Population Coding of Stimulus Location in Rat Somatosensory Cortex

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debate (Nirenberg et al., 2001; M.J. Berry II, personal in sensory cortex by applying information theoretic analyses to neuron pairs recorded simultaneously communication). In cortex, although the information from rat barrel cortex. We quantified the roles of indi- available in spike patterns compared to that available vidual spikes and spike patterns in encoding whisker in independent spikes has not been quantified, there is stimulus location. 82%–85% of the total information evidence suggesting that patterns might play a role in was contained in the timing of individual spikes: first neuronal coding. For example, some sensory stimuli spike time was particularly crucial. Spike patterns (Gray et al., 1989; deCharms and Merzenich, 1996; Villa
within neurons accounted for the remaining 15%–18% et al., 1999) and motor preparatory states (Abeles et al., **within neurons accounted for the remaining 15%–18%. et al., 1999) and motor preparatory states (Abeles et al., Neuron pairs located in the same barrel column coded 1993; Vaadia et al., 1995; Riehle et al., 1997) can elicit** redundantly, whereas pairs in neighboring barrel col-

umns coded independently. The barrel cortical popu-

lation code for stimulus location appears to be the

time of single neurons' first poststimulus spikes—a

fast, ro

It is widely accepted that sensory events are encoded

in cortex by numerous spikes distributed across large

spikes is greater than the summated information transmitted

spikes is greater than the summated information tra

millisecond scale can be a mechanism for information transmission about dynamic stimulus features both in nonmammalian neural structures (Bialek et al., 1991; International School for Advanced Studies Berry et al., 1997; Vickers et al., 2001) and in mammalian Via Beirut 2/4 cortex (Buracas et al., 1998). Precise timing of spikes 34014 Trieste even increases the information transmitted about stimuli Italy which contain no dynamic features (Panzeri et al., 2001; Reich et al., 2001): single neurons of the rat somatosen- 2Neural Systems Group Department of Psychology sory cortex, for example, encode 44% more information Ridley Building about stimulus location when spikes are binned with 5 University of Newcastle upon Tyne ms resolution than when they are simply counted over NE1 7RU one long response window (Panzeri et al., 2001).

United Kingdom Regarding the second question, both single neuron and multi-neuron spike patterns have recently been studied. For single cells of the fly, closely spaced spike Summary pairs carry more information than the spikes do individually (Brenner et al., 2000); for pairs of mouse retinal This study explores the nature of population coding ganglion cells, the role of cross-cell patterns is under

spikes and spike patterns, one can characterize neu- Introduction ronal coding as *synergistic* **or** *redundant***. A synergistic**

two questions using the rat somatosensory cortex as a
model. Our inquiry builds upon the considerable prog-
ress that has been made in recent years in understand-
of the cerebral cortex (Mountcastle, 1997), we hope to **ress that has been made in recent years in understand- of the cerebral cortex (Mountcastle, 1997), we hope to ing neural coding. With regard to the first question, there elucidate whether they function as ensemble encoding** units, or whether the constituent neurons convey infor**mation in an independent fashion.**

Rat somatosensory cortex offers several advantages ³

ically defined and have a one-to-one relationship with zeri et al., 2001). This analysis did not address the potenthe whiskers on the rat's snout (Woolsey and Van der tially important effect of spike timing across multiple Loos, 1970; Welker, 1971), allowing the columnar loca- neurons. Our first aim was therefore to uncover the role tion of each neuron to be identified. Another important of spike timing at the level of multiple neurons. While feature is that neurons tend to fire few spikes per trial. our earlier work was able to examine timing within a 40 This restricts the potential complexity of the code, ms response window with a bin size as small as 5 ms, allowing the experimenter to reliably estimate the infor- inclusion of two neurons allowed the current analysis mation conveyed by the spike trains of simultaneously to test for temporal resolution as fine as 10 ms. This recorded neuron pairs (Panzeri and Schultz, 2001; Panzeri limit was determined by the number of trials per stimulus et al., 2001), and thereby permitting a comprehensive anal- available—see Experimental Procedures. ysis of the role that individual spikes and spike patterns An example of a pair of cells recorded from barrel play in neural coding. Studying the coding of stimulus column D2 is shown in Figure 1a. At the left, the spike location, we have quantified the role of spike timing within times relative to stimulus onset are shown for each of 50 and across neuron pairs, and assessed whether the mode deflections of whiskers D1 and D2. Both cells responded of processing is redundant or synergistic. Under our con- strongly and rapidly to the principal whisker D2, but ditions, precise spike timing of single neurons signifi- weakly and with greater delay to nonprincipal whisker cantly increases the quantity of information available, D1. This observation is consistent with the well-known but spike timing does not appear to be exploited to functional properties of barrel cortex: in general, nongenerate synergistic patterns across neurons. These principal whiskers evoke spikes in a cortical barrel colfindings suggest a robust population coding mechanism
whose advantage—in, comparison, to complex, syner-**(Armstrong-James and Fox, 1987).** These properties are **whose advantage—in comparison to complex syner- (Armstrong-James and Fox, 1987). These properties are gistic coding—may be to ensure that each cortical col- reflected in the poststimulus time histograms (PSTHs) umn rapidly distributes the same message to multiple to deflection of D2 and each of the eight surrounding brain regions and to all neuronal targets within a brain whiskers (middle panel). The information about stimulus**

line) was similar to that in the spike count (dashed line). from the barrel cortex of urethane-anesthetized rats. Only pairs where each cell was recorded at a different
electrode were considered. In 52 cases, both neurons
were located in barrel column D2. In other cases, the
neadtitional information in spike timing. Clearly, one fact

as time = 0 ms.

To find out the time scale at which neurons transmit

inne whiskers of interest (middle panel) again reveal that

inne whiskers of interest (middle panel) again reveal that

terms of both *spike count* an the two spike sequences emitted on a given trial were
 $\frac{1}{108}$ was similar, 0.27 \pm 0.09 bits (mean \pm SD) and 0.25 \pm

considered. We measured the mutual information con-
 $\frac{0.08 \text{ bits}}{108}$, respectively. Howe **tained in each type of response about stimulus location, D2 cell pairs conveyed 0.31 0.10 bits by spike timing—**

We showed previously that precise spike timing allows panel), the advantage was 52%. *single* **neurons to transmit 44% more information about In order to estimate better the precision of the tempo-**

as an experimental model. Cortical columns are anatom- stimulus location than does the spike count alone (Pan-

location transmitted in spike count by this pair of neu- region. rons (right panel, dashed line) increased with the length of the response window until 20 ms, reflecting the fact Results that different whiskers elicited different numbers of We analyzed 212 pairs of simultaneously recorded cells spikes. Initially, the information in spike timing (solid

using the series expansion method (Panzeri et al., 1999; 25% more than by spike count. The advantage of spike Panzeri and Schultz, 2001); see Experimental Procedures. timing compared to spike count for cell pairs located in different barrel columns tended to be greater: for D1- Role of Spike Timing within D2 pairs (middle panel), the advantage was 29%; for and across Barrel Columns D2-D3 pairs, 33% (not shown). For D1-D3 pairs (right

Figure 1. Coding by Cell Pairs, within Column and across Columns

(a) Cell pair located within barrel column D2. Left: Raster plots for each cell in response to whisker stimuli D1 and D2 at 0.1 ms resolution. Middle: PSTHs for each of the nine whisker stimuli: responses of one cell are shown as solid lines; the other as dotted lines. Bin size is 10 ms. Right: mutual information between the stimulus set and the spike timing response evaluated with 10 ms bins. The information that the two cells conveyed by spike timing (solid line) was substantially more than that conveyed by spike count (dashed line). (b) Cell pair distributed across two barrel columns, D1 and D2. PSTHs and mutual information plotted as for part (a).

ral code, we measured the spike timing information for lier concerning single neurons (Panzeri and Schultz, **the response interval 0–20 ms with a bin size as small as 2001). Spike timing is particularly informative for popula-5 ms. If information increases as bin size is decreased, tions that encompass separate barrel columns. timing must be precise on the scale of the smaller bin size. For neuron pairs in D2 barrel column, information Information in Individual Spikes increased from 0.25** \pm 0.09 bits with 20 ms bins to 0.29 \pm and Spike Patterns **0.09 bits with 5 ms bins. The increase in information The information in spike timing described in the previous obtained by considering a resolution of 5 ms was even section could be generated in two ways. The simplest is greater for pairs located in different barrel columns: for if all the information were coded by stimulus-dependent D1-D2 pairs, information increased from 0.27 0.11 bits differences in the timing of individual spikes, within-trial for 20 ms bins to 0.36 0.15 bits for 5 ms bins; for D2- correlations between spike times not being informative. D3 pairs, it increased from 0.22 0.11 bits to 0.30 In this case, information can only be coded by variations 0.12 bits; for D1-D3 pairs, it increased from 0.24 0.12 in the PSTH structure across stimuli. The second way bits to 0.36 0.14 bits. Thus, the precision of the spike is if particular spike patterns were to occur within the timing code was at least 5 ms, and the 25%–52% advan- same trial, which could code information even in the tage for spike timing compared to spike count might be absence of stimulus-dependent PSTH structure. The seeven larger at smaller time bins. These results show that ries expansion method permits us to quantify the relative spike timing is important for the population coding of contribution of these two mechanisms. As detailed in stimulus location, extending the observations made ear- Experimental Procedures, the expansion expresses the**

Figure 2. Role of Spike Timing and Spike Patterns in Population Coding

Labels above the graphs refer to neuronal locations. (a) Information in spike timing (solid line) is plotted as a function of poststimulus time, together with information in spike count (dashed line), averaged over cell pairs. (b) Total information in spike timing (solid line) is compared to the contribution of each component in the series expansion, averaged over cell pairs. The total contribution of individual spikes (dashed line) is the sum of the first order term, Equation 3, and the PSTH similarity second order term, Equation 4. Spike patterns contributed much less (stimulus-independent patterns, Equation 5, dotted line; stimulus-dependent patterns, Equation 6, dash-dotted line). Bars denote SEM.

consisting of the sum of two terms arising from individual Redundancy is present if the PSTH value at a given spikes and two terms arising from spike patterns. **the state of the stimulus set with the** spikes and two terms arising from spike patterns.

conveys by the timing of individual spikes is the sum of or correlates with the PSTH value at any time bin an *independent spike timing* **term and a** *PSTH similarity* **for a different cell. This type of correlation has been term. The former term expresses the information that termed** *signal correlation* **(Gawne and Richmond, would be conveyed were the spikes to carry indepen- 1993), and Equation 4 quantifies the amount of redundent information; the latter term corrects this for any dancy that it introduces. redundancy arising from similarity of PSTHs across The remaining two terms in the series expansion approx- stimuli. More precisely: imation, given below, express any further effect that**

- **do not convey information, then** *all* **information must spikes.** be in the timing of individual spikes. Under these cir-
cumstances, the time-varying firing rate (PSTH) is a
complete description of the neuronal response, and
is the only statistic required in order to estimate the
inform
-

total information in spike timing as an approximation spikes, Equation 3 can overestimate the information. The amount of information that a neuronal population PSTH value at a different time bin for the same cell,

• *Independent spike timing***: if within-trial spike patterns spike patterns might have beyond that of individual**

the total information available in the response (De-
Weese, 1996; Brenner et al., 2000; Panzeri and pairs of spikes are quantified, for each stimulus, as
Rebulta 2001). Cabulta 2001 **the probability of spikes occurring in each of two time Schultz, 2001). bins. For** *within-cell patterns***, the bins come from the •** *PSTH similarity***: if there is any redundancy between same cell; for** *cross-cell patterns***, they come from**

Response variable #1

Figure 3. Effect of Stimulus-Independent Patterns on Population Coding

Each panel sketches hypothetical distributions of "responses" to three different stimuli. The response variables can be considered either to be different bins within the same cell or bins across different cells. Each ellipse indicates the set of responses elicited by a given stimulus. In each of these examples, signal correlations are positive whereas the sign of noise correlation differs. In the middle panel, noise correlation is zero, and stimulus-independent patterns exert no effect on the total information. When noise correlation is positive (left panel), responses to the stimuli are less discriminable and stimulus-independent spike patterns cause a redundant effect. When noise correlation is negative (right panel), responses are more discriminable and the contribution of stimulus-independent spike patterns is thus synergistic. In general, if signal and noise correlations have the same sign, the effect of stimulus-independent patterns is redundant, if they have opposite signs, it is synergistic.

greater the diversity, the greater the information available. This effect is quantified by Equation 6. Nature of the Spike Pattern Information

• Stimulus-independent spike patterns: even if not stim-

ulus dependent, spike patterns: even if not stim-

on the neuronal code through a subtle interaction

on the neuronal code through a subtle interaction

between si

components contributed to the coding of stimulus loca- panels of Figure 4. Again, the major finding was that tion. The left panel shows results averaged over all pairs within-cell spike patterns exerted a positive effect. For of neurons located in barrel column D2. At 40 ms post- D1-D2 and D1-D3 pairs, both stimulus-independent patstimulus, the timing of *individual spikes* **(dashed line) terns across cells and stimulus-dependent patterns accounted for 83 14% of the total information in spike (within and across cells) were negligible. timing (solid line). Stimulus-dependent spike patterns Overall, neither within nor across barrel columns did (dash-dotted line) accounted for 5 7%, stimulus-inde- cross-cell spike patterns seem to code information about**

different cells. In the terminology of Gawne and Rich- pendent patterns (dotted line) for 12 14%. Similar mond (1993), this joint probability is known as the results were obtained for pairs of neurons located in *noise correlation***. In the case of cross-cell synchrony, different barrel columns: D1-D2 pairs (middle panel) for example, the noise correlation will be greater than conveyed 17 6% by spike patterns (stimulus-depen**expected from the PSTHs. In the case of within-cell dent and stimulus-independent patterns considered to**refractoriness, where the presence of a spike in one gether), D2-D3 pairs (not shown) conveyed 15 7%, bin predicts the absence of a spike in the next bin, D1-D3 pairs (right panel) conveyed 18 6%. Thus spike the noise correlation will be** *less* **than that expected patterns conveyed about 15%–18% of the total informafrom the PSTH. tion in the population spike train, and we will analyze** The amount of information conveyed by stimulus-depen-
dent spike patterns depends, analogously to the PSTH
information, on how much the noise correlations (nor-
malized by firing rate) vary across the stimulus set: the
mal

Figure 2b shows how these different, timing-dependent ent barrel columns are shown in the middle and right

Figure 4. Contributions of Within-Cell Patterns and Cross-Cell Patterns to the Spike Timing Code For each cell pair, the contribution to the second order terms of the series expansion was split into within-cell and cross-cell components. Labels above the graphs refer to neuronal locations. Results for stimulus-dependent patterns and signal-noise interaction are plotted averaged over cell pairs. Bars denote SEM.

to the population code was almost entirely attributable tion is less than that conveyed independently. The picto within-cell patterns. Since stimulus-independent ture is complicated by the fact that some spike patterns **spike patterns within individual neurons transmitted a produced by a neuron pair can be synergistic, while tional analyses to determine the nature of these spike order term, Equation 3, is precisely the information conpatterns. As noted above, the information conveyed by veyed by spikes independently. Therefore, to evaluate stimulus-independent spike patterns depends on the whether the coding of stimulus location is synergistic relationship between signal correlations and noise cor- or redundant, we evaluated the sum of the three higher relations. To find out which of the three modes of interac- order terms—Equations 4, 5, and 6. To examine the we plotted the (Pearson) signal correlation coefficient these terms into separate within-cell and cross-cell (averaged over time bin combinations) against the noise components. correlation coefficient (averaged over both time bin Figure 6 shows that neuron pairs in the same barrel combinations and stimuli). Figure 5a shows results for column (D2-D2) were highly redundant (white bar). The within-cell patterns. For both same-column (left panel) value of 0.055 0.067 bits of redundant information and cross-column (middle and right panels) pairs, signal corresponds to 19% of the total information in spike correlation coefficients were usually positive and noise timing. This was due exclusively to cross-cell contribucorrelation coefficients negative. A positive signal corre- tions (gray bar). Within-cell contributions (black bar), lation coefficient means that pairs of PSTH bins tend to by themselves, were slightly synergistic (0.005 bits); for have similar values across different stimuli. A negative cross-cell contributions, redundancy caused by spikes noise correlation coefficient means that spikes co-occur in different cells being correlated across stimuli was in pairs of bins less frequently than expected from the much stronger than any positive effect of information-PSTHs. Since signal and noise correlations had different bearing spike patterns. signs, their interaction resembled that shown schemati- For neuron pairs located in different barrel columns, cally in Figure 3c, making the stimulus-independent the overall effect (white bars) was close to zero: 0.001**

patterns. For cell pairs located in barrel column D2 (left of the total information), and 0.017 0.042 bits for D1 panel), both signal correlations and noise correlations D3 pairs (7% of the total information). Again, different tended to be positive (in contrast to the observation for types of spike pattern exerted opposing effects: within-cell within-cell patterns). Hence, their interaction resembled patterns were synergistic; cross-cell patterns redundant. that shown in Figure 3a, making the stimulus-independent pattern term negative. For neuron pairs in different Coding by the First Poststimulus Spike barrel columns (middle and right panels) noise correla- The previous sections showed that the coding of stimutions tended to be positive, but signal correlation values lus location is achieved mainly by the timing of individual were scattered around zero (Figure 3b), consistent with spikes—a simple mechanism that does not depend on the finding that the effect of cross-cell stimulus-inde- cross-cell synergy. Beyond pointing out the remarkable pendent spike patterns was negligible for neurons in amount of information carried by single spikes, we

A given pattern of spikes is synergistic if the transmitted subset of individual spikes crucial? Indeed, a preceding information is greater than that conveyed by the constit- study of barrel cortex showed that, in single cells, the

stimulus location: the net contribution of spike patterns uent spikes independently; it is redundant if the informasignificant quantity of information, we carried out addi- others are redundant. In the series expansion, the first tion illustrated in Figure 3 applied, for each cell pair, origin of the synergy/redundancy in more detail, we split

spike pattern information term positive. 0.023 bits for D1-D2 pairs (0.5% of the total information), Figure 5b shows corresponding results for cross-cell 0.003 0.026 bits for D2-D3 pairs (not shown, 0.4%

different barrel columns (Figure 4). asked whether it is possible to further specify the nature of the code: is a similar quantity of information transmit-Synergy or Redundancy? ted by any single spike or, alternatively, is a particular

Figure 5. The Relationship between Signal Correlation and Noise Correlation, across and within Cells Labels above the graphs refer to neuronal locations. (a) For each cell pair, average within-cell signal correlation coefficient is plotted against average within-cell noise correlation coefficient (see text for details). (b) Corresponding results for cross-cell correlations.

Figure 6. Synergy/Redundancy within and across Cells

Total synergy (white bars) was estimated as the sum of second

order terms, as explained in Experimental Procedures. This was split

into cross-cell (gray bars) and wit Results were averaged over cell pairs according to location; bars **denote SEM. tion. We characterize this as a simple, spike-time popu-**

overwhelming part of the total information was ac- spike at the population level, we repeated the above counted for by the timing of the *first* **poststimulus spike analyses considering only the first, second, or third (Panzeri et al., 2001). To examine the role of the first spikes per cell recorded on each stimulus trial. The information conveyed by the individual spike terms of the series expansion (Equations 3 and 4) was compared to the corresponding data for the whole spike train. For neuron pairs in barrel column D2, the first spikes conveyed almost as much information as the entire spike train (Figure 7). The mean first spike information was 91 7% of that in the entire 40 ms spike trains. For neurons in different barrel columns (not illustrated), the corresponding values were 87 7% (D1-D2 pairs), 91 9% (D2-D3 pairs), and 89 9% (D1-D3 pairs). The mean information conveyed by D2-D2 pairs in the second and** third spikes was $43 \pm 18\%$ and $18 \pm 14\%$, respectively, **of that present in the individual spikes of the whole spike train. Similar results for second and third spikes were obtained for cell pairs distributed across different barrel columns. Since nearly all the information in the entire spike train was already present in the first poststimulus spike, the later spikes were almost completely redundant, both for neuron pairs within and across barrel columns.**

train, averaged over all cell pairs within D2 barrel column (solid line),

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is plotted as a function of poststimulus time, together with that

conve conveyed only by the first spike in each cell (dotted line), the second **spike (dash-dotted line), and the third spike (dashed line). Bars might be to integrate information from larger populadenote SEM. tions of neurons.**

ization seems to be the single neuron rather than the bution of spike timing with 5–10 ms time bins. We de-

Coding and Decoding Mechanisms

Weuronal populations can transmit information in three

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ways: (1) by individual spikes (Bialek et al., 1991; (2) by

spike patterns mi

coding of whisker location in rat barrel cortex using the spike time of cortical responses encodes visual contrast spike trains of many simultaneously recorded neurons, (Gawne et al., 1996; Reich et al., 2001) and sound source struct stimulus location (Ghazanfar et al., 2000), or by thus *available* **in first spike times, it is not always safe (Petersen and Diamond, 2000). In both cases, the popu- rest of the animal's brain. Unlike the experimenter, an lation code was found to be "distributed," in the sense animal likely does not have independent knowledge of that stimulus discriminability increased with the number stimulus time. In the rat whisker system, two possible of neurons included in the analysis. Having identified solutions to this decoding problem seem plausible. (1) the distributed character of the code, the next question Since the collection of vibrissal sensory data under natuis: what are the specific information-bearing units within ral conditions is an active process initiated by a motor it? Under the present experimental conditions, the series command, the sensory system could use the output**

expansion method permitted us to identify which aspects of neuronal activity carry sensory information individual spikes, single cell spike patterns, or crosscell spike patterns. The timing of individual spikes accounted for 82%–85% of the total information transmitted by neuron pairs, whereas the remaining 15%– 18% was almost entirely due to within-cell, but not cross-cell, spike patterns.

The contribution of individual spikes could be accounted for primarily (87%–91%) by the times of the first spikes following whisker deflection, later spikes being redundant. Since these initial, information-rich spikes could also occur at long latencies (note the response of the D2 neurons to whisker D1 in Figure 1), the information grew progressively across poststimulus time (Figures 1 and 2): for D1-D2 neuron pairs, the available information was 127% greater at 40 ms than at 10 ms. Our analysis shows the amount of information that is
Available: whether the brain uses the earliest available
Mean information conveyed by individual spikes in the whole spike
Also means alliable later simple is a

How might these results generalize when barrel cortex is studied under different conditions? Time scale is one lation code. Under the conditions reported here, the issue to consider: most of the results presented here basic functional unit of barrel cortex for stimulus local- and previously (Panzeri et al., 2001) concern the contrineuronal ensemble. tected no trend toward spike patterns having a more important role at temporal resolutions as fine as 5 ms (Panzeri et al., 2001). Still, the present analysis cannot Discussion completely exclude the possibility that cross-cell spike

Interval (a spike pattern code).
Recent studies have considered mechanisms for the an important role in other sensory systems. The first
coding of whisker location in rat barrel cortex using the spike time of cortical resp **location (Furukawa et al., 2000). Although information is estimating stimulus discriminability using population** *d* **to assume that such information can be** *used* **by the** **from the motor system as an estimate of stimulus time. has recently been reported in both rat prefrontal cortex (2) Complementing information that might be available and monkey extrastriate cortex (Jung et al., 2000; Bair from** *absolute* **timing relative to the motor command, the et al., 2001). sensory system could use the** *relative* **timing between Across barrel columns, however, signal correlations spikes in the neuronal population (Buonomano and Mer- were weak. Stimulus-independent spike patterns have zenich, 1999; Jenison, 2001; Van Rullen and Thorpe, little effect under these circumstances, and the coding 2001). In the present case, for example, deflection of was consequently near independent. Thus, information whisker D1 elicits spikes first in barrel column D1 and can increase approximately linearly until the limit dic***subsequently* **in barrel column D2; whereas deflection tated by the information available in the stimulus set is**

The first of these decoding solutions (motor efference 1997). signal), acting alone, would probably not possess suffi- The redundancy that we found within barrel columns cient temporal precision (Kleinfeld et al., 1999) to permit was mainly due to individual spikes conveying similar the representation of information by first spike times, messages. Hence, sampling large populations of neubut it may constrain sensory analysis to a time window rons within a given barrel column would confer little within which relative spike timing would convey the rele- improvement in coding accuracy. This conclusion is vant information. In a broader context, use of a motor consistent with previous studies of neighboring cells in command for decoding first spike time information can primate neocortex (Gawne and Richmond, 1993; Zohary apply only to modalities where sensory activity is elicited et al., 1994; Lee et al., 1998). Across different sensory by motor output, but would not be relevant in cases systems and species, it appears that same column cortiwhere sensory activity is elicited purely by external cal cells have high (positive) signal correlation and posi**changes. tive noise correlation. Information theory tells us that**

train is already present in the first poststimulus spike, we seem to be an inefficient coding mechanism, causing argue that the efficiency of cortical processing of stimulus thousands of neurons to produce a similar message, location is enhanced by mechanisms that suppress with little gain in accuracy. But its benefits could include subsequent, redundant spikes. One such mechanism is **to multiple targets. represented by the powerful GABAergic intracortical inhibitory input that quickly curtails the excitatory dis- Experimental Procedures charge evoked by single whisker deflection (Simons and** Woolsey, 1984; Kyriazi and Simons, 1993; Kyriazi et al., **Electrophysiology 1996; Swadlow and Gusev, 2000). The functional cir- Methodology is described in detail by Lebedev et al. (2000). All cuitry of barrel cortex ensures that there is a very short procedures conformed to N.I.H. and international standards conwindow after whisker stimulation during which cortical cerning the use of experimental animals. Twenty-two adult male**

elucidate whether they function as ensemble encoding was maintained near 37.5C and, during the recording session, anesunits, or whether the constituent neurons convey infor- thetic depth was held at a consistent depth by monitoring hindpaw mation in an independent fashion. The answer hinges withdrawal, corneal reflex, and respiration rate. on the nature of neuronal cross-correlations. We found
 At the experiment, subjects were perfusion followed by 4% paraformaldehyde. After postfixation in 20% suthe average cross-cell noise correlation coefficient
within a cortical barrel column to be $0.25 - a$ figure
within a cortical barrel column to be $0.25 - a$ figure
tangential sections, and processed for nitric oxide synthase **broadly consistent with studies of the primate visual (Valtschanoff et al., 1993) in order to visualize barrel columns in (Gawne and Richmond, 1993; Zohary et al., 1994) and layer IV. To determine the columnar location of sampled neurons,** motor systems (Lee et al., 1998), as well as rat prefrontal electrode per periode per intervals and the historia

sections cortex (Jung et al., 2000). The agreement among these
reports suggests that a small, positive cross-cell noise
reports suggests that a small, positive cross-cell noise
row or as a 2 × 3 matrix, with 300 ± 50 μ m horizon **correlation may be a general principle of cortical colum- between adjacent electrode tips, was advanced into the cortical nar operation. Zohary et al. (1994) argued that correlated barrel field, centered on barrel column D2. Typically, 1–2 electrodes noise between cells imposes a strict limit on the amount** penetrated any single barrel column under the array. The whole
of information available from a neuronal population (it array was advanced in 100 µm steps. The grea of information available from a neuronal population (it
causes redundancy). The series expansion method
makes explicit the connection between information and
minate (Lu and Lin, 1993). Since the methodology did not permit **signal/noise correlations, showing that this limit holds us to register electrode depth with accuracy better than about 100** *provided* **both that cross-cell signal correlations are m, we did not attempt to classify single neurons according to positive and that there is no strong stimulus-dependent laminar position.** structure in the cross-cell noise correlations. In the pres-
ent case, both these conditions were true of cells within erange 300–7500 Hz. Action potentials were digitized at 25 KHz,
22 points per waveform, and time-stampe **the same barrel column, so that cross-cell effects indeed (Datawave, Boulder, CO). Offline, single unit action potentials were caused redundancy. The same pattern of correlations discriminated by differences in shape and amplitude.**

of whisker D2 elicits the opposite sequence of spikes. approached (Gawne and Richmond, 1993; Rolls et al.,

redundancy is likely in this case. We suggest that redun-Information Transmission in Columnar Systems dant coding is a general characteristic of columnar pro-Given that nearly all the information in the entire spike cessing. As compared to synergy, redundancy might

neurons are able to emit a few, information-rich spikes.
Because columns are thought to be the basic informa-
tion processing modules of cerebral cortex, we set out to
the set our to a stereotactic apparatus (Narishige, To

Individual whiskers were stimulated 3 mm from their base by *ECSaibj* **(4) a piezoelectric wafer (Morgan Matroc, Bedford, OH), which was controlled by a signal generator (A.M.P.I., Jerusalem).**

method, the key step is to estimate the conditional probability $P(n|s)$ expected value of CS_{aib} for PSTHs that are uncorrelated across
of each possible response n, given each of the possible stimuli s. stimuli. I_{ta} r can be a single cell response, or a cell pair response and either between spikes. I_{ita} and I_t together express any information that the **population conveys purely by the timing of individual spikes (time- a spike count or a spike sequence. The stimulus-average response** population conveys purely by the timing of individual spikes (time-
probability P(n) probability *P(n)*, and the stimulus probability *P(s)* must also be esti-

The influence of multi-spike patterns is expressed by the re-

The influence of multi-spike patterns is expressed by the remated. The mutual information can be written (Shannon, 1948):

$$
I(S,R) = \left\langle \sum_{n} P(n|S) \log \frac{P(n|S)}{P(n)} \right\rangle_{s}
$$
 (1)

(5) Information quantifies *diversity* **in the set of probabilities** *^P***(***n*|*s***). If these are all equal, for a given response** *n***, and hence equal to** *P(n)***,** *CNaibjs* **the argument of the logarithm is one and the response contributes (noise correlation) is the** *joint* **PSTH of bin** *i* **of cell** *a* **and bin**

the above conditional probabilities accurately, given the number of **complet of CN_{aibjs}** for statistically independent spikes. Note that "noise" is the above conditional probabilities accurately, given the number of **com** trials presented in a typical physiological experiment. Fluctuations **presence of information, as explained below. This expression is in the estimated conditional probabilities lead to spurious diversity that mimics the effect of genuine stimulus-coding responses. positive when the normalized signal and noise correlations have Hence, the effect of limited sampling is an** *upward* **bias in the esti-
mate of the mutual information: the size of the bias being inversely when the same signs mate of the mutual information; the size of the bias being inversely ure 3. The final term (stimulus-dependent patterns) is: related to the number of trials. Provided that the number of trials is at least the number of different responses, there is a formula for the bias magnitude that can be used to improve the accuracy of** information estimation (Panzeri and Treves, 1996; Golomb et al., **1997). Considering pairs of neurons, stimulated with 50 trials, re**sponse "words" of length not exceeding 2 can be considered using
the direct method. The direct method is not, therefore, useful for
studying coding by spike timing in neuronal populations.
The variety of possible spike se

complexity of the neural code, increases rapidly with the number
of spikes emitted per trial; conversely, low firing rates limit the complexity. Since typical firing rates in the barrel cortex are just 0-3
spikes per whisker deflection, the mutual information can be well
approximated by a second order power series expansion in the time
window T, which depe permits information to be estimated at greater temporal resolution. **In the present case, words of length 4 per cell in a pair could be analyzed. Most of the results reported here are for the time window The series expansion also allows us to express the total synergy in 0–40 ms, divided into 10 ms bins. However, we checked that the terms of a within-cell part** *Sw* **and a cross-cell part** *Sc***.** *Sw* **is the sum basic pattern of results was similar at small bins, by considering of the same cell (***a* **smaller response intervals. measures the net effect of within-cell spike patterns.** *Sc* **is the sum**

The series expansion approximation for the information conveyed of the cross-cell (*a* **by spike timing (Panzeri and Schultz, 2001) consists of one first cell spike patterns. order, and three second order terms:**

$$
I(S,R) = I_t + I_{tta} + I_{ttb} + I_{ttc}
$$
 (2)

$$
I_t = \sum_{a,i} \left\langle \overline{n}_{\text{ais}} \log_2 \frac{\overline{n}_{\text{ais}}}{\langle \overline{n}_{\text{ais}} \rangle_{s'}} \right\rangle_s \tag{3}
$$

 n_{ais} is the response in time bin *i* of cell *a* to stimulus *s* on a particular trial. The bar $\overline{ }$ means an average over trials, thus \overline{n}_{ais} is simply the over pairs. Third, we compared information in the spike count, esti**corresponding PSTH. The angle brackets …***^s* **denote an average mated using the series expansion, to that estimated using the direct over stimuli, weighted by the stimulus probabilities** $P(s)$ **. Equation 3 conveys information contained in the timing of independent spikes. over pairs. Fourth, as reported in Panzeri et al. (2001), we compared**

$$
I_{tta} = \frac{1}{2} \sum_{a,b,i} \left[CS_{aibj} \left(1 - log_2 \frac{CS_{aibj}}{MS_{ai}MS_{bj}} \right) - ECS_{aibj} \right]
$$
(4)

Here *MSai* - *nais^s* **is the average of the PSTH over stimuli for time b**in *i* of cell a; $CS_{\text{aibj}} = \langle n_{\text{ais}} \, n_{\text{bjs}} \rangle_{\text{s}}$ is the signal correlation between time bin *i* of cell *a* and bin *j* of cell *b*; $\text{ECS}_{\text{aibj}} = \text{MS}_{\text{a}i} \text{ MS}_{\text{b}j}$ is the To evaluate the mutual information using the direct (or "brute force") time bin *i* of cell a and bin *j* of cell *b*; $\text{ECS}_{\text{albj}} = MS_{\text{alj}} MS_{\text{bj}}$ is the method the key step is the stimate the conditional probability

> **maining two second order terms. The first of these (stimulus-independent patterns) is:**

$$
I_{\text{tt}} = -\frac{1}{2\log_2 e} \sum_{a,b,i,j} \left\langle CN_{aibjs} - ECN_{aibjs}\right\rangle_s \log_e \frac{CS_{aibj}}{ECS_{aibj}} \tag{5}
$$

nothing to $I(S,R)$. The same structure of the set of the *i* - *j***, in which case it is zero.** *ECNaibjs* -The problem with the direct method is that it is difficult to estimate $i=j$, in which case it is zero. $ECN_{\text{alips}} = n_{\text{ais}}~n_{\text{bis}}$ is the expected value
e above conditional probabilities accurately, given the number of of

$$
I_{\text{tc}} = \frac{1}{2} \sum_{a,b,i,j} \left\langle CN_{aibjs} \log_{2} \left[\frac{CN_{aibjs}}{ECN_{aibjs}} \div \frac{\langle CN_{aibjs'} \rangle_{s'}}{\langle ECN_{aibjs'} \rangle_{s'}} \right] \right\rangle_{s'} \tag{6}
$$

rately the $a = b$ and $a \neq b$ components in Equations 4, 5, and 6.

$$
S = I_{tta} + I_{ttb} + I_{ttc} \tag{7}
$$

of the same cell $(a = b)$ components of the second order terms and of the cross-cell $(a \neq b)$ ones, and measures the net effect of cross-

R **Checking the Method**

*I***Ve performed several analyses to check that the series expansion** (There is also a series expansion for spike counts—see Panzeri et approximation was accurate. In the following, results are given for al. [1999]). An important feature of the method is that the contribution al. [1999]). A **finite precision; the ratio** *CSabij***/***ECSabij* **must not diverge at any time resolution** *dt***. Second, we estimated the response entropy in spike (3) timing for each cell pair, both directly with the "brute force" method and using the series expansion (Schultz and Panzeri, 2001). For** *dt* -10 ms and $T = 40$ ms, these estimates differed by 1.3% averaged method. For $T = 40$ ms, these values differed by 1.2% averaged **The first of the second order terms (PSTH similarity) is: information in spike timing for single cells, with the direct ("brute**

force") and series expansion methods at values of *dt* **and** *T* **for which Ghazanfar, A.A., Stambaugh, C.R., and Nicolelis, M.A. (2000). En**the former method was well sampled. For $dt = 10$ ms and $T =$ **40 ms, the corresponding information estimates differed by 1.5%, cal ensembles. J. Neurosci.** *20***, 3761–3775. averaged over cells. Fifth, we made the same comparison for pairs Golomb, D., Hertz, J., Panzeri, S., Treves, A., and Richmond, B.** of cells. For $dt = 10$ ms and $T =$ of cells. For dt = 10 ms and T = 20 ms, the estimates differed by [1997]. How well can we estimate the information carried in neuronal
1.0%, averaged over pairs of cells. Lastly, we estimated a lower responses from limited **1.0%, averaged over pairs of cells. Lastly, we estimated a lower responses from limited samples? Neural Comput.** *9***, 649–665.** source on the ran spire uning information that is very robust to

sampling problems (introduced to spike train analysis by Reich et

al. [2000]) and compared this to the information in the spike train

action which reflec $=$ 10 ms and $T = 40$

 $Collectively, these results indicate that the series expansion$

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