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Parametric CFD Analysis to Study the Influence of Fin Geometry on the Performance of a Fin and Tube Heat Exchanger

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Abstract — Heat transfer and pressure loss characteristics of a fin and tube heat exchanger are numerically investigated based on parametric fin geometry. The cross-flow type heat exchanger with circular tubes and rectangular fin profile is selected as a reference design. The fin geometry is varied using a design aspect ratio as a variable parameter in a range of 0.1-1.0 to predict the impact on overall performance of the heat exchanger. In this paper, geometric profiles with a constant thickness of fin base are studied. Threedimensional, steady state CFD model is developed using commercially available Multiphysics software COMSOL v5.2. The numerical results are obtained for Reynolds number in a range from 5000 to 13000 and verified with the developed correlations. Dimensionless experimentally performance parameters such as Nusselt number, Euler number, efficiency index, and area-goodness factor are determined. The best performed geometric fin profile based on the higher heat transfer and lower pressure loss is predicted. The study provides insights into the impact of fin geometry on the heat transfer performance which help escalate the understanding of heat exchanger designing and manufacturing at a minimum cost.

Keywords — Fin and tube heat exchanger; numerical modelling; fin profile; conjugate heat transfer; turbulent flow; pressure loss.

I. INTRODUCTION

Fins are the extended surfaces used in heat exchangers to enhance the heat transfer rate between heat transfer surfaces and the flowing fluid [1]. The increment in the heat transfer performance through fin surfaces is widely employed in many industrial applications. Application of waste heat recovery systems has received tremendous attention during the last decade due to the resulting saving of primary fuel, increased energy efficiency and lower greenhouse gas emissions. Heat exchangers are one of the important components of these waste heat recovery systems. During past few years, H-type finned and tube heat exchangers have been studied both experimentally [2-4] and numerically [5-7]. The studies mainly focused on examining the heat transfer and flow resistance characteristics for a reference design of the H-type finned tube bundles. In addition, combined heat and mass transfer analysis on H-type design with three types of finned tube namely-dimple finned tube, longitudinal vortex generators (LVGs) finned tube, and finned tube with compound dimples and LVGs together was conducted [8, 9].

The implementation of fins on the primary heat surface enhances the complexity, volume and weight which make the design and construction of fin surfaces of vital importance in heat exchanger applications. Very limited research on different fin types or geometry profiles is available due to restricted experimental conditions and numerical challenges. This limitation overshadows the current knowledge of design factors that has an influence on the heat transfer and pressure loss characteristics. Hence, it becomes imperative to study the different fin geometric profiles in order to determine the optimal fin design for a given H-type fin and tube heat exchanger application.

In this paper, we used Computational Fluid Dynamics (CFD) to obtain the solution of governing equations of physical phenomena in a cross-flow type fin and tube heat exchanger. The parametric study of fin geometry is conducted using air as a working fluid considering the 'rectangular' fin as reference geometric profile. Heat transfer and pressure loss characteristics in a fin and tube heat exchanger with different geometric fin profiles are predicted and compared with the reference fin profile geometry.

II. NUMERICAL MODEL DEVELOPMENT

A. Heat exchanger geometry

The heat exchanger used in the present study is fin and tube type. The design entails circular tubes and rectangular fins which are attached to the set of two tubes with a fixed gap in between. This particular design is also called 'Htype' finned tube heat exchanger due to the typical arrangement of fins on tubes resembling the letter 'H'. An orderly arrangement of the single unit results in the complete heat exchanger configuration which can be scaled for desired applications based on the heat transfer rate and allowable pressure loss. Fig. 1 shows the pictorial view of fin and tube heat exchanger configuration used in the present study. The design typically used in waste heat recovery applications such as marine boilers, where hot exhaust gas flows over the finned tube bundle and cold water flows inside the tubes as can be seen in Fig.1. The heat transfers from hot exhaust gases, by convection through fins and conduction within fin and tube thickness, to the water inside the tubes for steam generation for other application purposes

B. Computational geometry

The geometry of the fin and tube heat exchanger simulated in the present study is shown in Fig. 2. In order to save the computational effort, the geometry to be studied is reduced to one-half of the single unit.

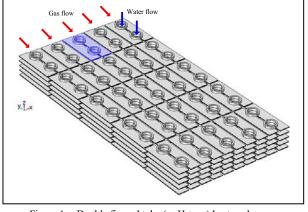


Figure 1. Double fin and tube (or H-type) heat exchanger configuration.

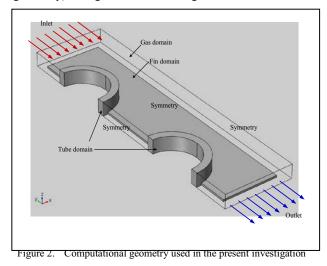
The computational geometry is divided into three domains- fin, tube and gas; and boundaries- inlet, outlet, and symmetry. The geometric dimensions of the heat exchanger design are given in Table I.

C. Formulation of the fin geometric profile

In the present work, the geometry of the fin is varied using aspect ratio (α) as a profile parameter which is defined as the ratio of thickness of fin tip (δ_{fi}) to the thickness of fin base (δ_{fb}) and can be expressed as-

$$\alpha = \frac{\delta_{fi}}{\delta_{fb,r}} \tag{1}$$

In order to simplify the analysis and geometric complexity, rectangular geometry of the fin is considered as a reference geometric profile and the thickness of fin base is kept constant as of reference rectangular fin $(\delta_{fb,r})$ while the thickness of the fin tip is subjected to a variation (Fig. 3). The aspect ratio is varied in a range α =1.0- 0.1 transforming the reference rectangular fin profile (at α =1.0) into the trapezoidal profile (at α =0.7, 0.5, 0.3) which eventually resembles a triangular profile (at α =0.1). With the change in aspect ratio, total heat transfer area, the thermal contact area between the fin and tubes and, the weight of the heat exchanger unit (computational geometry) changes as shown in Fig. 4.



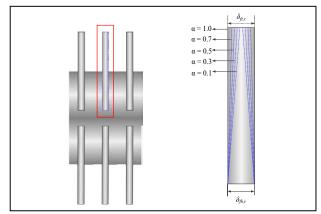


Figure 3. Schematic view of reference rectangular fin (on left) and different fin geometric profiles (on right) investigated in the present study

TABLE I. DESIGN PARAMETERS AND OPERATING CONDITIONS FOR A SINGLE UNIT OF THE EXCHANGER

Parameter	Symbol	Value	Unit
Length of the fin	L_f	0.145	m
Width of the fin	W_f	0.070	m
Thickness of the reference fin base	$\delta_{fb,r}$	0.002	m
Thickness of the reference fin tip	$\delta_{\mathit{ft,r}}$	0.002	m
Width of the gap between fins	δ_a	0.007	m
Inner diameter of the tube	D_i	0.030	m
Outer diameter of the tube	D_o	0.038	m
Tube pitch	p_t	0.077	m
Length of the gas domain	L_g	0.155	m
Width of the gas domain	W_{g}	0.080	m
Fin pitch	p_f	0.015	m
Temperature at gas inlet	T_{in}	573.15	Κ
Pressure at gas outlet	p_{out}	0.0	Ра
Temperature of inner tube wall	T_w	453.15	Κ

D. Governing equations

3D CFD model is developed using commercially available Multiphysics software COMSOL v5.2. Following assumptions are made in the present model-

- Steady state flow and heat transfer
- Incompressible flow
- Negligible thermal contact resistance

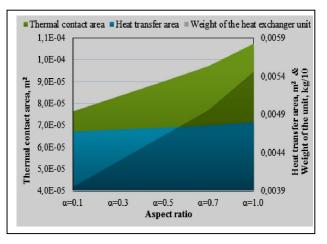


Figure 4. Variation of geometric profile parameters with respect to the aspect ratio of the fin

- Temperature dependent fluid property
- Constant inner tube wall temperature
- No periodic boundary condition (i.e. model is valid for the first unit of the heat exchanger as shown in Fig.1).

The mass and momentum balance for flow in the gas domain and energy balance in terms of heat transfer are given as-

 $\rho C_p \mathbf{u} \cdot \nabla T + \nabla \cdot \mathbf{q} = \mathbf{Q}$

 $\mathbf{q} = -k\nabla T$

$$\nabla \cdot \mathbf{u} = 0 \tag{2}$$

(4)

$$\rho(\mathbf{u} \cdot \nabla)\mathbf{u} = \nabla \cdot [-p\mathbf{I} + \mu(\nabla \mathbf{u} + (\nabla \mathbf{u})^T)] + \mathbf{F}$$
(3)

where,

Based on the mass flow rate and the heat exchanger configuration, Shear Stress Transport (SST) model is adopted. The governing equations of two-equation SST model are formulated in terms of k and ω as [10]-

$$\rho \frac{\partial k}{\partial t} + \rho \mathbf{u} \cdot \nabla k = P - \rho \beta_o k \omega + \nabla \cdot ((\mu + \sigma_k \mu_T) \nabla k)$$
(5)

$$\rho \frac{\partial \omega}{\partial t} + \rho \mathbf{u} \cdot \nabla \omega = \frac{\rho \gamma}{\mu_T} P - \rho \beta \omega^2 + \nabla \cdot ((\mu + \sigma_\omega \mu_T) \nabla \omega) +$$
(6)

$$2(1-f_{v1})\frac{\rho\sigma_{\omega 2}}{\omega}\nabla\omega\cdot\nabla k$$

The default model parameters used to solve the governing equations are defined in the Appendix. Table II lists initial conditions for a steady state simulation [11] and boundary conditions used to numerically solve the computational model and achieving preliminary results.

III. MODEL VALIDATION

A. Experimental validation

The validation of numerical results is performed using the experimentally developed correlations by Chen et al. [4] and a comparison is shown in Fig. 5. Correlations for Nusselt number and Euler number given by (7) and (8) are valid for Reynolds number range of 5000-18000 with a relative error of 2.79% and 3.70%, respectively. The average percent deviation of numerically predicted Nusselt and Euler numbers from the correlation values is calculated to be 5.61% and 5.72%, respectively. The deviation accounts for the assumptions in the present study or and the experimental errors in developing the correlations.

 TABLE II.
 Design Parameters and Operating Conditions for a Single Unit of the Exchanger

Initial	Condition	
Gas domain	$\mathbf{u} = 0 \ ; \ p = 0 \ ; \ k = \left(\frac{10 \cdot \mu}{\rho(0.1 \cdot l_{rof})}\right)^2 \ ; \ \varepsilon = \frac{C_{\mu} k_{init}^{3/2}}{0.1 \cdot l_{rof}} \ ; \ \omega_{init} = \frac{\sqrt{k_{init}}}{0.1 \cdot l_{rof}}$	
All domains	T = 298.15 K	
Boundary	Condition	
Inlet	$T = T_{in}; \ u = 0, v = -u_{in}, w = 0$	
Wall	$\mathbf{u} \cdot \mathbf{n} = 0; \nabla k_e \cdot \mathbf{n} = 0; \ \varepsilon = \frac{C_{\mu}^{3/4} k_e^{3/2}}{\kappa_v \delta_w}$	
Inner tube wall	$T = T_w$	
Outlet	$p = p_{out}, -\mathbf{n} \cdot \mathbf{q} = 0$; $\nabla k_e \cdot \mathbf{n} = 0$; $\nabla \varepsilon \cdot \mathbf{n} = 0$	
Symmetry	$\mathbf{u} \cdot \mathbf{n} = 0 ; \ -\mathbf{n} \cdot \mathbf{q} = 0 ; \ \nabla k_e \cdot \mathbf{n} = 0 ; \ \nabla \varepsilon \cdot \mathbf{n} = 0$	

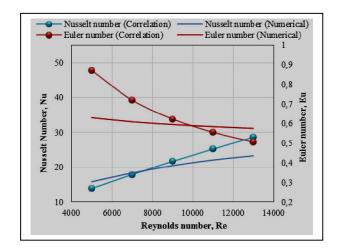


Figure 5. Comparison of numerical and correlation results

These deviations are in acceptable range and hence, the results are assumed accurate enough to predict the physical behavior.

$$Nu = 0.053Re^{0.756} \left(\frac{D_o}{P_f}\right)^{-0.212} \left(\frac{L_f}{P_f}\right)^{-0.294} \left(\frac{W_f}{P_f}\right)^{0.155}$$
(7)
$$Eu = 19.14Re^{-0.57} \left(\frac{L_f}{D_o}\right)^{1.32}$$
(8)

B. Mesh independence test

Mesh independence test is made on the reference fin using temperature difference across the gas domain as an objective property. Five different meshes with 375860, 657449, 997272, 1716992 and 2130500 elements are used in the simulation. The test result suggests the mesh with 1716992 elements as a good choice in relation to accuracy and computational time.

IV. RESULTS AND DISCUSSION

The results predicted from the present study are discussed in this section. Table III expresses the dimensionless parameters used to evaluate the performance of the heat exchanger design. The Nusselt number and Euler number are used to assess the heat transfer and pressure loss characteristics of the heat exchanger with different fin geometric profile.

TABLE III. PERFORMANCE PARAMETERS

Performance parameter	Expression
Nusselt number, Nu	$\frac{hD_o}{k}$
Euler number, Eu	$\frac{\Delta p}{\frac{1}{2}\rho_g u_{\max}^2}$
Efficiency index, η	$\frac{Nu}{\left(\frac{\Delta p}{\frac{1}{2}\rho_g u_{in}^2}\right)}$
Area-goodness factor, j/f	$\frac{\left(\frac{Nu}{RePr^{\frac{1}{3}}}\right)}{\left(\frac{\Delta pD_o}{\frac{1}{2}\rho_{g}u_{ig}^2L_{g}}\right)}$

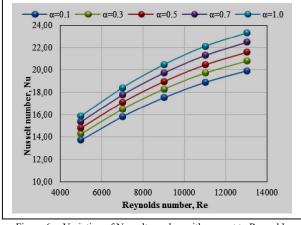


Figure 6. Variation of Nusselt number with respect to Reynolds number

As observed from Fig. 6, Nusselt number increases with the Reynolds number which shows thermal performance increases as the flow velocity increases. Moreover, Nusselt number is higher for α =1.0 i.e. for rectangular fin profile and then decreases as α approaches to 0.1 where the fin geometric profile becomes nearly triangular. This effect results from the decreasing flow velocity as α varies from 1.0 to 0.1 which further decreases the convective heat transfer.

Variation in Euler number with Reynolds number for different fin geometric profiles can be seen from Fig. 7. Euler number decreases as α varies from 1.0 to 0.1, which is a clear demonstration of reduced pressure loss on a transition of rectangular fin profile (α =1.0) to triangular profile (α =0.1). At Re = 13000, Euler number for α =0.1 decreases by 7.23% than α =1.0.

In order to evaluate the overall performance of the heat exchanger in terms of both, heat transfer and pressure loss, efficiency index (Table III) is calculated. Fig. 8 shows a variation in efficiency index with respect to Reynolds number for different fin geometric profiles. The efficiency index increases with the Reynolds number and so thus the overall performance of the heat exchanger design. As observed, efficiency index increases as α goes down from 1.0 to 0.1 which dictates that the fin with tapered geometric profile performs better in comparison to the conventional rectangular fin geometric profile.

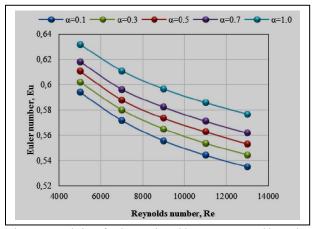


Figure 7. Variation of Euler number with respect to Reynolds number

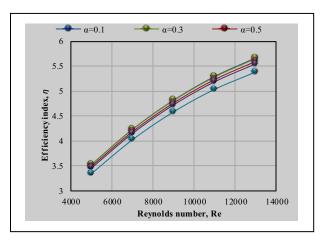


Figure 8. Variation of efficiency number with respect to Reynolds number

This trend of efficiency index explains that as α varies from 1.0 to 0.1, the pressure reduction is dominant than that of increment in thermal performance. In addition, the heat exchanger with α =0.1 and α =0.3 shows nearly equivalent performance. For instance, at Re=13000 efficiency index at α =0.1 is only 0.23 % higher than α =0.3. Heat transfer through the fin can be predicted from the temperature gradients on the fin surface.

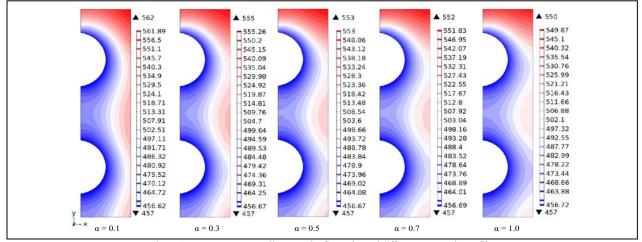


Figure 9. Temperature gradients on the fin surface of different geometric profiles

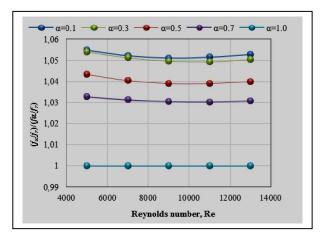


Figure 10. Performance comparison of different geometric fin profile

Fig. 9 shows temperature gradients on the fin surface of different geometric profiles. The dissipation of the heat from hot gas to the fin is evident from the higher temperatures away from fin and tube interface where the heat is conducted from the fin to the tube wall resulting in lower temperatures in those regions. Relatively, higher temperature gradients on the fin surface with $\alpha=0.1$ are evident of lower heat transfer rate due to the lower temperature difference between the gas and the fin which further reduces the heat transfer performance.

To determine the impact of different fin profiles on the overall performance at the equitable basis, a dimensionless parameter called 'area-goodness factor' is used. It is defined as a ratio of Colburn j factor to the friction factor, f of the heat exchanger design with respect to the reference fin geometry (Table III). Fig. 10 shows the comparative performance of the heat exchanger with different fin geometric profiles at Reynolds number range 5000-13000. It can be observed that fin at $\alpha=0.1$ (i.e. nearly triangular geometric profile) has the highest performance factor in comparison to the other fin profiles under similar operating conditions.

In many industrial applications of fin and tube heat exchangers such as waste heat recovery, aerospace, airconditioning, automobile radiator, marine vessels etc., the available volume space and heat exchanger unit weight is a primary design consideration.



Figure 11. Comparison of the change in weight of heat exchanger unit with different geometric fin profile

To investigate the most suitable geometric fin profile, the reduction in the weight of the heat exchanger unit as the fin geometric profile varies from $\alpha=1.0$ to $\alpha=0.1$ is determined and is shown in Fig. 11. As α reduces from 1.0 the weight of the heat exchanger unit (considered one-half in the present study, Fig. 2) reduces and accounts for approximately 28 % reduction when α =0.1. Based on the results and discussion, it can be observed that fin geometric profile at α =0.1 when fin has nearly triangular geometric profile shows better performance with less weight than the reference rectangular fin geometry at $\alpha = 1.0.$

V CONCLUSION

In the present study, the impact of different fin geometric profiles on the heat transfer performance and pressure loss in a fin and tube heat exchanger design are analyzed. The numerical study concludes that the fin with triangular at α =0.1 profile can enhance the heat transfer with reduced pressure loss in comparison to the conventional rectangular fin profile, $\alpha = 1.0$. Furthermore, the fin with $\alpha=0.1$ reduces the heat exchanger weight up to 28 % which is always desirable in the industrial applications of fin and tube heat exchangers. The work presented in this paper encourages the further investigation on different possible fin geometric profiles in order to optimize the material and manufacturing cost which are the main controlling factors in designing a fin and tube heat exchangers at the industrial scale.

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NOMENCLATURE

- D diameter of the tube, m
- Eu Euler number
- F body force vector, N/m³
- Convective heat transfer coefficient, W/m².K h
- Κ thermal conductivity, W/m.K
- turbulent kinetic energy, m^2/s^2 k
- L length, m
- Nu Nusselt Number
- pressure, Pa р
- pressure difference across the gas domain, Pa Δp
- Pr Prandtl number
- Q heat flux vector, W/m²
- Re Reynolds number
- Т temperature, K
- heat source or sink, W/m³ Q
- flow velocity, m/s u
- average velocity vector, m/s

u Syı bols

- Specific dissipation rate, 1/s ω
- density, kg/m³
- ρ
- dynamic viscosity of the gas, Pa.s μ

Subscripts

- ģ gas or gas domain
- l liquid
- fin f
- inner tube wall w
- inner tube i

o outer tube

max maximum

r reference fin geometric profile

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APPENDIX

In (5),
$$P = \min(P_k, 10\rho\beta_o k\omega)$$
 (i)

where,
$$P_k = \mu_T (\nabla \mathbf{u} : (\nabla \mathbf{u} + (\nabla \mathbf{u})^T) - \frac{2}{3} (\nabla \cdot \mathbf{u})^2 - \frac{2}{3} \rho k \nabla \cdot \mathbf{u}$$
 (ii)

The turbulent viscosity is,
$$\mu_T = \frac{\rho a_1 k}{\max(a_1 \omega, Sf_{v2})}$$
 (iii)

where, S is the characteristic magnitude of the mean velocity gradients,

$$S = \sqrt{2S_{ij}S_{ij}} \tag{iv}$$

The other model constants are given in terms of interpolation functions as,

$$\phi = f_{v1}\phi_1 + (1 - f_{v1})\phi_2 \quad \text{for } \phi = \beta, \gamma, \sigma_k, \sigma_\omega \text{ and } f_{v1} = \tanh(\theta_1^A)$$
$$\theta_1 = \min\left[\max\left(\frac{\sqrt{k}}{\beta_o \omega l_\omega}, \frac{500\mu}{\rho \omega l_\omega^2}\right), \frac{4\rho\sigma_{\omega 2}k}{CD_{k\omega}l_\omega^2}\right] \quad (iv)$$

where, lw is the distance to the closest wall.

$$CD_{k\omega} = \max\left(\frac{2\rho\sigma_{\omega^2}}{\omega}\nabla\omega\cdot\nabla k, 10^{-10}\right)$$
(v)

$$f_{\nu 2} = \tanh(\theta_2^2) \text{ and } \theta_2 = \max\left(\frac{2\sqrt{k}}{\beta_o \omega l_o}, \frac{500\mu}{\rho \omega l_o^2}\right)$$
 (vi)

The other default model parameter values are,

 $\beta_1 = 0.075, \gamma_1 = 5/9, \sigma_{k1} = 0.85, \sigma_{\omega 1} = 0.5,$ $\beta_2 = 0.0828, \gamma_2 = 0.44, \sigma_{k2} = 1.0, \sigma_{\omega 2} = 0.856,$

$$\beta_o = 0.09, a_1 = 0.31$$
 (vii)

(viii)

The Reynolds number calculated as:

$$Re = \frac{\rho u_{\text{max}} D_o}{\mu}$$

The gas-side convective heat transfer coefficient is determined by overall heat transfer coefficient as [17]:

$$\frac{1}{U} = \frac{1}{h_g} + \frac{A_l}{A_l} \left(\frac{1}{h_l} + \frac{(D_o - D_l)}{2K} \right)$$
(ix)
On further simplification,

$$\frac{1}{UA_{i}} = \frac{1}{h_{g}A_{i}} + \frac{1}{h_{i}A_{i}} + \frac{1}{\left[\frac{2KA_{i}}{(D_{o} - D_{i})}\right]}$$
(x)

Since the heat transfer coefficient inside the tube is high (~ 10^4 W/m2.K), the second term in (x) is omitted. The above equation can be further simplified without losing accuracy as the tubes being analyzed are of small thickness (~ 10^3 m) and higher thermal conductivity (~50 W/m.K) which makes the third term very small and hence negligible. This results in a much simpler expression,

$$\frac{1}{UA_i} = \frac{1}{h_g A_i} \tag{xi}$$

$$U = h_g$$
 (xii)

Overall heat transfer coefficient can be determined as:

$$U = \frac{Q_t}{A_t \Delta T_{tm}}$$
(xiii)

where,
$$\Delta T_{lm} = \frac{(T_w - \overline{T}_{in}) - (T_w - \overline{T}_{out})}{\ln \left[\frac{(T_w - \overline{T}_{in})}{(T_w - \overline{T}_{out})} \right]}$$
 (xiv)