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1	On hydrodynamic characteristics of gap resonance between two fixed bodies in close						
2	proximity						
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12							
13	Abstract:						
14	The resonant water motion inside a narrow gap between two identical fixed boxes that are in						
15	side-by-side configuration is investigated using a two-dimensional (2D) numerical wave tank based						
16	on OpenFOAM®, an open source CFD package. Gap resonance is excited by regular waves with						
17	various wave heights, ranging from linear waves to strong nonlinear waves. This paper mainly						
18	focuses on the harmonic analyses of the free-surface elevation in the narrow gap and wave loads						
19	(including the horizontal wave forces, the vertical wave forces and the moments) on the bodies. It						
20	is found that the influences of the incident wave height on the higher-order harmonic components						
21	of different physical quantities are quite different. The effects of the incident wave height on the						
22	reflection, transmission and energy loss coefficients are also discussed. Finally, aiming at the						
23	quantitative estimation of the response time and the damping time of gap resonance, two different						
24	methods are proposed and verified for the first time on gap resonance.						
25							
26	Keywords: Gap resonance; Wave height amplification; Wave force; Harmonic analysis; Response						
27	time and damping time of gap resonance; OpenFOAM®						
28							

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1. Introduction

In the past few decades, as the oil and gas industry have moved towards deeper waters and 30 31 harsher environments, Floating Production Storage and Offloading (FPSO) platforms have shown great potential as the most economic ways to process and distribute the hydrocarbon products. One 32 of the key challenges for FPSO platforms lies in the safe offloading operations from them to a shuttle 33 34 tanker when the tanker is positioned side-by-side with them. When multiple floating bodies are deployed side-by-side in close proximity and are subjected to incident water waves, drastic water 35 36 surface oscillations may occur inside the narrow gaps between them at certain frequencies. This phenomenon is normally referred to as "gap resonance". 37

38 The hydrodynamic interactions of multiple bodies with narrow gaps between have been investigated extensively due to its relevance to offloading facilities for FPSO. The methods used in 39 40 these studies include theoretical analyses, physical experiments and numerical simulations. The 41 theoretical analyses were mainly used in the early studies of the gap resonance problem and were 42 mainly based on the linear potential flow theory (Miao et al., 2000; Molin, 2001). Subsequently, to better understand gap resonance and to validate the theoretical analyses, a large number of physical 43 44 model tests in 2D and 3D wave basins were also implemented by previous researchers (e.g., Iwata 45 et al. (2007); Saitoh et al. (2006); Zhao et al. (2017)). The numerical investigations conducted so far are mainly based on the classical potential flow model employing the boundary element method and 46 47 scaled boundary finite element method (e.g., Li et al. (2005); Li and Zhang (2016); Sun et al. (2010)).

48 Although both theoretical analyses and the numerical simulations based on the potential flow theory have been shown to predict the resonant frequency well, they were reported to significantly 49 50 over-estimate the resonant wave height inside the gap and the wave forces on the floating bodies, 51 because the physical energy dissipation due to the fluid viscosity, vortex shedding and even 52 turbulences cannot be considered in the context of potential flow theory. To overcome this problem, 53 several particular numerical techniques that artificially introduce wave energy dissipation term into the potential flow model were developed so far (Chen, 2004; Huijsmans et al., 2001; Lu et al., 2010b; 54 55 Newman, 2004; Ning et al., 2015a, b). However, the introduction of artificial damping term seems 56 somewhat arbitrary for the rigorous potential theory, and under some conditions it was found to be 57 difficult to obtain a unique value of the damping parameter (Pauw et al., 2007; Tan et al., 2014). In 58 recent years, with the fast developments of computing technology, the CFD simulation has gradually

59 become an alternative method in investigating the gap resonance problem (Jiang et al. (2018); Lu et al. (2010a); Lu et al. (2011a); Lu et al. (2011b); Moradi et al. (2015, 2016)). All these studies found 60 61 that the results obtained by the CFD simulations agreed well with those from existing experiments. While many research efforts into the gap resonance have been undertaken, the majority have 62 concentrated on the analyses of the overall resonant wave height in the narrow gap and the overall 63 64 wave loads on the boxes under the condition of the linear or weakly nonlinear regular waves (e.g., Feng et al. (2017); Jiang et al. (2018); Lu et al. (2010a); Lu et al. (2010b); Lu et al. (2011a); Lu et 65 66 al. (2011b); Moradi et al. (2015, 2016)). The investigations on the harmonic analyses of the wave height and wave loads are relatively rare. By using a semi-analytical formulation of the velocity 67 68 potentials, Mavrakos and Chatjigeorgiou (2009) investigated the significance of the second-order effects to the total wave loading on a cylindrical moonpool, especially in the frequency regions in 69 70 which the fluid resonance occurs. Sun et al. (2010) employed a 3D boundary element code 71 DIFFRACT to investigate the first- and second-order loads and free-surface elevations for two side-72 by-side rectangular barges. However, both of their methods are based on the classical potential flow 73 theory which does not consider the physical energy dissipation due to the viscous effect. Hence, 74 some of their findings may not reflect real phenomena of the fluid resonance in the narrow gap or 75 in the moonpool, where the physical energy dissipation plays an important role. Zhao et al. (2017) 76 investigated experimentally the first and higher harmonic components of the resonant fluid response 77 in the gap between two identical fixed rectangular boxes excited by the transient focused wave 78 groups in a 3D wave basin. However, the gap resonance induced by the regular waves and the 79 harmonic analyses on wave loads were not considered in that paper.

80 To further improve the understanding of related phenomena involved in gap resonance, this 81 paper mainly focuses on the variations of the first and higher harmonic components of free-surface 82 elevation inside the gap and wave loads on boxes with respect to the wave height of the incident 83 regular waves when gap resonance occurs. In this paper, the system of two identical boxes is taken 84 as the background of this study. For comparison, the same problem is also investigated when the 85 free-surface elevation in the narrow gap is under non-resonant conditions. Compared to the previous 86 investigations (i.e., Feng et al. (2017); Jiang et al. (2018); Lu et al. (2010a); Lu et al. (2010b); Lu et 87 al. (2011a); Lu et al. (2011b); Moradi et al. (2015, 2016)), stronger nonlinear incident waves are 88 used in this paper, which is necessary due to the fact that FPSO platforms are often exposed to severe

89 wave conditions. Subsequently, the variations of the reflection coefficient C_r , the transmission coefficient C_t and the energy loss coefficient $L_e = 1 - C_r^2 - C_t^2$ with respect to the frequency of 90 91 the incident waves with various wave heights are also discussed, because an integral comprehension 92 of these coefficients may promote the better understanding of the mechanism essence of the gap 93 resonance (Jiang et al., 2018). Meanwhile, these previous studies were mainly concerned on the 94 related hydrodynamic phenomena after the free-surface resonance in the narrow gap reached the 95 steady state, and both the response and the damp phases were paid little attention to. In the current 96 paper, both the response time and the damping time of gap resonance are quantitatively evaluated by two different methods. In practical engineering applications, the fast and accurate estimation of 97 98 the response time and the damping time is very important for the safe evacuation of staff and the reasonable arrangement of operation time during the offloading operations from a FPSO platform 99 100 to a shuttle tanker under gap resonance conditions.

In Sections 2, 3 and 4, the numerical model employed in this work, numerical experimental setup and the validations of the numerical model against available experimental and numerical data are presented, respectively. The numerical results and discussions are presented in Section 5. Finally, conclusions are drawn in Section 6.

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106 2. Numerical model description

To consider the physical energy dissipation near the gap due to the viscous effect, a viscous flow solver is necessary. In this paper, the numerical wave tank is based on the OpenFOAM[®] multiphase solver "interFoam", and waves are generated and dissipated using the relaxation-based wave generation toolbox "waves2Foam" proposed by Jacobsen et al. (2012).

111 2.1. Governing equations

112 The continuity and Navier-Stokes equations are utilized as the governing equations to solve 113 the two-phase flow of water and air:

114

$$\frac{\partial \rho}{\partial t} + \nabla \cdot \left(\rho \mathbf{u} \right) = 0 , \qquad (1)$$

115
$$\frac{\partial \rho \mathbf{u}}{\partial t} + \nabla \cdot (\rho \mathbf{u} \mathbf{u}^T) = -\nabla P - (\mathbf{g} \cdot \mathbf{x}) \nabla \rho + \nabla \cdot (\mu \nabla \mathbf{u}) + \sigma_t k_{\alpha} \nabla \alpha , \qquad (2)$$

116 where ρ is the fluid density, $\nabla = \left(\frac{\partial}{\partial x}, \frac{\partial}{\partial y}, \frac{\partial}{\partial z}\right)$ is the gradient operation, $\mathbf{u} = (u, v, w)$ is the velocity 117 vector of the fluid, $\mathbf{x} = (x, y, z)$ is the Cartesian coordinate vector, \mathbf{g} is the gravitational acceleration, 118 *P* is the pressure in excess of the hydrostatic part, μ is the dynamic viscosity of the fluid, σ_t is the 119 surface tension coefficient and k_{α} is the surface curvature. The above equations are solved for 120 both water and air simultaneously. α denotes the volume fraction of water in the computational cell, 121 which takes a value of 1 for water and 0 for air and intermediate values for a mixture of water and 122 air. The distribution of α is modelled by the following advection transport equation:

123
$$\frac{\partial \alpha}{\partial t} + \nabla \cdot (\alpha \mathbf{u}) + \nabla \cdot [\alpha (1 - \alpha) \mathbf{u}_{\mathrm{r}}] = 0, \qquad (3)$$

124 in which $\mathbf{u}_{r} = \mathbf{u}_{water} - \mathbf{u}_{air}$ is a relative velocity between the water and the air. Using α , the spatial 125 variation of any fluid property φ (e.g., the fluid density ρ and the dynamic viscosity μ) can be 126 expressed through the weighting

127 $\varphi = \alpha \varphi_{\text{water}} + (1 - \alpha) \varphi_{\text{air}}, \qquad (4)$

where the subscripts "water" and "air" denote the corresponding fluid property of water and air,respectively.

130 2.2. Boundary conditions and numerical implementations

The toolbox "waves2Foam" proposed by Jacobsen et al. (2012) is employed to generate and 131 132 absorb waves at the boundaries (see Fig. 1). At the inlet and the outlet boundaries, the velocities are defined as that of a regular incoming wave and as zero, respectively, and the pressure gradients are 133 134 set to zero. Two relaxation zones are deployed at the inlet and the outlet boundaries to absorb the reflected and the transmitted waves. At the upper part of the tank, the boundary condition is set as 135 "atmosphere"; while at the bottom of the tank and the solid walls of the fixed boxes, "no-slip" 136 boundary condition is applied. For a 2D problem, the boundary condition on the walls in the third 137 dimension is set to "empty". 138

The governing equations (1)-(2) and the advection transport equation (3) are solved based on the finite volume method. The velocity-pressure coupling is calculated using the PISO (Pressure Implicit with Splitting of Operator) algorithm. Gradients are approximated by the Gaussian integration method based on a linear interpolation form cell centers to cell faces. The time derivatives are solved by a first-order Euler scheme. The Gauss Convection-specific schemes are used for the evaluation of the divergence terms. Identical to Feng et al. (2017), to produce accurate and stable results, the largest Courant number is set to 0.25 in all simulations.

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Once Eqs. (1)-(3) are solved at each time step, the wave force and the moment on the structure

can be calculated by the following formulations: 147

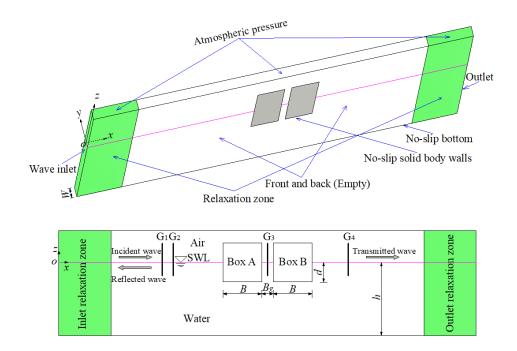
 $\mathbf{F} = \int_{\Omega} \left[P \mathbf{n} + \mu (\partial \mathbf{u}_{\tau} / \partial \mathbf{n}) \right] ds ,$

- 149 and
- 150

$$\mathbf{M} = \int_{\Omega} \mathbf{r} \times [P\mathbf{n} + \mu(\partial \mathbf{u}_{\tau} / \partial \mathbf{n})] ds , \qquad (6)$$

(5)

151 where **F** and **M** are the vectors of the wave force and the moment, respectively, \mathbf{u}_r is the tangent 152 velocity component, \mathbf{n} is the unit normal vector, ds is the surface area differential on the wet solid surface Ω , and **r** is the position vector of ds relative to a certain space point. For the gap resonance 153 154 problem that will be described in detail in Section 3, the moments on the two fixed boxes correspond 155 to their respective centroids. As for the harmonic analysis for various variables (i.e., the free-surface elevation in the gap, the horizontal and vertical wave forces and the moments on the two boxes), 156 they are performed by using the discrete Fourier transform for the time-histories of their respective 157 158 signals.



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Fig. 1. Sketch of the numerical wave tank: (a) boundary conditions and the definition of the coordinate system; (b) positions of wave gauges and the definition of the geometric parameters. 161

162 3. Numerical wave tank

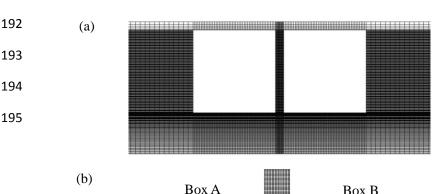
Fig. 1 illustrates the sketch of the 2D numerical wave tank used in the present study. The wave 163 tank has a length of 18.5 m, a height of 0.8 m and a width of W=0.1 m. The origin of the coordinate 164 system is located at the still water level (SWL) of the left inlet boundary. The x-axis is in the wave 165

propagation direction, and the *z*-axis is in the upward direction. The thickness of the wave tank in y-direction corresponds to a cell. Two identical fixed boxes are placed at the middle of the wave tank. The box height is H=0.5 m, the breadth is B=0.5 m, the draft d=0.25 m, the gap width $B_g=0.05$ m, the water depth is h=0.5 m, and the air depth is $h_a=0.3$ m. This configuration is in accordance with the physical experiments in Saitoh et al. (2006) as well as the numerical investigations in Lu et al. (2008; 2011a; 2011b).

172 Five sets of simulations are implemented, in which the wave heights of the incident regular waves are set to $H_0 = 0.010$ m, 0.024 m, 0.050 m, 0.075 m and 0.100 m, respectively. The wave 173 frequency, ω , considered in all the five sets of simulations ranges from 4.456 rad/s to 7.534 rad/s. 174 175 Correspondingly, the dimensionless wavenumber, kh, ranges from 1.210 to 2.910, where $k=2\pi/L$ 176 denotes the wavenumber and L denotes the wavelength. Four wave gauges, G_1 - G_4 , are arranged to record the free-surface elevations. G_1 and G_2 are utilized to decompose the incident and reflected 177 178 waves, and their distance is set to 0.25 m. G_3 and G_4 are used to obtain the free surfaces inside the gap and the transmitted waves. G₃ is placed in the middle of the gap; while G₂ and G₄ are positioned 179 180 at 1.50 m from the left side of Box A and the right side of Box B, respectively. Two relaxation zones 181 of 5.50 m long each are placed at the inlet and outlet boundaries of the wave tank to absorb the 182 reflected and transmitted waves. The length of 5.50 m is approximately 2.11 times of the maximum 183 wavelength that corresponds to the incident waves with $\omega = 4.456$ rad/s.

A built-in mesh generation utility supplied with OpenFOAM[®], "blockMesh", is employed to generate meshes. A typical computational mesh is shown in Fig. 2. Non-uniform meshes are adopted for saving the computational time. The fine meshes with higher resolution are used around the boxes, especially in the vicinity of the narrow gap. To capture the interface between water and air, the meshes gradually become denser from the bottom and the atmosphere boundaries to the still water level.





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202 Fig. 2. Side view of typical meshes in the computational domain: (a) the meshes around the boxes;
203 (b) the meshes close to the gap inlet
204

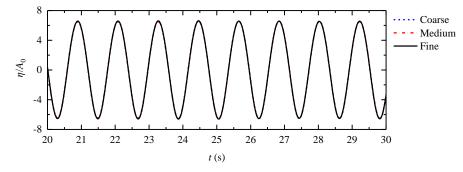


Fig. 3. Dependence of the free-surface elevation in the gap on the mesh resolution for the incident waves with kh=1.556 and $H_0=0.010$ m, in which $A_0=H_0/2$ denotes the amplitude of the incident waves.

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210 To examine the dependence of the numerical results on the mesh resolution, the free-surface response in the narrow gap is simulated using three different meshes, namely the coarse, medium 211 212 and fine meshes. The numbers of the cells for these three meshes are 143600, 224060 and 340880, 213 respectively. Based on the numerical results that will be shown in Section 4.1, the free-surface 214 resonance in the gap occurs at kh=1.556. Fig. 3 presents the resonant free surfaces inside the gap 215 induced by the incident waves with kh=1.556 and $H_0=0.010$ m. $A_0=H_0/2$ in this figure denotes the incident wave amplitude. It is seen that the time histories of the free-surface elevations for the three 216 217 mesh configurations are almost identical to each other. Meanwhile, considering that the medium 218 mesh can provide more accurate simulations of the wave fields excited by the incident waves with 219 higher frequencies as compared to the coarse mesh, in all our numerical simulations, the medium mesh configuration is employed. 220

221	For most of the simulations, a total time of 40.0 s is considered. However, to study the damping
222	time of the resonant free surface, for the five cases in which the incident wave frequency equals the
223	resonant frequency, a total time of 70.0 s is employed. The wave inlet boundary stops working after
224	40.0 s, and the numerical model continues to simulate the damping process. It can be seen from Fig.
225	3 that the free-surface elevation in the gap has already reached the steady state at $t=20.0$ s. All the
226	numerial results that will be presented in Section 4.1 and Sections 5.1–5.3 are based on the simulated
227	steady-state data from 20.0 s to 40.0 s. While in Section 5.4, the time histories of the free-surface
228	elevation in the gap between $0 - 20.0$ s and 40.0 s $- 70.0$ s are utilized to investigate the response
229	time and the damping time of gap resonance, respectively.

231 4. Numerical model validations

To guarantee the reliability of the model and the accuracy of the numerical results, the 232 numerical model and the numerical wave tank illustrated in Sections 2 and 3 are first validated by 233 comparing the present results obtained by OpenFOAM® with available experimental data and 234 numerical results in previous literatures. For the simulations with $H_0=0.024$ m described in Section 235 236 3, Saitoh et al. (2006) and Lu et al. (2011b) have measured the amplification of the free-surface elevation inside the gap and the wave forces on boxes by using physical experiments and a viscous 237 flow model, respectively. Comparisons of the present results with those in the two papers will be 238 239 presented in Section 4.1. Because the current research mainly focuses on the harmonic analysis of 240 the free-surface elevation in the gap and the wave loads on the boxes, it is essential to further examine the capability of the present model to predict the higher-order harmonic components of the 241 242 free-surface elevation or the wave loads. To the best of our knowledge, for the gap resonance 243 problem, the experimental data on the higher-order harmonic components of the free-surface 244 elevation or the wave loads are rare. However, Rodríguez et al. (2016) implemented physical 245 experiments on the interactions between regular waves and one fixed box, and the experimental data of the vertical wave force on the box (including the first- and second-order harmonic components) 246 247 were presented in that paper. The numerical reproduction for part of their experiments will be 248 implemented in Section 4.2.

249 4.1. Two-boxes condition

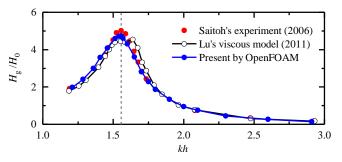


Fig. 4. Amplification of the free-surface elevation inside the narrow gap for the cases with H_0 =0.024 m, in which H_g denotes the wave height inside the narrow gap.

Fig. 4 illustrates the amplification of the free-surface elevation inside the narrow gap excited by the incident waves with $H_0=0.024$ m. It can be seen that the predicted resonant frequency, kh=1.556, by the present numerical model is almost identical to those obtained by both the laboratory tests of Saitoh et al. (2006) and the CFD results of Lu et al. (2011b). Besides, in general, the variation of H_e/H_0 with respect to kh also agrees well with their results. Fig. 5 further presents the comparisons of the horizontal and vertical wave forces on Boxes A and B predicted by OpenFOAM® and those by the CFD results in Lu et al. (2011b). Similar to Fig. 4, the overall agreement between the present results and those in Lu et al. (2011b) is also observed.

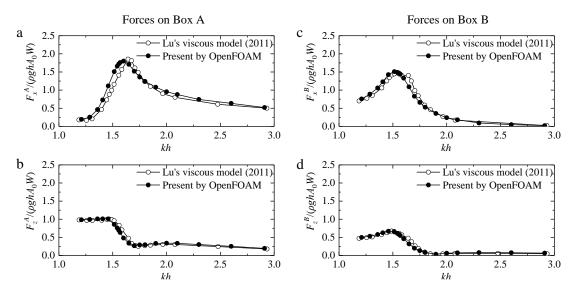


Fig. 5. Variations of the wave forces on the two boxes with respect to the incident wave frequency.(a) and (b) correspond to the horizontal and vertical forces on Box A, respectively; (c) and (d) correspond to the horizontal and vertical forces on Box B, respectively.

269 Rodríguez et al. (2016) performed laboratory experiments in a 2.79 m wide and 63.00 m long 270 wave tank, and the water depth is h=1.25 m. A rectangular box was placed approximately in the center of the wave tank, at x=29 m, where x=0 defines the location of the wave-maker. Because the 271 experimental study sought to achieve 2D flow conditions, the width of the rectangular box was 272 273 chosen as 2.76m, leaving only a very small gap of 0.015 m to either of the tank's sidewalls. Single box geometry with the breadth B=0.50 m and the draught d=0.25 m. The regular incident waves 274 with $0.4 \le kB \le 2.4$ were considered. Two series of physical experiments were carried out with two 275 steepnesses of the incident waves $kA_0 = 0.05$ and 0.10. To examine the performance of the numerical 276 model for the strongly nonlinear wave conditions, the series of experiments with $kA_0 = 0.10$ are 277 reproduced by OpenFOAM[®] here. Considering that the box used in Rodríguez et al. (2016) has the 278 same breadth and draft with the two boxes shown in Fig. 1, a very similar numerical wave tank (not 279 280 shown in this paper for brevity) with that in Fig. 1 is employed to implement the present simulations. 281 Compared to the wave tank shown in Fig. 1, there only exist two main differences in the present wave tank. First, there is only a single box located in the middle of the present wave tank. Second, 282 283 the water depth is deepened from 0.50 m to 1.25 m. A mesh configuration that has a similar mesh 284 density with the medium mesh described in Section 3 is utilized. It should be noted that due to the relaxation zone deployed around the inlet and outlet boundaries, it is not necessary for the numerical 285 286 wave tank to set the same length, 63.00 m, as the physical wave tank, and the numerical tank with 287 a length of 18.5 m is already long enough.

Fig. 6 presents the simulated and experimental time-histories of the non-dimensional vertical wave force, $F_z(t)/(0.5\rho gA_0 BW)$, for three cases with kB=0.8, 1.4, and 2.0. It can be obviously seen that significant nonlinearities are present, particularly for kB=1.4 and 2.0, due to the vertical asymmetry of the force traces. Overall, the agreement between the present numerical results and the experimental data is good. Fig. 7 further quantitatively compares the first- and second-order harmonic components of the experimental and numerical vertical forces for all cases with $kA_0=0.10$. Good agreement between the experimental and numerical results is also observed.

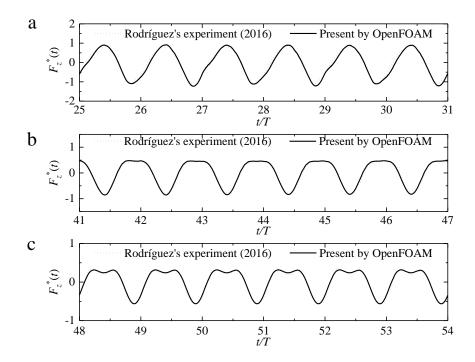
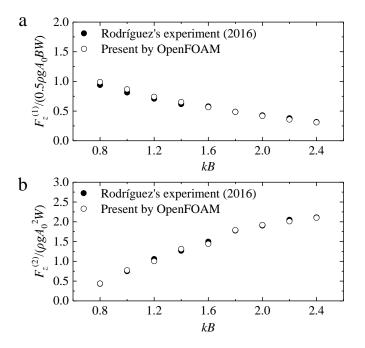




Fig. 6. Time histories of the vertical wave forces excited by the regular waves with $kA_0=0.10$ and (a) kB=0.8, (b) kB=1.4 and (c) kB=2.0, in which $F_z^*(t) = F_z(t)/(0.5\rho gA_0 BW)$ denotes the time history of the non-dimensional vertical wave forces.



300

Fig. 7. Non-dimensional (a) first-order and (b) second-order vertical wave forces excited by the

- incident regular waves with $kA_0=0.10$
- 303
- 304

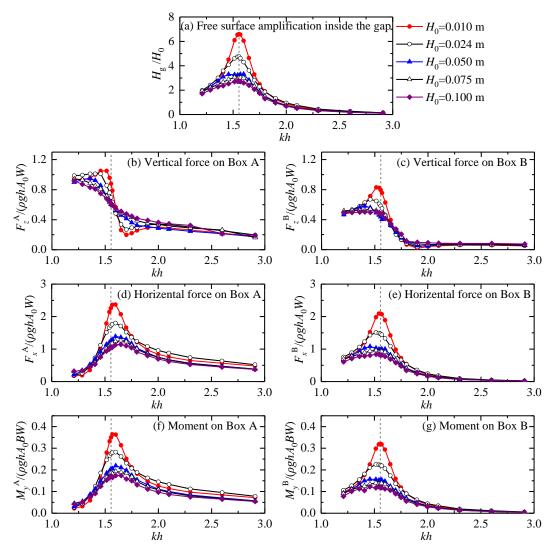
5. Numerical results and discussion

In order to present an overall impression of the hydrodynamic characteristics of gap resonance 306 307 under the conditions of various incident wave heights on the reader, the variations of the overall wave height amplification in the narrow gap and the overall wave loads on boxes with respect to the 308 incident wave frequency are first illustrated and discussed in Section 5.1. Subsequently, to find out 309 310 the relative importance of different harmonic components, the first three order harmonic 311 components of the free-surface elevation in the narrow gap and the wave loads on boxes are 312 analyzed in Section 5.2. Then, to better explain some phenomena presented in Sections 5.1 and 5.2 and better understand the mechanism essence of gap resonance, the variations of the reflection, 313 314 transmission and energy loss coefficients with respect to the frequency of the incident waves with various wave heights are discussed in Section 5.3. Finally, considering the importance of the fast 315 and accurate estimation of the response time and the damping time of gap resonance, two different 316 317 estimation methods are proposed and verified in Section 5.4.

318

319 5.1 Overall wave height amplifications and overall wave loads

320 Fig. 8 shows the overall free-surface amplification in the narrow gap and the overall wave 321 forces and moments impacting on Boxes A and B excited by the incident regular waves with various wave heights. Four obvious phenomena can be easily seen. First, it is seen from Fig. 8a that the 322 323 resonant frequency seems not sensitive to the incident wave height. For the cases with $H_0=0.010$ m, 0.024 m and 0.100 m, all the three variation curves of the free-surface amplification with the 324 frequency present perfect single-peak shapes, and the maximum free-surface amplification in the 325 326 narrow gap always occurs at the resonant frequency, i.e., kh=1.556. However, for the cases with 327 $H_0=0.050$ m and 0.075 m, the two variation curves of the free-surface amplification do not show the 328 perfect single-peak shape. The two curves around the resonant frequency become flat, and the values of free-surface amplification at kh=1.556 are even slightly less than the ones at its both adjacent 329 sides. The reason for this phenomenon can be attributed to the almost invariable reflection 330 331 coefficients around the resonant frequency under the conditions of $H_0=0.050$ m and 0.075 m (it will 332 be shown in Section 5.3).



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Fig. 8. The overall free surface amplification in the gap and the overall wave forces and moments
on Boxes A and B induced by the incident regular waves with various wave heights. The vertical
dash line refers to the position of the resonant frequency.

338 Second, for the vertical wave forces on both the two boxes (Fig. 8b and c), there exist obvious deviations between the frequency at which the maximum vertical wave force appears and the 339 340 resonant frequency. However, there are some different features for the changing trends of the vertical wave forces on the two boxes. For Box A, the difference between the frequency at which the 341 maximum vertical wave force appears and the resonant frequency monotonously increases with the 342 incident wave height. Besides, the vertical wave forces excited by the incident wave with small 343 height tends to increase first, then sharply decrease, then slowly increase, and then slowly decrease 344 with the non-dimensional wavenumber, kh. However, with the increase of the incident wave height, 345

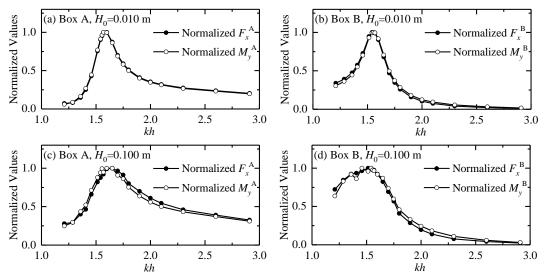
the vertical wave forces gradually become monotonic decrease with *kh*. For Box B, when the incident wave height is small, the changing trend of the vertical wave forces with *kh* is similar to that for Box A. When the incident wave height becomes large, the value of the vertical wave force seems insensible to the incident wave frequency at the ranges of kh < 1.5 and kh > 1.9, and its value only decreases sharply with the incident wave frequency at the range of 1.5 < kh < 1.9.

351 Third, for the horizontal wave forces on Box A (Fig. 8d), the frequency at which the maximum 352 horizontal force occurs is obviously larger than the resonant frequency; the larger the incident wave 353 height is, the more obvious the deviation becomes. While for the horizontal wave forces on Box B (Fig. 8e), the frequency at which the maximum horizontal force occurs is equal to or just slightly 354 355 less than the resonant frequency. It is due to the fact that the magnitude of the horizontal force is 356 determined by the free-surface elevation difference between the opposite sides of the each box (Lu et al., 2011b). The free-surface elevation at the left side of Box A is much larger than that at the right 357 358 side of Box B. It leads to that the free-surface elevation difference between the opposite sides of Box A is more different from the free-surface elevation in the gap, while the free-surface elevation 359 360 difference between the opposite sides of Box B is more close to the free-surface elevation in the gap. 361 As for the reason why the free-surface elevation at the left side of Box A is much larger than that at the right side of Box B, there are two main reasons: (1) the reflected wave height is always larger 362 than the transmitted wave height (i.e., $C_r > C_t$, which will be shown in Section 5.3), and (2) the left 363 364 side of Box A locates at a antinode of the partially standing waves composed of the incident and the reflected waves, which causes the wave height at the left side of Box A is approximately equal to 365 the summation of the incident and the reflected wave heights. 366

367 Fourth, for the moments on Boxes A and B (Fig. 8f and g), for all the incident wave heights considered in this paper, the variation curves of the moment on each box with the frequency is very 368 369 similar to those of the horizontal force on the corresponding box. Hence, the phenomena described above for the horizontal forces are also applicable for the moments. To further examine the 370 phenomenon that the variation curves of the moment on each box with the frequency are very similar 371 372 to those of the horizontal force on the corresponding box for all the incident wave heights studied 373 in this paper, Fig. 9 presents the comparisons of the normalized curves of the horizontal forces and the moments on Boxes A and B for $H_0=0.010$ m and 0.100 m. The normalized curve refers to the 374 original variation curve divided by the corresponding peak value of the original variation curve. 375

Hence, the normalized curve always has a maximum value, 1.0. It can be seen that for both the two boxes and for both the two incident wave heights, the normalized curves of the horizontal wave forces are almost identical to those of the moments. For the other three incident wave heights (i.e., $H_0=0.024$ m, 0.050 m and 0.075 m), the similar phenomenon can also be clearly observed (their comparisons are not shown in the paper for brevity).

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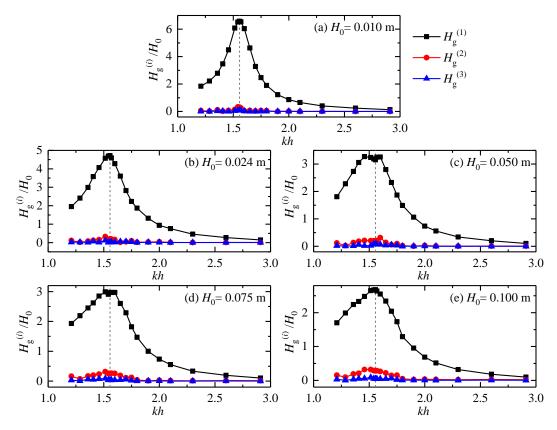
Fig. 9. Comparisons of the normalized curves of the horizontal wave forces and the moments onBoxes A and B

385 5.2 Harmonic analyses of wave height amplifications and wave loads

386 Fig. 10 illustrates the variation of the first three order harmonic components of the free-surface 387 elevation in the gap with respect to the frequency under the conditions of various incident wave heights. $H_g^{(i)}$ (*i*=1, 2 and 3) in the figure denotes the *i*th-order harmonic component of the free-surface 388 elevation in the gap. The following three phenomena can be easily observed. First, the first-order 389 390 component of the free-surface elevation is significantly larger than the second- and third-order 391 components. Second, around the resonant frequency, the second-order component is larger than the 392 corresponding third-order one; the larger the incident wave height is, the more obvious the phenomenon becomes. Third, all the first three order harmonic components around the resonant 393 394 frequency are remarkably larger than the corresponding ones for the non-resonant conditions.

To quantify the relative importance of higher-order components to the first-order component, Fig. 11 further shows the ratios of the second- and third-order harmonic components to the firstorder harmonic components for the free-surface elevation in the gap under the conditions of various

398 incident wave heights. It is seen that at the range of 1.3 < kh < 1.9, there existing obvious peak points 399 around the resonant frequency for both the second- and third-order harmonic components. For the second-order harmonic components, the maximum of their ratios to the first-order harmonic 400 401 components reaches up to about 13%. It can be attributed to the fact that the free-surface elevation around the resonant frequency is remarkably amplified, and naturally the higher-order harmonic 402 components of the free-surface elevation are enhanced due to the wave nonlinearity. While at the 403 ranges of kh < 1.3 and kh > 1.9, as the wave frequency becomes far from the resonant frequency, the 404 405 ratios of the second- and third-order components to the first-order components tend to gradually increase. It is mainly due to that the value of the first-order component significantly decreases as 406 the wave frequency becomes far from the resonant frequency, especially for the high-frequency 407 408 range (i.e., *kh*>1.9).





410 Fig. 10. The first three order harmonic components of the free-surface elevation in the gap under411 the conditions of various incident wave heights

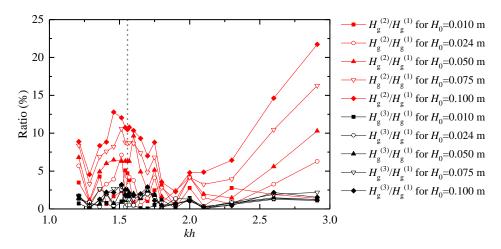
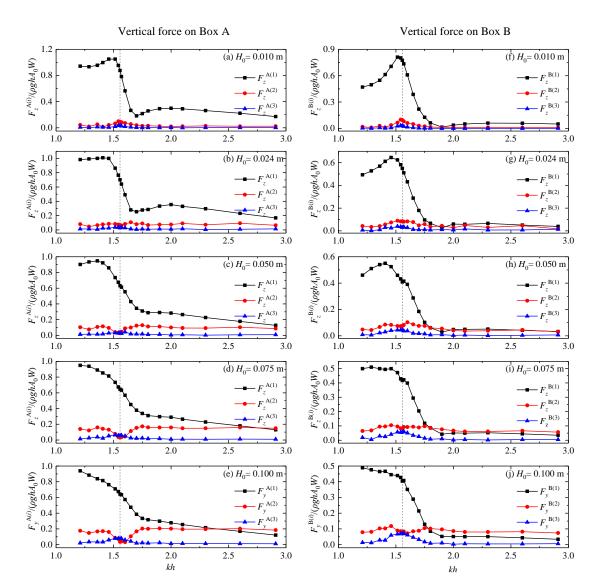


Fig. 11. Ratios of the second- and third-order harmonic components to the first-order harmonic
components for the free-surface elevation in the gap under the conditions of various incident wave
heights

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Fig. 12 illustrates the first three order harmonic components of the vertical wave forces on 417 Boxes A and B for all the simulations. $F_z^{A(i)}$ and $F_z^{B(i)}$ (*i*=1, 2 and 3) in this figure refer to the *i*th-418 order harmonic components of the vertical wave forces on Boxes A and B, respectively. The 419 420 following three phenomena can be easily seen. First, the first-order harmonic components of the 421 vertical wave force are much larger than the higher-order components near the resonant frequency. 422 Second, when the incident wave height is small (Fig. 12a and f), the second-order harmonic component is obviously larger than the third-order ones around the resonant frequency. As the 423 424 incident wave height increases, the third-order harmonic components around the resonant frequency gradually become obviously larger than those far away from the resonant frequency; on the contrary, 425 the second-order harmonic components around the resonant frequency become smaller and smaller 426 427 compared with those far away from the resonant frequency. When the incident wave height increases up to $H_0=0.100$ m (Fig. 12e and j), the third-order harmonic components have approached (for Box 428 429 B) or even exceeded (for Box A) the second-order ones. Third, for the high-frequency range, because the first-order harmonic components decease sharply with the wave frequency, the second-430 order harmonic components approach and even exceed the corresponding first-order ones for both 431 the two boxes. 432

Fig. 13 further shows the ratios of the second- and third-order harmonic components to the first-order harmonic components for the vertical wave forces on the two boxes for all the simulations. 435 It can be easily observed that for both the two boxes and for the wave frequency far away from the resonant frequency, the ratio of the second- to the first-order components is always larger than the 436 437 ratio of the third- to the first-order components, while around the resonant frequency, the latter approaches or even exceeds the former. Besides, for the second-order components, their ratios near 438 the resonant frequency are less than those far from the resonant frequency. While for the third-order 439 components, their ratios near the resonant frequency tend to be larger than those far from the 440 resonant frequency (it is valid for the whole frequency range considered in this paper for Box A, 441 442 and for *kh*<1.800 for Box B).



444

445 Fig. 12. The first three order harmonic components of the vertical wave forces on Boxes A and B446 under the conditions of various incident wave heights.

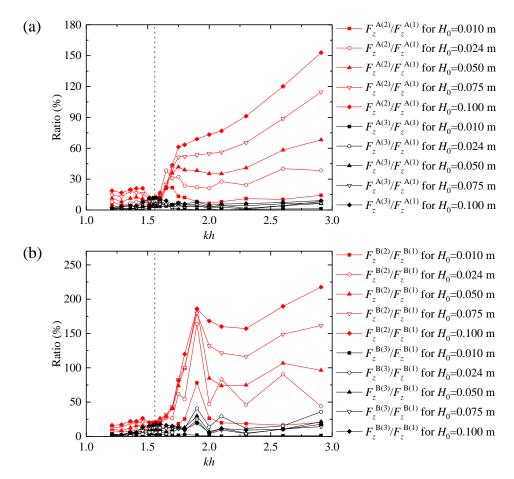


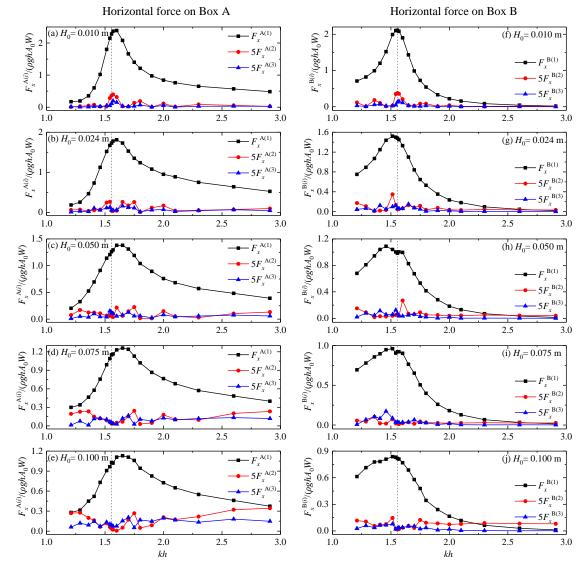
Fig. 13. Ratios of the second- and third-order harmonic components to the first-order harmonic
components for the vertical wave forces on (a) Box A and (b) Box B under the conditions of various
incident wave heights

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Fig. 14 presents the first three order harmonic components of the horizontal wave forces on 452 Boxes A and B for all the simulations. $F_x^{A(i)}$ and $F_x^{B(i)}$ (*i*=1, 2 and 3) in this figure refer to the *i*th-453 order harmonic components of the horizontal wave forces on Boxes A and B, respectively. Because 454 both the second- and third-order harmonic components of the horizontal wave forces around the 455 resonant frequency are extremely small compared to the corresponding first-order components, in 456 order to better show the variations of all these three harmonic components with the incident wave 457 frequency, the values of both the second- and third-order harmonic components shown in this figure 458 are enlarged five times. In general, the above three phenomena for the vertical wave forces shown 459 460 in Fig. 12 can also be observed in this figure.

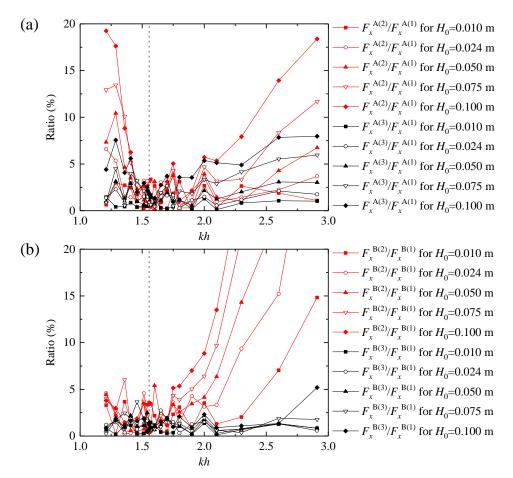
Fig. 15 further presents the ratios of the second- and third-order harmonic components to the first-order harmonic components for the horizontal wave forces on the two boxes for all the simulations. It should be noted that, for Box B (Fig. 15b), when kh=2.910 and $H_0=0.100$ m, the value of $F_x^{B(2)} / F_x^{B(1)}$ has already exceeded 140%. However, to better show the variation characteristics of the ratios around the resonant frequency, the maximum changing range of the *y*axis is only set to 20%. Again, in general, all the phenomena for the vertical wave forces presented in Fig. 13 can also be observed in this figure, except that the ratios of the third- to the first-order components near the resonant frequency shown in this figure tend to be smaller than those far from the resonant frequency.

470



471

Fig. 14. The first three order harmonic components of the horizontal wave forces on Boxes A andB under the conditions of various incident wave heights.



476 Fig. 15. Ratios of the second- and third-order harmonic components to the first-order harmonic
477 components for the horizontal wave forces on (a) Box A and (b) Box B under the conditions of
478 various incident wave heights

Fig. 16 presents the first three order harmonic components of the moments on Boxes A and B 491 for all the simulations, in which $M_y^{A(i)}$ and $M_y^{B(i)}$ (*i*=1, 2 and 3) refer to the *i*th-order harmonic 492 493 components of the moments on Boxes A and B, respectively. It is obviously seen that when the incident wave height is small (refer to Fig. 16a and f), both the second- and third-order harmonic 494 components are much smaller than the corresponding first-order ones around the resonant frequency 495 for both the two boxes. However, as the incident wave height increases, the values of the second-496 order harmonic components around the resonant frequency gradually increase. Compared to the 497 498 first-order harmonic components, the second-order harmonic components have reached a considerable values when $H_0=0.100$ m (refer to Fig. 16e and j). To better illustrate this point, the 499 ratios of the second- and third-order harmonic components to the first-order harmonic components 500 501 for the moments on both the two boxes under the conditions of various incident wave heights are presented in Fig. 17. It can be seen that when the incident wave height is small (i.e., $H_0=0.010$ m), 502 both the values of $M_y^{A(2)} / M_y^{A(1)}$ and $M_y^{B(2)} / M_y^{B(1)}$ are approximately 5%. However, when the 503 incident wave height increases to $H_0=0.100$ m, both their values reach up to near 20%. 504

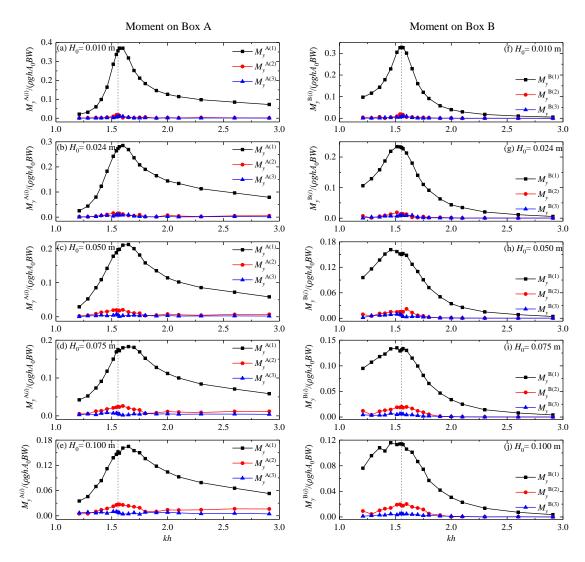
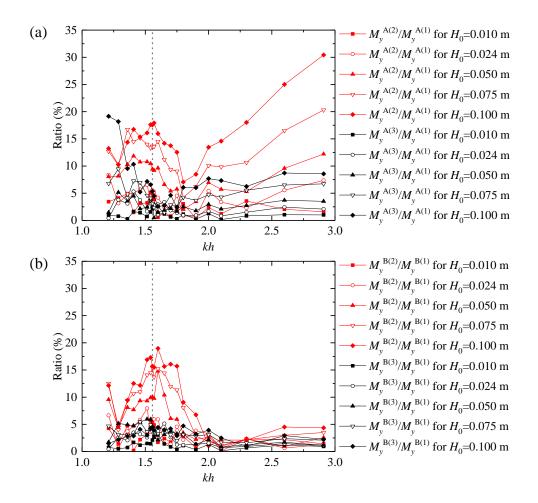


Fig. 16. The first three order harmonic components of the moments on Boxes A and B under theconditions of various incident wave heights.



510

Fig. 17. Ratios of the second- and third-order harmonic components to the first-order harmonic
components for the moments on (a) Box A and (b) Box B under the conditions of various incident
wave heights

515 5.3 Reflection, transmission and energy loss coefficients

Based on the wave analysis technique in Goda and Suzuki (1976), the wave height of the 516 517 reflected waves from the two-box system can be obtained by using the free-surface elevations at G_1 and G_2 (refer to Fig. 1). The reflection coefficient C_r is further calculated as the ratio of the reflected 518 wave height to the incident wave height H_0 . The transmission coefficient C_t is defined as the ratio 519 of the transmitted wave height to H_0 , and the transmitted wave height can be obtained by the free-520 surface elevation at G₄. Then, the energy loss coefficient $L_e = 1 - C_r^2 - C_t^2$ is calculated. The effects 521 of the incident wave height on the reflection, transmission and energy loss coefficients, C_r , C_t and 522 L_e , are illustrated in Fig. 18. For the reflection coefficient (Fig. 18a), the following three phenomena 523 can be easily observed. First, the reflection coefficients C_r near the resonant frequency are always 524

less than those away from the resonant frequency. Second, the reflection coefficient at the resonant frequency increases with the increasing of the incident wave height. Third, under the conditions of $H_0=0.050$ m and 0.075 m, both the two variation curves of the reflection coefficient around the resonant frequency almost become flat, which indicates that the similar wave energy can propagate into the gap. Hence, this leads to the relatively flat variation curves of H_g/H_0 around the resonant frequency for $H_0=0.050$ m and 0.075 m shown in Fig. 8a.

531 For the transmission coefficient (Fig. 18b), the frequency at which the maximum transmission 532 coefficient C_t occurs is always less than the resonant frequency. The larger the incident wave height 533 is, the more obvious their difference becomes. When the incident wave height is small, the 534 transmission coefficient first increases, then sharply decreases, then slowly increases, and then slowly decreases with the non-dimensional wavenumber, kh. However, with the increase of the 535 incident wave height, the vertical wave forces gradually become monotonic decrease with kh. These 536 537 effects of the incident wave height on the variation characteristics of the transmission coefficient are very similar to its effects on those of the vertical wave forces on Boxes A and B (see Fig. 8b and 538 c). 539

540 By carefully comparing Fig. 18a and b, it can be found that for all the incident wave heights 541 considered in this paper, the reflection coefficients are always larger than the transmission coefficient, no matter whether the gap resonance occurs or not. The larger the incident wave height 542 543 is, the more obvious the difference between C_r and C_t becomes. This explains that phenomenon shown in Fig. 8d and e that for the horizontal wave forces on Box A, the frequency at which the 544 maximum horizontal force occurs obviously deviates from the resonant frequency; while for the 545 546 horizontal wave forces on Box B, the frequency at which the maximum horizontal force occurs is 547 approximately equal to the resonant frequency.

For the energy loss coefficient (Fig. 18c), it is seen that for all the incident wave heights considered in this paper, almost all the maximum energy loss coefficients appear at (or very close to) the resonant frequency. Besides, with the increase of the incident wave height, the energy loss coefficient at the resonant frequency becomes smaller and smaller. It should be noted that, intuitively, this finding seems to be incompatible with that phenomenon shown in Fig. 8a that larger incident wave height leads to smaller amplification of the free-surface elevation in the gap. In fact, these two findings are compatible with each other. The reason lies on that the increase of the incident wave height tends to remarkably augment the reflection coefficient at the resonant frequency, and hence
relatively less wave energy can propagate into the gap. Therefore, less energy dissipation and
smaller free-surface amplification in the narrow gap can be observed at the resonant frequency,
which agrees with the related findings in Jiang et al. (2018).

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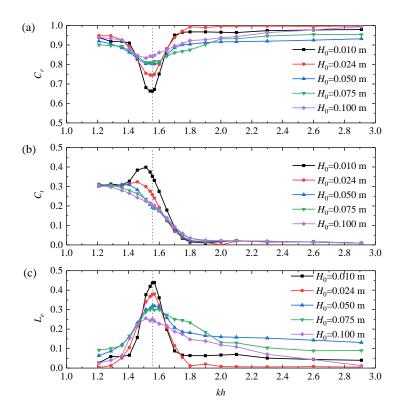
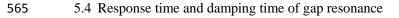




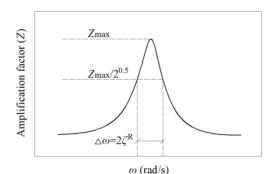
Fig. 18. Variations of (a) the reflection coefficient, (b) the transmission coefficient and (c) the energy
loss coefficient with respect to the wave frequency under the conditions of various incident wave
heights

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In practical engineering applications, the fast and accurate estimation of the response time and the damping time is crucial for the safe evacuation of staff and the reasonable arrangement of operation time during the offloading operations from FPSO platforms to a shuttle tanker under gap resonance conditions. In this section, a general method is proposed for accurately estimating both the response time and the damping time of free-surface elevation in the gap under resonance. The general method is based on fitting the envelope of the free-surface elevation. For the evaluation of the response time, there is an alternative method which is based on the amplification curve of the







587

Fig. 19. Generic amplification curve; $\Delta \omega$ is the half-power spectral bandwidth

These methods are inspired by Bellotti (2007) and Dong et al. (2010) who investigated the 578 response time and the damping time of the harbor to long waves under the condition of harbor 579 580 resonance. In order to facilitate the understanding of the reader, the basic principle of these methods is briefly explained here. To illustrate the basic principle, Fig. 19 shows a generic amplification 581 curve, in which Z is the amplification factor. The free-surface elevation in the narrow gap can be 582 considered as typical of a 1D system like a mass-spring system, moving along a line, connected to 583 584 a damper, forced by a periodically unit force. If the considered mass starts from rest (i.e., from the position z=0), when the frequency of the force equals the natural frequency of the system, its position 585 along the axis (z) can be formulated as 586

$$z = Z_{\max} \cos\left(-\omega \cdot t^*\right) \left(1 - e^{-\zeta^{\mathcal{R}} \cdot t^*}\right),\tag{7}$$

588 in which ζ^{R} is a parameter governing the response time of the resonator, Z_{max} is the maximum 589 amplification factor and t^{*} denotes the relative time with respect to the moment that the mass just 590 begins to move from rest. It requires infinite time for the fluctuation to reach its maximum, following 591 Eq. (7). The time $t^{*}_{\alpha\%}$ needed for the waves to reach $\alpha\%$ of the maximum can be formulated as

592 $t^*_{\alpha\%} = -\frac{\ln(1-\alpha\%)}{\zeta^{\mathsf{R}}}.$ (8)

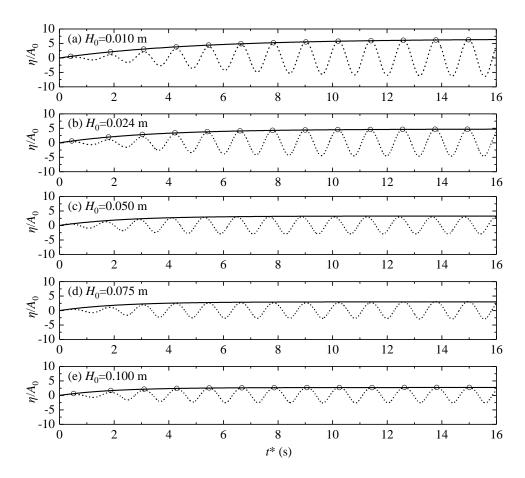
Similarity, if the mass damps from the steady-state maximum to the rest state, its position can beexpressed as

595 $z = Z_{\max} \cos(-\omega \cdot \tau) e^{-\zeta^{D} \cdot \tau} , \qquad (9)$

596 where ζ^{D} is a parameter controlling the damping time of the resonator and τ denotes the relative 597 time with respect to the moment that the mass just begins to damp from the steady-state maximum. 598 The time $\tau_{\beta\%}$ needed by the wave to decrease to $\beta\%$ of the maximum can be expressed as

$$\tau_{\beta\%} = -\frac{\ln(\beta\%)}{\zeta^{\rm D}} \,. \tag{10}$$

600 It can be found from Eqs. (8) and (10) that the key step to quantitatively evaluate the response time and the damping time lies on how to find the values of ζ^{R} and ζ^{D} . A general method to obtain 601 their values is to directly fit the measured (or simulated) envelopes of the displacement of the mass 602 603 with the theoretical ones formulated by Eqs. (7) and (9). It can be demonstrated that for 1D resonators, the value of ζ^{R} can also be evaluated from the amplification curve. More specifically, 604 $\zeta^{R} = \Delta \omega / 2$, in which $\Delta \omega$ is the half-power spectral bandwidth (i.e., the width of the part of the 605 amplification curve with values larger than Z_{max} / 2^{0.5}). Identical to Bellotti (2007) and Dong et al. 606 (2010), $t^*_{95\%}$ and $\tau_{5\%}$ are selected in this article to represent the response time and the damping 607 608 time of the resonant free-surface elevations, respectively.



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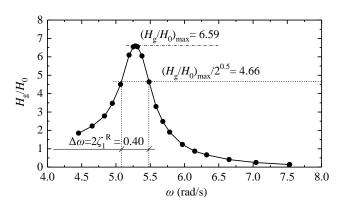
Fig. 20. The response process of the free-surface elevation (η/A_0) in the narrow gap excited by the incident regular waves with the resonant frequency (i.e., kh=1.556, or equivalently $\omega=5.285$ rad/s) and various heights. Dashed lines denote the time histories of the simulated free-surface elevations

613 obtain by the numerical model. Solid lines refer to the fitted envelope of η/A_0 obtained by directly 614 fitting the simulated envelopes with the theoretical ones formulated by Eq. (7). Small circles 615 represent the envelope of η/A_0 as obtained by Eq. (7) using the amplification curve method for 616 estimating ζ^{R} .

617

618 Fig. 20 shows the time histories of the free-surface elevations in the narrow gap, obtained by using the time-resolving numerical model, from the calm to the steady state. The frequency of all 619 620 the incident regular waves corresponds to the resonant frequency (i.e., kh=1.556, or equivalently 621 ω =5.285 rad/s). By directly fitting the simulated envelopes with the theoretical ones formulated by Eq. (7), the numerical values of ζ^{R} can be obtained. Besides, by measuring the half-power spectral 622 bandwidth of the amplification curve as shown in Fig. 19, the values of ζ^{R} can also be calculated. It 623 is noted here that, to facilitate comparing the values of ζ^{R} obtained by these two different methods, 624 two different symbols, ζ_1^R and ζ_2^R , are used separately to represent the values of ζ^R obtained by the 625 amplification curve method and by the direct envelope-fitting method in the following. As a 626 concrete example of employing the amplification curve method to evaluate the value of ζ_1^R , Fig. 21 627 illustrates the amplification curve of the free-surface elevation in the narrow gap under the condition 628 of $H_0=0.010$ m. It can be seen that the value of ζ_1^R under the condition of $H_0=0.010$ m is equal to 629 630 0.20.

631



632

Fig. 21. Amplification curve of the free-surface elevation in the narrow gap under the condition of $H_0=0.010 \text{ m}$

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Table 1 further lists all the values of ζ_1^R and ζ_2^R , their relative percentage errors, *Err*, and

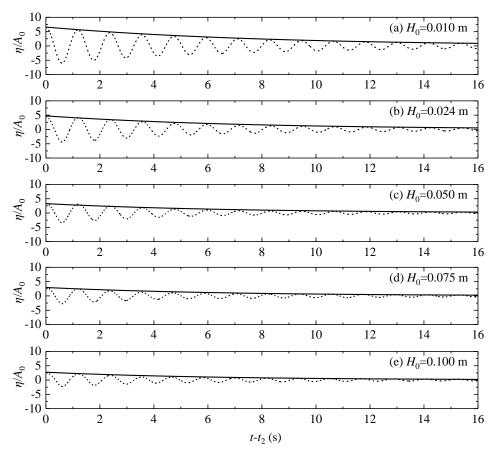
636 the response time, $t_{95\%}^*$ for the free-surface elevations shown in Fig. 20. The response time, $t_{95\%}^*$, in this table is calculated by employing Eq. (8) and the value of ζ_2^R . As mentioned in Section 5.1, 637 unlike the typical amplification curves shown in Figs. 19 and 21, the two free-surface amplification 638 curves for $H_0=0.050$ m and 0.075 m do not present the perfect single-peak shape; the two curves 639 around the resonant frequency become flat, and the values of the amplification factor at kh=1.556640 641 are even slightly less than the ones at its both adjacent sides (refer to Fig. 8a). Hence, the values of ζ_1^R for H₀=0.050 m and 0.075 m are absent. For the other three wave heights, the relative 642 percentage errors between ζ_1^R and ζ_2^R are shown to be extremely small. Besides, observing Fig. 643 644 20 can easily find that for all the incident wave heights considered in this paper, both the two envelopes of the free-surface elevations obtained by ζ_1^R and ζ_2^R agree well with the corresponding 645 simulated free-surface elevations by using the time-resolving numerical model. These phenomena 646 indicate that both the two above-mentioned methods for evaluating the response time of gap 647 resonance are accurate and reliable. 648

649

Table 1. All the parameters related to the response time and the damping time of the resonant freesurface elevations shown in Figs. 20 and 22. *Err* denotes the relative percentage error between ζ_1^R and ζ_2^R . $t^*_{95\%}$ and $\tau_{5\%}$ refers to the response time and the damping time of the free-surface elevations, respectively. The evaluation of $t^*_{95\%}$ is based on Eq. (8) and the value of ζ_2^R .

1	$H_0(\mathbf{m})$	ζ_1^{R}	ζ_2^{R}	<i>Err</i> (%)	$t_{_{95\%}}^{*}(s)$	ζ^{D}	$ au_{5\%}\left(\mathbf{s} ight)$	$ au_{5\%}/t_{95\%}$
	0.010	0.200	0.202	0.99	14.83	0.125	23.97	1.62
	0.024	0.306	0.299	2.34	10.02	0.136	22.03	2.20
	0.050	-	0.421	-	7.12	0.145	20.66	2.91
	0.075	-	0.467	-	6.41	0.151	19.84	3.09
	0.100	0.512	0.499	2.60	6.00	0.158	18.96	3.16

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Fig. 22. The damping process of the free-surface elevation (η/A_0) in the narrow gap excited by the 658 incident regular waves with the resonant frequency (i.e., kh=1.556, or equivalently $\omega=5.285$ rad/s) and various heights. Dashed lines denote the time histories of the simulated free-surface elevations obtain by the numerical model. Solid lines represent the fitted envelope of η/A_0 obtained by directly fitting the simulated envelopes with the theoretical ones formulated by Eq. (9).

662

Fig. 22 illustrates the time histories of the simulated free-surface elevations in the narrow gap 663 and their fitted envelopes obtained by directly fitting the simulated envelopes with the theoretical 664 ones formulated by Eq. (9) during their damping processes. It is seen that for all the incident wave 665 heights considered in this paper, Eq. (9) can describe the damping process of the resonant free-666 surface elevation in the gap very well. All the values of $\zeta^{\rm D}$ gained by the direct envelope-fitting 667 method and the damping time $\tau_{5\%}$ under the conditions of various wave heights are also presented 668 in Table 1. 669

670 According to the response time and the damping time presented in Table 1, the following two phenomena can be easily observed. First, for all the incident wave heights, the damping time is 671 always significantly larger than the corresponding response time. The ratio of the damping time to 672

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the response time gradually increases from 1.62 for H_0 =0.100 m to 3.16 for H_0 =0.100 m. This indicates that once the gap resonance is excited, it will persist for a rather long time. Second, both the response time and the damping time decrease with the incident wave height, and the decreasing degree of the response time is obviously larger than that of the damping time. The response time falls up to 60 % from H_0 =0.010 m to H_0 =0.100 m, while the damping time reduces only about 21%.

678

679 6. Conclusions

680 The CFD numerical model, OpenFOAM®, together with the wave generation toolbox "waves2Foam" proposed by Jacobsen et al. (2012), is adopted for investigating the hydrodynamic 681 682 behaviors of water resonance in a narrow gap formed by two side-by-side identical boxes excited by incident regular waves with various wave heights. The overall free-surface amplification in the 683 gap and the overall wave loads on the boxes are firstly presented. Then, the harmonic analyses of 684 685 free-surface elevation and wave loads are mainly investigated. Next, the reflection, transmission and energy loss coefficients of the two-box system are discussed. Finally, two different methods to 686 evaluate the response time and the damping time of gap resonance are proposed. The results of this 687 688 study have provided new insights of the hydrodynamic characteristics involved in the gap resonance. 689 The following conclusions can be drawn from the results of the present study:

(1) The frequencies at which the maximum vertical wave forces on both boxes and the maximum
horizontal wave force on Box A occur appear to obviously deviate from the resonant frequency,
and a larger incident wave height tends to cause more obvious differences between them. While
the frequency at which the maximum horizontal force on Box B occurs is equal or very close
to the resonant frequency.

695 (2) For the free-surface elevation in the gap and the moments on boxes, the ratios of their second696 order components to the corresponding first-order ones around the resonant frequency are
697 normally larger than those at the frequencies far from the resonant frequency (except those at
698 the very high frequency band). The larger the incident wave height is, the larger the ratios of
699 the second- to the first-order components around the resonant frequency becomes.

(3) For both the vertical and horizontal wave forces on both boxes, the ratios of their second- to the
 first-order components near the resonant frequency are less than those far away from the
 resonant frequency. Besides, when the incident wave height is small, their second-order

components are obviously larger than the corresponding third-order ones around the resonant
frequency. However, as the incident wave height increases, the third-order components around
the resonant frequency gradually approach and even exceed the second-order ones.

(4) Both the minimum reflection coefficient and the maximum energy loss coefficient always 706 appear at (or very close to) the resonant frequency, while the frequency at which the maximum 707 708 transmission coefficient appears is obvious less than the resonant frequency. The reflection 709 coefficient is always larger than the transmission coefficient, and the larger the incident wave 710 height is, the more obvious their difference becomes. Besides, the energy loss coefficient under the gap resonance condition gradually decreases with the increase of the incident wave height. 711 (5) Both the amplification curve method and the direct envelope-fitting method are able to 712 accurately evaluate the response time and the damping time of the resonant free-surface 713 714 elevation in the gap, and it is shown that the damping time is always significantly larger than 715 the corresponding response time. Besides, with the increase of the incident wave height, both 716 the response time and the damping time decrease, and the decreasing degree of the former is obviously larger than that of the latter. 717

Finally, we reaffirm here that these conclusions are only valid for the given geometric layout
(including the size and draft of the two boxes, the gap width and the water depth) and the ranges of
the incident wave height and the incident wave frequency studied in this paper.

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