energy; hybrid system; wave attenuation; wave focusing

## 1. Introduction

Wave energy attracts broad interest in recent years. Many wave energy converters and related hybrid energy harvesting systems have been proposed (e.g., Ref. [1]-[4]). Recently, wave energy converters were combined with breakwaters to form a system that the two kinds of devices share mutual benefits of function compatibility and cost reduction [5]. Due to the diversity of breakwaters [6] and wave energy converters [7], many systems were proposed [8]-[20] based on various integration methods. Here we restrict the scope within a promising and relatively new scenario [19][20], in which flexibly arranged point absorber wave energy converters (PAWECs) [21] are deployed in front of an easily-constructed and low-cost pontoon

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1 breakwater. PAWECs, with their captured energy proportional to the square of wave height in ideal cases,  
2 take advantage of high local waves generated by the disturbance of pontoon breakwater and in return offer  
3 it protection from direct wave impact [19]. Better wave energy conversion and attenuation are desired for  
4 this hybrid system. For energy conversion, besides the optimization strategies for a single PAWEC or array  
5 [22]-[24], waves amplified by the breakwater are also a great auxiliary; on the other hand, attenuation of  
6 the system heavily relies on the breakwater [19]. In this sense, the breakwater is supposed to have a  
7 promotive amplification on the premise that its attenuation is guaranteed.

8 The idea of using artificial architecture to focus high waves for a better energy harvesting has long been  
9 investigated, although such approaches based on wave refraction [25]-[27] or Bragg resonance [28] were  
10 not first applied to breakwaters. One method was the so-called wave lens [30]. Flat plates or horizontal  
11 circular cylinders were assembled underwater in an overall biconvex [29], Fresnel [30], crescent [31], or  
12 other [32] planform. While passing through a wave lens, a monochromatic wave train is refracted by the  
13 sudden decrease in water depth and directed toward a pre-selected focal point. The mechanism is similar to  
14 that of its optical counterpart. An amplification factor (maximum focused surface elevation/incident wave  
15 amplitude) as high as 15 could be obtained for a particular wave frequency [32]. Despite its effectiveness,  
16 this method cannot be straightforwardly adapted for the pontoon breakwater and PAWECs hybrid system  
17 since the focal point is always on the lee side of the wave lens. However, inspired by the thought of directed  
18 refraction in the wave lens approach, a breakwater may instead use directed reflection to focus waves at  
19 certain locations on the stoss side. For this purpose, the breakwater's opening wall needs to be made to a  
20 particular shape that satisfies the focusing condition. One such breakwater was proposed in [33]. The  
21 planform contour of the opening wall is bent from a straight line to a parabola, analogous to the reflection  
22 of light by a two-dimensional concave mirror.

23 Many innovative methods have been proposed to improve the attenuation of a pontoon breakwater [34]-  
24 [43]. Perhaps the most straightforward way is slightly changing its geometry. As demonstrated in [44] and  
25 [45], width is a key factor. In two-dimensional (2D) cases, the transmission coefficient could be reduced  
26 through either extending the width of a single pontoon or placing multiple pontoons side by side. The latter  
27 may have a better performance for the same overall horizontal dimension [44], reflected by vast twin-  
28 pontoon designs [42]-[45]. Another way that can be regarded as increasing the horizontal dimension of a  
29 breakwater is by bending the structure to make its planform a circular arc [46] or V-shaped [47] pattern. By  
30 the Fermat principle of least time [48], this method also helps create a greater leeward shadow for the  
31 breakwater. The effectiveness of such an approach is demonstrated in a single arc [49] and double arc [50]  
32 configurations. Either the structure is concave toward the stoss side or the lee side, the attenuation effects  
33 are similarly effective [50]. While adapting the bending method, most of the cases are floating or bottom-  
34 mounted vertical plate breakwaters. Pontoon breakwaters are rarely seen.

35 The practical application of the pontoon breakwater and PAWECs multifunctional system is restricted  
36 by two inadequacies in the previous researches. The first is that an integrated evaluation of both attenuated

1 waves and amplified waves was necessary but rare. On the one hand, these two aspects were always studied  
2 in a separative manner, and concerns were mostly focused on the attenuated waves. On the other hand,  
3 studies on the integrated system are mainly concerned about interactions between the breakwater and the  
4 PAWECs in order to optimize the energy harvesting performance [19][20]. The second, partly due to the  
5 first, is that a simple way to simultaneously enhance both the attenuation and the amplification of waves  
6 was expected but absent. The exclusive improvement methods for attenuation were described in the  
7 literature in the previous paragraph. In [19] the authors reported that the presence of both a breakwater and  
8 a PAWEC was superior in attenuation to the presence of either. The latest only investigation on wave  
9 focusing using a pontoon breakwater was Ref. [33], in which attenuation was not considered. To remedy  
10 the inadequacies, we thereby propose a parabolic arc breakwater in the light of compatibility behind the  
11 method of changing the opening wall shape and the method of bending the whole structure. This concept  
12 can be generalized to other forms of breakwaters, but herein we demonstrate its effectiveness through the  
13 pontoon type. The novelty and motivation of this study are reflected as follows. The first is to establish a  
14 set of criteria, aiming at three-dimensional (3D) problems as those presented in the paper, to evaluate the  
15 overall performance of a breakwater considering simultaneously the wave attenuation and the wave  
16 focusing. The second is to demonstrate the superior performance of a parabolic arc breakwater through a  
17 comparative study. The third is to explore the influence of geometric factors (draft, width, and chord length)  
18 on the performance of a parabolic arc breakwater through a parametric study, hence providing a reference  
19 for practical applications.

20 The rest of the paper is structured as follows. In section 2 we validate the modeling and declare the  
21 performance criteria. In section 3 we carry out a comparative study between parabolic arc breakwaters and  
22 a straight breakwater. In section 4 we perform a parametric study on the parabolic arc breakwater  
23 dimensions. In section 5 we draw conclusions and remarks on future work.

## 24 **2. Methodology and validation**

### 25 *2.1 Parabolic arc breakwater*

26 The sketch of top view and side view of the proposed parabolic arc pontoon breakwater in the Cartesian  
27 coordinate system  $xyz$  is in Figure 1. The breakwater is freely floating. From the top view, the breakwater  
28 is a parabolic band with a uniform width  $w$ . It is symmetric about the  $x$ -axis and placed in a manner that the  
29 opening wall is tangent to the  $oyz$  plane at the  $z$ -axis. The curvature of the structure is determined by its  
30 focal distance  $f$ . The lateral dimension is characterized by chord length  $l$ . From the side view, the draft in  
31 calm water is denoted as  $d$ . The overall horizontal dimension is characterized by occupation width  $w_0$ . Water  
32 depth is denoted as  $h$ . The incident wave propagates in the positive  $x$ -direction with an angular frequency  
33  $\omega$ .

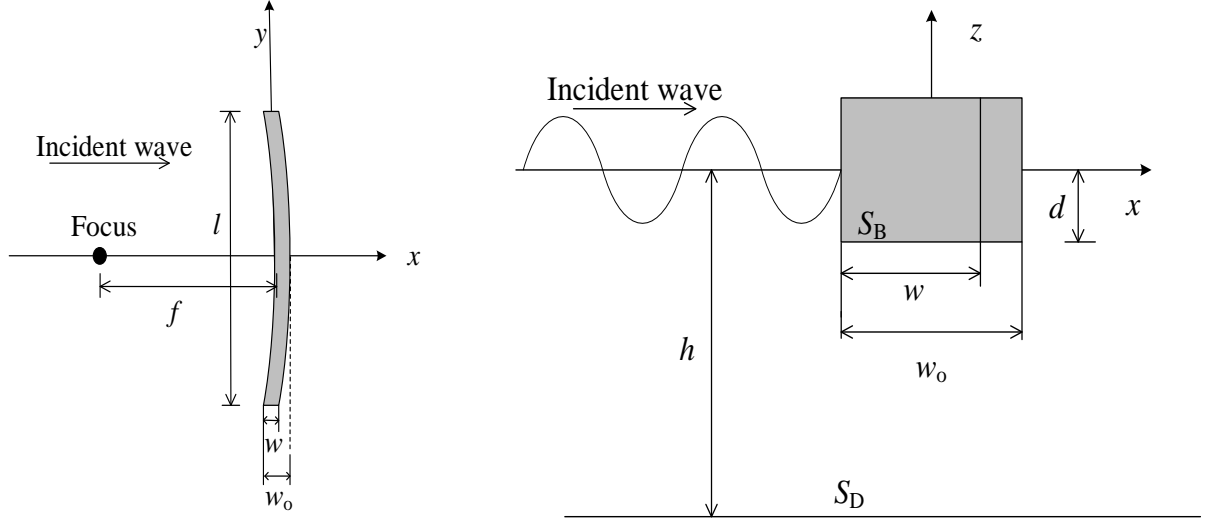


Figure 1 Sketch of the parabolic arc breakwater: top view and side view

## 2.2 Hydrodynamics and normalization of physical terms

Based on the potential wave theory, interactions between water waves and breakwaters are simulated by the HAMS program developed by Liu [51], incorporating an open-source package of free-surface Green function [52]. The fluid is assumed incompressible, inviscid, and irrotational, and the governing equation is the Laplace equation,

$$\nabla^2 \phi = 0 \quad (1)$$

where  $\phi = \phi_0 + \phi_s + \phi_r$  is the total velocity potential.  $\phi_0$  is the incident potential,  $\phi_s$  is the scattered potential, and  $\phi_r = i\omega \sum_{j=1}^6 \xi_j \phi_{rj}$  is the total radiation potential.  $\xi_j$  is the motion response and  $\phi_{rj}$  is the radiation potential in  $j$ th mode oscillating with unit amplitude, respectively. The velocity potential  $\phi$  satisfies the boundary conditions on the free surface  $S_F$ , the immersed body surface  $S_B$ , and the seabed  $S_D$  (as shown in Figure 1),

$$\left. \begin{aligned} \frac{\partial \phi}{\partial z} |_{S_F} &= \frac{\omega^2}{g} \phi \\ \frac{\partial \phi}{\partial n} |_{S_B} &= \mathbf{v}_n \\ \frac{\partial \phi}{\partial z} |_{S_D} &= 0 \end{aligned} \right\} \quad (2)$$

where  $\mathbf{v}_n$  is the normal component of the fluid velocity on the immersed body surface  $S_B$ . The problem can be solved in the frequency domain numerically by the Boundary Element Method using HAMS. For a planar wave, the incident potential is

$$\phi_0 = \frac{igA}{\omega} \frac{\cosh[k(z+h)]}{\cosh kh} e^{-ikx \cos \beta -iky \sin \beta} \quad (3)$$

where  $A$  is the incident wave amplitude,  $g$  is the acceleration of gravity,  $k$  is the wave number, and  $\beta$  is the

1 incident angle. According to Ref. **Error! Reference source not found.**, the complex surface elevation can  
 2 be expressed as

$$3 \quad \eta_c = \frac{\phi_o + \phi_s}{ig/\omega} + \frac{\omega^2}{g} \sum_{j=1}^6 \xi_j \phi_{rj} \quad (4)$$

4 The motion response vector  $\xi$  can be derived from the matrix form equation of motion in the frequency  
 5 domain

$$6 \quad [-\omega^2(\mathbf{m} + \mathbf{a}) + i\omega\mathbf{b} + \mathbf{k}_s]\xi = \mathbf{F}_e \quad (5)$$

7 where  $\mathbf{m}$  is the mass matrix,  $\mathbf{a}$  the add mass matrix,  $\mathbf{b}$  the radiation damping matrix, and  $\mathbf{k}_s$  the  
 8 hydrostatic stiffness matrix of the breakwater.  $\mathbf{F}_e$  is the wave excitation force.

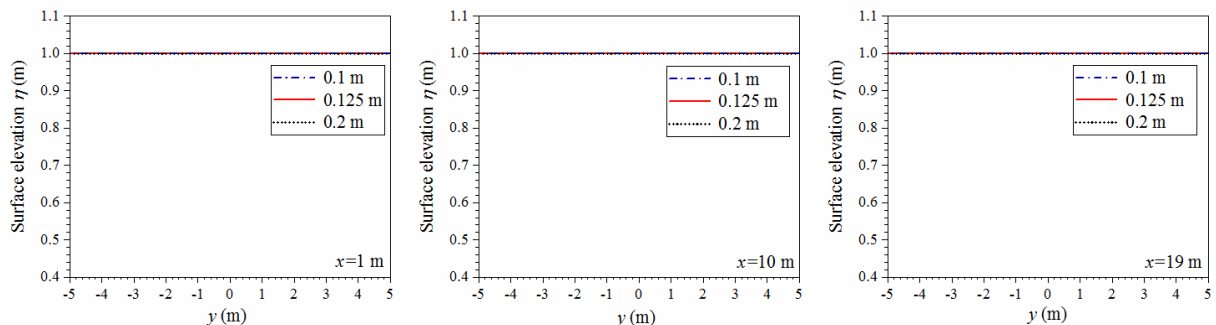
9 A list of major nomenclature is shown in Table 1.

10 **Table 1** Major nomenclature

Breakwater		Water		Wave	
Chord length	$l$	Surface elevation	$\eta$	Angular frequency	$\omega$
Width	$w$	Average elevation	$\eta_a$	Period	$T$
Occupation width	$w_o$	Depth	$h$	Critical frequency	$\omega_c$
Focal distance	$f$	Amplification factor	$a$		
Draft	$d$	Critical elevation	$\eta_c$		

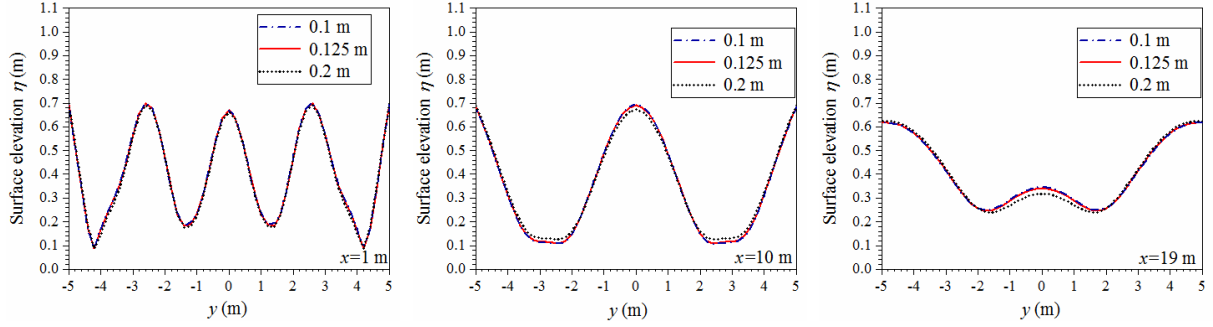
### 11 2.3 Convergence test

12 We perform a convergence test to validate the mesh to be used in the subsequent computations.  
 13 A straight pontoon breakwater with  $l=10$  m,  $w=1$  m,  $d=1$  m is selected as the test model. The water  
 14 depth is  $h=5$  m. Three incident waves covering a wide range with  $\omega=0.5, 3,$  and  $5$  rad/s are used.  
 15 Three sets of mesh with a grid size of  $0.1, 0.125,$  and  $0.2$  m are tested. Surface elevations on the  
 16 cutting lines on the lee side of the breakwater at  $x=1, 10,$  and  $19$  m are displayed in Figure 2. The  
 17 two sets of mesh of  $0.1$  m and  $0.125$  m match well. Hereafter the  $0.125$  m grid size is used in all  
 18 the cases.



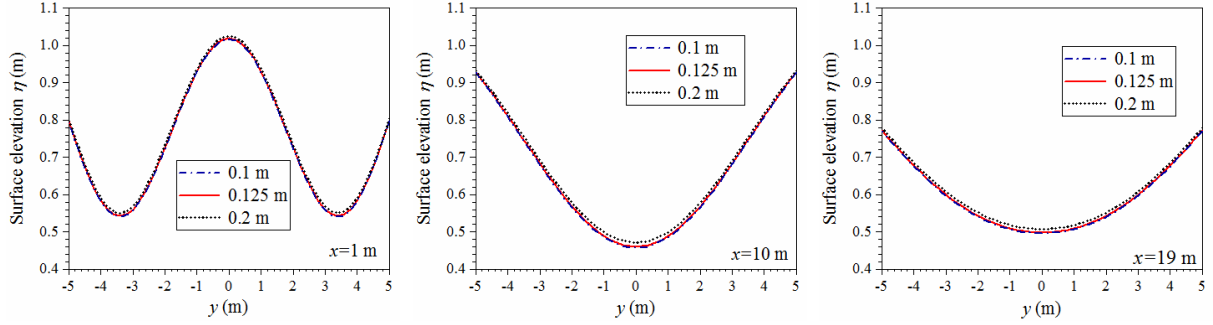
19

1

(a)  $\omega=0.5$  rad/s

2

3

(b)  $\omega=5$  rad/s

4

5

(c)  $\omega=3$  rad/s

**Figure 2** Convergence test of the mesh with grid size of 0.1, 0.125, and 0.2 m, in three representative waves  $\omega=0.1$ , 3, and 5 rad/s, at locations  $x=1$ , 10, and 19 m.

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## 2.4 Performance criteria

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The performance of a pontoon breakwater in this study is evaluated in two aspects: wave attenuation on the lee side and focusing on the stoss side. Since the main functionality of a breakwater is to reduce leeward wave elevation, attenuation is considered as the key criterion with the first priority. On the other hand, the breakwater is expected to focus high waves at some locations (possibly at the focus of the parabola) for PAWECs. High-quality focal areas are expected to have higher waves, a more regular shape (such as a square or a circle that has similar lateral and horizontal dimensions), and a larger area. Besides the criteria of attenuation and focusing, the parabolic arc breakwater should not be too curved to violate practical construction and application.

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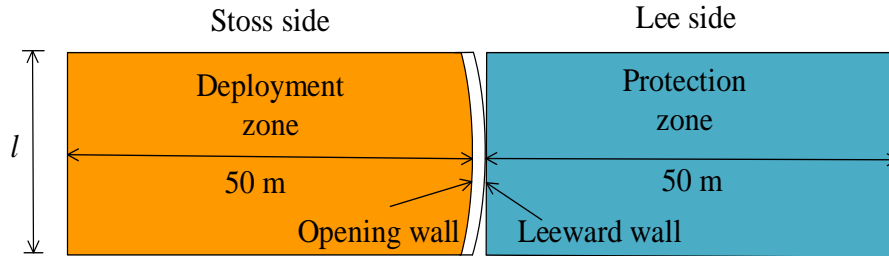
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In 2D problems, wave attenuation features of a breakwater can be characterized by the transmission coefficient  $T$  and reflection coefficient  $R$ . Whereas in 3D problems, such as the present study, the concepts of  $R$  and  $T$  are no longer applicable since the surface elevation distribution in the lateral direction should not be considered as uniform (as shown in Figure 2). In such a situation, we use the surface elevation on the stoss side and the lee side to respectively describe the attenuation and focusing features. In most cases of the paper, a  $50 \text{ m} \times l$  rectangular protection zone counted from the leeward wall center and a  $50 \text{ m} \times l$  deployment zone counted from the opening wall center are selected in which surface elevation is measured (Figure 3). To acquire a comprehensive knowledge of attenuation, two properties throughout the protection zone are necessary: the average elevation  $\eta_a$  characterizing general attenuation effectiveness, and the

1 surface elevation  $\eta$  illustrating complementary details. For focusing on the deployment zone, the preference  
 2 is seeking high-quality locations. In ordinary reflection by a plain obstacle, the superposition of incident  
 3 and reflection waves could create waves with a maximum amplitude two times the incident amplitude. To  
 4 demonstrate the superior focusing effect of parabolic arc breakwaters, areas with wave amplitude larger  
 5 than 2 m and proper shape and size are marked. Associated with each focal area, the amplification factor  $a$   
 6 is also given.



7  
8 **Figure 3** Protection zone and deployment zone

9 **3. Comparative study between parabolic arc and straight breakwaters**

10 According to the performance criteria, a comparative study is carried out to demonstrate the  
 11 effectiveness of parabolic arc breakwater in wave attenuation and focusing. Seven parabolic arc  
 12 breakwaters with  $f=10, 15, 20, 25, 30, 35, 40$  m are thereby selected in comparison to a straight breakwater.  
 13 It starts from  $f=10$  m since the curvature is considered better not to be large. In all the breakwaters, the  
 14 chord length is  $l=20$  m, the width is  $w=1$  m, and the draft is  $d=1$  m. The water depth is  $h=5$  m. Nine groups  
 15 of incident regular waves with an angular frequency  $\omega$  ranging from  $\omega=1$  to 5 rad/s with an increment of  
 16 0.5 rad/s are used to check the performance of breakwaters in a different wave environment.

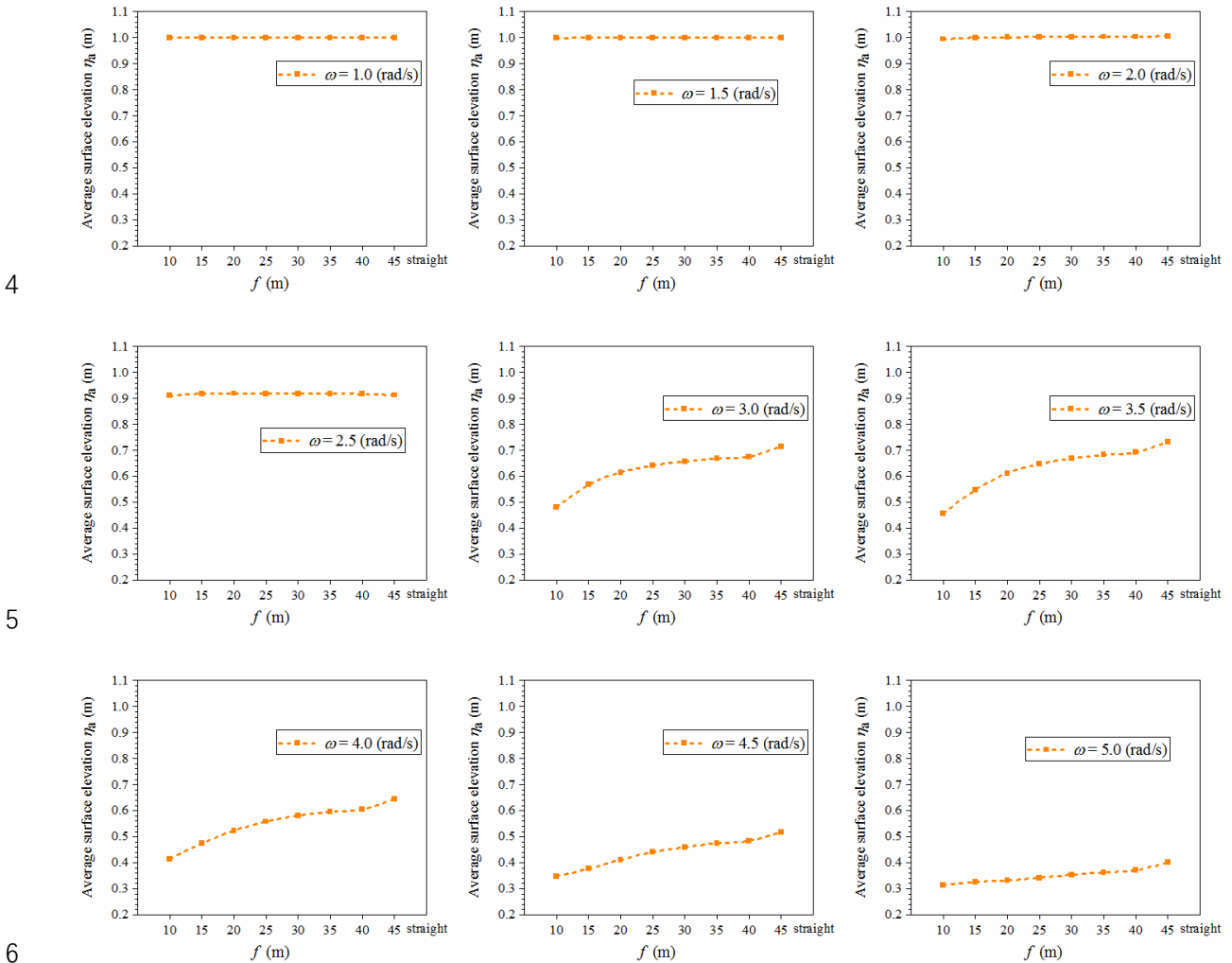
17 **3.1 Attenuation**

18 The comparative results of the average elevation  $\eta_a$  for each wave are displayed in Figure 4. For  $\omega=1,$   
 19 1.5, and 2 rad/s,  $\eta_a$  around all the eight breakwaters keeps close to 1 m. Either a parabolic or straight  
 20 breakwater is almost useless. For  $\omega=2.5$  rad/s, the breakwaters begin to work but are similarly ineffective  
 21 with a  $\eta_a$  about 0.9 m. The  $f=10$  m parabolic arc breakwater is a little better than the rest. For  $\omega=3, 3.5, 4,$   
 22 4.5, and 5 rad/s,  $\eta_a$  of all the breakwaters drops a lot. It is evident that  $\eta_a$  of the seven parabolic arc  
 23 breakwaters is lower than that of the straight breakwater. To sum up, in our selected cases, the parabolic arc  
 24 breakwaters are as good as or better than the straight breakwater, especially in the high-frequency waves.  
 25 Also, for  $\omega \geq 3$  rad/s, attenuation is stronger as the focal distance  $f$  increases (the straight breakwater may be  
 26 regarded as a parabolic arc breakwater with  $f=+\infty$ ). The  $f=10$  m parabolic arc breakwater has an overall best  
 27 attenuation at an average level.

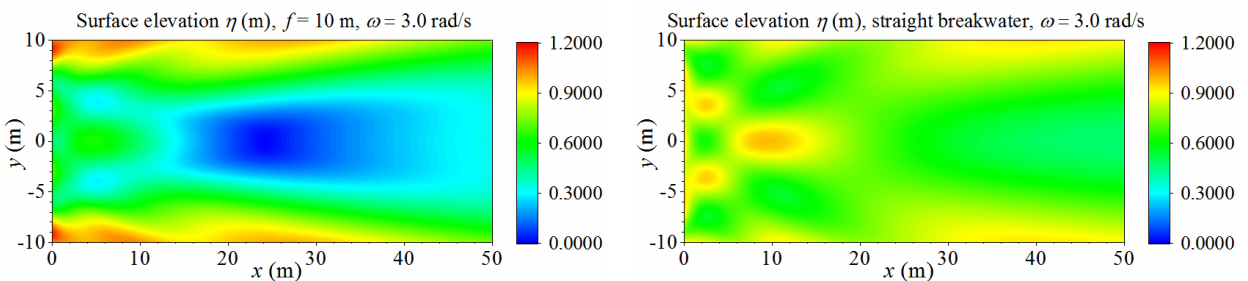
28 Next, we look closely to see how better the attenuation of the  $f=10$  m parabolic arc breakwater could be  
 29 in contrast to that of the straight breakwater in the high-frequency waves. By calculating the ratio of



1 difference  $(\eta_{a|straight}-\eta_{a|f=10\text{ m}})/\eta_{a|f=10\text{ m}}$ , we have for  $\omega=3, 3.5, 4, 4.5,$  and  $5$  rad/s,  $\eta_a$  of the  $f=10$  m parabolic arc  
 2 breakwater is less than that of the straight breakwater by respective ratios of 44.23%, 55.32%, 54.17%,  
 3 51.55%, and 30.26%.



7 **Figure 4** Trends of average elevation  $\eta_a$  in protection zone, with respect to seven parabolic arc breakwaters with  
 8  $f=10, 15, 20, 25, 30, 35, 40$  m and a straight breakwater.  $w=1$  m.  $d=1$  m.  $\omega=1$  to  $5$  rad/s with an increment of  $0.5$   
 9 rad/s.



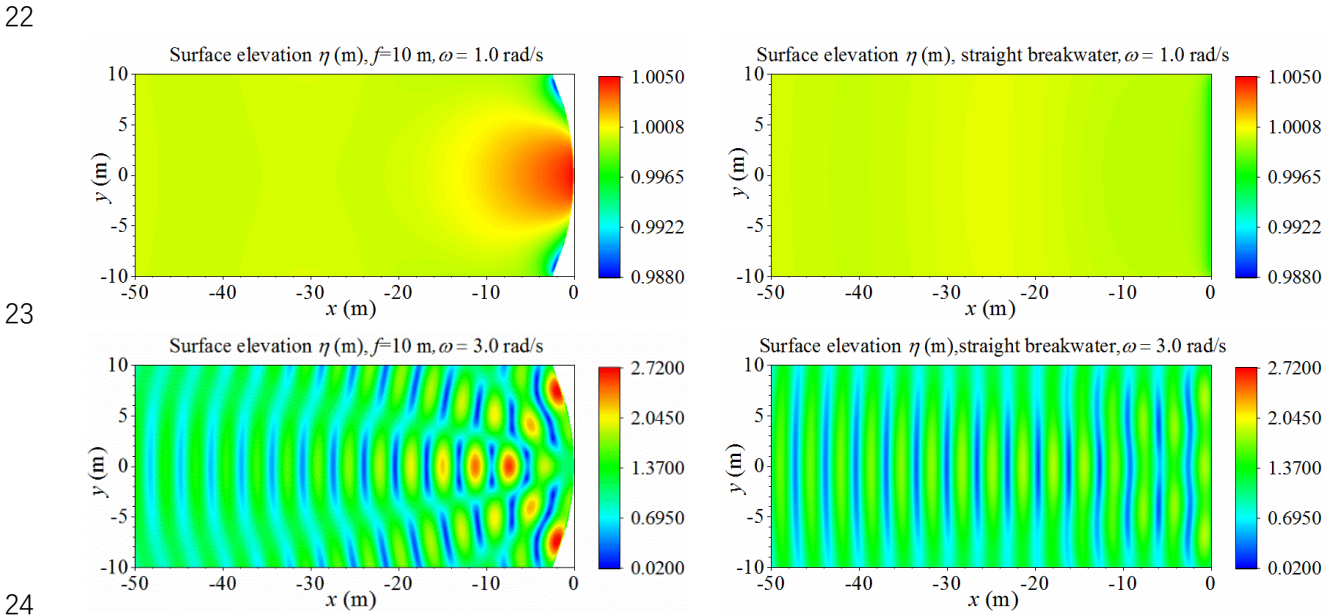
13 **Figure 5** Surface elevation  $\eta$  in the protection zone of the  $f=10$  m parabolic arc breakwater (left) and straight  
 12 breakwaters (right), where  $w=1$  m,  $d=1$  m,  $l=20$  m,  $\omega=3$  rad/s.

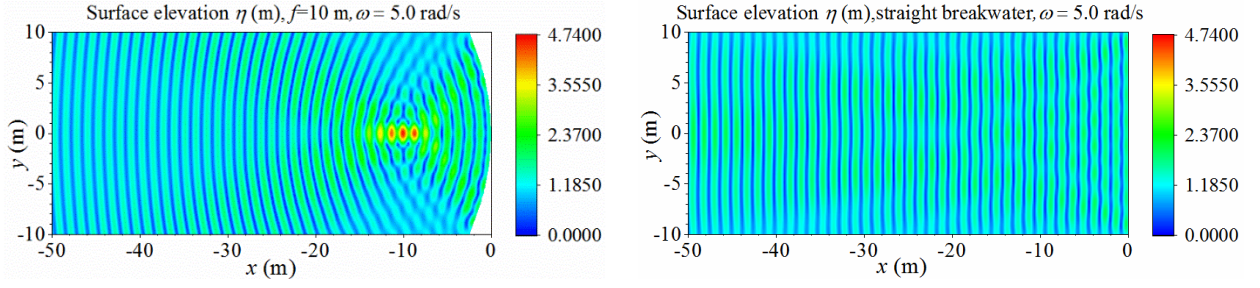
Surface elevation  $\eta$  distribution is illustrated as complementary details for the comparison of attenuation

1 between the  $f=10$  m parabolic arc breakwater and the straight breakwater. Here we take the  $\omega=3$  rad/s case  
 2 as an example (Figure 5). The most distinctive character of the leeward wave field of the parabolic arc  
 3 breakwater is the roughly stratified pattern in  $y$ -direction: narrow high elevation layer (yellow and red) on  
 4 the boundaries, low elevation layer (mainly blue) in the central part, and the medium elevation layer (green)  
 5 in between. No high elevation spot is mixed in the low and medium elevation areas as that in the pattern of  
 6 the straight breakwater. Laterally, from outer to inner of the protection zone, wave motion decreases. In a  
 7 large area (mainly blue) in the central part, wave motion could be quite faint. According to the Fermat  
 8 principle of least time [48], the convex leeward wall is able to direct waves outward the central zone,  
 9 reducing interactions between waves and preventing focusing. This may explain the distribution pattern  
 10 and the better attenuation of the parabolic arc breakwater.

11 *3.2 Focusing*

12 To examine the wave focusing performance of the  $f=10$  m parabolic arc breakwater and the  
 13 straight breakwater, the distribution of  $\eta$  in three representative waves (from low to high,  $\omega=1, 3,$   
 14 and  $5$  rad/s) are displayed in Figure 6. For each wave in this case and hereafter, the maximum  
 15 elevation in the entire deployment zone is used as the upper bound in the rainbow ribbon on the  
 16 right side of the pictures. The lower bounds are chosen accordingly for the best clarity. In all three  
 17 waves, the straight breakwater, in general, shows a wave field with a periodical strip pattern,  
 18 revealing little apparent focusing. Whereas the parabolic arc breakwater is able to focus higher  
 19 waves in some locations (red spots), the focusing strength is varying in different waves. High  
 20 focusing happens in high-frequency waves. As we see in  $\omega=5$  rad/s,  $a$  could be  $4.74$ . The incident  
 21 wave is amplified by nearly five times at the focus of the parabola.





**Figure 6** Surface elevation  $\eta$  in the deployment zone of the  $f=10$  m parabolic arc breakwater (left column) and straight breakwater (right column), where  $w=1$  m,  $d=1$  m,  $l=20$  m,  $\omega=1, 3, 5$  rad/s.

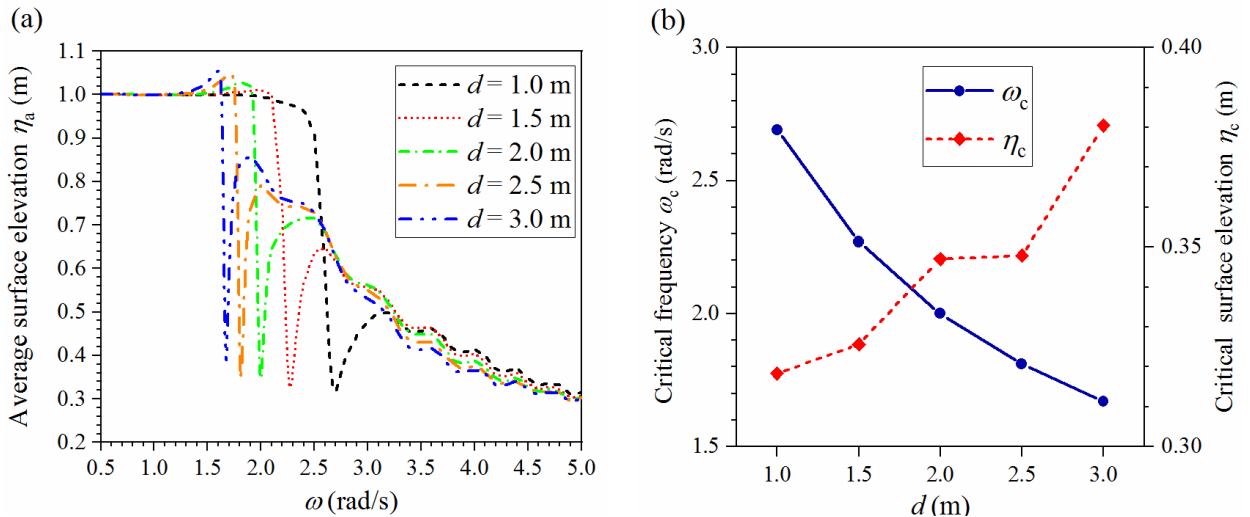
#### 4. Parametric study on the dimensions of the parabolic arc breakwater

In the previous section, we demonstrate the performance of a representative  $f=10$  m parabolic arc breakwater in wave attenuation and focusing. In this part, we will study the influence of its draft, width, and chord length on the performance. The water depth is  $h=5$  m. Incident waves are from 0.5 to 5 rad/s with an increment of 0.01 rad/s.

##### 4.1 Draft

Here the width and chord length are kept fixed as  $w=1$  m and  $l=20$  m. A series of draft  $d=1, 1.5, 2, 2.5, 3$  m are used.

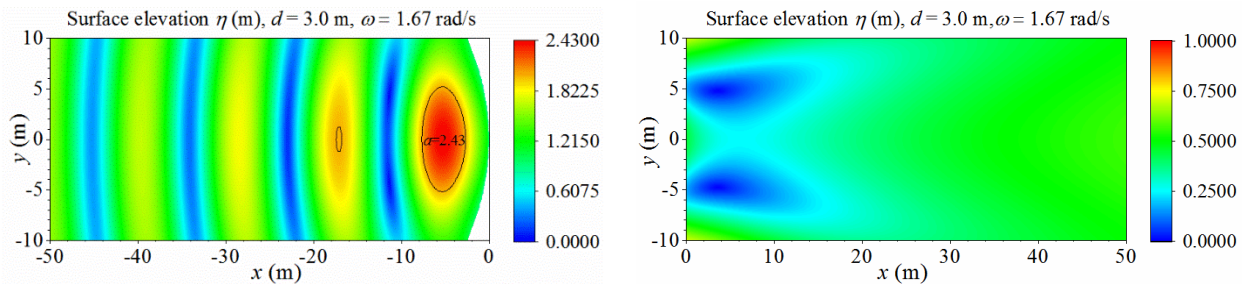
The results of  $\eta_a$  in the protection zone of the five breakwaters are in Figure 7a. We see that attenuation in the five cases shows similar general trends in the frequency domain. The most interesting finding is the existence of sharp local minima. On this point and in the narrow adjacent range around it, relatively low-frequency waves can be effectively attenuated. Herein we would name this particular frequency as the critical frequency by denoting it as  $\omega_c$ . The corresponding local minima of  $\eta_a$  is named as the critical elevation by denoting it as  $\eta_c$ . The breakwater can be potentially tuned to make its critical frequency match the local wave frequency in order to obtain a satisfying attenuation effect.



**Figure 7** a. Average elevation  $\eta_a$  in the frequency domain in the protection zone of the  $f=10$  m parabolic arc breakwaters. b. Trend of critical frequency  $\omega_c$  and critical elevation  $\eta_c$  with respect to  $d$ , where  $w=1$  m,  $l=20$  m,  $d=1, 1.5, 2, 2.5, 3$  m.

Results of  $\omega_c$  and  $\eta_c$  for the different drafts are displayed in Figure 7b. As  $d$  increases from 1 to 3 m,  $\omega_c$  decreases a lot from 2.69 to 1.67 rad/s,  $\eta_c$  increases not much from 0.315 to 0.38 m.  $\omega_c$  is quite sensitive to the change of  $d$ , whereas  $\eta_c$  is not. It indicates that the critical frequency of the breakwater can be effectively reduced by increasing the draft, without loss of much attenuation ability. But such an approach may have some latent limits. First, although the critical elevation does not increase much, it still increases (about 20%), and the attenuation worsens. Other methods, such as installing extended porous plates [39] on the bottom of the leeward wall, may be an alleviation. Second, from Figure 7b one could observe that the decreasing of the critical frequency is slower as the draft increases. Using this method to reduce the critical frequency could be harder for a large draft. Third, as the draft increases, the pattern around the critical point becomes sharper. The effective band is narrower, and the attenuation performance is more sensitive to a varying incident wave frequency around the critical point.

In the five critical frequencies,  $\omega_c=1.81$  rad/s for  $d=2.5$  m and  $\omega_c=1.67$  rad/s for  $d=3$  m are in the range from 1 to 2 rad/s, which is commonly observed in some coastal areas in southwest England [54] and Shandong, China [4]. Here we take the latter case with lower  $\omega_c$  for further investigation. The results of  $\eta$  in the deployment zone and protection zone under the critical condition are shown in Figure 8. The focal areas with  $a>2$  are circled by black lines, and the amplification factor  $a$  in the large one (maximum surface elevation in the circled area/incident wave amplitude) is shown. For attenuation, the low elevation zone (blue) appears a butterfly shape and is mainly in the region closed to the leeward wall. The breakwater could be properly placed to cover targeted infrastructures in this area. The elevation is mostly around 0.5 m in the rest of the area, which is also a reasonable shelter. On the stoss side, the breakwater mainly focuses a large elliptic  $a>2$  area with  $a=2.43$ . Between  $-20$  m  $< x < -10$  m, another  $a>2$  area may be discarded since it is small.

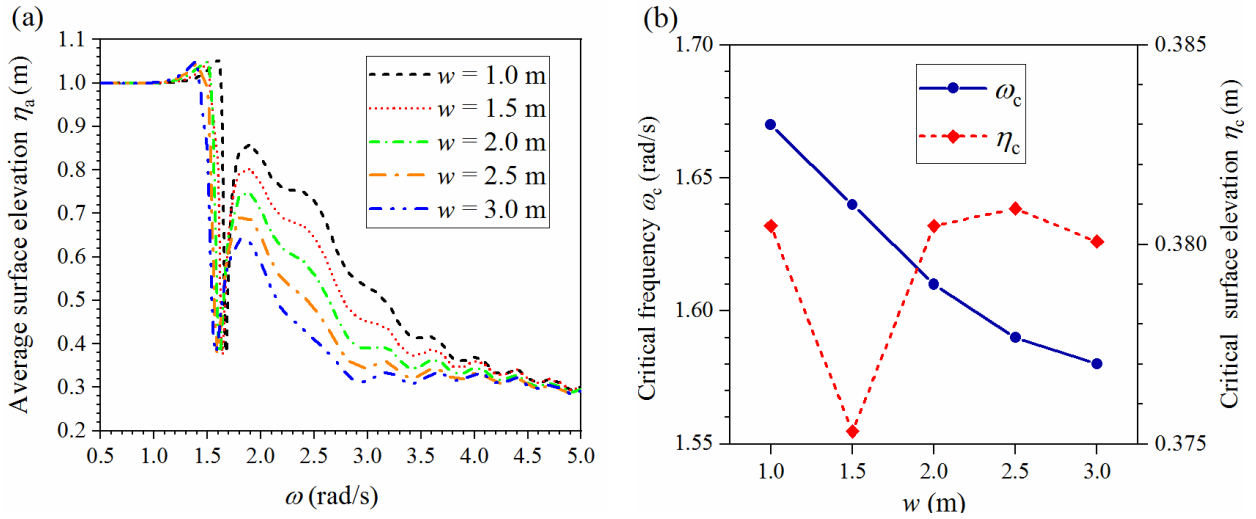


**Figure 8** Surface elevation  $\eta$  in the deployment zone (left) and protection zone (right) behind the  $f=10$  m parabolic arc breakwater in the  $d=3$  m case, where  $w=1$  m,  $l=20$  m. Focal areas with  $a>2$  are circled by the solid line.

Amplification factor  $a$  in the large focal area is given.

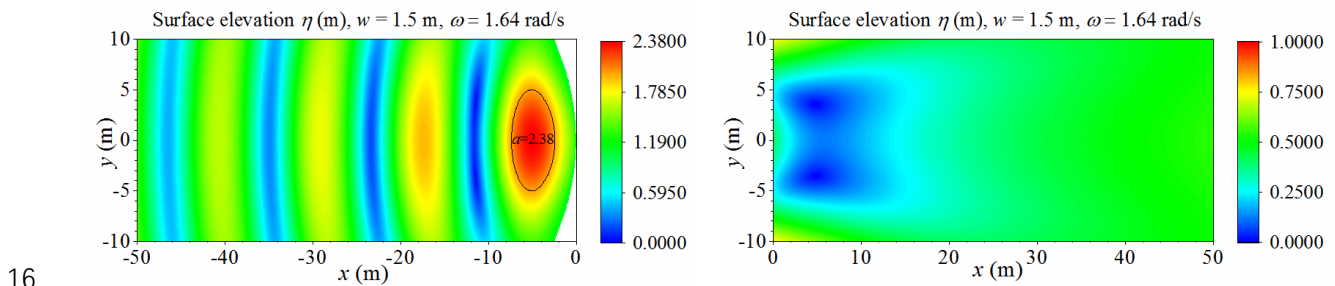
1 4.2 Width

2 Here the draft is  $d=3$  m, and the chord length is  $l=20$  m. A series of width  $w=1, 1.5, 2, 2.5, 3$  m are used.

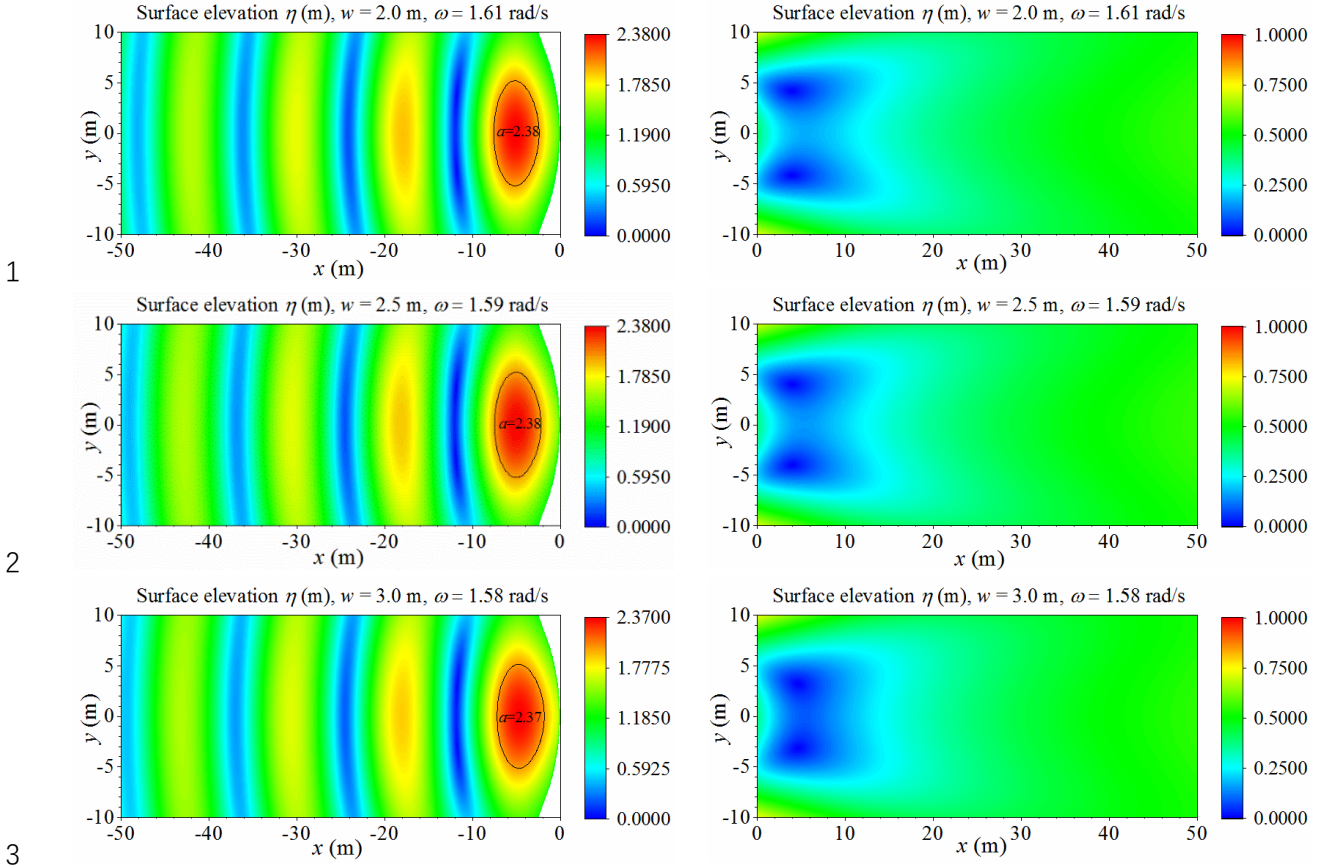


3  
4 **Figure 9** a. Average elevation  $\eta_a$  in the frequency domain in the protection zone of the  $f=10$  m parabolic arc  
5 breakwaters. b. The trend of critical frequency  $\omega_c$  and critical elevation  $\eta_c$  with respect to  $w$ , where  $d=1$  m,  $l=20$  m,  
6  $w=1, 1.5, 2, 2.5, 3$  m.

7 The results of  $\eta_a$  in the frequency domain are in Figure 9a. As  $w$  increases,  $\eta_a$  after  $\omega_c$  is greatly reduced,  
8 but  $\eta_a$  before  $\omega_c$  is hardly affected. Also, the pattern around the critical point is less sharp.  $\omega_c$  and  $\eta_c$  for  
9 different width are displayed in Figure 9b.  $\omega_c$  drops not much from 1.67 rad/s for  $w=1$  to 1.58 rad/s for  $w=3$   
10 m, whereas  $\eta_c$  has only tiny fluctuation around 0.38 m. From the above results, the critical frequency could  
11 be reduced by increasing its width, but the method is not as effective as an increasing draft (Figure 7b). The  
12 decreasing of critical frequency also shows a slowdown as the width increases. For attenuation under the  
13 critical condition, increasing width has a negligible effort, but the effective band around the critical point  
14 becomes wider, making the attenuation less sensitive to a varying incident wave frequency. Besides, an  
15 increased width is quite effective in suppressing high-frequency waves.



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**Figure 10** Surface elevation  $\eta$  in the deployment zone (left) and protection zone (right) behind the  $f=10$  m parabolic arc breakwater for  $w=1.5, 2, 2.5, 3$  m, where  $d=1$  m,  $l=20$  m. Focal areas with  $a>2$  are circled by solid line.

Amplification factor  $a$  in each large focal area is given.

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The distribution of  $\eta$  in the deployment zone and protection zone of the  $w=1.5, 2, 2.5, 3$  m breakwaters under the critical condition are in Figure 10. Together with Figure 8, we find that changing width has a very limited influence on the shape and amplification factor  $a$  of the high elevation area. The distribution in the protection zone is also not affected much.

11

### 4.3 Chord length

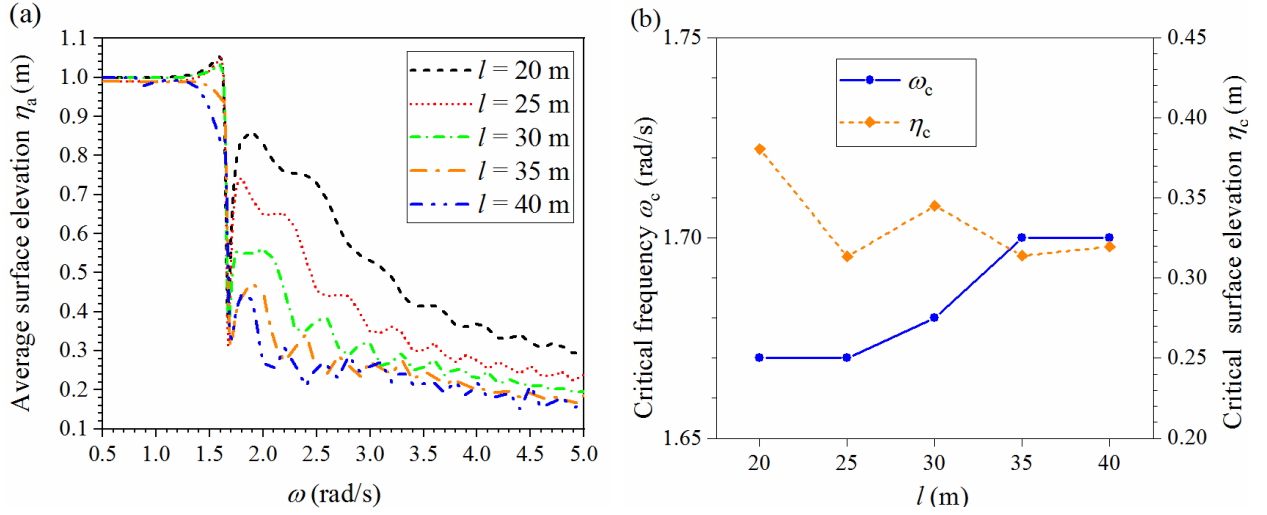
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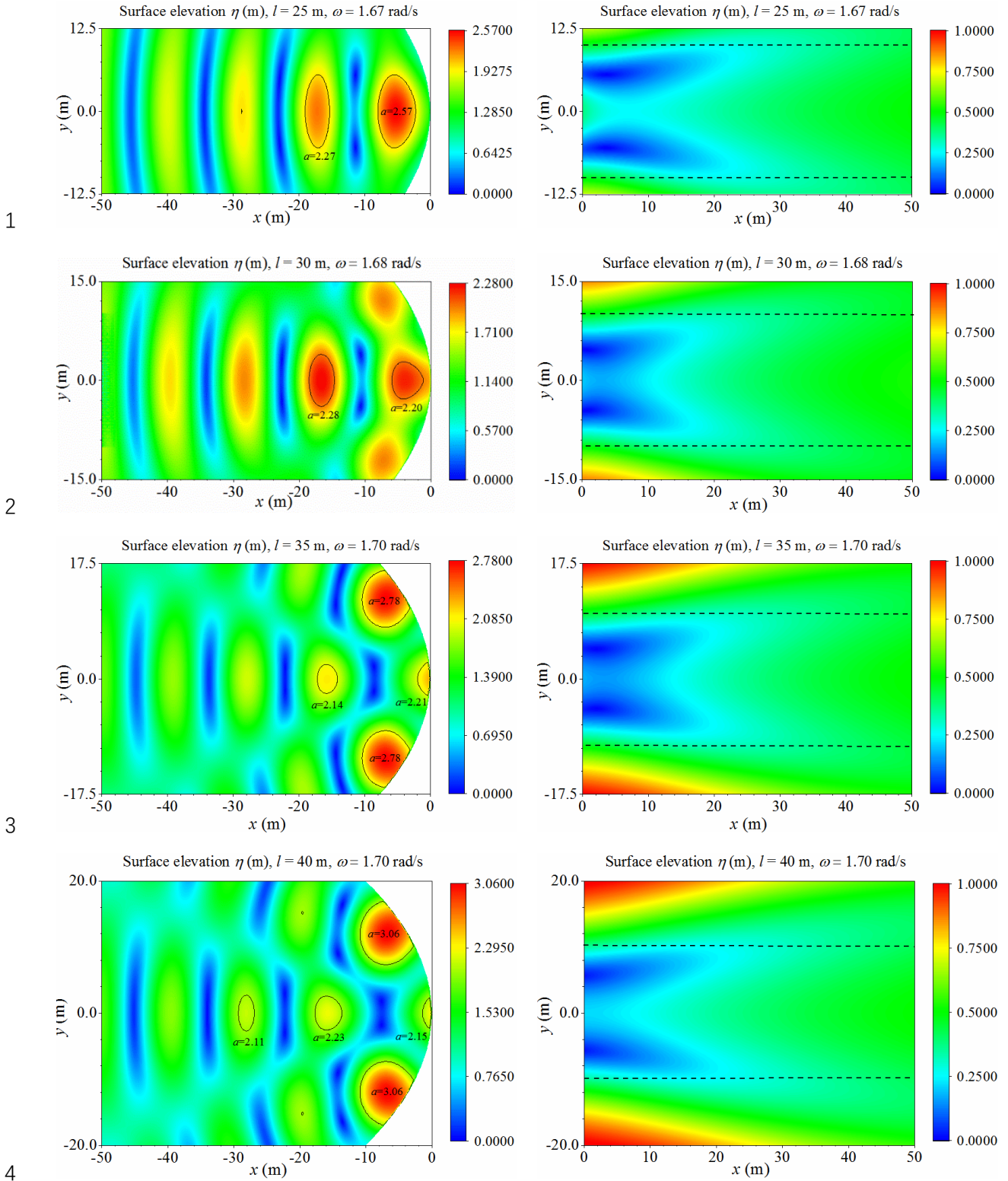
In this part, as we increase the chord length of the breakwater, we keep the targeted protection zone invariant as a  $50 \text{ m} \times 20 \text{ m}$  area, as in the previous sections. The deployment zone is changing with the breakwater as a  $50 \text{ m} \times l$  area. The draft is  $d=3$  m, and the width is  $w=1$  m. Chord length  $l=20, 25, 30, 35, 40$  m are used.



1 **Figure 11** a. Average elevation  $\eta_a$  in the frequency domain in the protection zone of the  $f=10$  m parabolic arc  
 2 breakwaters. b. The trend of critical frequency  $\omega_c$  and critical elevation  $\eta_c$  with respect to  $l$ , where  $w=1$  m,  $d=1$  m,  
 3  $l=20, 25, 30, 35, 40$  m.  
 4

5 In Figure 11a, we see that as  $l$  increases,  $\eta_a$  after the critical point is greatly reduced. This method is  
 6 more effective than increasing the width (Figure 9a) in suppressing waves beyond the critical frequency.  
 7 The pattern around the critical point becomes less sharp; attenuation is less sensitive to a varying spectrum.  
 8 In Figure 11b,  $\omega_c$  slightly increases from 1.67 rad/s for  $l=20$  m to 1.7 rad/s for  $l=40$  m, whereas  $\eta_c$  fluctuates  
 9 in a range from 0.31 to 0.38 m. Increasing chord length has a little negative effect on the reduction of critical  
 10 frequency and a relatively random effect on attenuation under the critical condition.

11 The distribution of  $\eta$  in the deployment zone and protection zone (bounded by dashed lines) of the  $l=25$ ,  
 12 30, 35, 40 m breakwaters under the critical condition are in Figure 12. Amplification factor  $a$  in each large  
 13 focal area is marked. Together with that in Figure 8, the pattern in the protection zone in the five cases are  
 14 similar. The low elevation region is closely behind the leeward wall. In the deployment zone, as the chord  
 15 length increases, high focal areas gradually move from the central part to the sides. As the attenuation and  
 16 focusing are not changing monotonically with the chord length, the five cases need to be treated accordingly.  
 17 First, we should discard the  $l=30$  m case. With an increase in the construction material, higher critical  
 18 frequency and elevation, lower amplification factors, and not larger focal areas, it has little advantage  
 19 comparing with the  $l=25$  m case. The  $l=25$  m case is quite good, the critical frequency and elevation are  
 20 among the lowest, and the two focal areas are relatively large with reasonable amplification factors. The  
 21  $l=35$  and 40 m cases are similar in attenuation, and they both mainly have two symmetric high focal areas.  
 22 The  $l=40$  m case has a bit advantage in the amplification factor and size of the focal area. The low and small  
 23 focal areas could be used for PAWECs, but the high and large focal areas are much better.



5 **Figure 12** Surface elevation  $\eta$  in the deployment zone (left column) and protection zone (right column) behind the  
6  $f=10$  parabolic arc breakwater for  $l=25, 30, 35, 40$  m, where  $w=1$  m,  $d=1$  m. Protection zones are bounded by dashed  
7 lines. Focal areas with  $a>2$  are circled by the solid line. Amplification factor  $a$  in each large focal area is given.

8 Except for the  $l=30$  m case, attenuation, especially in high-frequency waves, and focusing are generally  
9 improved as we increase chord length. However, we should also consider the geometry of the breakwater.



1 The occupation width (see Figure 1) is  $w_o = w + l^2/16f$ . For fixed  $f$  and  $w$ ,  $w_o - w$  is proportional to  $l^2$ . As  $l$   
2 increases,  $w_o$  increases in an approximately quadratic speed. If the chord length is made very large, the  
3 occupation width and total length (the length of the parabola) will be much larger, leading to an abnormal  
4 shape and excessive use of construction material. A compromise between the performance and the shape  
5 has to be made.

## 6 **5. Conclusion**

7 The hybrid system of wave energy converters and breakwaters has become an active research area. This  
8 study proposes a novel parabolic arc pontoon breakwater to improve attenuation performance and focus  
9 high waves for PAWECs. The adaption of the code is validated by a convergence test. Surface elevation in  
10 the development zone and protection zone and amplification factor are used as the main criteria for the  
11 assessment of attenuation and focusing performance. Through a comparative study between the parabolic  
12 arc and straight breakwaters in nine different waves and a parametric study on the  $f=10$  m parabolic arc  
13 breakwater in a wide frequency range, the major remarks are concluded as follows:

14 1. A parabolic arc breakwater is as good as or better than a straight breakwater in attenuation, especially  
15 in high-frequency waves. The  $f=10$  m parabolic arc breakwater is able to focus high waves at certain  
16 locations, whereas the straight breakwater is not.

17 2. A relatively-low critical frequency is found in the narrow band around which the parabolic arc  
18 breakwater has excellent attenuation and focusing performance. The strategy of the breakwater design could  
19 be formulated so as to match the critical frequency with the peak frequency at the operation sites.

20 3. Increasing draft of the parabolic arc breakwater is the most effective way to reduce the critical  
21 frequency, whereas slightly rise the corresponding critical elevation. Increasing width can slightly reduce  
22 the critical frequency and has a small influence on the critical elevation. Increasing chord length raises the  
23 critical frequency a little and has an uncertain but not large influence on the critical elevation. While doing  
24 so, the balance between the performance and shape of the parabolic arc breakwater should also be  
25 considered. A combination of the methods of varying dimensions and others is possible to tune the  
26 breakwater to be effective in a prescribed wave environment. Based on the present study, a breakwater is  
27 found to be capable of attenuating approximate 68% of the elevation as well as to focus two large areas  
28 with an amplified factor of 3.06 in a 3.7s wave, which is commonly observed in some coastal areas in  
29 southwest England and Shandong Province, China.

30 Future work will explore in detail the general design criteria of a parabolic arc breakwater considering  
31 the wave attenuation and focusing performance based on the findings of the present study, which will be  
32 investigated in a later stage.

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3 Open Research Fund through grant LP1815.

## 4 Appendix

5 The Position of center of gravity, mass, and moment of inertia of the floating breakwaters used in this  
6 study are listed in Table 2. The body-fixed coordinate system  $OXYZ$  is located at the center of gravity of a  
7 breakwater. The deployment of the breakwater is shown in Figure 1.

8 **Table 2** Position of center of gravity, mass, and moment of inertia of the floating breakwaters

<b><math>l=20</math> m, <math>w=1</math> m, <math>d=1</math> m</b>					
$f$ (m)	Position of center of gravity in the inertia coordinate system (m)	Breakwater mass (Kg)	Moment of inertia (Kg·m <sup>2</sup> )		
			$I_{XX}$	$I_{YY}$	$I_{ZZ}$
10	(-0.333, 0, 0)	2.050E+04	7.510E+05	2.803E+04	7.568E+05
15	(-0.056, 0, 0)	2.050E+04	7.444E+05	2.083E+04	7.428E+05
20	(0.083, 0, 0)	2.050E+04	7.419E+05	1.833 E+04	7.378E+05
25	(0.167, 0, 0)	2.050E+04	7.417E+05	1.717 E+04	7.355E+05
30	(0.222, 0, 0)	2.050E+04	7.401E+05	1.655 E+04	7.342E+05
35	(0.262, 0, 0)	2.050E+04	7.397E+05	1.617 E+04	7.334E+05
40	(0.292, 0, 0)	2.050E+04	7.395E+05	1.593E+04	7.329E+05
straight	(0.5, 0, 0)	2.050E+04	7.386E+05	1.513E+04	7.313E+05
<b><math>f=10</math> m, <math>l=20</math> m, <math>w=1</math> m</b>					
$d$ (m)	Position of center of gravity in the inertia coordinate system (m)	Breakwater mass (Kg)	Moment of inertia (Kg·m <sup>2</sup> )		
			$I_{XX}$	$I_{YY}$	$I_{ZZ}$
1.5	(-0.333, 0, 0)	3.075E+04	1.154E+06	5.988E+04	1.146E+06
2	(-0.333, 0, 0)	4.100E+04	1.576E+06	1.103E+05	1.536E+06
2.5	(-0.333, 0, 0)	5.125E+04	2.023E+06	1.843E+05	1.927E+06
3	(-0.333, 0, 0)	6.150E+04	2.498E+06	2.872E+05	2.319E+06
<b><math>f=10</math> m, <math>l=20</math> m, <math>d=3</math> m</b>					
$w$ (m)	Position of center of gravity in the inertia coordinate system (m)	Breakwater mass (Kg)	Moment of inertia (Kg·m <sup>2</sup> )		
			$I_{XX}$	$I_{YY}$	$I_{ZZ}$
1.5	(-0.083, 0, 0)	9.255E+04	3.862E+06	4.850E+05	3.591E+06
2	(0.167, 0, 0)	1.230E+05	5.280E+06	7.226E+05	4.931E+06
2.5	(0.417, 0, 0)	1.538E+05	6.742E+06	1.003E+06	6.336E+06
3	(0.667, 0, 0)	1.845E+05	8.238E+06	1.330E+06	7.806E+06
<b><math>f=10</math> m, <math>d=3</math> m, <math>w=1</math> m</b>					
$l$ (m)	Position of center of gravity in the inertia coordinate system (m)	Breakwater mass (Kg)	Moment of inertia (Kg·m <sup>2</sup> )		
			$I_{XX}$	$I_{YY}$	$I_{ZZ}$
25	(-0.802, 0, 0)	7.688E+04	4.700E+06	4.284E+05	4.546E+06
30	(-1.375, 0, 0)	9.225E+04	7.989E+06	6.646E+05	7.957E+06
35	(-2.052, 0, 0)	1.076E+05	1.262E+07	1.065E+06	1.287E+07
40	(-2.833, 0, 0)	1.230E+05	1.885E+07	1.725E+06	1.966E+07

## 9 Reference

- 1 [1] Ning, D. Z., Wang, R. Q., Zou, Q. P., & Teng, B. (2016). An experimental investigation of  
2 hydrodynamics of a fixed OWC Wave Energy Converter. *Applied Energy*, 168, 636-648.
- 3 [2] Perez-Collazo, C., Greaves, D., & Iglesias, G. (2018). Hydrodynamic response of the WEC sub-system  
4 of a novel hybrid wind-wave energy converter. *Energy Conversion and Management*, 171, 307-325.
- 5 [3] Elhanafi, A., Macfarlane, G., & Ning, D. (2018). Hydrodynamic performance of single-chamber and  
6 dual-chamber offshore-stationary Oscillating Water Column devices using CFD. *Applied Energy*, 228,  
7 82-96.
- 8 [4] Hu, J., Zhou, B., Vogel, C., Liu, P., Willden, R., Sun, K., ... & Collu, M. (2020). Optimal design and  
9 performance analysis of a hybrid system combining a floating wind platform and wave energy converters.  
10 *Applied Energy*.
- 11 [5] Mustapa, M. A., Yaakob, O. B., Ahmed, Y. M., Rheem, C. K., Koh, K. K., & Adnan, F. A. (2017).  
12 Wave energy device and breakwater integration: A review. *Renewable and Sustainable Energy  
13 Reviews*, 77, 43-58.
- 14 [6] Dai, J., Wang, C. M., Utsunomiya, T., & Duan, W. (2018). Review of recent research and developments  
15 on floating breakwaters. *Ocean Engineering*, 158, 132-151.
- 16 [7] Babarit, A. (2017). *Ocean wave energy conversion: resource, technologies and performance*. Elsevier.
- 17 [8] Xu, C., & Huang, Z. (2018). A dual-functional wave-power plant for wave-energy extraction and shore  
18 protection: A wave-flume study. *Applied Energy*, 229, 963-976.
- 19 [9] Zheng, S., & Zhang, Y. (2018). Analytical study on wave power extraction from a hybrid wave energy  
20 converter. *Ocean Engineering*, 165, 252-263.
- 21 [10] Chen, B., Bruce, T., Greated, C. A., & Kang, H. (2017). Dynamic behavior of a wave power buoy with  
22 interior on-board linear generator. *Ocean Engineering*, 129, 374-381.
- 23 [11] Krishnendu, P., & Balaji, R. (2020). Hydrodynamic performance analysis of an integrated wave energy  
24 absorption system. *Ocean Engineering*, 195, 106499.
- 25 [12] Zhang, H., Zhou, B., Vogel, C., Willden, R., Zang, J., & Zhang, L. (2020). Hydrodynamic performance  
26 of a floating breakwater as an oscillating-buoy type wave energy converter. *Applied Energy*, 257,  
27 113996.
- 28 [13] Zhang, X., Zeng, Q., & Liu, Z. (2019). Hydrodynamic Performance of Rectangular Heaving Buoys  
29 for an Integrated Floating Breakwater. *Journal of Marine Science and Engineering*, 7(8), 239.
- 30 [14] Peng, W., Fan, Y., & Zhang, J. (2018). Numerical Study on Optimization of the Float in a Shoreline  
31 Wave Energy Converter. *Journal of Coastal Research*, 85(sp1), 1296-1300.
- 32 [15] Madhi, F., & Yeung, R. W. (2018). On survivability of asymmetric wave-energy converters in extreme  
33 waves. *Renewable Energy*, 119, 891-909.
- 34 [16] De Almeida, J. L. (2017). REEFS: An artificial reef for wave energy harnessing and shore protection–  
35 A new concept towards multipurpose sustainable solutions. *Renewable energy*, 114, 817-829.
- 36 [17] Di Lauro, E., Lara, J. L., Maza, M., Losada, I. J., Contestabile, P., & Vicinanza, D. (2019). Stability  
37 analysis of a non-conventional breakwater for wave energy conversion. *Coastal Engineering*, 145, 36-  
38 52.
- 39 [18] Vicinanza, D., & Frigaard, P. (2008). Wave pressure acting on a seawave slot-cone generator. *Coastal  
40 Engineering*, 55(6), 553-568.
- 41 [19] Zhang, H., Zhou, B., Vogel, C., Willden, R., Zang, J., & Geng, J. (2020). Hydrodynamic performance  
42 of a dual-floater hybrid system combining a floating breakwater and an oscillating-buoy type wave

- 1 energy converter. *Applied Energy*, 259, 114212.
- 2 [20] Reabroy, R., Zheng, X., Zhang, L., Zang, J., Yuan, Z., Liu, M., ... & Tiaple, Y. (2019). Hydrodynamic  
3 response and power efficiency analysis of heaving wave energy converter integrated with  
4 breakwater. *Energy Conversion and Management*, 195, 1174-1186.
- 5 [21] Zheng, S., Zhang, Y., & Iglesias, G. (2020). Concept and performance of a novel wave energy  
6 converter: Variable Aperture Point-Absorber (VAPA). *Renewable Energy*, 153, 681-700.
- 7 [22] Bachynski, E. E., Young, Y. L., & Yeung, R. W. (2012). Analysis and optimization of a tethered wave  
8 energy converter in irregular waves. *Renewable energy*, 48, 133-145.
- 9 [23] Jin, P., Zhou, B., Götteman, M., Chen, Z., & Zhang, L. (2019). Performance optimization of a coaxial-  
10 cylinder wave energy converter. *Energy*, 174, 450-459.
- 11 [24] Noad, I. F., & Porter, R. (2015). Optimisation of arrays of flap-type oscillating wave surge  
12 converters. *Applied Ocean Research*, 50, 237-253.
- 13 [25] Mehlum, E., & Stamnes, J. (1978). On the focusing of ocean swells and its significance in power  
14 production. *Cent. Inst. for Indust. Res., Blindern, Oslo, SI Rep*, 77, 01-38.
- 15 [26] Hu, X., & Chan, C. T. (2005). Refraction of water waves by periodic cylinder arrays. *Physical review  
16 letters*, 95(15), 154501.
- 17 [27] Griffiths, L. S., & Porter, R. (2012). Focusing of surface waves by variable bathymetry. *Applied Ocean  
18 Research*, 34, 150-163.
- 19 [28] Elandt, R. B., Shakeri, M., & Alam, M. R. (2014). Surface gravity-wave lensing. *Physical Review  
20 E*, 89(2), 023012.
- 21 [29] Murashige, S., & Kinoshita, T. (1992). An ideal ocean wave focusing lens and its shape. *Applied ocean  
22 research*, 14(5), 275-290.
- 23 [30] Stamnes, J. J., Løvhaugen, O., Spjelkavik, B., Mei, C. C., Lo, E., & Yue, D. K. (1983). Nonlinear  
24 focusing of surface waves by a lens—theory and experiment. *Journal of Fluid Mechanics*, 135, 71-94.
- 25 [31] Li, C. Y., Shih, R. S., & Weng, W. K. (2020). Investigation of Ocean-Wave-Focusing Characteristics  
26 Induced by a Submerged Crescent-Shaped Plate for Long-Crested Waves. *Water*, 12(2), 509.
- 27 [32] Newman, J. N. (2015). Amplification of waves by submerged plates. In *30th International Workshop  
28 on Water Waves and Floating Bodies (IWWWFB)*, Bristol, UK (pp. 153-156).
- 29 [33] Zhang, C., & Ning, D. (2019). Hydrodynamic study of a novel breakwater with parabolic openings for  
30 wave energy harvest. *Ocean Engineering*, 182, 540-551.
- 31 [34] Liu, Z., Wang, Y., Wang, W., & Hua, X. (2019). Numerical modeling and optimization of a winged  
32 box-type floating breakwater by Smoothed Particle Hydrodynamics. *Ocean Engineering*, 188, 106246.
- 33 [35] Zhang, X. S., Ma, S., & Duan, W. Y. (2018). A new L type floating breakwater derived from vortex  
34 dissipation simulation. *Ocean Engineering*, 164, 455-464.
- 35 [36] Christensen, E. D., Bingham, H. B., Friis, A. P. S., Larsen, A. K., & Jensen, K. L. (2018). An  
36 experimental and numerical study of floating breakwaters. *Coastal engineering*, 137, 43-58.
- 37 [37] He, F., Huang, Z., & Law, A. W. K. (2013). An experimental study of a floating breakwater with  
38 asymmetric pneumatic chambers for wave energy extraction. *Applied energy*, 106, 222-231.
- 39 [38] Diamantoulaki, I., & Angelides, D. C. (2010). Analysis of performance of hinged floating  
40 breakwaters. *Engineering Structures*, 32(8), 2407-2423.

- 1 [39] Koutandos, E. V., & Prinos, P. E. (2011). Hydrodynamic characteristics of semi-immersed breakwater  
2 with an attached porous plate. *Ocean Engineering*, 38(1), 34-48.
- 3 [40] Uzaki, K. I., Ikehata, Y., & Matsunaga, N. (2011). Performance of the wave energy dissipation of a  
4 floating breakwater with truss structures and the quantification of transmission coefficients. *Journal*  
5 *of Coastal Research*, 27(4), 687-697.
- 6 [41] Singla, S., Behera, H., Martha, S. C., & Sahoo, T. (2019). Scattering of obliquely incident water waves  
7 by a surface-piercing porous box. *Ocean Engineering*, 193, 106577.
- 8 [42] Ji, C. Y., Chen, X., Cui, J., Gaidai, O., & Incecik, A. (2016). Experimental study on configuration  
9 optimization of floating breakwaters. *Ocean Engineering*, 117, 302-310.
- 10 [43] Koo, W. (2009). Nonlinear time-domain analysis of motion-restrained pneumatic floating  
11 breakwater. *Ocean Engineering*, 36(9-10), 723-731.
- 12 [44] Williams, A. N., Lee, H. S., & Huang, Z. (2000). Floating pontoon breakwaters. *Ocean*  
13 *Engineering*, 27(3), 221-240.
- 14 [45] Dong, G. H., Zheng, Y. N., Li, Y. C., Teng, B., Guan, C. T., & Lin, D. F. (2008). Experiments on wave  
15 transmission coefficients of floating breakwaters. *Ocean Engineering*, 35(8-9), 931-938.
- 16 [46] Duan, J. H., Cheng, J. S., Wang, J. P., & Wang, J. Q. (2012). Wave diffraction on arc-shaped floating  
17 perforated breakwaters. *China Ocean Engineering*, 26(2), 305-316.
- 18 [47] Chang, K. H., Tsaur, D. H., & Huang, L. H. (2012). Accurate solution to diffraction around a modified  
19 V-shaped breakwater. *Coastal engineering*, 68, 56-66.
- 20 [48] Feynman, R. P., Leighton, R. B., & Sands, M. (2011). *The Feynman lectures on physics, Vol. I: The*  
21 *new millennium edition: mainly mechanics, radiation, and heat* (Vol. 1). Basic books.
- 22 [49] Chu, Y. C., Cheng, J. S., Wang, J. Q., Li, Z. G., & Jiang, K. B. (2014). Hydrodynamic performance of  
23 the arc-shaped bottom-mounted breakwater. *China Ocean Engineering*, 28(6), 749-760.
- 24 [50] Liu, J., & Lin, G. (2013). Scaled boundary FEM solution of short-crested wave interaction with a  
25 concentric structure with double-layer arc-shaped perforated cylinders. *Computers & Fluids*, 79, 82-  
26 104.
- 27 [51] Liu, Y. (2019). HAMS: A Frequency-Domain Preprocessor for Wave-Structure Interactions—Theory,  
28 Development, and Application. *Journal of Marine Science and Engineering*, 7(3), 81.
- 29 [52] Liu, Y., Yoshida, S., Hu, C., Sueyoshi, M., Sun, L., Gao, J., Cong P. & He, G. (2018). A reliable open-  
30 source package for performance evaluation of floating renewable energy systems in coastal and  
31 offshore regions. *Energy conversion and management*, 174, 516-536.
- 32 [53] Lee, C. H., & Newman, J. N. (1999). *WAMIT User manual*. Dept. of Ocean Engineering,  
33 Massachusetts Institute of Technology, Cambridge, MA.
- 34 [54] Plymouth coastal observatory. (2020). Live waves and tides. Retrieved from  
35 <http://southwest.coastalmonitoring.org/live-waves-and-tides/>.